



National  
Qualifications  
2025

X857/77/11

**Physics  
Relationships sheet**

THURSDAY, 15 MAY

9:00 AM – 12:00 NOON

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## Relationships required for Physics Advanced Higher

$$v = \frac{ds}{dt}$$

$$E_{k(rotational)} = \frac{1}{2} I \omega^2$$

$$a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$E_P = E_{k(translational)} + E_{k(rotational)}$$

$$v = u + at$$

$$F = \frac{GMm}{r^2}$$

$$s = ut + \frac{1}{2}at^2$$

$$F = \frac{GMm}{r^2} = \frac{mv^2}{r} = mr\omega^2 = mr\left(\frac{2\pi}{T}\right)^2$$

$$v^2 = u^2 + 2as$$

$$V = -\frac{GM}{r}$$

$$\omega = \frac{d\theta}{dt}$$

$$E_P = Vm = -\frac{GMm}{r}$$

$$\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$$

$$v_{esc} = \sqrt{\frac{2GM}{r}}$$

$$\omega = \omega_o + at$$

$$\omega^2 = \omega_o^2 + 2\alpha\theta$$

$$r_{Schwarzschild} = \frac{2GM}{c^2}$$

$$\theta = \omega_o t + \frac{1}{2}at^2$$

$$b = \frac{L}{4\pi d^2}$$

$$s = r\theta$$

$$\frac{P}{A} = \sigma T^4$$

$$a_t = r\alpha$$

$$L = 4\pi r^2 \sigma T^4$$

$$\omega = \frac{2\pi}{T}$$

$$E = hf$$

$$\omega = 2\pi f$$

$$mv_r = \frac{nh}{2\pi}$$

$$a_r = \frac{v^2}{r} = r\omega^2$$

$$\lambda = \frac{h}{p}$$

$$F = \frac{mv^2}{r} = mr\omega^2$$

$$\Delta x \Delta p_x \geq \frac{h}{4\pi}$$

$$I = \sum mr^2$$

$$\tau = Fr$$

$$\Delta E \Delta t \geq \frac{h}{4\pi}$$

$$\tau = I\alpha$$

$$F = qvB$$

$$L = mv_r = mr^2\omega$$

$$F = \frac{mv^2}{r}$$

$$L = I\omega$$

$$F = -ky$$

$$\omega = 2\pi f = \frac{2\pi}{T}$$

$$a = \frac{d^2y}{dt^2} = -\omega^2 y$$

$$y = A \cos \omega t \quad \text{or} \quad y = A \sin \omega t$$

$$F = QE$$

$$V = Ed$$

$$W = QV$$

$$E_k = \frac{1}{2}mv^2$$

$$v = \pm \omega \sqrt{(A^2 - y^2)}$$

$$B = \frac{\mu_o I}{2\pi r}$$

$$E_k = \frac{1}{2}m\omega^2(A^2 - y^2)$$

$$F = IlB \sin \theta$$

$$E_P = \frac{1}{2}m\omega^2 y^2$$

$$F = qvB$$

$$E = kA^2$$

$$\tau = RC$$

$$y = A \sin 2\pi \left( ft - \frac{x}{\lambda} \right)$$

$$X_C = \frac{V}{I}$$

$$\phi = \frac{2\pi x}{\lambda}$$

$$X_C = \frac{1}{2\pi f C}$$

$$opd = n \times gpd$$

$$\varepsilon = -L \frac{dI}{dt}$$

$$opd = m\lambda \text{ or } \left(m + \frac{1}{2}\right)\lambda \text{ where } m = 0, 1, 2, \dots$$

$$\Delta x = \frac{\lambda l}{2d}$$

$$E = \frac{1}{2}LI^2$$

$$d = \frac{\lambda}{4n}$$

$$X_L = \frac{V}{I}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$X_L = 2\pi f L$$

