

# 可验证对称加密搜索问题 分析与研究

(申请清华大学工程硕士专业学位论文)

培 养 单 位: 计 算 机 科 学 与 技 术 系

学 科: 计 算 机 技 术

申 请 人: 朱 洁

指 导 教 师: 李 琦 副 研 究 员

二〇一八年四月



# **Analysis and Research of Verifiable Searchable Symmetric Encryption**

Thesis Submitted to  
**Tsinghua University**  
in partial fulfillment of the requirement  
for the professional degree of  
**Master of Engineering**

by  
**Zhu Jie**  
**( Computer Technology )**

Thesis Supervisor : Professor Li Qi

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## 摘 要

云计算的发展使得用户可以很方便的存储、获取与分享数据。但与此同时，云存储也带来了很多安全问题，例如，数据隐私泄露。对称加密搜索的提出解决了数据隐私泄露的问题，同时也保证了数据的可用性。通过使用对称加密搜索方案，用户可以在上传数据之前，对数据进行加密，同时云服务器可以在用户的加密数据上进行搜索，从而确保数据的隐私性。

本文的创新点主要有：

- 用例子来解释模板的使用方法；
- 用废话来填充无关紧要的部分；
- 一边学习摸索一边编写新代码。

**关键词：**对称加密搜索；结果验证；云计算，云存储

## Abstract

Searchable Symmetric Encryption (SSE) has been widely studied in cloud storage, which allows cloud services to directly search over encrypted data. Most SSE schemes only work with honest-but-curious cloud services that do not deviate from the prescribed protocols. However, this assumption does not always hold in practice due to the untrusted nature in storage outsourcing. To alleviate the issue, there have been studies on Verifiable Searchable Symmetric Encryption (VSSE), which functions against malicious cloud services by enabling results verification. But to our best knowledge, existing VSSE schemes exhibit very limited applicability, such as only supporting static database, demanding specific SSE constructions, or only working in the single-user model. In this paper, we propose GSSE, the first generic verifiable SSE scheme in the single-owner multiple-user model, which provides verifiability for any SSE schemes and further supports data updates. To generically support result verification, we first decouple the proof index in GSSE from SSE. We then leverage Merkle Patricia Tree (MPT) and Incremental Hash to build the proof index with data update support. We also develop a timestamp-chain for data freshness maintenance across multiple users. Rigorous analysis and experimental evaluations show that GSSE is secure and introduces small overhead for result verification.

**Key words:** Searchable Symmetric Encryption; Result Verification; Cloud Computing; Cloud Storage



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## 主要符号对照表

HPC	高性能计算 (High Performance Computing)
cluster	集群
Itanium	安腾
SMP	对称多处理
API	应用程序编程接口
PI	聚酰亚胺
MPI	聚酰亚胺模型化合物, N-苯基邻苯酰亚胺
PBI	聚苯并咪唑
MPBI	聚苯并咪唑模型化合物, N-苯基苯并咪唑
PY	聚吡咯
PMDA-BDA	均苯四酸二酐与联苯四胺合成的聚吡咯薄膜
$\Delta G$	活化自由能 (Activation Free Energy)
$\chi$	传输系数 (Transmission Coefficient)
$E$	能量
$m$	质量
$c$	光速
$P$	概率
$T$	时间
$v$	速度
劝学	<p>君子曰：学不可以已。青，取之于蓝，而青于蓝；冰，水为之，而寒于水。木直中绳。鞣以为轮，其曲中规。虽有槁暴，不复挺者，鞣使之然也。故木受绳则直，金就砺则利，君子博学而日参省乎己，则知明而行无过矣。吾尝终日而思矣，不如须臾之所学也；吾尝跂而望矣，不如登高之博见也。登高而招，臂非加长也，而见者远；顺风而呼，声非加疾也，而闻者彰。假舆马者，非利足也，而致千里；假舟楫者，非能水也，而绝江河，君子生非异也，善假于物也。积土成山，风雨兴焉；积水成渊，蛟龙生焉；积善成德，而神明自得，圣心备焉。故不积跬步，无以至千里；不积小流，无以成江海。骐骥一跃，不能十步；驽马十驾，功在不舍。锲而舍之，朽木不折；锲而不舍，金石可镂。蚓无爪牙之利，筋骨之强，上食埃土，下饮黄泉，用心一也。蟹</p>

