# ajuste modelo

April 5, 2021

Hello. This Jupyter notebook details the statistical estimation of an asset valuation model that I am currently working on. The model constitutes the central part of my thesis project (Economics) at COLMEX. The datasets are publicly available online, and the sources are cited below. All the mathematical details and theoretical results are written down in the main body of the thesis document, which will available once it is (hopefully) approved.

#### 1 Data sources

• Historical asset returns for USA:

http://pages.stern.nyu.edu/~adamodar/New\_Home\_Page/datafile/histretSP.html

• Real per capita consumption for USA:

https://fred.stlouisfed.org/series/A794RX0Q048SBEA

• Consumer price index for USA:

https://fred.stlouisfed.org/series/CPIAUCSL

# 2 Data preparation

```
[262]: # Import requiered libraries
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
from scipy.stats import shapiro, kstest, anderson

# 'pub_quality' is a flag variable:
# - If true, automatically exports all plots to PDF at 200 dpi.
# - If false, all plots are displayed inline al 70 dpi.
pub_quality = False

if pub_quality:
    plt.rcParams['figure.dpi'] = 200
else:
    plt.rcParams['figure.dpi'] = 70
```

```
# Preferred style for the plotting engine
plt.style.use('seaborn-talk')

# Set a random seed
np.random.seed(0)

# Load data
data = pd.read_excel('datos.xlsx', engine = 'openpyxl')
data.head()
```

```
[262]:
         year
                sp500
                       tbill
                               tbond
                                         baa
                                              rpc_consumption
                                                                  price
      0 1947
               0.0520 0.0060 0.0092
                                      0.0026
                                                     8971.75
                                                              22.331667
      1 1948 0.0570 0.0105 0.0195
                                      0.0344
                                                     9017.75
                                                              24.045000
      2 1949 0.1830 0.0112 0.0466
                                                              23.809167
                                      0.0538
                                                     9109.50
      3 1950 0.3081 0.0120 0.0043 0.0424
                                                     9534.75
                                                              24.062500
      4 1951 0.2368 0.0152 -0.0030 -0.0019
                                                     9521.50
                                                              25.973333
```

The inflation rate  $i_t$  at period t is calculated as

$$i_t = \frac{p_t - p_{t-1}}{p_{t-1}}$$

where  $p_t$  is the price index at period t.

The gross return  $R_t$  of an asset is calculated using the inflation rate  $i_t$  and the nominal net return  $n_t$  as

$$R_t = \frac{1 + n_t}{1 + i_t}$$

We will store the real gross return of the risky asset as r, and the real gross return of the riskfree asset as rf. The risk premium (stored as  $risk\_premium$ ) is the difference between r and rf for every period t.

```
[263]: # Calculate inflation rate
data['inflation'] = (data['price'] - data['price'].shift(1)) / data['price'].

shift(1)

# Calculate real returns on both assets
data['r'] = (1 + data['sp500']) / (1 + data['inflation'])
data['rf'] = (1 + (data['tbill'] + data['tbond'] + data['baa']) / 3) / (1 + outline)

shift(1)

# The risk premium is the difference beetween the return of the risky asset and outline the riskfree one
data['risk_premium'] = data['r'] - data['rf']

data.head()
```

```
[263]:
                sp500
                      tbill
                                         baa rpc_consumption
                                                                  price \
         year
                              tbond
      0 1947 0.0520 0.0060 0.0092 0.0026
                                                      8971.75
                                                              22.331667
      1 1948 0.0570 0.0105 0.0195 0.0344
                                                      9017.75
                                                              24.045000
      2 1949 0.1830 0.0112 0.0466 0.0538
                                                      9109.50
                                                              23.809167
      3 1950 0.3081 0.0120 0.0043 0.0424
                                                      9534.75
                                                              24.062500
      4 1951 0.2368 0.0152 -0.0030 -0.0019
                                                      9521.50
                                                              25.973333
         inflation
                           r
                                       risk_premium
                                   rf
      0
               NaN
                        {\tt NaN}
                                                NaN
                                  NaN
      1
          0.076722 0.981683
                             0.948682
                                           0.033001
      2 -0.009808 1.194718
                                           0.147244
                             1.047474
          0.010640 1.294328
                                           0.285496
      3
                             1.008833
          0.079411 1.145810 0.929612
                                           0.216198
```

