Assignment 1, COMP4702

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Question 1.2

The first column of the data is a timestamp, with each value being around 30 minutes apart. The data starts at the first of January 2015 and ends in the last day of December.

The second column appears to be a unique ID for each entry, as this number is never repeated and goes up by 1 for each record.

The third column contains numbers between 25 and 30, this is possibly a temperature in degrees. The values also change gradually which seems correct for the given time intervals.

Viewing data on the graph shows that the temperature is low at the start of the year and gradually climbs to it's max around 6 months in, then returns back to a lower temperature in December. This suggests that it is probably temperature measured in the northern hemisphere. Additionally this data has outliers, which is probably instrumentation error.

The fourth column contains numbers between 26 and around 50000. If this is plotted against the date, it can be seen that there are three distinct dips in the data. Two of the dips are at the start of the year and the last is towards the end.

The fifth column contains numbers between 7.3 and 8.3, with a mean of 7.846 and a standard StdDev of 0.142. This suggests that the value doesn't change much. Viewing the data over the date does not show any trends in the data.

When the sixth column is plotted against the fifth column, a linear relationship can be seen, as the values in the sixth column increases when the values of the fifth column increases. This indicates there is some form of relationship between two sets of data.

The last two columns don't provide much information, apart from increased outliers at the end of the year, suggesting that the sensors may be starting to fail.

It could possibly be weather data, containing temperature, humidity, etc.

Question 1.6

```
1 % in is the input array
2 % n is the group size
3 function out = q6(in, n)
4
5 out = [];
6
7 chunks = length(in)/n;
8
9 for i = 1:chunks
```

```
end_ind = length(in) - i * n + n;

start_ind = end_ind - n + 1;
start_ind = max([1, start_ind]);

temp = in(start_ind:end_ind);

temp = in(start_ind:end_ind);

out = [out, temp];

end
end
end
```

Question 2.1

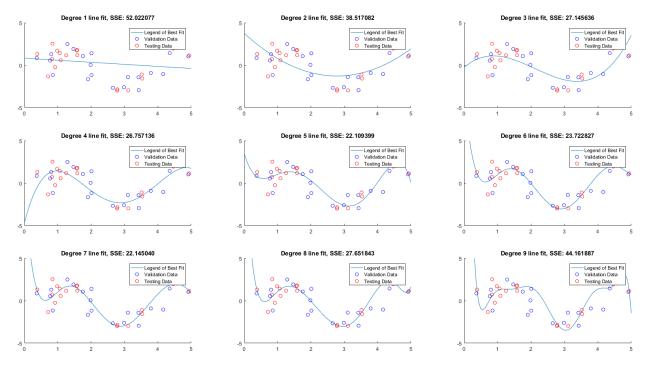


Figure 1: Lines of best fit

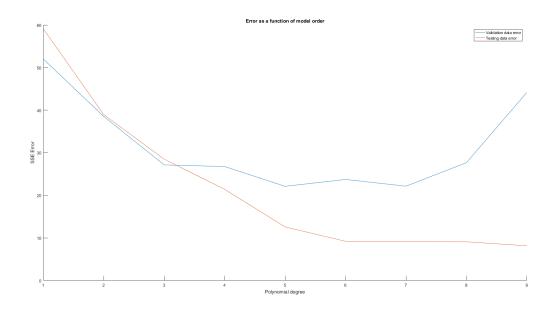


Figure 2: Error vs Polynomial Degree

The above figure shows that as more polynomial degrees are introduced the error on the testing data decreases, which is expected as this was the data the model was trained on. However the error on the validation data increases after the 7th polynomial, thus we are overfitting the data.

