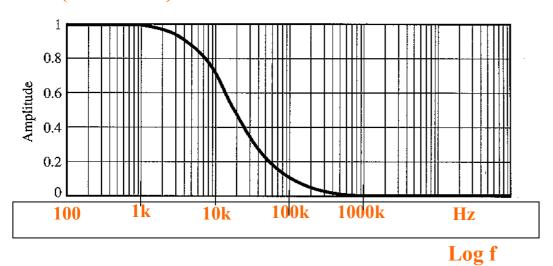
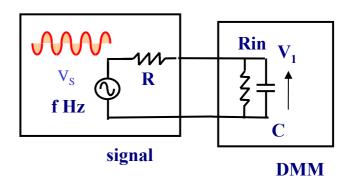
1

1. In the circuit, V_1 versus log-frequency f is given as shown. Find roughly the magnitude of V_S in V, bandwidth of DMM, and V_1 at bandwidth in Vrms. (13)

V1 (x 2.8Vrms)





magnitude $Vm \approx 4V$ (5)

bandwidth $\approx 10 \text{kHz}$ (4)

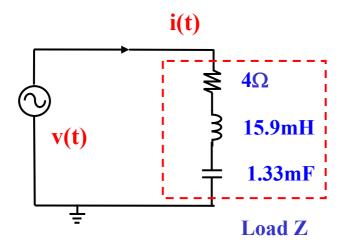
At bandwidth, V1 \approx 0.7 x 2.8 Vrms (4)

2a. In the circuit, $\mathbf{v}(\mathbf{t}) = 120\sqrt{2}\cos(2\pi60\mathbf{t})\mathbf{V}$

Find the frequency and period of v(t), and the V phasor of v(t). Show also the impedance of load Z is roughly

 $4+j4\Omega$, and hence show that $~i(t)\cong 30\cos(2\pi 60t-45^{o})A$. (24)

2b. Plot v(t) and i(t) together. Show clearly the phase angles and amplitudes. Find the phase angles between v(t) and i(t). Does v(t) lead i(t)? Plot also phasor V and I in a phasor diagram. (14)



2a

Find frequency f of v(t)

$$\mathbf{f} = 60\,\mathbf{Hz} \tag{2}$$

Find period of v(t)

$$T = \frac{1}{f} = \frac{1}{60 \text{ Hz}} \cong 16.7 \text{ ms}$$
 (3)

Find V phasor

$$\mathbf{V} = 120\sqrt{2} \angle 0^{\circ} \mathbf{V}$$
 (2)

Find impedance Z

$$\frac{1}{\mathbf{j}\omega\mathbf{C}} = \frac{1}{\mathbf{j}(2\pi60)(1.33\mathbf{mF})} \cong -2\mathbf{j}\Omega \quad (3)$$

$$\mathbf{j}\omega\mathbf{L} = \mathbf{j} * 2\pi 60 * 15.9 \mathbf{mH} \cong 6\mathbf{j}\Omega$$
 (3)

$$\mathbf{Z} = \mathbf{R} + \mathbf{j}\omega\mathbf{L} + \frac{1}{\mathbf{j}\omega\mathbf{C}} = 4 + \mathbf{j}6 - \mathbf{j}2\Omega$$

$$= 4 + \mathbf{j}4\Omega$$
(2)

Find I

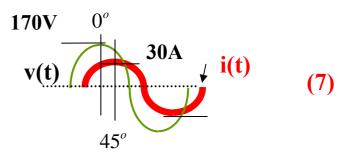
 $=4\sqrt{2}\angle 45^{\circ}\Omega$

$$\therefore \mathbf{I} = \frac{\mathbf{V}}{\mathbf{Z}} = \frac{120\sqrt{2} \angle 0^{\circ} \mathbf{V}}{4\sqrt{2} \angle 45^{\circ} \Omega}$$

$$= 30 \angle -45^{\circ} \mathbf{A}$$
(5)

$$i(t) = 30 \cos(2\pi 60t - 45^{\circ}) A$$

2b

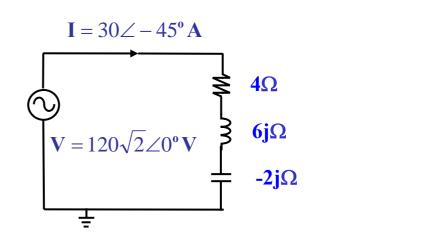


$$i(t) lags v(t) by 45^{\circ}$$
 (3)

$$\mathbf{V} = 120\sqrt{2}\angle 0^{\circ} \mathbf{V}$$

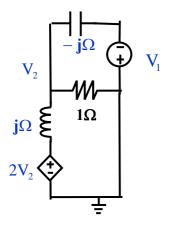
$$\mathbf{I} = 30\angle -45^{\circ} \mathbf{A}$$

