



National  
Qualifications  
2019

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X757/77/11

**Physics**  
**Relationships sheet**

WEDNESDAY, 15 MAY

9:00 AM – 11:30 AM

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# Relationships required for Physics Advanced Higher

$$v = \frac{ds}{dt}$$

$$E_K = \frac{1}{2} I \omega^2$$

$$a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$F = G \frac{Mm}{r^2}$$

$$v = u + at$$

$$V = -\frac{GM}{r}$$

$$s = ut + \frac{1}{2}at^2$$

$$E_P = Vm = -\frac{GMm}{r}$$

$$v^2 = u^2 + 2as$$

$$\omega = \frac{d\theta}{dt}$$

$$v = \sqrt{\frac{2GM}{r}}$$

$$\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$$

$$\text{apparent brightness, } b = \frac{L}{4\pi r^2}$$

$$\omega = \omega_o + at$$

$$\text{Power per unit area} = \sigma T^4$$

$$\theta = \omega_o t + \frac{1}{2}at^2$$

$$L = 4\pi r^2 \sigma T^4$$

$$\omega^2 = \omega_o^2 + 2\alpha\theta$$

$$r_{\text{Schwarzschild}} = \frac{2GM}{c^2}$$

$$s = r\theta$$

$$E = hf$$

$$v = r\omega$$

$$\lambda = \frac{h}{p}$$

$$a_t = r\alpha$$

$$mv_r = \frac{nh}{2\pi}$$

$$a_r = \frac{v^2}{r} = r\omega^2$$

$$\Delta x \Delta p_x \geq \frac{h}{4\pi}$$

$$F = \frac{mv^2}{r} = mr\omega^2$$

$$\Delta E \Delta t \geq \frac{h}{4\pi}$$

$$T = Fr$$

$$T = I\alpha$$

$$F = qvB$$

$$L = mv_r = mr^2\omega$$

$$\omega = 2\pi f$$

$$L = I\omega$$

$$\omega = \frac{2\pi}{T}$$

$$a = \frac{d^2y}{dt^2} = -\omega^2 y$$

$$F = IlB \sin \theta$$

$$y = A \cos \omega t \quad \text{or} \quad y = A \sin \omega t$$

$$B = \frac{\mu_o I}{2\pi r}$$

$$v = \pm \omega \sqrt{(A^2 - y^2)}$$

$$c = \frac{1}{\sqrt{\epsilon_o \mu_o}}$$

$$E_k = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$t = RC$$

$$y = A \sin 2\pi(f t - \frac{x}{\lambda})$$

$$X_C = \frac{V}{I}$$

$$E = kA^2$$

$$X_C = \frac{1}{2\pi f C}$$

$$\phi = \frac{2\pi x}{\lambda}$$

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$\text{optical path difference} = m\lambda \quad \text{or} \quad \left(m + \frac{1}{2}\right)\lambda$$

$$E = \frac{1}{2} L I^2$$

where  $m = 0, 1, 2, \dots$

$$\text{optical path difference} = n \times \text{geometrical path difference}$$

$$X_L = \frac{V}{I}$$

$$\Delta x = \frac{\lambda l}{2d}$$

$$X_L = 2\pi f L$$

$$d = \frac{\lambda}{4n}$$

$$\frac{\Delta W}{W} = \sqrt{\left(\frac{\Delta X}{X}\right)^2 + \left(\frac{\Delta Y}{Y}\right)^2 + \left(\frac{\Delta Z}{Z}\right)^2}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$\Delta W = \sqrt{\Delta X^2 + \Delta Y^2 + \Delta Z^2}$$