Question 2.4

```
function q4(data, class)
       class_names = unique(class);
       x_values = 1: length(class);
       class1 = zeros(1, length(class));
       class2 = zeros(1, length(class));
       for i = x_values
           if strcmp(class{i}, class_names{1})
9
               class1(i) = 1;
10
           else
11
               class2(i) = 1;
12
           end
13
      end
14
15
      % Verify the classes are correct
```

```
% figure;
      % hold on;
18
      % scatter (1: length (class1), class1);
19
      % scatter (1: length (class2), class2);
20
      % hold off;
21
22
       estimate\_range = 1:0.1:8;
23
24
       class1_data = data;
25
       class1_data(class2 == 1) = NaN;
26
^{27}
       class1_mle = mle(class1_data);
28
       class1_pdf = normpdf(estimate_range, class1_mle(1), class1_mle
29
          (2));
30
       class2_data = data;
31
       class2_data(class1 == 1) = NaN;
32
33
       class2\_mle = mle(class2\_data);
34
       class2_pdf = normpdf(estimate_range, class2_mle(1), class2_mle
35
          (2));
36
37
      % figure;
39
      % scatter(x_values, data);
40
41
      % Verify the classes are divided
42
       figure;
43
44
       hold on;
45
46
       yyaxis left;
47
       scatter(class1_data, x_values, 'r');
48
       scatter(class2_data, x_values, 'b');
49
50
       yyaxis right;
51
       plot(estimate_range, class1_pdf, 'r');
52
       plot(estimate_range, class2_pdf, 'b');
53
       legend('Iris Setosa', 'Iris Versicolor');
54
       hold off;
55
56
      % Plot the likelihood
57
       figure;
58
       hold on;
```

```
plot(estimate_range, class1_pdf);
60
       plot(estimate_range, class2_pdf);
61
       x \lim ([1, 10]);
62
63
       title ('Likelihoods');
       xlabel('x');
65
       ylabel('P(x|C_i)');
66
67
       p_class1 = class1_pdf ./ (class1_pdf + class2_pdf);
68
       p_class2 = class2_pdf ./ (class1_pdf + class2_pdf);
69
70
       figure;
71
       hold on
72
73
       plot(estimate_range, p_class1);
74
       plot(estimate_range, p_class2);
75
76
       title('Posteriors');
77
       xlabel('x');
78
       ylabel('P(x|C_i)');
79
80
       hold off;
81
82
  end
83
```

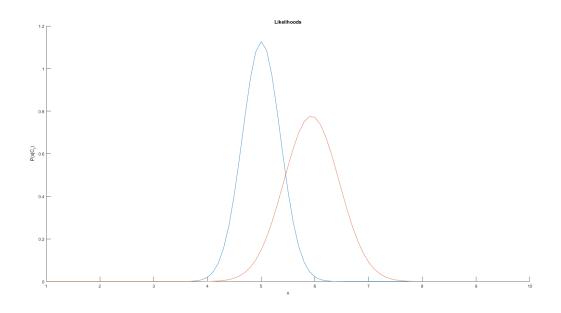


Figure 3: Likelihoods

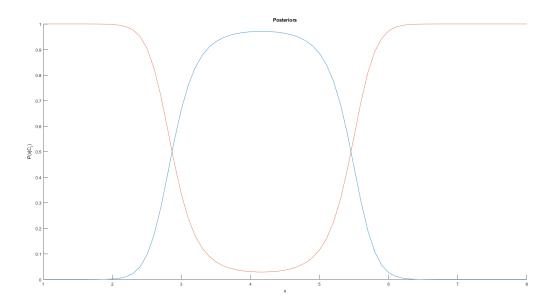


Figure 4: Posteriors

Question 3.1

With the given dataset, we want to find a way to classify the two classes, this can be given by the posterior $P(C_i|x)$. To do so we first need to estimate the prior $P(C_i)$ and p(x|C). This will allow us to estimate the proportion of data points for a given class i. p(x|c) can easily be found by using the matlab function mvnpdf.

Finding the posteriors for each class yields the below graph.