$$(5)$$



3

3. In the circuit, if $V_1(t) = 4\cos(1kt)V$, find $V_2(t)$. The voltage controlled voltage source is in volt and equal to $2V_2(t)$. Hint: apply KCL. (20)



$$V_1(t) = 4\cos(1kt)V \qquad \implies \qquad 4\angle 0^{\circ} V \tag{2}$$

$$\frac{2\mathbf{V}_2 - \mathbf{V}_2}{\mathbf{j}\Omega} = \frac{\mathbf{V}_2}{1\Omega} + \frac{\mathbf{V}_2 + 4}{-\mathbf{j}\Omega}$$

$$2\mathbf{V}_2 - \mathbf{V}_2 = \mathbf{j}\mathbf{V}_2 - (\mathbf{V}_2 + 4)$$
(7)

$$2\mathbf{v}_2 - \mathbf{v}_2 - \mathbf{j}\mathbf{v}_2 - (\mathbf{v}_2 + \mathbf{4})$$

$$2\mathbf{V}_2 = \mathbf{j}\mathbf{V}_2 - 4$$

$$\therefore \mathbf{V}_2 = \frac{-4}{2 - \mathbf{j}} = \frac{-4 \angle 0^{\circ}}{\sqrt{5} \angle -26.6^{\circ}}$$
 (7)

$$V_2 = \frac{-4}{\sqrt{5}} \angle 26.6^{\circ}$$
 (2)

:
$$V_2(t) = \frac{-4}{\sqrt{5}} \cos(1kt + 26.6^{\circ})V$$
 (2)

$$\frac{-4+4(2-\mathbf{j})}{(2-\mathbf{j})^*-\mathbf{j}} + \frac{4-4\mathbf{j}}{2-\mathbf{j}} = \frac{4+4\mathbf{j}}{2-\mathbf{j}}$$

$$\frac{-4}{(2-\mathbf{j})^*\mathbf{j}} = \frac{-4}{1+2\mathbf{j}}$$

$$\frac{-4}{(2-\mathbf{j})^*\mathbf{j}} = \frac{-4}{1+2\mathbf{j}}$$

$$\frac{-8}{2-\mathbf{j}}$$

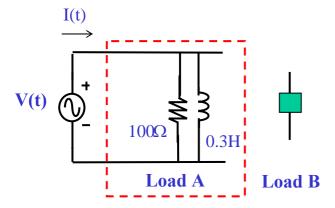
4. Load A is connected to V(t) as shown. $V(t) = 200\sqrt{2}\cos(2\pi50t)V$

(a) Show that the power absorbed by load A is 400W. Find also the power stored by load A.

(b) Show that the power supplied by V(t) is roughly 583VA. Find also the power factor of load A. (25)

4. (c) Show that $I(t) \cong 4.1\cos(2\pi 50t + 47^{\circ})A$

(d) If load B is connected in parallel to load A such that the power factor of the combined load is 1, find the element and value of load B. Show also new $I(t) \cong 2.8 \cos(2\pi 50t)A$. (25)



4a

power absorbed by load A = P (2)

$$\mathbf{P} = \frac{\mathbf{V}^2}{\mathbf{R}} = \frac{200\mathbf{V_{rms}}^2}{100\Omega} = 400\mathbf{W}$$
 (4)

power stored by load A = Q (2)

$$Q = \frac{V^2}{\omega L} = \frac{200V_{rms}^2}{2\pi (50Hz)0.3H} \approx 424.4VAR(L)$$
 (5)

4b

power supplied by v(t) = S (2)

$$\therefore S = \sqrt{P^2 + Q^2} \cong \sqrt{400^2 + 424.4^2} \cong 583.2VA$$
 (4)

power factor of load A = PF

:. PF =
$$\frac{P}{S} = \frac{400}{583.2} \approx 0.686$$
 lagging (6)

