Selectivity functions that estimate the relation between a variable and its probabilities

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Contents

1 Types 'const', 'full', and 'plat.full'

These relations are the simplest that can be used. While 'const' stands for a constant probability of one for all values of x (Figure 1), the other two have "all-or-nothing" types of probabilities. One or two thresholds (inflection points) need to be defined for types 'full' and 'plat.full'. The main difference between 'full' (Figure 2 & 3) and 'plat.full' (Figure 4, 5 & 6) types are the number of thresholds. For all types, 'plat' stands for "plateau".

const.sel (x)

full.sel (x, infl1, pos=TRUE, lv=0, uv=1)

plat.full.sel (x, infl1, infl2, pos=TRUE, lv=c(0,0), uv=c(1,1))

where x is a numeric vector for which probabilities are estimated, infl1 and infl2 are the inflection points, pos indicates if the trend at the beginning is positive (TRUE) or negative (FALSE), lv defines the lower probability values of the relation, and uv defines the upper probability values of the relation. By default, all fonctions have pos=TRUE, lv=c(0,0), and uv=c(1,1).

Here is an example for 'const' type:
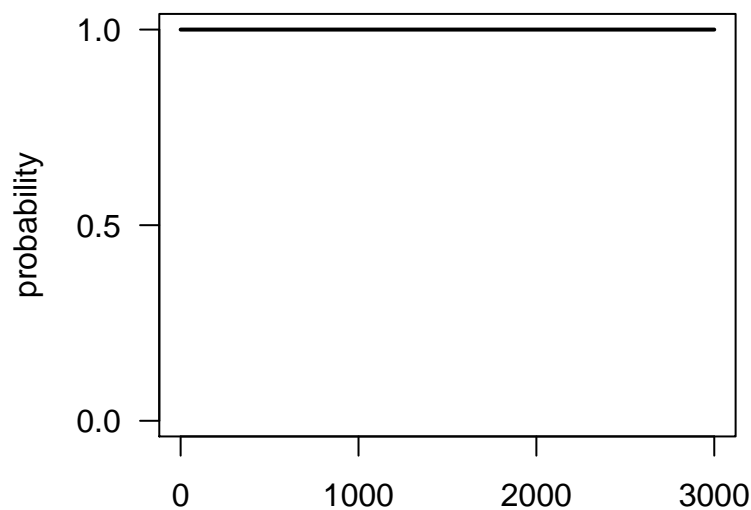
```
> data=0:3000
> const.sel(x=data)
```


Figure 1: Type 'const' probabilities.

Here are examples for 'full' type:

```
> data=0:3000
> full.sel(x=data, infl1=1500, pos=TRUE)
> full.sel(x=data, infl1=1500, pos=FALSE)
```
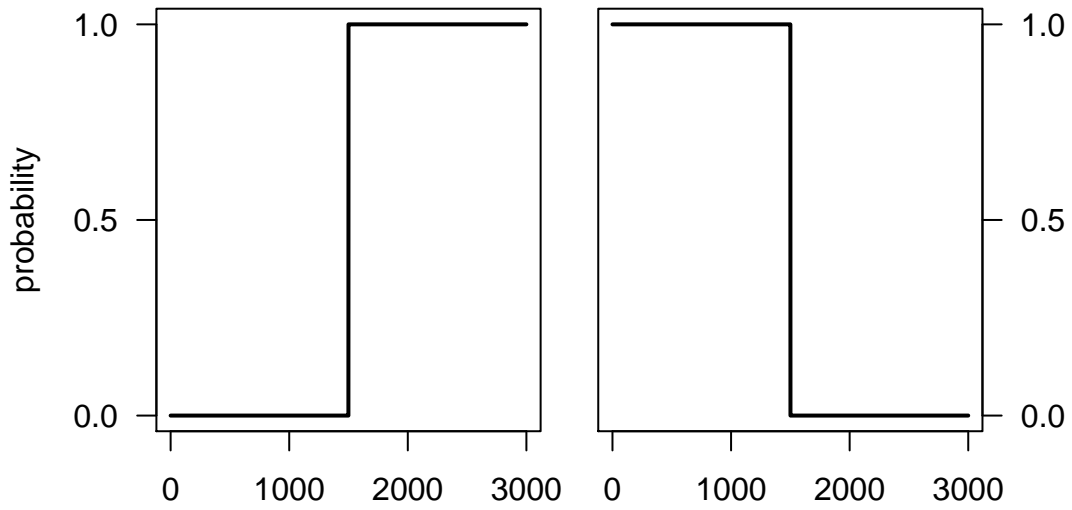

