



National
Qualifications
2017

X757/77/11

**Physics
Relationships Sheet**

WEDNESDAY, 17 MAY

9:00 AM – 11:30 AM



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Relationships required for Physics Advanced Higher

$$v = \frac{ds}{dt}$$

$$L = I\omega$$

$$a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$E_K = \frac{1}{2} I\omega^2$$

$$v = u + at$$

$$F = G \frac{Mm}{r^2}$$

$$s = ut + \frac{1}{2}at^2$$

$$V = -\frac{GM}{r}$$

$$v^2 = u^2 + 2as$$

$$v = \sqrt{\frac{2GM}{r}}$$

$$\omega = \frac{d\theta}{dt}$$

$$\text{apparent brightness, } b = \frac{L}{4\pi r^2}$$

$$\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$$

$$\text{Power per unit area} = \sigma T^4$$

$$\omega = \omega_o + at$$

$$L = 4\pi r^2 \sigma T^4$$

$$\theta = \omega_o t + \frac{1}{2}at^2$$

$$r_{\text{Schwarzschild}} = \frac{2GM}{c^2}$$

$$\omega^2 = \omega_o^2 + 2\alpha\theta$$

$$E = hf$$

$$s = r\theta$$

$$\lambda = \frac{h}{p}$$

$$a_t = r\alpha$$

$$mv_r = \frac{nh}{2\pi}$$

$$a_r = \frac{v^2}{r} = r\omega^2$$

$$\Delta x \Delta p_x \geq \frac{h}{4\pi}$$

$$F = \frac{mv^2}{r} = mr\omega^2$$

$$\Delta E \Delta t \geq \frac{h}{4\pi}$$

$$T = Fr$$

$$F = qvB$$

$$T = I\alpha$$

$$\omega = 2\pi f$$

$$L = mv_r = mr^2\omega$$

$$a = \frac{d^2y}{dt^2} = -\omega^2 y$$

$$y = A \cos \omega t \quad \text{or} \quad y = A \sin \omega t$$

$$v = \pm \omega \sqrt{(A^2 - y^2)}$$

$$E_K = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$E_P = \frac{1}{2} m \omega^2 y^2$$

$$y = A \sin 2\pi(f t - \frac{x}{\lambda})$$

$$E = kA^2$$

$$\phi = \frac{2\pi x}{\lambda}$$

optical path difference = $m\lambda$ or $\left(m + \frac{1}{2}\right)\lambda$
where $m = 0, 1, 2, \dots$

$$\Delta x = \frac{\lambda l}{2d}$$

$$d = \frac{\lambda}{4n}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$n = \tan i_p$$

$$F = \frac{Q_1 Q_2}{4\pi \epsilon_0 r^2}$$

$$E = \frac{Q}{4\pi \epsilon_0 r^2}$$

$$V = \frac{Q}{4\pi \epsilon_0 r}$$

$$F = QE$$

$$V = Ed$$

$$F = IlB \sin \theta$$

$$B = \frac{\mu_0 I}{2\pi r}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

$$t = RC$$

$$X_C = \frac{V}{I}$$

$$X_C = \frac{1}{2\pi f C}$$

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$E = \frac{1}{2} L I^2$$

$$X_L = \frac{V}{I}$$

$$X_L = 2\pi f L$$

$$\frac{\Delta W}{W} = \sqrt{\left(\frac{\Delta X}{X}\right)^2 + \left(\frac{\Delta Y}{Y}\right)^2 + \left(\frac{\Delta Z}{Z}\right)^2}$$

