# **Emojify!**

Welcome to the second assignment of Week 2. You are going to use word vector representations to build an Emojifier.

Have you ever wanted to make your text messages more expressive? Your emojifier app will help you do that. So rather than writing "Congratulations on the promotion! Lets get coffee and talk. Love you!" the emojifier can automatically turn this into "Congratulations on the promotion! ▲ Lets get coffee and talk. ♣ Love you! ♥"

You will implement a model which inputs a sentence (such as "Let's go see the baseball game tonight!") and finds the most appropriate emoji to be used with this sentence (③). In many emoji interfaces, you need to remember that visual is the "heart" symbol rather than the "love" symbol. But using word vectors, you'll see that even if your training set explicitly relates only a few words to a particular emoji, your algorithm will be able to generalize and associate words in the test set to the same emoji even if those words don't even appear in the training set. This allows you to build an accurate classifier mapping from sentences to emojis, even using a small training set.

In this exercise, you'll start with a baseline model (Emojifier-V1) using word embeddings, then build a more sophisticated model (Emojifier-V2) that further incorporates an LSTM.

Lets get started! Run the following cell to load the package you are going to use.

In [1]: import numpy as np
 from emo\_utils import \*
 import emoji
 import matplotlib.pyplot as plt

%matplotlib inline

## 1 - Baseline model: Emojifier-V1

### 1.1 - Dataset EMOJISET

Let's start by building a simple baseline classifier.

You have a tiny dataset (X, Y) where:

- X contains 127 sentences (strings)
- Only 127 sentences!!!
- Y contains a integer label between 0 and 4 corresponding to an emoji for each sentence

Out[4]: ['it', 'is', 'the', 'worst', 'day', 'in', 'my', 'life']

X (sentences)	Y (labels)
	,
I love you	0
Congrats on the new job	2
I think I will end up alone	3
I want to have sushi for dinner!	4
It was funny lol	2
she did not answer my text	3
Happy new year	2
my algorithm performs poorly	3
he can pitch really well	1
you are failing this exercise	3
you did well on your exam.	2
What you did was awesome	2
I am frustrated	3

code	emoji	label
:heart:	<b>(</b>	0
:baseball:		1
:smile:	$\odot$	2
:disappointed:	6	3
:fork_and_knife	: 1	4

\*\*Figure 1\*\*: EMOJISET - a classification problem with 5 classes. A few examples of sentences are given here.

Let's load the dataset using the code below. We split the dataset between training (127 examples) and testing (56 examples).

```
In [2]: X_train, Y_train = read_csv('data/train_emoji.csv')
X_test, Y_test = read_csv('data/tesss.csv')

Note that this gives you the sentence with the most characters, not the most words.

To get the sentence with the most word you need to use this code

maxLen = len(max(X_train, key=len).split())

maxLen = len(max(X_train, key=lambda p:len(p.split() ) ). split() )
```

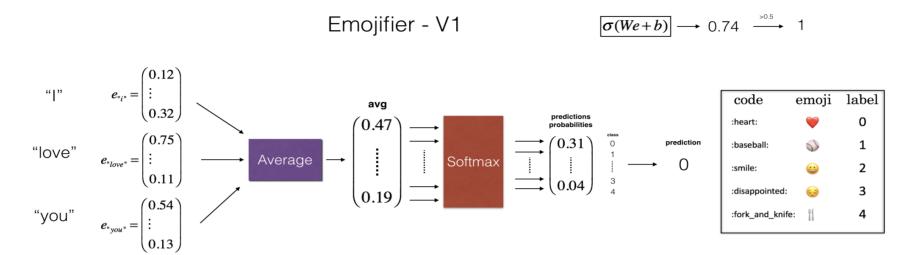
Run the following cell to print sentences from X\_train and corresponding labels from Y\_train. Change index to see different examples. Because of the font the iPython notebook uses, the heart emoji may be colored black rather than red.

```
In [4]: index = 2
print(X_train[index], label_to_emoji(Y_train[index]))
sentence = X_train[index]
sentence.lower().split()

It is the worst day in my life ②
```

## 1.2 - Overview of the Emojifier-V1

In this part, you are going to implement a baseline model called "Emojifier-v1".



\*\*Figure 2\*\*: Baseline model (Emojifier-V1).

The input of the model is a string corresponding to a sentence (e.g. "I love you). In the code, the output will be a probability vector of shape (1,5), that you then pass in an argmax layer to extract the index of the most likely emoji output.

