

Machine learning for shape memory graphene nanoribbons and applications in biomedical engineering

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Abstract: Shape memory materials have been playing an important role in a wide range of bioengineering applications. At the same time, recent developments of graphene-based nanostructures, such as nanoribbons, have demonstrated that, due to the unique properties of graphene, they can manifest superior electronic, thermal, mechanical, and optical characteristics ideally suited for their potential usage for the next generation of diagnostic devices, drug delivery systems, and other biomedical applications. One of the most intriguing parts of these new developments lies in the fact that certain types of such graphene nanoribbons can exhibit shape memory effects. In this paper, we apply machine learning tools to build an interatomic potential from DFT calculations for highly ordered graphene oxide nanoribbons, a material that had demonstrated shape memory effects with a recovery strain up to 14.5% for 2D layers. The graphene oxide layer can shrink to a metastable phase with lower constant lattice through the application of an electric field, and returns to the initial phase through an external mechanical force. The deformation leads to an electronic rearrangement and induces magnetization around the oxygen atoms. DFT calculations show no magnetization for sufficiently narrow nanoribbons, while the machine learning model can predict the suppression of the metastable phase for the same narrower nanoribbons. We can improve the prediction accuracy by analyzing only the evolution of the metastable phase, where no magnetization is found according to DFT calculations. The model developed here allows also us to study the evolution of the phases for wider nanoribbons, that would be computationally inaccessible through a pure DFT approach. Moreover, we extend our analysis to realistic systems that include vacancies and boron or nitrogen impurities at the oxygen atomic positions. Finally, we provide a brief overview of the current and potential applications of the materials exhibiting shape memory effects in bioengineering and biomedical fields.

Keywords: Shape memory effects; DFT calculations; physics-based multiscale modelling; data-driven dynamic environments; knowledge engineering and machine learning; critical size of nanostructures; first-principles studies; biomedical applications; moment tensor potentials; phase transformations.

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1. Introduction

Materials with shape memory effects have revolutionized the fields of bioengineering and biomedicine. Some prominent examples of their applications in these fields include sensors and actuators, medical implants, coronary stents, organ frame retractors, artificial muscles, to name just a few. Shape memory materials (SMMs), a subgroup of intelligent materials, have taken their prominent place in these fields due to their ability not only to sense environmental changes, such as temperature, forces, electromagnetic fields, solvents, humidity, but also to respond to such changes, adjusting their parameters in order to return to their original state [1]. The role of such parameters can be taken by their shape, position, strain, etc. Therefore, it should not come as a surprise that SMM applications cover also many other areas, well beyond already mentioned, and may also

38 include deployable components of complex systems, energy conversion, and energy
39 harvesting. Today, such areas as orthopedics and orthodontics, with a wide range
40 SMM-based biomedical devices, are simply unimaginable without an extensive usage of
41 these materials.

42 Concurrently with the continuing developments in conventional shape-memory
43 materials, more recent research on advanced biomedical applications has also been
44 focusing on graphene-based nanostructures, and in particular on graphene nanoribbons
45 (GNRs, [2]). The latter structures are known for their superior properties, including large
46 surface area, enhanced mechanical strength, and improved electro-conductivity, which
47 make them a major candidate for many applications in biomedicine and bioengineering,
48 including biosensing and diagnostics. GNRs can be used for fast DNA sequencing
49 and can also make good memories, as has been known for quite some time [3,4]. The
50 scope of applications of graphene-based materials, also termed as “smart”, has grown
51 significantly over the recent years [5,6]. With the rise of data-driven modelling [7–9],
52 machine learning tools and associated methodologies of computational statistics become
53 increasingly important for further progress in these fields [10].

54 The search for materials that can lead to the fabrication of devices with low-
55 energy consumption has attracted the scientific community to the 2D materials realm.
56 Graphene promises not only that but also a myriad of exotic properties. Its derivatives
57 can further improve certain desired properties. Graphene oxide (GO) is among these
58 derivative systems that can modulate or enhance the thermomechanical and energy
59 storage properties, due to the presence of oxygen functional groups attached to the
60 layer. Compared to the pristine graphene, GO is cheaper to produce [11] and easy
61 to deposit on a variety of substrates making it suitable for flexible electronics and
62 bioengineering applications [12–14]. GO can be synthesized by either bottom-up or top-
63 down techniques including the Staudenmaier, Brodie, Offeman, Hummer methods [15],
64 and environmentally friendly modifications of them to eliminate the emission of toxic
65 gases [11]. The presence of the epoxide groups alters the electronic band structure and
66 density of states near the Fermi level [16]. As a result, a non-zero bandgap is generated
67 which can be modulated by rearranging the distribution and concentration of oxygen
68 atoms in the surface. The bandgap can be used to take advantage of GO as a luminescent
69 material to be used for biological imaging [17,18]. Epoxide groups can also be used to
70 trap lithium atoms in regions with poor electronic density [19], allowing the use of GO
71 in Li storage devices. GO has also found potential applications for hydrogen storage
72 [20,21] and water purification [22,23].

73 On the other hand, GO nanostructures can be employed as nanofillers to strengthen
74 mechanical properties of polymers [24] and can be used to fabricate artificial tough
75 nacre of interest in aerospace applications [25,26]. Also, GO can endow with shape
76 memory behavior to nanocomposites [27,28] for bone repair with minimal invasive
77 surgery [29], and electrical actuators with low power consumption [30], essential for
78 many applications in bioengineering. Recently, first-principle calculations have shown
79 that GO with highly ordered epoxy groups can experience shape memory effect on its
80 own without the presence of a polymer matrix [31,32] and can experience recoverable
81 strain rates up to 14%. Applications for such shape memory nanomaterials include
82 resonators, artificial muscles, and molecular robots [33], among many others. The
83 carbon-oxygen-carbon interfaces in the GO layer induce the presence of an additional
84 stable phase. The two phases, located at different lattice constant values, are separated
85 by about ~ 100 meV. The system can be deformed from one phase into the other one by
86 application of an external force or an electric field [31].

