

Package ‘fitdistrplus’

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Title Help to fit of a parametric distribution to non-censored or censored data

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Depends R (>= 2.8.0)

Description Several functions to help the fit of a parametric distribution to non-censored or censored data. Censored data may contain left censored, right censored and interval censored values, with several lower and upper bounds.

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bootdist

*Bootstrap simulation of uncertainty for non-censored data***Description**

Uses parametric or nonparametric bootstrap resampling in order to simulate uncertainty in the parameters of the distribution fitted to non-censored data.

Usage

```
bootdist(f, bootmethod="param", niter=999)
## S3 method for class 'bootdist':
print(x, ...)
## S3 method for class 'bootdist':
plot(x, ...)
## S3 method for class 'bootdist':
summary(object, ...)
```

Arguments

<code>f</code>	An object of class 'fitdist' result of the function <code>fitdist</code> .
<code>bootmethod</code>	A character string coding for the type of resampling: "param" for a parametric resampling and "nonparam" for a nonparametric resampling of data.
<code>niter</code>	The number of samples drawn by bootstrap.
<code>x</code>	an object of class 'bootdist'.
<code>object</code>	an object of class 'bootdist'.
<code>...</code>	further arguments passed to other methods

Details

Samples are drawn by parametric bootstrap (resampling from the distribution fitted by `fitdist`) or non parametric bootstrap (resampling with replacement from the data set). On each bootstrap sample the function `mledist` or the function `momdist` (according to the component `f$method` of the object of class 'fitdist') is used to estimate bootstrapped values of parameters. When `mledist` fails to converge, NA values are returned. Medians and 2.5 and 97.5 percentiles are computed by removing NA values. The number of iterations for which `mledist` converges is printed in the summary with the medians and the 95 percent confidence intervals of parameters (2.5 and 97.5 percentiles).

The plot of an object of class 'bootdist' consists in a scatterplot or a matrix of scatterplots of the bootstrapped values of parameters. It uses the function `stripchart` when the fitted distribution is characterized by only one parameter, and the function `plot` in other cases. In these last cases, it provides a representation of the joint uncertainty distribution of the fitted parameters.

Value

`bootdist` returns an object of class 'bootdist', a list with 4 components,

<code>estim</code>	a data frame containing the bootstrapped values of parameters.
<code>converg</code>	a vector containing the codes for convergence obtained when using <code>mledist</code> on each bootraped data set or NULL if <code>momdist</code> is used.

method	A character string coding for the type of resampling : "param" for a parametric resampling and "nonparam" for a nonparametric resampling of data.
CI	bootstrap medians and 95 percent confidence intervals of parameters.

Author(s)

Marie-Laure Delignette-Muller <ml.delignette@vet-lyon.fr>

References

Cullen AC and Frey HC (1999) Probabilistic techniques in exposure assessment. Plenum Press, USA, pp. 181-241.

See Also

[fitdist](#), [mledist](#) and [momdist](#).

Examples

```
x1<-c(6.4,13.3,4.1,1.3,14.1,10.6,9.9,9.6,15.3,22.1,13.4,
13.2,8.4,6.3,8.9,5.2,10.9,14.4)

f1<-fitdist(x1,"norm",method="mle")
b1<-bootdist(f1)
print(b1)
plot(b1)
summary(b1)

b1b<-bootdist(f1,bootmethod="nonparam")
summary(b1b)

f1b<-fitdist(x1,"gamma",method="mle")
b1b<-bootdist(f1b)
plot(b1b)

x2<-c(rep(4,1),rep(2,3),rep(1,7),rep(0,12))
f2<-fitdist(x2,"pois",method="mom")
b2<-bootdist(f2)
plot(b2,pch=16)
summary(b2)
```

bootdistcens

Bootstrap simulation of uncertainty for censored data

Description

Uses nonparametric bootstrap resampling in order to simulate uncertainty in the parameters of the distribution fitted to censored data.

