

2019 Mathematics

National 5 - Paper 2

Finalised Marking Instructions

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General marking principles for National 5 Mathematics

Always apply these general principles. Use them in conjunction with the detailed marking instructions, which identify the key features required in candidates' responses.

For each question, the marking instructions are generally in two sections:

- generic scheme this indicates why each mark is awarded
- illustrative scheme this covers methods which are commonly seen throughout the marking

In general, you should use the illustrative scheme. Only use the generic scheme where a candidate has used a method not covered in the illustrative scheme.

- (a) Always use positive marking. This means candidates accumulate marks for the demonstration of relevant skills, knowledge and understanding; marks are not deducted for errors or omissions.
- (b) If you are uncertain how to assess a specific candidate response because it is not covered by the general marking principles or the detailed marking instructions, you must seek guidance from your team leader.
- (c) One mark is available for each •. There are no half marks.
- (d) If a candidate's response contains an error, all working subsequent to this error must still be marked. Only award marks if the level of difficulty in their working is similar to the level of difficulty in the illustrative scheme.
- (e) Only award full marks where the solution contains appropriate working. A correct answer with no working receives no mark, unless specifically mentioned in the marking instructions.
- (f) Candidates may use any mathematically correct method to answer questions, except in cases where a particular method is specified or excluded.
- (g) If an error is trivial, casual or insignificant, for example $6 \times 6 = 12$, candidates lose the opportunity to gain a mark, except for instances such as the second example in point (h) below.

(h) If a candidate makes a transcription error (question paper to script or within script), they lose the opportunity to gain the next process mark, for example

This is a transcription error and so the mark is not awarded. $x^2 + 5x + 7 = 9x + 4$ This is no longer a solution of a quadratic equation, so the mark is not awarded. x = 1

The following example is an exception to the above

This error is not treated as a transcription error, as the candidate deals with the intended quadratic equation. The candidate has been given the benefit of the doubt and all marks awarded. $x^2 + 5x + 7 = 9x + 4$ x - 4x + 3 = 0(x - 3)(x - 1) = 0x = 1 or 3

(i) Horizontal/vertical marking

If a question results in two pairs of solutions, apply the following technique, but only if indicated in the detailed marking instructions for the question.

Example:

•5 •6
•5
$$x = 2$$
 $x = -4$
•6 $y = 5$ $y = -7$

Horizontal: $\bullet^5 x = 2$ and x = -4 Vertical: $\bullet^5 x = 2$ and y = 5 $\bullet^6 y = 5$ and y = -7 Vertical: $\bullet^5 x = 2$ and y = 5

You must choose whichever method benefits the candidate, **not** a combination of both.

(j) In final answers, candidates should simplify numerical values as far as possible unless specifically mentioned in the detailed marking instruction. For example

 $\frac{15}{12}$ must be simplified to $\frac{5}{4}$ or $1\frac{1}{4}$ $\frac{43}{1}$ must be simplified to 43

 $\frac{15}{0.3}$ must be simplified to 50 $\frac{\frac{4}{5}}{3}$ must be simplified to $\frac{4}{15}$

 $\sqrt{64}$ must be simplified to 8*

*The square root of perfect squares up to and including 100 must be known.

- (k) Commonly Observed Responses (COR) are shown in the marking instructions to help mark common and/or non-routine solutions. CORs may also be used as a guide when marking similar non-routine candidate responses.
- (I) Do not penalise candidates for any of the following, unless specifically mentioned in the detailed marking instructions:
 - working subsequent to a correct answer
 - correct working in the wrong part of a question
 - legitimate variations in numerical answers/algebraic expressions, for example angles in degrees rounded to nearest degree
 - omission of units
 - bad form (bad form only becomes bad form if subsequent working is correct), for example

$$(x^3 + 2x^2 + 3x + 2)(2x + 1)$$
 written as
 $(x^3 + 2x^2 + 3x + 2) \times 2x + 1$
 $= 2x^4 + 5x^3 + 8x^2 + 7x + 2$
gains full credit

- repeated error within a question, but not between questions or papers
- (m) In any 'Show that...' question, where candidates have to arrive at a required result, the last mark is not awarded as a follow-through from a previous error, unless specified in the detailed marking instructions.
- (n) You must check all working carefully, even where a fundamental misunderstanding is apparent early in a candidate's response. You may still be able to award marks later in the question so you must refer continually to the marking instructions. The appearance of the correct answer does not necessarily indicate that you can award all the available marks to a candidate.
- (o) You should mark legible scored-out working that has not been replaced. However, if the scored-out working has been replaced, you must only mark the replacement working.
- (p) If candidates make multiple attempts using the same strategy and do not identify their final answer, mark all attempts and award the lowest mark. If candidates try different valid strategies, apply the above rule to attempts within each strategy and then award the highest mark.

For example:

Strategy 1 attempt 1 is worth 3 marks.	Strategy 2 attempt 1 is worth 1 mark.
Strategy 1 attempt 2 is worth 4 marks.	Strategy 2 attempt 2 is worth 5 marks.
From the attempts using strategy 1, the resultant mark would be 3.	From the attempts using strategy 2, the resultant mark would be 1.

In this case, award 3 marks.

