## Boosted Regression Trees for ecological modeling

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## 1 Introduction

This is a brief tutorial to accompany a set of functions that we have written to facilitate fitting BRT (boosted regression tree) models in R. This tutorial is a modified version of the tutorial accompaniying Elith, Leathwick and Hastie's article in Journal of Animal Ecology. It has been adjusted to match the implementation of these functions in the 'dismo' package. The gbm\* functions in the dismo package extend functions in the 'gbm' package by Greg Ridgeway. The goal of our functions is to make the functions in the 'gbm' package easier to apply to ecological data, and to enhance interpretation.

The tutorial is aimed at helping you to learn the mechanics of how to use the functions and to develop a BRT model in R. It does not explain what a BRT model is - for that, see the references at the end of the tutorial, and the documentation of the gbm package. For an example application with similar data as in this tutorial, see Elith et al., 2008.

The gbm functions in 'dismo' are as follows:

- 1. gbm.step Fits a gbm model to one or more response variables, using cross-validation to estimate the optimal number of trees. This requires use of the utility functions roc, calibration and calc.deviance.
- 2. gbm.fixed, gbm.holdout Alternative functions for fitting gbm models, implementing options provided in the gbm package.
- 3. gbm.simplify Code to perform backwards elimination of variables, to drop those that give no evidence of improving predictive performance.
- 4. gbm.plot Plots the partial dependence of the response on one or more predictors.
- 5. gbm.plot.fits Plots the fitted values from a gbm object returned by any of the model fitting options. This can give a more reliable guide to the shape of the fitted surface than can be obtained from the individual functions, particularly when predictor variables are correlated and/or samples are unevenly distributed in environmental space.
- 6. gbm.interactions Tests whether interactions have been detected and modelled, and reports the relative strength of these. Results can be visualised with gbm.perspec

## 2 Example data

Two sets of presence/absence data for Anguilla australis (Angaus) are available. One for model training (building) and one for model testing (evaluation). In the example below we load the training data. Presence (1) and absence (0) is recorded in column 2. The environmental variables are in columns 3 to 14. This is the same data as used in Elith, Leathwick and Hastie (2008).

```
> library(dismo)
raster version 1.6-15 (7-November-2010)
> data(Anguilla_train)
> head(Anguilla_train)
```

```
Site Angaus SegSumT SegTSeas SegLowFlow DSDist DSMaxSlope USAvgT USRainDays
1
                   16.0
                           -0.10
                                                             0.57
                                                                    0.09
                                                                                2.470
     1
             0
                                        1.036 50.20
2
     2
             1
                   18.7
                             1.51
                                        1.003 132.53
                                                             1.15
                                                                    0.20
                                                                                1.153
3
     3
             0
                   18.3
                            0.37
                                                             0.57
                                                                    0.49
                                        1.001 107.44
                                                                                0.847
4
     4
                   16.7
                           -3.80
                                        1.000 166.82
                                                             1.72
                                                                    0.90
                                                                                0.210
     5
5
                   17.2
                            0.33
                                        1.005
                                                                   -1.20
             1
                                                3.95
                                                             1.15
                                                                                1.980
6
     6
             0
                   15.1
                             1.83
                                        1.015
                                                             1.72
                                                                   -0.20
                                                                                3.300
                                               11.17
  USSlope USNative DSDam
                             Method LocSed
      9.8
               0.81
1
                         0 electric
                                         4.8
2
      8.3
               0.34
                         0 electric
                                         2.0
3
      0.4
               0.00
                         0
                                         1.0
                                 spo
4
      0.4
               0.22
                                         4.0
                         1 electric
5
     21.9
               0.96
                         0 electric
                                         4.7
6
     25.7
               1.00
                         0 electric
                                         4.5
```

## 3 Fitting a model

To fit a gbm model, you need to decide what settings to use the article associated with this tutorial gives you information on what to use as rules of thumb. These data have 1000 sites, comprising 202 presence records for the short-finned eel (the command sum(model.data\$Angaus)will give you the total number of presences). As a first guess you could decide: 1. There are enough data to model interactions of reasonable complexity 2. A lr of about 0.01 could be a reasonable starting point.