Usage

```
bootdistcens(f, niter=999)
## S3 method for class 'bootdistcens':
print(x,...)
## S3 method for class 'bootdistcens':
plot(x,...)
## S3 method for class 'bootdistcens':
summary(object,...)
```

Arguments

<code>f</code>	An object of class 'fitdistcens' result of the function <code>fitdistcens</code> .
<code>niter</code>	The number of samples drawn by bootstrap.
<code>x</code>	an object of class 'bootdistcens'.
<code>object</code>	an object of class 'bootdistcens'.
<code>...</code>	further arguments passed to other methods

Details

Samples are drawn by non parametric bootstrap (resampling with replacement from the data set). On each bootstrap sample the function `mledistcens` is used to estimate bootstrapped values of parameters. When `mledistcens` fails to converge, NA values are returned. Medians and 2.5 and 97.5 percentiles are computed by removing NA values. The number of iterations for which `mledistcens` converges is printed in the summary with the medians and the 95 percent confidence intervals of parameters (2.5 and 97.5 percentiles).

The plot of an object of class 'bootdistcens' consists in a scatterplot or a matrix of scatterplots of the bootstrapped values of parameters. It uses the function `stripchart` when the fitted distribution is characterized by only one parameter, and the function `plot` in other cases. In these last cases, it provides a representation of the joint uncertainty distribution of the fitted parameters.

Value

`bootdistcens` returns an object of class 'bootdistcens', a list with 3 components,

<code>estim</code>	a data frame containing the bootstrapped values of parameters.
<code>converg</code>	a vector containing the codes for convergence obtained when using <code>mledist</code> on each bootraped data set or NULL if <code>momdist</code> is used.
<code>CI</code>	bootstrap medians and 95 percent confidence intervals of parameters.

Author(s)

Marie-Laure Delignette-Muller <ml.delignette@vet-lyon.fr>

References

Cullen AC and Frey HC (1999) Probabilistic techniques in exposure assessment. Plenum Press, USA, pp. 181-241.

See Also

`fitdistcens` and `mledistcens`.

Examples

```
d1<-data.frame(
left=c(1.73,1.51,0.77,1.96,1.96,-1.4,-1.4,NA,-0.11,0.55,
0.41,2.56,NA,-0.53,0.63,-1.4,-1.4,-1.4,NA,0.13),
right=c(1.73,1.51,0.77,1.96,1.96,0,-0.7,-1.4,-0.11,0.55,
0.41,2.56,-1.4,-0.53,0.63,0,-0.7,NA,-1.4,0.13))
f1<-fitdistcens(d1, "norm")
b1<-bootdistcens(f1)
b1
summary(b1)
plot(b1)
```

descdist	<i>Description of an empirical distribution for non-censored data</i>
----------	---

Description

Computes descriptive parameters of an empirical distribution for non-censored data and provides a skewness-kurtosis plot.

Usage

```
descdist(data, discrete=FALSE, boot=NULL, graph=TRUE)
```

Arguments

data	A numeric vector.
discrete	If TRUE, the distribution is considered as discrete.
boot	If not NULL, boot values of skewness and kurtosis are plotted from bootstrap samples of data. boot must be fixed in this case to an integer above 10.
graph	If FALSE, the graph is not plotted.

Details

Minimum, maximum, median, mean, sample sd, sample skewness and sample kurtosis values are printed. A skewness-kurtosis plot such as the one proposed by Cullen and Frey (1999) is given for the empirical distribution. On this plot, values for common distributions are also displayed as a tools to help the choice of distributions to fit to data. In order to take into account the uncertainty of the estimated values of kurtosis and skewness, the data set may be bootstrapped by fixing the argument boot to an integer above 10. boot values of skewness and kurtosis corresponding to the boot bootstrap samples are then computed and reported in blue color on the skewness-kurtosis plot.

If discrete is TRUE, these common distributions are the Poisson, negative binomial and normal distributions. If discrete is FALSE, these are uniform, normal, lognormal, beta and gamma distributions. The Weibull distribution is not represented on the graph but it is indicated on the legend that shapes close to lognormal and gamma distributions may be obtained with this distribution.

Value

descdist returns a list with 7 components,

min	the minimum value
max	the maximum value
median	the median value
mean	the mean value
sd	the standard deviation sample value
skewness	the skewness sample value
kurtosis	the kurtosis sample value

Author(s)

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References

Cullen AC and Frey HC (1999) Probabilistic techniques in exposure assessment. Plenum Press, USA, pp. 81-159. Evans M, Hastings N and Peacock B (2000) Statistical distributions. John Wiley and Sons Inc.