$$\Delta W = \sqrt{\Delta X^2 + \Delta Y^2 + \Delta Z^2}$$

| | | |
|--|--|--|
| $d = \bar{v}t$ | $W = QV$ | $V_{peak} = \sqrt{2}V_{rms}$ |
| $s = \bar{v}t$ | $E = mc^2$ | $I_{peak} = \sqrt{2}I_{rms}$ |
| $v = u + at$ | $E = hf$ | $Q = It$ |
| $s = ut + \frac{1}{2}at^2$ | $E_K = hf - hf_0$ | $V = IR$ |
| $v^2 = u^2 + 2as$ | $E_2 - E_1 = hf$ | $P = IV = I^2R = \frac{V^2}{R}$ |
| $s = \frac{1}{2}(u+v)t$ | $T = \frac{1}{f}$ | $R_T = R_1 + R_2 + \dots$ |
| $W = mg$ | $v = f\lambda$ | $\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$ |
| $F = ma$ | $d \sin \theta = m\lambda$ | $E = V + Ir$ |
| $E_w = Fd$ | $n = \frac{\sin \theta_1}{\sin \theta_2}$ | $V_1 = \left(\frac{R_1}{R_1 + R_2} \right) V_s$ |
| $E_p = mgh$ | $\frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$ | $\frac{V_1}{V_2} = \frac{R_1}{R_2}$ |
| $E_K = \frac{1}{2}mv^2$ | $\sin \theta_c = \frac{1}{n}$ | $C = \frac{Q}{V}$ |
| $P = \frac{E}{t}$ | $I = \frac{k}{d^2}$ | $E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}$ |
| $p = mv$ | $I = \frac{P}{A}$ | path difference = $m\lambda$ or $\left(m + \frac{1}{2}\right)\lambda$ where $m = 0, 1, 2, \dots$ |
| $Ft = mv - mu$ | random uncertainty = $\frac{\text{max. value} - \text{min. value}}{\text{number of values}}$ | |
| $F = G \frac{Mm}{r^2}$ | | |
| $t' = \frac{t}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$ | | |
| $l' = l\sqrt{1 - \left(\frac{v}{c}\right)^2}$ | | |
| $f_o = f_s \left(\frac{v}{v \pm v_s} \right)$ | | |
| $z = \frac{\lambda_{observed} - \lambda_{rest}}{\lambda_{rest}}$ | | |
| $z = \frac{v}{c}$ | | |
| $v = H_0 d$ | | |

Additional Relationships

Circle

$$\text{circumference} = 2\pi r$$

$$\text{area} = \pi r^2$$

Sphere

$$\text{area} = 4\pi r^2$$

$$\text{volume} = \frac{4}{3}\pi r^3$$

Table of standard derivatives

| $f(x)$ | $f'(x)$ |
|-----------|--------------|
| $\sin ax$ | $a \cos ax$ |
| $\cos ax$ | $-a \sin ax$ |

Trigonometry

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

Table of standard integrals

| $f(x)$ | $\int f(x)dx$ |
|-----------|----------------------------|
| $\sin ax$ | $-\frac{1}{a} \cos ax + C$ |
| $\cos ax$ | $\frac{1}{a} \sin ax + C$ |

