



National  
Qualifications  
2016

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X757/77/11

**Physics  
Relationships Sheet**

TUESDAY, 24 MAY

9:00 AM – 11:30 AM

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# Relationships required for Physics Advanced Higher

$$v = \frac{ds}{dt}$$

$$L = I\omega$$

$$a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$E_K = \frac{1}{2}I\omega^2$$

$$v = u + at$$

$$F = G \frac{Mm}{r^2}$$

$$s = ut + \frac{1}{2}at^2$$

$$V = -\frac{GM}{r}$$

$$v^2 = u^2 + 2as$$

$$v = \sqrt{\frac{2GM}{r}}$$

$$\omega = \frac{d\theta}{dt}$$

$$\text{apparent brightness, } b = \frac{L}{4\pi r^2}$$

$$\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$$

$$\text{Power per unit area} = \sigma T^4$$

$$\omega = \omega_o + \alpha t$$

$$L = 4\pi r^2 \sigma T^4$$

$$\theta = \omega_o t + \frac{1}{2}\alpha t^2$$

$$r_{\text{Schwarzschild}} = \frac{2GM}{c^2}$$

$$\omega^2 = \omega_o^2 + 2\alpha\theta$$

$$E = hf$$

$$s = r\theta$$

$$\lambda = \frac{h}{p}$$

$$v = r\omega$$

$$mv_r = \frac{nh}{2\pi}$$

$$a_t = r\alpha$$

$$a_r = \frac{v^2}{r} = r\omega^2$$

$$\Delta x \Delta p_x \geq \frac{h}{4\pi}$$

$$F = \frac{mv^2}{r} = mr\omega^2$$

$$\Delta E \Delta t \geq \frac{h}{4\pi}$$

$$T = Fr$$

$$F = qvB$$

$$T = I\alpha$$

$$\omega = 2\pi f$$

$$L = mvr = mr^2\omega$$

$$a = \frac{d^2y}{dt^2} = -\omega^2 y$$

$$y = A \cos \omega t \quad \text{or} \quad y = A \sin \omega t$$

$$v = \pm \omega \sqrt{(A^2 - y^2)}$$

$$E_K = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$E_P = \frac{1}{2} m \omega^2 y^2$$

$$y = A \sin 2\pi(f t - \frac{x}{\lambda})$$

$$E = kA^2$$

$$\phi = \frac{2\pi x}{\lambda}$$

$$\text{optical path difference} = m\lambda \quad \text{or} \quad \left(m + \frac{1}{2}\right)\lambda$$

where  $m = 0, 1, 2, \dots$

$$\Delta x = \frac{\lambda l}{2d}$$

$$d = \frac{\lambda}{4n}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$n = \tan i_p$$

$$F = \frac{Q_1 Q_2}{4\pi \epsilon_0 r^2}$$

$$E = \frac{Q}{4\pi \epsilon_0 r^2}$$

$$V = \frac{Q}{4\pi \epsilon_0 r}$$

$$F = QE$$

$$V = Ed$$

$$F = IlB \sin \theta$$

$$B = \frac{\mu_0 I}{2\pi r}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

$$t = RC$$

$$X_C = \frac{V}{I}$$

$$X_C = \frac{1}{2\pi f C}$$

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$E = \frac{1}{2} L I^2$$

$$X_L = \frac{V}{I}$$

$$X_L = 2\pi f L$$

$$\frac{\Delta W}{W} = \sqrt{\left(\frac{\Delta X}{X}\right)^2 + \left(\frac{\Delta Y}{Y}\right)^2 + \left(\frac{\Delta Z}{Z}\right)^2}$$

$$\Delta W = \sqrt{\Delta X^2 + \Delta Y^2 + \Delta Z^2}$$

$$d = \bar{v}t$$

$$E_w = QV$$

$$V_{peak} = \sqrt{2}V_{rms}$$

$$s = \bar{v}t$$

$$E = mc^2$$

$$I_{peak} = \sqrt{2}I_{rms}$$

$$v = u + at$$

$$E = hf$$

$$Q = It$$

$$s = ut + \frac{1}{2}at^2$$

$$E_K = hf - hf_0$$

$$V = IR$$

$$v^2 = u^2 + 2as$$

$$E_2 - E_1 = hf$$

$$P = IV = I^2R = \frac{V^2}{R}$$

$$s = \frac{1}{2}(u+v)t$$

$$T = \frac{1}{f}$$

$$R_T = R_1 + R_2 + \dots$$

$$W = mg$$

$$v = f\lambda$$

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

$$F = ma$$

$$ds \sin \theta = m\lambda$$

$$E = V + Ir$$

$$E_w = Fd$$

$$n = \frac{\sin \theta_1}{\sin \theta_2}$$

$$V_1 = \left( \frac{R_1}{R_1 + R_2} \right) V_s$$

$$E_P = mgh$$

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

$$\frac{V_1}{V_2} = \frac{R_1}{R_2}$$

$$E_K = \frac{1}{2}mv^2$$

$$\sin \theta_c = \frac{1}{n}$$

$$C = \frac{Q}{V}$$

$$P = \frac{E}{t}$$

$$I = \frac{k}{d^2}$$

$$E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}$$

$$p = mv$$

$$I = \frac{P}{A}$$

$$\text{path difference} = m\lambda \quad \text{or} \quad \left(m + \frac{1}{2}\right)\lambda \quad \text{where } m = 0, 1, 2, \dots$$