Figure 2: Type 'full' probabilities (left -> pos=TRUE | right -> pos=FALSE).

```
> data=0:3000
> full.sel(x=data, infl1=1500, pos=TRUE, lv=0.2,uv=0.8)
> full.sel(x=data, infl1=1500, pos=FALSE, lv=0.2,uv=0.8)
```
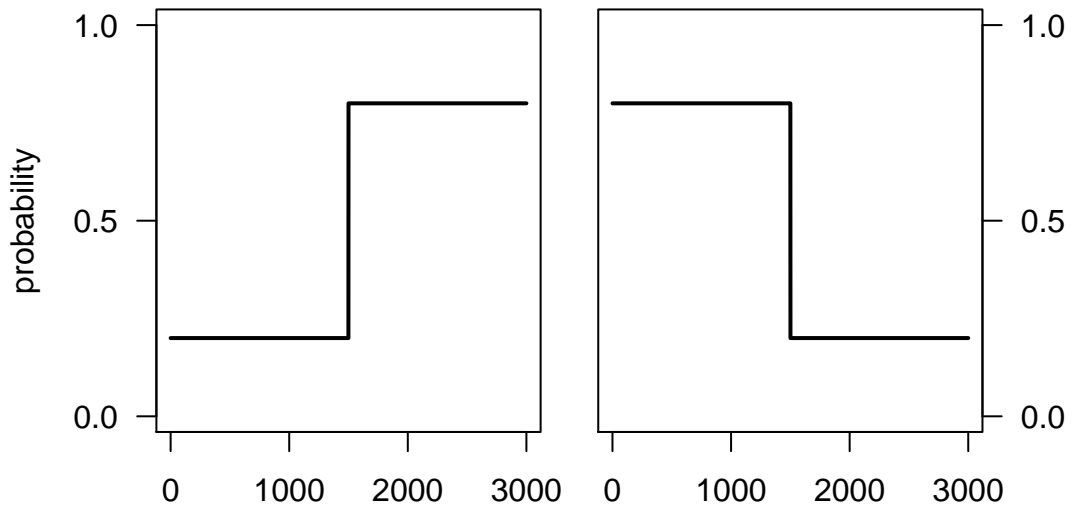

Figure 3: Type 'full' probabilities (left -> pos=TRUE | right -> pos=FALSE). In this example, minimum and maximum probabilities are respectively lv=0.2 and uv=0.8.

Here are examples for 'plat.full' type:

```
> data=0:3000
> plat.full.sel(x=data, infl1=1000, infl2=2000, pos=TRUE)
> plat.full.sel(x=data, infl1=1000, infl2=2000, pos=FALSE)
```
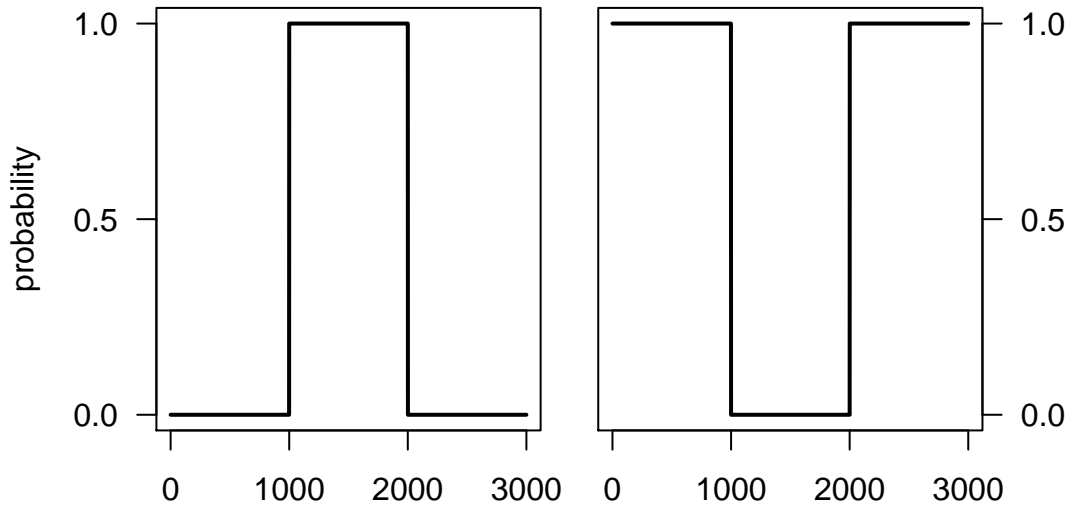

