

Where We Are

Source code
(character
stream)

```
if (b == 0) a = b;
```

Lexical Analysis
(Scanning)

Syntactic Analysis
(Parsing)

Semantic Analysis



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```
if (b == 0) a = b;  
i f ( b = = 0 ) a = b ;  
  0 )   a   =  
b ;
```

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if (b == 0) a = b;  
i f ( b = =  
  0 )   a =  
b ;
```

Token
stream

```
if ( b == 0 ) a = b ;
```

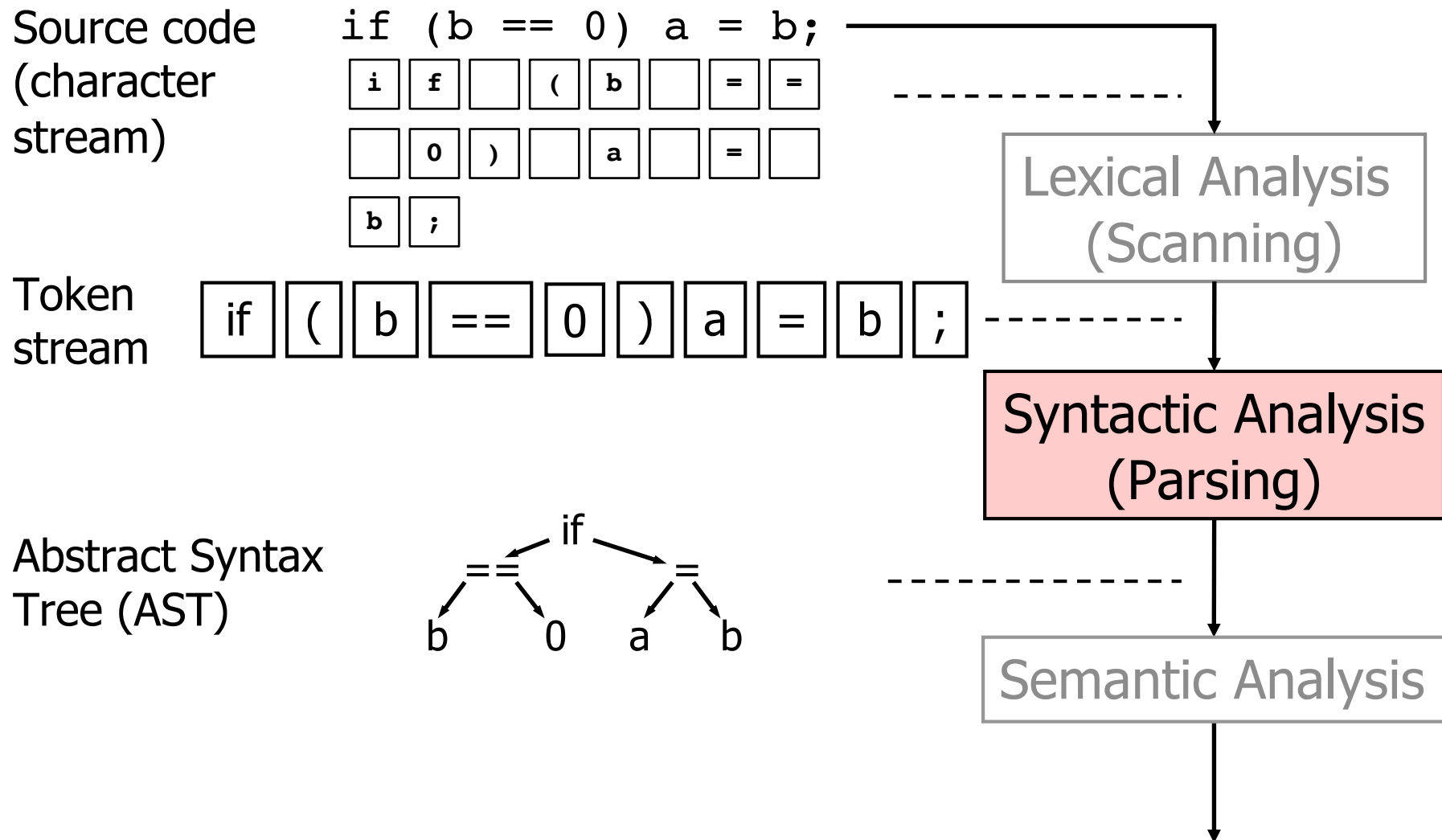
Lexical Analysis
(Scanning)

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Where We Are



Formalism

- Language vs. grammar
 - Language: A set (generally infinite) of strings over some alphabet.
 - Grammar: A finite generative description of a language.
 - Given a grammar G , $L(G)$ is the language that it generates.

Formalism

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 - Grammar: A finite generative description of a language.
 - Given a grammar G , $L(G)$ is the language that it generates.
- Context-Free Grammar $G = (N, T, P, S)$, where
 - N is a set of non-terminals;
 - T is a set of terminals (aka tokens);
 - P is a finite set of productions (rewrite rules) of the form $A \rightarrow \alpha$, where $A \in N$ and α is a **sentential form**;
 - $S \in N$ is the start symbol.

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- Sentential forms and sentences
 - Sentential form: A string that can be obtained by starting with S and using productions as rewrite rules to rewrite non-terminals.
 - Sentence: A sentential form without non-terminals, i.e., a word in the language $L(G)$.

Recognition vs. Parsing

- Given a grammar G and a sentence s
 - Recognition is a decision problem: $s \in L(G)$?
 - Parsing is a construction problem: Show a **derivation** (proof) that $s \in L(G)$.

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- Derivation of string using grammar
 - Start from S and repeatedly re-write one non-terminal at a time using the productions of the grammar, until there are no non-terminals left to re-write.
 - Leftmost/rightmost derivation: A derivation in which the leftmost/rightmost non-terminal of the current sentential form is rewritten at each step.

Example: Simple Expression Grammar

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Grammar: $E \rightarrow (E + E) \mid \text{num}$

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- Leftmost derivation

- $E \Rightarrow (E + E) \Rightarrow (2 + E) \Rightarrow (2 + 3)$

- Rightmost derivation

- $E \Rightarrow (E + E) \Rightarrow (E + 3) \Rightarrow (2 + 3)$

Ambiguity in Grammars

- Ambiguous grammar
 - A grammar in which there are two or more leftmost derivations for some sentence $s \in L(G)$.

- Consider

Grammar: $E \rightarrow E + E \mid E * E \mid (E) \mid \text{num}$

- The string $2 + 3 * 5$ has two distinct leftmost derivations.
 - $E \Rightarrow E + E \Rightarrow 2 + E \Rightarrow 2 + E * E \Rightarrow 2 + 3 * E \Rightarrow 2 + 3 * 5$
 - $E \Rightarrow E * E \Rightarrow E + E * E \Rightarrow 2 + E * E \Rightarrow 2 + 3 * E \Rightarrow 2 + 3 * 5$
- However, the strings $(2 + 3) * 5$ and $2 + (3 * 5)$ do have unique leftmost derivations.
 - $E \Rightarrow E * E \Rightarrow (E) * E \Rightarrow (E + E) * E \Rightarrow \dots \Rightarrow (2 + 3) * 5$
 - $E \Rightarrow E + E \Rightarrow E + (E) \Rightarrow E + (E * E) \Rightarrow \dots \Rightarrow 2 + (3 * 5)$