Marking instructions for each question

Question		n	Generic scheme	Illustrative scheme	Max mark
1.			•¹ know how to increase by 15%	•¹ ×1·15	3
			•² know how to calculate number of packages after 3 years	• 2 80 000×1·15 ³	
			•³ evaluate	•³ 121 670	

Notes:

1. Correct answer without working

award 3/3

2. Where an incorrect percentage is used, the working must be followed through to give the possibility of awarding 2/3

eg 80
$$000 \times 0.15^3 = 270$$

award 2/3 × ✓ ✓

3. Where an incorrect power (≥ 2) is used, the working must be followed through to give the possibility of awarding 2/3

eg
$$80\,000\times1\cdot15^2=105\,800$$
, $80\,000\times1\cdot15^4=139\,920(\cdot5)$ or $139\,921$

award 2/3 √×√

- 4. Where division is used
 - (a) along with 1.15, \bullet^1 is not available eg 80 000 ÷ 1.15³ = 52601(·2...)

award 2/3 ×√√

(b) along with an incorrect percentage, \bullet^1 and \bullet^2 are not available eg $80~000 \div 0.85^3 = 130266(.6...)$ or 130266

award 1/3 ××√

Commonly observed responses:

1.
$$80\,000\times1\cdot015^3=83654(\cdot27)$$

award 2/3 ×√√

2.
$$80\,000 \times 0.85^3 = 49\,130$$

award 2/3 ×√√

3.
$$80\,000 \times 1.15 = 92\,000$$

award 1/3 √××

4.
$$80\,000 \times 1.15 \times 3 = 276\,000$$

award 1/3 √××

award 1/3 √××

5.
$$80\,000 \times 0.15 = 12\,000 \rightarrow 80\,000 + 3 \times 12\,000 = 116\,000$$

6.
$$80\,000\times0.15\times3=36\,000$$

award 0/3

Question		n	Generic scheme	Illustrative scheme	Max mark	
2.			•¹ start process	$\bullet^1 6^2 + 27^2 + (-18)^2$	2	
			•² consistent solution	•² 33		
	Notes: 1. Correct answer without working					

- 1. Correct answer without working,
- award 2/2

- 2. Accept $6^2 + 27^2 + 18^2$ for the award of \bullet^1
- 3. For a solution of $21(\sqrt{6^2+27^2-18^2})$, with or without working, award 1/2
- 4. For eg $\sqrt{6^2 + (-18)^2} = \sqrt{360} = 18.97...$ or $6\sqrt{10}$ award 0/2
- 5. For eg $\frac{\sqrt{6^2 + 27^2 + (-18)^2}}{2 \times 6 \times 27} = \frac{33}{324} = \frac{11}{108} = 0.1...$ award 0/2

Commonly Observed Responses:

No working necessary

- 1. $\sqrt{1089}$ or 1089 award 1/2 \checkmark ×

Notes:

- 1. Correct answer without working award 2/2
- 2. For $45 \times 70 \times \sin 129 = 2448(.0...)$ award $1/2 \times \sqrt{}$
- 3. Inappropriate use of RAD or GRAD should only be penalised once in Qu 3, 7, 11, 14 or 19
 - (a) \pm 304·7...(RAD) [no working necessary] award 1/2 \checkmark × (b) 1414·3... (GRAD) [no working necessary] award 1/2 \checkmark ×
- 4. Where cosine rule is used award 0/2

1.
$$\frac{1}{2} \times 45 \times 70 \times \sin 129 = \sqrt{1224 \cdot ...} = 34 \cdot 9...$$
 award 1/2

Question		Generic scheme	Illustrative scheme	Max mark
4.		•¹ correct method	• $0.08 \times 3.6 \times 10^{-6}$ or equivalent	2
		•² answer	• 2 2.88×10^{-7} (kg)	

1. Correct answer without working

award 2/2

2. Accept 2.9×10^{-7} (no working necessary)

award 2/2

- 3. Accept $100\% = 3.6 \times 10^{-6} \rightarrow 1\% = ... \rightarrow 8\% = ...$ for the award of \bullet^1
- 4. For 0.000000288 or $\frac{9}{31250000}$ (no working necessary)

award 1/2 √×

5. For $(0.08 \times 3.6 = 0.288 \rightarrow) 0.288 \times 10^{-6}$ (no working necessary)

award 1/2 √×

6. •² is available for correctly carrying out calculation(s) involving a number expressed in scientific notation and a change in the power of 10; the answer must be given in scientific notation.

Commonly observed responses:

1. $0.08 \times 3.6 \times 10^{-6} = 2.8 \times 10^{-7}$

award 1/2 √×

2. $0.08 \times 3600000 = 2.88 \times 10^5$

award 1/2 ×√

3. $3.6 \times 10^{-6} \div 8 = 4.5 \times 10^{-7}$

award 1/2 ×√

4.(a) $3.6 \times 10^{-6} \div 8\% = 4.5 \times 10^{-5}$

award 1/2 ×√

(b) $3.6 \times 10^{-6} \div 8\% = 4.5 \times 10^{-7}$

award 0/2

Question		n	Generic Scheme	Illustrative Scheme	Max Mark
5.			•¹ state coordinates of A	•1 (3,0,0)	2
			•² state coordinates of B	•² (3,3,8)	

- 1. The maximum mark available is 1/2 where brackets are omitted and/or answers are given in component form See COR 1.
- 2. (a) For (3,0,0) and (3,3,8) (b) For B(3,0,0) and A(3,3,8)

award 2/2 award 1/2

3. For eg (0,0,3) **and** (8,3,3) [repeated error]

award 1/2

- 4. 2 is available for answers of the form $A(x,0,0) \rightarrow B(x,x,8)$ See COR 2.
- 5. Answer(s) given in two dimensions
 - (a) Where both answers are given in 2D award 0/2
 - (b) Where one answer is given in 2D and one in 3D
 - (i) award 1/2 for the correct answer eg (3,0) and (3,3,8)
- award 1/2 award 0/2

(ii)follow through mark is not available

- eg (6,0) and (6,6,8)

Commonly observed responses:

