

Planar data classification with one hidden layer

Welcome to your week 3 programming assignment. It's time to build your first neural network, which will have a hidden layer. You will see a big difference between this model and the one you implemented using logistic regression.

You will learn how to:

- Implement a 2-class classification neural network with a single hidden layer
- Use units with a non-linear activation function, such as tanh
- Compute the cross entropy loss
- Implement forward and backward propagation

1 - Packages

Let's first import all the packages that you will need during this assignment.

- [numpy](http://www.numpy.org) (www.numpy.org) is the fundamental package for scientific computing with Python.
- [sklearn](http://scikit-learn.org/stable/) (<http://scikit-learn.org/stable/>) provides simple and efficient tools for data mining and data analysis.
- [matplotlib](http://matplotlib.org) (<http://matplotlib.org>) is a library for plotting graphs in Python.
- testCases provides some test examples to assess the correctness of your functions
- planar_utils provide various useful functions used in this assignment

```
In [1]: # Package imports
import numpy as np
import matplotlib.pyplot as plt
from testCases_v2 import *
import sklearn
import sklearn.datasets
import sklearn.linear_model
from planar_utils import plot_decision_boundary, sigmoid, load_planar_dataset,
load_extra_datasets

%matplotlib inline

np.random.seed(1) # set a seed so that the results are consistent
```

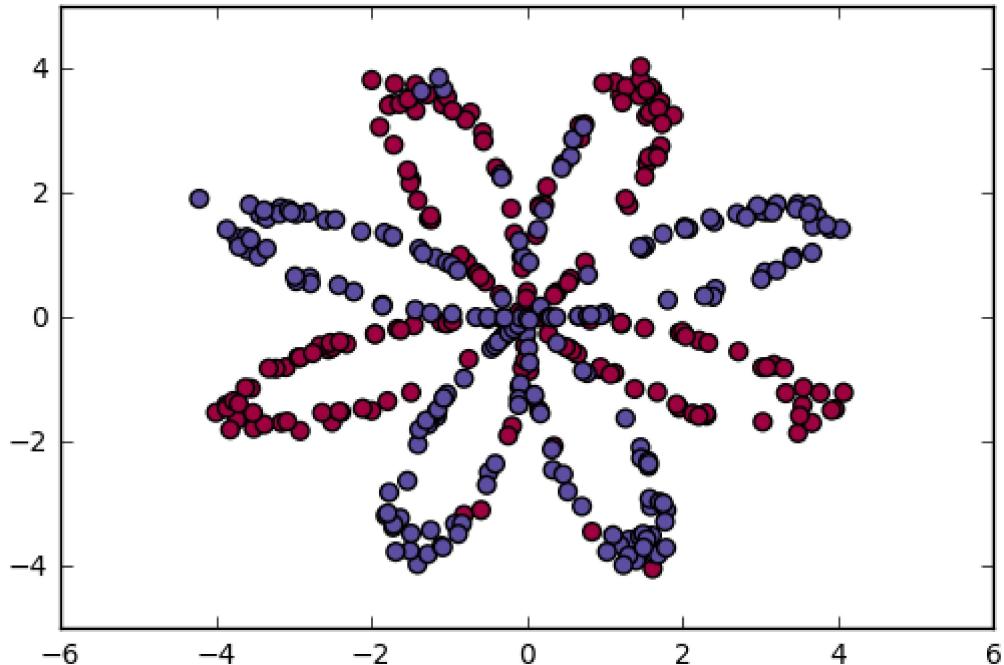
2 - Dataset

First, let's get the dataset you will work on. The following code will load a "flower" 2-class dataset into variables X and Y.

```
In [2]: X, Y = load_planar_dataset()
```

Visualize the dataset using matplotlib. The data looks like a "flower" with some red (label $y=0$) and some blue ($y=1$) points. Your goal is to build a model to fit this data.

```
In [3]: # Visualize the data:  
plt.scatter(X[0, :], X[1, :], c=Y, s=40, cmap=plt.cm.Spectral);
```



You have:

- a numpy-array (matrix) X that contains your features (x_1, x_2)
- a numpy-array (vector) Y that contains your labels (red:0, blue:1).

Lets first get a better sense of what our data is like.

Exercise: How many training examples do you have? In addition, what is the shape of the variables X and Y ?

Hint: How do you get the shape of a numpy array? ([help](#))

(<https://docs.scipy.org/doc/numpy/reference/generated/numpy.ndarray.shape.html>)

```
In [5]: ### START CODE HERE ### (≈ 3 Lines of code)
shape_X = np.shape(X)
shape_Y = np.shape(Y)
m = shape_X[1] # training set size
### END CODE HERE ###

print ('The shape of X is: ' + str(shape_X))
print ('The shape of Y is: ' + str(shape_Y))
print ('I have m = %d training examples!' % (m))
```

```
The shape of X is: (2, 400)
The shape of Y is: (1, 400)
I have m = 400 training examples!
```

Expected Output:

shape of X	(2, 400)
shape of Y	(1, 400)
m	400

3 - Simple Logistic Regression

Before building a full neural network, lets first see how logistic regression performs on this problem. You can use sklearn's built-in functions to do that. Run the code below to train a logistic regression classifier on the dataset.

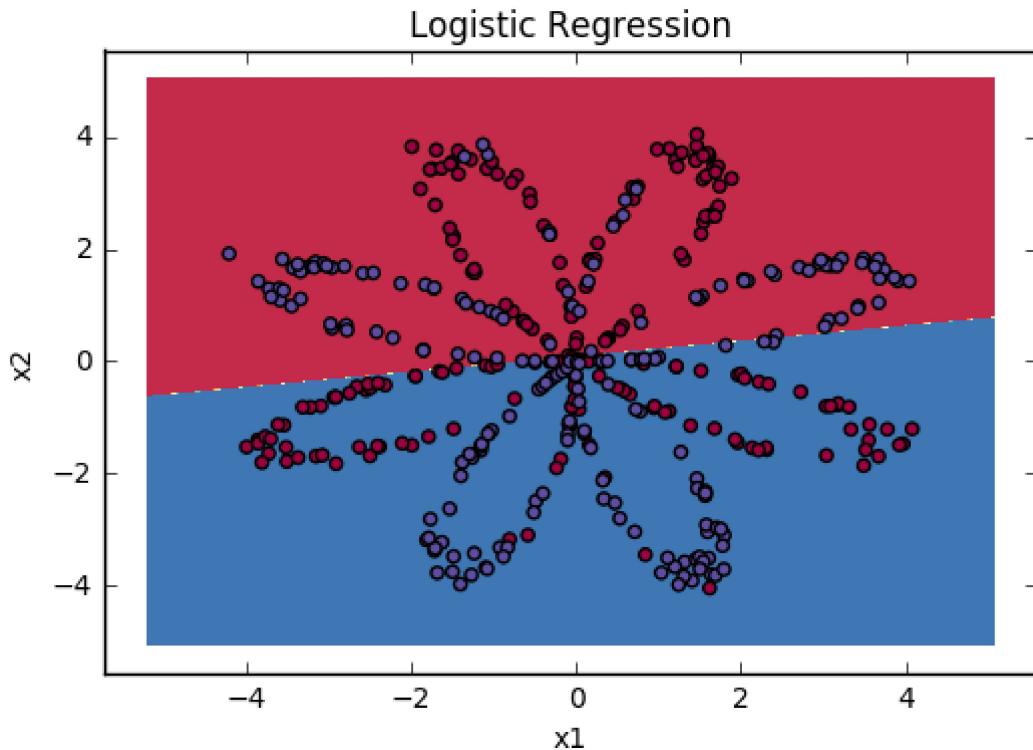
```
In [7]: # Train the Logistic regression classifier
clf = sklearn.linear_model.LogisticRegressionCV();
clf.fit(X.T, Y.T);
```

You can now plot the decision boundary of these models. Run the code below.

```
In [8]: # Plot the decision boundary for logistic regression
plot_decision_boundary(lambda x: clf.predict(x), X, Y)
plt.title("Logistic Regression")

# Print accuracy
LR_predictions = clf.predict(X.T)
print ('Accuracy of logistic regression: %d ' % float((np.dot(Y,LR_predictions) + np.dot(1-Y,1-LR_predictions))/float(Y.size)*100) +
      '% ' + "(percentage of correctly labelled datapoints)")
```

Accuracy of logistic regression: 47 % (percentage of correctly labelled datapoints)



Expected Output:

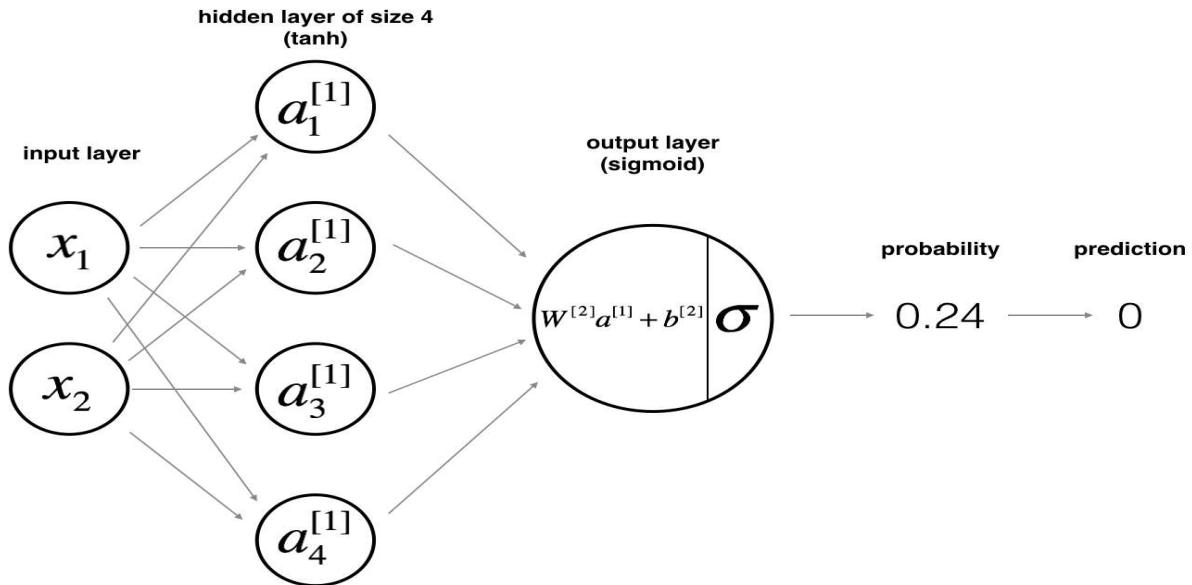
Accuracy	47%
--------------	-----

Interpretation: The dataset is not linearly separable, so logistic regression doesn't perform well. Hopefully a neural network will do better. Let's try this now!

