



York Health Economics Consortium



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Investigating Input Correlation in Probabilistic Sensitivity Analysis

HARRIET FEWSTER, Statistician

ERIN BARKER, Senior Statistician

KARINA WATTS, Medical Writer

DR EMILY GREGG, Senior Medical Writer

PROFESSOR MATTHEW TAYLOR, Director

harriet.fewster@york.ac.uk

www.yhec.co.uk



Background

PSA is used to characterise uncertainty in cost-effectiveness models.

Inputs in PSA are often varied independently even when they may be correlated¹. As a result, PSA results could be misestimating uncertainty.

Uncertainty is a key factor for HTA agencies when deciding whether to approve an intervention.

¹Lanitis T, Muszbek N, Tichy E. The Probability of a Successful Probabilistic Sensitivity Analysis. *The Evidence Forum*. 2014:30-33

Methods

Eight-state Markov model to compare a hypothetical treatment and comparator.

R and Shiny used for ease of programming and user-friendly interface.

Parameters varied in PSA (per health state)

- Five costs
- One QALY value
- Eight transition probabilities

Correlation options

- No correlation
- Partial correlation (within but not between costs, QALYs and transition matrices)
- Perfect correlation

R model

Function to generate n PSA samples of a single cost

No correlation: costs are i.i.d. gamma

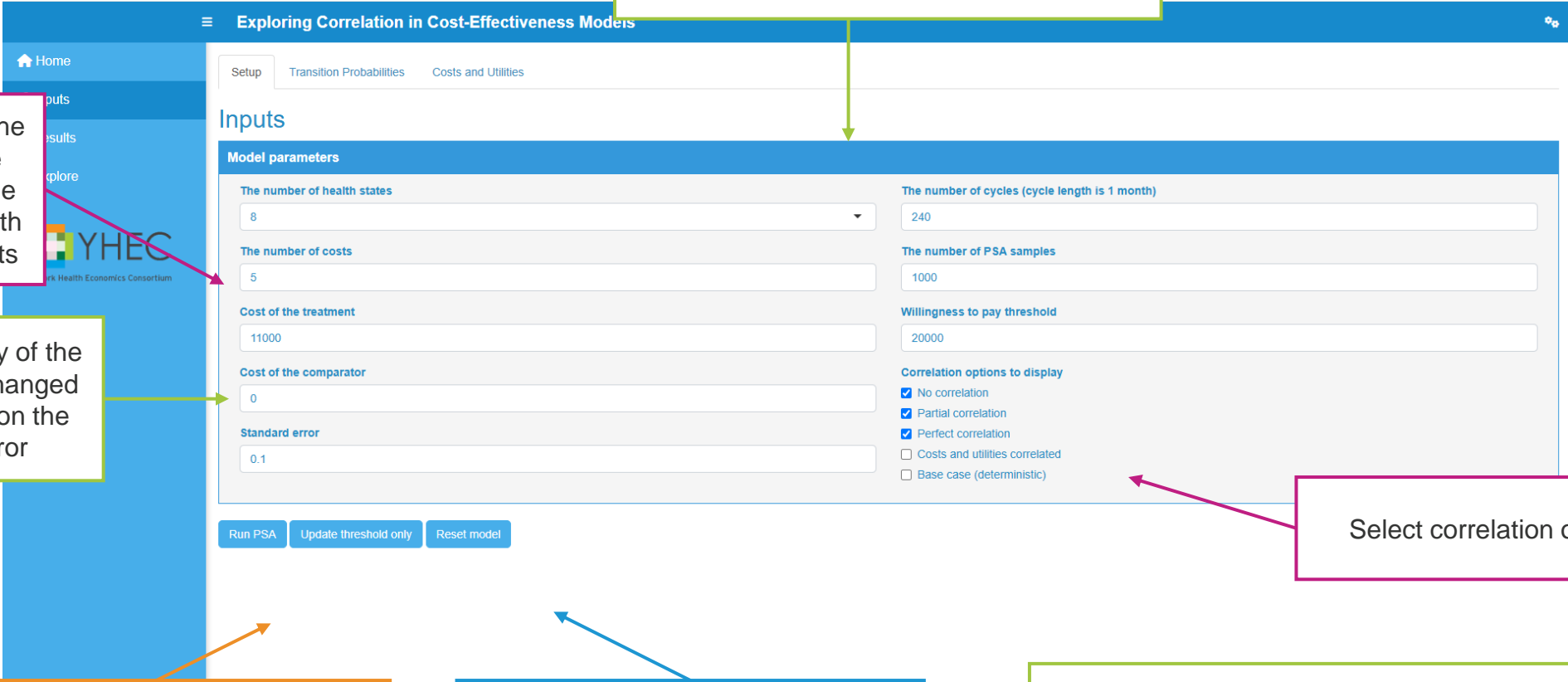
Partial/perfect correlation: lognormal multiplier applied to the mean