The Python list T\_list contains the number (as integers) of possible years to be considered in an investment period. We will use 1, 3, 5 and 10 years as investment horizons to fit the model.

```
[264]: # Investmment period length (in years)
       t_list = [1, 3, 5, 10]
       # We will store the modified data in a dictionary called tdata
       tdata = {t: None for t in t list}
       for t in t list:
           years = list(data['year'])
           periods = []
           consumption = []
           r returns = []
           rf returns = []
           # Loop through the original data to form periods of length t
           for i in range(0, len(years) - t, t):
               # 'year 1' and 'year 2' are the starting and ending points of the period
               year_1 = years[i]
               year_2 = years[i + t - 1]
               periods.append((year_1, year_2))
               # 'sample' is the data from the current period
               sample = data.query('year >= ' + str(year_1) + ' & year <= ' +__</pre>
        →str(year 2))
               # Aggregate the consumption and return data
               consumption.append(sample['rpc_consumption'].sum())
               r_returns.append(sample['r'].product())
               rf_returns.append(sample['rf'].product())
           # Finally store the aggregated data in a tempral dataframe calleng
        \rightarrow data_period
           data_period = pd.DataFrame({
```

```
'vear':
                              [period[1] for period in periods],
               'consumption': consumption,
               'r':
                              r_returns,
               'rf':
                              rf_returns
           })
           # Gross growth rate of per capita consumption and its logarithm
           data_period['delta_consumption_gross'] = data_period['consumption'] /__

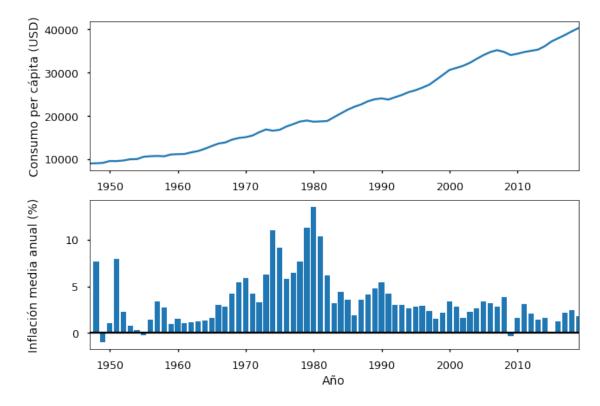
→data period['consumption'].shift(1)
           data_period['log_delta_consumption_gross'] = np.
        →log(data_period['delta_consumption_gross'])
           # Net growth rate of per capita consumption
           data_period['delta_consumption_net'] =__

→data_period['delta_consumption_gross'] - 1
           # Long term (gross) risky return
           data_period['r2'] = data_period['r'] * data_period['r'].shift(1)
           # Set 'year' as index
           data_period = data_period.set_index('year')
           # And save
           tdata[t] = data_period
       # Check if it worked
       tdata[1].head()
[264]:
             consumption
                                              delta_consumption_gross \
                                 r
       year
       1947
                 8971.75 1.000000 1.000000
                                                                  NaN
       1948
                 9017.75 0.981683 0.948682
                                                             1.005127
                                                             1.010174
       1949
                 9109.50 1.194718 1.047474
       1950
                 9534.75 1.294328 1.008833
                                                             1.046682
       1951
                 9521.50 1.145810 0.929612
                                                             0.998610
             log_delta_consumption_gross delta_consumption_net
                                                                        r2
      year
       1947
                                     NaN
                                                            {\tt NaN}
                                                                       NaN
                                                       0.005127 0.981683
       1948
                                0.005114
       1949
                                0.010123
                                                       0.010174
                                                                 1.172834
       1950
                                0.045625
                                                       0.046682
                                                                 1.546357
       1951
                               -0.001391
                                                      -0.001390 1.483054
[265]: # Get the sample size for every t:
       print('t\t', 'sample size')
       for t in t_list:
           print(str(t) + '\t', len(tdata[t]))
               sample size
      t
      1
               72
```

```
3 24
5 14
10 7
```

### 3 Exploratory data analysis

```
[266]: # Set the index of the original data
       data = data.set_index('year')
[267]: # Statistical summary of the returns before 2001
       data[['r', 'rf']].apply(lambda x: (x-1)*100).query('year <= 2000').describe()
[267]:
                        53.000000
       count
             53.000000
      mean
              10.034553
                          2.132340
       std
             16.645748
                          5.864550
            -33.249899 -10.391962
      min
      25%
             -1.233586 -1.504402
      50%
             11.950001
                          1.142218
      75%
             20.446117
                          5.670785
             52.011053 16.954208
      max
[268]: # Statistical summary of the returns over the whole series
       data[['r', 'rf']].apply(lambda x: (x-1)*100).describe()
[268]:
                                rf
      count 72.000000 72.000000
      mean
              9.050630
                        2.243095
      std
              16.955085
                          5.254157
      min
            -38.881637 -10.391962
      25%
             -1.159901 -0.735508
       50%
             11.370268
                        2.211642
       75%
              19.715364
                         5.385028
      max
             52.011053 16.954208
[269]: # Plot of real consumption per capita and inflation rate
       fig = plt.figure()
       plt.subplot(2, 1, 1)
       plt.plot(data['rpc_consumption'])
       axes = plt.gca()
       axes.set_xlim([1947, 2019])
       plt.ylabel('Consumo per cápita (USD)')
       plt.subplot(2, 1, 2)
       plt.bar(data.index, data['inflation']*100)
```