4 - Neural Network model

Logistic regression did not work well on the "flower dataset". You are going to train a Neural Network with a single hidden layer.

Here is our model:



Mathematically:

For one example $x^{(i)}$:

$$z^{[1](i)} = W^{[1]} x^{(i)} + b^{[1]} \quad (1)$$

$$a^{[1](i)} = \tanh(z^{[1](i)}) \quad (2)$$

$$z^{[2](i)} = W^{[2]} a^{[1](i)} + b^{[2]} \quad (3)$$

$$\hat{y}^{(i)} = a^{[2](i)} = \sigma(z^{[2](i)}) \quad (4)$$

$$y_{\text{prediction}}^{(i)} = \begin{cases} 1 & \text{if } a^{[2](i)} > 0.5 \\ 0 & \text{otherwise} \end{cases} \quad (5)$$

Given the predictions on all the examples, you can also compute the cost J as follows:

$$J = -\frac{1}{m} \sum_{i=0}^m \left(y^{(i)} \log(a^{[2](i)}) + (1 - y^{(i)}) \log(1 - a^{[2](i)}) \right) \quad (6)$$

Reminder: The general methodology to build a Neural Network is to:

1. Define the neural network structure (# of input units, # of hidden units, etc).
2. Initialize the model's parameters
3. Loop:
 - Implement forward propagation
 - Compute loss
 - Implement backward propagation to get the gradients
 - Update parameters (gradient descent)

You often build helper functions to compute steps 1-3 and then merge them into one function we call `nn_model()`. Once you've built `nn_model()` and learnt the right parameters, you can make predictions on new data.

4.1 - Defining the neural network structure

Exercise: Define three variables:

- `n_x`: the size of the input layer
- `n_h`: the size of the hidden layer (set this to 4)
- `n_y`: the size of the output layer

Hint: Use shapes of X and Y to find `n_x` and `n_y`. Also, hard code the hidden layer size to be 4.

```
In [11]: # GRADED FUNCTION: layer_sizes

def layer_sizes(X, Y):
    """
    Arguments:
    X -- input dataset of shape (input size, number of examples)
    Y -- Labels of shape (output size, number of examples)

    Returns:
    n_x -- the size of the input Layer
    n_h -- the size of the hidden Layer
    n_y -- the size of the output Layer
    """
    ### START CODE HERE ### (~ 3 lines of code)
    n_x = X.shape[0] # size of input layer
    n_h = 4
    n_y = Y.shape[0] # size of output layer
    ### END CODE HERE ###
    return (n_x, n_h, n_y)
```

```
In [12]: X_assess, Y_assess = layer_sizes_test_case()
(n_x, n_h, n_y) = layer_sizes(X_assess, Y_assess)
print("The size of the input layer is: n_x = " + str(n_x))
print("The size of the hidden layer is: n_h = " + str(n_h))
print("The size of the output layer is: n_y = " + str(n_y))
```

```
The size of the input layer is: n_x = 5
The size of the hidden layer is: n_h = 4
The size of the output layer is: n_y = 2
```

Expected Output (these are not the sizes you will use for your network, they are just used to assess the function you've just coded).

n_x	5
n_h	4
n_y	2

4.2 - Initialize the model's parameters

Exercise: Implement the function `initialize_parameters()`.

Instructions:

- Make sure your parameters' sizes are right. Refer to the neural network figure above if needed.
- You will initialize the weights matrices with random values.
 - Use: `np.random.randn(a,b) * 0.01` to randomly initialize a matrix of shape (a,b).
- You will initialize the bias vectors as zeros.
 - Use: `np.zeros((a,b))` to initialize a matrix of shape (a,b) with zeros.

```
In [15]: # GRADED FUNCTION: initialize_parameters
```

```
def initialize_parameters(n_x, n_h, n_y):  
    """  
    Argument:  
    n_x -- size of the input layer  
    n_h -- size of the hidden layer  
    n_y -- size of the output layer  
  
    Returns:  
    params -- python dictionary containing your parameters:  
        W1 -- weight matrix of shape (n_h, n_x)  
        b1 -- bias vector of shape (n_h, 1)  
        W2 -- weight matrix of shape (n_y, n_h)  
        b2 -- bias vector of shape (n_y, 1)  
    """  
  
    np.random.seed(2) # we set up a seed so that your output matches ours al  
though the initialization is random.  
  
    ### START CODE HERE ### (~ 4 Lines of code)  
    W1 = np.random.randn(n_h, n_x) * 0.01  
    b1 = np.zeros((n_h, 1))  
    W2 = np.random.randn(n_y, n_h) * 0.01  
    b2 = np.zeros((n_y, 1))  
    ### END CODE HERE ###  
  
    assert (W1.shape == (n_h, n_x))  
    assert (b1.shape == (n_h, 1))  
    assert (W2.shape == (n_y, n_h))  
    assert (b2.shape == (n_y, 1))  
  
    parameters = {"W1": W1,  
                  "b1": b1,  
                  "W2": W2,  
                  "b2": b2}  
  
    return parameters
```

```
In [16]: n_x, n_h, n_y = initialize_parameters_test_case()

parameters = initialize_parameters(n_x, n_h, n_y)
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))

W1 = [[-0.00416758 -0.00056267]
      [-0.02136196  0.01640271]
      [-0.01793436 -0.00841747]
      [ 0.00502881 -0.01245288]]
b1 = [[ 0.]
      [ 0.]
      [ 0.]
      [ 0.]]
W2 = [[-0.01057952 -0.00909008  0.00551454  0.02292208]]
b2 = [[ 0.]]
```

Expected Output:

W1	$\begin{bmatrix} [-0.00416758 \ -0.00056267] & [-0.02136196 \ 0.01640271] & [-0.01793436 \ -0.00841747] & [0.00502881 \ -0.01245288] \end{bmatrix}$
b1	$\begin{bmatrix} [0.] \\ [0.] \\ [0.] \\ [0.] \end{bmatrix}$
W2	$\begin{bmatrix} [-0.01057952 \ -0.00909008 \ 0.00551454 \ 0.02292208] \end{bmatrix}$
b2	$\begin{bmatrix} [0.] \end{bmatrix}$

4.3 - The Loop

Question: Implement forward_propagation().

Instructions:

- Look above at the mathematical representation of your classifier.
- You can use the function `sigmoid()`. It is built-in (imported) in the notebook.
- You can use the function `np.tanh()`. It is part of the numpy library.
- The steps you have to implement are:
 1. Retrieve each parameter from the dictionary "parameters" (which is the output of `initialize_parameters()`) by using `parameters[".."]`.
 2. Implement Forward Propagation. Compute $Z^{[1]}, A^{[1]}, Z^{[2]}$ and $A^{[2]}$ (the vector of all your predictions on all the examples in the training set).
- Values needed in the backpropagation are stored in "cache". The cache will be given as an input to the backpropagation function.

```
In [19]: # GRADED FUNCTION: forward_propagation
```

```
def forward_propagation(X, parameters):
    """
    Argument:
    X -- input data of size (n_x, m)
    parameters -- python dictionary containing your parameters (output of initialization function)

    Returns:
    A2 -- The sigmoid output of the second activation
    cache -- a dictionary containing "Z1", "A1", "Z2" and "A2"
    """
    # Retrieve each parameter from the dictionary "parameters"
    ### START CODE HERE ### (≈ 4 Lines of code)
    W1 = parameters["W1"]
    b1 = parameters["b1"]
    W2 = parameters["W2"]
    b2 = parameters["b2"]
    ### END CODE HERE ###

    # Implement Forward Propagation to calculate A2 (probabilities)
    ### START CODE HERE ### (≈ 4 Lines of code)
    Z1 = np.dot(W1, X) + b1
    A1 = np.tanh(Z1)
    Z2 = np.dot(W2, A1) + b2
    A2 = sigmoid(Z2)
    ### END CODE HERE ###

    assert(A2.shape == (1, X.shape[1]))

    cache = {"Z1": Z1,
              "A1": A1,
              "Z2": Z2,
              "A2": A2}

    return A2, cache
```

```
In [20]: X_assess, parameters = forward_propagation_test_case()
A2, cache = forward_propagation(X_assess, parameters)
```

```
# Note: we use the mean here just to make sure that your output matches ours.
print(np.mean(cache['Z1']), np.mean(cache['A1']), np.mean(cache['Z2']), np.mean(cache['A2']))
```

```
0.262818640198 0.091999045227 -1.30766601287 0.212877681719
```

Expected Output:

0.262818640198 0.091999045227 -1.30766601287 0.212877681719
--

Now that you have computed $A^{[2]}$ (in the Python variable "A2"), which contains $a^{[2](i)}$ for every example, you can compute the cost function as follows:

$$J = -\frac{1}{m} \sum_{i=0}^m \left(y^{(i)} \log(a^{[2](i)}) + (1 - y^{(i)}) \log(1 - a^{[2](i)}) \right) \quad (13)$$

Exercise: Implement `compute_cost()` to compute the value of the cost J .

Instructions:

- There are many ways to implement the cross-entropy loss. To help you, we give you how we would

$$\text{have implemented } - \sum_{i=0}^m y^{(i)} \log(a^{[2](i)}):$$

```
logprobs = np.multiply(np.log(A2), Y)
cost = - np.sum(logprobs) # no need to use a for loop!
```

(you can use either `np.multiply()` and then `np.sum()` or directly `np.dot()`).

In [21]: `# GRADED FUNCTION: compute_cost`

```
def compute_cost(A2, Y, parameters):
    """
    Computes the cross-entropy cost given in equation (13)

    Arguments:
    A2 -- The sigmoid output of the second activation, of shape (1, number of
    examples)
    Y -- "true" labels vector of shape (1, number of examples)
    parameters -- python dictionary containing your parameters W1, b1, W2 and
    b2

    Returns:
    cost -- cross-entropy cost given equation (13)
    """

    m = Y.shape[1] # number of example

    # Compute the cross-entropy cost
    ### START CODE HERE ### (~ 2 lines of code)
    logprobs = np.multiply(np.log(A2), Y) + np.multiply(np.log(1 - A2), (1 - Y))
    cost = np.divide(np.sum(logprobs), -m)
    ### END CODE HERE ###

    cost = np.squeeze(cost) # makes sure cost is the dimension we expect.
                            # E.g., turns [[17]] into 17
    assert(isinstance(cost, float))

    return cost
```

```
In [22]: A2, Y_assess, parameters = compute_cost_test_case()

print("cost = " + str(compute_cost(A2, Y_assess, parameters)))

cost = 0.693058761039
```

Expected Output:

cost	0.693058761...
----------	----------------

Using the cache computed during forward propagation, you can now implement backward propagation.