87 In this work, we use machine learning (ML) to study GO nanostructures not only
88 to reduce the computational cost involved in the estimation of the two stable phases,
89 but also to analyze the response of GO nanoribbons subject to deformations, and the
90 presence of vacancies and impurities. This work is an extension of [34]. Here, we show
91 different approaches used to improve the model prediction, the approximate critical

nanoribbon size for which shape memory effect is suppressed, and its validation with actual DFT results. Finally, the machine learning potential is used for a systematic study in which a more realistic distribution of oxygen positions covers the GO surface instead of a highly ordered distribution, the effect of vacancies, and impurities such as boron and nitrogen atoms.

2. Methods

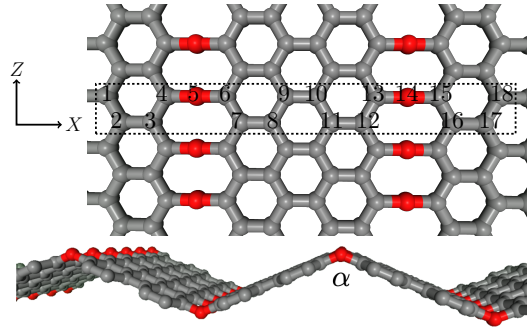


Figure 1. Top: GO structure before structural optimization. The unit cell is shown in between dashed lines. The unit cell's length along the X-direction defines the lattice constant, a_{lat} . **Bottom:** Side view of the optimized GO structure using DFT. Gray(red) balls represent carbon(oxygen) atoms.

From the different arrangements in which a highly oxygen-ordered configuration can be found in a GO layer, we focus our attention in the C_8O structure defined in [31] since it exhibits shape memory effect and the two different phases in which it can be energetically stable. The unit cell is depicted in Fig.1. The periodicity of the unit cell along the X and Z directions defines a 2D sheet. From the figure, it can be noticed that the oxygen epoxy groups define graphene stripes of zigzag interfaces. The electronic re-arrangement around the zigzag interfaces bends the 2D layer at angle α , as shown by the optimized DFT structure also represented in Fig.1. According to [31], the GO sheet presents two phases around $\alpha = 104^\circ$ and 133° [31,32], corresponding to lattice constants of $a_{\text{lat}} \sim 16 \text{ \AA}$ and 18.5 \AA . The two phases are separated by $\sim 100 \text{ meV}$. First-principles DFT calculations will be used to validate literature results.

Specifically, we perform spin-polarized DFT calculations to relax the atomic positions at several fixed lattice constants to build the energy vs lattice constant curve. All of our DFT calculations were performed by using the Quantum ESPRESSO simulation package [35], plane-wave basis sets, and ultrasoft pseudopotentials [36], while employing the gradient approximation with the PBE exchange-correlation functional [37]. Our tests of convergence showed optimal values for a wavefunction energy cutoff of 60 Ry and a $4 \times 1 \times 4$ Monkhorst-Pack k-point grid (periodicity is along the X and Z directions). Here we used an interlayer separation of 18 \AA to ensure a minimum distance of $\sim 12 \text{ \AA}$ between atoms, even with a bent structure for the range of lattice constant values considered (from $a_{\text{lat}} = 14 \text{ \AA}$ to $a_{\text{lat}} = 19 \text{ \AA}$).

2.1. Moment tensor potentials (MTP)

After the validation, we have employed ML approaches that can mimic the DFT results and allows us to predict the behavior of nanoribbons with very big super unit cells, multiples of the unit cell shown in Fig.1 with periodicity only along the X-direction. We use a physics-based ML model designed for materials, coded in the MLIP package [38] that we use to build an interatomic potential for the GO system.

The MLIP code is based on moment tensor potentials (MTP) [38,39]. In this machine learning approach, the quantum mechanical energy of a structure, E_{QM} , is approximated as a sum of interatomic potentials, V ,

$$E_{\text{QM}} \approx \sum_i V(\mathbf{n}_i), \quad (1)$$

where \mathbf{n}_i represents the neighborhood of the i -th atom, given by a collection of atomic positions and species of each neighbor atom up to cutoff radius. V is expressed as an expansion of polynomials

$$V(\mathbf{n}_i) = \sum_{\alpha=1}^N c_{\alpha} B_{\alpha}(\mathbf{n}_i), \quad (2)$$

where the expansion in the polynomial B_{α} and its construction ensures V to be invariant to structure's rotation and permutations of the same-species elements. B_{α} is build in terms of the moment tensor potentials $M_{\mu,v}$ defined as

$$M_{\mu,v}(\mathbf{n}_i) = \sum_j |r_i|^{2\mu} r_i^{\otimes v}, \quad (3)$$

where $r_i^{\otimes v}$ indicates the v -times the Kronecker product of r_i .

The model is trained by finding the coefficients c_{α} that best fit not only the quantum mechanical energy of the system in expression (1), but also the forces on each atom (derivative of (1) with respect to atomic positions), and stress values (proportional to the derivative of (1) with respect to lattice constants), values that were found in static DFT results.

The model built through the learning of energy, forces, and stress values can be used to relax the atomic positions. In the relaxation process, the different configurations generated are graded according to geometric considerations. If a configuration is found to be an extrapolation from the training set and its grade is higher than a threshold grade value ("active learning"), a static DFT calculation is required on the new configuration to obtain its energy, forces, and stress.

2.2. ML implementation for a GO layer

We generate an initial set (IS) of 41 artificial structures as shown in Fig.1 with lattice constant values over the range from 14 to 20 Å to analyze the GO energy dependence on the structure length along the X-direction and learn from the associated stress. Atomic equilibrium positions were approximated to a pristine graphene nanoribbon with a carbon-carbon distance of 1.42 Å.

Given the IS, the relaxed structures have been found by MTP and compared to DFT calculations. In the process of building the interatomic potential, a training set (TS) is generated, from which static DFT calculations are performed. Now, the interatomic potential is created. However, it is possible to build a new potential with higher accuracy prediction by choosing new configurations closer to the ground state, although the new potential will have an energy prediction valid for a window of energies restricted to the neighborhood above the ground state.