To get our labels into a format suitable for training a softmax classifier, lets convert Y from its current shape current shape (m,1) into a "one-hot representation" (m,5), where each row is a one-hot vector giving the label of one example, You can do so using this next code snipper. Here, Y\_oh stands for "Y-one-hot" in the variable names Y\_oh\_train and Y\_oh\_test:

Let's see what convert\_to\_one\_hot() did. Feel free to change index to print out different values.

refer to Books and mag/python/Making one hot vector in a Cool way using python

```
In [6]: index = 50
print(Y_train[index], "is converted into one hot", Y_oh_train[index])
0 is converted into one hot [ 1. 0. 0. 0. 0.]
```

Labels must be converted to one-hot to correspond to softmax

All the data is now ready to be fed into the Emojify-V1 model. Let's implement the model!

## 1.3 - Implementing Emojifier-V1

As shown in Figure (2), the first step is to convert an input sentence into the word vector representation, which then get averaged together. Similar to the previous exercise, we will use pretrained 50-dimensional GloVe embeddings. Run the following cell to load the word\_to\_vec\_map, which contains all the vector representations.

```
In [7]: word_to_index, index_to_word, word_to_vec_map = read_glove_vecs('data/glove.6B.50d.txt')
```

#### You've loaded:

- word\_to\_index: dictionary mapping from words to their indices in the vocabulary (400,001 words, with the valid indices ranging from 0 to 400,000)
- index to word: dictionary mapping from indices to their corresponding words in the vocabulary
- word to vec map: dictionary mapping words to their GloVe vector representation.

Run the following cell to check if it works.

```
In [8]: word = "cucumber"
   index = 289846
   print("the index of", word, "in the vocabulary is", word_to_index[word])
   print("the", str(index) + "th word in the vocabulary is", index_to_word[index])

the index of cucumber in the vocabulary is 113317
   the 289846th word in the vocabulary is potatos
```

**Exercise**: Implement sentence to avg(). You will need to carry out two steps:

- 1. Convert every sentence to lower-case, then split the sentence into a list of words. X.lower() and X.split() might be useful.
- 2. For each word in the sentence, access its GloVe representation. Then, average all these values.

```
In [9]: # GRADED FUNCTION: sentence to ava
        def sentence_to_avg(sentence, word_to_vec_map):
            Converts a sentence (string) into a list of words (strings). Extracts the GloVe representation of each word
            and averages its value into a single vector encoding the meaning of the sentence.
            Arguments:
            sentence -- string, one training example from X
            word_to_vec_map -- dictionary mapping every word in a vocabulary into its 50-dimensional vector representation
            Returns:
            avg -- average vector encoding information about the sentence, numpy-array of shape (50,)
            ### START CODE HERE ###
            # Step 1: Split sentence into list of lower case words (≈ 1 line)
            words = sentence.lower().split()
            # Initialize the average word vector, should have the same shape as your word vectors.
            avg = np.zeros(word to vec map[words[0]].shape)
            # Step 2: average the word vectors. You can loop over the words in the list "words".
            for w in words:
                avg += word to vec map[w]
            avg = avg/len(words)
            ### END CODE HERE ###
            return avg
```

```
In [10]: avg = sentence to avg("Morrocan couscous is my favorite dish", word to vec map)
       print("avg = ", avg)
                      0.56370833 -0.50427333 0.258865
                                                  0.55131103 0.03104983
       avg = [-0.008005]
        -0.21013718 0.16893933 -0.09590267 0.141784 -0.15708967 0.18525867
        0.05820667 -0.01578167 -0.12078833 -0.02471267 0.4128455
                                                      0.5152061
        0.38756167 -0.898661 -0.535145
                                   0.33501167 0.68806933 -0.2156265
        1.797155
                 0.10476933 -0.36775333 0.750785
                                             0.10282583 0.348925
                          -0.10706167 -0.283635
                                            0.59580117 0.28747333
        -0.27262833 0.66768
        0.1445417 0.09808667]
```

### **Expected Output:**

\*\*avg=

 $\begin{bmatrix} -0.008005\ 0.56370833\ -0.50427333\ 0.258865\ 0.55131103\ 0.03104983\ -0.21013718\ 0.16893933\ -0.09590267\ 0.141784\ -0.15708967\ 0.18525867\ 0.6495785\ 0.38371117\ 0.21102167\ 0.11301667\ 0.02613967\ 0.26037767\ 0.05820667\ -0.01578167\ -0.12078833\ -0.02471267\ 0.4128455\ 0.5152061\ 0.38756167\ -0.898661\ -0.535145\ 0.33501167\ 0.68806933\ -0.2156265\ 1.797155\ 0.10476933\ -0.36775333\ 0.750785\ 0.10282583\ 0.348925\ -0.27262833\ 0.66768\ -0.10706167\ -0.283635\ 0.59580117\ 0.28747333\ -0.3366635\ 0.23393817\ 0.34349183\ 0.178405\ 0.1166155\ -0.076433\ 0.1445417\ 0.098086671 \end{bmatrix}$ 

#### Model

You now have all the pieces to finish implementing the model() function. After using sentence\_to\_avg() you need to pass the average through forward propagation, compute the cost, and then backpropagate to update the softmax's parameters.