Question: Implement the function `backward_propagation()`.

Instructions: Backpropagation is usually the hardest (most mathematical) part in deep learning. To help you, here again is the slide from the lecture on backpropagation. You'll want to use the six equations on the right of this slide, since you are building a vectorized implementation.

Summary of gradient descent

$dz^{[2]} = a^{[2]} - y$ $dW^{[2]} = dz^{[2]} a^{[1]T}$ $db^{[2]} = dz^{[2]}$ $dz^{[1]} = W^{[2]T} dz^{[2]} * g^{[1]'}(z^{[1]})$ $dW^{[1]} = dz^{[1]} x^T$ $db^{[1]} = dz^{[1]}$	$dZ^{[2]} = A^{[2]} - Y$ $dW^{[2]} = \frac{1}{m} dZ^{[2]} A^{[1]T}$ $db^{[2]} = \frac{1}{m} np.sum(dZ^{[2]}, axis = 1, keepdims = True)$ $dZ^{[1]} = W^{[2]T} dZ^{[2]} * g^{[1]'}(Z^{[1]})$ $dW^{[1]} = \frac{1}{m} dZ^{[1]} X^T$ $db^{[1]} = \frac{1}{m} np.sum(dZ^{[1]}, axis = 1, keepdims = True)$
--	--

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- Tips:

- To compute dZ_1 you'll need to compute $g^{[1]'}(Z^{[1]})$. Since $g^{[1]}(\cdot)$ is the tanh activation function, if $a = g^{[1]}(z)$ then $g^{[1]'}(z) = 1 - a^2$. So you can compute $g^{[1]'}(Z^{[1]})$ using `(1 - np.power(A1, 2))`.

```
In [31]: # GRADED FUNCTION: backward_propagation
```

```
def backward_propagation(parameters, cache, X, Y):
    """
    Implement the backward propagation using the instructions above.

    Arguments:
    parameters -- python dictionary containing our parameters
    cache -- a dictionary containing "Z1", "A1", "Z2" and "A2".
    X -- input data of shape (2, number of examples)
    Y -- "true" Labels vector of shape (1, number of examples)

    Returns:
    grads -- python dictionary containing your gradients with respect to different parameters
    """
    m = X.shape[1]

    # First, retrieve W1 and W2 from the dictionary "parameters".
    ### START CODE HERE ### (~ 2 lines of code)
    W1 = parameters["W1"]
    W2 = parameters["W2"]
    ### END CODE HERE ###

    # Retrieve also A1 and A2 from dictionary "cache".
    ### START CODE HERE ### (~ 2 lines of code)
    A1 = cache["A1"]
    A2 = cache["A2"]
    ### END CODE HERE ###

    # Backward propagation: calculate dW1, db1, dW2, db2.
    ### START CODE HERE ### (~ 6 lines of code, corresponding to 6 equations on slide above)
    dZ2 = A2 - Y
    dW2 = np.divide(np.dot(dZ2, A1.T), m)
    db2 = np.divide(np.sum(dZ2, axis = 1, keepdims = True), m)
    dZ1 = np.multiply(np.dot(W2.T, dZ2), 1 - np.power(A1, 2))
    dW1 = np.divide(np.dot(dZ1, X.T), m)
    db1 = np.divide(np.sum(dZ1, axis = 1, keepdims = True), m)
    ### END CODE HERE ###

    grads = {"dW1": dW1,
             "db1": db1,
             "dW2": dW2,
             "db2": db2}

    return grads
```

```
In [32]: parameters, cache, X_assess, Y_assess = backward_propagation_test_case()

grads = backward_propagation(parameters, cache, X_assess, Y_assess)
print ("dw1 = " + str(grads["dw1"]))
print ("db1 = " + str(grads["db1"]))
print ("dw2 = " + str(grads["dw2"]))
print ("db2 = " + str(grads["db2"]))

dw1 = [[ 0.00301023 -0.00747267]
[ 0.00257968 -0.00641288]
[-0.00156892  0.003893 ]
[-0.00652037  0.01618243]]
db1 = [[ 0.00176201]
[ 0.00150995]
[-0.00091736]
[-0.00381422]]
dw2 = [[ 0.00078841  0.01765429 -0.00084166 -0.01022527]]
db2 = [[-0.16655712]]
```

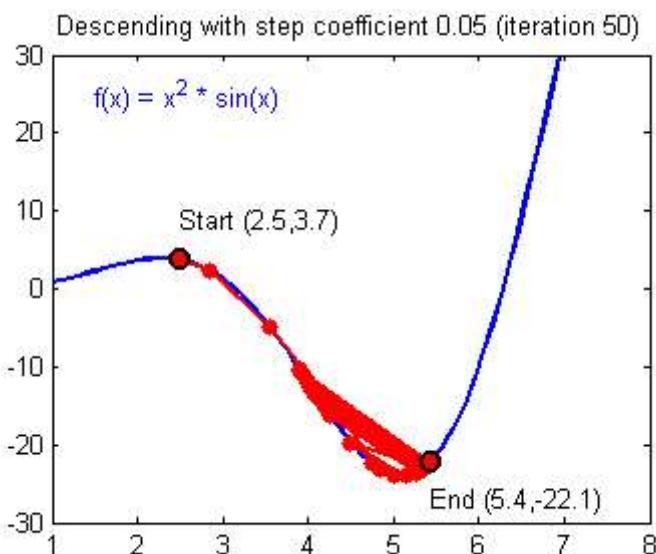
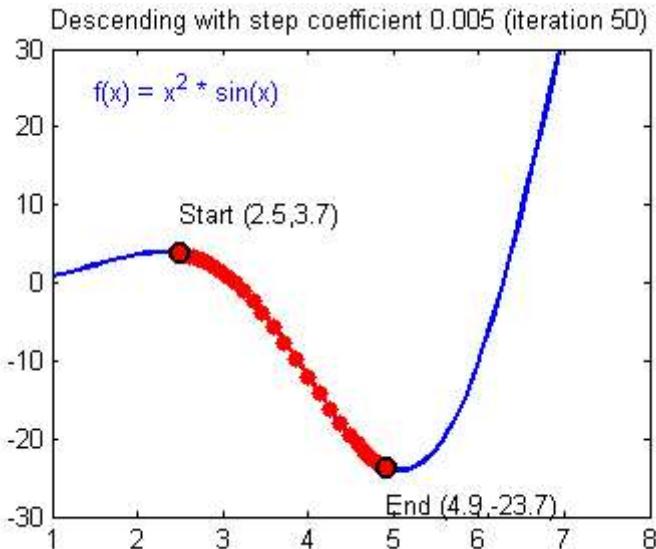
Expected output:

dw1	[[0.00301023 -0.00747267] [0.00257968 -0.00641288] [-0.00156892 0.003893] [-0.00652037 0.01618243]]
db1	[[0.00176201] [0.00150995] [-0.00091736] [-0.00381422]]
dw2	[[0.00078841 0.01765429 -0.00084166 -0.01022527]]
db2	[[-0.16655712]]

Question: Implement the update rule. Use gradient descent. You have to use $(dW1, db1, dW2, db2)$ in order to update $(W1, b1, W2, b2)$.

General gradient descent rule: $\theta = \theta - \alpha \frac{\partial J}{\partial \theta}$ where α is the learning rate and θ represents a parameter.

Illustration: The gradient descent algorithm with a good learning rate (converging) and a bad learning rate (diverging). Images courtesy of Adam Harley.



```
In [33]: # GRADED FUNCTION: update_parameters

def update_parameters(parameters, grads, learning_rate = 1.2):
    """
    Updates parameters using the gradient descent update rule given above

    Arguments:
    parameters -- python dictionary containing your parameters
    grads -- python dictionary containing your gradients

    Returns:
    parameters -- python dictionary containing your updated parameters
    """
    # Retrieve each parameter from the dictionary "parameters"
    ### START CODE HERE ### ( $\approx$  4 Lines of code)
    W1 = parameters["W1"]
    b1 = parameters["b1"]
    W2 = parameters["W2"]
    b2 = parameters["b2"]
    ### END CODE HERE ###

    # Retrieve each gradient from the dictionary "grads"
    ### START CODE HERE ### ( $\approx$  4 Lines of code)
    dW1 = grads["dW1"]
    db1 = grads["db1"]
    dW2 = grads["dW2"]
    db2 = grads["db2"]
    ## END CODE HERE ##

    # Update rule for each parameter
    ### START CODE HERE ### ( $\approx$  4 lines of code)
    W1 = W1 - np.multiply(learning_rate, dW1)
    b1 = b1 - np.multiply(learning_rate, db1)
    W2 = W2 - np.multiply(learning_rate, dW2)
    b2 = b2 - np.multiply(learning_rate, db2)
    ### END CODE HERE ###

    parameters = {"W1": W1,
                  "b1": b1,
                  "W2": W2,
                  "b2": b2}

return parameters
```

```
In [34]: parameters, grads = update_parameters_test_case()
parameters = update_parameters(parameters, grads)

print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))

W1 = [[-0.00643025  0.01936718]
      [-0.02410458  0.03978052]
      [-0.01653973 -0.02096177]
      [ 0.01046864 -0.05990141]]
b1 = [[ -1.02420756e-06]
      [ 1.27373948e-05]
      [ 8.32996807e-07]
      [ -3.20136836e-06]]
W2 = [[-0.01041081 -0.04463285  0.01758031  0.04747113]]
b2 = [[ 0.00010457]]
```

Expected Output:

W1	[[-0.00643025 0.01936718] [-0.02410458 0.03978052] [-0.01653973 -0.02096177] [0.01046864 -0.05990141]]
b1	[[-1.02420756e-06] [1.27373948e-05] [8.32996807e-07] [-3.20136836e-06]]
W2	[[-0.01041081 -0.04463285 0.01758031 0.04747113]]
b2	[[0.00010457]]

4.4 - Integrate parts 4.1, 4.2 and 4.3 in nn_model()

Question: Build your neural network model in nn_model().