Moment of inertia

point mass

$$I = mr^2$$

rod about centre

$$I = \frac{1}{12}ml^2$$

rod about end

$$I = \frac{1}{3}ml^2$$

disc about centre

$$I = \frac{1}{2}mr^2$$

sphere about centre

$$I = \frac{2}{5}mr^2$$

Electron Arrangements of Elements

| Key | | Periodic Table of Elements | | | | | | | | | | | | | | | |
|-----|---------------|----------------------------|---------------|----------------------|---------------|----------------|--------------|-----|-----|------------|------------|------|------|-----|------|----|-------|
| | Atomic number | Symbol | | Electron arrangement | | | | | | | | | | | | | |
| | Name | Transition Elements | | | | | | | | | | | | | | | |
| | | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | | | | |
| 1 | H | Hydrogen | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | He | | | |
| 3 | Li | Beryllium | 2,1 | Be | 2,2 | | Boron | C | N | O | F | Ne | 11 | H | | | |
| 11 | Na | Sodium | 2,8,1 | Mg | 2,8,2 | | Magnesium | Al | Si | P | S | Cl | Ar | 13 | | | |
| 19 | K | Calcium | 2,8,8,1 | Ca | 2,8,8,2 | | Scandium | 21 | Ti | V | Mn | Fe | Co | 22 | B | | |
| 21 | Sc | Titanium | 2,8,9,2 | Ti | 2,8,10,2 | 2,8,11,2 | Cr | 24 | Cr | 25 | Mn | Fe | Ni | 23 | C | | |
| 23 | Cr | Vanadium | | | | 2,8,13,1 | 2,8,13,2 | 26 | Fe | 27 | Co | Ni | Cu | 24 | N | | |
| 25 | Mn | Chromium | | | | 2,8,14,2 | 2,8,14,2 | 28 | Co | 29 | Ni | Cu | Zn | 25 | O | | |
| 27 | Fe | Manganese | | | | 2,8,15,2 | 2,8,15,2 | 28 | Ni | 29 | Cu | Zn | Zinc | 26 | F | | |
| 28 | Co | Iron | | | | 2,8,16,2 | 2,8,16,2 | 28 | Cu | 29 | Zn | Zinc | | 2,7 | Neon | | |
| 29 | Ni | Copper | | | | 2,8,18,1 | 2,8,18,1 | 28 | Zn | 30 | | | | | | | |
| 30 | Zn | | | | | 2,8,18,2 | 2,8,18,2 | | | | | | | | | | |
| 37 | Rb | Strontium | 2,8,18,8,1 | Sr | 2,8,18,8,2 | | Yttrium | 39 | Zr | Nb | Mo | Tc | Ru | Pd | 46 | Al | |
| 39 | Y | Zirconium | 2,8,18,9,2 | Zr | 2,8,18,10,2 | 2,8,18,12,1 | Niobium | 40 | Nb | 2,8,18,13, | 2,8,18,13, | 42 | 43 | 44 | 45 | 13 | B |
| 40 | Nb | Molybdenum | | | | 2,8,18,13, | 2,8,18,13, | 42 | Mo | 2,8,18,13, | 2,8,18,13, | 43 | 44 | 45 | 46 | 14 | C |
| 41 | Mo | Technetium | | | | 2,8,18,13, | 2,8,18,13, | 43 | Tc | 2,8,18,15, | 2,8,18,15, | 44 | Ru | Rh | Pd | 15 | N |
| 42 | Tc | Ruthenium | | | | 2,8,18,15, | 2,8,18,15, | 44 | Ru | 2,8,18,16, | 2,8,18,16, | 45 | Rh | Ag | Ag | 16 | O |
| 43 | Ru | Rhodium | | | | 2,8,18,16, | 2,8,18,16, | 45 | Rh | 2,8,18,16, | 2,8,18,16, | 46 | Pd | Cd | Cd | 17 | F |
| 44 | Rh | Palladium | | | | 2,8,18,16, | 2,8,18,16, | 46 | Pd | 2,8,18,18, | 2,8,18,18, | 47 | Ag | Ag | Ag | 18 | Neon |
| 45 | Pd | | | | | 2,8,18,18, | 2,8,18,18, | 47 | Ag | 2,8,18,18, | 2,8,18,18, | 48 | Cd | Ag | Ag | 19 | |
| 46 | Ag | | | | | 2,8,18,18, | 2,8,18,18, | 48 | Cd | 2,8,18,18, | 2,8,18,18, | 49 | Ge | Ga | Ga | 20 | Argon |
| 47 | Cd | Cadmium | | | | 2,8,18,18, | 2,8,18,18, | 49 | Ge | 2,8,18,18, | 2,8,18,18, | 50 | As | Ge | Ge | 21 | |
| 48 | Ag | | | | | 2,8,18,18, | 2,8,18,18, | 50 | As | 2,8,18,18, | 2,8,18,18, | 51 | Se | As | As | 22 | |
| 49 | Ge | Gallium | | | | 2,8,18,18, | 2,8,18,18, | 51 | Se | 2,8,18,18, | 2,8,18,18, | 52 | Br | Se | Br | 23 | |
| 50 | As | Germanium | | | | 2,8,18,18, | 2,8,18,18, | 52 | Br | 2,8,18,18, | 2,8,18,18, | 53 | Kr | Br | Kr | 24 | |
| 51 | Se | Arsenic | | | | 2,8,18,18, | 2,8,18,18, | 53 | Kr | 2,8,18,18, | 2,8,18,18, | 54 | Xe | Kr | Xe | 25 | |
| 52 | Br | Bromine | | | | 2,8,18,18, | 2,8,18,18, | 54 | Xe | 2,8,18,18, | 2,8,18,18, | 55 | I | Xe | Xe | 26 | |
| 53 | Kr | Krypton | | | | 2,8,18,18, | 2,8,18,18, | 55 | I | 2,8,18,18, | 2,8,18,18, | 56 | He | Xe | He | 27 | |
| 54 | Xe | | | | | 2,8,18,18, | 2,8,18,18, | 56 | He | 2,8,18,18, | 2,8,18,18, | 57 | Li | Xe | He | 28 | |
| 55 | La | Hafnium | 2,8,18,18,8,1 | Hf | 2,8,18,18,8,2 | 2,8,18,18,10,2 | Tantalum | 57 | Ta | W | Re | Os | Ir | Pt | 71 | He | |