**Exercise**: Implement the model() function described in Figure (2). Assuming here that Yoh ("Y one hot") is the one-hot encoding of the output labels, the equations you need to implement in the forward pass and to compute the cross-entropy cost are:

$$z^{(i)} = W.\,avg^{(i)} + b \ a^{(i)} = softmax(z^{(i)}) \ \mathcal{L}^{(i)} = -\sum_{k=0}^{n_y-1} Yoh_k^{(i)} * leg(a_k^{(i)})$$

It is possible to come up with a more efficient vectorized implementation. But since we are using a for-loop to convert the sentences one at a time into the avg^{(i)} representation anyway, let's not bother this time.

We provided you a function softmax().

```
In [11]: # GRADED FUNCTION: model

def model(X, Y, word_to_vec_map, learning_rate = 0.01, num_iterations = 400):
    """

Model to train word vector representations in numpy.

Arguments:
    X -- input data, numpy array of sentences as strings, of shape (m, 1)
    Y -- labels, numpy array of integers between 0 and 7, numpy-array of shape (m, 1)
    word_to_vec_map -- dictionary mapping every word in a vocabulary into its 50-dimensional vector representation
    learning_rate -- learning_rate for the stochastic gradient descent algorithm
    num_iterations -- number of iterations

Returns:
    pred -- vector of predictions, numpy-array of shape (m, 1)
    W -- weight matrix of the softmax layer, of shape (n_y, n_h)
    b -- bias of the softmax layer, of shape (n_y, )
"""
```

```
np.random.seed(1)
    # Define number of training examples
                                            # number of training examples
    m = Y.shape[0]
    n y = 5
                                            # number of classes
    n h = 50
                                            # dimensions of the GloVe vectors
    # Initialize parameters using Xavier initialization
    W = np.random.randn(n_y, n_h) / np.sqrt(n_h)
    b = np.zeros((n y,))
   # Convert Y to Y_onehot with n_y classes
   Y_oh = convert_to_one_hot(Y, C = n_y)
    # Optimization Loop
    for t in range(num_iterations):
                                                         # Loop over the number of iterations
        for i in range(m):
                                                         # Loop over the training examples
            ### START CODE HERE ### (≈ 4 lines of code)
            # Average the word vectors of the words from the i'th training example
            avg = sentence_to_avg(X[i,], word_to_vec_map)
            # Forward propagate the avg through the softmax layer
            z = np.dot(W, avg) + b
            a = softmax(z)
            # Compute cost using the i'th training label's one hot representation and "A" (the output of the softmax)
            cost = Y oh*np.log(a) wrong! should be
                                                           cost = -np.sum(Y_oh[i] * np.log(a))
            ### END CODE HERE ###
            # Compute gradients
            dz = a - N \circ [i]
            dW = np.dot(dz.reshape(n_y,1), avg.reshape(1, n_h))
                                                                                       SGD
chain rule
                                                                 avg.transpose
            db = dz
            # Update parameters with Stochastic Gradient Descent
            W = W - learning_rate * dW
            b = b - learning rate * db
        if t % 100 == 0:
            print("Epoch: " + str(t) + " --- cost = " + str(cost))
            pred = predict(X, Y, W, b, word to vec map)
    return pred, W, b
```

```
In [12]: print(X train.shape)
         print(Y train.shape)
         print(np.eye(5)[Y_train.reshape(-1)].shape)
         print(X_train[0])
         print(type(X_train))
         Y = np.asarray([5,0,0,5, 4, 4, 4, 6, 6, 4, 1, 1, 5, 6, 6, 3, 6, 3, 4, 4])
         print(Y.shape)
         X = np.asarray(['I am going to the bar tonight', 'I love you', 'miss you my dear',
          'Lets go party and drinks', 'Congrats on the new job', 'Congratulations',
          'I am so happy for you', 'Why are you feeling bad', 'What is wrong with you',
          'You totally deserve this prize', 'Let us go play football',
          'Are you down for football this afternoon', 'Work hard play harder',
          'It is suprising how people can be dumb sometimes',
          'I am very disappointed', 'It is the best day in my life',
          'I think I will end up alone', 'My life is so boring', 'Good job',
          'Great so awesome'])
         print(X.shape)
         print(np.eye(5)[Y train.reshape(-1)].shape)
         print(type(X_train))
         (132,)
         (132,)
         (132, 5)
```

Run the next cell to train your model and learn the softmax parameters (W,b).