Instructions: The neural network model has to use the previous functions in the right order.

```
In [35]: # GRADED FUNCTION: nn_model
```

```
def nn_model(X, Y, n_h, num_iterations = 10000, print_cost=False):
    """
    Arguments:
    X -- dataset of shape (2, number of examples)
    Y -- Labels of shape (1, number of examples)
    n_h -- size of the hidden layer
    num_iterations -- Number of iterations in gradient descent loop
    print_cost -- if True, print the cost every 1000 iterations

    Returns:
    parameters -- parameters learnt by the model. They can then be used to predict.
    """
    np.random.seed(3)
    n_x = layer_sizes(X, Y)[0]
    n_y = layer_sizes(X, Y)[2]

    # Initialize parameters, then retrieve W1, b1, W2, b2. Inputs: "n_x, n_h, n_y".
    # Outputs = "W1, b1, W2, b2, parameters".
    #### START CODE HERE #### (≈ 5 lines of code)
    parameters = initialize_parameters(n_x, n_h, n_y)
    W1 = parameters["W1"]
    b1 = parameters["b1"]
    W2 = parameters["W2"]
    b2 = parameters["b2"]
    #### END CODE HERE ####

    # Loop (gradient descent)

    for i in range(0, num_iterations):

        #### START CODE HERE #### (≈ 4 lines of code)
        # Forward propagation. Inputs: "X, parameters". Outputs: "A2, cache".
        A2, cache = forward_propagation(X, parameters)

        # Cost function. Inputs: "A2, Y, parameters". Outputs: "cost".
        cost = compute_cost(A2, Y, parameters)

        # Backpropagation. Inputs: "parameters, cache, X, Y". Outputs: "grads".
        grads = backward_propagation(parameters, cache, X, Y)

        # Gradient descent parameter update. Inputs: "parameters, grads". Outputs: "parameters".
        parameters = update_parameters(parameters, grads)

        #### END CODE HERE ####

        # Print the cost every 1000 iterations
        if print_cost and i % 1000 == 0:
            print ("Cost after iteration %i: %f" %(i, cost))

    return parameters
```

```
In [36]: X_assess, Y_assess = nn_model_test_case()
parameters = nn_model(X_assess, Y_assess, 4, num_iterations=10000, print_cost=True)
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))

Cost after iteration 0: 0.692739
Cost after iteration 1000: 0.000218
Cost after iteration 2000: 0.000107
Cost after iteration 3000: 0.000071
Cost after iteration 4000: 0.000053
Cost after iteration 5000: 0.000042
Cost after iteration 6000: 0.000035
Cost after iteration 7000: 0.000030
Cost after iteration 8000: 0.000026
Cost after iteration 9000: 0.000023
W1 = [[-0.65848169  1.21866811]
      [-0.76204273  1.39377573]
      [ 0.5792005 -1.10397703]
      [ 0.76773391 -1.41477129]]
b1 = [[ 0.287592 ]
      [ 0.3511264 ]
      [-0.2431246 ]
      [-0.35772805]]
W2 = [[-2.45566237 -3.27042274  2.00784958  3.36773273]]
b2 = [[ 0.20459656]]
```

Expected Output:

cost after iteration 0	0.692739
:	:
W1	$[[-0.65848169 \ 1.21866811] \ [-0.76204273 \ 1.39377573] \ [0.5792005 \ -1.10397703] \ [0.76773391 \ -1.41477129]]$
b1	$[[0.287592] \ [0.3511264] \ [-0.2431246] \ [-0.35772805]]$
W2	$[[-2.45566237 \ -3.27042274 \ 2.00784958 \ 3.36773273]]$
b2	$[[0.20459656]]$

4.5 Predictions

Question: Use your model to predict by building predict(). Use forward propagation to predict results.

Reminder: $\text{predictions} = y_{\text{prediction}} = 1\{\text{activation} > 0.5\} = \begin{cases} 1 & \text{if } \text{activation} > 0.5 \\ 0 & \text{otherwise} \end{cases}$

As an example, if you would like to set the entries of a matrix X to 0 and 1 based on a threshold you would do:
`X_new = (X > threshold)`

```
In [37]: # GRADED FUNCTION: predict

def predict(parameters, X):
    """
    Using the Learned parameters, predicts a class for each example in X

    Arguments:
    parameters -- python dictionary containing your parameters
    X -- input data of size (n_x, m)

    Returns
    predictions -- vector of predictions of our model (red: 0 / blue: 1)
    """

    # Computes probabilities using forward propagation, and classifies to 0/1
    # using 0.5 as the threshold.
    ### START CODE HERE ### (~ 2 lines of code)
    A2, cache = forward_propagation(X, parameters)
    predictions = A2 > 0.5
    ### END CODE HERE ###

    return predictions
```

```
In [38]: parameters, X_assess = predict_test_case()

predictions = predict(parameters, X_assess)
print("predictions mean = " + str(np.mean(predictions)))

predictions mean = 0.666666666667
```

Expected Output:

predictions mean	0.666666666667
----------------------	----------------

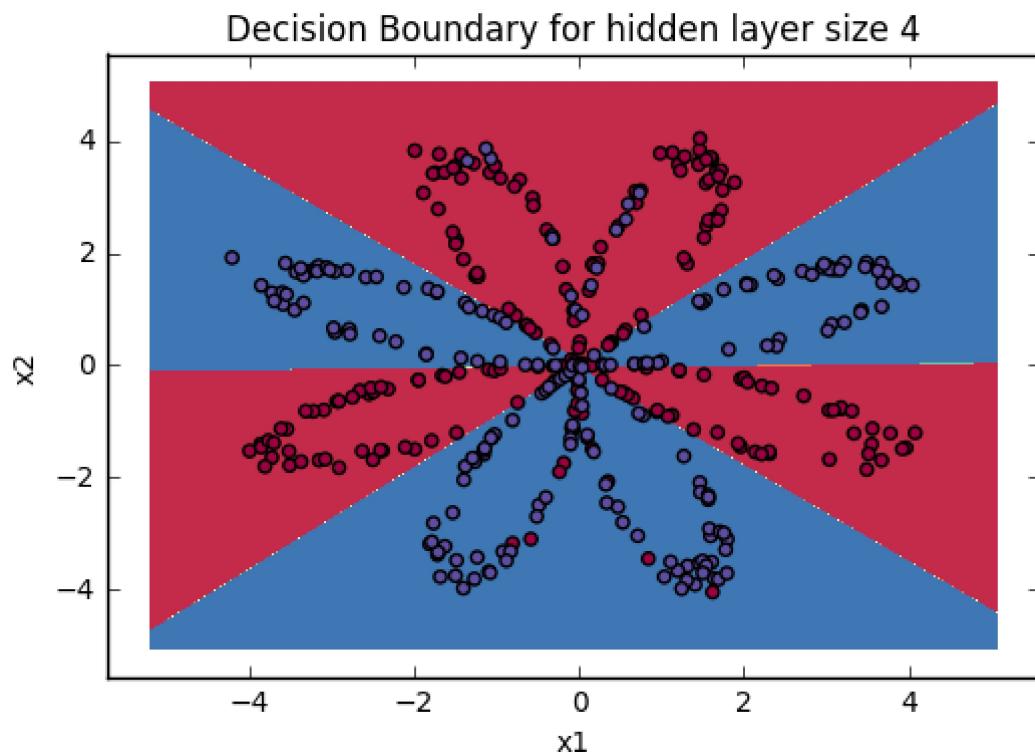
It is time to run the model and see how it performs on a planar dataset. Run the following code to test your model with a single hidden layer of n_h hidden units.

```
In [39]: # Build a model with a n_h-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 4, num_iterations = 10000, print_cost=True)

# Plot the decision boundary
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(4))
```

Cost after iteration 0: 0.693048
 Cost after iteration 1000: 0.288083
 Cost after iteration 2000: 0.254385
 Cost after iteration 3000: 0.233864
 Cost after iteration 4000: 0.226792
 Cost after iteration 5000: 0.222644
 Cost after iteration 6000: 0.219731
 Cost after iteration 7000: 0.217504
 Cost after iteration 8000: 0.219471
 Cost after iteration 9000: 0.218612

Out[39]: <matplotlib.text.Text at 0x7fa92af48ba8>



Expected Output:

Cost after iteration 9000	0.218607
-------------------------------	----------

```
In [40]: # Print accuracy
predictions = predict(parameters, X)
print ('Accuracy: %d' % float((np.dot(Y,predictions.T) + np.dot(1-Y,1-predictions.T))/float(Y.size)*100) + '%')
```

Accuracy: 90%

Expected Output:

Accuracy	90%
--------------	-----

Accuracy is really high compared to Logistic Regression. The model has learnt the leaf patterns of the flower! Neural networks are able to learn even highly non-linear decision boundaries, unlike logistic regression.

Now, let's try out several hidden layer sizes.