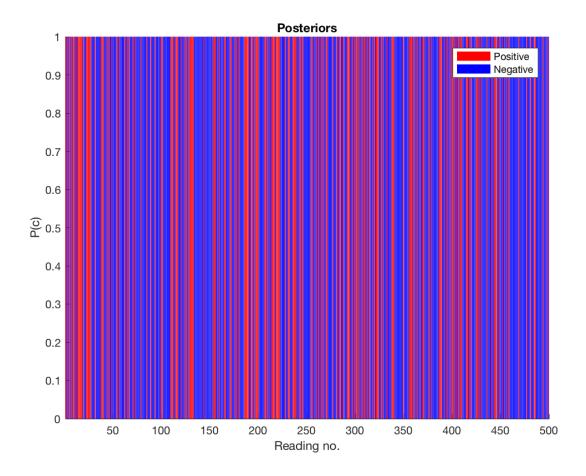


Figure 5: Posteriors

This shows the classification of the algorithm, visually we can see that there is more blue than red, meaning more people test negative to diabetes than positive, which makes sense when you look at the raw data.

The error on the training set was found to be 330.42, while the error on the testing set was found to be 181.18. This is possibly caused by the training set containing many more data rows than the testing set.

The model parameters were found to be the following:

```
1 const =
2 3 14.5107
4 5 6 linear =
7 8 -0.0230
```

```
0.0030
9
        0.0465
10
        0.0089
11
      -0.0099
12
      -0.3704
13
        1.7751
14
      -0.2770
15
16
17
   quadratic =
18
19
     Columns 1 through 6
20
21
                   -0.0004
                                0.0002
      -0.0388
                                           -0.0014
                                                         0.0002
                                                                     0.0012
22
      -0.0004
                   -0.0003
                                0.0001
                                           -0.0001
                                                                     0.0000
                                                         0.0001
23
       0.0002
                    0.0001
                               -0.0008
                                           -0.0003
                                                         0.0000
                                                                     0.0015
24
      -0.0014
                   -0.0001
                               -0.0003
                                           -0.0004
                                                        -0.0000
                                                                     0.0011
25
                                                        -0.0000
       0.0002
                    0.0001
                                0.0000
                                           -0.0000
                                                                     0.0002
26
        0.0012
                    0.0000
                                0.0015
                                            0.0011
                                                         0.0002
                                                                    -0.0019
27
      -0.0717
                                0.0040
                                           -0.0262
                                                         0.0064
                                                                    -0.0130
                   -0.0056
28
        0.0043
                                            0.0008
                    0.0005
                               -0.0004
                                                        -0.0003
                                                                     0.0016
29
30
     Columns 7 through 8
31
      -0.0717
                    0.0043
33
      -0.0056
                    0.0005
34
       0.0040
                   -0.0004
35
      -0.0262
                    0.0008
36
       0.0064
                   -0.0003
37
      -0.0130
                    0.0016
38
      -2.5106
                    0.0301
39
        0.0301
                    0.0005
40
```