Figure 4: Type 'plat.full' probabilities (left -> pos=TRUE | right -> pos=FALSE).

```
> data=0:3000
> plat.full.sel(x=data, infl1=1000, infl2=2000, pos=TRUE,
lv=0.2,uv=0.8)
> plat.full.sel(x=data, infl1=1000, infl2=2000, pos=FALSE,
lv=0.2,uv=0.8)
```
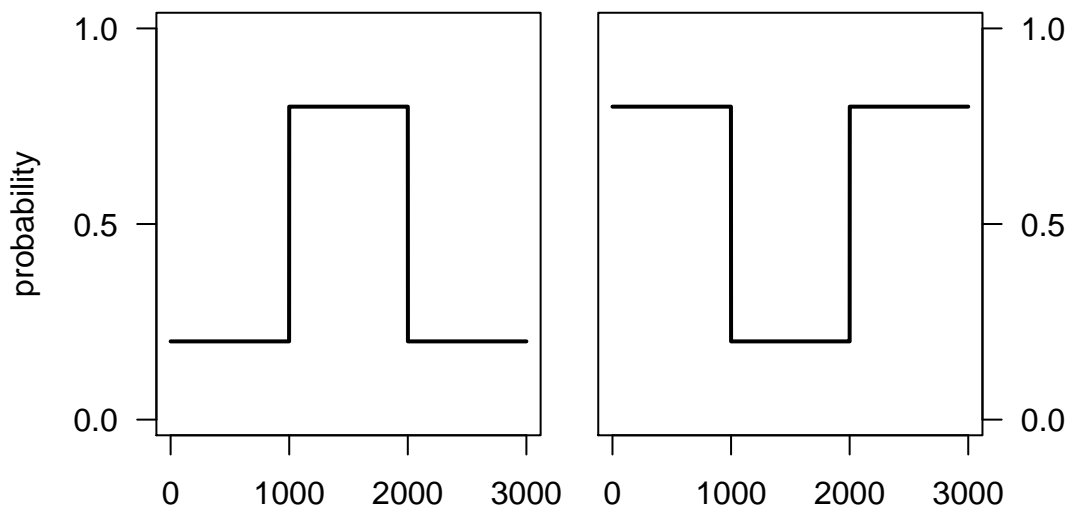

Figure 5: Type 'plat.full' probabilities (left -> pos=TRUE | right -> pos=FALSE). In this example, minimum and maximum probabilities are respectively lv=0.2 and uv=0.8.

```
> data=0:3000
> plat.full.sel(x=data, infl1=1000, infl2=2000, pos=TRUE,
lv=c(0.2,0.4),uv=0.8)
> plat.full.sel(x=data, infl1=1000, infl2=2000, pos=FALSE,
lv=0.2,uv=c(0.8,0.6))
```
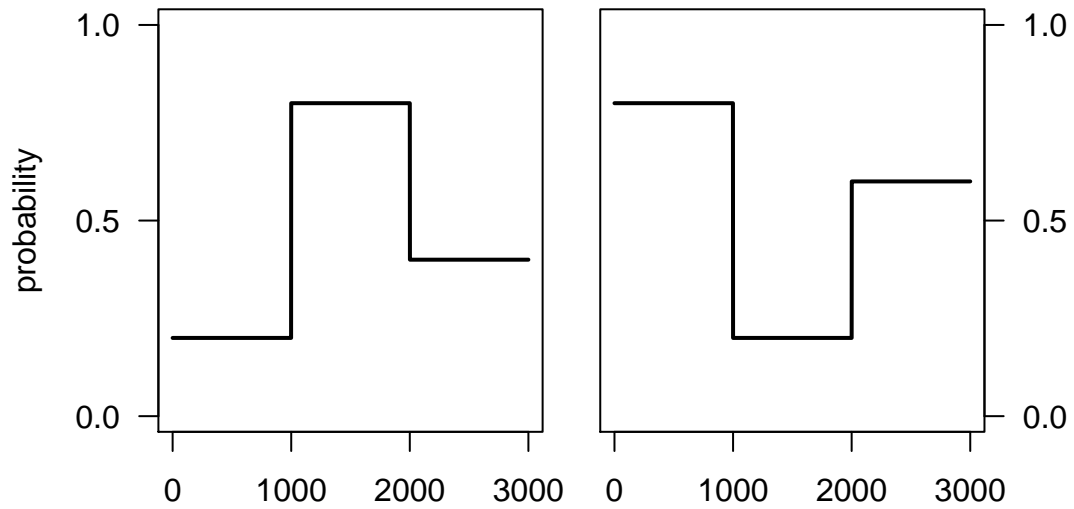

Figure 6: Type 'plat.full' probabilities (left -> pos=TRUE, lv=c(0.2,0.4) , uv=0.8 | right -> pos=FALSE, lv=0.2, uv=c(0.8,0.6)).

2   Types 'ramp' and 'plat.ramp'

These relations involve adding a gradual increase (or decrease) of probabitily between two inflection points. They are an 'upgraded' version of 'full' and 'plat.full'. Two or four inflection points are needed. The main difference between 'ramp'(Figure 7 & 8) and 'plat.ramp' (Figure 9, 10 & 11) types are the number inflection points.

ramp.sel (x, infl1, infl2, pos=TRUE, lv=0, uv=1)

plat.ramp.sel (x, infl1, infl2, infl3, infl4, pos=TRUE, lv=c(0,0), uv=c(1,1))

where `x` is a numeric vector for which probabilities are estimated, `infl1` to `infl4` are the inflection points, `pos` indicates if the trend at the beginning is positive (`TRUE`) or negative (`FALSE`), `lv` defines the lower probability values of the relation, and `uv` defines the upper probability values of the relation. By default, all fonctions have `pos=TRUE`, `lv=c(0,0)`, and `uv=c(1,1)`.