1. (a)
$$\begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix}$$
 and
$$\begin{pmatrix} 3 \\ 3 \\ 8 \end{pmatrix}$$

award 1/2 ×√

- 3 3
- (b) 0 and 3 0 8

award 1/2 ×√

2. (a) (6,0,0) and (6,6,8)

award 1/2 ×√

(b) (6,0,0) and (6,3,8)

Question	Generic scheme	Illustrative scheme	Max mark
6.	 •¹ correct substitution into quadratic formula •² evaluate discriminant •³ calculate both roots correct to one decimal place 	•¹ $\frac{-9 \pm \sqrt{9^2 - 4 \times 3 \times (-2)}}{2 \times 3}$ •² 105 (stated or implied by •³) •³ $-3.2, 0.2$	3

1. Correct answer without working

award 0/3

2. • 3 is only available when $b^2 - 4ac > 0$, and the roots require rounding.

1.
$$105(b^2-4ac)$$

2.
$$\frac{-9 \pm \sqrt{9^2 - 4 \times 3 \times (-2)}}{2 \times 3} = \frac{-9 \pm \sqrt{57}}{6} = -2 \cdot 8, -0 \cdot 2$$

3.
$$\frac{-9 \pm \sqrt{9^2 - 4 \times 3 \times 2}}{2 \times 3} = \frac{-9 \pm \sqrt{57}}{6} = -2 \cdot 8, -0 \cdot 2$$

4.
$$\frac{-9 \pm \sqrt{9^2 - 4 \times 3 \times \left(-2\right)}}{2 \times 3} = \frac{-9 \pm \sqrt{105}}{6} = -10 \cdot 7, -7 \cdot 3$$

5.
$$-9\frac{\pm\sqrt{9^2-4\times3\times(-2)}}{2\times3} = -9\frac{\pm\sqrt{105}}{6} = -10\cdot7, -7\cdot3$$

Q	Question		Generic Scheme	Illustrative Scheme	Max Mark
7.			 1 correct substitution into cosine rule to find angle Z 2 evaluate 3 calculate angle 	• $^{1} (\cos Z =) \frac{7 \cdot 2^{2} + 8 \cdot 5^{2} - 6 \cdot 3^{2}}{2 \times 7 \cdot 2 \times 8 \cdot 5}$ • $^{2} (\cos Z =) \frac{84 \cdot 4}{122 \cdot 4} \left(= \frac{211}{306} = 0.689 \right)$ • $^{3} (Z =) 46 \cdot 406$	3

- 1. Correct answer without working award 0/3
- 2. Where two or three more angles are calculated correctly
 - (a) all three angles are calculated correctly; 46·4 need not be identified

award 3/3

(b) two angles are calculated correctly and 46·4 has been clearly identified

award 3/3

(c) two angles are calculated correctly and 46·4 has **NOT** been clearly identified

award 2/3 √√×

- 3. Do not penalise omission of degrees sign
- 4. Disregard errors due to premature rounding provided there is evidence
- 5. Inappropriate use of RAD or GRAD should only be penalised once in Qu 3, 7, 11, 14 or 19
 - (a) 0.81... (RAD)
 - (b) 51.56... (GRAD)

Commonly observed responses:

1.
$$\frac{8 \cdot 5^2 + 6 \cdot 3^2 - 7 \cdot 2^2}{2 \times 8 \cdot 5 \times 6 \cdot 3} \left(= \frac{60 \cdot 1}{107 \cdot 1} = \frac{601}{1071} = 0 \cdot 561... \right) \rightarrow 55 \cdot 86...$$

award 2/3 ×√√

2.
$$\frac{7 \cdot 2^2 + 6 \cdot 3^2 - 8 \cdot 5^2}{2 \times 7 \cdot 2 \times 6 \cdot 3} \left(= \frac{19 \cdot 28}{90 \cdot 72} = \frac{241}{1134} = 0 \cdot 212... \right) \rightarrow 77 \cdot 72...$$

award 2/3 × ✓ ✓

3.
$$(\cos Z =) \frac{7 \cdot 2^2 + 8 \cdot 5^2 - 6 \cdot 3^2}{2 \times 7 \cdot 2 \times 8 \cdot 5} = \sqrt{0.689...} \rightarrow Z = 33.8...$$

award 2/3 √×√

Q	Question		Generic Scheme	Illustrative Scheme	Max Mark
8.			•¹ correct substitution into formula for volume of sphere	$\bullet^1 \frac{4}{3} \times \pi \times 12^3$	5
			•² correct substitution into formula for volume of cylinder	$\bullet^2 \pi \times 12^2 \times 58$	
			• know to add volume of hemisphere to volume of cylinder	$\bullet^3 \frac{1}{2} \times \frac{4}{3} \times \pi \times 12^3 + \pi \times 12^2 \times 58$	
			• all calculations correct (must involve the sum or difference of two different calculations both involving π)	$\bullet^{4}(3619\cdot1+26238\cdot5)=29857\cdot$	
			• round final answer to 3 significant figures and state correct units	• ⁵ 29 900 cm ³	