To below example shows how to use our function that steps forward and identifies the optimal number of trees (nt).

```
> angaus.tc5.lr01 <- gbm.step(data = Anguilla_train, gbm.x = 3:13,
+ gbm.y = 2, family = "bernoulli", tree.complexity = 5, learning.rate = 0.01,
+ bag.fraction = 0.5)</pre>
```

<sup>&</sup>gt; Anguilla\_train = Anguilla\_train[1:500, ]

#### Loaded gbm 1.6-3.1

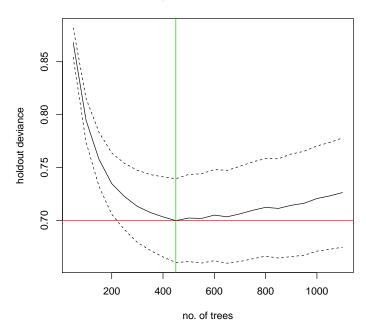
#### GBM STEP - version 2.9

Performing cross-validation optimisation of a boosted regression tree model for Angaus with dataframe Anguilla\_train and using a family of bernoulli Using 500 observations and 11 predictors creating 10 initial models of 50 trees

```
folds are stratified by prevalence
total mean deviance = 1.0279
tolerance is fixed at 0.001
ntrees resid. dev.
     0.8647
50
now adding trees...
     0.7961
100
150
     0.7618
200
     0.7404
250
     0.7293
300
     0.7227
350
     0.7208
400
     0.7193
450
     0.7157
500
     0.7146
550
     0.7162
600
     0.7144
650
     0.7139
700
     0.7163
     0.7176
750
800
     0.7202
850
     0.7204
900
     0.7238
950
     0.7264
      0.7288
1000
1050
      0.7314
1100
      0.7331
      0.7358
1150
fitting final gbm model with a fixed number of 650 trees for Angaus
mean total deviance = 1.028
mean residual deviance = 0.341
estimated cv deviance = 0.714; se = 0.056
training data correlation = 0.873
```

```
cv correlation = 0.571 ; se = 0.05
training data ROC score = 0.989
cv ROC score = 0.869 ; se = 0.022
elapsed time - 0.18 minutes
```

Angaus, d - 5, lr - 0.01



Above we used the function gbm.step, this function is an alternative to the cross-validation provided in the gbm package. We have passed information to the function about data and settings. We have defined:

the dataframe containing the data = Anguilla\_train;

the predictor variables - gbm.x = c(3:13) - which we do using a vector consisting of the indices for the data columns containing the predictors (i.e., here the predictors are columns 3 to 13 in Anguilla\_train);

the response variable - gbm.y = 2 - indicating the column number for the species (response) data;

the nature of the error structure - For example, family = 'bernoulli' (note the quotes);

the tree complexity - we are trying a tree complexity of 5 for a start;

the learning rate - we are trying with 0.01;

the bag fraction - our default is 0.75; here we are using 0.5;

Everything else - i.e. all the other things that we could change if we wanted to (see the help file, and the documentation of the gbm package) - are set at

their defaults if they are not named in the call. If you want to see what else you could change, you can type gbm.step and all the code will write itself to screen, or type args(gbm.step) and it will open in an editor window.

Running a model such as that described above writes progress reports to the screen, makes a graph, and returns an object containing a number of components. Firstly, the things you can see: The R console will show something like this (not identical, because remember that these models are stochastic and therefore slightly different each time you run them, unless you set the seed or make them deterministic by using a bag fraction of 1)

This reports a brief model summary. All these values are also retained in the model object, so they will be permanently kept (as long as you save the R workspace before quitting).

This model was built with the default 10-fold cross-validation. The solid black curve is the mean, and the dotted curves about 1 standard error, for the changes in predictive deviance (ie as measured on the excluded folds of the cross-validation). The red line shows the minimum of the mean, and the green line the number of trees at which that occurs. The final model that is returned in the model object is built on the full data set, using the number of trees identified as optimal.