See Also

[plotdist](#)

Examples

```
x1<-c(6.4,13.3,4.1,1.3,14.1,10.6,9.9,9.6,15.3,22.1,13.4,
13.2,8.4,6.3,8.9,5.2,10.9,14.4)
descdist(x1)
descdist(x1,boot=1000)

x2<-c(rep(4,1),rep(2,3),rep(1,7),rep(0,12))
descdist(x2,discrete=TRUE)

x3<-rbeta(100,shape1=0.05,shape2=1)
descdist(x3,boot=1000)
```

fitdist

Fitting of univariate distributions to non-censored data and goodness-of-fit statistics

Description

Fits a univariate distribution to non-censored data by maximum likelihood or matching moments, and computes goodness-of-fit statistics.

Usage

```
fitdist(data, distr, method="mle", start, chisqbreaks, meancount)
## S3 method for class 'fitdist':
print(x,...)
## S3 method for class 'fitdist':
plot(x,breaks="default",...)
## S3 method for class 'fitdist':
summary(object,...)
```

Arguments

<code>data</code>	A numeric vector.
<code>distr</code>	A character string "name" naming a distribution for which the corresponding density function <code>dname</code> , the corresponding distribution function <code>pname</code> and the corresponding quantile function <code>qname</code> must be defined, or directly the density function.
<code>method</code>	A character string coding for the fitting method: "mle" for 'maximum likelihood' and "mom" for 'matching moments'.
<code>start</code>	A named list giving the initial values of parameters of the named distribution. This argument will not be taken into account if <code>method="mom"</code> , and may be omitted for some distributions for which reasonable starting values are computed if <code>method="mle"</code> (see details).
<code>chisqbreaks</code>	A numeric vector defining the breaks of the cells used to compute the chi-squared statistic. If omitted, these breaks are automatically computed from the data in order to reach roughly the same number of observations per cell, roughly equal to the argument <code>meancount</code> , or slightly more if there are some ties.
<code>meancount</code>	The mean number of observations per cell expected for the definition of the breaks of the cells used to compute the chi-squared statistic. This argument will not be taken into account if the breaks are directly defined in the argument <code>chisqbreaks</code> . If <code>chisqbreaks</code> and <code>meancount</code> are both omitted, <code>meancount</code> is fixed in order to obtain roughly $(4n)^{2/5}$ cells with n the length of the dataset.
<code>x</code>	an object of class 'fitdist'.
<code>object</code>	an object of class 'fitdist'.
<code>breaks</code>	If "default" the histogram is plotted with the function <code>hist</code> with its default breaks definition. Else <code>breaks</code> is passed to the function <code>hist</code> . This argument is not taken into account with discrete distributions: "binom", "nbinom", "geom", "hyper" and "pois".
<code>...</code>	further arguments passed to or from other methods

Details

When `method="mle"`, maximum likelihood estimations of the distribution parameters are computed using the function `mledist`. Direct optimization of the log-likelihood is performed using `optim`, with its default method "Nelder-Mead" for distributions characterized by more than one parameter and the method "BFGS" for distributions characterized by only one parameter. For the following named distributions, reasonable starting values will be computed if `start` is omitted: "norm", "lnorm", "exp" and "pois", "cauchy", "gamma", "logis", "nbinom" (parametrized by `mu` and `size`), "geom", "beta" and "weibull". Note that these starting values may not be good enough if the fit is poor. The function is not able to fit a uniform distribution.

With the parameter estimates, the function returns the log-likelihood and the standard errors of the estimates calculated from the Hessian at the solution found by `optim`.

When `method="mom"`, the estimated values of the distribution parameters are provided only for the following distributions : "norm", "lnorm", "pois", "exp", "gamma", "nbinom", "geom", "beta", "unif" and "logis". For distributions characterized by one parameter ("geom", "pois" and "exp"), this parameter is simply estimated by matching theoretical and observed means, and for distributions characterized by two parameters, these parameters are estimated by matching theoretical and observed means and variances (Vose, 2000).

Goodness-of-fit statistics are computed. The Chi-squared statistic is computed using cells defined by the argument `chisqbreaks` or cells automatically defined from the data in order to reach roughly the same number of observations per cell, roughly equal to the argument `meancount`, or slightly more if there are some ties. If `chisqbreaks` and `meancount` are both omitted, `meancount` is fixed in order to obtain roughly $(4n)^{2/5}$ cells, with n the length of the dataset (Vose, 2000). The Chi-squared statistic is not computed if the program fails to define enough cells due to a too small dataset. When the Chi-squared statistic is computed, and if the degree of freedom (nb of cells - nb of parameters - 1) of the corresponding distribution is strictly positive, the p-value of the Chi-squared test is returned.