Partial: multiplier shared by all costs for iteration i

Perfect: multiplier shared by all costs, QALYs, and transition probabilities for iteration i

```
cost_function <- function(n_samples, cost_mean, se, scenario, multiplier) {  
  if (scenario == "base_case" | cost_mean == 0) {  
    # FOR DETERMINISTIC  
    state_costs <- rep(cost_mean, n_samples)  
  } else if (scenario == "independent") {  
    # FOR NO CORRELATION  
    # Estimate gamma parameters  
    cost_se <- cost_mean * se  
    gamma_para <- gamma_function(cost_mean, cost_se^2)  
    # Generate costs from gamma distribution  
    state_costs <- rgamma(n_samples, shape = gamma_para$shape, scale = gamma_para$scale)  
  } else if (scenario %in% c("part_correlation", "part_correlation2", "full_correlation")) {  
    # FOR PARTIAL/PERFECT CORRELATION  
    # Generate costs by applying a multiplier  
    state_costs <- cost_mean * multiplier  
  }  
  state_costs %<>%  
    pmax(0)  
  return(state_costs)  
}
```

Shiny model



The screenshot shows the 'Exploring Correlation in Cost-Effectiveness Models' Shiny application. The interface includes a sidebar with navigation links (Home, Inputs, Results, Explore) and a main content area with tabs for Setup, Transition Probabilities, and Costs and Utilities. The 'Inputs' tab is active, displaying 'Model parameters' with various input fields and checkboxes. Annotations with arrows point to specific features: a green box at the top points to the dashboard layout; a pink box points to the 'The number of health states' dropdown; a green box points to the 'Standard error' input field; an orange box points to the 'Run PSA' button; a blue box points to the 'Reset model' button; a pink box points to the 'Correlation options to display' section; and a green box at the bottom right describes features not pictured.

Dashboard layout with shinydashboard and shinydashboardPlus

Complexity of the model can be changed via the number of health states and costs

Overall variability of the model can be changed via a multiplier on the standard error

Select correlation options

Option to run the PSA or update the willingness-to-pay threshold

Reset button with shinyjs

Not pictured: editable tables with DT, informative popovers with shinyBS, loading screens with waiter

