

Understanding GloVe (Global Vectors for Word Representation)

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CS 747

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2. GloVe model
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1. Introduction

- **The statistics of word occurrences** in a corpus is the primary source of information available to all unsupervised methods for learning word representations.
- Although many such methods now exist, the question still remains as to **how meaning is generated from these statistics**, and **how the resulting word vectors might represent that meaning**.

1. Introduction

- Recent methods for learning vector space representations of words have succeeded in capturing fine-grained semantic and syntactic regularities using vector arithmetic,
- But the origin of these regularities has remained opaque.

1. Introduction

- Matrix Factorization Methods : methods that reduce a matrix into constituent parts that make it easier to calculate more complex matrix operations .
- Shallow Window-Based Methods: Another approach is to learn word representations that aid in making predictions within local context windows.

1. Introduction : pros & cons

Count based vs direct prediction

LSA, HAL (Lund & Burgess),
COALS (Rohde et al),
Hellinger-PCA (Lebret & Collobert)

- Fast training
- Efficient usage of statistics
- Primarily used to capture word similarity
- Disproportionate importance given to large counts

NNLM, HLBL, RNN, Skip-gram/
CBOW, (Bengio et al; Collobert & Weston;
Huang et al; Mnih & Hinton; Mikolov et al;
Mnih & Kavukcuoglu)

- Scales with corpus size
- Inefficient usage of statistics
- Generate improved performance on other tasks
- Can capture complex patterns beyond word similarity

2. GloVe model

- Combines the advantages of the two major model families in the literature:
 - global matrix factorization and,
 - local context window methods
- Our model efficiently leverages statistical information by training only on the nonzero elements in a word–word co–occurrence matrix, rather than on the entire sparse matrix or on individual context windows in a large corpus.

Matrix of word-word co-occurrence counts

- I like deep learning.
- I like NLP.
- I enjoy flying.

counts	I	like	enjoy	deep	learning	NLP	flying	.
I	0	2	1	0	0	0	0	0
like	2	0	0	1	0	1	0	0
enjoy	1	0	0	0	0	0	1	0
deep	0	1	0	0	1	0	0	0
learning	0	0	0	1	0	0	0	1
NLP	0	1	0	0	0	0	0	1
flying	0	0	1	0	0	0	0	1
.	0	0	0	0	1	1	1	0

3. GloVe cost function

$$J = \sum_{i,j=1}^V f(X_{ij}) (w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij})^2$$

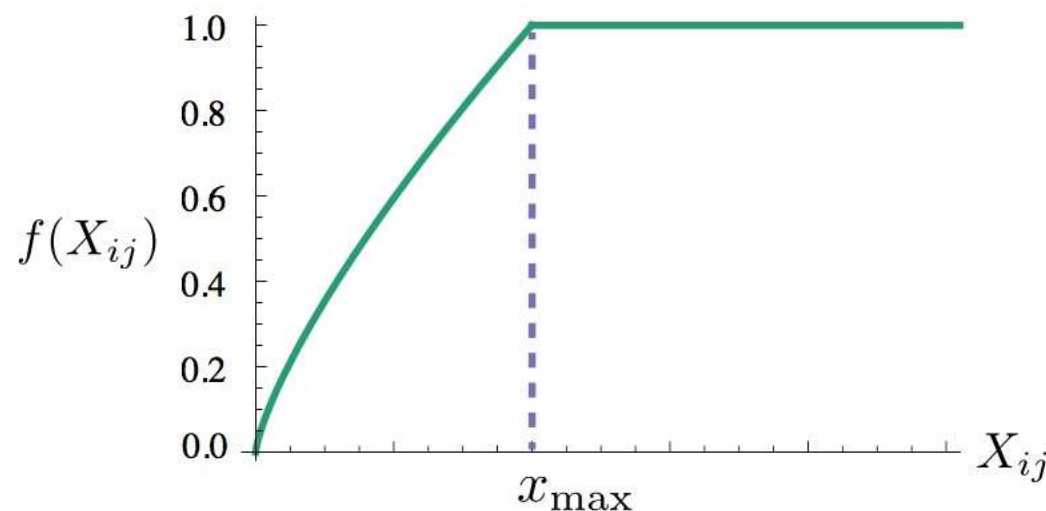


Figure 1: Weighting function f with $\alpha = 3/4$.