4c

∴
$$\theta \cong \cos^{-1} 0.686 \cong 46.7^{\circ}$$
 (4)

$$\mathbf{I} = \frac{\mathbf{S}}{\mathbf{V}} = \frac{583.2\mathbf{V}\mathbf{A}}{200\mathbf{V}_{\text{rms}}} \cong 2.92\mathbf{A}_{\text{rms}} \qquad (6)$$

$$I(t) \approx 2.92\sqrt{2}\cos(2\pi 50t - 46.7^{\circ}) A$$

4d

load B is capacitance

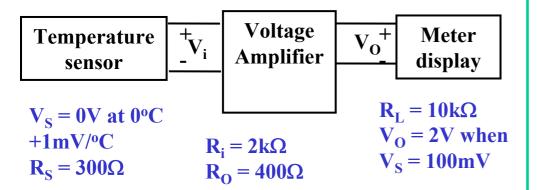
$$\mathbf{Q} = \mathbf{V}^2 \mathbf{\omega} \mathbf{C}$$

$$\therefore \mathbf{C} = \frac{\mathbf{Q}}{\mathbf{V}^2 \mathbf{\omega}} = \frac{424.4 \mathbf{V} \mathbf{A} \mathbf{R}}{200^2 (2\pi 50)} \cong 33.8 \mu \mathbf{F}$$
(9)

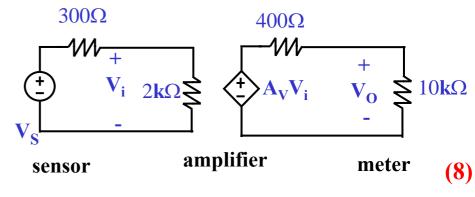
$$\mathbf{I} = \frac{\mathbf{V}}{\mathbf{R}} = \frac{200\mathbf{V}_{\text{rms}}}{100\Omega} = 2\mathbf{A}_{\text{rms}}$$
 (6)

$$I(t) = 2\sqrt{2}\cos(2\pi 50t) A$$

7. A voltage amplifier is used to amplifier the temperature sensor signal (0 to 100mV) to drive the meter display (0 to 2V) as shown. Draw the <u>circuit model</u> and then find the voltage gain of the voltage amplifier. (22).



Circuit Model



Use voltage divider

$$\mathbf{V_o} = \mathbf{A_V} * \mathbf{V_i} * \frac{10\mathbf{k}\Omega}{10\mathbf{k}\Omega + 400\Omega}$$

$$= \mathbf{A_V} * \mathbf{V_S} * \frac{2\mathbf{k}\Omega}{2\mathbf{k}\Omega + 300\Omega} * \frac{10\mathbf{k}\Omega}{10\mathbf{k}\Omega + 400\Omega}$$
(8)

$$2\mathbf{V} = \mathbf{A}_{\mathbf{V}} * 100 \mathbf{m} \mathbf{V} * \frac{2\mathbf{k}\Omega}{2.3\mathbf{k}\Omega} * \frac{10\mathbf{k}\Omega}{10.4\mathbf{k}\Omega}$$

$$\therefore \mathbf{A}_{\mathbf{V}} \cong 24 \tag{6}$$

8a. Find V_0 of the 741 op amp. (10)

8a

999mV
$$V_0$$
 741 op amp
1000mV $A = 200k$

$$V_0 = A * Vi = A * (V_+ - V_-)$$

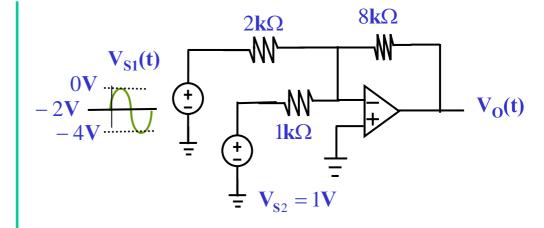
= 200k * (999mV - 1000mV) = -200V (7)

$$V_0 < -15V \Rightarrow \text{op amp saturates}$$

 $\Rightarrow V_0 \cong -15V$ (3)

8b

8b. Plot $V_0(t)$. Assume ideal op amp. (18)



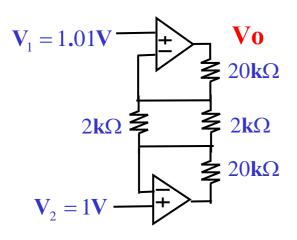
$$V_{o}(t) \cong -\frac{R_{2}}{R_{S1}}V_{S1} - \frac{R_{2}}{R_{S2}}V_{S2}$$
 (8)

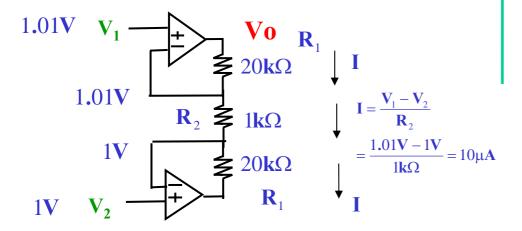
$$= -\frac{8\mathbf{k}\Omega}{2\mathbf{k}\Omega}\mathbf{V}_{S1}(\mathbf{t}) - \frac{8\mathbf{k}\Omega}{1\mathbf{k}\Omega}\mathbf{V}_{S2}$$
 (2)

$$= -4V_{S1}(t) - 8V (2)$$

$$\mathbf{V_{O}(t)}$$
 $0V$ (6)