We assume that gross consumption growth  $c_t/c_{t-1}$  is lognormally distributed. This is the case only if its logarithm is normally distributed. Therefore we will conduct normality tests on  $\ln(c_t/c_{t-1})$ .

```
# Mean and standard deviation for the reference sample
   m = tdata[t]['log_delta_consumption_gross'].mean()
   s = tdata[t]['log_delta_consumption_gross'].std()
   # Test (data) sample
   test_sample = tdata[t]['log_delta_consumption_gross'].copy().dropna()
   normal_sample = pd.Series(np.random.normal(m, s, 1000))
   test_quantiles = test_sample.quantile(quantiles)
   normal_quantiles = normal_sample.quantile(quantiles)
   # Run some built-in normality tests
   normality_tests[t] = shapiro(test_sample), kstest(test_sample, 'norm', __
 →args=(m ,s)), anderson(test_sample, dist='norm')
   # Plot limits
   lim_inf = m - 2.5 * s
   \lim \sup = m + 2.5 * s
   # Straight line
   straight = np.linspace(lim_inf, lim_sup, 10)
   quants[t] = {
       'test_quantiles': test_quantiles,
       'normal_quantiles': normal_quantiles,
       'straight': straight,
       'lim_inf': lim_inf,
       'lim_sup': lim_sup
   }
t2axes = {
   1: [0, 0],
   3: [0, 1],
   5: [1, 0],
   10: [1, 1]
}
# QQ plots
fig, axes = plt.subplots(nrows=2, ncols=2)
fig.add_subplot(111, frame_on=False)
for t in t_list:
   axes[t2axes[t][0], t2axes[t][1]].plot(quants[t]['straight'],__
axes[t2axes[t][0], t2axes[t][1]].scatter(quants[t]['normal_quantiles'],
axes[t2axes[t][0], t2axes[t][1]].set_xlim([quants[t]['lim_inf'],__

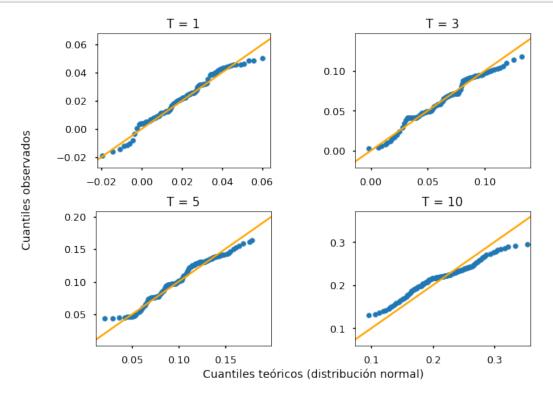
quants[t]['lim_sup']])
```

```
axes[t2axes[t][0], t2axes[t][1]].set_title('T = ' + str(t))
axes[t2axes[t][0], t2axes[t][1]].set_aspect(0.7)

plt.tick_params(labelcolor="none", bottom=False, left=False)
plt.xlabel('Cuantiles teóricos (distribución normal)')
plt.ylabel('Cuantiles observados')

fig.tight_layout()

if pub_quality: fig.savefig('figures/fig_qqplots.pdf', bbox_inches='tight')
```



```
[271]: # Show the results of the normality tests:
for T in normality_tests.keys():
    print('T=' + str(T), normality_tests[T],'\n')
```

T=1 (ShapiroResult(statistic=0.9777632355690002, pvalue=0.2394152581691742), KstestResult(statistic=0.07176932165192118, pvalue=0.8322467696864853), AndersonResult(statistic=0.36012523601594637, critical\_values=array([0.548, 0.624, 0.749, 0.873, 1.039]), significance\_level=array([15. , 10. , 5. , 2.5, 1. ])))

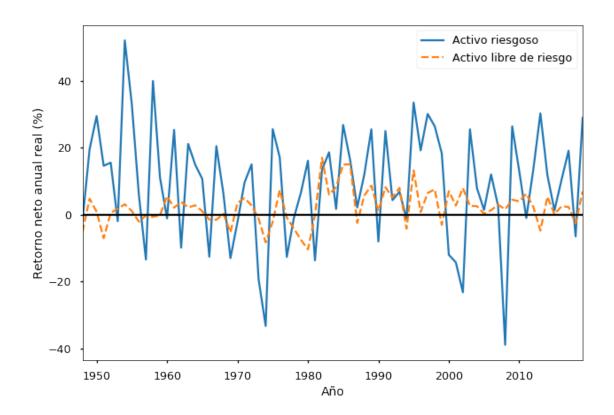
T=3 (ShapiroResult(statistic=0.9787319898605347, pvalue=0.8834728002548218), KstestResult(statistic=0.10406010446142763, pvalue=0.9426601195148988), AndersonResult(statistic=0.21271804064711475, critical\_values=array([0.511,

