

# hyperSpec Introduction

Claudia Beleites <cbeleites@units.it>  
CENMAT, DMRN, University of Trieste

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## Reproducing the Examples in this Vignette

All spectra used in this manual are installed automatically with *hyperSpec*.

The source data files of the **flu** and **laser** data sets as well as of the paracetamol spectrum are shipped with the package. For reproducing the examples in a live session, the full file names of the spectra can be found with the command:

```
> Sys.glob (paste (.libPaths ()), "hyperSpec/doc/rawdata/*.txt", sep = "/")
```

Note that some definitions are executed in **vignette.defs**.

The source data file of the **chondro** data, however, needs to be obtained separately. It is available for download as a .zip file at *hyperSpec*'s home page (<http://r-forge.r-project.org/projects/hyperspec/>, ca. 8.5 MB). The original file (ca. 31 MB) is far too large to be included in the package.

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## 1 Introduction

*hyperSpec* is a R package that allows convenient handling of (hyper)spectral data sets, i.e. data sets comprising spectra together with further data on a per-spectrum basis. The spectra can be anything that is recorded over a common discretized axis, the *so-called* wavelength axis. Throughout the documentation of the package, the terms intensity and wavelength refer to the spectral ordinate and abscissa, respectively.

However, *hyperSpec* works perfectly fine with any data that fits in that general scheme, so that the three terms may also be used for:

wavelength: frequency, wavenumbers, chemical shift, Raman shift,  $\frac{m}{z}$ , etc.

intensity: transmission, absorbance,  $\frac{e^-}{s}$ , ...

extra data: spatial information (spectral images, maps, or profiles), temporal information (kinetics, time series), concentrations (calibration series), class membership information, etc.  
Note that there is no restriction on the number of extra data columns.

This vignette gives an introduction on basic working techniques using the R package *hyperSpec*. It comes with three data sets,

**chondro** a Raman map of chondrocytes in cartilage,

**flu** a set of fluorescence spectra of a calibration series, and

**laser** a time series of an unstable laser emission

In this vignette, all three data sets are used in an intermixed way to illustrate appropriate procedures for different tasks.

In addition, each of the data sets is accompanied by an vignette that shows an exemplary work flow how to analyze the data.

This document describes how to accomplish spectroscopic tasks. It does not give a complete reference on particular functions. It is therefore recommended to look up the methods in R's help system using `? command`.

## 1.1 Notation

This vignette demonstrates working techniques mostly from a spectroscopic point of view: rather than going through the functions provided by *hyperSpec*, it is organized more closely on spectroscopic tasks. However, the functions discussed are printed on the margin for a fast overview.

In R, slots of a S4 class can be accessed directly by the `@` operator. In this vignette, the notation `@xxx` will thus mean “slot *xxx* of an object” see figure 1 on page 5).

Likewise, named elements of a *list*, like the columns of a *data.frame*, are accessed by the `$` operator, and `$xxx` will be used for “column *xxx*”, and as an abbreviation for “column *xxx* of the *data.frame* in slot *data* of the object” see figure 1 on page 5) .

## 2 Remarks on R

### 2.1 Generic Functions

*Generic Functions* are functions that apply to a wide range of data types or classes, e. g. *plot*, *print*, mathematical operators, etc. These functions can be implemented in a specialized way by each class.

*hyperSpec* implements with a variety of such functions, see table 1 on page 6.

## 2.2 Functionality Can be Extended at Runtime

The concept of functions in R offers much flexibility. Functions may be added or changed by the user in his *workspace* at any time. This is also true for methods belonging to a certain class. Neither restart of R nor reloading of the package or anything the like is needed. At the same time, the original function is not deleted, it is just masked by the user's new function but stays accessible if the change should be reverted.

This offers the opportunity of easily writing specialized functions that are adapted to specific tasks. As an example, see the setup of the plotting function for the spectra matrix in section 11.2 (page 16)

## 2.3 Validity Checking

S4 classes have a mechanism to define and enforce that the data actually stored in the object is appropriate for this class. In other words, there is a mechanism of *validity checking*.

The functions provided by *hyperSpec* check the validity of *hyperSpec* objects at the beginning, and — if the validity could be broken by inappropriate arguments — also before leaving the function.

It is highly recommended to use validity checking also for user-defined functions. In addition, non-generic functions need to ensure that the argument actually is a *hyperSpec* object. The two tasks are accomplished by:

```
> .is.hy (object)
> validObject (object)
```

The first line checks whether `object` is a *hyperSpec* object, the second checks its validity. Both functions return TRUE if the checks succeed, otherwise they raise an error and stop.

## 3 Loading the package

To load *hyperSpec*, use

```
> library (hyperSpec)
```

## 4 The structure of hyperSpec objects

*hyperSpec* is a S4 (or new-style) class. It has four so-called *slots* that hold the data:

<code>@wavelength</code>	containing a numeric vector with the wavelength axis of the spectra.
<code>@data</code>	a <i>data.frame</i> with the spectra and all further information belonging to the spectra
<code>@label</code>	a list with appropriate labels (particularly for axis annotations)
<code>@log</code>	a <i>data.frame</i> keeping track of what is done with the object

However, it is good practice to use the functions provided by *hyperSpec* to handle the objects rather than accessing the slots directly. This also helps ensuring that proper (*valid*) objects are retained.

Most of the data is stored in `@data`. This *data.frame* has one special column, `$spec`. It is the column that actually contains the spectra. The spectra are stored in a matrix inside this column, as

Figure 1: The structure of the data in a *hyperSpec* object.

illustrated in figure 1. Even if there are no spectra, `$spc` must still be present but it can contain a matrix with zero columns.

Slot `@label` contains an element for each of the columns in `@data` plus one holding the label for the wavelength axis, `.wavelength`. The elements of the list may be anything suitable for axis annotations, i.e. they should be either character strings or expressions for prettier axis annotations (see figure 3 on page 15). To get familiar with expressions for axis annotation, see

```
> ? plotmath
```

and

```
> demo (plotmath)
```

## 5 Functions provided by hyperSpec

Table 1 and 2 give an overview of the functions implemented by *hyperSpec*. 2 is a reference card providing an overview which functions help to accomplish what (spectroscopic) task.

## 6 Obtaining Basic Information about hyperSpec Objects

As usual, the *print* and *show* methods display information about the object, and *summary* yields some additional details about the data handling done so far:

```
> chondro
```

```
hyperSpec object
  875 spectra
  4 data columns
  300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (875 rows x 4 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix300] rng 80.04420 81.75761 ... 1858.881
  4. clusters: clusters [factor] rng cell lacuna matrix + NA
```

```
> summary (chondro)
```

```
hyperSpec object
  875 spectra
  4 data columns
  300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (875 rows x 4 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix300] rng 80.04420 81.75761 ... 1858.881
```

Table 1: Generic methods implemented by *hyperSpec* and some closely related functions. *Emphasized* names indicate non-generic functions.

Function	Explanation
<code>new ("hyperSpec", ...), initialize</code>	create and initialize an object
<code>validObject</code>	validity checking
<b>Display</b>	
<code>print, show, summary</code>	print information about the object
<code>plot</code>	plotting
<b>Basic information</b>	
<code>dim, ncol, nrow, nwl</code>	the dimensions of the object
<code>dimnames, colnames, rownames</code>	names of the spectra, data columns, and both plus the names of the wavelengths
<b>Parts of the object</b>	
<code>[, [, \$</code>	extract parts of an object
<code>[&lt;-, [[&lt;-, \$&lt;-</code>	assign parts of an object
<code>labels, labels&lt;-</code>	labels for axis annotations etc.
<code>wl, wl&lt;-</code>	access to the wavelength axis
<code>logbook, logentry</code>	logbook and adding a logbook entry
<b>Calculations on the spectra matrix</b>	
<code>+ - * ^ %% %/% / %*%</code>	arithmetical operators work on <code>\$spc</code>
<code>&gt; &lt; == &gt;= &lt;=</code>	comparison operators work on <code>\$spc</code> yielding a logic matrix
<code>all.equal</code>	checking equality of <i>hyperSpec</i> objects on different levels
<code>log, log10, exp, etc.</code>	basic math functions work on <code>\$spc</code> , see also: ? "hyperSpec Math"
<code>min, max, range</code>	minimum, maximum, and range of the intensities in <code>\$spc</code>
<b>Combining and splitting</b>	
<code>cbind, rbind, cbind2, rbind2, bind</code>	combine two objects by columns or rows
<code>split</code>	split an object into a list of objects
<b>Vectorization of calculations</b>	
<code>apply</code>	apply a function row- or column-wise, calculate e.g. the mean spectrum or normalization factors
<code>aggregate (ave)</code>	calculate sum characteristics for groups of spectra, e.g. cluster mean spectra. <i>hyperSpec</i> 's <b>aggregate</b> method covers also the functionality of <b>ave</b> .
<code>sweep</code>	"sweep" a sum characteristic over rows or columns, e.g. centre the data by subtracting the mean spectrum.
<b>Type conversion</b>	
<code>as.character, as.matrix, as.data.frame, as.long.df</code>	type conversion functions
<code>[[, \$</code>	extract parts of an object as data.frame, matrix, or vector

Table 2: Further functions implemented by *hyperSpec*. *Emphasized* names indicate related functions provided by other R packages (package name before the colons).

Function	Explanation
<b>Baseline fitting</b>	
<code>spc.fit.poly</code>	least squares fit of a polynomial
<code>spc.fit.poly.below</code>	least squares fit of a polynomial with automatically determined supporting points (see <code>vignette("baselinebelow")</code> )
<b>Working with the wavelength axis</b>	
<code>spc.bin</code>	spectral binning
<code>spc.loess</code>	<code>loess</code> smoothing interpolation of wavelengths
<code>orderwl</code>	sort columns of spectra matrix according to the wavelengths
<code>wl2i, i2wl</code>	convert wavelengths to column indices for the spectra matrix and vice versa
<b>R internal import</b>	
<code>decomposition</code>	re-import results of decomposition techniques (scores or loadings/latent variables) into a <i>hyperSpec</i> object
<b>Data import/export</b>	
<code>read.txt.long</code> , <code>read.txt.wide</code> , <code>write.txt.long</code> , <code>write.txt.wide</code>	ASCII file import and export
<code>scan.txt.Renishaw</code>	import ASCII files written by Renishaw Wire software
<code>read.ENVI</code>	import ENVI hyperspectral images (works also with missing header files)
<code>read.ENVI.Nicolet</code>	import ENVI files written by Nicolet spectrometer software.
<code>read.spc</code>	import binary spectra files in Thermo Galactic's <code>spc</code> format.
<code>read.spc.KaiserMap</code>	import a collection of <code>.spc</code> files that belong to a Raman map obtained with Kaiser Optical Systems' Hologram software.
<code>R.matlab::readMat</code> , <code>R.matlab::writeMat</code>	package <i>R.Matlab</i> <sup>[1]</sup> provides <code>.mat</code> file import and export
<b>Specialized plotting</b>	
<code>plotspc</code>	spectra plots
<code>plotc</code>	intensity over one other dimension: calibration plots, depth profiles, time series, etc.
<code>plotmap</code>	color-coded intensity over two other dimensions: spectral images and maps, etc.
<code>plotmat</code>	color-coded intensity over wavelength axis and one other dimension: spectra matrix of time series, depth profiles, etc.
<code>stacked.offsets</code>	calculate offset values for stacking spectra or groups of spectra
<code>index.grid</code>	calculate a grid matrix holding the indices of the respective spectra (row indices)
<code>spc.identify</code> , <code>map.identify</code>	identify spectra and wavelength indices by clicking into plots produced by <code>plotspc</code> and <code>plotmap</code>

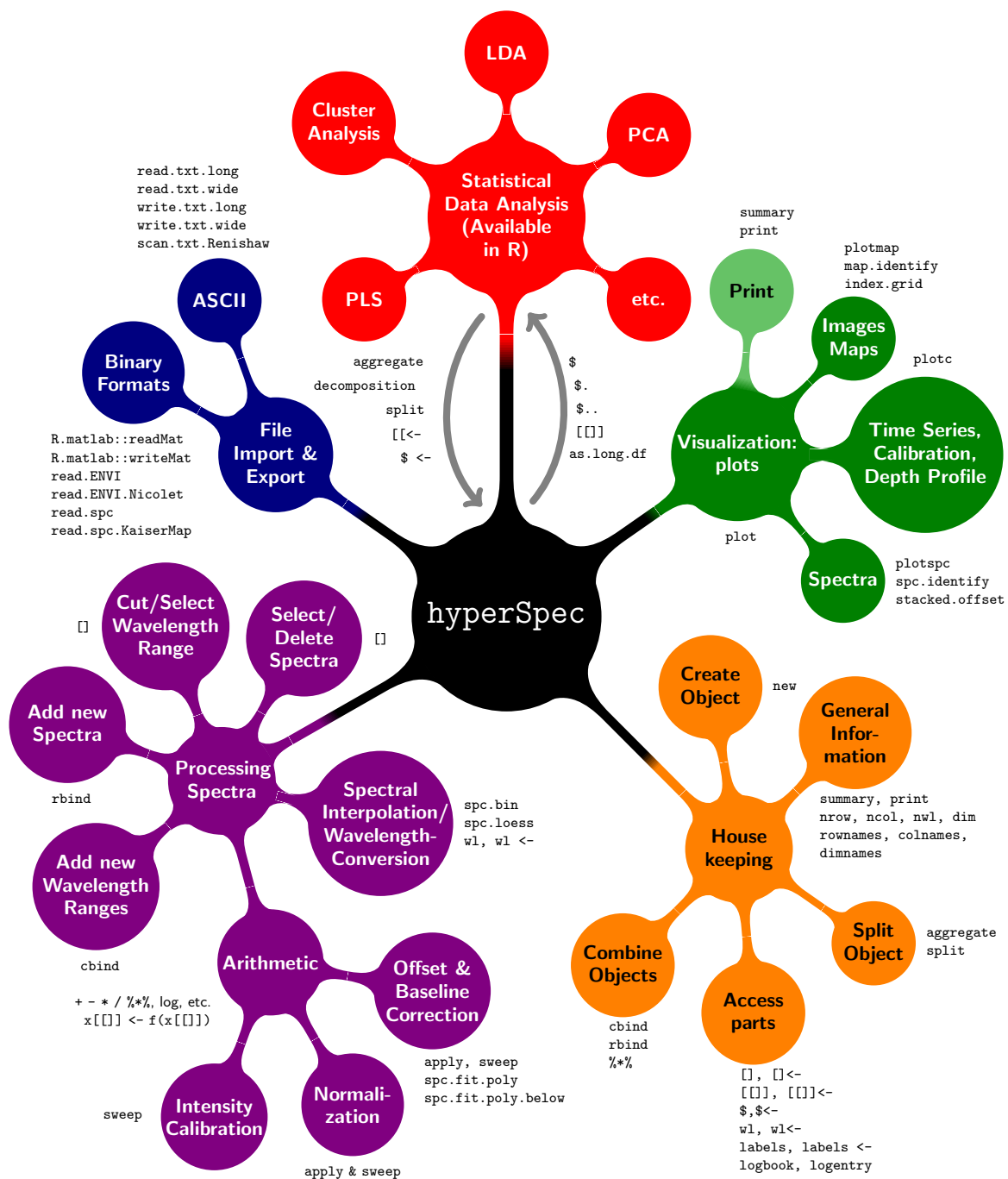


Figure 2: Overview of functions to accomplish common spectroscopic tasks.



Table 3: Utility functions provided by *hyperSpec* that are loosely related to working with spectra.

Function	Explanation
<code>mean_pm_sd</code> , <code>mean_sd</code>	calculate mean and standard deviation, and mean $\pm$ 1 standard deviation, respectively. Convenience function for <code>plotspc</code> , <code>aggregate</code> , etc.
<code>pearson.dist</code>	Pearson’s distance for use with cluster analysis
<code>array2df</code>	convert wide-format array into long-format matrix or data.frame
<code>array2vec</code> , <code>vec2array</code>	index conversion between array and vector notation
<code>wc</code>	try to use <code>wc</code> (word count) if installed on the system
<code>matlab.palette</code> , <code>matlab.dark.palette</code>	color palettes resembling Matlab’s “jet” palette, and a version with darker green values

```

4. clusters: clusters [factor] rng cell lacuna matrix + NA
log:
      short      long      date      user
1 scan.txt.Renishaw list(...) 2010-02-24 10:04:06 cb@cb
2      orderwl list(...) 2010-02-24 10:04:06 cb@cb
3      spc.loess list(...) 2010-02-24 10:04:29 cb@cb
4          $<- list(...) 2010-02-24 10:04:47 cb@cb
5          $<- list(...) 2010-02-24 10:04:47 cb@cb

```

The data set `chondro` consists of 875 spectra with 300 data points each, and 4 data columns: two for the spatial information plus `$spc`. These informations can be directly obtained by

```

> nrow (chondro)

[1] 875

> nwl (chondro)

[1] 300

> ncol (chondro)

[1] 4

> dim (chondro)

nrow ncol nwl
875    4  300

```

The names of the columns in `@data` are accessed by

```

> colnames (chondro)

[1] "y"      "x"      "spc"    "clusters"

```

Likewise, `rownames` returns the names assigned to the spectra, and `dimnames` yields a list of these three vectors (including also the column names of `$spc`).

## 7 Creating a hyperSpec Object, Data Import and Export

*hyperSpec* comes with filters for a variety of file formats. ASCII files are supported for import and export, Matlab files can be read and written with the help of package *R.matlab*. ENVI files can be read (for writing, see e.g. package *caTools*). Also reading of Thermo Galactic's .spc file format is supported.

E.g. to read a spectrum saved in Renishaw's ASCII file format, use:

```
> paracetamol <- scan.txt.Renishaw ("rawdata/paracetamol.txt", "spc")
> paracetamol

hyperSpec object
  1 spectra
  1 data columns
  4064 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 96.7865 98.1432 ... 3200.07
data: (1 rows x 1 columns)
  1. spc: I / a.u. [AsIs matrix x 4064] rng 299.229 317.041 ... 49052.2

> save (paracetamol, file = "paracetamol.rda")
```

Vignette `FileIO` discusses the available filters and also how to derive own filters for importing manufacturer specific data.

### 7.1 Creating a hyperSpec Object from Spectra Matrix and Wavelength Vector

If the data is in R's workspace, a *hyperSpec* object is created by:

```
spc <- new ("hyperSpec", spc = spectra.matrix, wavelength = wavelength.vector, data = extra.data)
```

You will usually give the following arguments:

<code>spc</code>	the spectra matrix
<code>wavelength</code>	the wavelength axis vector
<code>data</code>	the extra data (possibly already including the spectra matrix in column <code>spc</code> )
<code>label</code>	a list with the proper labels. Do not forget the wavelength axis label in <code>\$.wavelength</code> and the spectral intensity axis label in <code>\$spc</code> .

## 8 Decomposition

Matrix decompositions are common operations during chemometric data analysis. The results, e.g. of a principal component analysis are two matrices, the so-called scores and loadings. The results can have either the same number of rows as the spectra matrix they were calculated from (scores-like), or they have as many wavelengths as the spectra (loadings-like).

Both types of result objects can be “re-imported” into *hyperSpec* objects with function `decomposition`. A scores-like object retains all per-spectrum information (i.e. the extra data) while the spectra matrix and wavelength vector are replaced. A loadings-like object retains the wavelength information, while extra data is deleted (set to `NA`) unless the value is constant for all spectra.

For an example, see below (section [13.1](#) on page [22](#)).

## 9 Combining hyperspec Objects

%%

### 9.1 Matrix Multiplication

Matrix multiplication is the reverse of the above mentioned decomposition. Two *hyperSpec* objects can be matrix multiplied by `%%`. Again, this function is discussed with the principal component analysis example below (section 13.1 on page 22).

### 9.2 Binding Objects together

`cbind rbind`

*hyperSpec* Objects can be bound together, either by rows to append a new spectral range or by columns to append new spectra

```
> cbind (chondro [, , 600 ~ 800], chondro [, , 1600 ~ 1800])

hyperSpec object
  875 spectra
  4 data columns
  101 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (875 rows x 4 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix101] rng 80.04420 81.75761 ... 1541.625
  4. clusters: clusters [factor] rng cell lacuna matrix + NA

> rbind (chondro [, , 600 ~ 800], chondro [, , 600 ~ 800])

hyperSpec object
  1750 spectra
  4 data columns
  50 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 798
data: (1750 rows x 4 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix50] rng 195.5281 212.0432 ... 729.5765
  4. clusters: clusters [factor] rng cell lacuna matrix + NA
```

There is also a more general function, `bind`, taking the direction ("`r`" or "`c`") as first argument and then all objects to bind either in separate arguments or in a list.

## 10 Access to the data

### 10.1 Selecting and Deleting Spectra

The extraction function `[]` (or `[]()`, if the spectra *matrix* or the *data.frame* is needed rather than a *hyperSpec* object) takes the spectra as first argument (For detailed help: `? "[]"`). It may be a vector giving the indices of the spectra to extract (select), a vector with negative indices indicating which spectra should be deleted, or a logical

```
> flu [1 : 3]
```

```

hyperSpec object
  3 spectra
  3 data columns
  181 data points / spectrum
wavelength: lambda/nm [numeric] 405.0 405.5 ... 495
data: (3 rows x 3 columns)
  1. file: [factor] rng rawdata/flu1.txt rawdata/flu2.txt rawdata/flu3.txt
  2. spc: I[fl] / a.u. [AsIs matrix x 181] rng 27.15000 32.34467 ... 336.5057
  3. c: c / (mg / l) [numeric] rng 0.05 0.10 0.15

> flu [-3]

hyperSpec object
  5 spectra
  3 data columns
  181 data points / spectrum
wavelength: lambda/nm [numeric] 405.0 405.5 ... 495
data: (5 rows x 3 columns)
  1. file: [factor] rng rawdata/flu1.txt rawdata/flu2.txt rawdata/flu4.txt rawdata/flu5.txt rawdata/flu6.t
  2. spc: I[fl] / a.u. [AsIs matrix x 181] rng 27.15000 32.34467 ... 677.4947
  3. c: c / (mg / l) [numeric] rng 0.05 0.10 0.20 0.25 0.30

> chondro [chondro$y > 10]

hyperSpec object
  350 spectra
  4 data columns
  300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (350 rows x 4 columns)
  1. y: y/(mu * m) [numeric] rng 10.23 11.23 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix300] rng 88.98556 89.99474 ... 1745.724
  4. clusters: clusters [factor] rng cell lacuna matrix

```

## 10.2 Accessing the Extra Data

The second argument of the extraction functions `[]` and `[[[]]]` specifies the (extra) data columns. They can be given like any column specification for a *data.frame*, i. e. numeric, logical, or by a vector of the column names:

```

> colnames(chondro)

[1] "y"          "x"          "spc"        "clusters"

> chondro [[1 : 3, 1]]

      y
1 -4.77
2 -4.77
3 -4.77

> chondro [[1 : 3, -3]]

      y      x clusters
1 -4.77 -11.55 matrix
2 -4.77 -10.55 matrix
3 -4.77  -9.55 matrix

```

```
> chondro [[1 : 3, "x"]]

      x
1 -11.55
2 -10.55
3  -9.55

> chondro [[1 : 3, c (TRUE, FALSE, FALSE)]]

      y clusters
1 -4.77  matrix
2 -4.77  matrix
3 -4.77  matrix
```

To select one column, the `$` operator is more convenient:

```
> flu$c

[1] 0.05 0.10 0.15 0.20 0.25 0.30
```

The extra data may also be set this way:

```
> flu$n <- list (1 : 6, label = "sample no.")
```

This function will append new columns, if necessary.

## 10.3 Wavelengths and Spectral Axis

### 10.3.1 Wavelength Indices

wl2i i2wl

Spectra in *hyperSpec* have always discretized wavelength axes, they are stored in a matrix with column corresponding to one wavelength. *hyperSpec* provides two conversion functions: `i2wl` returns the wavelength corresponding to the given indices and `wl2i` calculates index vectors from wavelengths.

If the wavelengths are given as a numeric vector, they are each converted to the corresponding wavelength. In addition there is a more sophisticated possibility of specifying wavelength ranges using a *formula*. The basic syntax is *start*  $\sim$  *end*. This yields a vector *index of start* : *index of end*.

The result of the formula conversion differs from the numeric vector conversion in three ways:

- The colon operator for constructing vectors accepts only integer numbers, the tilde (for formulas) does not have this restriction.
- If the vector does not take into account the spectral resolution, one may get only every  $n^{th}$  point or repetitions of the same index:

```
> wl2i (flu, 405 : 410)

[1] 1 3 5 7 9 11

> wl2i (flu, 405 ~ 410)

[1] 1 2 3 4 5 6 7 8 9 10 11
```

```
> wl2i (chondro, 1000 : 1010)
[1] 100 101 101 101 101 102 102 102 102 103 103
> wl2i (chondro, 1000 ~ 1010)
[1] 100 101 102 103
```

- If the object's wavelength axis is not ordered, the formula approach doesn't work. In that (rare) case, use `orderwl` first to obtain an object with ordered wavelength axis.

`start` and `end` may contain the special variables `min` and `max` that correspond to the lowest and highest wavelengths of the object:

```
> wl2i (flu, min ~ 410)
[1] 1 2 3 4 5 6 7 8 9 10 11
```

Often, specifications like *wavelength  $\pm n$  data points* are needed. They can be given using complex numbers in the formula. The imaginary part is added to the index calculated from the wavelength in the real part:

```
> wl2i (flu, 450 - 2i ~ 450 + 2i)
[1] 89 90 91 92 93
> wl2i (flu, max - 2i ~ max)
[1] 179 180 181
```

To specify several wavelength ranges, use a list containing the formulas and vectors<sup>1</sup>:

```
> wl2i (flu, 450 - 2i ~ 450 + 2i)
[1] 89 90 91 92 93
> wl2i (flu, c (min ~ 406.5, max - 2i ~ max))
[1] 1 2 3 4 179 180 181
```

This mechanism also works for the wavelength arguments of `[]`, `[]()`, and `plotspc`.

### 10.3.2 Wavelength Axis Conversion

## 10.4 Fast Access to Parts of the hyperSpec Object

`[]` `$.` `$..`

*hyperSpec* comes with three abbreviation functions for easy access to the data:

```
x [[]] returns the spectra matrix (x$spc).
x [[i, , 1]] the cut spectra matrix is returned if wavelengths are specified in l.
x [[i, j, 1]] If data columns are selected (second index), the result is a data.frame.
x [[i, , 1]] <- Also, parts of the spectra matrix can be set (only indices for spectra and wavelength are allowed for this function).
x [i, j] <- sets parts of x@data.
x $. returns the complete data.frame x@data, with the spectra in column $spc.
x $.. returns the extra data (x@data without x$spc).
x $.. <- sets the extra data (x@data without x$spc). However, the columns must match exactly in this case.
```

---

<sup>1</sup>Formulas are combined to a list by `c`.

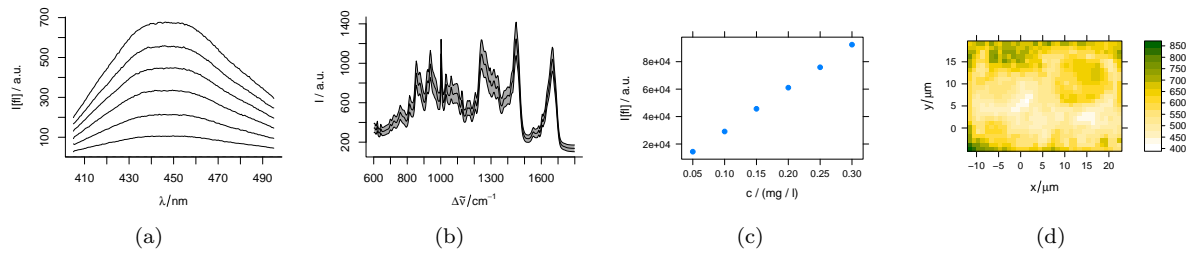


Figure 3: Some example plots. (a) `plotspc (flu)`, (b) `plot (chondro, "spcmeansd")`, (c) `plotc (flu)`, and (d) `plotmap (chondro, col.regions = YG (20))` (using a yellow-green palette).

## 11 Plotting

*hyperSpec* comes with three predefined plotting functions.

`plotspc` plots the spectra, i. e. the intensities `$spc` over the wavelengths `@wavelength`.

`plotmap` plots a false colour map: a single value (e. g. average intensity or cluster membership) over two data columns (default `$x` and `$y`).

`plotc` plots a time series or calibration plot: e. g. an intensity over a single other data column (like concentration, depth, or time).

All three plus some more handy abbreviations are also accessible via `plot`:

`plot`

`plot (flu, "spc")` is equivalent to `plotspc (flu)`

`plot (chondro, "spcmeansd")` plots mean spectrum  $\pm 1$  standard deviation

`plot (chondro, "spcprctl")` plots median, 16<sup>th</sup> and 84<sup>th</sup> percentile. This is similar to `"spcmeansd"`. Spectroscopic data frequently are not Gaussian distributed. The percentiles give a better idea of the true distribution. They are also less sensitive to outliers.

`plot (chondro, "spcprctl5")` like `"spcprctl"` plus 5<sup>th</sup> and 95<sup>th</sup> percentile.

`plot (chondro, "map")` is equivalent to `plotmap (chondro)`

`plot (flu, "c")` is equivalent to `plotc (flu)`

`plot (laser, "ts")` plots a time series plot, equivalent to `plotc (laser, use.c = "t")`

`plot (x, "depth")` plots a depth profile plot, equivalent to `plotc (laser, use.c = "z")`

Figure 3 shows some example plots.

`plot` uses its second argument to determine which of the three specialized plot functions to call. All further arguments are handed over to this function.

### 11.1 Plotting Spectra

`plotspc`

`plotspc` offers a variety of parameters for customized plots. To plot ...

**with reversed abscissa** use `wl.reverse = TRUE`

**in different colours** colours use `col = vector.of.colours`

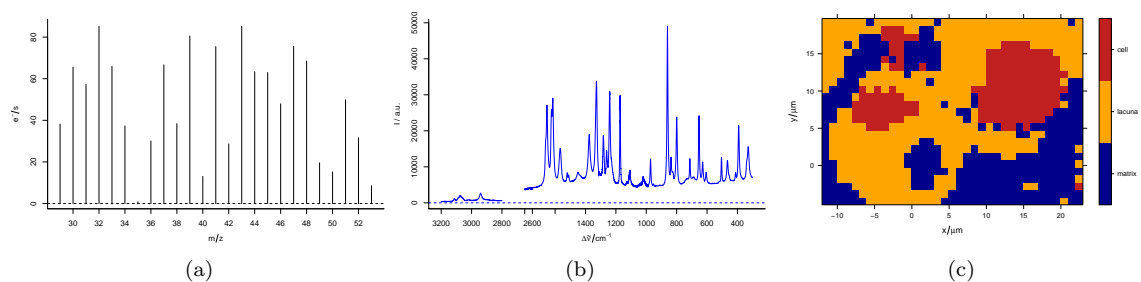


Figure 4: Arguments to `plotspc`. (a) `plot (fake.mass.spec, lines.args = list (type = "h"))` (b) `plotspc (paracetamol, wl.range = c (300 ~ 1800, 2800 ~ max), xoffset = 850, wl.reverse = TRUE)` (c) `plotmap` with a factor, see section 13.2.

**dots instead of lines** use `lines.args = list (pch = 20, type = "p")`

**mass spectra** use `lines.args = list (type = "h")`

**particular wavelength ranges** use `wl.range = list (600 ~ 1800, 2800 ~ 3100)`

If `wl.range` already contains indices: use `wl.index = TRUE`

Cut the wavelength axis appropriately with `xoffset = 800`

**stacked spectra** use `stacked`

**more spectra into an existing plot** use `add = TRUE`

**with different line at  $I = 0$**  use `zeroline = list.of.arguments.to.abline`. `NULL` suppresses the line.

## 11.2 Plotting the Spectra Matrix

It is often useful to plot the spectra against an additional coordinate, e.g. the time for time series, the depth for depth profiles, etc.

This is done by `levelplot`, or by using `plot (object, "mat", model = spc .wavelength * other.data.column)`. The actual plotting is done by `levelplot`, so the plots can be grouped or conditioned. See figure 5

```
> levelplot (spc ~ .wavelength * t, laser, col.regions = YG (20))
```

```
> print (plot (flu, "mat", contour = TRUE, labels = TRUE, col = "#00000080"))
```

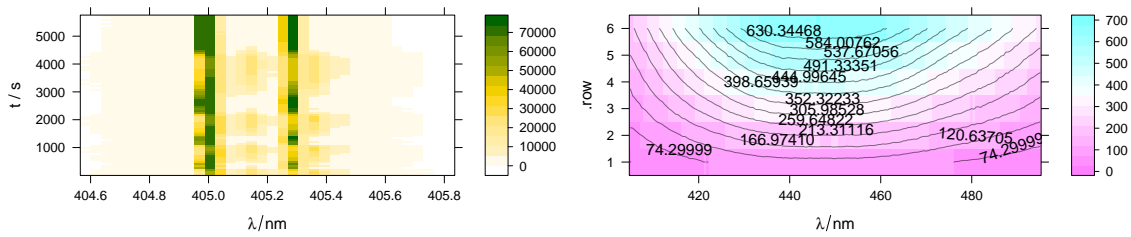
## 11.3 Calibration Plots, (Depth) Profiles, and Time Series Plots

`plotc`

`plotc` plots an intensity over one of the extra data columns. The abscissa uses column `$c` by default, another column can be specified using `use.c = name`. The ordinate can be calculated as a sum characteristic (with parameter `func= function`, defaulting to `sum`). If parameter `z` is given, these values are used instead. `z` may be the name of an extra data column, or a *numeric* that should be used directly.

To customize the plot, give any arguments that you would usually supply to `plot` as a list using argument `plot.args`.





(a) `levelplot (spc ~ wavelength * t, laser,  
col.regions = YG (20))`

(b) `plot (flu, "mat", contour = TRUE, labels =  
TRUE, col = "#00000080")`

Figure 5: plotting the spectra matrix.

## 11.4 Plotting False-Colour Maps

plotmap

`plotmap` uses `levelplot`, a *lattice* function. Therefore, in loops, functions, Sweave chunks, etc. the lattice object needs to be printed explicitly by `print (plotmap (object))` ([R FAQ: Why do lattice/trellis graphics not work?](#)).

`plotmap` produces a 3d plot, with the  $z$  axis colour-coded. `plotmap`'s arguments  $x$  and  $y$  take the name of extra data columns.

**The colour-coded axis.** Also  $z$  can be used to select one column of the extra data by name. Alternatively, it may be a numeric or factor directly giving the values to be used. Each level of a factor will have one colour. It is also possible to plot a sum characteristic of the spectra: supply the function in argument *func*. The default setting is to plot the average intensity (no  $z$  and *func*=`mean`).

To plot with a different palette, use `trellis.args= list (col.regions = palette)`.

**Conditioning.** Lattice graphics have a concept of conditioning a plot. Instead of plotting all data in one diagram, a diagram is produced for each of the groups specified by the condition. `plotmap`'s argument *cond* takes the name of the extra data column used for conditioning. This could e.g. be a column containing the sample number of a *hyperSpec* object that contains several samples.

## 12 Spectral (Pre)processing

### 12.1 Cutting the Spectral Range

□ □□

The extraction functions `[]` and `[[[]]` can be used to cut the spectra: Their third argument takes wavelength specifications as discussed above and also logicals (i.e. vectors specifying with `TRUE/FALSE` for each column of `$spc` whether it should be included or not).

`[]` returns a *hyperSpec* object, `[[[]]` the spectra *matrix*`$spc` (or the *data.frame*`@data` if data columns were specified, too) only.

```
> flu [, , min ~ 408.5]
```

```

hyperSpec object
  6 spectra
  4 data columns
  8 data points / spectrum
wavelength: lambda/nm [numeric] 405.0 405.5 ... 408.5
data: (6 rows x 4 columns)
  1. file: [factor] rng rawdata/flu1.txt rawdata/flu2.txt ... rawdata/flu6.txt
  2. spc: I[fl] / a.u. [AsIs matrix x 8] rng 27.15000 32.34467 ... 256.8913
  3. c: c / (mg / l) [numeric] rng 0.05 0.10 ... 0.3
  4. n: sample no. [integer] rng 1 2 ... 6

> flu [[, c (min ~ min + 2i, max - 2i ~ max)]]

      405      405.5      406      494      494.5      495
[1,] 27.15000 32.34467 33.37867 47.16267 46.41233 45.25633
[2,] 66.80133 63.71533 66.71200 96.60167 96.20600 94.61033
[3,] 93.14433 103.06767 106.19367 149.53900 148.52667 145.79333
[4,] 130.66367 139.99833 143.79767 201.48433 198.86733 195.86733
[5,] 167.26667 171.89833 177.47067 252.06567 248.06700 246.95200
[6,] 198.43033 209.45800 215.78500 307.51850 302.32550 294.64950

```

## 12.2 Spectral Interpolation and Smoothing

Frequently, a *hyperSpec* object needs to be interpolated onto a new wavelength axis. e.g. because measurements resulted in slightly shifted wavelength axes. Or data from a grating spectrometer with unequal data point spacing should be interpolated onto an evenly spaced wavelength axis. Also, the spectra can be smoothed: reducing the spectral resolution allows to increase the signal to noise ratio. For chemometric data analysis reducing the number of data points per spectrum may be crucial as it reduces the dimensionality of the data.

*hyperSpec* provides two functions to change the wavelength axis of *hyperSpec* objects: `spc.bin` and `spc.loess`.

`spc.bin` bins the spectral axis by averaging every *by* data points.

```

> plot (paracetamol, wl.range = c (300 ~ 1800, 2800 ~ max), xoffset = 850)
> p <- spc.loess (paracetamol, c(seq (300, 1800, 2), seq (2850, 3150, 2)))
> plot (p, wl.range = c (300 ~ 1800, 2800 ~ max), xoffset = 850, col = "red", add = TRUE)

```

`spc.loess` applies R's `loess` function for spectral interpolation. Figure 6 shows the result of interpolating from 300 to 1800 and 2850 to 3150  $\text{cm}^{-1}$  with 2  $\text{cm}^{-1}$  data point distance. This corresponds to a spectral resolution of about 4  $\text{cm}^{-1}$ , and the decrease in spectral resolution can be seen at the sharp bands where the maxima are not reached (due to the fact that the interpolation wavelength axis does not necessarily hit the maxima. The original spectrum had 4064 data points with unequal data point spacing (between 0 and 1.4  $\text{cm}^{-1}$ ). The interpolated spectrum has 902 data points.

## 12.3 Background Correction

To subtract a background spectrum of each of the spectra in an object, use `sweep (spectra, 2, background.spectrum, "-")`.

`spc.bin`  
`spc.loess`

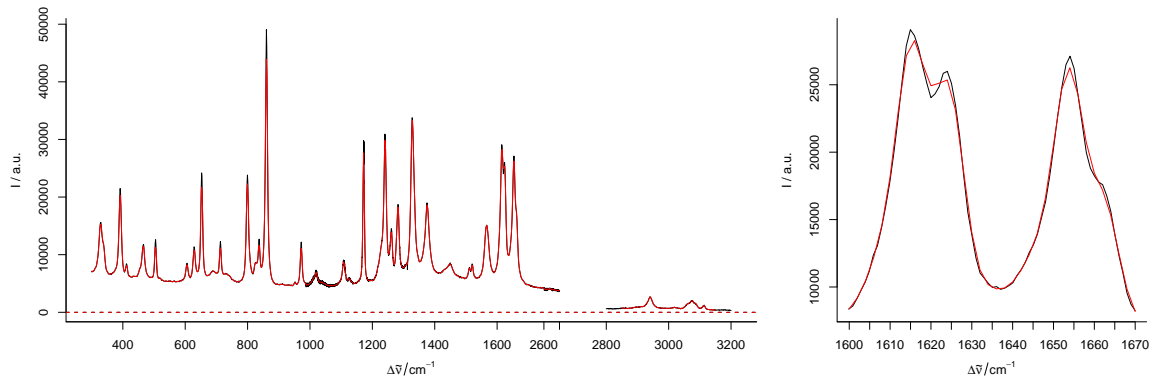


Figure 6: Smoothing interpolation by `spc.loess` with new data point spacing of  $2\text{ cm}^{-1}$ . The magnification on the right shows how interpolation may cause a loss in signal.

## 12.4 Offset Correction

Calculate the offsets and sweep them off the spectra:

```
> offsets <- apply (chondro, 1, min)
> chondro.offset.corrected <- sweep (chondro, 1, offsets, "-")
```

## 12.5 Baseline Correction

*hyperSpec* comes with two functions to fit polynomial baselines.

`spc.fit.poly` fits a polynomial baseline of the given order. A least-squares fit is done so that the function may be used on rather noisy spectra. However, the user must supply an object that is cut appropriately. Particularly, the supplied wavelength ranges are not weighted.

`spc.fit.poly.below` tries to find appropriate support points for the baseline iteratively.

Both functions return a *hyperSpec* object containing the fitted baselines. They need to be subtracted afterwards:

```
> bl <- spc.fit.poly.below (chondro)
Fitting with npts.min = 15
> chondro <- chondro - bl
```

For details, see vignette (`baselinebelow`).

## 12.6 Intensity Calibration

### 12.6.1 Correcting by a constant, e. g. Readout Bias

CCD cameras often operate with a bias, causing a constant value for each pixel. Such a constant can be immediately subtracted:

```
spectra - constant
```

### 12.6.2 Correcting Wavelength Dependence

This means that for each of the wavelengths the same correction needs to be applied to all spectra.

1. There might be wavelength dependent offsets (background or dark spectra). They are subtracted:  
`sweep (spectra, 2, offset.spectrum, "-")`
2. A multiplicative dependency such as a CCD's photon efficiency:  
`sweep (spectra, 2, photon.efficiency, "/")`

### 12.6.3 Spectra Dependent Correction

If the correction depends on the spectra (e.g. due to inhomogeneous illumination while collecting imaging data<sup>2</sup>), the *MARGIN* of the `sweep` function needs to be 1:

1. Pixel dependent offsets are subtracted:  
`sweep (spectra, 2, pixel.offsets, "-")`
2. A multiplicative dependency:  
`sweep (spectra, 2, illumination.factors, "*")`

## 12.7 Normalization

1. Calculate appropriate normalization factors:  
`factors <- 1 / apply (spectra, 1, sum)` for area normalization. `mean` gives equal results, just that the Intensities are on the same scale as before.  
For minimum-maximum-normalization, first do an offset- or baseline correction, then calculate the *factors* using `max`.  
You may calculate the factors using only a certain wavelength range, thereby normalizing on a particular band or peak.
2. Again, sweep the factor off the spectra:  
`normalized <- sweep (spectra, 1, factors, "*")`

```
> factors <- 1 / apply (chondro, 1, mean)
> chondro <- sweep (chondro, 1, factors, "*")
```

## 12.8 Centering the Data

Centering means that the mean spectrum is subtracted from each of the spectra. Many data analysis techniques, like principal component analysis, partial least squares, etc., work much better on centered data.

However, from a spectroscopic point of view it depends on the particular data set whether centering does make sense or not.

It is perfectly fine to centre the `flu` data set: the interpretation is that centering the data cancels the offset (background spectrum etc.) of the calibration:

---

<sup>2</sup>imaging (as opposed to mapping) refers to simultaneously collecting spatially resolved spectra, either 2d images or line imaging.

```
> flu.centered <- sweep (flu, 2, apply (flu, 2, mean), "-")
```

```
> plot (flu.centered)
```

On the other hand, the `chondro` data set consists of Raman spectra, so the spectroscopic interpretation of centering is getting rid of the the average chemical composition of the sample. But: what is the meaning of the “average spectrum” of an inhomogeneous sample? In this case it is better to subtract the minimum spectrum (which will hopefully have almost the same benefit on the data analysis) as it is the spectrum of that chemical composition that is underlying the whole sample.

One more point to consider is that the actual minimum spectrum will pick up lots of the negative noise. In order to avoid that, using e. g. the 5<sup>th</sup> percentile spectrum is more suitable:

```
> chondro <- sweep (chondro, 2, apply (chondro, 2, quantile, 0.05), "-")
```

```
> plot (chondro, "spcprct15")
```

## 12.9 Variance Scaling

Variance scaling is often used in multivariate analysis to adjust the influence and scaling of the variates (that are typically different physical values). However, it is hardly appropriate for spectra that do have the same scale of the same physical value.

## 12.10 Multiplicative Scatter Correction (MSC)

MSC can be done using `msc` from package *pls*[2]. It operates on the spectra matrix:

```
> library (pls)
> chondro.msc <- chondro
> chondro.msc [[]] <- msc (chondro [[]])
```

## 12.11 Spectral Arithmetic

Basic mathematical functions are defined for *hyperSpec* objects. You may convert spectra:  
`absorbance.spectra = - log10 (transmission.spectra)`

In this case, do not forget to adapt the label:

```
> labels (absorbance.spectra)$spc <- "A"
```

Be careful: R’s `log` function calculates the natural logarithm if no base is given.

The basic arithmetic operators work element-wise in R. Thus they all need either a scalar, or a matrix (or *hyperSpec* object) of the correct size.

Matrix multiplication is done by `%*%`, again each of the operands may be a matrix or a *hyperSpec* object, and must have the correct dimensions.

+ - \* / ^ log  
log10

labels

%\*%

## 13 Data Analysis

### 13.1 Data Analysis Methods using a data.frame

#### e. g. Principal Component Analysis with prcomp

The `$.` notation is handy, if a data analysis function expects a *data.frame*. The column names can then be used in the formula:

```
> pca <- prcomp (~ spc, data = chondro$., center = FALSE)
```

Results of such a decomposition can be put again into *hyperSpec* objects. This allows to plot e.g. the loading like spectra, or score maps, see figure 7.

```
> scores <- decomposition (chondro, pca$x, label.wavelength = "PC",
+                           label.spc = "score / a.u.")
> scores

hyperSpec object
  875 spectra
   4 data columns
 300 data points / spectrum
wavelength: PC [integer] 1 2 ... 300
data: (875 rows x 4 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: score / a.u. [AsIs matrix x 300] rng -2.003297 -1.173165 ... 1.918811
  4. clusters: clusters [factor] rng cell lacuna matrix + NA
```

The loadings can be similarly re-imported:

```
> loadings <- decomposition (chondro, t(pca$rotation), scores = FALSE,
+                             label.spc = "loading I / a.u.")
> loadings

hyperSpec object
  300 spectra
   1 data columns
 300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (300 rows x 1 columns)
  1. spc: loading I / a.u. [AsIs matrix x 300] rng -0.4384899 -0.3787975 ... 0.3816652
```

There is, however, one important difference. The loadings are thought of as values computed from all spectra together. Thus no meaningful extra data can be assigned for the loadings object (at least not if the column consists of different values). Therefore, the loadings object lost all extra data (see above).

*retain.columns* triggers whether columns that contain different values should be dropped. If it is set to `TRUE`, the columns are retained, but contain NAs:

```
> loadings <- decomposition (chondro, t(pca$rotation), scores = FALSE,
+                             retain.columns = TRUE, label.spc = "loading I / a.u.")
> loadings[1]$..
```

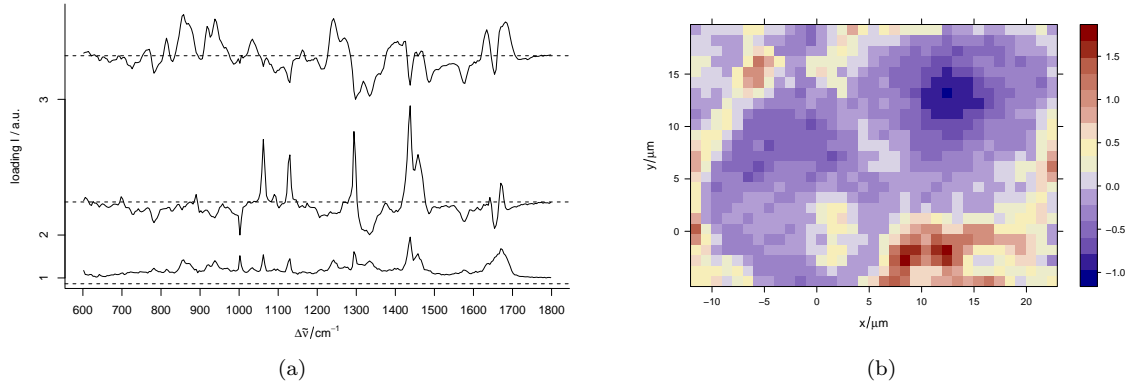


Figure 7: (a) The first three loadings: `plot(loadings[1 : 3], stacked = TRUE)`. (b) The second score map: `plotmap(scores[, , 2])`

```

      y  x clusters
1 NA NA      <NA>

```

If an extra data column does contain only one unique value, it is retained anyways:

```

> chondro$measurement <- 1
> loadings <- decomposition(chondro, t(pca$rotation), scores = FALSE,
+                           label.spc = "loading I / a.u.")
> loadings[1]$..

      measurement
1                1

```

### 13.1.1 PCA as Noise Filter

Principal component analysis is sometimes used as a noise filtering technique. The idea is that the relevant differences are captured in the first components while the higher components contain noise only. Thus the spectra are reconstructed using only the first  $p$  components.

This reconstruction is in fact a matrix multiplication:

$$spectra^{(nrow \times nwl)} = scores^{(nrow \times p)} loadings^{(p \times nwl)}$$

Note that this corresponds to a model based on the Beer-Lambert law:

$$A_n(\lambda) = c_{n,i} \epsilon(i, \lambda) + error$$

The matrix formulation puts the  $n$  spectra into the rows of  $A$  and  $c$ , while the  $i$  pure components appear in the columns of  $c$  and rows of the absorbance coefficients  $\epsilon$ .

For an ideal data set (constituents varying independently, sufficient signal to noise ratio) one would expect the principal component analysis to extract something like the concentrations and pure component spectra.

If we decide that only the first 10 components actually carry spectroscopic information, we can reconstruct spectra with better signal to noise ratio:

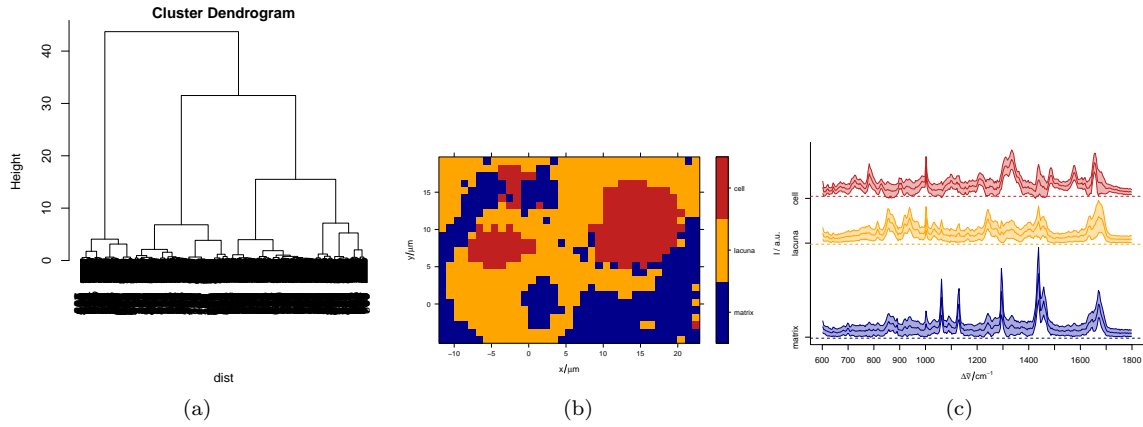


Figure 8: The results of the cluster analysis: (a) the dendrogram (b) the map of the 3 clusters (c) the mean spectra.

```
> smoothed <- scores[, , 1:10] %*% loadings[1:10]
```

Keep in mind, though, that we cannot be sure how much *useful* information was discarded with the higher components. This kind of noise reduction may influence further modeling of the data. Mathematically speaking, the rank of the  $875 \times 300$  spectra matrix was reduced to 10.

## 13.2 Data Analysis Methods using a matrix

### e. g. Hierarchical Cluster Analysis

```
> dist <- pearson.dist (chondro [[]])
> dendrogram <- hclust (dist, method = "ward")

> plot (dendrogram)
```

In order to plot a cluster map, the cluster membership needs to be calculated from the dendrogram. First, cut the dendrogram so that three clusters result:

```
> chondro$clusters <- as.factor (cutree (dendrogram, k = 3))
```

As the cluster membership was stored as factor, the levels can be meaningful names, which are displayed in the color legend.

```
> levels (chondro$clusters) <- c ("matrix", "lacuna", "cell")
```

Then the result may be plotted (figure 8b):

## 13.3 Calculating group-wise Sum Characteristics

### e. g. Cluster Mean Spectra

`aggregate` applies the function given in *FUN* to each of the groups of spectra specified in *by*.

`aggregate`

So we may plot the cluster mean spectra:

```
> means <- aggregate (chondro, by = chondro$clusters, mean_pm_sd)
> plot (means, col = cluster.cols, stacked = ".aggregate", fill = ".aggregate")
```



## 13.4 Splitting an Object

A *hyperSpec* object may also be split into a list of *hyperSpec* objects:

```
> clusters <- split (chondro, chondro$clusters)
> clusters

$matrix
hyperSpec object
  292 spectra
  5 data columns
  300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (292 rows x 5 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix300] rng -0.1372477 -0.1306328 ... 0.9382884
  4. clusters: clusters [factor] rng matrix
  5. measurement: measurement [numeric] rng 1

$lacuna
hyperSpec object
  417 spectra
  5 data columns
  300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (417 rows x 5 columns)
  1. y: y/(mu * m) [numeric] rng -4.77 -3.77 ... 19.23
  2. x: x/(mu * m) [numeric] rng -11.55 -10.55 ... 22.45
  3. spc: I / a.u. [matrix300] rng -0.2540939 -0.2373205 ... 1.043128
  4. clusters: clusters [factor] rng lacuna
  5. measurement: measurement [numeric] rng 1

$cell
hyperSpec object
  166 spectra
  5 data columns
  300 data points / spectrum
wavelength: Delta * tilde(nu)/cm^-1 [numeric] 602 606 ... 1798
data: (166 rows x 5 columns)
  1. y: y/(mu * m) [numeric] rng -2.77 5.23 ... 18.23
  2. x: x/(mu * m) [numeric] rng -7.55 -6.55 ... 22.45
  3. spc: I / a.u. [matrix300] rng -0.2713962 -0.2156510 ... 0.4380194
  4. clusters: clusters [factor] rng cell
  5. measurement: measurement [numeric] rng 1
```

Splitting can be reversed by `rbind` (see section 9.2, page 11).

## References

- [1] Henrik Bengtsson and Jason Riedy. *R.matlab: Read and write of MAT files together with R-to-Matlab connectivity*, 2008. URL <http://www.braju.com/R/>. R package version 1.2.4.
- [2] Ron Wehrens and Bjørn-Helge Mevik. *pls: Partial Least Squares Regression (PLSR) and Principal Component Regression (PCR)*, 2007. URL <http://mevik.net/work/software/pls.html>. R package version 2.1-0.