六跪而二螯，非蛇鱗之穴无可寄托者，用心躁也。——荀况

## 第 1 章 引言

## 第 2 章 相关研究综述

## 第 3 章 问题描述与定义

## 第 4 章 单用户下的可验证加密搜索方案研究

## 第 5 章 多用户下的可验证加密搜索方案研究



## 第 6 章 总结与展望

## 插图索引

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## 致 谢

衷心感谢导师 xxx 教授和物理系 xxx 副教授对本人的精心指导。他们的言传身教将使我终生受益。

在美国麻省理工学院化学系进行九个月的合作研究期间，承蒙 xxx 教授热心指导与帮助，不胜感激。感谢 xx 实验室主任 xx 教授，以及实验室全体老师和同学们的热情帮助和支持！本课题承蒙国家自然科学基金资助，特此致谢。

感谢 L<sup>A</sup>T<sub>E</sub>X 和 Th<sub>U</sub>T<sub>H</sub>ESIS<sup>[?]</sup>，帮我节省了不少时间。

## 声 明

本人郑重声明：所呈交的学位论文，是本人在导师指导下，独立进行研究工作所取得的成果。尽我所知，除文中已经注明引用的内容外，本学位论文的研究成果不包含任何他人享有著作权的内容。对本论文所涉及的研究工作做出贡献的其他个人和集体，均已在文中以明确方式标明。

签 名：\_\_\_\_\_ 日 期：\_\_\_\_\_

## 附录 A 外文资料原文

The title of the English paper

**Abstract:** As one of the most widely used techniques in operations research, *mathematical programming* is defined as a means of maximizing a quantity known as *objective function*, subject to a set of constraints represented by equations and inequalities. Some known subtopics of mathematical programming are linear programming, nonlinear programming, multiobjective programming, goal programming, dynamic programming, and multilevel programming<sup>[1]</sup>.

It is impossible to cover in a single chapter every concept of mathematical programming. This chapter introduces only the basic concepts and techniques of mathematical programming such that readers gain an understanding of them throughout the book<sup>[2,3]</sup>.

### A.1 Single-Objective Programming

The general form of single-objective programming (SOP) is written as follows,

$$\begin{cases} \max f(x) \\ \text{subject to:} \\ g_j(x) \leq 0, \quad j = 1, 2, \dots, p \end{cases} \quad (123)$$

which maximizes a real-valued function  $f$  of  $x = (x_1, x_2, \dots, x_n)$  subject to a set of constraints.

**Definition A.1:** In SOP, we call  $x$  a decision vector, and  $x_1, x_2, \dots, x_n$  decision variables. The function  $f$  is called the objective function. The set

$$S = \{x \in \mathbb{R}^n \mid g_j(x) \leq 0, j = 1, 2, \dots, p\} \quad (456)$$

is called the feasible set. An element  $x$  in  $S$  is called a feasible solution.

Definition A.2: A feasible solution  $x^*$  is called the optimal solution of SOP if and only if

$$f(x^*) \geq f(x) \quad (\text{A-1})$$

for any feasible solution  $x$ .

One of the outstanding contributions to mathematical programming was known as the Kuhn-Tucker conditions A-2. In order to introduce them, let us give some definitions. An inequality constraint  $g_j(x) \leq 0$  is said to be active at a point  $x^*$  if  $g_j(x^*) = 0$ . A point  $x^*$  satisfying  $g_j(x^*) \leq 0$  is said to be regular if the gradient vectors  $\nabla g_j(x)$  of all active constraints are linearly independent.

Let  $x^*$  be a regular point of the constraints of SOP and assume that all the functions  $f(x)$  and  $g_j(x)$ ,  $j = 1, 2, \dots, p$  are differentiable. If  $x^*$  is a local optimal solution, then there exist Lagrange multipliers  $\lambda_j$ ,  $j = 1, 2, \dots, p$  such that the following Kuhn-Tucker conditions hold,

$$\begin{cases} \nabla f(x^*) - \sum_{j=1}^p \lambda_j \nabla g_j(x^*) = 0 \\ \lambda_j g_j(x^*) = 0, \quad j = 1, 2, \dots, p \\ \lambda_j \geq 0, \quad j = 1, 2, \dots, p. \end{cases} \quad (\text{A-2})$$

If all the functions  $f(x)$  and  $g_j(x)$ ,  $j = 1, 2, \dots, p$  are convex and differentiable, and the point  $x^*$  satisfies the Kuhn-Tucker conditions (A-2), then it has been proved that the point  $x^*$  is a global optimal solution of SOP.