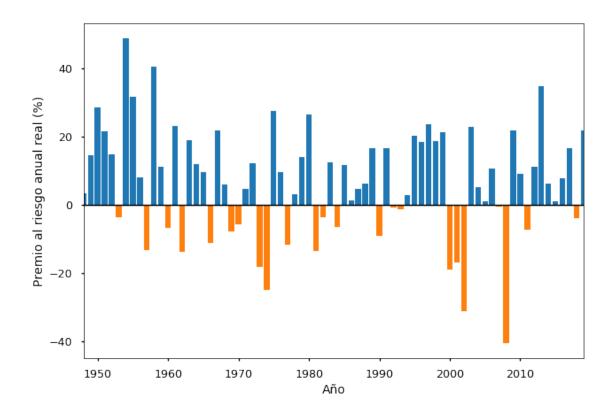
```
0.582, 0.699, 0.815, 0.969]), significance_level=array([15., 10., 5., 2.5,
      1. ])))
      T=5 (ShapiroResult(statistic=0.9622002243995667, pvalue=0.7872425317764282),
      KstestResult(statistic=0.1430313395989561, pvalue=0.9189390658446934),
      AndersonResult(statistic=0.23210396371063347, critical_values=array([0.497,
      0.566, 0.679, 0.792, 0.942]), significance level=array([15., 10., 5., 2.5,
      1. 1)))
      T=10 (ShapiroResult(statistic=0.9812653064727783, pvalue=0.9576718211174011),
      KstestResult(statistic=0.16396914765481485, pvalue=0.9873328087597973),
      AndersonResult(statistic=0.19022132552907944, critical_values=array([0.592,
      0.675, 0.809, 0.944, 1.123]), significance_level=array([15., 10., 5., 2.5,
      1. ])))
[272]: # Asset returns plot
      fig = plt.figure()
      plt.plot((data['r']-1)*100)
      plt.plot((data['rf']-1)*100, linestyle='dashed')
      plt.axhline(0, color='black', linestyle='-')
      plt.legend(labels = ['Activo riesgoso', 'Activo libre de riesgo'])
      plt.xlabel('Año')
      plt.ylabel('Retorno neto anual real (%)')
```

if pub\_quality: fig.savefig('figures/fig\_retornos.pdf', bbox\_inches='tight')

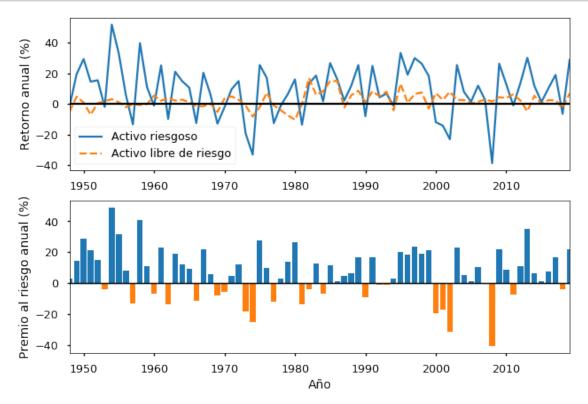
axes = plt.gca()

axes.set\_xlim([1948, 2019])





```
[274]: # Plot of real returns and risk premium
      fig = plt.figure()
      plt.subplot(2, 1, 1)
      plt.plot((data['r']-1)*100)
      plt.plot((data['rf']-1)*100, linestyle='dashed')
      plt.axhline(0, color='black', linestyle='-')
      axes = plt.gca()
      axes.set_xlim([1948, 2019])
      plt.ylabel('Retorno anual (%)')
      plt.legend(labels = ['Activo riesgoso', 'Activo libre de riesgo'])
      plt.subplot(2, 1, 2)
      plt.bar(data.query('risk_premium > 0').index, data.query('risk_premium >_
       plt.bar(data.query('risk_premium < 0').index, data.query('risk_premium < ∪
       →0')['risk_premium']*100)
      plt.axhline(0, color='black', linestyle='-', linewidth=1.5)
      axes = plt.gca()
      axes.set_xlim([1948, 2019])
      plt.ylabel('Premio al riesgo anual (%)')
```