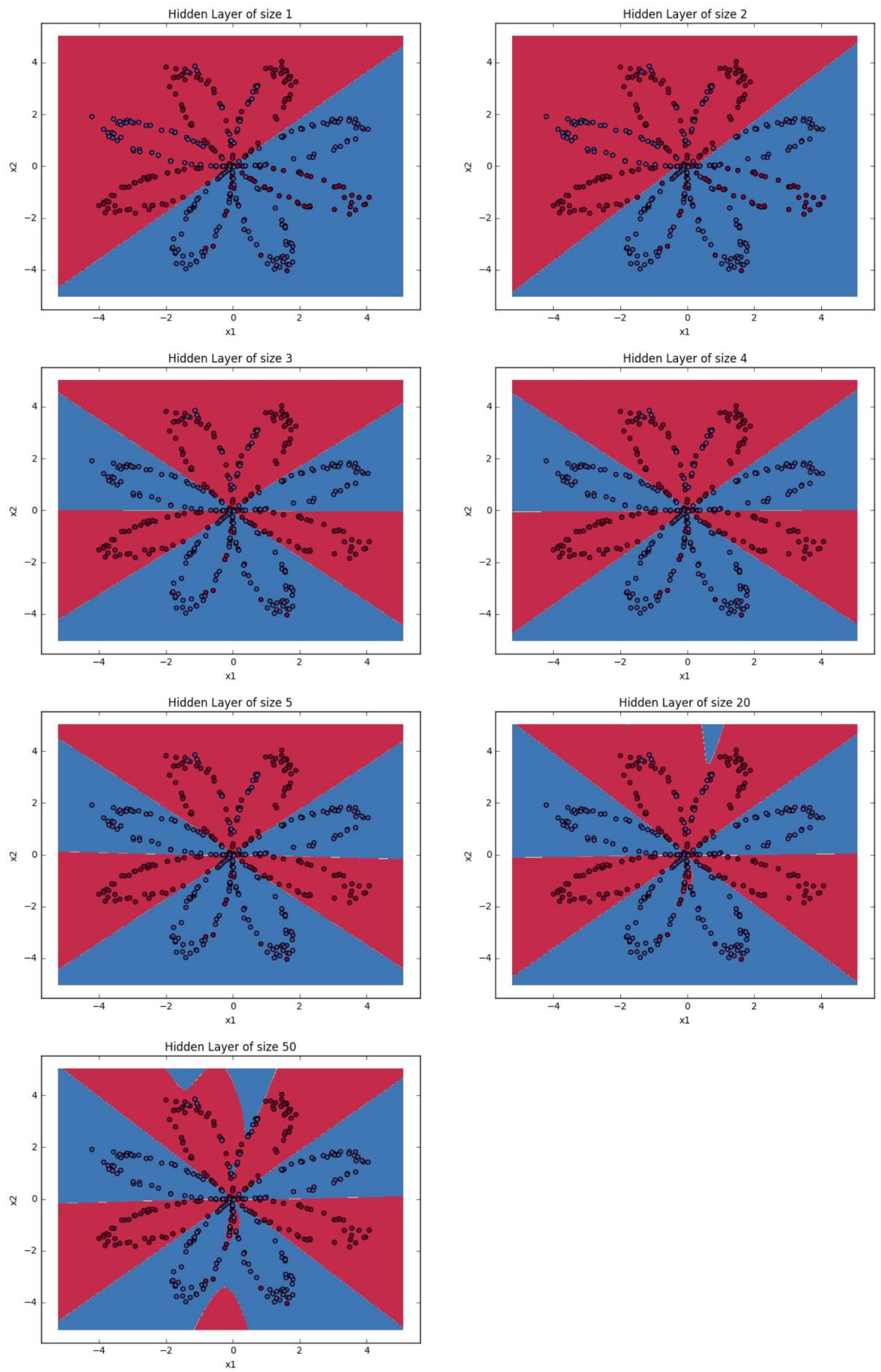
4.6 - Tuning hidden layer size (optional/ungraded exercise)

Run the following code. It may take 1-2 minutes. You will observe different behaviors of the model for various hidden layer sizes.

```
In [41]: # This may take about 2 minutes to run
```

```
plt.figure(figsize=(16, 32))
hidden_layer_sizes = [1, 2, 3, 4, 5, 20, 50]
for i, n_h in enumerate(hidden_layer_sizes):
    plt.subplot(5, 2, i+1)
    plt.title('Hidden Layer of size %d' % n_h)
    parameters = nn_model(X, Y, n_h, num_iterations = 5000)
    plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
    predictions = predict(parameters, X)
    accuracy = float((np.dot(Y,predictions.T) + np.dot(1-Y,1-predictions.T))/float(Y.size)*100)
    print ("Accuracy for {} hidden units: {} %".format(n_h, accuracy))
```

Accuracy for 1 hidden units: 67.5 %
Accuracy for 2 hidden units: 67.25 %
Accuracy for 3 hidden units: 90.75 %
Accuracy for 4 hidden units: 90.5 %
Accuracy for 5 hidden units: 91.25 %
Accuracy for 20 hidden units: 90.0 %
Accuracy for 50 hidden units: 90.25 %



Interpretation:

- The larger models (with more hidden units) are able to fit the training set better, until eventually the largest models overfit the data.
- The best hidden layer size seems to be around $n_h = 5$. Indeed, a value around here seems to fits the data well without also incurring noticeable overfitting.
- You will also learn later about regularization, which lets you use very large models (such as $n_h = 50$) without much overfitting.

Optional questions:

Note: Remember to submit the assignment by clicking the blue "Submit Assignment" button at the upper-right.

Some optional/ungraded questions that you can explore if you wish:

- What happens when you change the tanh activation for a sigmoid activation or a ReLU activation?
- Play with the learning_rate. What happens?
- What if we change the dataset? (See part 5 below!)

You've learnt to:

- Build a complete neural network with a hidden layer
- Make a good use of a non-linear unit
- Implemented forward propagation and backpropagation, and trained a neural network
- See the impact of varying the hidden layer size, including overfitting.

Nice work!

5) Performance on other datasets

If you want, you can rerun the whole notebook (minus the dataset part) for each of the following datasets.

```
In [62]: # Datasets
noisy_circles, noisy_moons, blobs, gaussian_quantiles, no_structure = load_extra_datasets()

datasets = {"noisy_circles": noisy_circles,
            "noisy_moons": noisy_moons,
            "blobs": blobs,
            "gaussian_quantiles": gaussian_quantiles}

### START CODE HERE ### (choose your dataset)
dataset = "noisy_circles"
### END CODE HERE ###

X, Y = datasets[dataset]
X, Y = X.T, Y.reshape(1, Y.shape[0])

# make blobs binary
if dataset == "blobs":
    Y = Y%2

# Visualize the data
plt.figure(0)
plt.scatter(X[0, :], X[1, :], c=Y, s=40, cmap=plt.cm.Spectral);

# Build a model with a 3-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 3, num_iterations = 10000, print_cost=True)

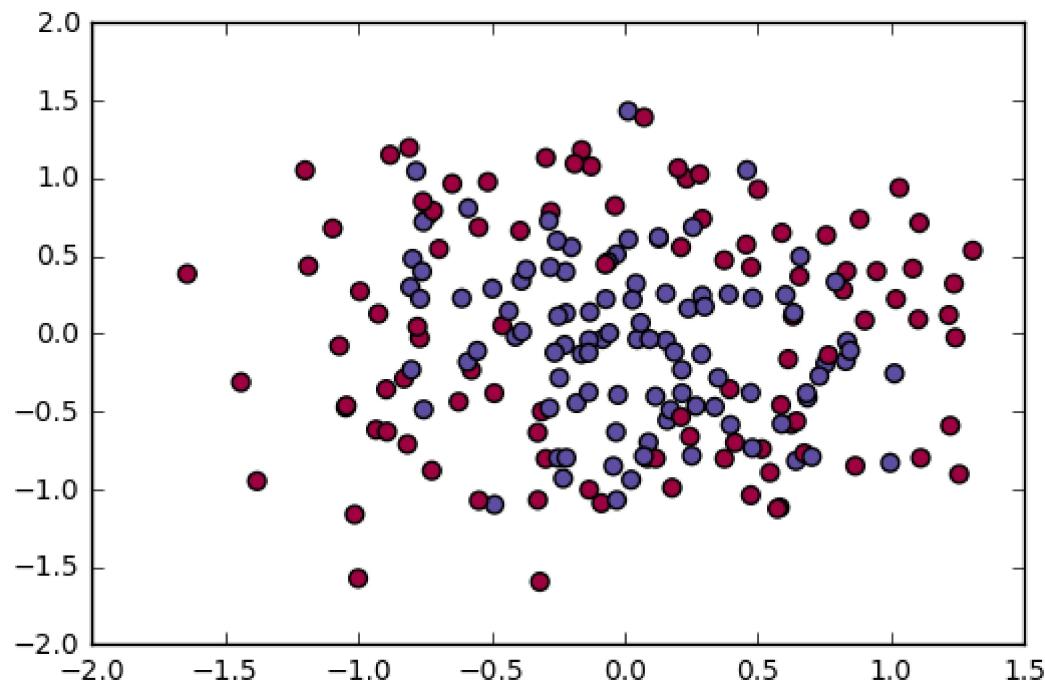
# Plot the decision boundary
plt.figure(1)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(3))

# Build a model with a 4-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 4, num_iterations = 10000, print_cost=True)

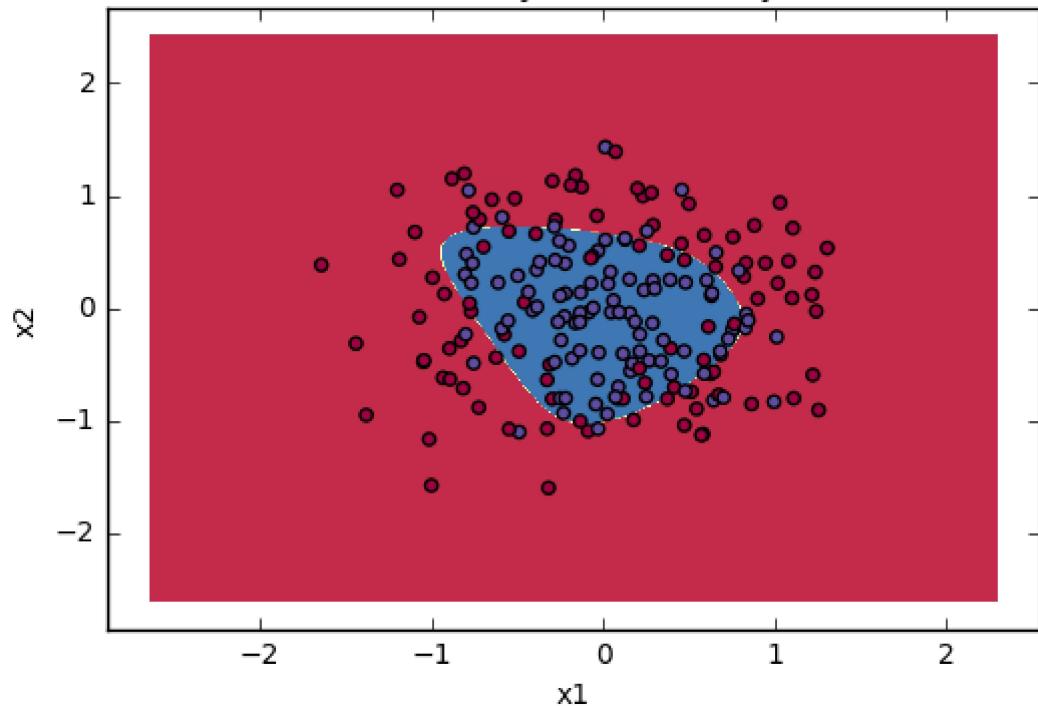
# Plot the decision boundary
plt.figure(2)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(4))
```

```
Cost after iteration 0: 0.693141
Cost after iteration 1000: 0.451286
Cost after iteration 2000: 0.448122
Cost after iteration 3000: 0.450220
Cost after iteration 4000: 0.450317
Cost after iteration 5000: 0.450284
Cost after iteration 6000: 0.450260
Cost after iteration 7000: 0.450244
Cost after iteration 8000: 0.450234
Cost after iteration 9000: 0.450226
Cost after iteration 0: 0.693137
Cost after iteration 1000: 0.450445
Cost after iteration 2000: 0.440800
Cost after iteration 3000: 0.437108
Cost after iteration 4000: 0.435077
Cost after iteration 5000: 0.434131
Cost after iteration 6000: 0.434225
Cost after iteration 7000: 0.433642
Cost after iteration 8000: 0.433534
Cost after iteration 9000: 0.433438
```