never talk to me again
<class 'numpy.ndarray'>

<class 'numpy.ndarray'>

(20,) (20,) (132, 5) In [13]: pred, W, b = model(X\_train, Y\_train, word\_to\_vec\_map)
 print(pred)

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Accuracy: 0.931818181818
Epoch: 200 --- cost = [[-0. -0.
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Accuracy: 0.954545454545
Epoch: 300 --- \cos t = [[-0.
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[-4.03247023	-0.	-0.	-0.	-0. ]
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Accuracy: 0.969696969697
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**Expected Output** (on a subset of iterations):

**Epoch: 0**	cost = 1.95204988128	Accuracy: 0.348484848485
**Epoch: 100**	cost = 0.0797181872601	Accuracy: 0.931818181818
**Epoch: 200**	cost = 0.0445636924368	Accuracy: 0.954545454545
**Epoch: 300**	cost = 0.0343226737879	Accuracy: 0.969696969697

Great! Your model has pretty high accuracy on the training set. Lets now see how it does on the test set.

## 1.4 - Examining test set performance

```
In [14]: print("Training set:")
    pred_train = predict(X_train, Y_train, W, b, word_to_vec_map)
    print('Test set:')
    pred_test = predict(X_test, Y_test, W, b, word_to_vec_map)
```

Training set:

Accuracy: 0.977272727273

Test set:

Accuracy: 0.857142857143

## **Expected Output:**

**Train set accuracy**	97.7
**Test set accuracy**	85.7

Random guessing would have had 20% accuracy given that there are 5 classes. This is pretty good performance after training on only 127 examples.

In the training set, the algorithm saw the sentence "I love you" with the label . You can check however that the word "adore" does not appear in the training set. Nonetheless, lets see what happens if you write "I adore you."

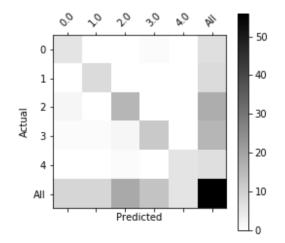
i adore you ♥
i love you ♥
funny lol ☺
lets play with a ball ☺
food is ready 悄
not feeling happy ☺

Amazing! Because adore has a similar embedding as love, the algorithm has generalized correctly even to a word it has never seen before. Words such as heart, dear, beloved or adore have embedding vectors similar to love, and so might work too--feel free to modify the inputs above and try out a variety of input sentences. How well does it work?

Note though that it doesn't get "not feeling happy" correct. This algorithm ignores word ordering, so is not good at understanding phrases like "not happy."

Printing the confusion matrix can also help understand which classes are more difficult for your model. A confusion matrix shows how often an example whose label is one class ("actual" class) is mislabeled by the algorithm with a different class ("predicted" class).

(56,)		_			4	
	•	ூ			11	
Predicted	0.0	1.0	2.0	3.0	4.0	All
Actual						
0	6	0	0	1	0	7
1	0	8	0	0	0	8
2	2	0	16	0	0	18
3	1	1	2	12	0	16
4	0	0	1	0	6	7
All	9	9	19	13	6	56



#### What you should remember from this part:

- Even with a 127 training examples, you can get a reasonably good model for Emojifying. This is due to the generalization power word vectors gives you.
- Emojify-V1 will perform poorly on sentences such as "This movie is not good and not enjoyable" because it doesn't understand combinations of words-it just averages all the words' embedding vectors together, without paying attention to the ordering of words. You will build a better algorithm in the next part.

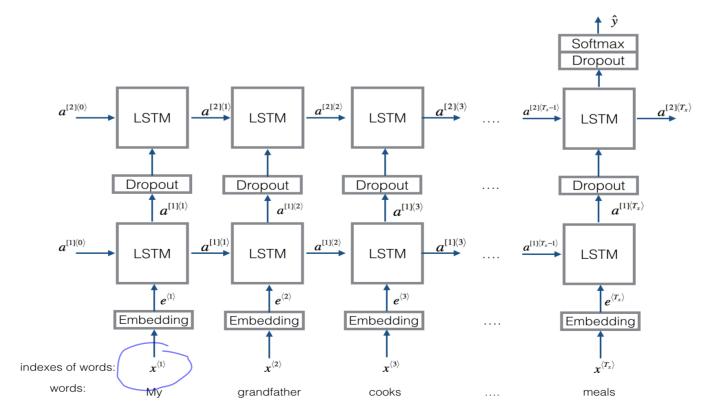
## 2 - Emojifier-V2: Using LSTMs in Keras:

Let's build an LSTM model that takes as input word sequences. This model will be able to take word ordering into account. Emojifier-V2 will continue to use pre-trained word embeddings to represent words, but will feed them into an LSTM, whose job it is to predict the most appropriate emoji.

Run the following cell to load the Keras packages.