The returned object is a list (see R documentation if you don't know what that is), and the names of the components can be seen by typing:

To pull out one component of the list, use a number (angaus.tc5.lr01[[29]]) or name (angaus.tc5.lr01\$cv.statistics) - but be careful, some are as big as the dataset, e.g. there will be 1000 fitted values. Find this by typing length(angaus.tc5.lr01\$fitted)

The way we organise our functions is to return exactly what Ridgeway's function in the gbm package returned, plus extra things that are relevant to our code. You will see by looking at the final parts of the gbm.step code that we have added components 25 onwards, that is, from gbm.call on. See the gbm documentation for what his parts comprise. Ours are:

gbm.call - A list containing the details of the original call to gbm.step fitted - The fitted values from the final tree, on the response scale fitted.vars - The variance of the fitted values, on the response scale residuals - The residuals for the fitted values, on the response scale contributions - The relative importance of the variables, produced from the gbm summary function

self.statistics - The relevant set of evaluation statistics, calculated on the fitted values - i.e. this is only interesting in so far as it demonstrates "evaluation" (i.e. fit) on the training data. It should NOT be reported as the model predictive performance.

cv.statistics These are the most appropriate evaluation statistics. We calculate each statistic within each fold (at the identified optimal number of trees that is calculated on the mean change in predictive deviance over all folds), then present here the mean and standard error of those fold-based statistics.

weights - the weights used in fitting the model (by default, "1" for each observation - i.e. equal weights).

trees.fitted - A record of the number of trees fitted at each step in the stagewise fitting; only relevant for later calculations

training.loss.values - The stagewise changes in deviance on the training data cv.values - the mean of the CV estimates of predictive deviance, calculated at each step in the stagewise process - this and the next are used in the plot shown above

cv.loss.ses - standard errors in CV estimates of predictive deviance at each step in the stagewise process

cv.loss.matrix - the matrix of values from which cv.values were calculated - as many rows as folds in the  ${\rm CV}$ 

cv.roc.matrix - as above, but the values in it are area under the curve estimated on the excluded data, instead of deviance in the cv.loss.matrix.

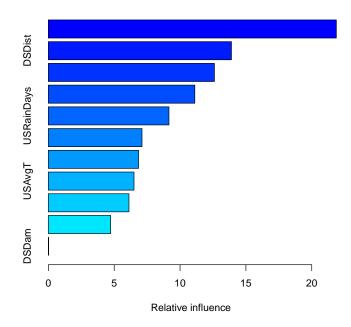
You can look at variable importance with the summary function

#### > names(angaus.tc5.lr01)

[1]	"initF"	"fit"	"train.error"
[4]	"valid.error"	"oobag.improve"	"trees"
[7]	"c.splits"	"bag.fraction"	"distribution"
[10]	"interaction.depth"	"n.minobsinnode"	"n.trees"
[13]	"nTrain"	"response.name"	"shrinkage"
[16]	"train.fraction"	"var.levels"	"var.monotone"
[19]	"var.names"	"var.type"	"verbose"
[22]	"data"	"Terms"	"cv.folds"
[25]	"gbm.call"	"fitted"	"fitted.vars"
[28]	"residuals"	"contributions"	"self.statistics"
[31]	"cv.statistics"	"weights"	"trees.fitted"
[34]	"training.loss.values"	"cv.values"	"cv.loss.ses"
[37]	"cv.loss.matrix"	"cv.roc.matrix"	

#### > summary(angaus.tc5.lr01)

	var	rel.inf			
1	SegSumT	21.86688274			
2	DSDist	13.90321607			
3	Method	12.61178594			
4	USNative	11.12178453			
5	${\tt USRainDays}$	9.15920349			
6	SegTSeas	7.11235944			
7	USSlope	6.84978466			
8	USAvgT	6.50541131			
9	SegLowFlow	6.12244296			
10	DSMaxSlope	4.73298799			
11	DSDam	0.01414089			



## 4 Choosing the settings

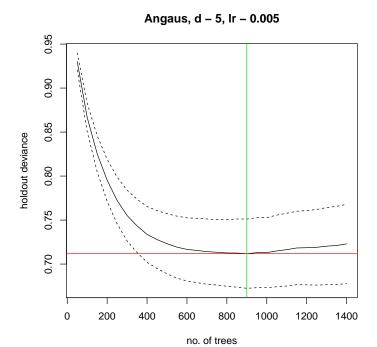
The above was a first guess at settings, using rules of thumb discussed in Elith et al. (2008). It made a model with only 650 trees, so our next step would be to reduce the lr. For example, try lr=0.005, to aim for over 1000 trees:

```
> angaus.tc5.lr005 <- gbm.step(data = Anguilla_train, gbm.x = 3:13,
+ gbm.y = 2, family = "bernoulli", tree.complexity = 5, learning.rate = 0.005,
+ bag.fraction = 0.5)</pre>
GBM STEP - version 2.9
```

