Unsupervised Learning Mini-Project

```
Core functions:
```

```
read.csv("YourFileName")
prcomp(x, scale = TRUE)
kmeans(x, centers = ?)
hclust(dist(x))

# Make Available Data for Project
wisc.df <- read.csv("WisconsinCancer.csv", row.names = 1)
# Separate data and physician diagnosis
wisc.data <- (wisc.df[,-1])
diagnosis <- (wisc.df[,1])</pre>
```

Exploratory Data Analysis.

#Q1. There are 569 observations in this dataset.

```
#Check how many observations have a malignant diagnosis.
x = 0
for(i in 1:length(diagnosis)) {
  if(diagnosis[i] == "M") {x <- x+1}
}</pre>
```

[1] 212

```
#also 'table(diagnosis)'
#also 'sum(diagnosis == "M")
```

#Q2. There are 212 observations with a malignant diagnosis.

```
# Check how many variables end with "_mean".
length(grep(pattern = "*_mean", x = colnames(wisc.data)))
```

[1] 10

 $\#\mathrm{Q}3.$ There are 10 variables suffixed with "_mean". $\#\mathrm{Principal}$ Component Analysis.

Check column means and standard deviations (1 = rows, 2 = cols) apply(wisc.data, 2, mean)

##	radius_mean	texture_mean	perimeter_mean
##	1.412729e+01	1.928965e+01	9.196903e+01
##	area_mean	${\tt smoothness_mean}$	compactness_mean
##	6.548891e+02	9.636028e-02	1.043410e-01
##	concavity_mean	concave.points_mean	symmetry_mean
##	8.879932e-02	4.891915e-02	1.811619e-01
##	fractal_dimension_mean	radius_se	texture_se
##	6.279761e-02	4.051721e-01	1.216853e+00
##	perimeter_se	area_se	smoothness_se
##	2.866059e+00	4.033708e+01	7.040979e-03
##	compactness_se	concavity_se	concave.points_se
##	2.547814e-02	3.189372e-02	1.179614e-02
##	symmetry_se	fractal_dimension_se	radius_worst
##	2.054230e-02	3.794904e-03	1.626919e+01
##	texture_worst	perimeter_worst	area_worst
##	2.567722e+01	1.072612e+02	8.805831e+02
##	smoothness_worst	compactness_worst	concavity_worst
##	1.323686e-01	2.542650e-01	2.721885e-01
##	concave.points_worst	symmetry_worst	${\tt fractal_dimension_worst}$
##	1.146062e-01	2.900756e-01	8.394582e-02

apply(wisc.data, 2, sd)

##	radius_mean	texture_mean	perimeter_mean
##	3.524049e+00	4.301036e+00	2.429898e+01
##	area_mean	${\tt smoothness_mean}$	compactness_mean
##	3.519141e+02	1.406413e-02	5.281276e-02
##	concavity_mean	concave.points_mean	symmetry_mean
##	7.971981e-02	3.880284e-02	2.741428e-02
##	fractal_dimension_mean	radius_se	texture_se
##	7.060363e-03	2.773127e-01	5.516484e-01
##	perimeter_se	area_se	smoothness_se
##	2.021855e+00	4.549101e+01	3.002518e-03
##	compactness_se	concavity_se	concave.points_se
##	1.790818e-02	3.018606e-02	6.170285e-03
##	symmetry_se	fractal_dimension_se	radius_worst
##	8.266372e-03	2.646071e-03	4.833242e+00
##	texture_worst	perimeter_worst	area_worst
##	6.146258e+00	3.360254e+01	5.693570e+02
##	smoothness_worst	compactness_worst	concavity_worst
##	2.283243e-02	1.573365e-01	2.086243e-01
##	concave.points_worst	symmetry_worst	${\tt fractal_dimension_worst}$
##	6.573234e-02	6.186747e-02	1.806127e-02