### 2.1 - Overview of the model

Here is the Emojifier-v2 you will implement:



\*\*Figure 3\*\*: Emojifier-V2. A 2-layer LSTM sequence classifier.

## 2.2 Keras and mini-batching

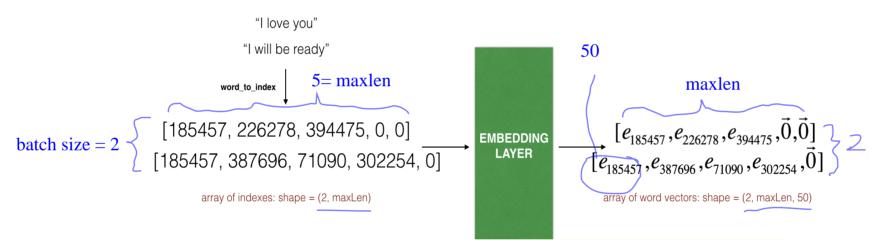
In this exercise, we want to train Keras using mini-batches. However, most deep learning frameworks require that all sequences in the same mini-batch have the same length. This is what allows vectorization to work; If you had a 3-word sentence and a 4-word sentence, then the computations needed for them are different (one takes 3 steps) of an LSTM, one takes 4 steps) so it's just not possible to do them both at the same time.

The common solution to this is to use padding. Specifically, set a maximum sequence length, and pad all sequences to the same length. For example, of the maximum sequence length is 20, we could pad every sentence with "0"s so that each input sentence is of length 20. Thus, a sentence "i love you" would be represented as  $(e_i, e_{love}, e_{you}, \vec{0}, \vec{0}, \dots, \vec{0})$  In this example, any sentences longer than 20 words would have to be truncated. One simple way to choose the maximum sequence length is to just pick the length of the longest sentence in the training set.

## 2.3 - The Embedding layer

In Keras, the embedding matrix is represented as a "layer", and maps positive integers (indices corresponding to words) into dense vectors of fixed size (the embedding vectors). It can be trained or initialized with a pretrained embedding. In this part, you will learn how to create an <a href="Embedding()">Embedding()</a> (https://keras.io/layers/embeddings/) layer in Keras, initialize it with the GloVe 50-dimensional vectors loaded earlier in the notebook. Because our training set is quite small, we will not update the word embeddings but will instead leave their values fixed. But in the code below, we'll show you how Keras allows you to either train or leave fixed this layer.

The Embedding() layer takes an integer matrix of size (batch size, max input length) as input. This corresponds to sentences converted into lists of indices (integers), as shown in the figure below.



\*\*Figure 4\*\*: Embedding layer. This example shows the propagation of two examples through the embedding layer. Both have been zero-padded to a length of `max\_len=5`. The final dimension of the representation is `(2,max\_len,50)` because the word embeddings we are using are 50 dimensional.

The largest integer (i.e. word index) in the input should be no larger than the vocabulary size. The layer outputs an array of shape (batch size, max input length, dimension of word vectors).

The first step is to convert all your training sentences into lists of indices, and then zero-pad all these lists so that their length is the length of the longest sentence.

Exercise: Implement the function below to convert X (array of sentences as strings) into an array of indices corresponding to words in the sentences. The output shape should be such that it can be given to Embedding() (described in Figure 4).

```
In [18]: # GRADED FUNCTION: sentences to indices
         def sentences to indices(X, word to index, max len):
             Converts an array of sentences (strings) into an array of indices corresponding to words in the sentences.
             The output shape should be such that it can be given to `Embedding()` (described in Figure 4).
             Arguments:
             X -- array of sentences (strings), of shape (m, 1)
             word to index -- a dictionary containing the each word mapped to its index
             max len -- maximum number of words in a sentence. You can assume every sentence in X is no longer than this.
             Returns:
             X_indices -- array of indices corresponding to words in the sentences from X, of shape (m, max_len)
             m = X.shape[0]
                                                              # number of training examples
             ### START CODE HERE ###
             # Initialize X_indices as a numpy matrix of zeros and the correct shape (≈ 1 line)
             X indices = np.zeros((m, max len))
             for i in range(m):
                                                              # loop over training examples
                 # Convert the ith training sentence in lower case and split is into words. You should get a list of words.
                 sentence words =X[i, ].lower().split()
                 # Initialize j to 0
                 j = 0
                 # Loop over the words of sentence_words
                 for w in sentence words:
                     # Set the (i,j)th entry of X_indices to the index of the correct word.
                     X indices[i, j] = word to index[w]
                     # Increment j to j + 1
                     j = j + 1
             ### END CODE HERE ###
             return X indices
```

Run the following cell to check what sentences\_to\_indices() does, and check your results.

```
In [19]: X1 = np.array(["funny lol", "lets play baseball", "food is ready for you"])
   X1_indices = sentences_to_indices(X1,word_to_index, max_len = 5)
   print("X1 =", X1)
   print("X1_indices =", X1_indices)

X1 = ['funny lol' 'lets play baseball' 'food is ready for you']
```

[ 220930. 286375. 69714. 0. 0.] [ 151204. 192973. 302254. 151349. 394475.]]