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flying	0	0	1	0	0	0	0	1
.	0	0	0	0	1	1	1	0

3. GloVe cost function

Probability and Ratio	$k = \text{solid}$	$k = \text{gas}$	$k = \text{water}$	$k = \text{fashion}$
$P(k \text{ice})$	1.9×10^{-4}	6.6×10^{-5}	3.0×10^{-3}	1.7×10^{-5}
$P(k \text{steam})$	2.2×10^{-5}	7.8×10^{-4}	2.2×10^{-3}	1.8×10^{-5}
$P(k \text{ice})/P(k \text{steam})$	8.9	8.5×10^{-2}	1.36	0.96

- Deriving the Cost Function
 - The above argument suggests that the appropriate starting point for word vector learning should be with **ratios of co-occurrence probabilities** rather than the **probabilities themselves**.

3. GloVe cost function

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- Establish some notations
 - let the matrix of word–word co–occurrence counts be denoted by X ,
 - whose entries X_{ij} tabulate the number of times word j occurs in the context of word i
 - let $X_i = \sum_k X_{ik}$ be the number of times any word appears in the context of word i
 - let $P_{ij} = P(i|j) = X_{ij}/X_i$ be the probability that word j appear in the context of word i

3. GloVe cost function

- Deriving the Cost Function
 - set a function F that represents **ratios of co-occurrence probabilities** rather than the probabilities themselves

$$F(w_i, w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}, \quad (1)$$

✓ Note that w_i and \tilde{w}_k are vectors from different vector-spaces

- we would like F to **encode the information** present in the ratio P_{ik}/P_{jk} **in the word vector space**. Since vector spaces are **inherently linear structures**, the most natural way to do this is **with vector differences**.

$$F(w_i - w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}. \quad (2)$$

3. GloVe cost function

- Deriving the Cost Function
 - We note that the arguments of F in Eqn. (2) are **vectors** while the right-hand side is a **scalar**.
 - While F could be taken to be a **complicated function** parameterized by, e.g., a neural network, doing so would **obfuscate the linear structure** we are trying to capture.
 - To avoid this issue, we can first take the **dot product** of the arguments, which prevents F from mixing the vector dimensions in undesirable ways.

$$F \left((w_i - w_j)^T \tilde{w}_k \right) = \frac{P_{ik}}{P_{jk}}, \quad (3)$$

3. GloVe cost function

- Deriving the Cost Function
 - for word–word co–occurrence matrices, the distinction between **a word** and **a context word** is arbitrary and that we are **free to exchange** the two roles.
 - **the symmetry** can be restored in two steps.
 - **First**, we require that F be a **homomorphism** between the groups $(\mathbb{R}, +)$ and $(\mathbb{R} > 0, \times)$, i.e.,

$$F \left((w_i - w_j)^T \tilde{w}_k \right) = \frac{F(w_i^T \tilde{w}_k)}{F(w_j^T \tilde{w}_k)}, \quad (4)$$

- which, by Eqn. (3), is solved by,

$$F(w_i^T \tilde{w}_k) = P_{ik} = \frac{X_{ik}}{X_i}. \quad (5)$$

3. GloVe cost function : homomorphism

Homomorphisms

$$G \quad *$$

$$x, y \in G$$

$$f: G \rightarrow H$$

$$H \quad \diamond$$

$$x * y = z$$

$$x \mapsto f(x)$$

$$y \mapsto f(y)$$

$$z \mapsto f(z)$$

$$x * y = z \Rightarrow f(x) \diamond f(y) = f(z)$$

$$\Rightarrow f(x) \diamond f(y) = f(x * y)$$

3. GloVe cost function : homomorphism

Example 1

$G = \mathbb{R}$ under +
abelian, identity = 0

$H = \mathbb{R}^+$ under \times
abelian, identity = 1

$f: G \rightarrow H$
 $x \mapsto e^x$

$f(x+y) = f(x) \times f(y)$
 $e^{x+y} = e^x \times e^y \quad \checkmark$

Homo (same)
+
Morph (shape)

3. GloVe cost function

- Deriving the Cost Function
 - The solution to Eqn. (4) is $F = \exp$ or,

$$w_i^T \tilde{w}_k = \log(P_{ik}) = \log(X_{ik}) - \log(X_i) . \quad (6)$$

- Next, we note that Eqn. (6) would exhibit the **exchange symmetry if not for the $\log(X_i)$** on the right-hand side.
- However, this term is independent of k so it can be absorbed into a bias b_i for w_i .
- Finally, adding an additional bias \tilde{b}_i for \tilde{w}_i **restores the symmetry**.

$$w_i^T \tilde{w}_k + b_i + \tilde{b}_k = \log(X_{ik}) . \quad (7)$$

3. GloVe cost function : weighting function

- Deriving the Cost Function

$$J = \sum_{i,j=1}^V f(X_{ij}) \left(w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij} \right)^2, \quad (8)$$

1. $f(0) = 0$. If f is viewed as a continuous function, it should vanish as $x \rightarrow 0$ fast enough that the $\lim_{x \rightarrow 0} f(x) \log^2 x$ is finite.
2. $f(x)$ should be non-decreasing so that rare co-occurrences are not overweighted.
3. $f(x)$ should be relatively small for large values of x , so that frequent co-occurrences are not overweighted.