### A.1.1 Linear Programming

If the functions  $f(x)$ ,  $g_j(x)$ ,  $j = 1, 2, \dots, p$  are all linear, then SOP is called a *linear programming*.

The feasible set of linear is always convex. A point  $x$  is called an extreme point of convex set  $S$  if  $x \in S$  and  $x$  cannot be expressed as a convex combination of two points in  $S$ . It has been shown that the optimal solution to linear programming corresponds to an extreme point of its feasible set provided that the feasible set  $S$  is bounded. This fact is the basis of the *simplex algorithm* which was developed by Dantzig as a very efficient method for solving linear programming.



Table 1 This is an example for manually numbered table, which would not appear in the list of tables

Network Topology		# of nodes	# of clients			Server
GT-ITM	Waxman Transit-Stub	600	2%	10%	50%	Max. Connectivity
Inet-2.1		6000				
Xue	Rui	Ni	THUThESIS			
	ABCDEF					

Roughly speaking, the simplex algorithm examines only the extreme points of the feasible set, rather than all feasible points. At first, the simplex algorithm selects an extreme point as the initial point. The successive extreme point is selected so as to improve the objective function value. The procedure is repeated until no improvement in objective function value can be made. The last extreme point is the optimal solution.

#### A.1.2 Nonlinear Programming

If at least one of the functions  $f(x)$ ,  $g_j(x)$ ,  $j = 1, 2, \dots, p$  is nonlinear, then SOP is called a *nonlinear programming*.

A large number of classical optimization methods have been developed to treat special-structural nonlinear programming based on the mathematical theory concerned with analyzing the structure of problems.



Figure 1 This is an example for manually numbered figure, which would not appear in the list of figures

Now we consider a nonlinear programming which is confronted solely with maximizing a real-valued function with domain  $\mathcal{R}^n$ . Whether derivatives are available or not, the usual strategy is first to select a point in  $\mathcal{R}^n$  which is thought to be the most likely place where the maximum exists. If there is no information available on which to base such a selection, a point is chosen at random. From this first point an attempt is made to construct a sequence of points, each of which yields an improved objective function value over its predecessor. The next point to be added to the sequence is chosen by analyzing the behavior of the function at the previous points. This construction continues until some

termination criterion is met. Methods based upon this strategy are called *ascent methods*, which can be classified as *direct methods*, *gradient methods*, and *Hessian methods* according to the information about the behavior of objective function  $f$ . Direct methods require only that the function can be evaluated at each point. Gradient methods require the evaluation of first derivatives of  $f$ . Hessian methods require the evaluation of second derivatives. In fact, there is no superior method for all problems. The efficiency of a method is very much dependent upon the objective function.

### A.1.3 Integer Programming

*Integer programming* is a special mathematical programming in which all of the variables are assumed to be only integer values. When there are not only integer variables but also conventional continuous variables, we call it *mixed integer programming*. If all the variables are assumed either 0 or 1, then the problem is termed a *zero-one programming*. Although integer programming can be solved by an *exhaustive enumeration* theoretically, it is impractical to solve realistically sized integer programming problems. The most successful algorithm so far found to solve integer programming is called the *branch-and-bound enumeration* developed by Balas (1965) and Dakin (1965). The other technique to integer programming is the *cutting plane method* developed by Gomory (1959).

*Uncertain Programming* (BaoDing Liu, 2006.2)

## References

*NOTE: These references are only for demonstration. They are not real citations in the original text.*

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附录 B 外文资料的调研阅读报告或书面翻译

英文资料的中文标题

**摘要：**本章为外文资料翻译内容。如果有摘要可以直接写上来，这部分好像没有明确的规定。

B.1 单目标规划

北冥有鱼，其名为鲲。鲲之大，不知其几千里也。化而为鸟，其名为鹏。鹏之背，不知其几千里也。怒而飞，其翼若垂天之云。是鸟也，海运则将徙于南冥。南冥者，天池也。

$$p(y|\mathbf{x}) = \frac{p(\mathbf{x}, y)}{p(\mathbf{x})} = \frac{p(\mathbf{x}|y)p(y)}{p(\mathbf{x})} \tag{123}$$