Here are examples for 'ramp' type:

```
> ramp.sel(x=data, infl1=1000, infl2=2000, pos=TRUE)
> ramp.sel(x=data, infl1=1000, infl2=2000, pos=FALSE)
```
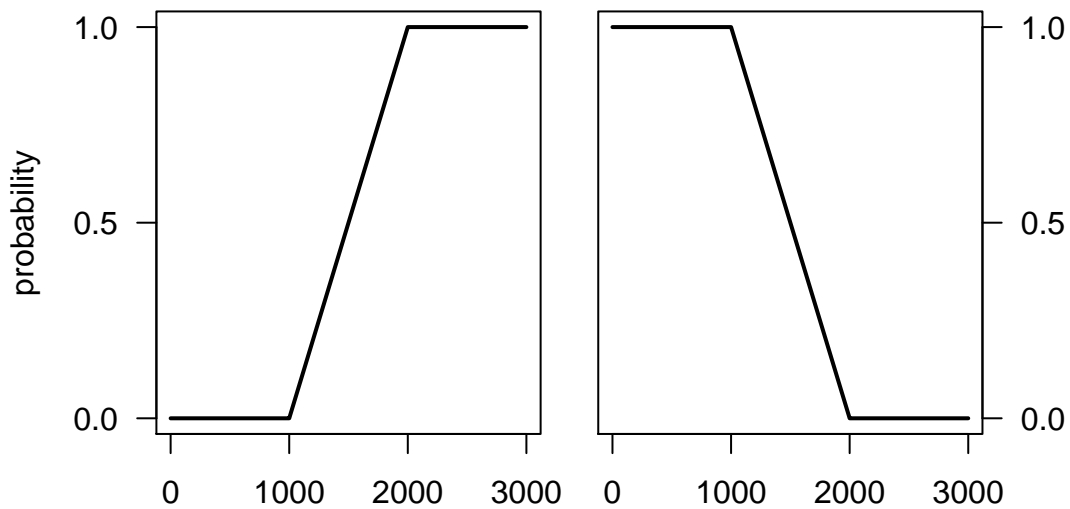

Figure 7: Type 'ramp' probabilities (left -> pos=TRUE | right -> pos=FALSE).

```
> ramp.sel(x=data, infl1=1000, infl2=2000, pos=TRUE, lv=0.2,uv=0.8)
> ramp.sel(x=data, infl1=1000, infl2=2000, pos=FALSE, lv=0.2,uv=0.8)
```
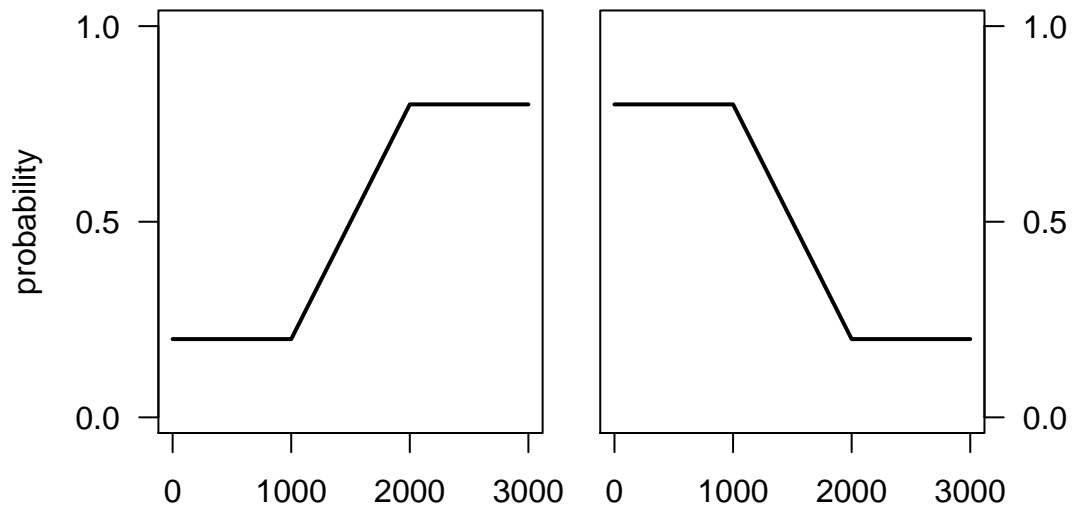

Figure 8: Type 'ramp' probabilities (left -> pos=TRUE | right -> pos=FALSE). In this example, minimum and maximum probabilities are respectively lv=0.2 and uv=0.8.