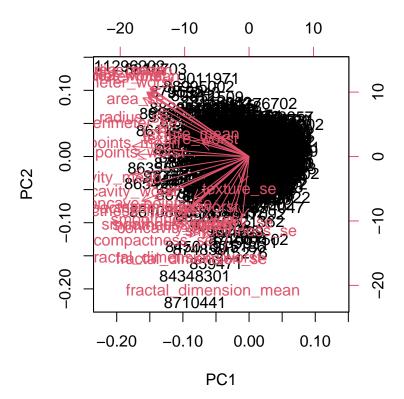
```
# Perform PCA on wisc.data by completing the following code
wisc.pr <- prcomp(wisc.data, scale=TRUE)
summary(wisc.pr)</pre>
```

```
## Importance of components:
                                            PC3
                                                     PC4
                                                             PC5
                                                                     PC6
                                                                             PC7
##
                             PC1
                                    PC2
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Standard deviation
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
## Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
##
                              PC8
                                     PC9
                                            PC10
                                                   PC11
                                                            PC12
                                                                    PC13
                                                                            PC14
## Standard deviation
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
##
                                             PC17
                             PC15
                                     PC16
                                                      PC18
                                                              PC19
                                                                      PC20
## Standard deviation
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                                                     PC25
##
                             PC22
                                     PC23
                                            PC24
                                                             PC26
                                                                     PC27
                                                                             PC28
## Standard deviation
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
## Cumulative Proportion
                          0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                             PC29
                                     PC30
##
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

The more PCs you need to describe the data, the more all-over-the-place it is...

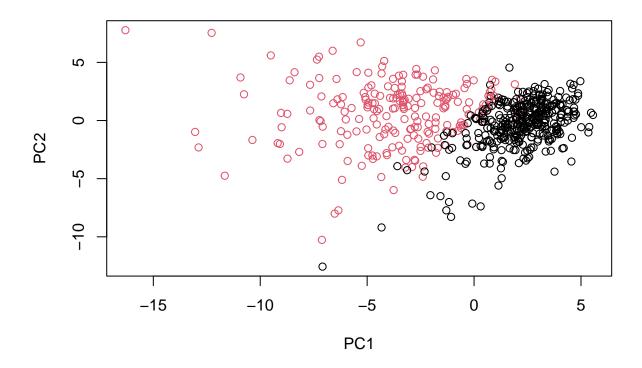
#Q4. The first principal component captures 44% of the variance in the data. #Q5. At least 3 PCs to describe >70% of the variance. #Q6. At least 7 PCs to describe >90% of the variance.

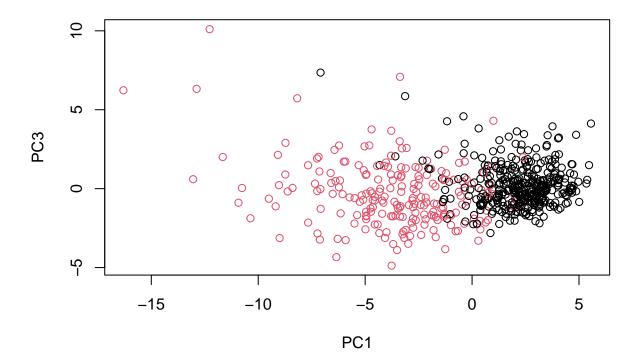
```
# Visualize PCA Results
biplot(wisc.pr)
```



#Q7. The plot contains a vast amount of data, but there seems to be an overall leftward trend. The plot is not at all easily interpretable.

```
# Visualize PCA Results, but better
factor_diagnosis <- as.factor(diagnosis)
plot(wisc.pr$x[,1:2] , col=factor_diagnosis)</pre>
```





#Q8. The plots are largely similiar. The only notable differences are that the P1/P2 plot seems to have negative outliers, whereas the P1/P3 plot has positive ones. These outliers change the y-scale of the plot, and the separation seems to be a little clearer in the P1/P2 plot, as the black values in the P1/P3 plot cross far into the red cluster territory.