Question	Generic scheme	Illustrative scheme	Max mark
Notes: 1. Correct ansv	wer without working	award 0/5	
2. Accept 29 9	00 ml or 29∙9 litres		
3. Accept varia			
eg $\frac{1}{2} \times \frac{4}{3} \times 3$	$3.14 \times 12^3 + 3.14 \times 12^2 \times 58 = 29842.56 =$	29800 cm ³	
4. ● ⁵ is not ava	ilable if final answer is given in terms o	· π	
$eg \frac{2}{3} \times \pi \times 1$	$2^3 + \pi \times 12^2 \times 58 = 1152\pi + 8352\pi = 9504\pi$	cm ³ award 4/5 \checkmark	c
5. In awarding	• ⁵ diate calculations need not be shown		
` '	$\frac{4}{3} \times \pi \times 12^3 + \pi \times 12^2 \times 58 = 29900 \text{ cm}^3$	award 5/5	
(b) Where in	ntermediate calculations are shown, the		
	four significant figures 9·1+ 26238·5= 3620+26200 = 298	20=29800 cm ³ award 4/5 \checkmark \checkmark \checkmark	
Commonly obse	erved responses:		
$1. \frac{1}{2} \times \frac{4}{3} \times \pi \times 2$	$24^3 + \pi \times 24^2 \times 58 = 134000\text{cm}^3$	award 4/5 ×√√√	/
$2. \frac{1}{2} \times \frac{4}{3} \times \pi \times 2$	$24^2 + \pi \times 24^2 \times 58 = 106000\text{cm}^3$	award 4/5 ×√√√√	/
$3. \frac{1}{2} \times \frac{4}{3} \times \pi \times 1$	$12^3 + \pi \times 12^2 \times 70 = 35300 \text{cm}^3$	award 4/5 ✓×√✓√	•
$4. \frac{1}{2} \times \frac{4}{3} \times \pi \times 2$	$24^3 + \pi \times 24^2 \times 70 = 156000\text{cm}^3$	award 3/5 ××√√√	
$5. \frac{4}{3} \times \pi \times 12^3 -$	$+\pi \times 12^2 \times 58 = 33500 \text{cm}^3$	award 4/5 ✓✓×✓✓	/
$6. \frac{1}{2} \times \frac{4}{3} \times \pi \times 1$	$12^3 + \pi \times 24 \times 58 = 7990 \text{cm}^3$	award 4/5 √×√√√	
$7. \frac{4}{3} \times \pi \times 12^3 =$	=7240 cm ³	award 2/5 √×××√	
$8. \frac{1}{2} \times \frac{4}{3} \times \pi \times 1$	$12^3 = 3620 \text{cm}^3$	award 2/5 √×××√	
9. $\pi \times 12^2 \times 58$	$= 26200 \text{cm}^3$	award 2/5 ×√××√	

	Question	n	Generic scheme		Illustrative scheme	Max mark
9.			• 1 know that $102.5\% = £977.85$	•1	$102 \cdot 5(\%) = 977 \cdot 85$	3
			•² begin valid strategy	● ²	977⋅85÷102⋅5 or equivalent	
			•³ complete calculation within valid strategy	•3	(£)23·85	
-	tes: Correct	answ	ver without working award 3/3			
2.		evide	35=24·45 ence of •¹		award 1/3 √×× award 0/3	
3.		evide	•85=953•40 ence of •¹		award 1/3 √×× award 0/3	
Co	mmonly	obse	rved responses:			
1.	977·85 1·025	= 95	4		award 2/3 √√×	
2.	(a) 97·5	5% = 9	$977.85 \rightarrow \frac{977.85}{0.975} = 1002.92$		award 1/3 ×√×	
	(b) $\frac{977}{0.9}$	·85 975	1002·92		award 0/3	
3.	(a) 2·5%	% = 97	$7.85 \rightarrow \frac{977.85}{0.025} = 39.114$		award 1/3 ×√×	

award 0/3

(b) $\frac{977.85}{0.025} = 39114$

Question		n	Generic scheme	Illustrative scheme	Max mark
10.			•¹ correct bracket with square	$\bullet^1 (x+5)^2 \dots$	2
			•² complete process	$ \bullet^2 (x5)^2 - 40$	

- 1. Correct answer without working award 2/2
- 2. Answer for \bullet^2 must be consistent with \bullet^1

eg (a)
$$(x\pm 10)^2 - 115$$

(b)
$$(x\pm 10)^2 - 40$$

award 0/2

Commonly observed responses:

No working necessary.

1. Award 2/2 for (a) $(x+5)^2 + (-40) \text{ or } (x+5)^2 + -40$

(b)
$$(x+5)(x+5)-40$$

2. Award 1/2 × \(\sqrt{a} \) for (a) $(x \pm 5) - 40$

(b)
$$(x^2 \pm 5) - 40$$

(c)
$$(x^2 \pm 5)^2 - 40$$

(d)
$$(x \pm 5x)^2 - 40$$

Q	uestio	n	Generic scheme	Illustrative scheme	Max mark
11.			Method 1	Method 1	4
			•1 use perimeter to find length of BC and use a valid strategy (Converse of Pythagoras' Theorem)	• 1 eg $600^{2} + 250^{2}$ and 650^{2}	
			•² evaluate	\bullet^2 $600^2 + 250^2 = 422500$ and $650^2 = 422500$	
			•³ explicit comparison	$\bullet^3 600^2 + 250^2 = 650^2$	
			• ⁴ conclusion with valid reason	• ⁴ Yes, as angle is a right angle.	
			Method 2	Method 2	
			 use perimeter to find length of BC and use a valid strategy (correct substitution into cosine rule) 	$\bullet^{1} (\cos B =) \frac{600^{2} + 250^{2} - 650^{2}}{2 \times 600 \times 250}$	
			•² evaluate	$ \bullet^2 (\cos B =) 0 $	
			•³ calculate angle	• $(B=)90$ [stated explicitly]	
			• 4 conclusion with reason	• ⁴ Yes, as angle is a right angle	