$$n = \tan i_P$$

$$\Delta W = \sqrt{\Delta X^2 + \Delta Y^2 + \Delta Z^2}$$

$$F = \frac{Q_1 Q_2}{4\pi \epsilon_o r^2}$$

$$c = \frac{1}{\sqrt{\epsilon_o \mu_o}}$$

$$V = \frac{Q}{4\pi \epsilon_o r}$$

$$\frac{\Delta W}{W} = \sqrt{\left(\frac{\Delta X}{X}\right)^2 + \left(\frac{\Delta Y}{Y}\right)^2 + \left(\frac{\Delta Z}{Z}\right)^2}$$

$$E = \frac{Q}{4\pi \epsilon_o r^2}$$

$$\left(\frac{\Delta W^n}{W^n}\right) = n \left(\frac{\Delta W}{W}\right)$$

|  |  |  |
|--|--|--|
| $d = \bar{v}t$   | $W = QV$   | $V_{peak} = \sqrt{2}V_{rms}$   |
| $s = \bar{v}t$   | $E = mc^2$   | $I_{peak} = \sqrt{2}I_{rms}$   |
| $v = u + at$   | $E = hf$   | $Q = It$   |
| $s = ut + \frac{1}{2}at^2$                                       | $E_K = hf - hf_0$  | $V = IR$   |
| $v^2 = u^2 + 2as$  | $E_2 - E_1 = hf$   | $P = IV = I^2R = \frac{V^2}{R}$  |
| $s = \frac{1}{2}(u+v)t$  | $T = \frac{1}{f}$  | $R_T = R_1 + R_2 + \dots$  |
| $W = mg$   | $v = f\lambda$   | $\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$  |
| $F = ma$   | $d \sin \theta = m\lambda$   | $E = V + Ir$   |
| $E_W = Fd$   | $n = \frac{\sin \theta_1}{\sin \theta_2}$  | $V_1 = \left( \frac{R_1}{R_1 + R_2} \right) V_S$   |
| $E_P = mgh$  | $\frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$        | $\frac{V_1}{V_2} = \frac{R_1}{R_2}$  |
| $E_K = \frac{1}{2}mv^2$  | $\sin \theta_c = \frac{1}{n}$  | $C = \frac{Q}{V}$  |
| $P = \frac{E}{t}$  | $I = \frac{k}{d^2}$  | $E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2} \frac{Q^2}{C}$                                |
| $p = mv$   | $I = \frac{P}{A}$  | path difference = $m\lambda$ or $\left(m + \frac{1}{2}\right)\lambda$ where $m = 0, 1, 2, \dots$ |
| $Ft = mv - mu$   | random uncertainty = $\frac{\text{max. value} - \text{min. value}}{\text{number of values}}$ |  |
| $F = G \frac{Mm}{r^2}$   | $t' = \frac{t}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$                                       |  |
| $l' = l \sqrt{1 - \left(\frac{v}{c}\right)^2}$                   | $f_o = f_s \left( \frac{v}{v \pm v_s} \right)$   |  |
| $z = \frac{\lambda_{observed} - \lambda_{rest}}{\lambda_{rest}}$ | $z = \frac{v}{c}$  |  |
| $v = H_0 d$  |  |  |

## Additional relationships

### Circle

$$\text{circumference} = 2\pi r$$

$$\text{area} = \pi r^2$$

### Sphere

$$\text{area} = 4\pi r^2$$

$$\text{volume} = \frac{4}{3}\pi r^3$$

### Table of standard derivatives

| $f(x)$    | $f'(x)$      |
|-----------|--------------|
| $\sin ax$ | $a \cos ax$  |
| $\cos ax$ | $-a \sin ax$ |

### Trigonometry

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

### Table of standard integrals

| $f(x)$    | $\int f(x)dx$              |
|-----------|----------------------------|
| $\sin ax$ | $-\frac{1}{a} \cos ax + C$ |
| $\cos ax$ | $\frac{1}{a} \sin ax + C$  |