| 56 | Ba | Tungsten | 2,8,18,18,8,2 | W | 2,8,18,32, | 2,8,18,32, | Rhenium | 72 | Re | 2,8,18,32, | 2,8,18,32, | 73 | Os | Ir | Pt | 57 | |
| 57 | La | Rhenium | 2,8,18,18,9,2 | Ir | 2,8,18,32, | 2,8,18,32, | Osmium | 74 | Os | 2,8,18,32, | 2,8,18,32, | 75 | Pt | Ir | Pt | 58 | |
| 58 | Ba | Platinum | 2,8,18,18,9,2 | Pt | 2,8,18,32, | 2,8,18,32, | Iridium | 76 | Pt | 2,8,18,32, | 2,8,18,32, | 77 | Bi | Pt | Pt | 59 | |
| 59 | La | Platinum | 2,8,18,18,9,2 | Bi | 2,8,18,32, | 2,8,18,32, | Platinum | 78 | Bi | 2,8,18,32, | 2,8,18,32, | 79 | Hg | Bi | Bi | 60 | |
| 60 | Ba | Darmstadtium | 2,8,18,18,9,2 | Hg | 2,8,18,32, | 2,8,18,32, | Darmstadtium | 80 | Hg | 2,8,18,32, | 2,8,18,32, | 81 | Tl | Hg | Hg | 61 | |
| 61 | La | Roentgenium | 2,8,18,18,9,2 | Tl | 2,8,18,32, | 2,8,18,32, | Roentgenium | 82 | Tl | 2,8,18,32, | 2,8,18,32, | 83 | Pb | Tl | Tl | 62 | |
| 62 | Ba | Copernicium | 2,8,18,18,9,2 | Pb | 2,8,18,32, | 2,8,18,32, | Copernicium | 84 | Pb | 2,8,18,32, | 2,8,18,32, | 85 | At | Pb | At | 63 | |
| 63 | La | | 2,8,18,18,9,2 | At | 2,8,18,32, | 2,8,18,32, | | 86 | At | 2,8,18,32, | 2,8,18,32, | 87 | Rn | At | Rn | 64 | |
| 64 | Ba | | 2,8,18,18,9,2 | Rn | 2,8,18,32, | 2,8,18,32, | | 88 | Rn | 2,8,18,32, | 2,8,18,32, | 89 | Lu | Rn | Lu | 65 | |
| 65 | La | Lanthanides | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Lanthanides | 90 | Lu | 2,8,18,32, | 2,8,18,32, | 91 | Lu | Lu | Lu | 66 | |
| 66 | Ba | Actinides | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Actinides | 92 | Lu | 2,8,18,32, | 2,8,18,32, | 93 | Lu | Lu | Lu | 67 | |
| 67 | La | Actinium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Actinium | 94 | Lu | 2,8,18,32, | 2,8,18,32, | 95 | Lu | Lu | Lu | 68 | |
| 68 | Ba | Thorium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Thorium | 96 | Lu | 2,8,18,32, | 2,8,18,32, | 97 | Lu | Lu | Lu | 69 | |
| 69 | La | Protactinium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Protactinium | 98 | Lu | 2,8,18,32, | 2,8,18,32, | 99 | Lu | Lu | Lu | 70 | |
| 70 | Ba | Uranium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Uranium | 100 | Lu | 2,8,18,32, | 2,8,18,32, | 101 | Lu | Lu | Lu | 71 | |
| 71 | La | Neptunium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Neptunium | 102 | Lu | 2,8,18,32, | 2,8,18,32, | 103 | Lu | Lu | Lu | 72 | |
| 72 | Ba | Plutonium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Plutonium | 104 | Lu | 2,8,18,32, | 2,8,18,32, | 105 | Lu | Lu | Lu | 73 | |
| 73 | La | Americium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Americium | 106 | Lu | 2,8,18,32, | 2,8,18,32, | 107 | Lu | Lu | Lu | 74 | |
| 74 | Ba | Curium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Curium | 108 | Lu | 2,8,18,32, | 2,8,18,32, | 109 | Lu | Lu | Lu | 75 | |
| 75 | La | Berkelium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Berkelium | 110 | Lu | 2,8,18,32, | 2,8,18,32, | 111 | Lu | Lu | Lu | 76 | |
| 76 | Ba | Californium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Californium | 112 | Lu | 2,8,18,32, | 2,8,18,32, | 113 | Lu | Lu | Lu | 77 | |
| 77 | La | Einsteinium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Einsteinium | 114 | Lu | 2,8,18,32, | 2,8,18,32, | 115 | Lu | Lu | Lu | 78 | |
| 78 | Ba | Fermium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Fermium | 116 | Lu | 2,8,18,32, | 2,8,18,32, | 117 | Lu | Lu | Lu | 79 | |
| 79 | La | Mendelevium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Mendelevium | 118 | Lu | 2,8,18,32, | 2,8,18,32, | 119 | Lu | Lu | Lu | 80 | |
| 80 | Ba | Nobelium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Nobelium | 120 | Lu | 2,8,18,32, | 2,8,18,32, | 121 | Lu | Lu | Lu | 81 | |
| 81 | La | Lawrencium | 2,8,18,18,9,2 | Lu | 2,8,18,32, | 2,8,18,32, | Lawrencium | 122 | Lu | 2,8,18,32, | 2,8,18,32, | 123 | Lu | Lu | Lu | 82 | |

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