Performing cross-validation optimisation of a boosted regression tree model for Angaus with dataframe Anguilla\_train and using a family of bernoulli Using 500 observations and 11 predictors creating 10 initial models of 50 trees

folds are stratified by prevalence total mean deviance = 1.0279 tolerance is fixed at 0.001 ntrees resid. dev. 50 0.9275

```
now adding trees...
     0.8645
100
150
     0.8239
200
     0.793
250
     0.7723
300
     0.7566
350
     0.7458
     0.7362
400
450
     0.7306
500
     0.7255
550
     0.7207
600
     0.7191
650
     0.7162
700
     0.7161
750
     0.7158
800
     0.7154
850
     0.7145
900
     0.7133
950
     0.7129
1000
      0.713
1050
      0.7125
1100
      0.7131
1150
      0.7147
1200
      0.716
1250
       0.7169
1300
       0.7177
1350
      0.7193
1400
      0.7211
       0.7228
1450
fitting final gbm model with a fixed number of 1050 trees for Angaus
mean total deviance = 1.028
mean residual deviance = 0.38
estimated cv deviance = 0.712; se = 0.044
training data correlation = 0.851
cv correlation = 0.585; se = 0.034
training data ROC score = 0.984
cv ROC score = 0.868; se = 0.012
elapsed time - 0.2 minutes
```



To more broadly explore whether other settings perform better, and assuming that these are the only data available, you could either split the data into a training and testing set or use the cross-validation results. You could systematically alter tc, Ir and the bag fraction and compare the results. See the later section on prediction to find out how to predict to independent data and calculate relevant statistics.

# 5 Alternative ways to fit models

The step function above is slower than just fitting one model and finding a minimum. If this is a problem, you could use our gbm.holdout code - this combines from the gbm package in ways we find useful. We tend to prefer gbm.step, especially when modelling many species, because it automatically finds the optimal number of trees. Alternatively, the gbm.fixed code allows you to fit a model of a set number of trees; this can be used, as in Elith et al. (2008), to predict to new data (see later section).

## 6 Simplifying the model

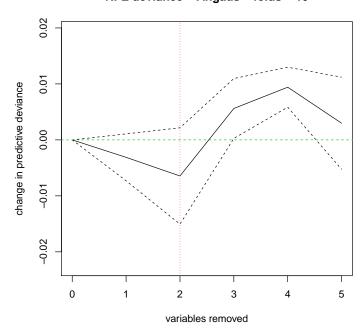
For a discussion of simplification see Appendix 2 of the online supplement to Elith et al (2008). Simplification builds many models, so it can be slow. For

example, the code below took a few minutes to run on a modern laptop. In it we assess the value in simplifying the model built with a lr of 0.005, but only test dropping up to 5 variables (the "n.drop" argument; the default is an automatic rule so it continues until the average change in predictive deviance exceeds its original standard error as calculated in gbm.step).

```
> angaus.simp <- gbm.simplify(angaus.tc5.lr005, n.drops = 5)</pre>
gbm.simplify - version 2.9
simplifying gbm.step model for Angaus with 11 predictors and 500 observations
original deviance = 0.7118(0.0393)
a fixed number of 5 drops will be tested
creating initial models...
dropping predictor: 1 2 3 4 5
now processing final dropping of variables with full data
1 - DSDam
```

- 2 DSMaxSlope
- 3 SegTSeas
- 4 SegLowFlow
- 5 USSlope

#### RFE deviance - Angaus - folds = 10



For our run, this estimated that the optimal number of variables to drop was 1; yours could be slightly different:

You can use the number indicated by the red vertical line, or look at the results in the angaus.simp object Now make a model with 1 predictor dropped, by indicating to the gbm.step call the relevant number of predictor(s) from the predictor list in the angaus.simp object - see highlights, below, in which we indicate we want to drop 1 variable by calling the second vector of predictor columns in the pred list, using a [[1]]:

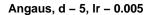
```
> angaus.tc5.lr005.simp <- gbm.step(Anguilla_train, gbm.x = angaus.simp$pred.list[[1]],
+ gbm.y = 2, tree.complexity = 5, learning.rate = 0.005)</pre>
```

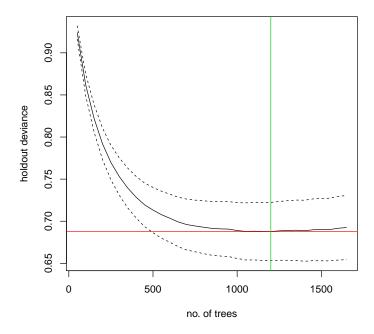
Performing cross-validation optimisation of a boosted regression tree model for Angaus with dataframe Anguilla\_train and using a family of bernoulli Using 500 observations and 10 predictors creating 10 initial models of 50 trees

folds are stratified by prevalence total mean deviance = 1.0279 tolerance is fixed at 0.001 ntrees resid. dev.