$$n = \tan i_p$$

$$F = \frac{Q_1 Q_2}{4\pi\epsilon_o r^2}$$

$$E = \frac{Q}{4\pi\epsilon_o r^2}$$

$$V = \frac{Q}{4\pi\epsilon_o r}$$

$$F = QE$$

$$V = Ed$$

$d = \bar{v}t$	$W = QV$	$V_{peak} = \sqrt{2}V_{rms}$
$s = \bar{v}t$	$E = mc^2$	$I_{peak} = \sqrt{2}I_{rms}$
$v = u + at$	$E = hf$	$Q = It$
$s = ut + \frac{1}{2}at^2$	$E_K = hf - hf_0$	$V = IR$
$v^2 = u^2 + 2as$	$E_2 - E_1 = hf$	$P = IV = I^2R = \frac{V^2}{R}$
$s = \frac{1}{2}(u+v)t$	$T = \frac{1}{f}$	$R_T = R_1 + R_2 + \dots$
$W = mg$	$v = f\lambda$	$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$
$F = ma$	$d \sin \theta = m\lambda$	$E = V + Ir$
$E_w = Fd$	$n = \frac{\sin \theta_1}{\sin \theta_2}$	$V_1 = \left( \frac{R_1}{R_1 + R_2} \right) V_s$
$E_p = mgh$	$\frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$	$\frac{V_1}{V_2} = \frac{R_1}{R_2}$
$E_K = \frac{1}{2}mv^2$	$\sin \theta_c = \frac{1}{n}$	$C = \frac{Q}{V}$
$P = \frac{E}{t}$	$I = \frac{k}{d^2}$	$E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}$
$p = mv$	$I = \frac{P}{A}$	path difference = $m\lambda$ or $\left(m + \frac{1}{2}\right)\lambda$ where $m = 0, 1, 2, \dots$
$Ft = mv - mu$	random uncertainty = $\frac{\text{max. value} - \text{min. value}}{\text{number of values}}$	
$F = G \frac{Mm}{r^2}$		
$t' = \frac{t}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$		
$l' = l\sqrt{1 - \left(\frac{v}{c}\right)^2}$		
$f_o = f_s \left( \frac{v}{v \pm v_s} \right)$		
$z = \frac{\lambda_{observed} - \lambda_{rest}}{\lambda_{rest}}$		
$z = \frac{v}{c}$		
$v = H_0 d$		

# Additional Relationships

## Circle

$$\text{circumference} = 2\pi r$$

$$\text{area} = \pi r^2$$

## Sphere

$$\text{area} = 4\pi r^2$$

$$\text{volume} = \frac{4}{3}\pi r^3$$

## Table of standard derivatives

$f(x)$	$f'(x)$
$\sin ax$	$a \cos ax$
$\cos ax$	$-a \sin ax$

## Trigonometry

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

## Table of standard integrals

$f(x)$	$\int f(x)dx$
$\sin ax$	$-\frac{1}{a} \cos ax + C$
$\cos ax$	$\frac{1}{a} \sin ax + C$

## Moment of inertia

point mass

$$I = mr^2$$

rod about centre

$$I = \frac{1}{12}ml^2$$

rod about end

$$I = \frac{1}{3}ml^2$$

disc about centre

$$I = \frac{1}{2}mr^2$$

sphere about centre

$$I = \frac{2}{5}mr^2$$

## Electron Arrangements of Elements

Key		Periodic Table of Elements																															
		Atomic number		Symbol		Electron arrangement																											
				Name																													
1	H		Hydrogen												2	He																	
3	Li	4	Be	2,1	2,2	(2)												2	He														
11	Na	12	Mg	2,8,1	2,8,2	Lithium												10	Ne														
Sodium		Magnesium		(3)												2,8,8		2	He														
19	K	20	Ca	2,8,8,1	2,8,8,2	Potassium												18	Ar														
37	Rb	38	Sr	2,8,18,8,1	2,8,18,8,2	Rubidium												17	Cl														
55	Cs	56	Ba	2,8,18,18,8,1	2,8,18,18,8,2	Csodium												16	S														
87	Fr	88	Ra	2,8,18,32,18,8,1	2,8,18,32,18,8,2	Francium												15	P														
Transition Elements		(4)		(5)		(6)		(7)		(8)		(9)		(10)		(11)		(12)															
21	Sc	22	Ti	23	V	24	Cr	25	Mn	26	Fe	27	Ni	28	Cu	29	Zn	30	Aluminum														
39	Y	40	Zr	41	Nb	42	Mo	43	Tc	44	Ru	45	Rh	46	Pd	47	Ag	48	Gallium														
57	La	72	Hf	73	Ta	74	Re	75	Os	76	Pt	77	Ir	78	Au	79	Hg	80	Germanium														
89	Ac	104	Rf	105	Db	106	Sg	107	Bh	108	Hs	109	Mt	110	Ds	111	Rg	112	Arsenic														
Lanthanides		57	La	58	Ce	59	Pr	60	Nd	61	Pm	62	Sm	63	Eu	64	Gd	65	Dy	66	Ho	67	Er	68	Tm	69	Yb	70	Lu	71	H		
Actinides		89	Th	90	Pa	91	U	92	Np	93	Pu	94	Am	95	Cm	96	Bk	97	Cf	98	Es	99	Fm	100	Md	101	No	102	Lr	103	He		
		Lanthanum		Cerium		Praseodymium		Neodymium		Promethium		Samarium		Europium		Gadolinium		Terbium		Dysprosium		Holmium		Erbium		Thulium		Ytterbium		Lutetium		H	
		Lanthanum		Cerium		Praseodymium		Neodymium		Promethium		Samarium		Europium		Gadolinium		Terbium		Dysprosium		Holmium		Erbium		Thulium		Ytterbium		Lutetium		H	
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