Question	Generic scheme	Illustrative scheme	Max mark
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- 1. For method 1 there must be an explicit comparison stated for the award of \bullet^3
- 2. The conclusion must include a reference to 90° or a right angle.
- 3. (a) Where candidate starts by stating that eg $650^2 = 600^2 + 250^2$, \bullet^1 and \bullet^3 are not available $650^2 = 600^2 + 250^2$ $\times \bullet^1 \times \bullet^3$ (marks not available) 422 $500 = 422 \, 500$ $\checkmark \bullet^2$ (evaluation) Yes, as it's right-angled $\checkmark \bullet^4$ (conclusion and reason) award $2/4 \times \checkmark \times \checkmark$
 - (b) Where candidate starts by stating that eg If triangle is right-angled then $650^2 = 600^2 + 250^2$ s not available

If triangle is right-angled then $650^2 = 600^2 + 250^2$ $\checkmark \bullet^1 \times \bullet^3$ (\bullet^3 not available) 422 500 = 422 500 $\checkmark \bullet^2$ (evaluation) Yes $\checkmark \bullet^4$ (conclusion; reason implicit in $\checkmark \bullet^1$) award $3/4 \checkmark \checkmark \times \checkmark$

- 4. (a) Where there is no working to indicate how 250 has been obtained, then assume it has been obtained using the perimeter.
 - (b) Where working shows that 250 has been obtained by the use of Pythagoras' theorem, \bullet^1 is not available; apply the MIs for the award of \bullet^2 , \bullet^3 and \bullet^4
- 5. Inappropriate use of RAD or GRAD should only be penalised once in Qu 3, 7, 11, 14 or 19 (a) 1.57... (RAD), no, angle is not a right angle
 - (b) 100 (GRAD), no, angle is not a right angle

Commonly observed responses:

1. Variation on Method 1: award 4/4

eg
$$600^2 + 250^2 = 422500$$

 $\sqrt{422500} = 650$
 $600^2 + 250^2 = 650^2$

Yes, as angle is a right angle

- 2. $(\cos A =)\frac{600^2 + 650^2 250^2}{2 \times 600 \times 650} = \frac{12}{13} \rightarrow A = 22 \cdot 6...$ award 2/4 × \checkmark ×
- 3. If triangle is right-angled then $BC^2 = 650^2 600^2$ $\checkmark \bullet^1$

BC = 250 $\checkmark \bullet^2$ (evaluation)

Yes $\checkmark \bullet^4$ (conclusion; reason implicit in $\checkmark \bullet^1$) award 4/4

(conclusion, reason implicit in a) award in a

4. $BC^2 = 650^2 - 600^2$ $\times \bullet^1$ (mark not available)

BC = 250 $\checkmark \bullet^2$ (evaluation)

Yes, as angle is a right angle $\checkmark \bullet^4$ (conclusion and reason) award 3/4 $\times \checkmark \checkmark \checkmark$

Q	uestio	n	Generic scheme	Illustrative scheme	Max mark
12.	(a)		Method 1 •¹ linear scale factor	•¹ 30 50	3
			•² know to multiply area by square of linear scale factor	$ \bullet^2 2750 \times \left(\frac{30}{50}\right)^2 $	
			• find area of smaller sector (calculation must include a power of the linear scale factor)	• ³ 990 (cm ²)	
			Method 2 ●¹ linear scale factor	$\bullet^1 \frac{50}{30}$	
			• know to divide area by square of linear scale factor	$\bullet^2 2750 \div \left(\frac{50}{30}\right)^2$	
			• find area of smaller sector (calculation must include a power of the linear scale factor)	• ³ 990 (cm ²)	
			Method 3 [Combination of (b) and (a)] •4•5•6 calculate size of angle ACB (see part (b) below)	• ⁴ • ⁵ • ⁶ 126(·05)	
			•¹ appropriate fraction	$ \bullet^1 \frac{126(\cdot 05)}{360} $	
			•² consistent substitution into area of sector formula	$\bullet^2 \frac{126(\cdot 05)}{360} \times \pi \times 30^2$	
			•³ calculate area of smaller sector	•³ 990 (cm²)	

Question	Generic scheme	Illustrative scheme	Max mark
Notes:	·		
1. Correct an	swer without working	award 0/3.	
	railable where there is invalid subsequent wo 990 = 1760	orking award 2/3 √√×	
3. Method 3:	Accept $\frac{126}{360} \times \pi \times 30^2 = 989.6 (0)$		
Commonly ob	served responses:		
1. $2750 \times \frac{30}{50}$	=1650	award 1/3 √××	
2. $2750 \times \left(\frac{30}{50}\right)$	$\left(\frac{1}{2} \right)^3 = 594$	award 2/3 ✓×✓	
3. $2750^2 \times \frac{30}{50}$	$\frac{1}{1} = 4537500$	award 1/3 √××	
4. $2750 \times \left(\frac{50}{30}\right)$	$\left(\frac{1}{2}\right)^2 = 7638(\cdot 8)$ or 7639	award 2/3 √×√	
5. $2750 \times \left(\frac{50}{30}\right)$	$\left(\frac{1}{100}\right)^2 = 2750 \times 1.67^2 = 7669(.4)$	award 1/3 √××	
(Premature	rounding leads to inaccurate answer)		
6. $2750 \div \left(\frac{50}{30}\right)$	$\left(\frac{1}{10000000000000000000000000000000000$	award 2/3 √√×	
(Premature	e rounding leads to inaccurate answer)		

Q	Question		Generic scheme		Illustrative scheme	Max mark
12.	(b)		Method 1 • expression for sector area	•4	$\frac{\text{angle}}{360} \times \pi \times 50^2$	3
			• ⁵ know how to find angle	• ⁵	$\frac{2750\times360}{\pi\times50^2}$	
			•6 calculate angle	•6	126(·05)	
			Method 2 • sector area: circle area ratio	•4	$\frac{2750}{\pi \times 50^2} \qquad \left(=0.35\right)$	
			•5 know how to find angle	• ⁵	$\frac{2750\times360}{\pi\times50^2}$	
			• ⁶ calculate angle	•6	126(·05)	