0.

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X1\_indices = [[ 155345. 225122.

### **Expected Output:**

**X1 =** ['funny lol' 'lets play football' 'food is ready fo			
	**X1_indices =**	[[ 155345. 225122. 0. 0. 0.] [ 220930. 286375. 151266. 0. 0.] [ 151204. 192973. 302254. 151349. 394475.]]	

Let's build the Embedding() layer in Keras, using pre-trained word vectors. After this layer is built, you will pass the output of sentences\_to\_indices() to it as an input, and the Embedding() layer will return the word embeddings for a sentence.

**Exercise**: Implement pretrained\_embedding\_layer(). You will need to carry out the following steps:

- 1. Initialize the embedding matrix as a numpy array of zeroes with the correct shape.
- 2. Fill in the embedding matrix with all the word embeddings extracted from word\_to\_vec\_map.
- 3. Define Keras embedding layer. Use Embedding() (https://keras.io/layers/embeddings/). Be sure to make this layer non-trainable, by setting trainable = False when calling Embedding(). If you were to set trainable = True, then it will allow the optimization algorithm to modify the values of the word embeddings.
- 4. Set the embedding weights to be equal to the embedding matrix

```
In [20]: # GRADED FUNCTION: pretrained embedding Layer
            def pretrained_embedding_layer(word_to_vec_map, word_to_index):
                Creates a Keras Embedding() Layer and Loads in pre-trained GloVe 50-dimensional vectors.
                Arauments:
                word to vec map -- dictionary mapping words to their GloVe vector representation.
                word to index -- dictionary mapping from words to their indices in the vocabulary (400,001 words)
                                                                                        word_to_index, index_to_word, word_to_vec_map = read_glove_vecs('data/glove.6B.50d.txt')
                embedding_layer -- pretrained layer Keras instance
                                                                     # adding 1 to fit Keras embedding (requirement) Note that zero is not used when building the word_to_index, hence it is "reserved"
                vocab_len = len(word_to_index) + 1
                emb dim = word to vec map["cucumber"].shape[0]
                                                                     # define dimensionality of your GloVe word vectors (= 50)
                ### START CODE HERE ###
                # Initialize the embedding matrix as a numpy array of zeros of shape (vocab len, dimensions of word vectors = emb dim)
                emb matrix = np.zeros((vocab len, emb dim))
                # Set each row "index" of the embedding matrix to be the word vector representation of the "index"th word of the vocabulary
                for word, index in word to index.items():
                    emb_matrix[index, :] = word_to_vec_map[word]
                # Define Keras embedding layer with the correct output/input sizes, make it trainable. Use Embedding(...). Make sure to set trainable=False.
                embedding layer = Embedding(vocab len, emb dim,trainable = False)
                ### END CODE HERE ###
                # Build the embedding layer, it is required before setting the weights of the embedding layer. Do not modify the "None".
embedding layer
                embedding layer.build((None,))
                                                                                                                         Can't google anything that explain why it is NONE
                # Set the weights of the embedding layer to the embedding matrix. Your layer is now pretrained.
                embedding layer.set weights([emb matrix])
                return embedding layer
  In [21]: embedding_layer = pretrained_embedding_layer(word_to_vec_map, word_to_index)
```

**Expected Output:** 

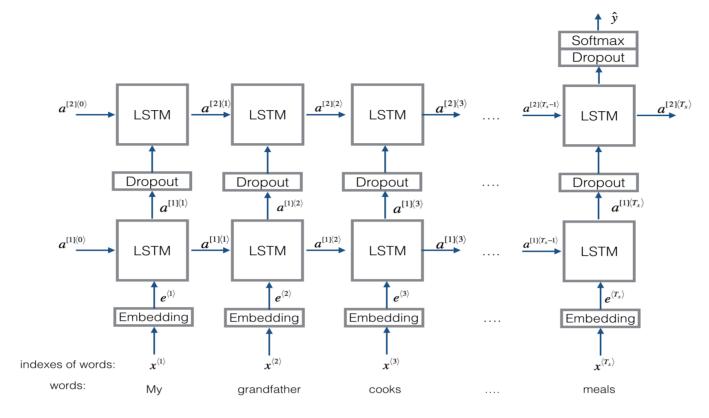
weights[0][1][3] = -0.3403

print("weights[0][1][3] =", embedding\_layer.get\_weights()[0][1][3])

\*\*weights[0][1][3] =\*\* -0.3403

# 2.3 Building the Emojifier-V2

Lets now build the Emojifier-V2 model. You will do so using the embedding layer you have built, and feed its output to an LSTM network.