# 4 Model fitting

```
[275]: # Subjective discount factors (beta)
betas = [0.1, 0.5, 0.90, 0.95, 1.0]

# Maximum value of the relative risk aversion coefficient (gamma)
gamma_max = 150

# Subjective probabilities of not experiencing a consumption shock (pi_2)
pis = [0.2, 0.4, 0.6, 0.8, 1.0]

# Generate the sample space for gamma
points = 1000
gammas = np.linspace(0, gamma_max, points)
```

```
[276]: | # The fitting results will be stored in a dictionary called 'treport'
       treport = {t: None for t in t_list}
       for t in t_list:
           # Mean returns
           r = tdata[t]['r'].mean()
           rf = tdata[t]['rf'].mean()
           # Standard deviations
           sr = tdata[t]['r'].std()
           sr2 = tdata[t]['r2'].std()
           # Mean and standard deviation of the rate of growth of consumption
           mc = tdata[t]['delta_consumption_gross'].mean() - 1
           sc = tdata[t]['delta_consumption_gross'].std()
           # The estimation of the return of the risky asset is stored in the
        → dictioonary 'report'
           # Each key corresponds to a value of the beta parameter
           report = {beta: None for beta in betas}
           # Estimation of the return of the risky asset
           for beta in betas:
                # For each value of beta, the estimation is stored in a temporary
        \rightarrow dataframe called 'results'
               results = pd.DataFrame({'gamma': gammas})
                # Loop over the values of the pi parameter
               for pi in pis:
                    # For each value of pi, the estimation is stored in 'result'
                    result = []
                    for gamma in gammas:
                        # Calculate the first and second central moments of the delta_
        \rightarrow discount factor
                        md1 = beta * np.exp(-gamma * mc + gamma ** 2 * sc ** 2 / 2)
                        md2 = beta ** 2 * np.exp(- 2 * gamma * mc + gamma ** 2 * sc **_{\sqcup}
        ⇒2)
                        sd1 = np.sqrt(beta ** 2 * np.exp(- 2 * gamma * mc + gamma ** 2_{\bot})
        \rightarrow* sc ** 2) * (np.exp(gamma ** 2 * sc ** 2) - 1))
                        sd2 = np.sqrt(beta ** 4 * np.exp(- 4 * gamma * mc + 2 * gamma_{\bot})
        \rightarrow** 2 * sc ** 2) * (np.exp(2 * gamma ** 2 * sc ** 2) - 1))
                        # Auxiliary factor c
                        c = (pi - 1) * sd1 * sr - pi ** 2 * sd2 * sr2 - md1 * rf - pi *_{\cup}
        \rightarrowmd2 * rf ** 2
                        # Estimator
                        r_{estimation} = (-md1 + np.sqrt(md1 ** 2 - 4 * pi * md2 * c)) / 
        \rightarrow (2 * pi * md2)
```

```
# The estimator is annualized for an easier interpretation
                       r_{estimation} = r_{estimation} ** (1 / T)
                       # Store
                       result.append((r_{estimation} - 1) * 100)
                   results[str(pi)] = result
               # Store
               report[beta] = results
           # Store
           treport[t] = report
       # Take a look
       treport[1][0.95].head()
[276]:
                                    0.4
                                              0.6
                                                        0.8
                                                                   1.0
                         0.2
             gamma
       0 0.000000 0.212675 0.212675 0.212675 0.212675 0.212675
       1 \quad 0.150150 \quad 0.215446 \quad 0.214960 \quad 0.214982 \quad 0.215279 \quad 0.215744
       2 0.300300 0.218219 0.217245 0.217286 0.217878 0.218805
       3 0.450450 0.220995 0.219531 0.219587 0.220472 0.221858
       4 0.600601 0.223772 0.221818 0.221887 0.223061 0.224903
[277]: # Line markers for each probability (this is just styling stuff)
       markers = {
           0.2: '$A$',
           0.4: '$B$',
           0.6: '$C$'.
           0.8: '$D$',
           1.0: '$E$'
       }
       # Override markers
       markers = {pi: None for pi in pis}
       # Labels for each probability
       labels = ['\$\pi_2 = \$' + str(pi) \text{ for pi in pis}]
       # Plotting function
       def graph(T, beta):
           fig = plt.figure()
           for pi in pis:
               plt.plot(gammas, treport[t][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(700,2000), markerfacecolor='black')
           plt.axhline((tdata[t]['r'].mean() ** (1/T) - 1) * 100, color='black',
        →linestyle='dashed')
           plt.axhline((tdata[t]['rf'].mean() ** (1/T) - 1) * 100, color='black', __
        →linestyle='dotted')
           plt.xlabel('Coeficiente de aversión relativa al riesgo')
```

```
plt.ylabel('Retorno neto anualizado (%)')

plt.legend(labels = labels + ['Activo riesgoso (media)', 'Activo sin riesgo

(media)'], bbox_to_anchor=(0.5, -0.37), loc='lower center', ncol=3)

plt.grid(linestyle="-", linewidth=0.5)

axes = plt.gca()

axes.set_xlim([0, 140])

axes.set_ylim([0, 9])

plt.title('T = ' + str(t))

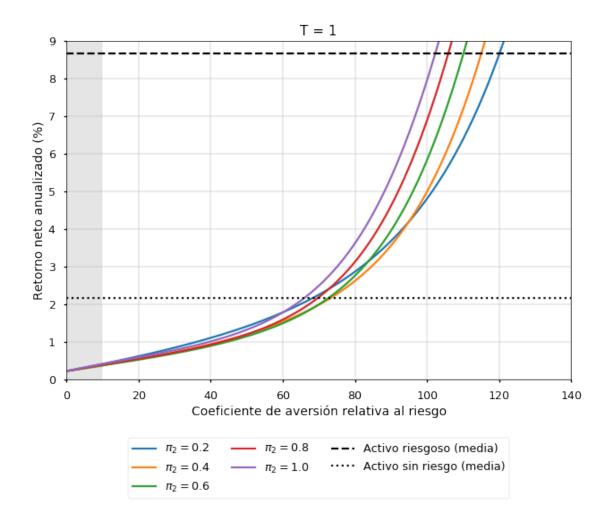
plt.axvspan(0, 10, alpha=0.1, color='black')

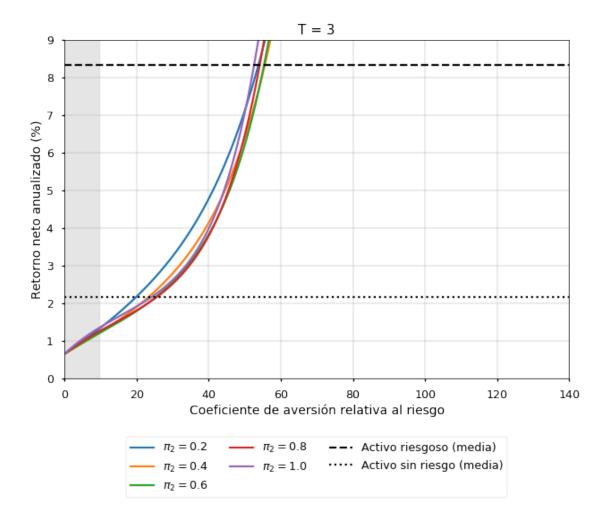
if pub_quality: fig.savefig('figures/fig_resultados_beta_' + str(int(100 *□

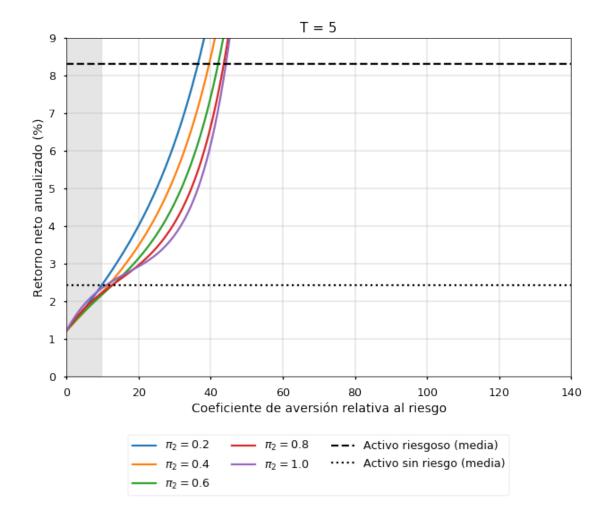
→beta)) + '_t_' + str(t) + '.pdf', bbox_inches='tight')
```