GBM STEP - version 2.9

```
50
     0.9282
now adding trees...
100
     0.8661
150
     0.8253
200
     0.7954
250
     0.7723
300
     0.7563
350
     0.7425
400
     0.7317
     0.7219
450
500
     0.7148
550
     0.7085
600
     0.7042
650
     0.7015
700
     0.6985
750
     0.6963
800
     0.6955
850
     0.6953
900
     0.6943
950
     0.6936
1000
      0.6927
1050
      0.6923
1100
      0.6928
1150
      0.6928
1200
      0.6937
1250
      0.6946
1300
      0.6953
1350
      0.6962
1400
      0.6978
      0.6981
1450
1500
      0.6984
1550
      0.6991
fitting final gbm model with a fixed number of 1050 trees for Angaus
mean total deviance = 1.028
mean residual deviance = 0.366
estimated cv deviance = 0.692; se = 0.06
training data correlation = 0.866
cv correlation = 0.586; se = 0.056
training data ROC score = 0.988
cv ROC score = 0.87; se = 0.027
elapsed time - 0.21 minutes
```



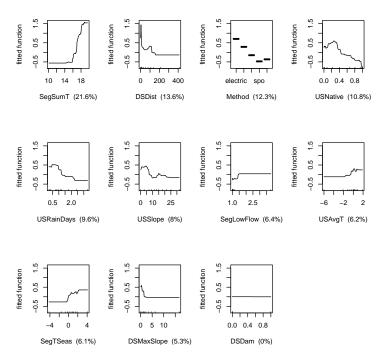


This has now made a new model (angaus.tc5.lr005.simp) with the same list components as described earlier. We could continue to use it, but given that we don't particularly want a more simple model (our view is that, in a dataset of this size, included variables that contribute little are acceptable), we won't use it further.

# 7 Plotting the functions and fitted values from the model

The fitted functions from a BRT model created from any of our functions can be plotted using gbm.plot. If you want to plot all variables on one sheet first set up a graphics device with the right set-up - here we will make one with 3 rows and 4 columns:

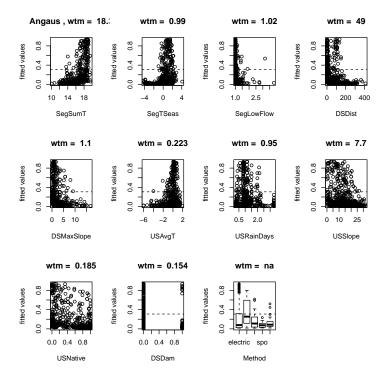
> gbm.plot(angaus.tc5.lr005, n.plots = 11, write.title = FALSE)



Additional arguments to this function allow for making a smoothed representation of the plot, allowing different vertical scales for each variable, omitting (and formatting) the rugs, and plotting a single variable.

Depending on the distribution of observations within the environmental space, fitted functions can give a misleading indication about the distribution of the fitted values in relation to each predictor. The function gbm.plot.fits has been provided to plot the fitted values in relation to each of the predictors used in the model.

> gbm.plot.fits(angaus.tc5.1r005)



This has options that allow for the plotting of all fitted values or of fitted values only for positive observations, or the plotting of fitted values in factor type graphs that are much quicker to print. Values above each graph indicate the weighted mean of fitted values in relation to each non-factor predictor.

## 8 Interrogate and plot the interactions

This code assesses the extent to which pairwise interactions exist in the data. find.int <- gbm.interactions(angaus.tc5.lr005). The returned object, here named test.int, is a list. The first 2 components summarise the results, first as a ranked list of the 5 most important pairwise interactions, and the second tabulating all pairwise interactions. The variable index numbers in \$rank.list can be used for plotting.