Here are examples for 'plat.ramp' type:

```
> data=0:3000
> plat.ramp.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=TRUE)
> plat.ramp.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=FALSE)
```
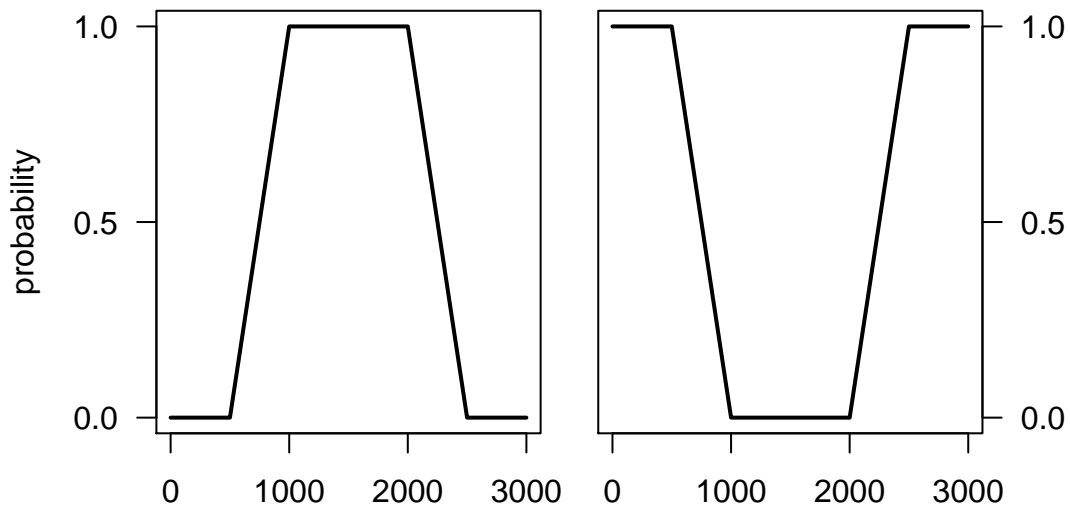

Figure 9: Type 'plat.ramp' probabilities (left -> pos=TRUE | right -> pos=FALSE).

```
> data=0:3000
> plat.ramp.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=TRUE, lv=0.2,uv=0.8)
> plat.ramp.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=FALSE, lv=0.2,uv=0.8)
```

```
> data=0:3000
> plat.ramp.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=TRUE, lv=c(0.2,0.4),uv=0.8)
> plat.ramp.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=FALSE, lv=0.2,uv=c(0.8,0.6))
```
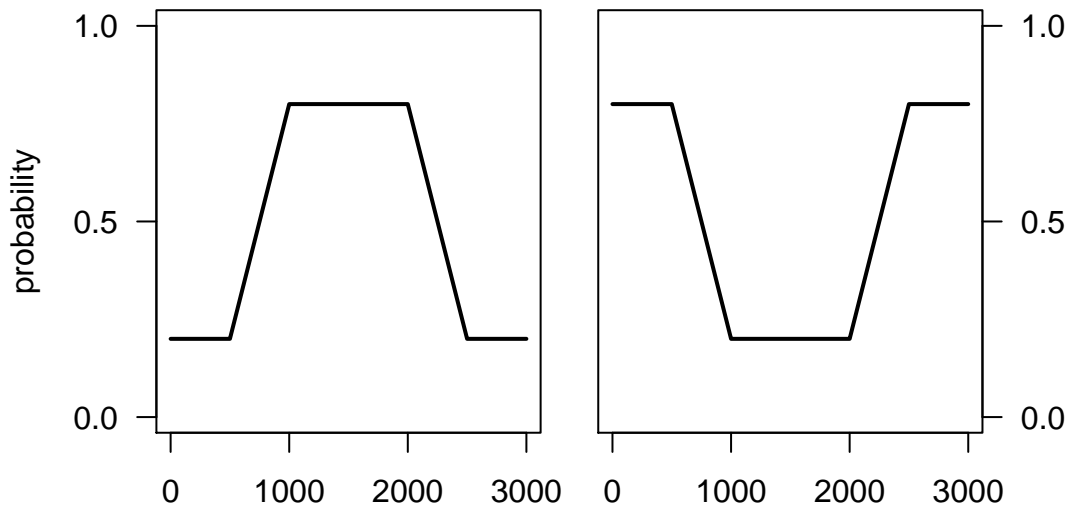
Figure 10: Type 'plat.ramp' probabilities (left -> pos=TRUE | right -> pos=FALSE). In this example, minimum and maximum probabilities are respectively lv=0.2 and uv=0.8.
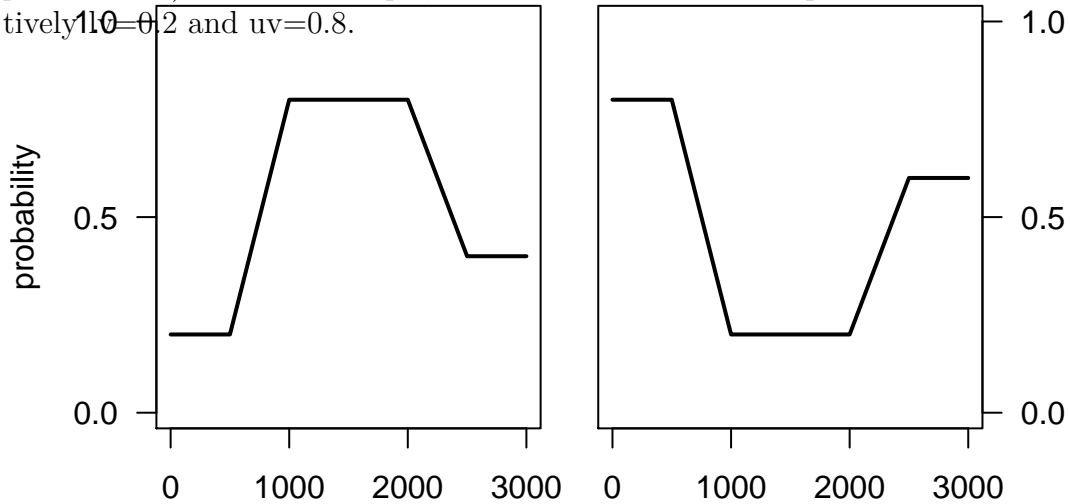

