

1. **Problem**

What is the derivative of $f(x) = x^7 e^{3.9x}$, evaluated at $x = 0.61$?

- (a) 3.89
- (b) 5.22
- (c) 4.23
- (d) 6.86
- (e) 3.01

Solution

Using the product rule for $f(x) = g(x) \cdot h(x)$, where $g(x) := x^7$ and $h(x) := e^{3.9x}$, we obtain

$$\begin{aligned} f'(x) &= [g(x) \cdot h(x)]' = g'(x) \cdot h(x) + g(x) \cdot h'(x) \\ &= 7x^{7-1} \cdot e^{3.9x} + x^7 \cdot e^{3.9x} \cdot 3.9 \\ &= e^{3.9x} \cdot (7x^6 + 3.9x^7) \\ &= e^{3.9x} \cdot x^6 \cdot (7 + 3.9x). \end{aligned}$$

Evaluated at $x = 0.61$, the answer is

$$e^{3.9 \cdot 0.61} \cdot 0.61^6 \cdot (7 + 3.9 \cdot 0.61) = 5.215814.$$

Thus, rounded to two digits we have $f'(0.61) = 5.22$.

- (a) False
- (b) True
- (c) False
- (d) False
- (e) False