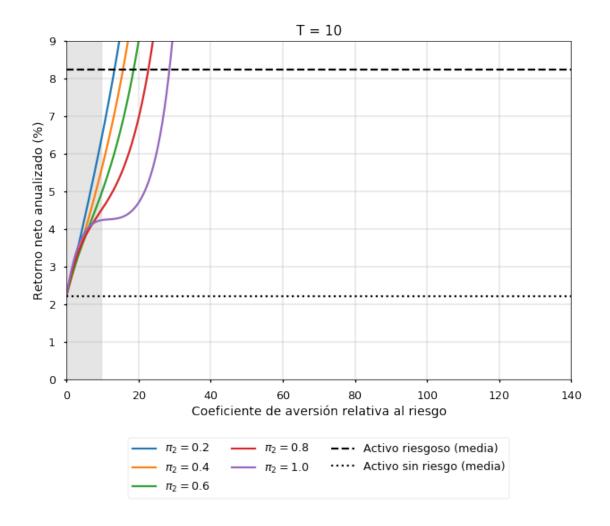
# [278]: # Plot the results for the given value of beta beta = 0.95 for t in t\_list: graph(t, beta)

```
/usr/local/Cellar/graph-tool/2.37/libexec/lib/python3.9/site-
packages/matplotlib/cbook/__init__.py:1402: FutureWarning: Support for multi-
dimensional indexing (e.g. `obj[:, None]`) is deprecated and will be removed in
a future version. Convert to a numpy array before indexing instead.
    x[:, None]
/usr/local/Cellar/graph-tool/2.37/libexec/lib/python3.9/site-
packages/matplotlib/axes/_base.py:278: FutureWarning: Support for multi-
dimensional indexing (e.g. `obj[:, None]`) is deprecated and will be removed in
a future version. Convert to a numpy array before indexing instead.
    y = y[:, np.newaxis]
```