For the distributions assumed continuous (all but "binom", "nbinom", "geom", "hyper" and "pois"), Kolmogorov-Smirnov and Anderson-Darling statistics are also computed, as defined by Cullen and Frey (1999).

An approximate Kolmogorov-Smirnov test is performed by assuming the distribution parameters known. The critical value defined by Stephens (1986) for a completely specified distribution is used to reject or not the distribution at the significance level 0.05. Because of this approximation, the result of the test (decision of rejection of the distribution or not) is returned only for datasets with more than 30 observations. Note that this approximate test may be too conservative.

For datasets with more than 5 observations and for distributions for which the test is described by Stephens (1986) ("norm", "lnorm", "exp", "cauchy", "gamma", "logis" and "weibull"), the Anderson-darling test is performed as described by Stephens (1986). This test takes into account the fact that the parameters are not known but estimated from the data. The result is the decision to reject or not the distribution at the significance level 0.05.

The plot of an object of class "fitdist" returned by `fitdist` uses the function `plotdist`.

Value

`fitdist` returns an object of class 'fitdist', a list with 16 components,

<code>estimate</code>	the parameter estimates
<code>method</code>	the character string coding for the fitting method : "mle" for 'maximum likelihood' and "mom" for 'matching moments'
<code>sd</code>	the estimated standard errors or NULL if <code>method="mom"</code>
<code>cor</code>	the estimated correlation matrix or NULL if <code>method="mom"</code>
<code>loglik</code>	the log-likelihood or NULL if <code>method="mom"</code>
<code>n</code>	the length of the data set
<code>data</code>	the dataset
<code>distname</code>	the name of the distribution
<code>chisq</code>	the Chi-squared statistic or NULL if not computed
<code>chisqbreaks</code>	breaks used to define cells in the Chi-squared statistic

chisqpvalue	p-value of the Chi-squared statistic or NULL if not computed
chisqdf	degree of freedom of the Chi-squared distribution or NULL if not computed
chisqtable	a table with observed and theoretical counts used for the Chi-squared calculations
ad	the Anderson-Darling statistic or NULL if not computed
adtest	the decision of the Anderson-Darling test or NULL if not computed
ks	the Kolmogorov-Smirnov statistic or NULL if not computed
kstest	the decision of the Kolmogorov-Smirnov test or NULL if not computed

Author(s)

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References

- Cullen AC and Frey HC (1999) Probabilistic techniques in exposure assessment. Plenum Press, USA, pp. 81-155.
- Stephens MA (1986) Tests based on edf statistics. In Goodness-of-fit techniques (D'Agostino RB and Stephens MA, eds), Marcel dekker, New York, pp. 97-194.
- Venables WN and Ripley BD (2002) Modern applied statistics with S. Springer, New York, pp. 435-446.
- Vose D (2000) Risk analysis, a quantitative guide. John Wiley & Sons Ltd, Chichester, England, pp. 99-143.

See Also

[plotdist](#), [optim](#), [mledist](#), [momdist](#) and [fitdistcens](#).

Examples

```
x1<-c(6.4,13.3,4.1,1.3,14.1,10.6,9.9,9.6,15.3,22.1,13.4,
13.2,8.4,6.3,8.9,5.2,10.9,14.4)
f1<-fitdist(x1,"norm")
print(f1)
plot(f1)
summary(f1)
f1$chisqtable

f1b<-fitdist(x1,"norm",method="mom",meancount=6)
summary(f1b)
f1b$chisqtable

f1c<-fitdist(x1,"lnorm",method="mom",meancount=6)
summary(f1c)
f1c$chisqtable

dgumbel<-function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel<-function(q,a,b) exp(-exp((a-q)/b))
qgumbel<-function(p,a,b) a-b*log(-log(p))
f1c<-fitdist(x1,"gumbel",start=list(a=10,b=5))
print(f1c)
plot(f1c)
```

```

x2<-c(rep(4,1),rep(2,3),rep(1,7),rep(0,12))
f2<-fitdist(x2,"pois",chisqbreaks=c(0,1))
plot(f2)
summary(f2)
f2$chisqtable

xw<-rweibull(n=100,shape=2,scale=1)
fa<-fitdist(xw,"weibull")
summary(fa)
fa$chisqtable
fb<-fitdist(xw,"gamma")
summary(fb)
fc<-fitdist(xw,"exp")
summary(fc)

```

fitdistcens

*Fitting of univariate distributions to censored data***Description**

Fits a univariate distribution to censored data by maximum likelihood.