2.3. ML implementation for GO nanoribbons

Finally, we extend the study to armchair GO nanoribbons (AGONRs) using an ML interatomic potential. The training set is composed of DFT optimized structures with different widths. The provided atomic environments will be used to train an MTP model which will be used as an interpolation tool to estimate the energy dependence over the lattice constant. This approach will let us study the effect of confinement on the shape memory behavior of a GO sheet, and the evolution of the two phases at finite nanoribbons widths.

The ML interatomic potential allows us to investigate GO nanoribbons of large widths compared to what is accessible through DFT calculations. Oxygen vacancies and lower ordered epoxy groups are considered as part of realistic configurations that can be

found in GO. We also analyze the effect of boron and nitrogen atoms replacing oxygen atoms.

3. Results and discussions

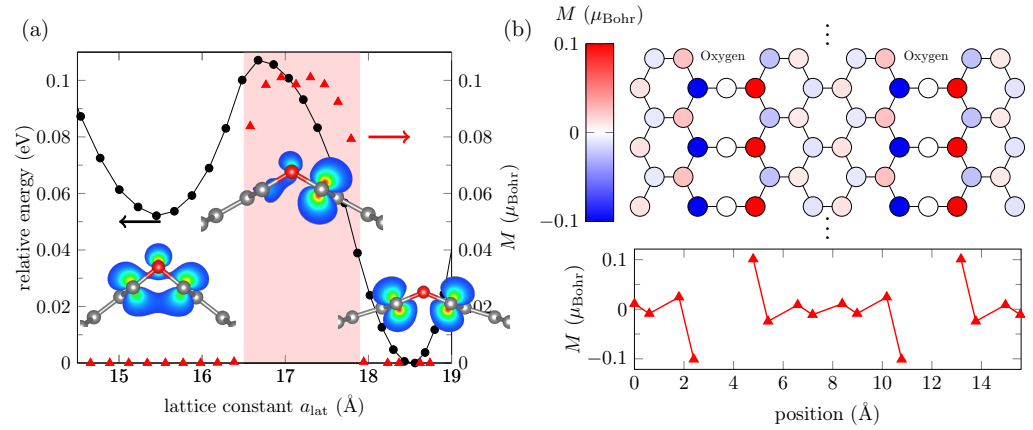


Figure 2. (a) Energy (black marks) and maximum magnetization (red marks) found in optimized GO nanoribbons of different widths, according to DFT calculations. The red shadowed area indicates non-zero magnetization for structures in the corresponding lattice constant range. The insets show partial charge densities around the oxygen atoms (red balls) and carbon atoms (gray balls) for three a_{lat} values: 15.5 Å, 17 Å, and 18.5 Å. (b) Magnetization at each atomic site in the unit cell of a GO layer of $a_{\text{lat}} = 17$ Å.

DFT validation is shown in Fig. 2a. The 2D system exhibits a stable phase at ~ 18.5 Å and a metastable phase at ~ 15.5 Å, separated by 60 meV. The symmetry evolution of the electronic wavefunction can be noticed in the inset of the same figure. The electronic distribution around the oxygen atoms is rearranged as the system is shrunk into an anti-bonding-like configuration, with higher energy, and then again into a bonding-like configuration, for ~ 17 Å and ~ 15.5 Å, respectively. The electronic rearrangement around the bendings in the red shadowed area in Fig. 2a behaves as quantum wells, effectively isolating the zigzag graphene nanoribbons (ZGNRs) between the rows of oxygen atoms. The electronic repulsion at carbon atoms in isolated ZGNRs leads to ground state magnetic solutions. The magnetic distribution in ZGNRs is similar to Fig. 2b, where magnetization reaches a maximum value at the edges. The application of an electric field has a parallel component to each ZGNRs plane, and it leads to a rearrangement of charges across the zigzag interfaces that could break the isolation of the ZGNRs, and hence lowering down the energy barrier between the phases. As shown in [31], the application of the right electric field intensity destroys the energy barrier between the two phases and generates instead a new global energy minimum. Therefore, the application of an electric field shrinks the system into a new lattice constant. In what follows, we will use ML to learn from this structure with no electric field applied.

3.1. ML results for a GO layer

The 41 structures in the IS were used to start the iterative process of selection, training, and relaxation. Convergence tolerance is achieved and the RMSE of the trained potential is 75 meV (or 4 meV per atom). 395 configurations are generated as the TS, and static DFT results are used to feed the training process. The TS spans over 1 eV above the ground state configurations, as shown in Fig. 3a. We use the trained interatomic potential to reproduce the DFT energies in the TS and to relax the configurations in the IS. Fig. 3b gives a better idea of the extent of the accuracy of the trained potential. While it can predict accurately enough for configurations with higher energies, it fails for about 10 meV for configurations around the second phase (~ 18.5 Å). We extract the atomic positions of DFT relaxed configurations to verify if the ML prediction energy agrees with