### Moment of inertia

point mass

$$I = mr^2$$

rod about centre

$$I = \frac{1}{12}ml^2$$

rod about end

$$I = \frac{1}{3}ml^2$$

disc about centre

$$I = \frac{1}{2}mr^2$$

sphere about centre

$$I = \frac{2}{5}mr^2$$

## Electron arrangements of elements

| Group 1                                    | Group 2                                    | Group 3                                     | Group 4                                      | Group 5                                      | Group 6                                      | Group 7                                      | Group 0                                      |
|--|--|---|--|--|--|--|--|
|  |  |   |  |  |  |  |  |
| <b>1</b><br><b>H</b><br>1<br>Hydrogen      | <b>2</b><br><b>(2)</b>                     | <b>3</b><br><b>Li</b><br>2,1                | <b>4</b><br><b>Be</b><br>2,2                 | <b>5</b><br><b>B</b><br>2,3                  | <b>6</b><br><b>C</b><br>2,4                  | <b>7</b><br><b>N</b><br>2,5                  | <b>8</b><br><b>O</b><br>2,6                  |
| <b>Lithium</b>                             | <b>Beryllium</b>                           | <b>Boron</b>                                | <b>Nitrogen</b>                              | <b>Oxygen</b>                                | <b>Fluorine</b>                              | <b>Neon</b>                                  | <b>He</b><br>2<br>Helium                     |
| <b>11</b><br><b>Na</b><br>2,8,1            | <b>12</b><br><b>Mg</b><br>2,8,2            | <b>13</b><br><b>Al</b><br>2,8,3             | <b>14</b><br><b>Si</b><br>2,8,4              | <b>15</b><br><b>P</b><br>2,8,5               | <b>16</b><br><b>S</b><br>2,8,6               | <b>17</b><br><b>Cl</b><br>2,8,7              | <b>18</b><br><b>Ar</b><br>2,8,8              |
| <b>Sodium</b>                              | <b>Magnesium</b>                           | <b>Aluminium</b>                            | <b>Silicon</b>                               | <b>Phosphorus</b>                            | <b>Sulfur</b>                                | <b>Chlorine</b>                              | <b>Argon</b>                                 |
| <b>19</b><br><b>K</b><br>2,8,8,1           | <b>20</b><br><b>Ca</b><br>2,8,8,2          | <b>21</b><br><b>Sc</b><br>2,8,9,2           | <b>22</b><br><b>Ti</b><br>2,8,10,2           | <b>23</b><br><b>V</b><br>2,8,11,2            | <b>24</b><br><b>Cr</b><br>2,8,13,1           | <b>25</b><br><b>Mn</b><br>2,8,13,2           | <b>26</b><br><b>Fe</b><br>2,8,14,2           |
| <b>Potassium</b>                           | <b>Calcium</b>                             | <b>Scandium</b>                             | <b>Titanium</b>                              | <b>Vanadium</b>                              | <b>Chromium</b>                              | <b>Manganese</b>                             | <b>Iron</b>                                  |
| <b>37</b><br><b>Rb</b><br>2,8,18,8,1       | <b>38</b><br><b>Sr</b><br>2,8,18,8,2       | <b>39</b><br><b>Y</b><br>2,8,18,9,2         | <b>40</b><br><b>Zr</b><br>2,8,18,10,2        | <b>41</b><br><b>Nb</b><br>2,8,18,12,1        | <b>42</b><br><b>Mo</b><br>2,8,18,13,1        | <b>43</b><br><b>Tc</b><br>2,8,18,13,2        | <b>44</b><br><b>Ru</b><br>2,8,18,15,1        |
| <b>Rubidium</b>                            | <b>Strontrium</b>                          | <b>Yttrium</b>                              | <b>Zirconium</b>                             | <b>Niobium</b>                               | <b>Molybdenum</b>                            | <b>Technetium</b>                            | <b>Ruthenium</b>                             |