Model parameters

The number of health states: 8

The number of costs: 5

Cost of the treatment: 11000

Cost of the comparator: 0

Standard error: 0.1

The number of cycles (cycle length is 1 month): 240

The number of PSA samples: 1000

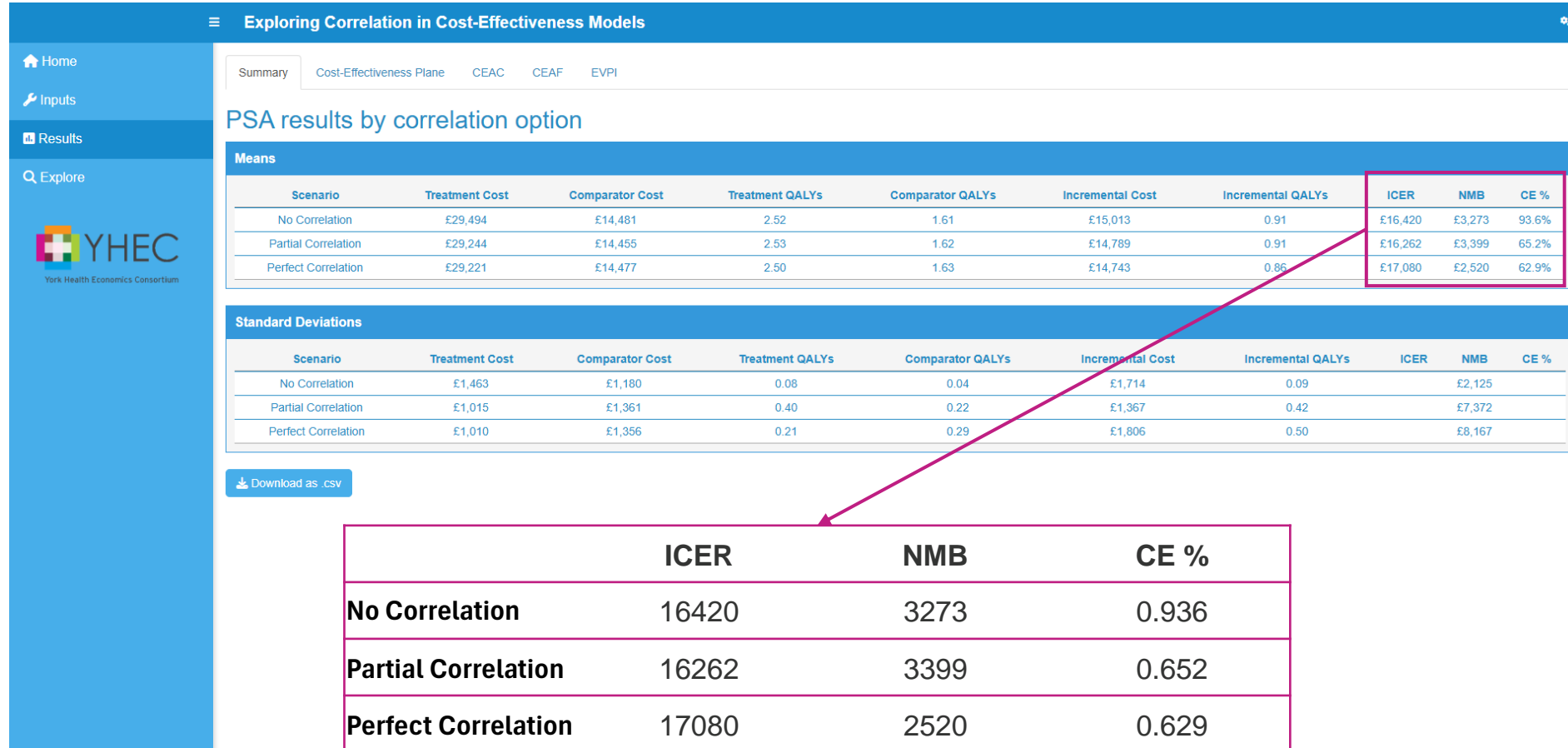
Willingness to pay threshold: 20000

Correlation options to display

- ☒ No correlation
- ☒ Partial correlation
- ☒ Perfect correlation
- ☐ Costs and utilities correlated
- ☐ Base case (deterministic)