Question	Generic scheme	Illustrative scheme	Max mark
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- 1. Correct answer without working award 0/3
- 2. Alternative Method 1: $\frac{\text{angle}}{360} \times \pi \times 30^2 \rightarrow \frac{990 \times 360}{\pi \times 30^2} = 126 (.05...)$
- 3. Alternative Method 2: $\frac{990}{\pi \times 30^2} \rightarrow \frac{990 \times 360}{\pi \times 30^2} = 126 (.05...)$
- 4. Where any of the above alternative methods are used, an incorrect answer to part (a) must be followed through with possibility of awarding 3/3 for part (b)
- 5. Accept variations in π
- 6. Premature rounding of $\frac{2750}{\pi \times 50^2}$ must be to at least 2 decimal places
- 7. For the award of \bullet^6 , the calculation must involve a division by a product. The calculation must include a sector area, π , 360 and the candidate's chosen radius or diameter.

1. (a)
$$1650 \rightarrow$$
 (b) $\frac{1650 \times 360}{\pi \times 30^2} = 210(.08...)$ award 3/3

2. (a)
$$1650 \rightarrow$$
 (b) $\frac{1650 \times 360}{\pi \times 50^2} = 75(.63...)$ award 2/3 × \checkmark

3.
$$\frac{2750 \times 360}{\pi \times 100^2} = 31.5(1...)$$
 award 2/3 × \checkmark

4.
$$\frac{2750 \times 360}{\pi \times 100} = 3151(\cdot 2...)$$
 award 2/3 × \checkmark

5.
$$\frac{2750 \times 360}{\pi \times 100} = \sqrt{3151(\cdot 2...)} = 56(\cdot 1...)$$
 award 1/3 ××√

6.
$$\frac{2750}{360} \times \pi \times 50^2 = 59995(.6...)$$
 award 0/3

Q	Question		Generic scheme Illust	rative scheme Max mark
13.			• correct substitution into gradient formula • $\frac{4p^2-9}{4p-6}$ or	$\begin{array}{c c} 9-4p^2 \\ 6-4p \end{array}$
			•² factorise using difference of two squares $ (2p+3)$,
			•³ factorise using common factor •³ or	$\frac{(2p-3)}{(-3)} = \frac{2p+3}{2}$ $\frac{(3-2p)}{(2p)} = \frac{3+2p}{2}$

1. Correct answer without working

award 0/3.

2. Accept $p + \frac{3}{2}$ for •³

3. For subsequent incorrect working \bullet^3 is not available

$$\operatorname{eg} \frac{\operatorname{\cancel{2}} p + 3}{\operatorname{\cancel{2}}} = p + 3$$

award 2/3 √√×

Question		n	Generic scheme	Illustrative scheme	Max mark
14.			•¹ rearrange equation	• $\cos x = -\frac{1}{5}$ or equivalent	3
			• find one value of x	• ² 101·5(3)	
			• 3 find second value of x	•³ 258·4(6)	

1. Correct answer without working

award 0/3.

- 2. Accept (a) 102 and 258 (b) 101·6 (180-78·4) and 258·4 (180+78·4) with valid working.
- 3. Do not penalise omission of degrees sign.
- 4. If $\cos x < 0$ then \bullet^2 and \bullet^3 are only available for consistent 2^{nd} and 3^{rd} quadrant angles

eg
$$\cos x = -\frac{1}{5} \rightarrow$$
 (a) 78·5, 101·5 award 2/3 $\checkmark \times \checkmark$ (b) 78·5, 258·5 award 2/3 $\checkmark \times \checkmark$ (c) 78·5, 281·5 award 1/3 $\checkmark \times \times$

5. If $\cos x > 0$ then \bullet^2 is not available (working eased) but \bullet^3 is available for consistent 4th quadrant angle

eg
$$\cos x = \frac{1}{5} \rightarrow$$
 (a) 78.5 , 101.5 award $0/3$
(b) 78.5 , 258.5 award $0/3$
(c) 78.5 , 281.5 award $1/3 \times \times \checkmark$
(d) 101.5 , 258.5 award $0/3$

6. If 78.5 is clearly included as one of the final answers then award marks as follows:

eg
$$\cos x = -\frac{1}{5}$$
 (a) 78·5, 101·5, 258·5 award 2/3 $\checkmark \times \checkmark$ (b) 78·5, 101·5, 281·5 award 1/3 $\checkmark \times \times$ (c) 78·5, 101·5, 258·5, 281·5 award 1/3 $\checkmark \times \times$

- 7. (a Inappropriate use of RAD should only be penalised once in Qu 3, 7, 11, 14 or 19 $\cos^{-1}\left(\frac{1}{5}\right) = 1 \cdot 3 \dots \rightarrow 178 \cdot 6 \dots$, $181 \cdot 3 \dots$
 - (b) However, for $\cos^{-1}\left(-\frac{1}{5}\right)=1.7...\to1.7...$, 358.3... award 1/3 \checkmark ×× since the answers are not 2nd and 3rd quadrant angles
- 8. Inappropriate use of GRAD should only be penalised once in Qu 3, 7, 11, 14 or 19

(a)
$$\cos^{-1}\left(\frac{1}{5}\right) = 87 \cdot 1... \rightarrow 92 \cdot 8..., 267 \cdot 1...$$