| <b>55</b><br><b>Cs</b><br>2,8,18,18,8,1    | <b>56</b><br><b>Ba</b><br>2,8,18,18,8,2    | <b>57</b><br><b>La</b><br>2,8,18,18,9,2     | <b>72</b><br><b>Hf</b><br>2,8,18,32,10,2     | <b>73</b><br><b>Ta</b><br>2,8,18,32,32,11,2  | <b>74</b><br><b>W</b><br>2,8,18,32,12,2      | <b>75</b><br><b>Re</b><br>2,8,18,32,13,2     | <b>76</b><br><b>Os</b><br>2,8,18,32,14,2     |
| <b>Cæsium</b>                              | <b>Barium</b>                              | <b>Lanthanum</b>                            | <b>Hafnium</b>                               | <b>Tantalum</b>                              | <b>Rhenium</b>                               | <b>Iridium</b>                               | <b>Palladium</b>                             |
| <b>87</b><br><b>Fr</b><br>2,8,18,32,18,8,1 | <b>88</b><br><b>Ra</b><br>2,8,18,32,18,8,2 | <b>89</b><br><b>Ac</b><br>2,8,18,32,18,9,2  | <b>104</b><br><b>Rf</b><br>2,8,18,32,32,10,2 | <b>105</b><br><b>Db</b><br>2,8,18,32,32,11,2 | <b>106</b><br><b>Sg</b><br>2,8,18,32,32,12,2 | <b>107</b><br><b>Bh</b><br>2,8,18,32,32,13,2 | <b>108</b><br><b>Hs</b><br>2,8,18,32,32,14,2 |
| <b>Francium</b>                            | <b>Radium</b>                              | <b>Actinium</b>                             | <b>Rutherfordium</b>                         | <b>Dubnium</b>                               | <b>Seaborgium</b>                            | <b>Bohrium</b>                               | <b>Hassium</b>                               |
| <b>Lanthanides</b>                         | <b>57</b><br><b>La</b><br>2,8,18,18,9,2    | <b>58</b><br><b>Ce</b><br>2,8,18,20,8,2     | <b>59</b><br><b>Pr</b><br>2,8,18,21,8,2      | <b>60</b><br><b>Nd</b><br>2,8,18,22,8,2      | <b>61</b><br><b>Pm</b><br>2,8,18,23,8,2      | <b>62</b><br><b>Sm</b><br>2,8,18,24,8,2      | <b>63</b><br><b>Eu</b><br>2,8,18,25,8,2      |
|  | <b>Cerium</b>                              | <b>Praseodymium</b>                         | <b>Neodymium</b>                             | <b>Promethium</b>                            | <b>Samarium</b>                              | <b>Gadolinium</b>                            | <b>Europium</b>                              |
| <b>Actinides</b>                           | <b>89</b><br><b>Ac</b><br>2,8,18,32,18,9,2 | <b>90</b><br><b>Th</b><br>2,8,18,32,18,10,2 | <b>91</b><br><b>Pa</b><br>2,8,18,32,20,9,2   | <b>92</b><br><b>U</b><br>2,8,19,9,2          | <b>93</b><br><b>Np</b><br>2,8,18,32,22,9,2   | <b>94</b><br><b>Pu</b><br>2,8,18,32,24,8,2   | <b>95</b><br><b>Am</b><br>2,8,18,32,25,8,2   |
|  | <b>Thorium</b>                             | <b>Protactinium</b>                         | <b>Uranium</b>                               | <b>Neptunium</b>                             | <b>Plutonium</b>                             | <b>Americium</b>                             | <b>Curium</b>                                |
|  | <b>Berkelium</b>                           | <b>Californium</b>                          | <b>Einsteinium</b>                           | <b>Fermium</b>                               | <b>Mendelevium</b>                           | <b>Noberium</b>                              | <b>Lawrencium</b>                            |

**Key**

|                             |
|-----------------------------|
| <b>Atomic number</b>        |
| <b>Symbol</b>               |
| <b>Electron arrangement</b> |
| <b>Name</b>                 |

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