```
# Visualize data in ggplot

# Create a data.frame for ggplot

df <- as.data.frame(wisc.pr$x)

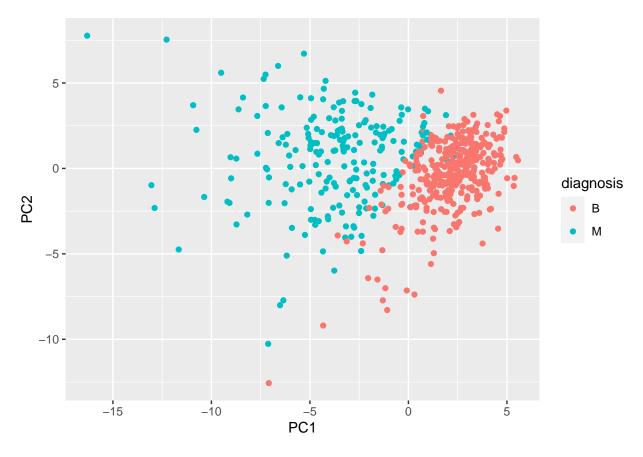
df$diagnosis <- factor_diagnosis

# Load the ggplot2 package

library(ggplot2)

# Make a scatter plot colored by diagnosis

ggplot(df) +
   aes(PC1, PC2, col=diagnosis) +
   geom_point()</pre>
```



```
# Visualize Variance Capturing by PCs

# Calculate variance from standard deviation

pr.var <- wisc.pr$sdev^2

pr.var

## [1] 1.328161e+01 5.691355e+00 2.817949e+00 1.980640e+00 1.648731e+00

## [6] 1.207357e+00 6.752201e-01 4.766171e-01 4.168948e-01 3.506935e-01

## [11] 2.939157e-01 2.611614e-01 2.413575e-01 1.570097e-01 9.413497e-02

## [16] 7.986280e-02 5.939904e-02 5.261878e-02 4.947759e-02 3.115940e-02

## [21] 2.997289e-02 2.743940e-02 2.434084e-02 1.805501e-02 1.548127e-02

## [26] 8.177640e-03 6.900464e-03 1.589338e-03 7.488031e-04 1.330448e-04

# Variance explained by each principal component: pve

pve <- pr.var / sum(pr.var)

# Plot variance explained for each principal component

plot(pve, xlab = "Principal Component",

ylab = "Proportion of Variance Explained",
```

ylim = c(0, 1), type = "o")



```
# Communicating PCA Results
wisc.pr$rotation["concave.points_mean",1]
```

[1] -0.2608538

#Q9. The component of the loading vector for "concave.points_mean" is -0.26. #Q10. At least 5 PCs to describe >80% of the variance.

Hierarchical Clustering.

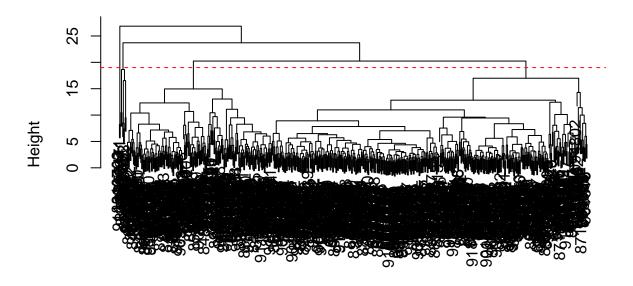
```
# Try 'complete' clustering method

# Calculate scaled Euclidean distances of data points
wisc.dist <- dist(scale(wisc.data))

# Cluster w/ 'hclust()'
wisc.hclust <- hclust(wisc.dist, method="complete")

# Visualize
plot(wisc.hclust)
abline(h=19, col="red", lty=2)</pre>
```

Cluster Dendrogram



wisc.dist hclust (*, "complete")

 $\#\mathrm{Q}11$. The abline must be placed at h=19 to cut the tree into 4 groups.