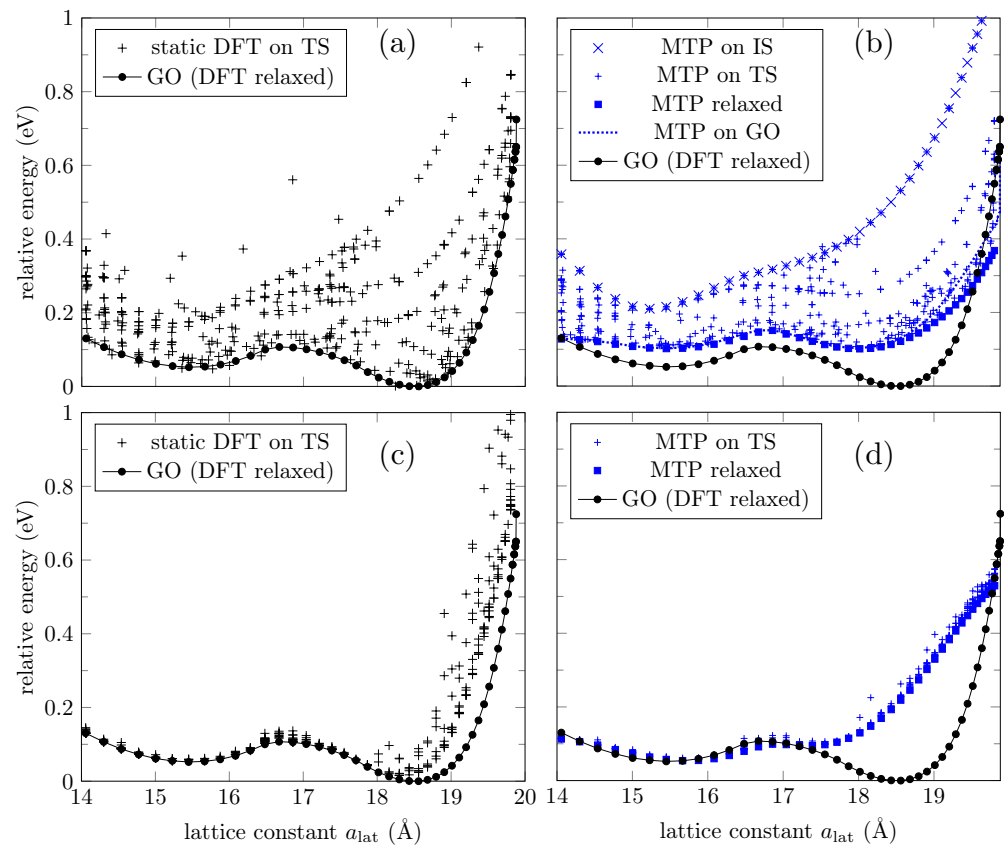


Figure 3. (a) Energy distribution of the training set (TS) compared to the ground state energies according to DFT calculations (circle marks). (b) Energy distribution of the input set (IS) and TS according to the ML potential. The IS has been relaxed using the ML potential (blue circle marks) and DFT (black circle marks). (c) Same as (a), but with an improved IS. (d) Energy distribution of the TS according to an improved ML potential.

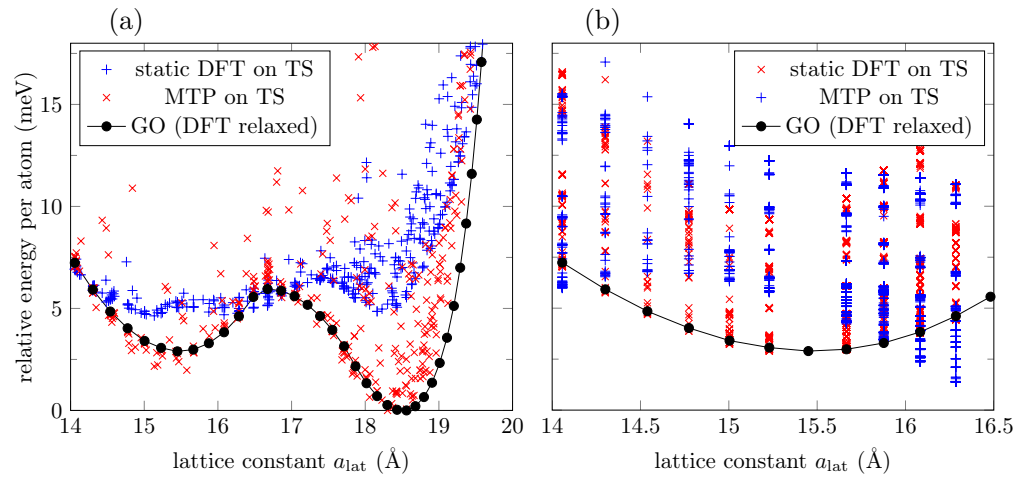


Figure 4. (a) Energy distribution of the TS for a model trained using a cutoff of 10 Å, according to DFT and MTP. (b) Energy distribution of the TS for a model trained on a restricted range of lattice constant values from 14 Å to 16.5 Å. For comparison, ground state energies, according to DFT calculations, are provided (black marks).

202 DFT. The potential agrees that those are the ground state configurations ("MTP relaxed"
 203 and "MTP on GO" curves coincide in Fig.3b), but again the energy prediction is higher
 204 around the second phase (see "GO" curve in Fig.3b). Still, the ML potential can find the
 205 two local minima around the two phases.

206 To increase the accuracy of the ML potential, we now take as IS to be the 41 MTP
 207 relaxed configurations in the previous process (configurations for which energies were
 208 plotted as the "MTP relaxed" curve in Fig.3b). In this specific case, the new IS already
 209 coincides with the DFT relaxed configuration, as discussed above. The iterative process
 210 of selection, training, and relaxation is repeated until convergence is achieved. The RMSE
 211 is 111 meV (or 6 meV per atom). 386 configurations were generated by MTP to train
 212 the ML potential. Fig.3c shows the energy distribution of the new TS compared to the
 213 ground state energies. We can notice that the TS includes ground state configurations up
 214 to ~ 18.5 Å only. The new ML potential is used to reproduce the energies of configuration
 215 in the TS, and the results are shown in Fig.3d. We also employ the ML potential to "relax"
 216 the IS (although they already coincide with the DFT relaxed configurations); we expected
 217 the energies to coincide with the ground state according to DFT. The results are exhibited
 218 as the "MTP relaxed" curve in Fig.3d. The curve partially recovers the DFT ground state
 219 energies, but fails to predict the behavior around the second phase. This result is in
 220 part due to the lack of the required configurations in the TS around the second phase,
 221 and in part due to the long-range interactions introduced by spin-polarized carbon
 222 atoms (see Fig.2b) that MTP is not able to learn from. MTP approximates the quantum
 223 mechanical energy of the system to a sum of local energies (Eq.1), and as stated in [39],
 224 the assumption could not be valid at all for systems with long-range interactions.

225 Letting MTP learn from larger atomic neighborhoods to account for long-range
 226 interactions might improve accuracy prediction. MTP learns from each atomic neighborhood
 227 (Eq.1) and so far we have worked with a default cutoff value of 5 Å, which includes
 228 interactions up to the third nearest neighbors in a graphene derivative. However,
 229 choosing an ML potential with a larger cutoff of 10 Å does not seem enough to improve
 230 accuracy prediction at low energies, as shown in Fig.4a.

