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Biomass Dynamic Models

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Init

■init, fig=false, echo=false■= dirMy="/home/lkell/flr/manual/ggplotFL" source(paste(dirMy,"R/ggplotFL.R",sep="/"))
@

1 Introduction

Introduction

2 Surplus Production

Surplus Production

The productivity (Pt) of a stock can be defined as the surplus production, i.e. following Hilborn (2001):

$$P_t + B_{t+1} - B_t - C_t$$

where B_t is total stock biomass, and B_t total catch weight (i.e yield) at time t.

Productivity is greatest at a biomass equivalent to B_{MSY} with a yield equivalent to MSY .

The same equation can be used to model stock dynamics

$$B_{t+1} = B_t - P_t - C_t$$

Where P_t is then modelled by a production function; a review of such biomass models is given by Kingsland (1982).

There are various functional forms for the production function that describes the relationship between surplus production and abundance e.g. Schaefer (1954), Gompertz (), Pella-Tomlinson (), Theta-logistic, Fletcher (), Pollacheck and Shepherd

2.1 Schaefer

Schaefer

$$B_t = B_{t-1} + rB_t \left(1 - \frac{B_t}{K}\right) - C_t$$

Where in biological terms, the second surplus production term combines recruitment, body growth, and natural mortalities.

Conceptually, the model describes the simplest case of linear recruitment, where all individuals have the same body weight, and the natural mortality rate is constant. Individuals reproduce as 1-year-olds and then die. After a period of removals, the population rebuilds towards K until the number of individuals dying from natural causes equals the recruitment.

The relative growth rate, as a fraction of current abundance, is $(B) = g(B)/B$,

$$B = r - \frac{rB}{K}$$

so the relative growth rate approaches r when the abundance is close to zero, and declines linearly with B until zero growth occurs at abundance K with a maximum at $K/2$

2.2 Gompertz

Gompertz

The Gompertz (1825) growth equation as applied in stock assessment by Fox (1970)

■fig1,echo=FALSE,fig=TRUE,width=10,height=8,sanitize=TRUE■= plot(*datx*, *daty*) @

Figure 1: Plot using R base graphics

2.3 Pella and Tomlinson

Pella and Tomlinson (1969)

When $p=1$ we get Schaefer and $p \rightarrow 0$ we get Gompertz,

The Pella-Tomlinson shape parameter p does not only shift B away from $0.5K$, but also changes the maximum height of the production curve. This is unfortunate, as the modeller might be interested in exploring different shapes without altering the maximum productivity.

2.4 Theta-logistic

Theta-logistic

Gilpin and Ayala (1973)

Different from Pella-Tomlinson, which has $\frac{r}{p}$ as the first term. The theta-logistic model has the nice property that r is the initial growth rate, independent of θ . The Pella-Tomlinson model has the nice property that it becomes the Gompertz model as $p \rightarrow 0$.

The theta-logistic model has a problem with low θ values. Maximum production tends towards zero with decreasing θ , so the model will need very large K when θ is small.

2.5 Fletcher

Fletcher

Prager (2002):

The Schaefer model corresponds to $n=2$ where $\gamma=4$,

Prager (2002) describes the shape of the production curve with the unitless ratio $\phi = \frac{B}{K}$, which has a more intuitive meaning than the n exponent. The relationship is:

Insert $n=2$ and note how the Schaefer model corresponds to $\phi = 0.5$, as expected:

2.6 Polacheck

Polacheck

Polacheck et al. (1993)

where p controls the asymmetry of the sustainable yield versus stock biomass relationship.

The authors note that the $\frac{r}{p}$ term is often omitted when the formula is presented.

2.7 Shepherd

Shepherd

3 FLBioDym Class

```
1 qplot(x, ..., data, geom)
```

Listing 1: Simple plotting with qplot

Table 1: plot

Syntax	
x	vector values of one variable of interest
data	<code>data.frame</code> other variables
geom	<code>ggplot</code> object that sets the type of plot to construct, i.e. <code>point</code> , <code>line</code> , <code>histogram</code> .

3.1 Slots

3.2 General Information

3.3 Data

3.4 Fitting

3.5 Results

3.5.1 Reference Points

3.5.2 Diagnostics

4 Uncertainty

4.1 Parametric

4.1.1 Confidence Intervals

4.1.2 Likelihood Ratio Test

4.2 Jackknife

4.3 Bootstrap

5 Management Advice

5.1 Simulations

5.2 Projection

5.2.1 Harvest Control Rules

5.2.2 Kobe

6 Validation and Testing

6.1 Validation

6.2 Testing

7 Examples

7.1 I

References

- Fox, W.W., Jr. 1970. An exponential surplus-yield model for optimizing exploited fish populations. *Trans. Am. Fish. Soc.* 99:80–88.
- Garrod, D.J. 1969. Empirical assessments of catch effort relationships in the North Atlantic cod stock. *ICNAF Res. Bull.* 6:26–34.
- Gilpin, M.E. and F.J. Ayala. 1973. Global models of growth and competition. *Proc. Natl. Acad. Sci. USA* 70:3590–3593.
- Gompertz, B. 1825. On the nature of the function expressive of the law of human mortality, and on a new mode of determining the value of life contingencies. *Phil. Trans. R. Soc. Lond.* 115:513–583.
- Kingsland, S. 1982. The refractory model: The logistic curve and the history of population ecology. *Q. Rev. Biol.* 57:29–52.
- Laloe, F. 1995. Should surplus production models be fishery description tools rather than biological models? *Aquat. Living Resour.* 8:1–16.
- Pella, J.J. and P.K. Tomlinson. 1969. A generalized stock production model. *IATTC Bull.* 13:421–496.
- Polacheck, T., R. Hilborn, and A.E. Punt. 1993. Fitting surplus production models: Comparing methods and measuring uncertainty. *Can. J. Fish. Aquat. Sci.* 50:2597–2607.
- Prager, M.H. 2002. Comparison of logistic and generalized surplus-production models applied to swordfish, *Xiphias gladius*, in the north Atlantic Ocean. *Fish. Res.* 58:41–57.
- Schaefer, M.B. 1954. Some aspects of the dynamics of populations important to the management of the commercial marine fisheries. *IATTC Bull.* 1:27–56.

7.2 Look up later

- Fletcher, R.I. 1978. On the restructuring of the Pella-Tomlinson system. *Fish. Bull.* 76:515–521.
- Fox, W.W., Jr. 1970. An exponential surplus-yield model for optimizing exploited fish populations. *Trans. Am. Fish. Soc.* 99:80–88.
- Garrod, D.J. 1969. Empirical assessments of catch effort relationships in the North Atlantic cod stock. *ICNAF Res. Bull.* 6:26–34.
- Hilborn, R. and C.J. Walters. 1992. *Quantitative fisheries stock assessment: Choice, dynamics and uncertainty.* New York: Chapman and Hall.
- Quinn, T.J., II and R.B. Deriso. 1999. *Quantitative fish dynamics.* New York: Oxford University Press.