Question 3.2

LDA can be implemented similar to the QDA done above.

```
1 %
2 % Q2
3 % Linear Discriminant Analysis
4 %
5
6 % General Steps
```

```
7 % 1. Compute d-dimensional means vectors for each class
 % 2. Compute 'Scatter' matrices in between class and within class
 % 3. Compute eigenvectors and corresponding eigenvalues for the
     scatter matrices
10 % 4. Sort the eigenvectors by decreasing eigenvalues and choose
     the largest to form a matrix (W)
  % 5. Use the new matrix to transform the samples onto the new
     subspace
12
  % Step 0: Load the data
  raw = readtable('pima_indians_diabetes.csv');
15
  raw_data = raw(:, 1:8);
16
17
  \% The classfied classes, e.g. positive or negative
18
  actual = table2array(raw(:, 9));
  training_actual = actual(1:500);
20
  testing_actual = actual(500:end);
21
22
  % Convert the table into an array
  data = table2array(raw_data);
  % Split into training and testing
26
  training = data(1:500, :);
  testing = data(500:end, :);
28
  % Divide training data into positive and negative classes
30
31
  % An array of data
32
  training_positive = NaN(500, 8);
33
  training_negative = NaN(500, 8);
34
35
  % Binary array of samples
36
  positive = zeros(1, 500);
37
  negative = zeros(1, 500);
  for i = 1:500
39
       if strcmp(training_actual(i), 'pos')
40
           positive(i) = 1;
41
           training_positive(i, :) = training(i, :);
42
       else
43
           negative(i) = 1;
44
           training_negative(i, :) = training(i, :);
45
      end
  end
47
48
```

```
zeros(1, length(testing_actual));
  pos_testing =
50
  neg_testing =
                   zeros(1, length(testing_actual));
51
52
  % Parse the testing data
  for i = 1:length(testing_actual)
54
       if strcmp(testing_actual(i), 'pos')
55
           pos_testing(i) = 1;
56
       else
57
           neg_testing(i) = 1;
58
       end
59
60
  end
61
62
  % Step 1: Calculate the mean vectors
63
64
  % Class 1 mean vector
65
  pos_mean_vector = nanmean(training_positive);
66
67
  % Class 2 mean vector
  neg_mean_vector = nanmean(training_negative);
69
70
  % Step 2: Compute scatter matrices
71
  % These will be 8x8 matrices for each class
73
  positive\_scatter\_matrix = zeros(8, 8);
  for i = 1:length(training_positive)
75
      mv = transpose(pos_mean_vector);
76
       row = transpose(training_positive(i, :));
77
78
       if not(any(isnan(row)))
79
           positive_scatter_matrix = positive_scatter_matrix + (row -
80
               mv) * (transpose(row - mv));
       end
81
  end
82
83
  within_class_scatter_matrix = positive_scatter_matrix;
84
85
  negative\_scatter\_matrix = zeros(8, 8);
  for i = 1:length(training_negative)
87
      mv = transpose (neg_mean_vector);
       row = transpose(training_negative(i, :));
89
90
       if not(any(isnan(row)))
91
```

```
negative_scatter_matrix = negative_scatter_matrix + (row -
                mv) * (transpose (row - mv));
       end
   end
94
   within_class_scatter_matrix = within_class_scatter_matrix +
96
      negative_scatter_matrix;
97
   \% Calculate the between class scatter matrix
   between_class_scatter_matrix = zeros(8, 8);
99
100
   overall_mean = transpose(mean(training));
101
102
   \% Do it for positive first
103
   mv = transpose (pos_mean_vector);
104
105
   n = length (find (all ("isnan (training_positive), 2)));
106
107
   temp = n * (mv - overall_mean) * transpose(mv - overall_mean);
108
109
   between_class_scatter_matrix = between_class_scatter_matrix + temp
110
111
   % Do it for negative
112
   mv = transpose (neg_mean_vector);
113
   n = length (find (all ("isnan (training_negative), 2)));
115
116
   temp = n * (mv - overall_mean) * transpose(mv - overall_mean);
117
118
   between_class_scatter_matrix = between_class_scatter_matrix + temp
119
120
   \%\% Step 3: Calculate the eigenvectors and eigenvalues
121
122
   e = eig(inv(within_class_scatter_matrix) *
123
      between_class_scatter_matrix);
   [V, D] = eig(inv(within_class_scatter_matrix) *
124
      between_class_scatter_matrix);
125
   5 Step 4: Sort the eigenvectors and eigenvalues by decreasing
126
      order
   [a, b] = sort(e, 'descend');
127
128
   best_eig_value = a(1);
129
```

```
best_eig_vector = V(b(1), :);
131
   second_best_eig_value = a(2);
132
   second_best_eig_vector = V(b(2), :);
133
  W = zeros(8, 2);
135
136
  W(:, 1) = transpose(best_eig_vector);
137
  W(:, 2) = transpose(second_best_eig_vector);
139
  % The W matrix
140
141
   real (W)
142
143
  % Multiply the training data with W to classify
144
   training_lda = training * W;
```

The error for the training set was found to be 319.41 and the error for the testing set was found to be 178.59.