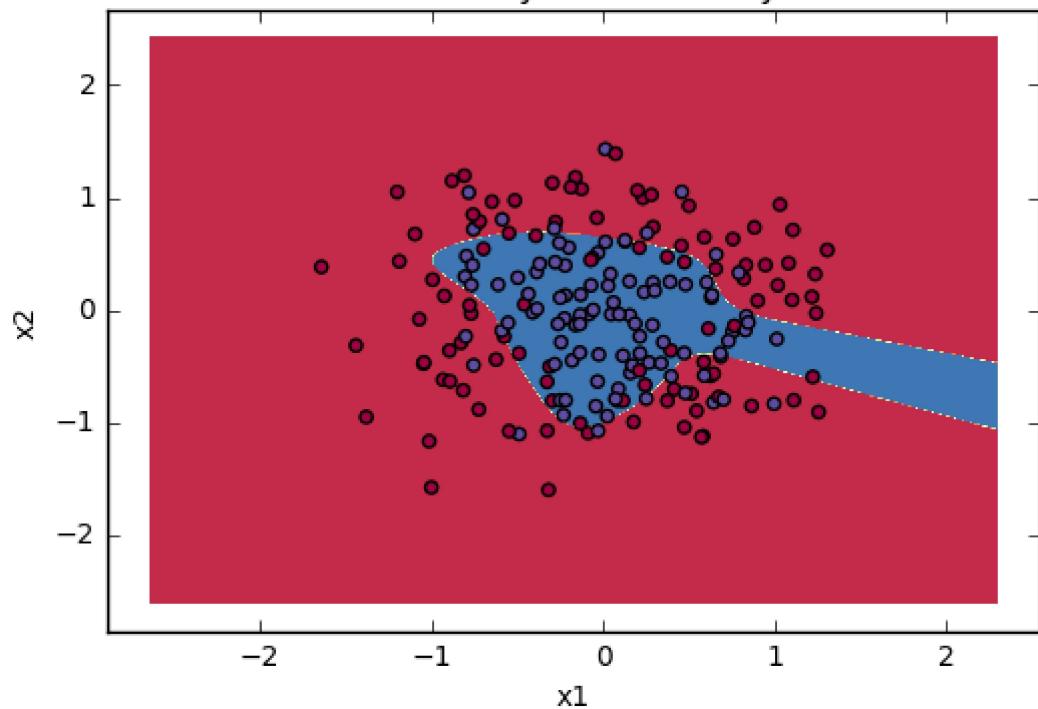
Out[62]: <matplotlib.text.Text at 0x7fa90d081cf8>



Decision Boundary for hidden layer size 3



Decision Boundary for hidden layer size 4



```
In [63]: ### START CODE HERE ### (choose your dataset)
dataset = "noisy_moons"
### END CODE HERE ###

X, Y = datasets[dataset]
X, Y = X.T, Y.reshape(1, Y.shape[0])

# make blobs binary
if dataset == "blobs":
    Y = Y%2

# Visualize the data
plt.figure(0)
plt.scatter(X[0, :], X[1, :], c=Y, s=40, cmap=plt.cm.Spectral);

# Build a model with a 3-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 3, num_iterations = 10000, print_cost=True
)

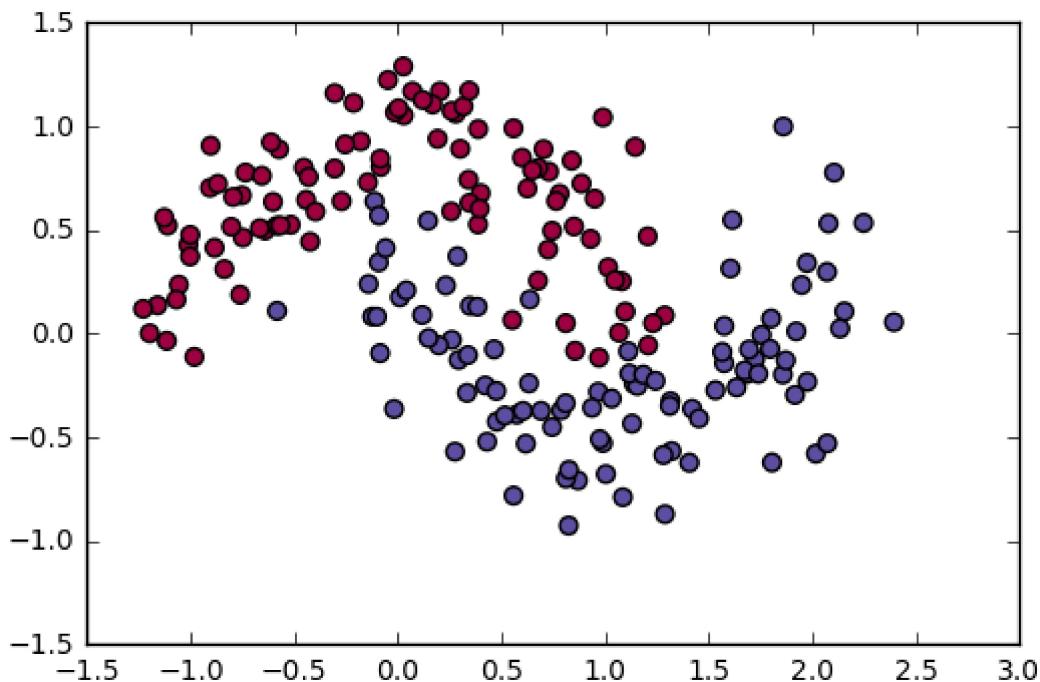
# Plot the decision boundary
plt.figure(1)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(3))

# Build a model with a 4-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 4, num_iterations = 10000, print_cost=True
)

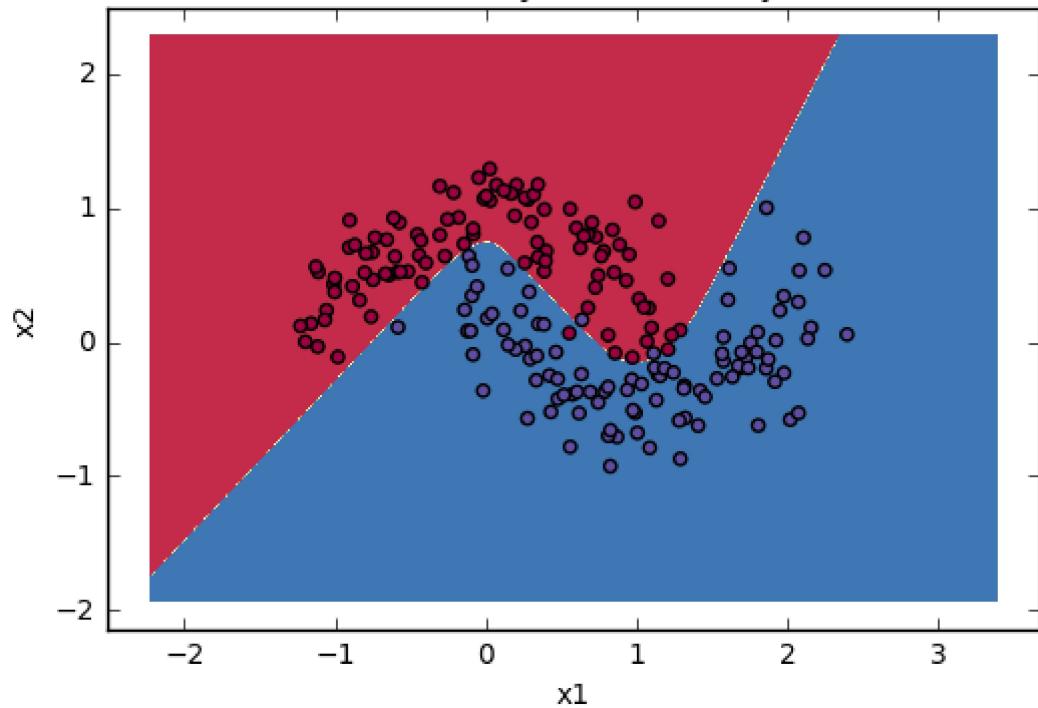
# Plot the decision boundary
plt.figure(2)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(4))
```

```
Cost after iteration 0: 0.693015
Cost after iteration 1000: 0.144005
Cost after iteration 2000: 0.050554
Cost after iteration 3000: 0.046160
Cost after iteration 4000: 0.044290
Cost after iteration 5000: 0.043239
Cost after iteration 6000: 0.042684
Cost after iteration 7000: 0.042363
Cost after iteration 8000: 0.096823
Cost after iteration 9000: 0.042350
Cost after iteration 0: 0.692992
Cost after iteration 1000: 0.057716
Cost after iteration 2000: 0.046927
Cost after iteration 3000: 0.042812
Cost after iteration 4000: 0.040617
Cost after iteration 5000: 0.039348
Cost after iteration 6000: 0.038498
Cost after iteration 7000: 0.037869
Cost after iteration 8000: 0.038560
Cost after iteration 9000: 0.038238
```