SegTSeas	0	0.00		1.00	0.60	0.05	0.43	3.44
SegLowFlow	0	0.00		0.00	0.39	0.12	0.09	0.02
DSDist	0	0.00		0.00	0.00	0.02	0.31	1.53
${\tt DSMaxSlope}$	0	0.00		0.00	0.00	0.00	0.62	0.07
USAvgT	0	0.00		0.00	0.00	0.00	0.00	0.83
USRainDays	0	0.00		0.00	0.00	0.00	0.00	0.00
USSlope	0	0.00		0.00	0.00	0.00	0.00	0.00
USNative	0	0.00		0.00	0.00	0.00	0.00	0.00
DSDam	0	0.00		0.00	0.00	0.00	0.00	0.00
Method	0	0.00		0.00	0.00	0.00	0.00	0.00
	USSlope	${\tt USNative}$	${\tt DSDam}$	Method				
SegSumT	10.68	1.61	0	37.57				
SegTSeas	0.70	0.92	0	3.35				
SegLowFlow	0.24	0.05	0	0.65				
DSDist	1.47	1.87	0	1.18				
${\tt DSMaxSlope}$	0.38	3.22	0	0.04				
USAvgT	0.78	0.78	0	3.49				
USRainDays	0.65	6.38	0	2.81				
USSlope	0.00	0.29	0	0.36				
USNative	0.00	0.00	0	2.09				
DSDam	0.00	0.00	0	0.00				

0.00

## > find.int\$rank.list

0.00

Method

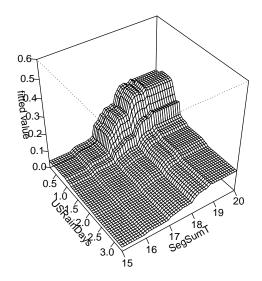
var1.index var1.names var2.index var2.names int.size 1 7 USRainDays 1 SegSumT37.77 2 Method SegSumT 37.57 11 3 SegSumT 6 USAvgT 1 12.29 SegSumT 4 8 1 10.68 USSlope SegSumT 5 4  ${\tt DSDist}$ 1 8.75 9 6  ${\tt USNative}$ 7 USRainDays 6.38

0.00

You can plot pairwise interactions like this:

```
> gbm.perspec(angaus.tc5.lr005, 7, 1, y.range = c(15, 20), z.range = c(0, + 0.6))
```

maximum value = 0.34



Additional options allow specifications of label names, rotations of the 3D graph and so on.

# 9 Predicting to new data

If you want to predict to a set of sites (rather than to a whole map), the general procedure is to set up a data frame with rows for sites and columns for the variables that are in your model. R is case sensitive; the names need to exactly match those in the model. Other columns such as site IDs etc can also exist in the data frame (and are ignored).

Our dataset for predicting to sites is in a file called Anguilla\_test. The "Method" column needs to be converted to a factor, with levels matching those in the modelling data. To make predictions to sites from the BRT model use predict (or predict.gbm) from the gbm package The predictions are in a vector called preds. These are evaluation sites, and have observations in column 1 (named Angaus\_obs). They are independent of the model building set and were used for an evaluation with independent data. Note that the calc.deviance function has different formulae for different distributions of data; the default is binomial, so we didn't specify it in the call

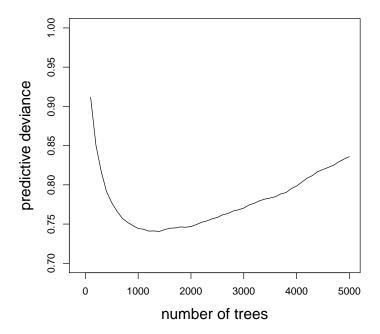
```
> data(Anguilla_test)
```

<sup>&</sup>gt; preds <- predict.gbm(angaus.tc5.1r005, Anguilla\_test, n.trees = angaus.tc5.1r005\$gbm.call\$

```
type = "response")
> calc.deviance(obs = Anguilla_test$Angaus_obs, pred = preds, calc.mean = TRUE)
[1] 0.746185
> d = cbind(Anguilla_test$Angaus_obs, preds)
> pres = d[d[, 1] == 1, 2]
> abs = d[d[, 1] == 0, 2]
> e = evaluate(p = pres, a = abs)
                 : ModelEvaluation
class
                 : 107
n presences
n absences
                 : 393
AUC
                 : 0.8578869
                 : 0.5247485
cor
TPR+TNR threshold: 0.143
```

One useful feature of prediction in gbm is you can predict to a varying number of trees. See the highlighted code below to how to predict to a vector of trees. The full set of code here shows how to make one of the graphed lines from Fig. 2 in our paper, using a model of 5000 trees developed with gbm.fixed