$$F = G \frac{Mm}{r^2}$$

$$\text{random uncertainty} = \frac{\text{max. value} - \text{min. value}}{\text{number of values}}$$

$$t' = \frac{t}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$$

$$l' = l\sqrt{1 - \left(\frac{v}{c}\right)^2}$$

$$f_o = f_s \left( \frac{v}{v \pm v_s} \right)$$

$$z = \frac{\lambda_{observed} - \lambda_{rest}}{\lambda_{rest}}$$

$$z = \frac{v}{c}$$

$$v = H_0 d$$

# Additional Relationships

## Circle

$$\text{circumference} = 2\pi r$$

$$\text{area} = \pi r^2$$

## Sphere

$$\text{area} = 4\pi r^2$$

$$\text{volume} = \frac{4}{3}\pi r^3$$

## Trigonometry

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

## Moment of inertia

point mass

$$I = mr^2$$

rod about centre

$$I = \frac{1}{12}ml^2$$

rod about end

$$I = \frac{1}{3}ml^2$$

disc about centre

$$I = \frac{1}{2}mr^2$$

sphere about centre

$$I = \frac{2}{5}mr^2$$

## Table of standard derivatives

$f(x)$	$f'(x)$
$\sin ax$	$a \cos ax$
$\cos ax$	$-a \sin ax$

## Table of standard integrals

$f(x)$	$\int f(x)dx$
$\sin ax$	$-\frac{1}{a} \cos ax + C$
$\cos ax$	$\frac{1}{a} \sin ax + C$

# Electron Arrangements of Elements

Group	Group	1	2
(1)		H	He
Hydrogen	(2)	1	1
Li	Be	3	4
Lithium	Beryllium	2,1	2,2
Na	Mg	11	12
Sodium	Magnesium	2,8,1	2,8,2
K	Ca	19	20
Potassium	Calcium	2,8,8,1	2,8,8,2
Rb	Sr	37	38
Rubidium	Strontrium	2,8,18,8,1	2,8,18,8,2
Cs	Ba	55	56
Cesium	Barium	2,8,18,18,8,1	2,8,18,18,8,2
Fr	Ra	87	88
Francium	Radium	2,8,18,32,18,8,1	2,8,18,32,18,8,2

(1)

(18)

