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GOST R 34.11-94: Hash Function Algorithm

Abstract

This document is intended to be a source of information about the Russian Federal standard hash function (GOST R 34.11-94), which is one of the Russian cryptographic standard algorithms (called GOST algorithms). Recently, Russian cryptography is being used in Internet applications, and this document has been created as information for developers and users of GOST R 34.11-94 for hash computation.

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1. Introduction

1.1. General Information

- 1. GOST R 34.11-94 [GOST3411] was developed by the Federal Agency for Government Communication and Information and by the All-Russia Scientific and Research Institute of Standardization.
- 2. GOST R 34.11-94 was accepted and activated by Act 154 of 23.05.1994 issued by the Russian Federal committee for standards.

1.2. The Purpose of GOST R 34.11-94

Expanding the application of information technologies when creating, processing, and storing documents requires, in some cases, confidentiality of their contents, maintenance of completeness, and authenticity.

Cryptography (cryptographic security) is one of the effective approaches for data security. It is widely applied in different areas of government and commercial activity.

Cryptographic data security methods are under serious scientific research and standardization efforts at national, regional, and international levels.

GOST R 34.11-94 defines a hash function calculation procedure for an arbitrary sequence of binary symbols.

The hash function maps an arbitrary set of data represented as a sequence of binary symbols onto its image of a fixed small length.

Thus, hash functions can be used in procedures related to the electronic digital signature, resulting in considerable reduction of elapsed time for the sign and verify stages. The effect of the reduction of time is due to the fact that only a short image of initial data is actually signed.

2. Applicability

GOST R 34.11-94 defines an algorithm and procedure for the calculation of a hash function for an arbitrary sequence of binary symbols. These algorithms and procedures should be applied in cryptographic methods of data processing and securing, including digital signature procedures employed for data transfer and data storage in computer-aided systems.

The hash function, defined in GOST R 34.11-94, is used for digital signature systems based on the asymmetric cryptographic algorithm according to GOST R 34.10-2001 (see section 3).

3. Conventions Used in This Document

The following notations are used in GOST R 34.11-94:

V_all is a set of all finite words in the alphabet $V = \{0,1\}$. The words are read from right to left and the alphabet symbols are numbered from right to left (i.e., the rightmost symbol of the word has the number one, the second rightmost symbol has number two, etc.).

Vk is a set of all words in alphabet $V = \{0,1\}$ of length k bits (k=16,64,256).

|A| is the length of a word A belonging to V_all.

 $A \mid B$ is a concatenation of words A, B belonging to V_all. Its length is $\mid A \mid + \mid B \mid$, where the left $\mid A \mid$ symbols come from the word A, and the right $\mid B \mid$ symbols come from the word B. One can also use the notation $A \mid B = A * B$.

 A^k is a concatenation of k copies of the word A (A belongs to V_{all}).

 N_k is a word of length k, containing a binary representation of $m \pmod{2^k}$ residue, with a non-negative integer N.

A^\$ is a non-negative integer with A as its binary representation.

(xor) is the bitwise modulo 2 addition of the words of the same length.

(+)' is the addition according to the rule A (+)' B = <A^\$+ B^\$>_k, where k = |A| = |B|.

M is a binary sequence to be hashed, M belongs to V_{all} . M is a message in digital signature systems.

h is a hash function that maps the sequence M belonging to V_{all} onto the word h(M) belonging to V_{all} .

E(k,A) is a result of the encryption of the word A using key K with the encryption algorithm according to [GOST28147] in the electronic codebook (ECB) mode (K belongs to V256, A belongs to V64).

h0 is an initial hash value.

e := g is the assignment of the value g to the parameter e.

^ is the power operator.

i = 1..8 is an interval with i being all the values from 1 to 8.

hUZ is the S-boxes described in [GOST28147].

4. General Statements

A hash function h is the mapping h: $V_{all} \rightarrow V256$, depending on the parameter (which is the initial hash value H, H is a word from V256). To define the hash function, it is necessary to have:

- a calculation algorithm for the step-by-step hash function

```
chi : V256 x V256 -> V256
```

- a description of an iterative procedure for calculating the hash value \boldsymbol{h}

A hash function h depends on two parameters, h0 and hUZ.