```
# Extract Data
ans <- NULL
for(i in 2:10) {
    x <- cutree(wisc.hclust, k=i)
    ans <- rbind(ans, x)
}
#ans

for(i in 1:9) {
    print(table(ans[i,], diagnosis))
}</pre>
```

```
##
      diagnosis
##
         В
             М
     1 357 210
##
##
         0
##
      diagnosis
##
         В
     1 355 205
##
##
         2
##
         0
##
      diagnosis
##
##
     1 12 165
```

```
##
    2 2 5
##
    3 343 40
            2
##
    4 0
##
     diagnosis
       B M
##
##
    1 12 165
    2 0
##
##
    3 343 40
       2
##
    4
            0
    5 0
##
            2
##
     diagnosis
##
       В
##
    1 12 165
##
    2 0
           5
##
    3 331 39
       2
            0
##
    4
##
    5 12
            1
    6 0
##
            2
##
     diagnosis
##
       В
           М
##
    1 12 165
##
    2 0
##
    3 331 39
       2
            0
##
    4
##
    5 12
            1
       0
            2
##
    6
##
    7
        0
            2
##
     diagnosis
##
        В
            М
    1 12 86
##
           79
##
    2
       0
##
    3
       0
           3
##
    4 331
          39
##
    5
       2
           0
##
    6 12
           1
##
    7
        0
            2
        0
##
            2
##
     diagnosis
##
        В
            Μ
    1 12 86
##
##
    2
       0
          79
##
    3
        0
            3
##
    4 331 39
##
    5
       2
            0
    6 12
##
            0
    7
##
       0
            2
       0
            2
##
    8
    9 0
            1
##
##
      diagnosis
##
         В
            М
##
        12 86
    1
##
    2
         0 59
##
    3
         0
            3
##
    4 331 39
```

```
##
      5
                20
      6
            2
                  0
##
##
      7
           12
                  0
                  2
##
      8
            0
##
      9
             0
                  2
##
      10
             0
```

#Q12. No, cutting the tree into any less groups ignores the split between the two large groups of patients, and cutting it into any more groups than 4 unnecessarily divides groups.

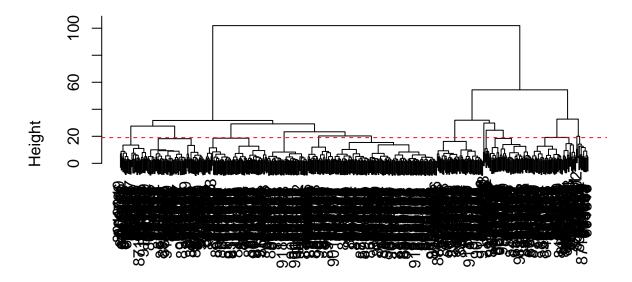
```
# Try 'ward.D2' method

# Calculate scaled Euclidean distances of data points
wisc.dist <- dist(scale(wisc.data))

# Cluster w/ 'hclust()'
wisc.hclust <- hclust(wisc.dist, method="ward.D2")

# Visualize
plot(wisc.hclust)
abline(h=19, col="red", lty=2)</pre>
```

Cluster Dendrogram



wisc.dist hclust (*, "ward.D2")

#Q13. Netiher the 'single' nor the 'average' method come up with any kind of clustering that separates the malignant and benign groups, but I don't think I can pick a favorite between the 'complete' and 'ward.D2' methods. While 'ward.D2' returns satisfactory results with separation into just two clusters, when 'complete' works, it separates more accurately (less erroneous results) than 'ward.D2'.

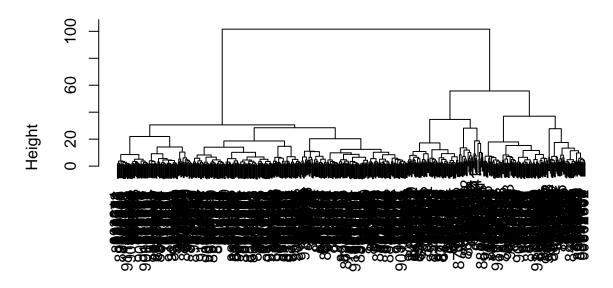
```
\# See if k-means clustering gives same result
wisc.km <- kmeans(wisc.data, centers= 2, nstart= 20)</pre>
# Check result with table
table(wisc.km$cluster, diagnosis) #kmeans clustering result
##
      diagnosis
##
         B M
##
         1 130
     2 356 82
##
table(ans [3,], diagnosis) #hclust result
##
      diagnosis
##
         В
             Μ
##
     1 12 165
        2
##
             5
     3 343 40
##
         0
```

#Q14. K-means satisfactorily separates the diagnoses. It is not as accurate as helust, but it is close behind. There are clearly two groups

Combining Methods