Figure 11: Type 'plat.ramp' probabilities (left -> pos=TRUE, lv=c(0.2,0.4) , uv=0.8 | right -> pos=FALSE, lv=0.2, uv=c(0.8,0.6)).

3 Types 'logit' and 'plat.logit'

These relations use logistic curves. Inflection points are defined as points where the intantaneous splope is a proportion (`prop`) of the intantenuous slope at x_{50}. These types make use of the function `find.beta()` of `package::bmisc`. Default value of `prop` is `0.1`. The end result is a logistic curve with x_{50} being the midpoint between the inflection points. Two or four inflection points are needed. The main difference between 'logit'(Figure 12 & 13) and 'plat.logit' (Figure 14, 15 & 16) types are the number inflection points.

logit.sel (x, infl1, infl2, pos=TRUE, lv=0, uv=1, ...)

plat.logit.sel (x, infl1, infl2, infl3, infl4, pos=TRUE,
    lv=c(0,0), uv=c(1,1), ...)

where x is a numeric vector for which probabilities are estimated, `infl1` to `infl4` are the inflection points, `pos` indicates if the trend at the beginning is positive (`TRUE`) or negative (`FALSE`), `lv` defines the lower probability values of the relation, and `uv` defines the upper probability values of the relation. By default, all fonctions have `pos=TRUE`, `lv=c(0,0)`, and `uv=c(1,1)`. Additionnal options of `find.beta()` can be added. Default values are `prob=NULL`, `prop=0.1`,`beta=0.2`, and `fast=TRUE`.

Here are examples for 'logit' type:

```
> logit.sel(x=data, infl1=1000, infl2=2000, pos=TRUE)
> logit.sel(x=data, infl1=1000, infl2=2000, pos=FALSE)
```
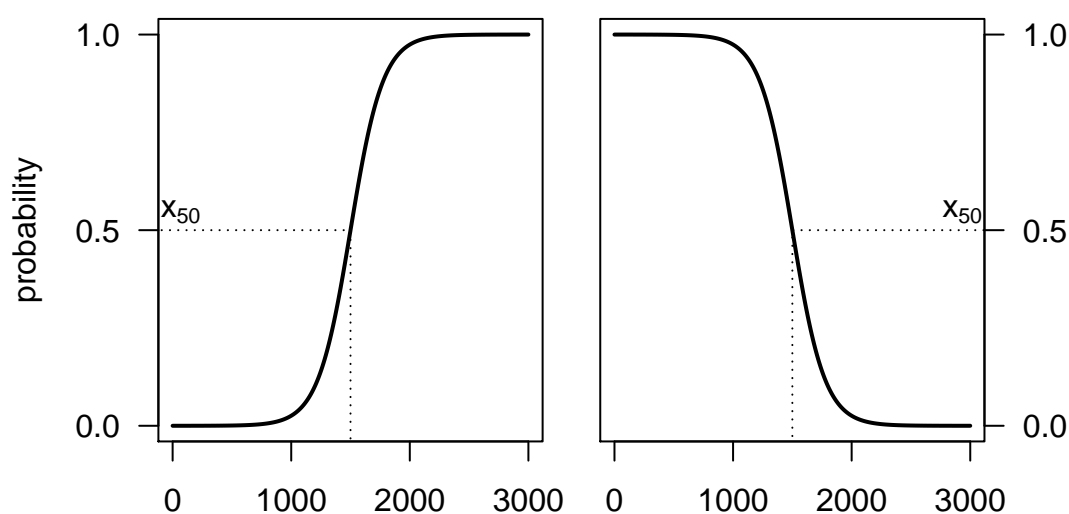

Figure 12: Type 'logit' probabilities (left -> pos=TRUE | right -> pos=FALSE).

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```
> logit.sel(x=data, infl1=1000, infl2=2000, pos=TRUE, lv=0.2,uv=0.8)
> logit.sel(x=data, infl1=1000, infl2=2000, pos=FALSE, lv=0.2,uv=0.8)
```
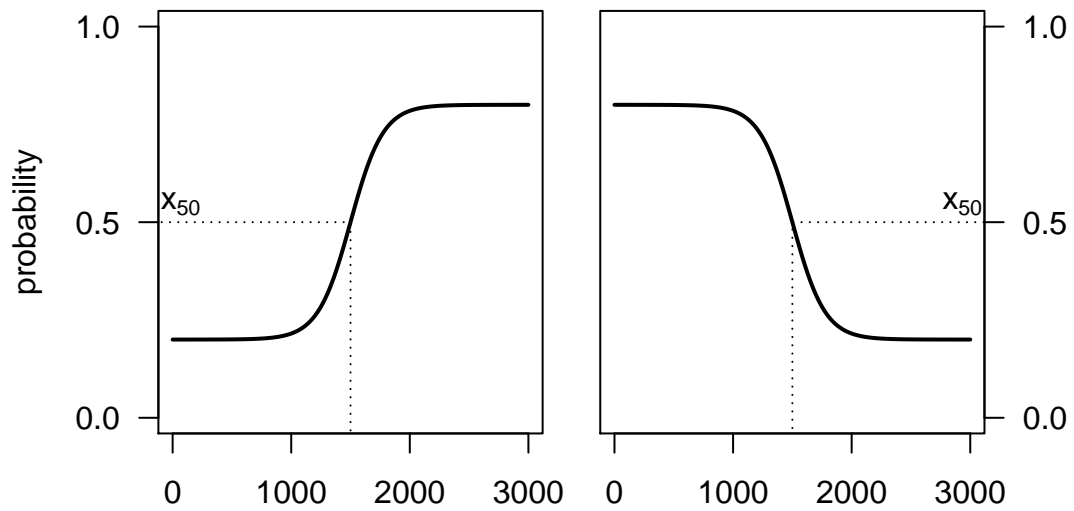

Figure 13: Type 'logit' probabilities (left -> pos=TRUE | right -> pos=FALSE). In this example, minimum and maximum probabilities are respectively lv=0.2 and uv=0.8.

Here are examples for 'plat.logit' type:

```
> data=0:3000
> plat.logit.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=TRUE)
> plat.logit.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=FALSE)
```
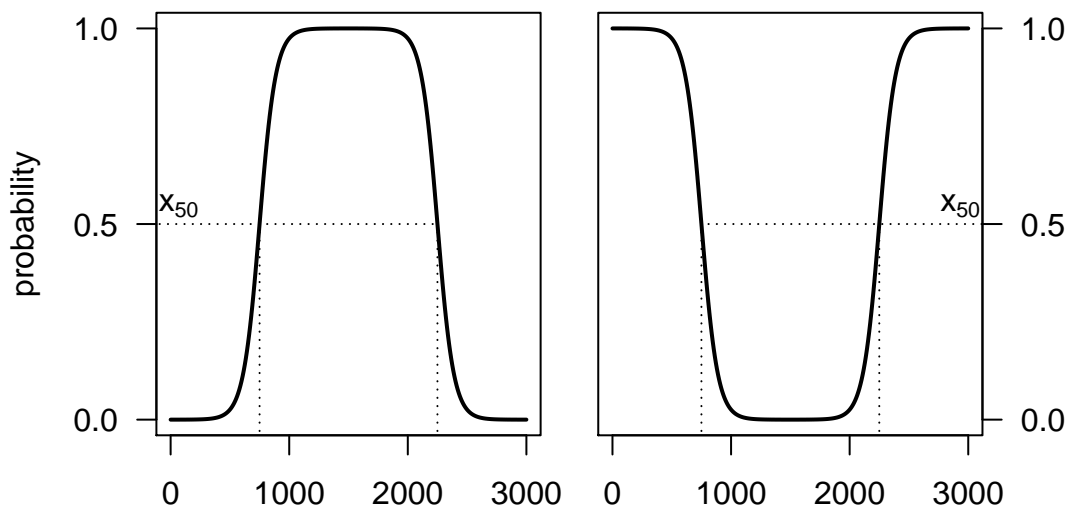

Figure 14: Type 'plat.logit' probabilities (left -> pos=TRUE | right -> pos=FALSE).