5. Step-by-Step Hash Function

A calculation algorithm for the step-by-step hash function contains three parts, which successively do:

- key generation, here keys are 256-bit words;
- an encryption transformation, that is encryption of 64-bit subwords of word H using keys K[i], (i = 1, 2, 3, 4) with the algorithm according to [GOST28147] in ECB mode; and
- a mixing transformation for the result of the encryption.

5.1 Key Generation

```
Consider X = (b[256], b[255], ..., b[1]) belongs to V256.
```

Let:

```
X = x[4] | |x[3]| | |x[2]| | |x[1]| = eta[16] | | [eta15] | | ... | | |eta[1]|
```

= xi[32] | |xi[31]| | ... | |xi[1]|, where

```
x[i] = (b[i*64],...,b[(i-1)*64+1]) belongs to V64, i = 1..4,
   eta[j] = (b[j*16],...,b[(j-1)*16+1]) belongs to V16, j = 1...16,
    xi[k] = (b[k*8],..., b[(k-1)*8+1]) belongs to V8, k = 1...32.
Yet, another notation: A(X) = (x[1](xor)x[2]) | |x[4]| |x[3]| |x[2].
The transformation P: V256 -> V256 maps the word xi32||...||xi1
onto the word xi[phi(32)] \mid | \dots | | xi[phi(1)],
where phi(i + 1 + 4 (k - 1)) = 8i + k, i = 0...3, k = 1...8.
For the key generation, one should use the following initial data:
   - words H, M belonging to V256,
   - parameters: words C[i] (i = 2, 3, 4), with values:
     C[2] = C[4] = 0^256;
     C[3] = 1^8 | 0^8 | 1^16 | 0^24 | 1^16 | 0^8 | (0^8 | 1^8)^2 | 1^8 | 0^8
            ||(0^8||1^8)^4||(1^8||0^8)^4.
The following algorithm is used for the key calculation:
1. Assign values:
   i := 1, U := H, V := M.
2. Calculate:
   W = U (xor) V , K[i] = P(W).
3. Assign:
   i := i + 1.
4. Verify condition:
   i = 5.
If it is true, go to step 7. If not, go to step 5.
5. Calculate:
```

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U := A(U)(xor)C[i], V := A(A(V)),

W := U(xor)V, K[i] = P(W).

- 6. Go to step 3.
- 7. End.

5.2. Encryption Transformation

At this stage, 64-bit subwords of the word H are encrypted using keys K[i] (i = 1, 2, 3, 4).

For the encryption transformation, one should use the following initial data:

```
H = h[4] | |h[3]| |h[2]| |h[1],
```

where h[i] belongs to V64, i = 1,2,3,4, and a key set is K[1], K[2], K[3], K[4].

The encryption algorithm is applied and the following words are obtained:

```
s[i] = E(K[i],h[i]), where: i = 1,2,3,4
```

As a result of the stage, the following sequence is formed:

```
S = s[4] | |s[3]| |s[2]| |s[1].
```

5.3. Mixing Transformation

At this stage, the obtained sequence is mixed using a shift register.

The initial data includes words H, M belonging to V256 and a word S belonging to V256 .

```
Let a mapping PSI(X): V256(2) -> V256(2) transform the word:
```

```
eta[16]||eta[15]||...||eta[1], eta[i] belongs to V16, i = 1..16
```

into the word:

```
eta[1](xor)eta[2](xor)eta[3](xor)eta[4](xor)eta[13](xor)eta[16]
||eta[16]||...||eta[2].
```

Then, the value of the step-by-step hash function value is the word:

```
chi(M, H) = PSI^61(H(xor)PSI(M(xor)PSI^12(S))),
```

where $PSI^i(X)$ is the transformation PSI applied i times to X.

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6. The Calculation Procedure for a Hash Function

The calculation procedure for a hash function h is assumed to be applied to a sequence M belonging to V_{all} . Its parameter is an initial hash value h0, which is an arbitrarily fixed word from V256.

The calculation procedure for the function h uses the following quantities at each step of iteration:

 $_{\rm M}$ belonging to ${\rm V_all}$ - a part of the sequence M, which was not hashed at previous iterations;

H belonging to V256 - the current hash value;

SIGMA belonging to V256 - the current check sum value;

 $\ensuremath{\mathtt{L}}$ belonging to V256 - the length of the partial sequence M processed at the previous iteration step.