The model parameters are listed below

```
const =
        7.4066
3
   linear =
      -0.1251
      -0.0319
       0.0114
10
       0.0041
11
       0.0008
12
      -0.0835
      -0.8727
14
      -0.0033
```

Question 3.5

The computed KL values are listed in the table below

| M and H1 | 2.6898 |
|----------|---------|
| M and K1 | 0.2741 |
| | 0 |
| M and K2 | 0.28186 |

There was an issue encountered while finding these variables, it was caused by the 0 values in some of the bins of the histogram estimator, this caused the division to produce Infinity values. This was fixed by replacing the infinity values with 0.

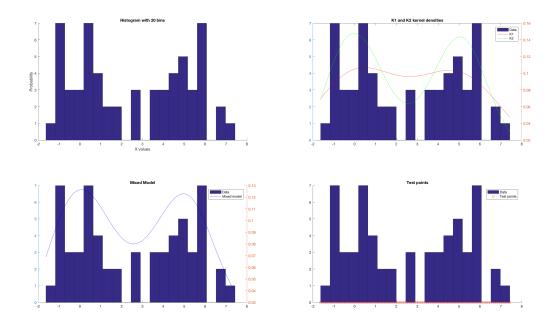


Figure 6: Q5

Below is the code used to calculate the KL function, see the function called KL at the bottom of the script.

```
1 % Q5
2
3 x = [randn(30, 1); 5 + randn(30, 1)];
4
5 subplot(2, 2, 1);
6 hold on;
7 hist(x, 20);
8 title('Histogram with 20 bins');
9 xlabel('X values');
10 ylabel('Probability');
11 hold off;
12
13 % Demo the results
```

```
subplot(2, 2, 2);
  yyaxis left;
  hist (x, 20);
  yyaxis right;
17
  % Generate 100 random datapoints between that covers the range of
     data in x
  x_{points} = \min(x) : ((\max(x) - \min(x)) / 99) : \max(x);
21
  % Generate the histogram bin counts
  [dist, edges] = histcounts(x, 20);
  N = sum(dist);
  x0 = edges(1);
  h = edges(2) - edges(1);
26
27
  data = zeros(1, 100);
28
29
  % Histogram estimator
30
  for i = 1:100
31
       bin = ceil((x_points(i) - x0) / h);
       x_{in}bin = dist(bin);
33
34
       data(i) = x_i n_b in / (N * h);
35
  end
37
  % Create the kernel density estimators
39
40
  \% Default kernel width
41
  [K1, k1x, bw1] = ksdensity(x, x_points);
42
43
  % Half of the default kernel width
  [K2, k2x, bw2] = ksdensity(x, x_points, 'width', bw1/2);
45
46
  hold on;
  plot (k1x, K1, 'r');
  plot (k2x, K2, 'g');
49
50
  title ('K1 and K2 kernel densities');
  legend('Data', 'K1', 'K2');
52
  hold off;
54
  % Calculate the Guassian mixed model
  mixed = K1/2 + K2/2;
57
```

```
subplot (2, 2, 3);
  hold on;
  yyaxis left;
  hist (x, 20);
  yyaxis right;
  plot (k1x, mixed, 'b');
63
  title ('Mixed Model');
65
  legend('Data', 'Mixed model');
  hold off;
67
68
  subplot(2, 2, 4);
69
  hold on;
  hist (x, 20);
71
  scatter(x_points, zeros(1, 100), 'r');
72
73
  title ('Test points');
  legend('Data', 'Test points');
  hold off;
76
  % Do the calculations
  KL(mixed, data)
  KL(mixed, K1)
  KL(mixed, K2)
82
83
  % Calculate the KL Divergence
85
  function result = KL(p, q)
86
       result = zeros(size(p));
87
88
       valid = p > 0 \& q > 0;
89
90
       result1 = sum(p(valid) .* log(p(valid) ./ q(valid)));
91
       result2 = sum(q(valid) .* log(q(valid) ./ p(valid)));
92
93
       result (valid) = result1 + result2;
94
95
       result = mode(result);
  end
97
```