(b)
$$\cos^{-1}\left(-\frac{1}{5}\right) = 112 \cdot 8... \rightarrow 112 \cdot 8..., 247 \cdot 2...$$

1.
$$\cos x = \frac{3}{5} \rightarrow 53.1$$
, 306.9 award 1/3 ××✓

Q	uestio	n	Generic scheme	illustrative scheme	Max mark
15.			•¹ correct denominator	• $(x-2)(x+5)$	3
			•² correct numerator	-2 $4(x+5)-3(x-2)$	
			• express in simplest form (remove brackets in numerator and collect like terms)	$\bullet^3 \frac{x+26}{(x-2)(x+5)}$	

- 1. Correct answer without working award 3/3
- 2. Accept $\frac{4(x+5)}{(x-2)(x+5)} \frac{3(x-2)}{(x-2)(x+5)}$ for the award of \bullet^1 and \bullet^2
- 3. Do not accept x-2(x+5) or (x-2)x+5 for the award of \bullet^1 unless the correct expansion appears in the final answer
- 4. Where a candidate chooses to expand the brackets in the denominator, then ●³ is only available for a correct expansion eg

(a)
$$\frac{4(x+5)}{(x-2)(x+5)} - \frac{3(x-2)}{(x-2)(x+5)} = \frac{x+26}{x^2+3x-10}$$
 award 3/3

(b)
$$\frac{4(x+5)}{(x-2)(x+5)} - \frac{3(x-2)}{(x-2)(x+5)} = \frac{x+26}{x^2-10}$$
 award 2/3 $\checkmark\checkmark$ ×

(c)
$$\frac{4(x+5)}{x^2-10} - \frac{3(x-2)}{x^2-10} = \frac{x+26}{x^2-10}$$
 award 2/3 × ✓

5. For subsequent incorrect working, \bullet^3 is not available eg

$$\frac{x+26}{x^2+3x-10} = \frac{26}{x^2-7}$$
 award 2/3 \sqrt{x}

1.
$$\frac{4x+20}{(x-2)(x+5)} - \frac{3x-6}{(x-2)(x+5)} = \frac{x+14}{(x-2)(x+5)}$$
 award 2/3 \checkmark ×

2.
$$\frac{4x+5}{(x-2)(x+5)} - \frac{3x-2}{(x-2)(x+5)} = \frac{x+7}{(x-2)(x+5)}$$
 award 1/3 $\checkmark \times \times$

Question		n	Generic scheme	Illustrative scheme	Max mark
16.			•1 apply $a^m \times ka^n = ka^{m+n}$	$\bullet^1 \text{eg } a^4 \times 3a = 3a^5$	3
			• evidence of $\sqrt{a} = a^{\frac{1}{2}}$	\bullet^2 $a^{\frac{1}{2}}$	
			•³ complete simplification	• $3a^{\frac{9}{2}}$	

- 1. Correct answer without working award 3/3.
- 2. Accept $3a^{4\frac{1}{2}}$ or $3a^{4\cdot 5}$ (as bad form).
- 3. (a) Accept $3\sqrt{a^9}$.
 - (b) Do not penalise $3a^{\frac{9}{2}} = 3\sqrt[9]{a^2}$.
- 4. Where candidate starts by rationalising the denominator, $ullet^1$ is available for

eg (i) obtaining
$$3a^5$$
 as follows: $\frac{a^4 \times 3a}{\sqrt{a}} \times \frac{\sqrt{a}}{\sqrt{a}} = \frac{3a^5 \times \sqrt{a}}{a}$

(ii) obtaining
$$3a^4$$
 as follows: $\frac{a^4 \times 3a}{\sqrt{a}} \times \frac{\sqrt{a}}{\sqrt{a}} = 3a^4 \times \sqrt{a}$ or $a^4 \times 3\sqrt{a}$

5. **BEWARE** \bullet^1 is not available where $3a^5$ has been obtained incorrectly

$$eg \frac{a^4 \times 3a}{\sqrt{a}} \times \frac{\sqrt{a}}{\sqrt{a}} = \frac{a^4 \times 3a \times \sqrt{a}}{a} = \frac{\sqrt{3a^5}}{a}$$

Question		n	Generic scheme	Illustrative scheme	Max mark
17.			•¹ expand brackets	$\bullet^1 \sin^2 x + \sin x \cos x + \cos x \sin x + \cos^2 x$	2
			•² simplify expression	\bullet^2 1+2 sin x cos x	

1. Correct answer without working

award 0/2

- 2. Do not penalise omission of degrees sign
- 3. Accept $1+\sin 2x$
- 4. Accept $(\sin x)^2$ and $(\cos x)^2$ or $\sin x \sin x$ and $\cos x \cos x$

eg (a) $(\sin x)^2 + 2\sin x \cos x + (\cos x)^2 = 1 + 2\sin x \cos x$

award 2/2

(b) $\sin x \sin x + 2\sin x \cos x + \cos x \cos x = 1 + 2\sin x \cos x$

award 2/2

5. Do not accept $\sin x^2$ and $\cos x^2$.

 $eg \sin x^2 + 2\sin x \cos x + \cos x^2 = 1 + 2\sin x \cos x$

award 1/2 ×√

6. \bullet^1 is not available if there are no variables

eg $\sin^2 + 2\sin\cos + \cos^2 = 1 + 2\sin\cos$

award 1/2 ×√

- 7. 2 is not available if there is invalid subsequent working
- 8. Alternative acceptable strategy:

$$\bullet^{1} \left(\frac{o}{h}\right)^{2} + \left(\frac{o}{h}\right) \left(\frac{a}{h}\right) + \left(\frac{a}{h}\right) \left(\frac{o}{h}\right) + \left(\frac{a}{h}\right)^{2}$$