```
> data=0:3000
> plat.logit.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=TRUE, lv=0.2,uv=0.8)
> plat.logit.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=FALSE, lv=0.2,uv=0.8)
```

```
> data=0:3000
> plat.logit.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=TRUE, lv=c(0.2,0.4),uv=0.8)
> plat.logit.sel(x=data, infl1=500, infl2=1000, infl3=2000,
infl4=2500, pos=FALSE, lv=0.2,uv=c(0.8,0.6))
```
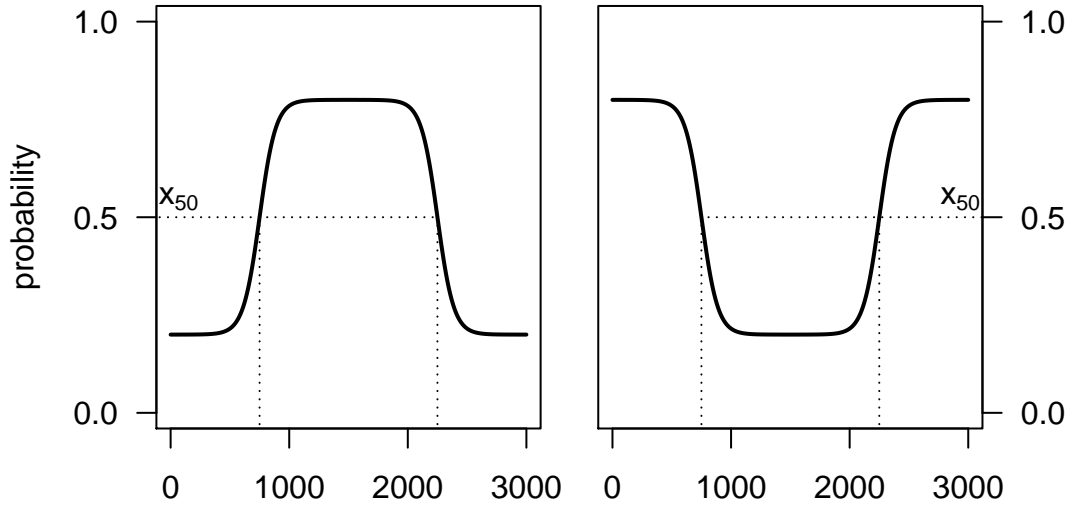
Figure 15: Type 'plat.logit' probabilities (left -> pos=TRUE | right -> pos=FALSE). In this example, minimum and maximum probabilities are respectively lv=0.2 and uv=0.8.
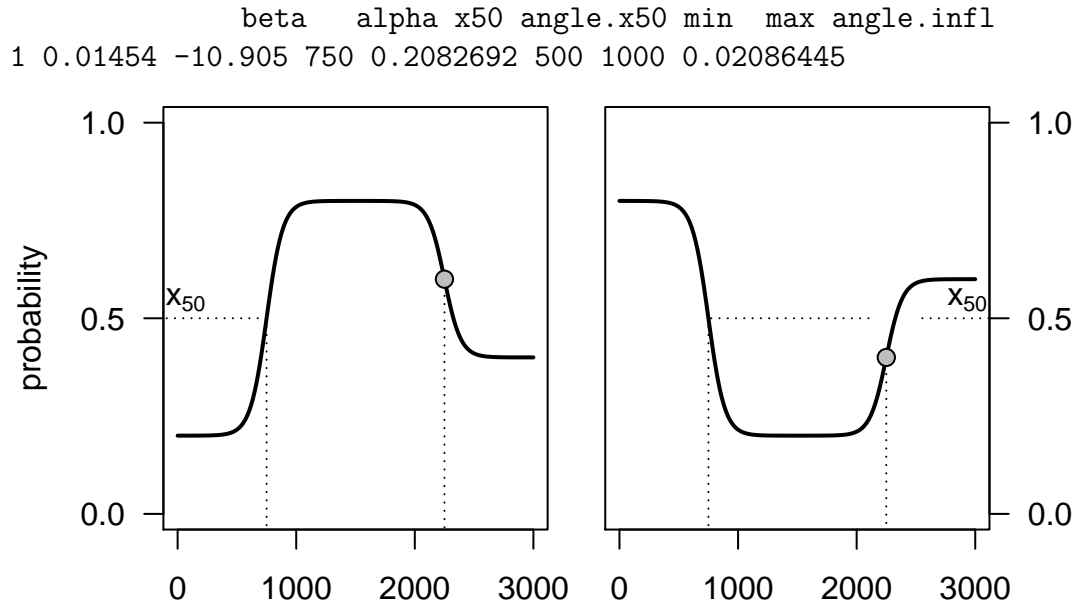
```
              beta    alpha x50 angle.x50 min  max angle.infl
1 0.01454 -10.905 750 0.2082692 500 1000 0.02086445
```


Figure 16: Type 'plat.logit' probabilities (left -> pos=TRUE, lv=c(0.2,0.4) , uv=0.8 | right -> pos=FALSE, lv=0.2, uv=c(0.8,0.6)).