\*\*Figure 3\*\*: Emojifier-v2. A 2-layer LSTM sequence classifier.

**Exercise:** Implement Emojify\_V2(), which builds a Keras graph of the architecture shown in Figure 3. The model takes as input an array of sentences of shape (m, max\_len, ) defined by input\_shape. It should output a softmax probability vector of shape (m, C = 5). You may need Input(shape = ..., dtype = '...'), <u>LSTM() (https://keras.io/layers/recurrent/#lstm)</u>, <u>Dropout() (https://keras.io/layers/core/#dropout)</u>, <u>Dense() (https://keras.io/layers/core/#dense)</u>, and <u>Activation() (https://keras.io/activations/)</u>.

```
In [50]: # GRADED FUNCTION: Emojify V2
                   def Emojify V2(input shape, word to vec map, word to index):
                           Function creating the Emojify-v2 model's graph.
                          Arauments:
                          input_shape -- shape of the input, usually (max Len,) This is usually (max_Len,) because the input features (i.e. Embeddings) will be attached only later.
                          word to vec map -- dictionary mapping every word in a vocabulary into its 50-dimensional vector representation
                           word to index -- dictionary mapping from words to their indices in the vocabulary (400,001 words)
                          Returns:
                           model -- a model instance in Keras
                           ### START CODE HERE ###
                           # Define sentence indices as the input of the graph, it should be of shape input shape and dtype 'int32' (as it contains indices).
                          sentence indices = Input(shape = input shape, dtype = 'int32') Input layer
                                                                                             (max Len.)
                           # Create the embedding layer pretrained with GloVe Vectors (≈1 line)
                          # Create the embedding layer pretrained with GloVe Vectors (~1 line)
embedding_layer = pretrained_embedding_layer(word_to_vec_map, word_to_index)
embedding_layer = Embedding_
                           # Propagate sentence indices through your embedding layer, you get back the embeddings
                           embeddings = embedding layer(sentence indices)
                           # Propagate the embeddings through an LSTM layer with 128-dimensional hidden state
                           # Be careful, the returned output should be a batch of sequences.
                          X = LSTM(128, return sequences = True)(embeddings)
                          # Add dropout with a probability of 0.5
                          X = Dropout(0.5)(X)
                           # Propagate X trough another LSTM Layer with 128-dimensional hidden state
                          # Be careful, the returned output should be a single hidden state, not a batch of sequences.
                          X = LSTM(128, return_sequences = False)(X)
                          # Add dropout with a probability of 0.5
                          X = Dropout(0.5)(X)
                           # Propagate X through a Dense Layer with softmax activation to get back a batch of 5-dimensional vectors.
                          X = Dense(5)(X)
                          # Add a softmax activation
                          X = Activation('softmax')(X)
                           # Create Model instance which converts sentence indices into X.
                          model = Model(sentence indices, X)
                           ### END CODE HERE ###
                           return model
```

Run the following cell to create your model and check its summary. Because all sentences in the dataset are less than 10 words, we chose  $max_1en = 10$ . You should see your architecture, it uses "20,223,927" parameters, of which 20,000,050 (the word embeddings) are non-trainable, and the remaining 223,877 are. Because our vocabulary size has 400,001 words (with valid indices from 0 to 400,000) there are 400,001\*50 = 20,000,050 non-trainable parameters.

```
In [51]: model = Emojify_V2((maxLen,), word_to_vec_map, word_to_index)
    model.summary()
```

Layer (type)	Output Shape	Param #
input_14 (InputLayer)	(None, 10)	0
embedding_23 (Embedding)	(None, 10, 50)	20000050
lstm_22 (LSTM)	(None, 10, 128)	91648
dropout_19 (Dropout)	(None, 10, 128)	0
1stm_23 (LSTM)	(None, 128)	131584
dropout_20 (Dropout)	(None, 128)	0
dense_10 (Dense)	(None, 5)	645
activation_6 (Activation)	(None, 5)	0
Total params: 20.223.927		

Total params: 20,223,927
Trainable params: 223,877

Non-trainable params: 20,000,050

As usual, after creating your model in Keras, you need to compile it and define what loss, optimizer and metrics your are want to use. Compile your model using categorical\_crossentropy loss, adam optimizer and ['accuracy'] metrics:

```
In [52]: model.compile(loss='categorical_crossentropy', optimizer='adam', metrics=['accuracy'])
```

It's time to train your model. Your Emojifier-V2 model takes as input an array of shape (m, max\_len) and outputs probability vectors of shape (m, number of classes). We thus have to convert X\_train (array of sentences as strings) to X\_train\_indices (array of sentences as list of word indices), and Y\_train (labels as indices) to Y\_train\_oh (labels as one-hot vectors).

```
In [53]: X_train_indices = sentences_to_indices(X_train, word_to_index, maxLen)
Y_train_oh = convert_to_one_hot(Y_train, C = 5)
```

Fit the Keras model on X\_train\_indices and Y\_train\_oh. We will use epochs = 50 and batch\_size = 32.