The calculation algorithm for function h consists of the following steps:

Step 1. Assign initial values to current quantities:

- $1.1 _M_ := M.$
- 1.2 H := h0.
- 1.3 SIGMA := 0^256.
- 1.4 L := 0^256.
- 1.5 Go to step 2.

Step 2.

2.1 Verify the condition $|_M_|>256$.

If it is true, go to step 3.

Else, make the following calculations:

$$2.2 L := \langle L^{\$} + |M| \rangle_{256}$$

$$2.3 \text{ M}' := 0^{(256 - |M|)|M}$$

2.4 SIGMA := SIGMA (+)' M'

```
2.5 H := chi (M', H)
2.6 H := chi (L, H)
2.7 H := chi (SIGMA, H)
2.8 End.
```

Step 3.

- 3.1 Calculate a subword M_s belonging to V256 of the word _M_ (_M_ = M_p | |M_s). Then make the following calculations:
- $3.2 \text{ H} := \text{chi} (M_s, H)$
- $3.3 L := <L^$ + 256>_256$
- 3.4 SIGMA := SIGMA (+)' M[s]
- $3.5 _M = M_p$
- 3.6 Go to step 2.

The quantity H obtained at step 2.7 is the value of the hash function h(M).

7. Test Examples (Informative)

It is recommended to use the values for substitution units pi[1], pi[2],..., pi[8] and the initial hash value H described in this appendix for the GOST R 34.11-94 test examples only.

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7.1. Usage of the Algorithm GOST 28147-89

The algorithm GOST 28147-89 [GOST28147] in ECB mode is used as an encryption transformation in the following examples. The following values of the substitution units pi[1], pi[2],..., pi[8] have been chosen:

- 8 7 6 5 4 3 2 1
- 0 1 D 4 6 7 5 E 4
- 1 F B B C D 8 B A
- 2 D 4 A 7 A 1 4 9
- 3 0 1 0 1 1 D C 2
- 4 5 3 7 5 0 A 6 D
- 5 7 F 2 F 8 3 D 8
- 6 A 5 1 D 9 4 F 0
- 7 4 9 D 8 F 2 A E
- 8 9 0 3 4 E E 2 6
- 9 2 A 6 A 4 F 3 B
- 10 3 E 8 9 6 C 8 1
- 11 E 7 5 E C 7 1 C
- 12 6 6 9 0 B 6 0 7
- 13 B 8 C 3 2 0 7 F
- 14 8 2 F B 5 9 5 5
- 15 CCE23B93

The hexadecimal value of pi[j](i) is given in a column number j,

j = 1..8, and in a row number i, i = 0..15.

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7.2. Representation of Vectors

We will put down binary symbol sequences as hexadecimal digits strings, where each digit corresponds to four signs of its binary representation.

7.3 Examples of the Hash Value Calculation

A zero vector, for example, can be taken as an initial hash value:

7.3.1. Hash Calculation for the Sample Message M

M = 73657479 62203233 3D687467 6E656C20 2C656761 7373656D 20736920 73696854

Initial values are assigned for the text:

M = 73657479 62203233 3D687467 6E656C20 2C656761 7373656D 20736920 73696854

for the hash function:

for the sum of text blocks:

for the length of the text:

If the length of the message to be hashed equals 256 bits (32 bytes), then:

M' = _M_ = 73657479 62203233 3D687467 6E656C20 2C656761 7373656D 20736920 73696854

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and there is no need to pad the current block with zeroes:

SIGMA=M' = 73657479 62203233 3D687467 6E656C20 2C656761 7373656D 20736920 73696854

The step-by-step hash function chi(M, N) values are calculated.

The keys are generated:

K[1] = 733D2C20 65686573 74746769 326C6568 626E7373 20657369 79676120 33206D54

K[2] = 110C733D 0D166568 130E7474 06417967 1D00626E 161A2065 090D326C 4D393320

K[3] = 80B111F3 730DF216 850013F1 C7E1F941 620C1DFF 3ABAE91A 3FA109F2 F513B239

The 64-bit subwords of block H are encrypted by the algorithm according to GOST 28147.