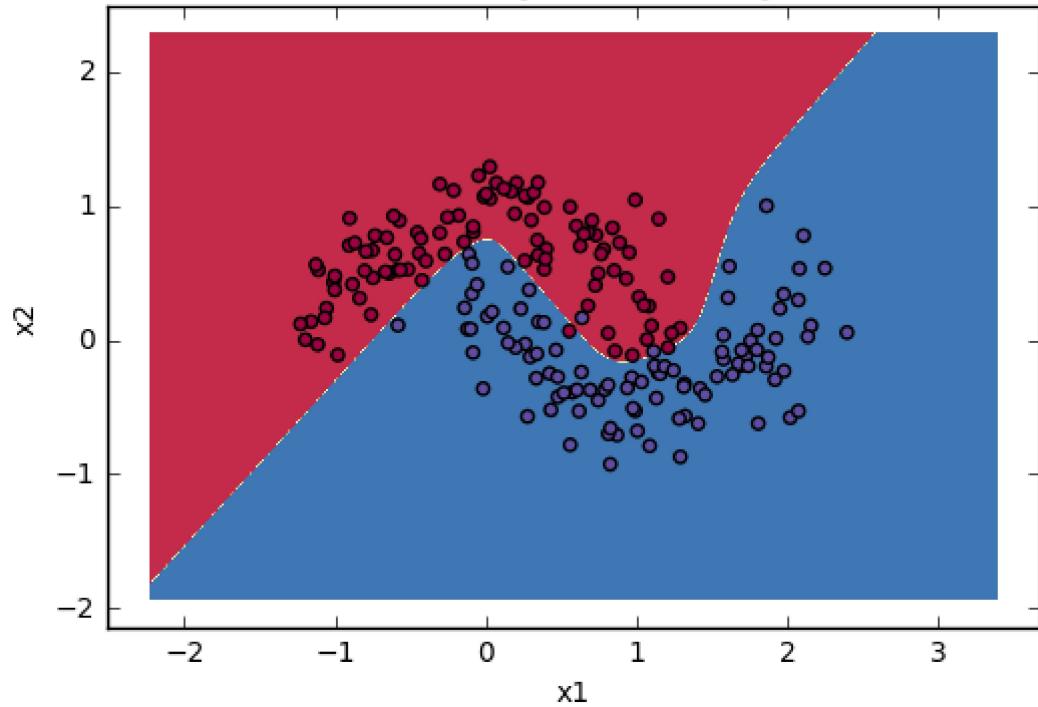
Out[63]: <matplotlib.text.Text at 0x7fa90cf4ca90>



Decision Boundary for hidden layer size 3



Decision Boundary for hidden layer size 4



```
In [66]: ### START CODE HERE ### (choose your dataset)
dataset = "blobs"
### END CODE HERE ###

X, Y = datasets[dataset]
X, Y = X.T, Y.reshape(1, Y.shape[0])

# make blobs binary
if dataset == "blobs":
    Y = Y%2

# Visualize the data
plt.figure(0)
plt.scatter(X[0, :], X[1, :], c=Y, s=40, cmap=plt.cm.Spectral);

# Build a model with a 3-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 3, num_iterations = 10000, print_cost=True
)

# Plot the decision boundary
plt.figure(1)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(3))

# Build a model with a 6-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 6, num_iterations = 10000, print_cost=True
)

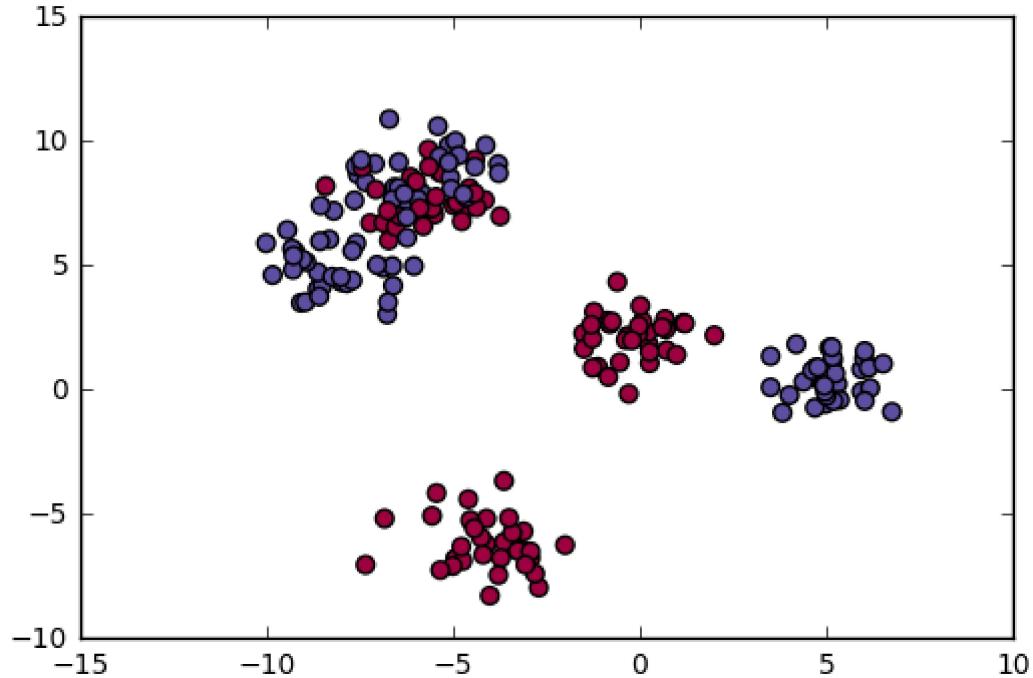
# Plot the decision boundary
plt.figure(2)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(6))

# Build a model with a 8-dimensional hidden layer
#parameters = nn_model(X, Y, n_h = 8, num_iterations = 10000, print_cost=True
)

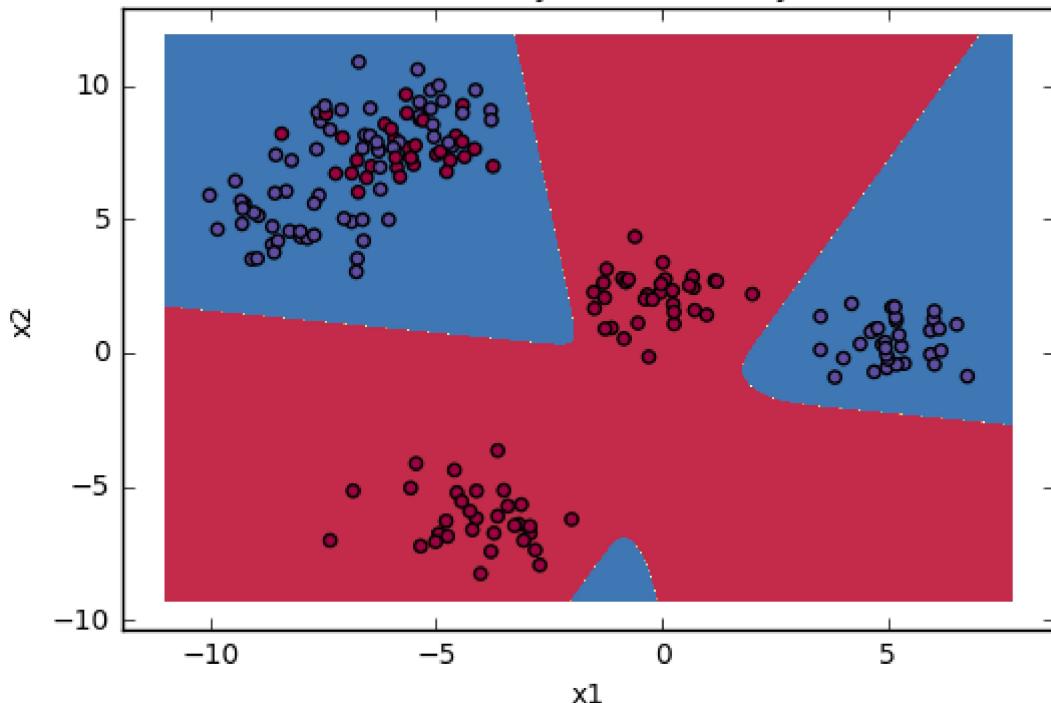
# Plot the decision boundary
#plt.figure(3)
#plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
#plt.title("Decision Boundary for hidden layer size " + str(8))
```

```
Cost after iteration 0: 0.693207
Cost after iteration 1000: 0.324009
Cost after iteration 2000: 0.323587
Cost after iteration 3000: 0.323085
Cost after iteration 4000: 0.322938
Cost after iteration 5000: 0.322860
Cost after iteration 6000: 0.322810
Cost after iteration 7000: 0.322776
Cost after iteration 8000: 0.322751
Cost after iteration 9000: 0.322732
Cost after iteration 0: 0.693030
Cost after iteration 1000: 0.243448
Cost after iteration 2000: 0.235428
Cost after iteration 3000: 0.234879
Cost after iteration 4000: 0.234280
Cost after iteration 5000: 0.235697
Cost after iteration 6000: 0.234654
Cost after iteration 7000: 0.234214
Cost after iteration 8000: 0.233931
Cost after iteration 9000: 0.233723
```

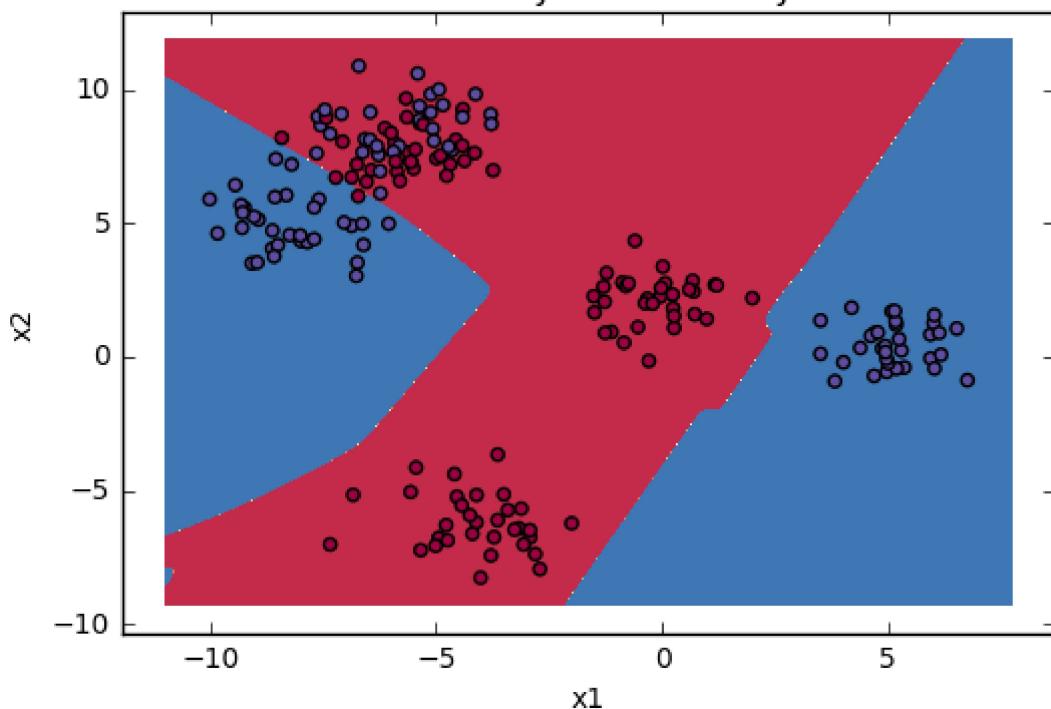
Out[66]: <matplotlib.text.Text at 0x7fa90cdebc50>