Usage

```

fitdistcens(censdata, distr, start)
## S3 method for class 'fitdistcens':
print(x,...)
## S3 method for class 'fitdistcens':
plot(x,...)
## S3 method for class 'fitdistcens':
summary(object,...)

```

Arguments

censdata	A dataframe of two columns respectively named <code>left</code> and <code>right</code> , describing each observed value as an interval. The <code>left</code> column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The <code>right</code> column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observations.
distr	A character string "name" naming a distribution, for which the corresponding density function <code>dname</code> and the corresponding distribution function <code>pname</code> must be defined, or directly the density function.
start	A named list giving the initial values of parameters of the named distribution. This argument may be omitted for some distributions for which reasonable starting values are computed (see details).
x	an object of class 'fitdistcens'.
object	an object of class 'fitdistcens'.
...	further arguments passed to or from other methods

Details

Maximum likelihood estimations of the distribution parameters are computed using the function `mledistcens`. Maximum likelihood estimations of the distribution parameters are computed. Direct optimization of the log-likelihood is performed using `optim`, with its default method "Nelder-Mead" for distributions characterized by more than one parameter and the method "BFGS" for distributions characterized by only one parameter. For the following named distributions, reasonable starting values will be computed if `start` is omitted: "norm", "lnorm", "exp" and "pois", "cauchy", "gamma", "logis", "nbinom" (parametrized by `mu` and `size`), "geom", "beta" and "weibull". Note that these starting values may not be good enough if the fit is poor. The function is not able to fit a uniform distribution. With the parameter estimates, the function returns the log-likelihood and the standard errors of the estimates calculated from the Hessian at the solution found by `optim`.

The plot of an object of class "fitdistcens" returned by `fitdistcens` uses the function `plotdistcens`.

Value

`fitdistcens` returns an object of class 'fitdistcens', a list with 5 components,

<code>estimate</code>	the parameter estimates
<code>sd</code>	the estimated standard errors
<code>cor</code>	the estimated correlation matrix
<code>loglik</code>	the log-likelihood
<code>censdata</code>	the censored dataset
<code>distname</code>	the name of the distribution

Author(s)

Marie-Laure Delignette-Muller <ml.delignette@vet-lyon.fr>

References

Venables WN and Ripley BD (2002) Modern applied statistics with S. Springer, New York, pp. 435-446.

See Also

`plotdistcens`, `optim`, `mledistcens` and `fitdist`.

Examples

```
d1<-data.frame(
  left=c(1.73,1.51,0.77,1.96,1.96,-1.4,-1.4,NA,-0.11,0.55,0.41,
        2.56,NA,-0.53,0.63,-1.4,-1.4,-1.4,NA,0.13),
  right=c(1.73,1.51,0.77,1.96,1.96,0,-0.7,-1.4,-0.11,0.55,0.41,
        2.56,-1.4,-0.53,0.63,0,-0.7,NA,-1.4,0.13))
f1n<-fitdistcens(d1, "norm")
f1n
summary(f1n)
plot(f1n,rightNA=3)

dgumbel<-function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel<-function(q,a,b) exp(-exp((a-q)/b))
f1g<-fitdistcens(d1,"gumbel",start=list(a=0,b=2))
```

```
summary(flg)
plot(flg, rightNA=3)

d3<-data.frame(left=10^(d1$left), right=10^(d1$right))
f3w<-fitdistcens(d3, "weibull")
summary(f3w)
plot(f3w, leftNA=0)
f3l<-fitdistcens(d3, "lnorm")
summary(f3l)
plot(f3l, leftNA=0)
f3e<-fitdistcens(d3, "exp")
summary(f3e)
plot(f3e, leftNA=0)
```

mledist

Maximum likelihood fitting of univariate distributions

Description

Fits a univariate distribution by maximum likelihood using the optimization function [optim](#).

Usage

```
mledist(data, distr, start)
```

Arguments

data	A numeric vector.
distr	A character string "name" naming a distribution for which the corresponding density function <code>dname</code> must be defined, or directly the density function.
start	A named list giving the initial values of parameters of the named distribution. This argument may be omitted for some distributions for which reasonable starting values are computed (see details).