231 Magnetic solutions introduce additional complexity that MTP cannot capture to
 232 make accurate energy predictions. Hence, we will focus on a lattice constant range for
 233 which no magnetic configurations have been found. The ML potentials have shown
 234 better accuracy prediction around the first phase, so we now restrict the IS and TS
 235 to configurations with $a_{\text{lat}} = 14$ Å to $a_{\text{lat}} = 16.5$ Å. Results are presented in Fig.4b.

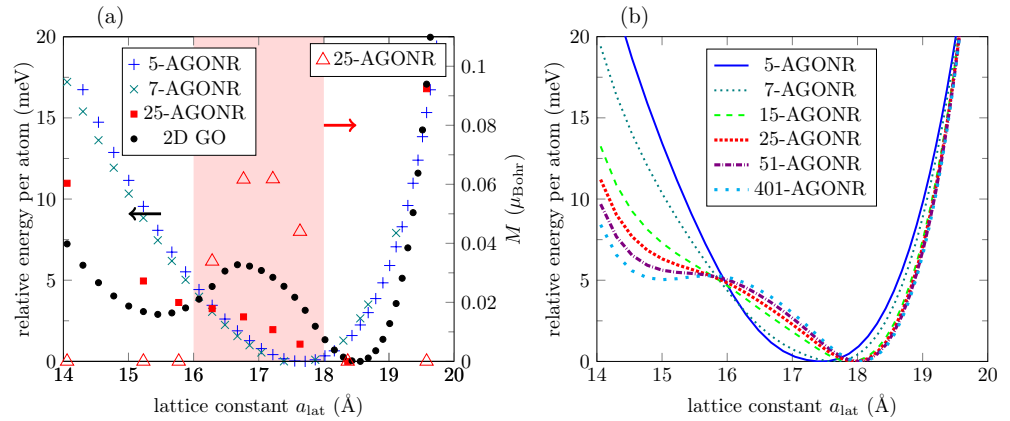


Figure 5. (a) Energy evolution of relaxed m -AGONRs with $m = 5, 7, 25$ armchair lines, according to DFT calculations. For comparison, ground state energies of the GO layer are included (black circle marks). The red shadowed area indicates non-zero magnetization for a nanoribbon with $m = 25$ in the corresponding lattice constant range. (b) Energy evolution for GO nanoribbons with different widths according to the ML potential.

236 However, the generated TS includes more than 1,000 configurations, so it is no longer
 237 computationally cost-effective to continue trading for a higher accuracy prediction.

238 3.2. ML results for GO nanoribbons

239 Training an ML model for the highly oxygen ordered C_8O layer involves the
 240 learning of atomic environments of 18 atoms per unit cell. For GO nanoribbons, ML
 241 training might result challenging due to the computational cost involved in the DFT
 242 calculations of the TS (even though they are static calculations), except for very narrow
 243 strips. Therefore, to build the ML model for nanoribbons we choose relatively narrow
 244 nanoribbons that have been DFT relaxed, and restrict our ML model to work with
 245 configurations very close to the ground state configurations. In this part, we are not
 246 following the selection, relaxation, and training iterations as we did for 2D GO. Here,
 247 MTP is not used to relax structures, instead we use MTP only as an interpolation tool
 248 to find the approximate energies of GO nanoribbons. To generate the TS, we combine
 249 DFT results for relaxed nanoribbons and 2D GO, so that MTP can find the interpolated
 250 energies for structures all the way from 1D to 2D structures.

251 Fig.5a displays the evolution of DFT relaxed nanoribbons of different widths
 252 compared to the GO layer. While the GO layer has a global minimum at ~ 18.5 Å,
 253 narrow nanoribbons have a minimum at ~ 17.5 Å. However, the global minimum
 254 shifts to larger lattice constants for wider nanoribbons, as revealed by the 25-AGONR's
 255 evolution. Additionally, narrow nanoribbons do not present ground state magnetic
 256 solutions. This scenario changes for 25-AGONR, in which maximum magnetization is
 257 no longer zero, but it is at half range to the maximum magnetization found for the 2D
 258 GO (compare triangle marks in Fig.5a and Fig.2a). Finally, Fig.5a shows that while 5-
 259 and 7-AGONRs evolve with a very well defined convexity, the 25-AGONR presents a
 260 noticeable change in the gradient at around ~ 15.5 Å, i.e., the formation of an additional
 261 phase begins to take place, although there is no local energy minimum defined yet.

262 As explained above, we combine DFT results for nanoribbons and the 2D layer
 263 to construct the TS which are used to train ML potentials. Several TS can be built:
 264 3-AGONR/GO, 5-AGONR/GO, 7-AGONR/GO, and combinations between them. The
 265 ML model with TS as 3-AGONR/GO can describe well the convergence to the 2D system,
 266 but overestimate the energies for narrow nanoribbons, possibly due to an overestimation
 267 of the edge to edge interaction, which should decrease rapidly for nanoribbons with
 268 higher widths. The potential trained with TS as 5-AGONR/GO can reproduce better
 269 DFT results for narrow nanoribbons, but fails to reproduce the formation of the two

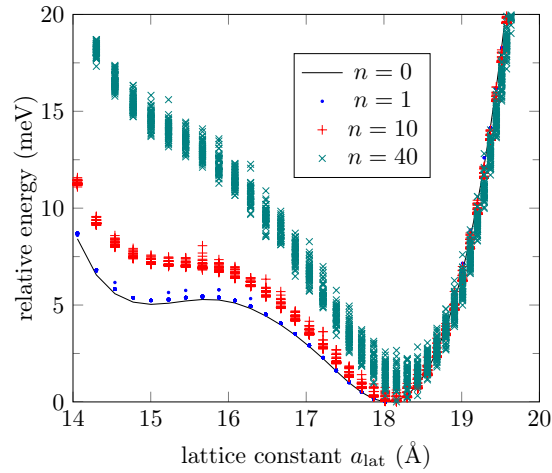


Figure 6. (a) Energy distribution, according to the ML potential, of a pristine 401-AGONR ($n = 0$), and in the presence of $n = 1, 10, 40$ vacancies out of 400 oxygen atoms at random positions. 50 samples are collected for each lattice constant and for each n .

phases at the 2D limit, possibly due to the lack of enough oxygen-oxygen interaction data (5-AGONR has only 2 Oxygen atoms at each bending). Fig.5b presents results for the best ML potential we found, in terms of convergence to the 2D limit, the evolution of the two phases for nanoribbons with higher widths, and the low energy prediction error for narrow nanoribbons. The ML potential was trained with TS as 7-AGONR/GO. It predicts the change in the gradient for the 25-AGONR energy curve (25-AGONR DFT results are not contained in the TS), and it can even describe the shift of the global minimum for wider nanoribbons.

Furthermore, Fig.5b tells us that the stable phase is rapidly created when increasing the nanoribbon width, while the metastable phase (at $a_{lat} \sim 15 \text{ Å}$) gradually appears at a slow rate. Therefore, the metastable phase is associated with the formation of new states due to the oxygen-oxygen interactions in the same row that strengthen as the width increases, and converges at the 2D limit. According to MTP, the first signatures of the metastable phase are predicted to appear around nanoribbons with 25 armchair lines (3 nm wide), results that are confirmed by DFT calculations, For 51-AGONR, the metastable phase is still evolving. For 401-AGONR, around $\sim 50 \text{ nm}$ width, a clear local minimum is obtained. This critical value seems reasonable when compared to the critical size of 60 nm for FePd nanostructures, either with experimental results [40] or via a phase-field model [41]. Here we have used a different approach on a different system to find a critical width in which the effect of confinement suppresses the shape memory behavior in GO nanoribbons.

3.3. Effect of oxygen defects in GO nanoribbons

The robustness of the second phase in the presence of imperfections can now be evaluated through the same ML potential built above (using a TS as 7-AGONR/GO). We consider the case in which the bendings of the GO nanoribbon are partially filled with oxygen atoms. Fig.6 shows the distribution of energies for a 401-AGONR at 0.25%, 2.5%, and 10% of vacancy concentrations (1, 10, and 40 out of 400 oxygen atoms, respectively). For each lattice constant value, 50 samples are generated by randomly removing oxygen atoms over the bendings, so the energies are spread over a range that could remove local minima. As expected, low vacancy concentrations lead to configuration energies close to the ground state. In contrast, the second phase is destroyed for vacancy concentrations around 10%.

So far, we have studied GO with highly ordered oxygen rows. We now address the case of a more realistic configuration in which oxygen atoms adhere to the GO

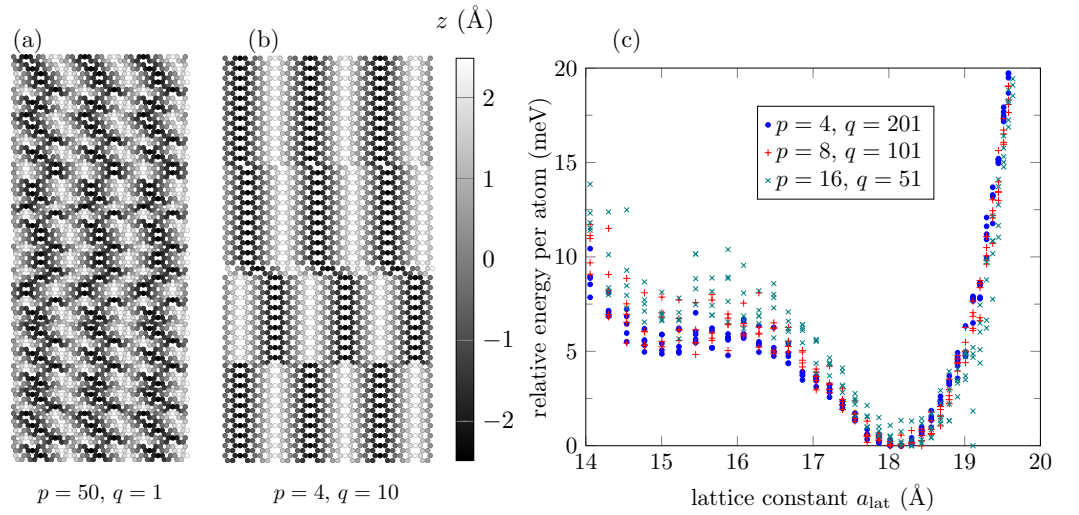


Figure 7. (a) Unit cell of a 50-AGONR with no ordered oxygen atoms over the surface ($q = 1$). (b) Unit cell of a 40-AGONR with partial ordered oxygen atoms, with the order covering a length of $q = 10$ armchair lines. Periodicity is along the horizontal direction (X -axis). Atoms are represented as balls in gray color levels to indicate their atomic height positions over the XY -plane. (c) Energy distribution of a 800-AGONR with partial ordered oxygen atoms at different levels, for $q = 201$ (highly ordered), 101, and 51.

nanoribbon surface at random positions, but are still restricted to the C_8O stoichiometry, as shown in Fig.7a. Yet, the preference for the formation of ordered oxygen rows can be modeled by keeping the same oxygen positions over q armchair lines, and then choose randomly a different oxygen position for the next q armchair lines. A balance between totally random oxygen positions and ordered rows is depicted in Fig.7b. Defects between the ordered interfaces, new oxygen-carbon atom interactions, and other long-range interactions could affect now the nanoribbon energy, as shown in Fig.7c for $q = 201$, in which the second phase still can be found (in the plot, 5 energy samples per lattice constant value were collected using configurations with $\sim 10,800$ atoms per unit cell). The second phase is not totally destroyed even for higher frequent change in the orderings ($p = 8$, and $p = 10$ in the figure), provided that the ordered strips formed between line defects are wide enough to exhibit the two phases if they were isolated from each other (above 51 armchair lines wide).