Run PSA Update threshold only Reset model

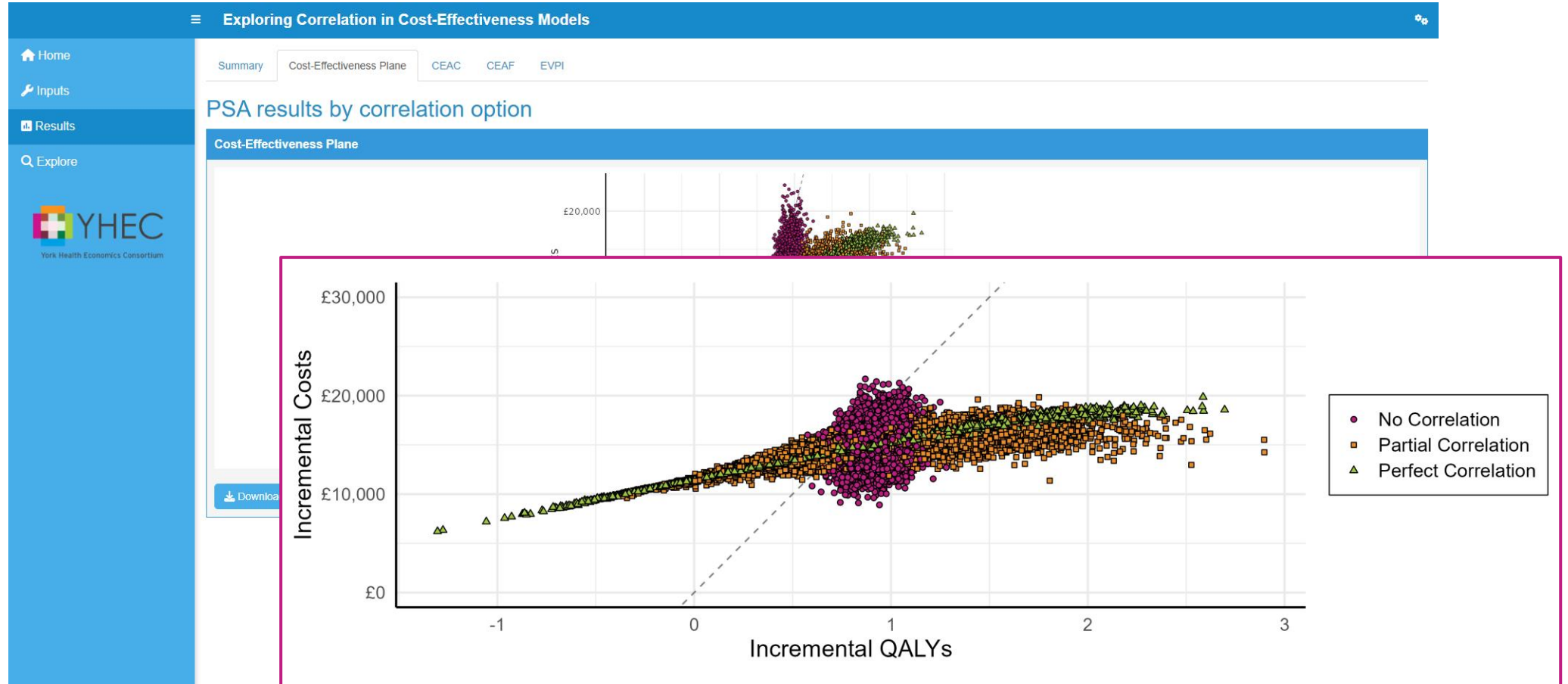
Results



https://shiny.york.ac.uk/PSA_Correlation/

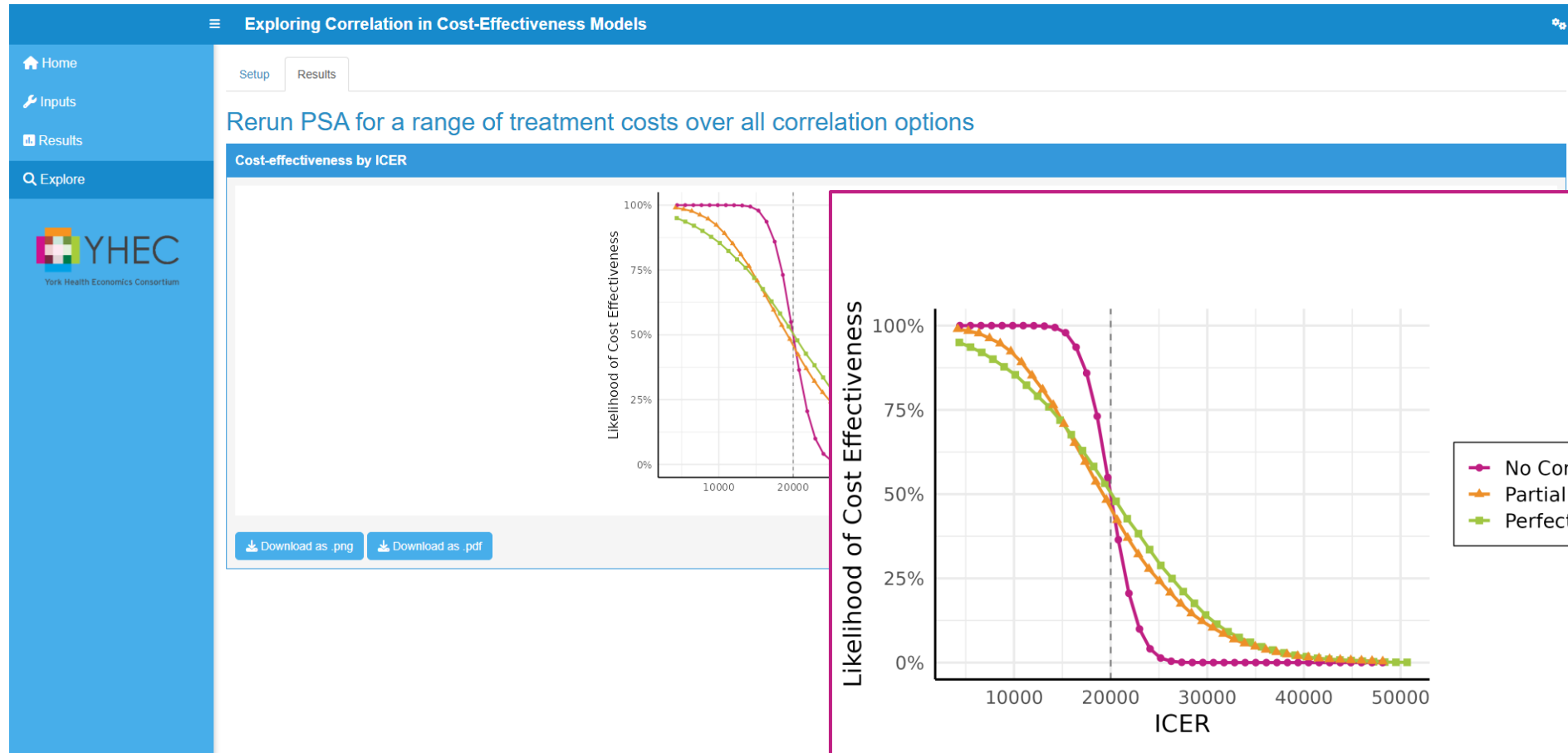
BCEA and hesim packages used under the hood to summarise results and generate plot data

Results (CE plane)



https://shiny.york.ac.uk/PSA_Correlation/

Explore



https://shiny.york.ac.uk/PSA_Correlation/

Limitations

No alternative model structures.

Fixed variation for all inputs.

One shape of scatter plot.

No real-world data.

Challenges

Preload base case results

- Display saved results if the run button is null
- Caching – storage concerns

Manage arbitrary health states, costs and correlation options

- Functional programming with `purrr::map`
- Long data format and `ggplot2`

Keep codebase under control

- Re-use code: Single module for transitions, costs and QALYs, generic plot module with download button

Speed up computations

- Check speed with microbenchmark
- Move code out of loops and avoid dataframes/tibbles

Thank you

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