3. GloVe cost function : weighting function

- Deriving the Cost Function

$$f(x) = \begin{cases} (x/x_{\max})^\alpha & \text{if } x < x_{\max} \\ 1 & \text{otherwise} \end{cases} \quad (9)$$

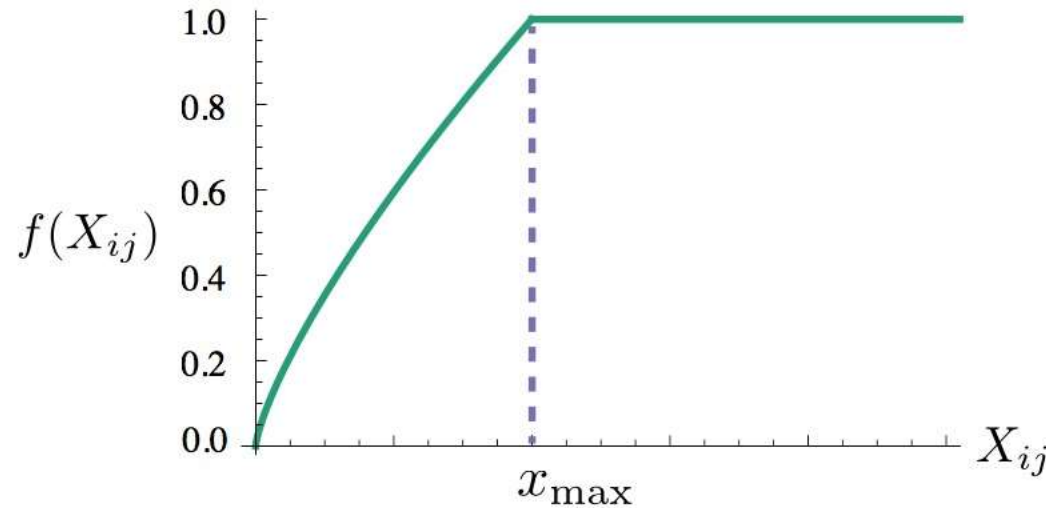


Figure 1: Weighting function f with $\alpha = 3/4$.

4. Experiments & Results

- Experiments
 - Word analogy
 - Word similarity
 - Named entity recognition (NER)
- Result