吾生也有涯，而知也无涯。以有涯随无涯，殆已！已而为知者，殆而已矣！为善无近名，为恶无近刑，缘督以为经，可以保身，可以全生，可以养亲，可以尽年。

B.1.1 线性规划

庖丁为文惠君解牛，手之所触，肩之所倚，足之所履，膝之所倚，砉然响然，奏刀騞然，莫不中音，合于桑林之舞，乃中经首之会。

表 1 这是手动编号但不出现在索引中的一个表格例子

Network Topology		# of nodes	# of clients			Server
GT-ITM	Waxman Transit-Stub	600	2%	10%	50%	Max. Connectivity
Inet-2.1		6000				
Xue	Rui	Ni	THUThESIS			
	ABCDEF					

文惠君曰：“嘻，善哉！技盖至此乎？”庖丁释刀对曰：“臣之所好者道也，进乎技矣。始臣之解牛之时，所见无非全牛者；三年之后，未尝见全牛也；方今之时，臣以神遇而不以目视，官知止而神欲行。依乎天理，批大郤，导大窾，因其固然。技经肯綮之未尝，而况大瓠乎！良庖岁更刀，割也；族庖月更刀，折也；今臣之刀十九年矣，所解数千牛矣，而刀刃若新发于硎。彼节者有间而刀刃者无厚，以

无厚入有间，恢恢乎其于游刃必有余地矣。是以十九年而刀刃若新发于硎。虽然，每至于族，吾见其难为，怵然为戒，视为止，行为迟，动刀甚微，謦然已解，如土委地。提刀而立，为之而四顾，为之踌躇满志，善刀而藏之。”

文惠君曰：“善哉！吾闻庖丁之言，得养生焉。”

### B.1.2 非线性规划

孔子与柳下季为友，柳下季之弟名曰盗跖。盗跖从卒九千人，横行天下，侵暴诸侯。穴室枢户，驱人牛马，取人妇女。贪得忘亲，不顾父母兄弟，不祭先祖。所过之邑，大国守城，小国入保，万民苦之。孔子谓柳下季曰：“夫为人父者，必能诏其子；为人兄者，必能教其弟。若父不能诏其子，兄不能教其弟，则无贵父子兄弟之亲矣。今先生，世之才士也，弟为盗跖，为天下害，而弗能教也，丘窃为先生羞之。丘请为先生往说之。”



图1 这是手动编号但不出现索引中的图片的例子

柳下季曰：“先生言为人父者必能诏其子，为人兄者必能教其弟，若子不听父之诏，弟不受兄之教，虽今先生之辩，将奈之何哉？且跖之为人也，心如涌泉，意如飘风，强足以距敌，辩足以饰非。顺其心则喜，逆其心则怒，易辱人以言。先生必无往。”

孔子不听，颜回为驭，子贡为右，往见盗跖。

### B.1.3 整数规划

盗跖乃方休卒徒大山之阳，脍人肝而铺之。孔子下车而前，见谒者曰：“鲁人孔丘，闻将军高义，敬再拜谒者。”谒者入通。盗跖闻之大怒，目如明星，发上指冠，曰：“此夫鲁国之巧伪人孔丘非邪？为我告之：尔作言造语，妄称文、武，冠枝木之冠，带死牛之胁，多辞缪说，不耕而食，不织而衣，摇唇鼓舌，擅生是非，以迷天下之主，使天下学士不反其本，妄作孝弟，而侥幸于封侯富贵者也。子之罪大极重，疾走归！不然，我将以子肝益昼铺之膳。”

## 附录 C 其它附录

前面两个附录主要是给本科生做例子。其它附录的内容可以放到这里，当然如果你愿意，可以把这部分也放到独立的文件中，然后将其 `\input` 到主文件中。

## 个人简历、在学期间发表的学术论文与研究成果

### 个人简历

xxxx 年 xx 月 xx 日出生于 xx 省 xx 县。

xxxx 年 9 月考入 xx 大学 xx 系 xx 专业, xxxx 年 7 月本科毕业并获得 xx 学士学位。

xxxx 年 9 月免试进入 xx 大学 xx 系攻读 xx 学位至今。

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综合论文训练记录表

学生姓名		学号		班级	
论文题目					
主要内容以及进度安排	<div>指导教师签字：_____</div> <div>考核组组长签字：_____</div> <div>年 月 日</div>				
中期考核意见	<div>考核组组长签字：_____</div> <div>年 月 日</div>				



指导教师评语	<div>指导教师签字：_____</div> <div>年      月      日</div>
评阅教师评语	<div>评阅教师签字：_____</div> <div>年      月      日</div>
答辩小组评语	<div>答辩小组组长签字：_____</div> <div>年      月      日</div>

总成绩：\_\_\_\_\_

教学负责人签字：\_\_\_\_\_

年      月      日