3.4. Effect of boron and nitrogen substitutions

Other realistic configurations include substitutions of oxygen atoms by impurities. We choose boron and nitrogen atoms as substitutes due that the valence electrons of B and N together equal those of a pair of C atoms. It is known that substitution of carbon by boron atoms in an armchair graphene nanoribbon (AGNR) breaks the conjugated electron system, creating a reflective barrier for the π -electrons, and can induce magnetized edge states [42]. The ordered oxygen atoms in the disposition shown in Fig.1 also define localized states for which a finite magnetization has been found for an interval of lattice constant values. However, oxygen substitutions by boron or nitrogen atoms destroy the two-phase feature, and hence its shape memory behavior. We include here DFT results for structural optimization for oxygen substitutions either by boron or nitrogen atoms (C_8B or C_8N), or with a boron-nitrogen pair of atoms ($C_8B_{0.5}N_{0.5}$). Fig.8 shows the relative energy to each case for different lattice constant values, with bending angles from 100° to 180° (flat system). The two-phase feature displayed by C_8O is lost.

We follow a similar procedure to generate configurations with oxygen vacancies in the previous section using the ML potential. Random oxygen atoms were chosen to be replaced either by boron atoms, presented in Fig.9.a, or nitrogen atoms, shown in Fig.

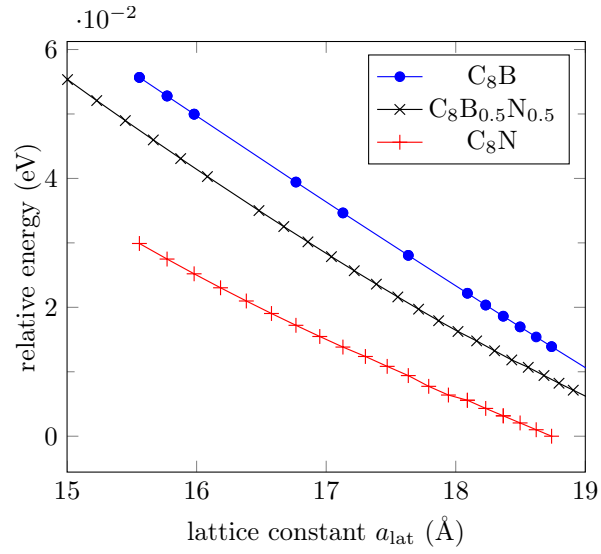


Figure 8. Energy evolution of relaxed GO layers when all oxygen atoms are replaced by boron (blue marks) or nitrogen (red marks) atoms or a pair B-N (black marks), according to DFT calculations.

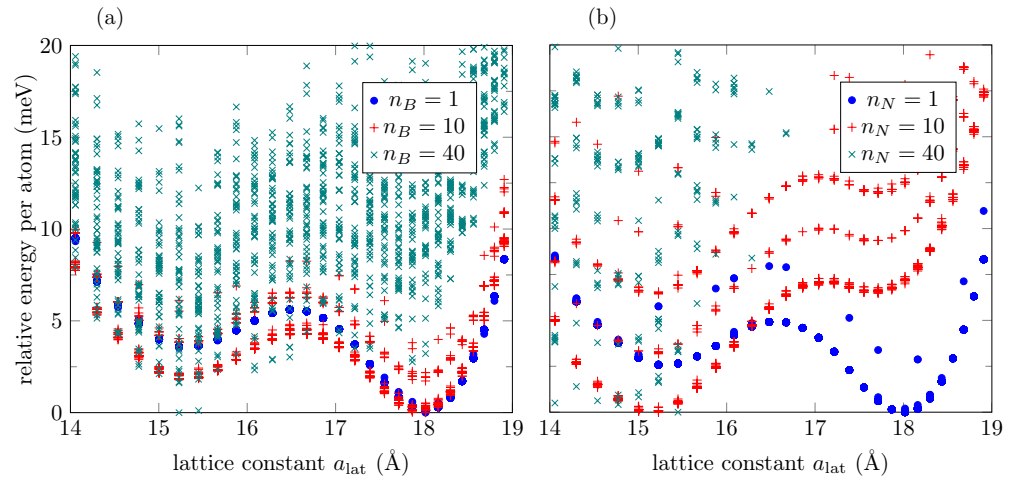


Figure 9. (a) Energy distribution, according to the ML potential, for a 401-AGONR where $n_B = 1, 10, 40$ oxygen atoms out of 400 are replaced by boron atoms at random positions. (b) Same as (a) for nitrogen substitutions. 50 samples are collected for each lattice constant and for each n_B or n_N value.

9.b. Low boron substitution concentration (0.25%: $n_B = 1$ out of 400 oxygen atoms) does not exhibit noticeable change. The two-phase feature is only destroyed for a 10% boron substitution concentration. This result contrasts with nitrogen substitutions, in which the two-phase feature is already affected by a 0.25% concentration, and destroyed for a 2.5% concentration.

4. Materials with shape memory effects and their applications in biomedical engineering

In designing materials for biology and medicine, materials with shape-memory effects have played a remarkable role [43]. From efficient responses to injuries and delivering drugs to hardening techniques in producing casts on broken bones, and to implants and prostheses, the healthcare system of today relies heavily on SMMs. Many areas, including orthopaedic surgery and orthodontics, are simply unimaginable without these materials. Moreover, SMMs continue molding many minimally invasive therapies and related bioengineering technologies. Indeed, these materials not only assist in accelerating wound healing, provide self-expandable vascular stents, and result in high clinical effectiveness, but also aid in developing new biomedical appliances, thanks to their biocompatibility properties. They are a critical component for biotribological systems [44,45] which, in their turn, inspire the development of new technologies in bio-related fields. Furthermore, SMMs for biocompatible microactuators, as biocompatible suture materials for tissues such as tendon [46], showed also excellent cytocompatibility properties for better cell adhesion and morphology in different cell culture systems [47]. SMMs have been vital in various methods of tissue engineering, including distraction osteogenesis [48].