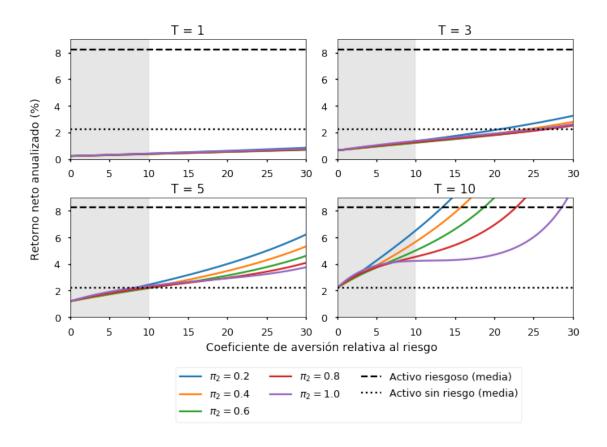
```
[279]: # A more compact plot
plt.gcf().clear()
fig, axes = plt.subplots(nrows=2, ncols=2)
fig.add_subplot(111, frame_on=False)

beta = 0.95

for pi in pis:
    axes[0, 0].plot(gammas, treport[1][beta][str(pi)], marker=markers[pi],
    markersize=9, markevery=(110,2000), markerfacecolor='black')
    axes[0, 0].axvspan(0, 10, alpha=0.04, color='gray')
for pi in pis:
    axes[0, 1].plot(gammas, treport[3][beta][str(pi)], marker=markers[pi],
    markersize=9, markevery=(110,2000), markerfacecolor='black')
    axes[0, 1].axvspan(0, 10, alpha=0.04, color='gray')
for pi in pis:
```

```
axes[1, 0].plot(gammas, treport[5][beta][str(pi)], marker=markers[pi],
→markersize=9, markevery=(110,2000), markerfacecolor='black')
   axes[1, 0].axvspan(0, 10, alpha=0.04, color='gray')
for pi in pis:
   axes[1, 1].plot(gammas, treport[10][beta][str(pi)], marker=markers[pi],
→markersize=9, markevery=(110,2000), markerfacecolor='black')
   axes[1, 1].axvspan(0, 10, alpha=0.04, color='gray')
for i in range (0, 2):
   for j in range(0, 2):
       axes[i, j].axhline((tdata[t]['r'].mean() ** (1/T) - 1) * 100,
axes[i, j].axhline((tdata[t]['rf'].mean() ** (1/T) - 1) * 100,
axes[0, 0].set_title('T = 1')
axes[0, 1].set_title('T = 3')
axes[1, 0].set_title('T = 5')
axes[1, 1].set_title('T = 10')
plt.setp(axes, xlim=(0, 30), ylim=(0, 9))
plt.tick params(labelcolor="none", bottom=False, left=False)
plt.xlabel('Coeficiente de aversión relativa al riesgo')
plt.ylabel('Retorno neto anualizado (%)')
fig.legend(labels = labels + ['Activo riesgoso (media)', 'Activo sin riesgou
fig.tight layout()
fig.subplots_adjust(bottom=0.25)
if pub_quality: fig.savefig('figures/fig_resultados_comparativo_beta_' +__
str(int(100 * beta)) + '.pdf', bbox_inches='tight')
```