Key	Atomic number Symbol	Electron arrangement	Name

## Transition Elements

	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
Sc	21	22	23	24	25	26	27	28	29	30
Scandium	2,8,9,2	2,8,10,2	2,8,11,2	2,8,13,1	2,8,13,2	2,8,14,2	2,8,15,2	2,8,16,2	2,8,17,1	Zn
Ti	28	29	30	31	32	33	34	35	36	Kr
Titanium	Chromium	Manganese	Iron	Nickel	Copper	Zinc	Arsenic	Selenium	Br	Neon
V	28	29	30	31	32	33	34	35	36	Krypton
Cr	28	29	30	31	32	33	34	35	36	
Mn	28	29	30	31	32	33	34	35	36	
Fe	28	29	30	31	32	33	34	35	36	
Co	28	29	30	31	32	33	34	35	36	
Ni	28	29	30	31	32	33	34	35	36	
Cu	28	29	30	31	32	33	34	35	36	
Zn	28	29	30	31	32	33	34	35	36	
Al	28,3	28,4	28,5	28,6	28,7	28,8	28,9	28,10	28,11	Ar
Si	28,3	28,4	28,5	28,6	28,7	28,8	28,9	28,10	28,11	Argon
Boron	Carbon	Nitrogen	Oxygen	F	Neon	Fluorine	Neon	Neon	Neon	
Aluminum	Gallium	Germanium	Silicon	Phosphorus	Sulphur	Chlorine	Chlorine	Chlorine	Chlorine	
13	14	15	16	17	18	19	20	21	22	He
Al	Si	P	S	Cl	Ar	Ar	Ar	Ar	Ar	He
14	15	16	17	18	19	20	21	22	23	He
15	16	17	18	19	20	21	22	23	24	He
16	17	18	19	20	21	22	23	24	25	He
17	18	19	20	21	22	23	24	25	26	He
18	19	20	21	22	23	24	25	26	27	He
19	20	21	22	23	24	25	26	27	28	He
20	21	22	23	24	25	26	27	28	29	He
21	22	23	24	25	26	27	28	29	30	He
22	23	24	25	26	27	28	29	30	31	He
23	24	25	26	27	28	29	30	31	32	He
24	25	26	27	28	29	30	31	32	33	He
25	26	27	28	29	30	31	32	33	34	He
26	27	28	29	30	31	32	33	34	35	He
27	28	29	30	31	32	33	34	35	36	He
28	29	30	31	32	33	34	35	36	37	He
29	30	31	32	33	34	35	36	37	38	He
30	31	32	33	34	35	36	37	38	39	He
31	32	33	34	35	36	37	38	39	40	He
32	33	34	35	36	37	38	39	40	41	He
33	34	35	36	37	38	39	40	41	42	He
34	35	36	37	38	39	40	41	42	43	He
35	36	37	38	39	40	41	42	43	44	He
36	37	38	39	40	41	42	43	44	45	He
37	38	39	40	41	42	43	44	45	46	He
38	39	40	41	42	43	44	45	46	47	He
39	40	41	42	43	44	45	46	47	48	He
40	41	42	43	44	45	46	47	48	49	He
41	42	43	44	45	46	47	48	49	50	He
42	43	44	45	46	47	48	49	50	51	He
43	44	45	46	47	48	49	50	51	52	He
44	45	46	47	48	49	50	51	52	53	He
45	46	47	48	49	50	51	52	53	54	He
46	47	48	49	50	51	52	53	54	55	He
47	48	49	50	51	52	53	54	55	56	He
48	49	50	51	52	53	54	55	56	57	He
49	50	51	52	53	54	55	56	57	58	He
50	51	52	53	54	55	56	57	58	59	He
51	52	53	54	55	56	57	58	59	60	He
52	53	54	55	56	57	58	59	60	61	He
53	54	55	56	57	58	59	60	61	62	He
54	55	56	57	58	59	60	61	62	63	He
55	56	57	58	59	60	61	62	63	64	He
56	57	58	59	60	61	62	63	64	65	He
57	58	59	60	61	62	63	64	65	66	He
58	59	60	61	62	63	64	65	66	67	He
59	60	61	62	63	64	65	66	67	68	He
60	61	62	63	64	65	66	67	68	69	He
61	62	63	64	65	66	67	68	69	70	He
62	63	64	65	66	67	68	69	70	71	He
63	64	65	66	67	68	69	70	71	72	He
64	65	66	67	68	69	70	71	72	73	He
65	66	67	68	69	70	71	72	73	74	He
66	67	68	69	70	71	72	73	74	75	He
67	68	69	70	71	72	73	74	75	76	He
68	69	70	71	72	73	74	75	76	77	He
69	70	71	72	73	74	75	76	77	78	He
70	71	72	73	74	75	76	77	78	79	He
71	72	73	74	75	76	77	78	79	80	He
72	73	74	75	76	77	78	79	80	81	He
73	74	75	76	77	78	79	80	81	82	He
74	75	76	77	78	79	80	81	82	83	He
75	76	77	78	79	80	81	82	83	84	He
76	77	78	79	80	81	82	83	84	85	He
77	78	79	80	81	82	83	84	85	86	He
78	79	80	81	82	83	84	85	86	87	He
79	80	81	82	83	84	85	86	87	88	He
80	81	82	83	84	85	86	87	88	89	He
81	82	83	84	85	86	87	88	89	90	He
82	83	84	85	86	87	88	89	90	91	He
83	84	85	86	87	88	89	90	91	92	He
84	85	86	87	88	89	90	91	92	93	He
85	86	87	88	89	90	91	92	93	94	He
86	87	88	89	90	91	92	93	94	95	He
87	88	89	90	91	92	93	94	95	96	He
88	89	90	91	92	93	94	95	96	97	He
89	90	91	92	93	94	95	96	97	98	He
90	91	92	93	94	95	96	97	98	99	He
91	92	93	94	95	96	97	98	99	100	He
92	93	94	95	96	97	98	99	100	101	He
93	94	95	96	97	98	99	100	101	102	He
94	95	96	97	98	99	100	101	102	103	He
95	96	97	98	99	100	101	102	103	104	He
96	97	98	99	100	101	102	103	104	105	He
97	98	99	100	101	102	103	104	105	106	He
98	99	100	101	102	103	104	105	106	107	He
99	100	101	102	103	104	105	106	107	108	He
100	101	102	103	104	105	106	107	108	109	He
101	102	103	104	105	106	107	108	109	110	He
102	103	104	105	106	107	108	109	110	111	He
103	104	105	106	107	108	109	110	111	112	He
104	105	106	107	108	109	110	111	112	113	He
105	106	107	108	109	110	111	112	113	114	He
106	107	108	109	110	111	112	113	114	115	He
107	108	109	110	111	112	113	114	115	116	He
108	109	110	111	112	113	114	115	116	117	He
109	110	111	112	113	114	115	116	117	118	He
110	111	112	113	114	115	116	117	118	119	He
111	112	113	114	115	116	117	118	119	120	He
112	113	114	115	116	117	118	119	120	121	He
113	114	115	116							

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