Block h[1] = 00000000 000000000 is encrypted using key K[1] and s[1] = 42ABBCCE 32BC0B1B is obtained.

Block h[2] = 00000000 000000000 is encrypted using key K[2] and s[2] = 5203EBC8 5D9BCFFD is obtained.

Block h[3] = 00000000 000000000 is encrypted using key K[3] and s[3] = 8D345899 00FF0E28 is obtained.

Block h[4] = 00000000 000000000 is encrypted using key K[4] and s[4] = E7860419 0D2A562D is obtained.

So S = E7860419 0D2A562D 8D345899 00FF0E28 5203EBC8 5D9BCFFD 42ABBCCE 32BC0B1B

is obtained.

The mixing transformation using a shift register is performed and

KSI = chi(M, H) = CF9A8C65 505967A4 68A03B8C 42DE7624 D99C4124 883DA687 561C7DE3 3315C034

is obtained.

```
Assign H = KSI and calculate chi(L, H):
K[1] = CF68D956 9AA09C1C 8C3B417D 658C24E3
      50428833 59DE3D15 6776A6C1 A4248734
K[2] = 8FCF68D9 809AA09C 3C8C3B41 C7658C24
      BB504288 2859DE3D 666676A6 B3A42487
K[3] = 4E70CF97 3C8065A0 853C8CC4 57389A8C
       CABB50BD E3D7A6DE D1996788 5CB35B24
K[4] = 584E70CF C53C8065 48853C8C 1657389A
      EDCABB50 78E3D7A6 EED19867 7F5CB35B
    = 66B70F5E F163F461 468A9528 61D60593
      E5EC8A37 3FD42279 3CD1602D DD783E86
KSI = 2B6EC233 C7BC89E4 2ABC2692 5FEA7285
      DD3848D1 C6AC997A 24F74E2B 09A3AEF7
Now assign H = KSI again and calculate chi( SIGMA, H):
K[1] = 5817F104 OBD45D84 B6522F27 4AF5B00B
      A531B57A 9C8FDFCA BB1EFCC6 D7A517A3
K[2] = E82759E0 C278D950 15CC523C FC72EBB6
      D2C73DA8 19A6CAC9 3E8440F5 C0DDB65A
K[3] = 77483AD9 F7C29CAA EB06D1D7 841BCAD3
      FBC3DAA0 7CB555F0 D4968080 0A9E56BC
K[4] = A1157965 2D9FBC9C 088C7CC2 46FB3DD2
      7684ADCB FA4ACA06 53EFF7D7 C0748708
   = 2AEBFA76 A85FB57D 6F164DE9 2951A581
      C31E7435 4930FD05 1F8A4942 550A582D
KSI = FAFF37A6 15A81669 1CFF3EF8 B68CA247
      E09525F3 9F811983 2EB81975 D366C4B1
Then, the hash result is:
  = FAFF37A6 15A81669 1CFF3EF8 B68CA247
```

E09525F3 9F811983 2EB81975 D366C4B1

7.3.2. Hash Calculation for the Sample Message M

Let M = 7365 74796220 3035203D 20687467 6E656C20 73616820 65676173 73656D20 6C616E69 6769726F 20656874 2065736F 70707553

As the length of the message to be hashed equals 400 bits (50 bytes), the message is divided into two blocks, and the second (high-order) one is padded with zeroes. During the calculations the following numbers are obtained:

STEP 1.

- M_s = 73616820 65676173 73656D20 6C616E69 6769726F 20656874 2065736F 70707553
- K[1] = 73736720 61656965 686D7273 20206F6F 656C2070 67616570 616E6875 73697453
- K[2] = 14477373 0C0C6165 1F01686D 4F002020 4C50656C 04156761 061D616E 1D277369
- K[3] = CBFF14B8 6D04F30C 96051FFE DFFFB000 35094CAF 72F9FB15 7CF006E2 AB1AE227
- K[4] = EBACCB00 F7006DFB E5E16905 B0B0DFFF BA1C3509 FD118DF9 F61B830F F8C554E5
- S = FF41797C EEAADAC2 43C9B1DF 2E14681C EDDC2210 1EE1ADF9 FA67E757 DAFE3AD9
- KSI = F0CEEA4E 368B5A60 C63D96C1 E5B51CD2 A93BEFBD 2634F0AD CBBB69CE ED2D5D9A

STEP 2.