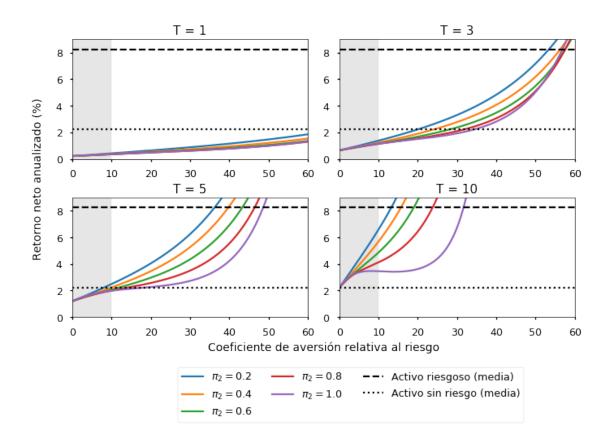
<Figure size 728x500.5 with 0 Axes>



```
[280]: str(int(100 * beta))# A more compact plot
      fig, axes = plt.subplots(nrows=2, ncols=2)
      fig.add_subplot(111, frame_on=False)
      beta = 0.5
      for pi in pis:
           axes[0, 0].plot(gammas, treport[1][beta][str(pi)], marker=markers[pi],
       →markersize=9, markevery=(110,2000), markerfacecolor='black')
           axes[0, 0].axvspan(0, 10, alpha=0.04, color='gray')
      for pi in pis:
          axes[0, 1].plot(gammas, treport[3][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(110,2000), markerfacecolor='black')
          axes[0, 1].axvspan(0, 10, alpha=0.04, color='gray')
      for pi in pis:
           axes[1, 0].plot(gammas, treport[5][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(110,2000), markerfacecolor='black')
           axes[1, 0].axvspan(0, 10, alpha=0.04, color='gray')
      for pi in pis:
          axes[1, 1].plot(gammas, treport[10][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(110,2000), markerfacecolor='black')
```

```
axes[1, 1].axvspan(0, 10, alpha=0.04, color='gray')
for i in range (0, 2):
   for j in range(0, 2):
       axes[i, j].axhline((tdata[t]['r'].mean() ** (1/T) - 1) * 100, __
axes[i, j].axhline((tdata[t]['rf'].mean() ** (1/T) - 1) * 100,
#axes[i, j].grid(linestyle="-", linewidth=0.5)
axes[0, 0].set_title('T = 1')
axes[0, 1].set title('T = 3')
axes[1, 0].set_title('T = 5')
axes[1, 1].set_title('T = 10')
plt.setp(axes, xlim=(0,60), ylim=(0, 9))
plt.tick_params(labelcolor="none", bottom=False, left=False)
plt.xlabel('Coeficiente de aversión relativa al riesgo')
plt.ylabel('Retorno neto anualizado (%)')
fig.legend(labels = labels + ['Activo riesgoso (media)', 'Activo sin riesgou
→ (media)'], bbox_to_anchor=(0.55, -0.01), loc='lower center', ncol=3)
fig.tight layout()
fig.subplots_adjust(bottom=0.25)
if pub_quality: fig.savefig('figures/fig_resultados_comparativo_beta_' + _ _

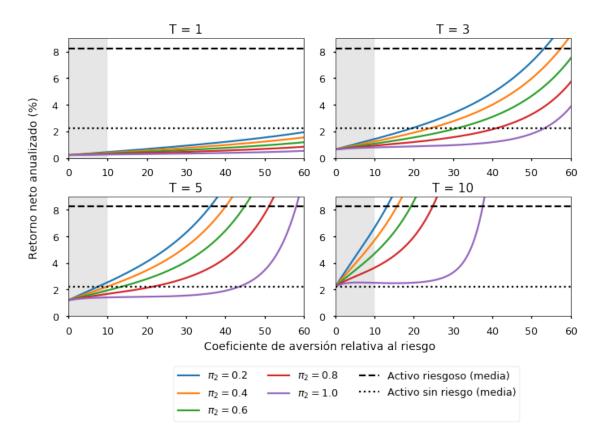
¬str(int(100 * beta)) + '.pdf', bbox_inches='tight')
```



```
[281]: # A more compact plot
      fig, axes = plt.subplots(nrows=2, ncols=2)
      fig.add_subplot(111, frame_on=False)
      beta = 0.1
      for pi in pis:
           axes[0, 0].plot(gammas, treport[1][beta][str(pi)], marker=markers[pi],
       →markersize=9, markevery=(110,2000), markerfacecolor='black')
           axes[0, 0].axvspan(0, 10, alpha=0.04, color='gray')
      for pi in pis:
          axes[0, 1].plot(gammas, treport[3][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(110,2000), markerfacecolor='black')
          axes[0, 1].axvspan(0, 10, alpha=0.04, color='gray')
      for pi in pis:
           axes[1, 0].plot(gammas, treport[5][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(110,2000), markerfacecolor='black')
           axes[1, 0].axvspan(0, 10, alpha=0.04, color='gray')
      for pi in pis:
          axes[1, 1].plot(gammas, treport[10][beta][str(pi)], marker=markers[pi],
        →markersize=9, markevery=(110,2000), markerfacecolor='black')
```

```
axes[1, 1].axvspan(0, 10, alpha=0.04, color='gray')
for i in range (0, 2):
   for j in range(0, 2):
       axes[i, j].axhline((tdata[t]['r'].mean() ** (1/T) - 1) * 100, __
axes[i, j].axhline((tdata[t]['rf'].mean() ** (1/T) - 1) * 100,
#axes[i, j].grid(linestyle="-", linewidth=0.5)
axes[0, 0].set_title('T = 1')
axes[0, 1].set_title('T = 3')
axes[1, 0].set_title('T = 5')
axes[1, 1].set_title('T = 10')
plt.setp(axes, xlim=(0,60), ylim=(0, 9))
plt.tick_params(labelcolor="none", bottom=False, left=False)
plt.xlabel('Coeficiente de aversión relativa al riesgo')
plt.ylabel('Retorno neto anualizado (%)')
fig.legend(labels = labels + ['Activo riesgoso (media)', 'Activo sin riesgo⊔
→ (media)'], bbox_to_anchor=(0.55, -0.01), loc='lower center', ncol=3)
fig.tight layout()
fig.subplots adjust(bottom=0.25)
if pub_quality: fig.savefig('figures/fig_resultados_comparativo_beta_' + _ _

¬str(int(100 * beta)) + '.pdf', bbox_inches='tight')
```



[]: