Outline

Chapter 10: Inference for regression models

Introductory Statistics for Engineering Experimentation

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10.1 Inference for a regression line

Section 10.1: Inference for a regression line

▶ Recall that a simple linear regression model is

$$\mathcal{Y}_i = \beta_0 + \beta_1 x_i + \epsilon_i, \quad i = 1, \dots, n$$

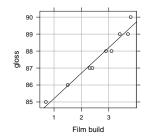
- ▶ The least squares estimates, $\widehat{\beta}_0$ and $\widehat{\beta}_1$, of the coefficients are functions of the data and hence are random variables. We associate *standard errors* with these estimates.
- ► The text derives formulas for the variance of the estimators. The formulas can be interesting but do not easily extend to more complex models. It is easier to simply read the standard error from the output.
- ▶ In the R output each coefficient estimate is accompanied by a Std. Error (standard error), a t value (the ratio of the estimate and its standard error) and a Pr(>|t|), which is the p-value for the two-sided hypothesis test. The confint extractor can be used to determine confidence intervals.

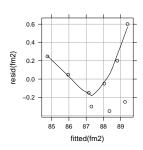
Examples 10.1.1 and 10.1.2

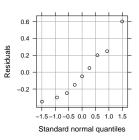
```
> summary(fm1 <- lm(time ~ temp, timetemp,
                      subset = type == "Repaired"))
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -37.4902
                         2.7833 -13.47 3.52e-08
             -1.8643
                         0.1069 -17.45 2.30e-09
Residual standard error: 0.7699 on 11 degrees of freedom
Multiple R-squared: 0.9651, Adjusted R-squared: 0.9619
F-statistic: 304.3 on 1 and 11 DF, p-value: 2.303e-09
> confint(fm1)
                 2.5 %
                           97.5 %
(Intercept) -43.616328 -31.364111
             -2.099460 -1.629053
temp
```

▶ The confidence interval ([-2.099, -1.629]) on β_1 , the slope, is of interest. The other confidence interval is not of interest because β_0 is meaningless for these data.

Example 10.1.3







Estimate Std. Error t value Pr(>|t|)

(Intercept) 83.7031 0.3184 262.86 3.04e-15 0.1130 13.27 3.23e-06 build 1.4988

Residual standard error: 0.3306 on 7 degrees of freedom Multiple R-squared: 0.9618, Adjusted R-squared: 0.9563 F-statistic: 176 on 1 and 7 DF, p-value: 3.234e-06

> confint(fm2)

2.5 % 97.5 % (Intercept) 82.950116 84.456061 build 1.231687 1.765977