Decision Boundary for hidden layer size 3



Decision Boundary for hidden layer size 6



```
In [68]: ### START CODE HERE ### (choose your dataset)
dataset = "gaussian_quantiles"
### END CODE HERE ###

X, Y = datasets[dataset]
X, Y = X.T, Y.reshape(1, Y.shape[0])

# make blobs binary
if dataset == "blobs":
    Y = Y%2

# Visualize the data
plt.figure(0)
plt.scatter(X[0, :], X[1, :], c=Y, s=40, cmap=plt.cm.Spectral);

# Build a model with a 2-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 2, num_iterations = 10000, print_cost=True
)

# Plot the decision boundary
plt.figure(1)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(2))

# Build a model with a 3-dimensional hidden layer
parameters = nn_model(X, Y, n_h = 3, num_iterations = 10000, print_cost=True
)

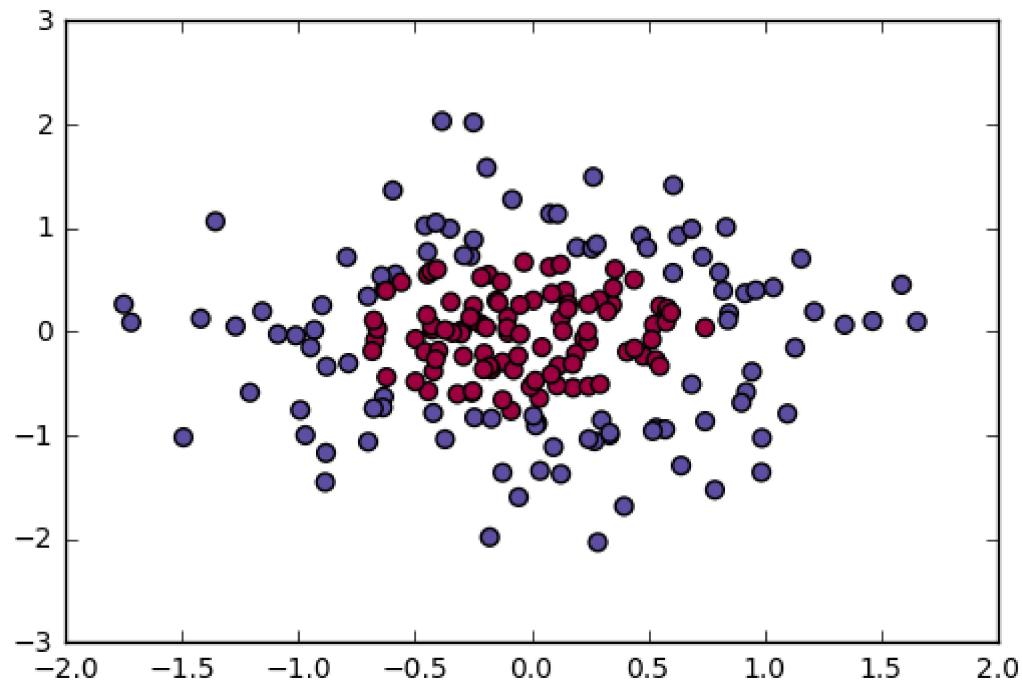
# Plot the decision boundary
plt.figure(2)
plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
plt.title("Decision Boundary for hidden layer size " + str(3))

# Build a model with a 8-dimensional hidden layer
#parameters = nn_model(X, Y, n_h = 8, num_iterations = 10000, print_cost=True
)

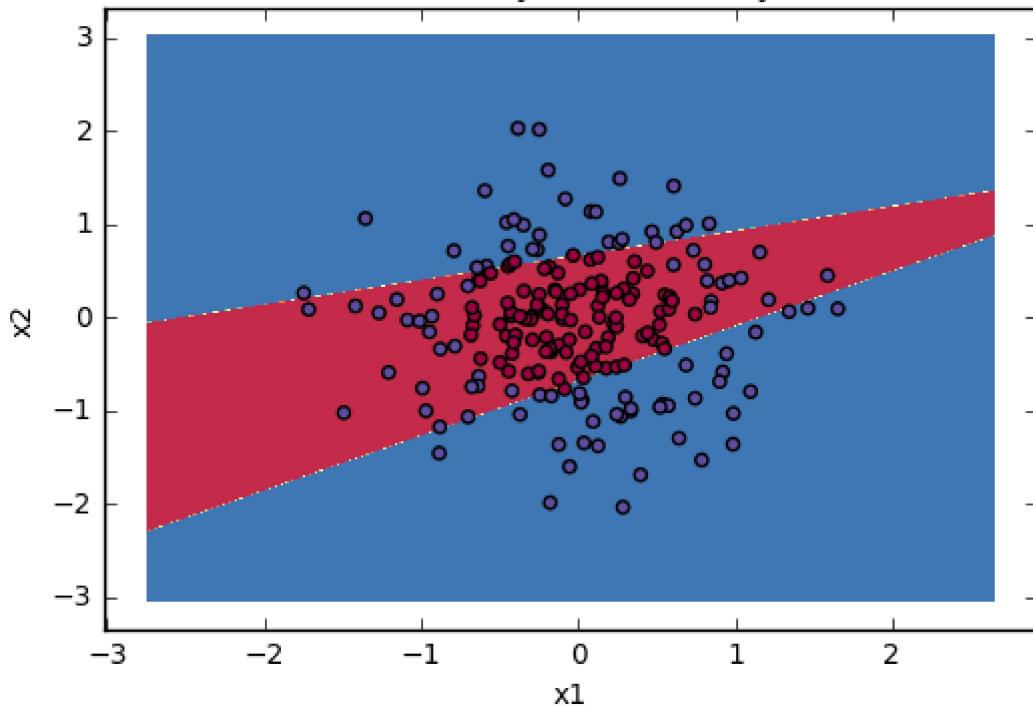
# Plot the decision boundary
#plt.figure(3)
#plot_decision_boundary(lambda x: predict(parameters, x.T), X, Y)
#plt.title("Decision Boundary for hidden layer size " + str(8))
```

```
Cost after iteration 0: 0.693140
Cost after iteration 1000: 0.433512
Cost after iteration 2000: 0.428122
Cost after iteration 3000: 0.424812
Cost after iteration 4000: 0.422405
Cost after iteration 5000: 0.420528
Cost after iteration 6000: 0.419012
Cost after iteration 7000: 0.417768
Cost after iteration 8000: 0.416735
Cost after iteration 9000: 0.415866
Cost after iteration 0: 0.693137
Cost after iteration 1000: 0.106708
Cost after iteration 2000: 0.101721
Cost after iteration 3000: 0.101754
Cost after iteration 4000: 0.100634
Cost after iteration 5000: 0.077337
Cost after iteration 6000: 0.237002
Cost after iteration 7000: 0.166830
Cost after iteration 8000: 0.138285
Cost after iteration 9000: 0.300500
```

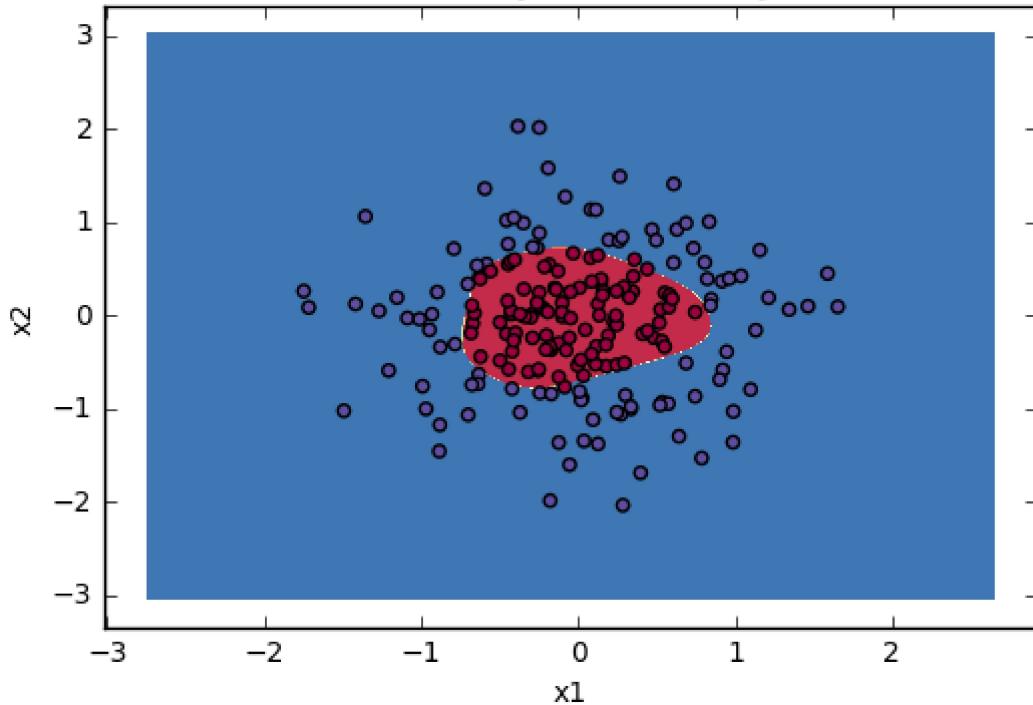
Out[68]: <matplotlib.text.Text at 0x7fa90d103128>



Decision Boundary for hidden layer size 2



Decision Boundary for hidden layer size 3



Congrats on finishing this Programming Assignment!

Reference:

- <http://scs.ryerson.ca/~aharley/neural-networks/> (<http://scs.ryerson.ca/~aharley/neural-networks/>)
- <http://cs231n.github.io/neural-networks-case-study/> (<http://cs231n.github.io/neural-networks-case-study/>)