In [54]: model.fit(X\_train\_indices, Y\_train\_oh, epochs = 50, batch\_size = 32, shuffle=True)

Keras shuffles for you

F h. 4 /FO
Epoch 1/50 132/132 [====================================
Epoch 2/50
132/132 [====================================
Epoch 3/50
132/132 [====================================
Epoch 4/50
132/132 [====================================
Epoch 5/50
132/132 [====================================
Epoch 6/50
132/132 [====================================
Epoch 7/50 132/132 [====================================
Epoch 8/50
132/132 [====================================
Epoch 9/50
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Epoch 10/50
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Epoch 11/50
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Epoch 12/50 132/132 [====================================
Epoch 13/50
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Epoch 14/50
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Epoch 15/50
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Epoch 16/50
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Epoch 18/50
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Epoch 19/50
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Epoch 20/50
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Epoch 21/50
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Epoch 27/50
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Epoch 28/50
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Epoch 29/50
132/132 [====================================
Epoch 30/50

```
Epoch 31/50
   Epoch 32/50
   Epoch 33/50
   Epoch 34/50
   132/132 [============== ] - 0s - loss: 0.2808 - acc: 0.9091
   Epoch 35/50
   Epoch 36/50
   Epoch 37/50
   132/132 [============== ] - 0s - loss: 0.1150 - acc: 0.9848
   Epoch 38/50
   Epoch 39/50
   132/132 [============= ] - 0s - loss: 0.0919 - acc: 0.9848
   Epoch 40/50
   Epoch 41/50
   Epoch 42/50
   Epoch 43/50
   Epoch 44/50
   132/132 [============= ] - 0s - loss: 0.0139 - acc: 1.0000
   Epoch 45/50
   Epoch 46/50
   132/132 [============= ] - 0s - loss: 0.0107 - acc: 1.0000
   Epoch 47/50
   Epoch 48/50
   Epoch 49/50
   Epoch 50/50
   Out[54]: <keras.callbacks.History at 0x7f638b58b710>
```

Your model should perform close to 100% accuracy on the training set. The exact accuracy you get may be a little different. Run the following cell to evaluate your model on the test set.

```
In [55]: X_test_indices = sentences_to_indices(X_test, word_to_index, max_len = maxLen)
Y_test_oh = convert_to_one_hot(Y_test, C = 5)
loss, acc = model.evaluate(X_test_indices, Y_test_oh)
print()
print("Test accuracy = ", acc)
32/56 [=========>.....] - ETA: 0s
```

You should get a test accuracy between 80% and 95%. Run the cell below to see the mislabelled examples.

Test accuracy = 0.875

Expected emoji:∜ prediction: I did not have breakfast ♥

Expected emoji: prediction: she is a bully Expected emoji: prediction: go away

Expected emoji: prediction: yesterday we lost again

Now you can try it on your own example. Write your own sentence below.

Previously, Emojify-V1 model did not correctly label "not feeling happy," but our implementation of Emojiy-V2 got it right. (Keras' outputs are slightly random each time, so you may not have obtained the same result.) The current model still isn't very robust at understanding negation (like "not happy") because the training set is small and so doesn't have a lot of examples of negation. But if the training set were larger, the LSTM model would be much better than the Emojify-V1 model at understanding such complex sentences.

## Congratulations!

You have completed this notebook! ♥♥♥

#### What you should remember:

- If you have an NLP task where the training set is small, using word embeddings can help your algorithm significantly. Word embeddings allow your model to work on words in the test set that may not even have appeared in your training set.
- Training sequence models in Keras (and in most other deep learning frameworks) requires a few important details:
  - To use mini-batches, the sequences need to be padded so that all the examples in a mini-batch have the same length.
  - An Embedding() layer can be initialized with pretrained values. These values can be either fixed or trained further on your dataset. If however your labeled dataset is small, it's usually not worth trying to train a large pre-trained set of embeddings.
  - LSTM() has a flag called return\_sequences to decide if you would like to return every hidden states or only the last one.
  - You can use Dropout() right after LSTM() to regularize your network.

Congratulations on finishing this assignment and building an Emojifier. We hope you're happy with what you've accomplished in this notebook!