From the modelling point of view, much research in these fields is based on the phase-field theory, where the Landau order parameter framework can be applied in the areas ranging from traditional materials science to the phase transitions in the genome-wide dynamic networks and other complex systems. For example, single-molecule stretching experiments on DNA, RNA, and other biological macromolecules opened up the possibility of impressive progress in many fields of life and medical sciences [49], and the methodologies for the analysis in these areas are frequently based on non-convex free energies, which is akin to the analysis of force-induced martensitic phase transformations in SMMs. Since reversibility of structural phase transformations in these materials has profound technological implications, covering many areas including bioengineering, it is important to develop dynamic models of underlying processes [50]. Coupled thermoelastic martensitic phase transformations and microstructure evolution are behind these processes. At the same time, in order to make the dynamic problem tractable in engineering applications, a dimensional reduction of the fully coupled dynamic three-dimensional model for SMMs needs to be carried out, which was for the first time proposed in [51]. The reduced model was approximated by a system of differential-algebraic equations and was applied to the modelling of SMM-based devices such as actuators [52]. This approach allowed to study both stress- and temperature-induced phase transformations and associated hysteresis phenomena in SMM structures in a unified manner [53] and to extend the developed technique to the Cattaneo-Vernotte law for heat conduction, following principles of extended thermodynamics in the context of SMMs [54]. The problems at hand require the development of multiscale approaches [55] and by now we know that a synergy between multiscale modelling and machine learning can provide a very powerful tool for this research [56]. For example, in [57] polycrystalline structures with microstructure properties have been a subject of studies with machine learning and deep learning approaches, combined with multiscale analysis. The interest in machine learning tools for studies of martensitic phase transformations, typical for SMMs, has been growing significantly over recent years [58], and this direction of research has also included various approaches for developing interatomic potentials [59].

387 In parallel with the above research, the search for new composition regions of
388 SMMs to achieve improved control of SMM properties has been underway [60]. One
389 of the key candidates for this search has always been polymeric materials that exhibit
390 shape memory properties. They come in a wide range of forms, from those that can be
391 extracted from biological oils [61] to those that use carbon nanotube reinforcement [62],
392 with many other forms of shape memory polymers and their composites currently under
393 investigation [63,64]. Indeed, each class of such smart, stimuli-responsive shape-memory
394 polymers is designed according to the specific requirements [65], e.g. programmed to
395 a specific temporary shape and such that they can recover their original shape upon
396 the application of various stimuli, depending on a specific application (temperature,
397 electric and/or magnetic field, solvents, light irradiation, etc). In such cases, shape
398 memory properties are influenced by many factors which, in the case of computational
399 studies, would need to be investigated with refined techniques such as first-principles
400 calculations. In the development of various adaptive composite materials for biological
401 applications with embedded shape memory components, other coupled field properties
402 of smart materials, such as piezoelectric, flexoelectric, auxetic, may also become important
403 in the analysis and their applications at the device level [66]. At the smaller scales, shape
404 memory effects and martensitic transformations have also been observed in superlattices
405 [67].

406 In the meantime, the interest in graphene oxide and carbon-based composites
407 with shape memory effects have been grown significantly over the last few years
408 [1,68–71]. Among multiple promising directions, this interest includes also research
409 studies in the context of sustainability pertinent to biomass as the associated carbon
410 source [72] and to 4D printing technologies [73,74]. Other coupled field properties
411 mentioned above, such as auxetic, have also been a subject of studies in graphene-based
412 2D materials [75]. As we mentioned earlier, the issue of microstructure evolution in
413 SMMs has been important since the development of coupled dynamic models describing
414 phase transformations in these materials and the methods for the solution of such
415 models [76]. This issue remains critical for our better understanding of the dynamics of
416 shape memory polymer composites and graphene-based structure with shape memory
417 effects [77]. With graphene- and carbon-based composites exhibiting shape memory
418 effects, new exciting applications continue to arise. Natural sunlight-actuated shape-
419 memory materials with reversible shape change and self-healing abilities based on
420 carbon nanotubes filled conductive polymer composites have recently been reported in
421 [78]. Such composites can be fast healed under IR irradiation and as such, these natural
422 sunlight-responsive materials are amenable to large-scale production, providing new
423 opportunities for the design and fabrication of sunlight-actuated smart devices and
424 soft robotics which can be used in biomedical applications. Bioinspired shape memory
425 graphene properties such as tunable wettability [79] can also bring new applications
426 in these fields, as well as graphene oxide applications for shape memory actuators
427 implemented in micro/nanomechanical systems (MEMS/NEMS, [32]), together with
428 new GNRs with shape memory effects. Finally, we would also mention graphene's
429 environmental stability and staggering transport properties [19], nonvolatile memories
430 based on graphene [80], along with other astonishing characteristics, that can lead to
431 sustainable applications in the future. This, combined with biocompatibility, biodegradability,
432 and unique mechanical properties, will continue contributing to the application of SMMs
433 in the fields of biomedicine and bioengineering.

434 5. Conclusions

435 Motivated by a wide range of applications of materials with shape memory effects in
436 biomedical engineering, which include a growing number of graphene-based structures,
437 in this paper we have paid our special attention to GNRs with shape memory effects.
438 A pair of physics-based ML potentials (based on MTP) has been developed to relax
439 2-dimensional GO structures, each of them targets for different energy prediction range

and accuracy. Long-range interactions due to the magnetism found in ground state structures affect the ML accuracy. A third potential has been generated for energy prediction of GO nanoribbons close to ground state configurations, which allows the study of samples with thousands of atoms, computationally expensive for a purely DFT approach. The ML potential has been used to analyze the evolution of the two-phase feature for nanoribbons with different widths. The suppression process begins around ~ 50 nm and finishes around ~ 6 nm nanoribbon's width, although the magnetization associated with the second phase is still present for 3 nm nanoribbon's width. The ML potential feature predictions for a 3 nm nanoribbon's width have been validated by DFT results.

Furthermore, the ML potential has been used to analyze different defects that can be found in realistic GO nanoribbons. We found that the two shape memory behavior is destroyed for 10% of oxygen vacancy concentrations, but it is stable in front of line defects that break the high oxygen order, provided that the generated strip domains are wide enough to show the two-phase feature on their own. moreover, we found that the two shape memory behavior can be strongly affected by the introduction of nitrogen atoms replacing oxygen atoms, compared to the substitution of oxygen by boron atoms. We expect that future research will involve the generation of an ML potential to account for magnetic effects and the stability of larger structures at non-zero temperatures. Finally, an overview of the current and potential applications of SMMs in biomedical applications has been provided.

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