```
# Apply hierarchical clustering to PCA Analysis
wisc.pr.hclust <- hclust(dist(wisc.pr$x[,1:7]), method="ward.D2")
# Visualize
plot(wisc.pr.hclust)</pre>
```

Cluster Dendrogram



dist(wisc.pr\$x[, 1:7]) hclust (*, "ward.D2")

```
# Split up the tree into groups
wisc.pr.hclust.cut <- cutree(wisc.pr.hclust, k=2)
table(wisc.pr.hclust.cut, diagnosis)

## diagnosis
## wisc.pr.hclust.cut B M
## 1 28 188</pre>
```

#Q15. This new model has an error rate of 9%. It is a slight improvement over the hierarchical clustering we did on the raw data. (52 errors now, over 61 errors previously).

##

2 329

24

```
# Compare all Results

## K-means Clustering
table(wisc.km$cluster, diagnosis)

## diagnosis
## B M
## 1 1 130
## 2 356 82

## Hierarchical Clustering on Data
table(ans [3,], diagnosis)
```

```
##
      diagnosis
##
         В
              М
        12 165
##
         2
##
     2
              5
##
     3 343
             40
          0
##
```

```
## Hierarchical Clustering on PCA Analysis
table(wisc.pr.hclust.cut, diagnosis)
```

```
## diagnosis
## wisc.pr.hclust.cut B M
## 1 28 188
## 2 329 24
```

#Q16. Accuracy-wise overall, hierarchical clustering on PCA Analysis takes the win. It also identifies the lowest number of false negatives, which makes this the safest method for its application.

Sensitivity/ Specificity

#Q17. Total Malignant: 212, Total Benign: 357

K-means Clustering

Sensitivity: 130/212 = 61.3%

Specificity: 356/357 = 99.7%

Hierarchical Clustering

Sensitivity: 165/212 = 77.8%

Specificity: 343/357 = 96.1%

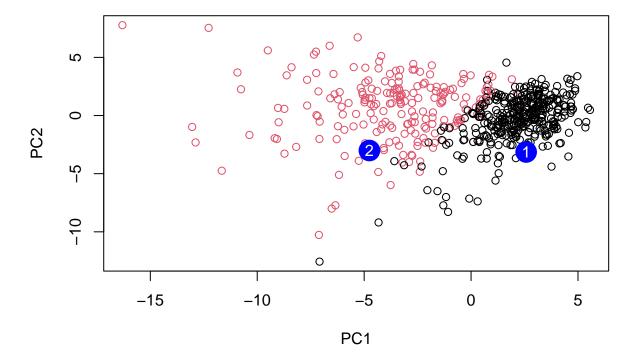
Hierarchical Clustering on Principal Components

Sensitivity: 188/212 = 88.7%

Specificity: 329/357 = 92.2%

```
# Import New Data Points
new <- read.csv("new_samples.csv")
npc <- predict(wisc.pr, newdata=new)

# Plot Old Data with Two New Points Overlay
plot(wisc.pr$x[,1:2], col=factor_diagnosis)
points(npc[,1], npc[,2], col="blue", pch=16, cex=3)
text(npc[,1], npc[,2], c(1,2), col="white")</pre>
```



 $\#\mathrm{Q}18.$ Patient 2 should be prioritized as they probably have the malignant tumor.