Details

Maximum likelihood estimations of the distribution parameters are computed. Direct optimization of the log-likelihood is performed using [optim](#), with its default method "Nelder-Mead" for distributions characterized by more than one parameter and the method "BFGS" for distributions characterized by only one parameter. For the following named distributions, reasonable starting values will be computed if `start` is omitted: "norm", "lnorm", "exp" and "pois", "cauchy", "gamma", "logis", "nbinom" (parametrized by `mu` and `size`), "geom", "beta" and "weibull". Note that these starting values may not be good enough if the fit is poor. The function is not able to fit a uniform distribution.

This function is not intended to be called directly but is internally called in [fitdist](#) and [bootdist](#) when used with the maximum likelihood method.

Value

mledist returns a list with 4 components,

estimate	the parameter estimates
convergence	an integer code for the convergence of <code>optim</code> . 0 indicates successful convergence. 1 indicates that the iteration limit of <code>optim</code> has been reached. 10 indicates degeneracy of the Nelder-Mead simplex. 100 indicates that <code>optim</code> encountered an internal error.
loglik	the log-likelihood
hessian	a symmetric matrix computed by <code>optim</code> as an estimate of the Hessian at the solution found. It is used in <code>fitdist</code> to estimate standard errors.

Author(s)

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References

Venables WN and Ripley BD (2002) Modern applied statistics with S. Springer, New York, pp. 435-446.

See Also

[momdist](#), [fitdist](#), [optim](#) and [bootdist](#).

Examples

```
x1<-c(6.4,13.3,4.1,1.3,14.1,10.6,9.9,9.6,15.3,22.1,13.4,
13.2,8.4,6.3,8.9,5.2,10.9,14.4)
mledist(x1,"norm")

dgumbel<-function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
mledist(x1,"gumbel",start=list(a=10,b=5))

x2<-c(rep(4,1),rep(2,3),rep(1,7),rep(0,12))
mledist(x2,"pois")
mledist(x2,"nbinom")

x3<-c(0.80,0.72,0.88,0.84,0.38,0.64,0.69,0.48,0.73,0.58,0.81,
0.83,0.71,0.75,0.59)
mledist(x3,"beta")
```

mledistcens	<i>Maximum likelihood fitting of univariate distributions from censored data</i>
-------------	--

Description

Fits a univariate distribution from censored data by maximum likelihood using the optimization function `optim`.

Usage

```
mledistcens(censdata, distr, start)
```

Arguments

<code>censdata</code>	A dataframe of two columns respectively named <code>left</code> and <code>right</code> , describing each observed value as an interval. The <code>left</code> column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The <code>right</code> column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observations.
<code>distr</code>	A character string "name" naming a distribution, for which the corresponding density function <code>dname</code> and the corresponding distribution function <code>pname</code> must be defined, or directly the density function.
<code>start</code>	A named list giving the initial values of parameters of the named distribution. This argument may be omitted for some distributions for which reasonable starting values are computed (see details).

Details

Maximum likelihood estimations of the distribution parameters are computed. Direct optimization of the log-likelihood is performed using `optim`, with its default method "Nelder-Mead" for distributions characterized by more than one parameter and the method "BFGS" for distributions characterized by only one parameter. For the following named distributions, reasonable starting values will be computed if `start` is omitted: "norm", "lnorm", "exp" and "pois", "cauchy", "gamma", "logis", "nbinom" (parametrized by `mu` and `size`), "geom", "beta" and "weibull". Note that these starting values may not be good enough if the fit is poor. The function is not able to fit a uniform distribution.

This function is not intended to be called directly but is internally called in `fitdistcens` and `bootdistcens`.

Value

`mledistcens` returns a list with 4 components,

<code>estimate</code>	the parameter estimates
<code>convergence</code>	an integer code for the convergence of <code>optim</code> . 0 indicates successful convergence. 1 indicates that the iteration limit of <code>optim</code> has been reached.

	10 indicates degeneracy of the Nealder-Mead simplex.
	100 indicates that <code>optim</code> encountered an internal error.
<code>loglik</code>	the log-likelihood
<code>hessian</code>	a symmetric matrix computed by <code>optim</code> as an estimate of the Hessian at the solution found. It is used in <code>fitdistcens</code> to estimate standard errors.

Author(s)

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References

Venables WN and Ripley BD (2002) Modern applied statistics with S. Springer, New York, pp. 435-446.

See Also

`fitdistcens`, `optim` and `bootdistcens`.

Examples

```
dl<-data.frame(
  left=c(1.73,1.51,0.77,1.96,1.96,-1.4,-1.4,NA,-0.11,0.55,0.41,
        2.56,NA,-0.53,0.63,-1.4,-1.4,-1.4,NA,0.13),
  right=c(1.73,1.51,0.77,1.96,1.96,0,-0.7,-1.4,-0.11,0.55,0.41,
        2.56,-1.4,-0.53,0.63,0,-0.7,NA,-1.4,0.13))
mledistcens(dl,"norm")

dgumbel<-function(x,a,b) 1/b*exp((a-x)/b)*exp(-exp((a-x)/b))
pgumbel<-function(q,a,b) exp(-exp((a-q)/b))
mledistcens(dl,"gumbel",start=list(a=0,b=2))
```

momdist

Fitting of univariate distributions by matching moments

Description

Fits a univariate distribution by matching moments.

Usage

```
momdist(data, distr)
```

Arguments

<code>data</code>	A numeric vector.
<code>distr</code>	A character string "name" naming a distribution or directly the density function <code>dname</code> . The estimated values of the distribution parameters are provided only for the following distributions : "norm", "lnorm", "exp" and "pois", "gamma", "logis", "nbinom", "geom", "beta" and "unif".

Details

For distributions characterized by one parameter ("geom", "pois" and "exp"), this parameter is simply estimated by matching theoretical and observed means, and for distributions characterized by two parameters, these parameters are estimated by matching theoretical and observed means and variances (Vose, 2000).

This function is not intended to be called directly but is internally called in `fitdist` and `bootdist` when used with the matching moments method.

Value

`momdist` returns the named parameter or a named vector of parameters.

Author(s)

Marie-Laure Delignette-Muller (ml.delignette@vet-lyon.fr)

References

Vose D (2000) Risk analysis, a quantitative guide. John Wiley & Sons Ltd, Chichester, England, pp. 99-143. Evans M, Hastings N and Peacock B (2000) Statistical distributions. John Wiley and Sons Inc.

See Also

`mledist`, `fitdist` and `bootdist`.

Examples

```
x1<-c(6.4,13.3,4.1,1.3,14.1,10.6,9.9,9.6,15.3,22.1,13.4,
13.2,8.4,6.3,8.9,5.2,10.9,14.4)
momdist(x1,"norm")

x2<-c(rep(4,1),rep(2,3),rep(1,7),rep(0,12))
momdist(x2,"pois")

x3<-c(0.80,0.72,0.88,0.84,0.38,0.64,0.69,0.48,0.73,0.58,0.81,
0.83,0.71,0.75,0.59)
momdist(x3,"beta")
```

plotdist

Plot of empirical and theoretical distributions for non-censored data

Description

Plots an empirical distribution (non-censored data) with a theoretical one if specified.

Usage

```
plotdist(data,distr,para,breaks="default",discrete=FALSE,...)
```


Arguments

<code>data</code>	A numeric vector.
<code>distr</code>	A character string "name" naming a distribution for which the corresponding density function <code>dname</code> , the corresponding distribution function <code>pname</code> and the corresponding quantile function <code>qname</code> must be defined, or directly the density function. This argument may be omitted only if <code>para</code> is omitted.
<code>para</code>	A named list giving the parameters of the named distribution. This argument may be omitted only if <code>distname</code> is omitted.
<code>breaks</code>	If "default" the histogram is plotted with the function <code>hist</code> with its default breaks definition. Else <code>breaks</code> is passed to the function <code>hist</code> . This argument is not taken into account if <code>discrete</code> is TRUE.
<code>discrete</code>	If TRUE, the distribution is considered as discrete. This argument is not taken into account if <code>distname</code> is defined. In this last case, the distribution is automatically assumed discrete if and only if <code>distname</code> is "binom", "nbinom", "geom", "hyper" or "pois".
<code>...</code>	further graphical arguments passed to other methods

Details

Empirical and, if specified, theoretical distributions are plotted in density and in cdf. For continuous distributions, the function `hist` is used with its default breaks definition if `breaks` is "default" or passing `breaks` as an argument if it differs from "default". For continuous distribution and when a theoretical distribution is specified by both arguments `distname` and `para`, Q-Q plot and P-P plot are also plotted (Cullen and Fray, 1999). The function `ppoints` is used for the Q-Q plot, to generate the set of probabilities at which to evaluate the inverse distribution.