 $e^2 \left(\frac{o}{h}\right)^2 + 2\left(\frac{o}{h}\right)\left(\frac{a}{h}\right) + \left(\frac{a}{h}\right)^2 = 1 + 2\sin x \cos x$

award 2/2

Commonly observed responses:

1. $(\sin x + \cos x)^2 = \sin^2 x + \cos^2 x = 1$

award 0/2

2. $(\sin x + \cos x)^2 = \sin^2 x + \sin x \cos x + \cos^2 x = 1 + \sin x \cos x$

award 1/2 ×√

Q	Question		Generic scheme	Illustrative scheme	Max mark
18.			• marshal facts and recognise right-angled triangle	•¹ 7·5 7·5	4
			•² consistent Pythagoras statement	$\bullet^2 7.5^2 + 7.5^2$	
			•³ calculate radius of larger circle	•³ 10·6	
			• ⁴ calculate CD	• ⁴ 25·6(cm)	

1. Correct answer without working

award 0/4.

2. In the absence of a diagram, or a diagram without right angle indicated, accept $7.5^2 + 7.5^2$ as evidence for the award of \bullet^1 and \bullet^2 .

3. **BEWARE**

Where a diagram is shown, working must be consistent with the diagram.

- 4. \bullet^2 and \bullet^3 are available for a valid trigonometric method.
- 5. 3 is available for a consistent calculation of a length using Pythagoras or trigonometry
- 6. 4 is only available following a Pythagoras (or trigonometric) calculation within a right-angled triangle involving 7.5 or 15.
- 7. Disregard errors due to premature rounding provided there is evidence.

Commonly observed responses:

- 1. [Triangle SBT with SB = ST = 15] $r^2 = 15^2 + 15^2 \rightarrow r = 21.2 \rightarrow CD = 51.2$
 - (a) working inconsistent with correct diagram

award 3/4 √×√√

award 3/4 × ✓ ✓ ✓

(b) working consistent with candidate's diagram (c) no diagram

award 2/4 ××√√

- 2. [Square with side AB] $d^2 = 15^2 + 15^2 \rightarrow r = 10.6 \rightarrow CD = 25.6$ If consistent with a correct diagram award 4/4; otherwise apply COR 1 MIs
- 3. [Triangle ATB] $r^2 + r^2 = 15^2 \rightarrow r = 10.6 \rightarrow CD = 25.6$

Apply MIs and Note 2 becomes accept $r^2 + r^2 = 15^2$ as evidence for the award of \bullet^1 and \bullet^2

Q	uestion	Generic scheme		Illustrative scheme	Max mark
19.		Method 1 •¹ correct substitution into sine rule	•1	$\frac{BK}{\sin 34} = \frac{350}{\sin 94}$	5
		•² re-arrange formula	•2	$BK = \frac{350\sin 34}{\sin 94}$	
		•³ calculate BK	•3	196(·195)	
		• 4 consistent substitution into appropriate trig formula	•4	$\sin 52 = \frac{h}{196} \text{ or } \frac{h}{\sin 52} = \frac{196}{\sin 90}$	
		• calculate height using trigonometry	•5	154·6 (m)	
		Method 2 •¹ correct substitution into sine rule	•1	$\frac{BM}{\sin 52} = \frac{350}{\sin 94}$	
		•² re-arrange formula	•2	$BM = \frac{350\sin 52}{\sin 94}$	
		•³ calculate BM	•3	276(·477)	
		• consistent substitution into appropriate trig formula	•4	$\sin 34 = \frac{h}{276} \text{ or } \frac{h}{\sin 34} = \frac{276}{\sin 90}$	
		• calculate height using trigonometry	•5	154·6 (m)	

Question	Generic scheme	Illustrative scheme	Max mark
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1. Correct answer without working

award 0/5.

- 2. Do not penalise omission of degrees signs.
- 3. Disregard errors due to premature rounding provided there is evidence. However, do not accept sin34, sin52 or sin94 rounded to less than 3 decimal places.

eg BM =
$$\frac{350\sin 52}{\sin 94} = \frac{275 \cdot 8}{0.99} = 275 \cdot 59 \rightarrow h = 275 \cdot 59 \sin 34 = 155 \cdot 8$$
 awa

award 4/5 √√×√√

- 4. Where both BK and BM are calculated but one is calculated incorrectly, if there is
 - (a) further working then apply the MIs based on the length used to calculate the height
 - (b) no further working disregard incorrect length ie

award 3/5

5. Alternative strategy for •⁴ and •⁵

eg •⁴ A =
$$\frac{1}{2} \times 350 \times 196 (.195...) \times \sin 52 (= 27055...)$$

•5
$$\frac{1}{2} \times 350 \times h = 27055 \cdot ... \rightarrow h = 154 \cdot 6$$

- 6. Inappropriate use of GRAD or RAD should only be penalised once in Qu 3, 7, 11, 14 or 19
 - (a) 130·4... (GRAD)
 - (b) $\pm 744 \cdot 9...$ (RAD); \bullet^5 is **not** available due to the negative length. However, \bullet^3 is available if use of RAD has already been penalised in Qu 3, 7, 11, 14 or 19

Commonly observed responses:

1.
$$\frac{x}{\sin 52} = \frac{350}{\sin 34} \rightarrow x = 493(\dots)$$

award 2/5 × ✓ ✓ × ×

2. eg
$$\frac{BK}{34} = \frac{350}{94} \rightarrow BK = 126(.59...) \rightarrow h = 126(.59...) \times \sin 52 = 99(.75...)$$

award 2/5 xxx//

[END OF MARKING INSTRUCTIONS]