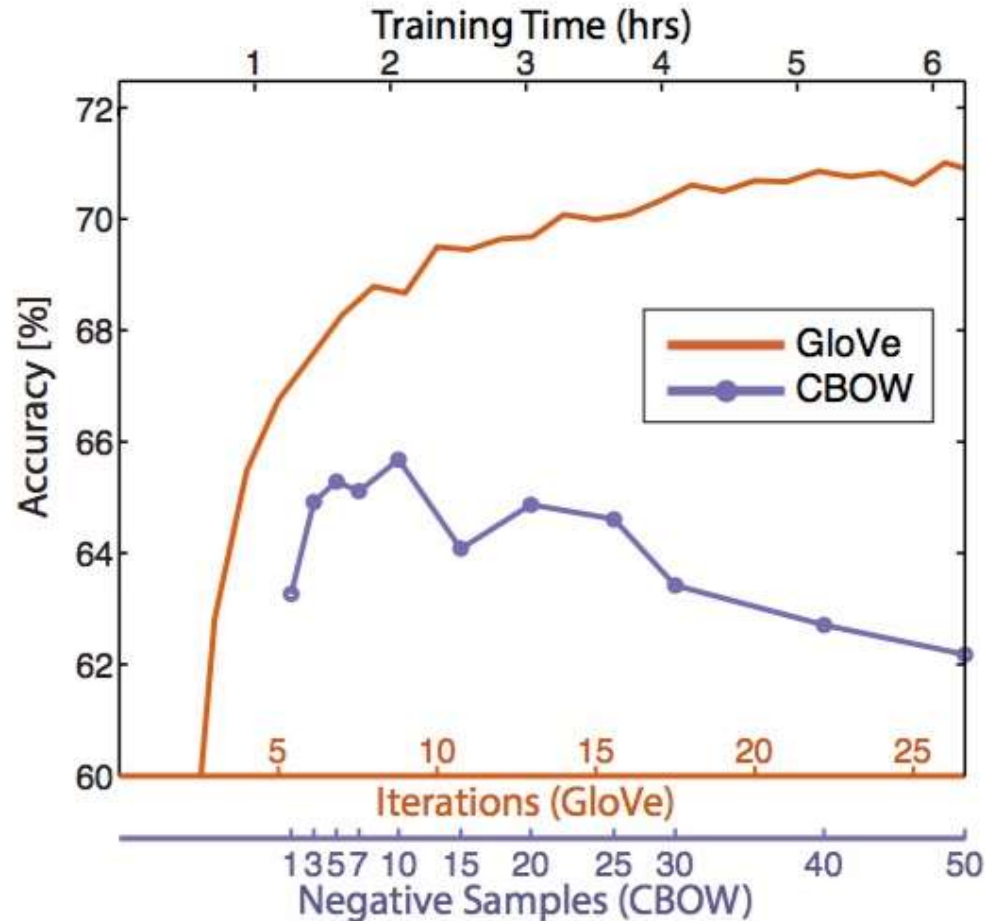
4. Experiments : analogy task

- The word analogy task consists of questions like, “a is to b as c is to ____?”
- The semantic questions, like “Athens is to Greece as Berlin is to ____?”.
- The syntactic questions like, “dance is to dancing as fly is to ____?”