Author(s)

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References

Cullen AC and Frey HC (1999) Probabilistic techniques in exposure assessment. Plenum Press, USA, pp. 81-159.

See Also

`descdist`, `hist`, `plotdistcens` and `ppoints`.

Examples

```
x1<-c(6.4,13.3,4.1,1.3,14.1,10.6,9.9,9.6,15.3,22.1,13.4,
13.2,8.4,6.3,8.9,5.2,10.9,14.4)
plotdist(x1)

x2<-c(rep(4,1),rep(2,3),rep(1,7),rep(0,12))
plotdist(x2,discrete=TRUE)
plotdist(x2,"pois",para=list(lambda=mean(x2)))

xn<-rnorm(n=100,mean=10,sd=5)
plotdist(xn,"norm",para=list(mean=mean(xn),sd=sd(xn)))
```

plotdistcens

*Plot of empirical and theoretical distributions for censored data***Description**

Plots an empirical distribution for censored data with a theoretical one if specified.

Usage

```
plotdistcens(censdata, distr, para, leftNA=-Inf, rightNA=Inf, ...)
```

Arguments

<code>censdata</code>	A dataframe of two columns respectively named <code>left</code> and <code>right</code> , describing each observed value as an interval. The <code>left</code> column contains either NA for left censored observations, the left bound of the interval for interval censored observations, or the observed value for non-censored observations. The <code>right</code> column contains either NA for right censored observations, the right bound of the interval for interval censored observations, or the observed value for non-censored observations.
<code>distr</code>	A character string "name" naming a distribution, for which the corresponding density function <code>dname</code> and the corresponding distribution function <code>pname</code> must be defined, or directly the density function.
<code>para</code>	A named list giving the parameters of the named distribution. This argument may be omitted only if <code>distrname</code> is omitted.
<code>leftNA</code>	the real value of the left bound of left censored observations : <code>-Inf</code> or a finite value such as 0 for positive data for example.
<code>rightNA</code>	the real value of the right bound of right censored observations : <code>Inf</code> or a finite value such as a realistic maximum value.
<code>...</code>	further graphical arguments passed to other methods

Details

Empirical and, if specified, theoretical distributions are plotted in cdf. Data are reported directly as segments for interval, left and right censored data, and as points for non-censored data. Before plotting, observations are ordered and a rank `r` is associated to each of them. Left censored observations are ordered first, by their right bounds. Interval censored and non censored observations are then ordered by their mid-points and, at last, right censored observations are ordered by their left bounds. If `leftNA` (resp. `rightNA`) is finite, left censored (resp. right censored) observations are considered as interval censored observations and ordered by mid-points with non-censored and interval censored data. It is sometimes necessary to fix `rightNA` or `leftNA` to a realistic extreme value, even if not exactly known, to obtain a reasonable global ranking of observations.

After ranking, each of the `n` observations is plotted as a point (one x-value) or a segment (an interval of possible x-values), with an y-value equal to `r/n`, `r` being the rank of each observation in the global ordering previously described.

Author(s)

Marie-Laure Delignette-Muller <ml.delignette@vet-lyon.fr>

See Also[plotdist.](#)**Examples**

```
d1<-data.frame(  
  left=c(1.73,1.51,0.77,1.96,1.96,-1.4,-1.4,NA,-0.11,0.55,  
         0.41,2.56,NA,-0.53,0.63,-1.4,-1.4,-1.4,NA,0.13),  
  right=c(1.73,1.51,0.77,1.96,1.96,0,-0.7,-1.4,-0.11,0.55,  
         0.41,2.56,-1.4,-0.53,0.63,0,-0.7,NA,-1.4,0.13))  
plotdistcens(d1)  
plotdistcens(d1,rightNA=3)  
plotdistcens(d1,"norm",para=list(mean=0.12,sd=1.4),rightNA=3)  
  
d3<-data.frame(left=10^(d1$left),right=10^(d1$right))  
plotdistcens(d3,leftNA=0)  
plotdistcens(d3,"lnorm",para=list(meanlog=0.27,sdlog=3.3),leftNA=0)
```

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