9a. Find Vo. Assume ideal op amp. (18)



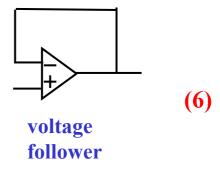


$$V_0 = V_1 + I * 20k\Omega = 1.01V + 10\mu A * 20k\Omega$$

= 1.01V + 0.2V = 1.21V (18)

9b

Draw the circuit of an op amp <u>voltage follower</u> and name two advantages of the circuit. (12)



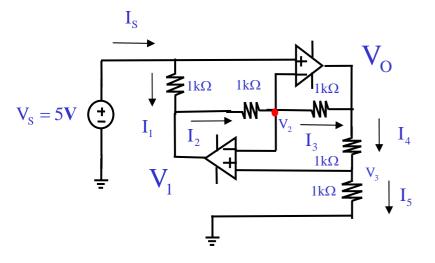
(6)

- 1. Very high input resistance
- 2. Very low output resistance

10

10. Find V_0 and I_S .

Assume ideal op amp. (28)

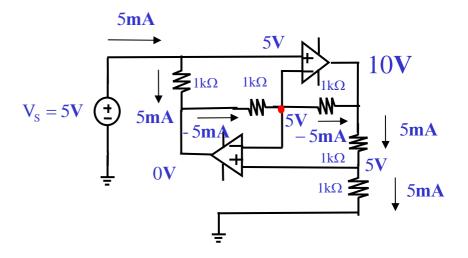


$$V_2 = 5V$$
 (3)
 $V_3 = 5V$ (3)
 $I_5 = 5mA$ (3)
 $I_4 = 5mA$ (3)
 $V_0 = V_3 + I_4 * 1k\Omega = 5V + 5mA * 1k\Omega = 10V$ (4)
 $I_3 = -5mA$ (3)
 $I_2 = -5mA$ (3)

 $I_1 = 5mA$

 $\therefore \mathbf{V}_1 = 0\mathbf{V}$

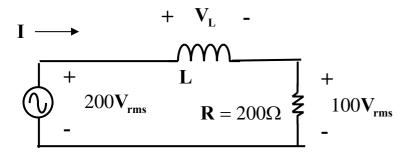
 $I_S = 5mA$



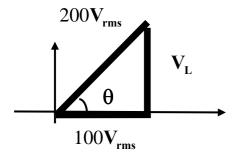
(3)

11a

11a. Find V_L and I. (12)



$$200\mathbf{V}_{rms} \angle \theta = \mathbf{I}(\mathbf{R} + \mathbf{j}\omega \mathbf{L}) = 100\mathbf{V}_{rms} + \mathbf{j}\mathbf{V}_{\mathbf{L}}$$



$$V_{L} = \sqrt{200V_{rms}^{2} - 100V_{rms}^{2}}$$

$$\approx 173V_{rms}$$
(9)

$$I = \frac{100V_{\rm rms}}{200O} = 0.5A_{\rm rms}$$
 (3)

11b

11b. In the circuit, X is an unknown element. . (22)

- (i) If $V_m = 10V$, $I_m = 2A$, $\theta = \phi = 45^{\circ}$, find X in Ω , power factor of X, and power absorbed by X.
- (ii) If $V_m = 8V$, $I_m = 4A$, $\theta = 0^{\circ}$, $\phi = 90^{\circ}$, find X in Ω , power factor of X, and power absorbed by X.

$$\mathbf{v}(\mathbf{t}) = \mathbf{V}_{\mathbf{m}} \cos(\omega \mathbf{t} + \phi)$$

$$+$$

$$-$$

$$\frac{\mathbf{i}(\mathbf{t}) = \mathbf{I}_{\mathbf{m}} \cos(\omega \mathbf{t} + \phi)}{\mathbf{X}}$$

$$\mathbf{X} = \mathbf{R} = \frac{\mathbf{V_m}}{\mathbf{I_m}} = \frac{10\mathbf{V}}{2\mathbf{A}} = 5\Omega \tag{3}$$

$$\mathbf{PF} = 1 \tag{3}$$

$$P_{R} = I^{2} * R = (\frac{4A}{\sqrt{2}})^{2} * 5\Omega = 40W$$
 (4)

$$\mathbf{X} = \mathbf{C} = -\mathbf{j}2\Omega \tag{5}$$

$$\mathbf{PF} = 0 \tag{3}$$

$$\mathbf{P} = 0\mathbf{W} \tag{4}$$