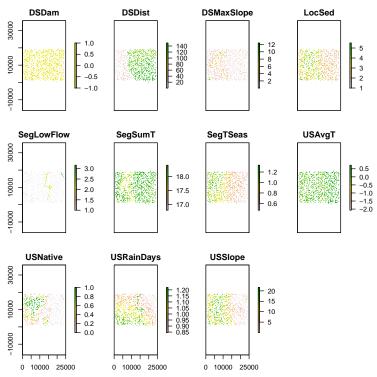
Note that the code above makes a matrix, with each column being the predictions from the model angaus.5000 to the number of trees specified by that element of tree.list - for example, the predictions in column 5 are for tree.list[5] = 500 trees. Now to calculate the deviance of all these results, and plot them:



# 10 spatial prediction

Here we show how to predict to a whole map (technically to a RasterLayer object) using the predict version in the package 'raster'. The predictor variables are available as a RasterBrick (multi-layered raster) in Anguilla\_grids.

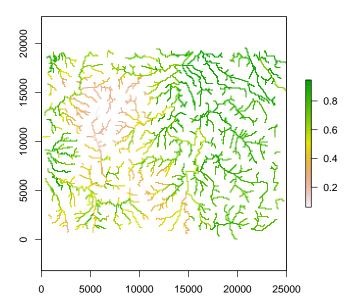
- > data(Anguilla\_grids)
- > plot(Anguilla\_grids)



There is (obviously) no grid for fishing method. We create a data.frame with a constant value (of class 'factor') and pass that on to the predict function.

```
> Method = factor("electric", levels = levels(Anguilla_train$Method))
> add = data.frame(Method)
> p = predict(Anguilla_grids, angaus.tc5.lr005, const = add, n.trees = angaus.tc5.lr005$gbm.+ type = "response")
> p = mask(p, raster(Anguilla_grids, 1))
> plot(p, main = "Angaus - BRT prediction")
```

#### Angaus - BRT prediction



## 11 Further reading

The following includes a mix of both statistical papers and ecological applications:

Elith, J., Leathwick, J.R., and Hastie, T. (2008). Boosted regression trees - a new technique for modelling ecological data. Journal of Animal Ecology Friedman, J.H. (2001) Greedy function approximation: a gradient boosting machine. The Annals of Statistics, 29, 1189-1232.

Friedman, J.H. (2002) Stochastic gradient boosting. Computational Statistics and Data Analysis, 38, 367-378.

Friedman, J.H., Hastie, T., and Tibshirani, R. (2000) Additive logistic regression: a statistical view of boosting. The Annals of Statistics, 28, 337-407.

Friedman, J.H. and Meulman, J.J. (2003) Multiple additive regression trees with application in epidemiology. Statistics in Medicine, 22, 1365-1381.

Hastie, T., R. Tibshirani, and J. H. Friedman. 2001. The Elements of Statistical Learning: Data Mining, Inference, and Prediction. Springer-Verlag, New York.

Leathwick, J.R., Elith, J., Francis, M.P., Hastie, T., and Taylor, P. (2006a) Variation in demersal fish species richness in the oceans surrounding New Zealand: an analysis using boosted regression trees. Marine Ecology Progress Series, 321, 267-281.

- Moisen, G.G., Freeman, E.A., Blackard, J.A., Frescino, T.S., Zimmermann, N.E., and Edwards, T.C.. (2006) Predicting tree species presence and basal area in Utah: a comparison of stochastic gradient boosting, generalized additive models, and tree-based methods. Ecological Modelling, 199, 176-187.
- Ridgeway, G. (1999) The state of boosting. Computing Science and Statistics, 31, 172-181.
- Ridgeway, G. (2006) Generalized boosted regression models. Documentation on the R package "gbm", version 1.5-7. http://www.i-pensieri.com/gregr/gbm.shtml.
- Schapire, R. (2003). The boosting approach to machine learning an overview. In MSRI Workshop on Nonlinear Estimation and Classification, 2002. (eds D.D. Denison, M.H. Hansen, C. Holmes, B. Mallick and B. Yu), Springer, NY.
- Wintle, B. A., J. Elith, and J. Potts. 2005. Fauna habitat modelling and mapping in an urbanising environment; A case study in the Lower Hunter Central Coast region of NSW. Austral Ecology 30:729-748.