- M' = 00000000 00000000 00000000 00007365 74796220 3035203D 20687467 6E656C20
- K[1] = F0C6DDEB CE3D42D3 EA968D1D 4EC19DA9 36E51683 8BB50148 5A6FD031 60B790BA

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K[2]	=	16A4C6A9 FB68E526	F9DF3D3B 2CDBB534	E4FC96EF FE161C83	5309C1BD 6F7DD2C8
K[3]	=	C49D846D 9DCB0644	1780482C D1E641E5	9086887F A02109AF	C48C9186 9D52C7CF
K[4]	=	BDB0C9F0 1CAD9536	756E9131 F4E4B674	E1F290EA 99F31E29	50E4CBB1 70C52AFA
S	=	62A07EA5 6881EB66	EF3C3309 F5C7959F	2CE1B076 63FCA1F1	173D48CC D33C31B8
KSI	=	95BEA0BE B8287CB6	88D5AA02 2CBC135B	FE3C9D45 3E339EFE	436CE821 F6576CA9
STEP	3.				
Н	=	95BEA0BE B8287CB6	88D5AA02 2CBC135B	FE3C9D45 3E339EFE	436CE821 F6576CA9
L	=	00000000	00000000	00000000	00000000 00000190
K[1]	=	95FEB83E 88432CF6	BE3C2833 D56CBC57	A09D7C9E AAE8136D	BE45B6FE 02215B39
K[2]	=	8695FEB8 DA88432C	1BBE3C28 EBD56CBC	E2A09D7C 7FABE813	48BE45B6 F292215B
K[2]	=	8695FEB8 DA88432C	1BBE3C28 EBD56CBC	E2A09D7C 7FABE813	48BE45B6 F292215B
K[3]	=	B9799501 6FDA88BC	141B413C D0142A6C	1EE2A062 FA80AA16	0CB74145 15F2FDB1
K[4]	=	94B97995 346FDA88	7D141B41 46D0142A	C21EE2A0 BDFA81AA	040CB741 DC1562FD
S	=			6C65478A 94FD9D6D	
KSI	=			7D473785 08AA4C24	
STEP	4.				
Н	=			7D473785 08AA4C24	

- SIGMA = 73616820 65676173 73656D20 6C61E1CE DBE2D48F 509A88B1 40CDE7D6 DED5E173
- K[1] = 340E7848 83223B67 025AAAAB DDA5F1F2 5B6AF7ED 1575DE87 19E64326 D2BDF236
- K[2] = 03DC0ED0 F4CD26BC 8B595F13 F5A4A55E A8B063CB ED3D7325 6511662A 7963008D
- K[3] = C954EF19 D0779A68 ED37D3FB 7DA5ADDC 4A9D0277 78EF765B C4731191 7EBB21B1
- K[4] = 6D12BC47 D9363D19 1E3C696F 28F2DC02 F2137F37 64E4C18B 69CCFBF8 EF72B7E3
- S = 790DD7A1 066544EA 2829563C 3C39D781 25EF9645 EE2C05DD A5ECAD92 2511A4D1
- KSI = 0852F562 3B89DD57 AEB4781F E54DF14E EAFBC135 0613763A 0D770AA6 57BA1A47

Then, the hash result is:

H = 0852F562 3B89DD57 AEB4781F E54DF14E EAFBC135 0613763A 0D770AA6 57BA1A47

8. Security Considerations

This entire document is about security considerations.

Current cryptographic resistance of GOST R 34.11-94 hash algorithm is estimated as 2^128 operations of computations of step hash functions. (There is a known method to reduce this estimate to 2^105 operations, but it demands padding the colliding message with 1024 random bit blocks each of 256-bit length; thus, it cannot be used in any practical implementation).

9. Normative References

- [GOST28147] "Cryptographic Protection for Data Processing System",
 GOST 28147-89, Gosudarstvennyi Standard of USSR,
 Government Committee of the USSR for Standards, 1989.
 (In Russian)
- [GOST3411] "Information technology. Cryptographic Data Security.
 Hashing function.", GOST R 34.10-94, Gosudarstvennyi
 Standard of Russian Federation, Government Committee of
 the Russia for Standards, 1994. (In Russian)

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