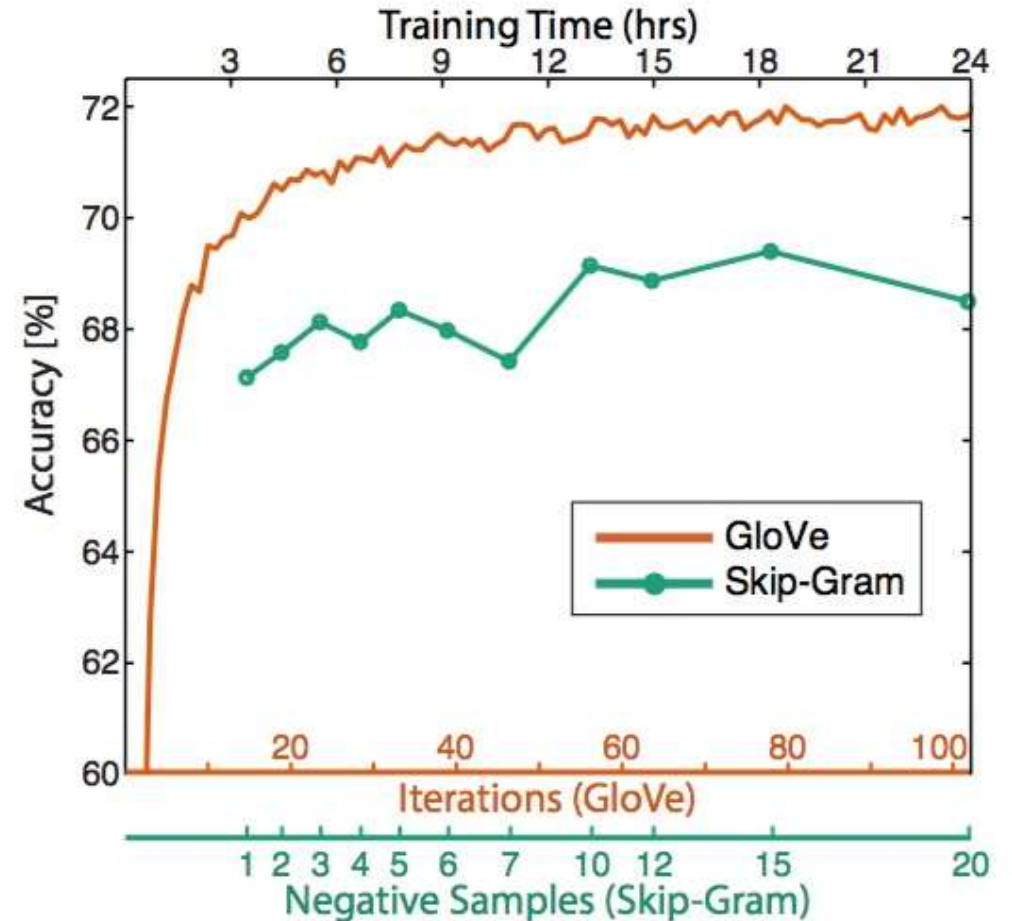
4. Experiments : analogy task

Model	Dim.	Size	Sem.	Syn.	Tot.
ivLBL	100	1.5B	55.9	50.1	53.2
HPCA	100	1.6B	4.2	16.4	10.8
GloVe	100	1.6B	<u>67.5</u>	<u>54.3</u>	<u>60.3</u>
SG	300	1B	61	61	61
CBOW	300	1.6B	16.1	52.6	36.1
vLBL	300	1.5B	54.2	<u>64.8</u>	60.0
ivLBL	300	1.5B	65.2	63.0	64.0
GloVe	300	1.6B	<u>80.8</u>	61.5	<u>70.3</u>
SVD	300	6B	6.3	8.1	7.3
SVD-S	300	6B	36.7	46.6	42.1
SVD-L	300	6B	56.6	63.0	60.1
CBOW [†]	300	6B	63.6	<u>67.4</u>	65.7
SG [†]	300	6B	73.0	<u>66.0</u>	69.1
GloVe	300	6B	<u>77.4</u>	67.0	<u>71.7</u>
CBOW	1000	6B	57.3	68.9	63.7
SG	1000	6B	66.1	65.1	65.6
SVD-L	300	42B	38.4	58.2	49.2
GloVe	300	42B	<u>81.9</u>	<u>69.3</u>	<u>75.0</u>

4. Experiments : analogy task



(a) GloVe vs CBOW



(b) GloVe vs Skip-Gram

4. Experiments : similarity task

- A similarity score is obtained from the word vectors by first normalizing each feature across the vocabulary and then calculating the cosine similarity.
- We compute Spearman's rank correlation coefficient between this score and the human judgments.

4. Experiments : similarity task

Glove results

Nearest words to
frog:

1. frogs
2. toad
3. litoria
4. leptodactylidae
5. rana
6. lizard
7. eleutherodactylus



litoria



leptodactylidae



rana



eleutherodactylus

4. Experiments : similarity task

Model	Size	WS353	MC	RG	SCWS	RW
SVD	6B	35.3	35.1	42.5	38.3	25.6
SVD-S	6B	56.5	71.5	71.0	53.6	34.7
SVD-L	6B	65.7	<u>72.7</u>	75.1	56.5	37.0
CBOW [†]	6B	57.2	65.6	68.2	57.0	32.5
SG [†]	6B	62.8	65.2	69.7	<u>58.1</u>	37.2
GloVe	6B	<u>65.8</u>	<u>72.7</u>	<u>77.8</u>	53.9	<u>38.1</u>
SVD-L	42B	74.0	76.4	74.1	58.3	39.9
GloVe	42B	<u>75.9</u>	<u>83.6</u>	<u>82.9</u>	<u>59.6</u>	<u>47.8</u>
CBOW*	100B	68.4	79.6	75.4	59.4	45.5

4. Experiments : NER task

- The CoNLL–2003 English benchmark dataset for NER is a collection of documents from Reuters newswire articles, annotated with four entity types:
 - Person
 - Location
 - Organization
 - Miscellaneous
- We train models on CoNLL–03 training data on test on three datasets:
 - 1) ConLL–03 testing data
 - 2) ACE Phase 2 (2001–02) and ACE–2003 data
 - 3) MUC7 Formal Run test set.

4. Experiments : NER task

Model	Dev	Test	ACE	MUC7
Discrete	91.0	85.4	77.4	73.4
SVD	90.8	85.7	77.3	73.7
SVD-S	91.0	85.5	77.6	74.3
SVD-L	90.5	84.8	73.6	71.5
HPCA	92.6	88.7	81.7	80.7
HSMN	90.5	85.7	78.7	74.7
CW	92.2	87.4	81.7	80.2
CBOW	93.1	88.2	82.2	81.1
GloVe	93.2	88.3	82.9	82.2

4. Result

- GloVe, is a new global log–bilinear regression model for the unsupervised learning of word representations that outperforms other models on word analogy, word similarity, and named entity recognition tasks.

5. References

- GloVe
 - <https://nlp.stanford.edu/projects/glove/>
- Stanford NLP lecture
 - <http://web.stanford.edu/class/cs224n/>
 - <https://www.youtube.com/watch?v=ASn7ExxLZws&t=43s>
- Socratica's video about homomorphism
 - <https://www.youtube.com/watch?v=cYzp5lWqCsg>

