

Transformation matrices;

$$T_{b_1}(0,0,0)$$
 $T_{b_2}(0,0,-0)$

Adjoints:

$$A_{b1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad A_{b1} = \begin{bmatrix} 1 & 0 & 0 \\ -0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Inverse Adjoints:

$$A_{1b} = \begin{bmatrix} 1 & 0 & 0 \\ -0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad A_{1b} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Body Twist in the Wheel Frames

Left wheel;

$$\begin{bmatrix} \dot{\theta} \\ v_{x1} \\ v_{y1} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ -0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dot{\theta} \\ v_{x} \\ v_{y} \end{bmatrix} = \begin{bmatrix} \dot{\theta} \\ -0 \dot{\theta} + v_{x} \\ v_{y} \end{bmatrix}$$

Right wheel:

$$\begin{bmatrix} \dot{\theta} \\ v_{\times 1} \\ v_{Y_1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dot{\theta} \\ v_{\times} \\ v_{Y} \end{bmatrix} = \begin{bmatrix} \dot{\theta} \\ 0 \dot{\theta} + v_{\times} \\ v_{Y} \end{bmatrix}$$

Body Twist to Wheel Motion

Left wheel:

$$\begin{bmatrix} \dot{\theta} \\ \dot{r}\dot{\phi}_1 \\ 0 \end{bmatrix} = \begin{bmatrix} \dot{\theta} \\ -0\dot{\theta} + v_{xx} \end{bmatrix}$$

$$\left[\phi_{1} \right] = \left[\frac{-0}{r} \frac{1}{r} \quad 0 \right] \left[\begin{array}{c} \dot{\theta} \\ v_{n} \\ v_{y} \end{array} \right]$$

Right wheel:

Inverse Kinematics

$$\begin{bmatrix} \dot{\phi}_1 \\ \dot{\phi}_1 \end{bmatrix} = \frac{1}{r} \begin{bmatrix} -D & I & 0 \\ D & I & 0 \end{bmatrix} \begin{bmatrix} \dot{\phi} \\ v_x \\ v_y \end{bmatrix}$$

$$\dot{\Phi}_1 = \frac{1}{\epsilon} \left(- D \dot{\theta} + V_{\infty} \right) \tag{1}$$

$$\dot{\Phi}_{1} = \frac{1}{6} \left(D \dot{\theta} + V_{x} \right) \tag{2}$$

Forward Kinematics

$$\begin{bmatrix} \dot{\theta} \\ v_x \\ v_y \end{bmatrix} = \frac{r}{2} \begin{bmatrix} -\frac{1}{0} & \frac{1}{0} \\ 1 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$\dot{\Theta} = \frac{r}{2} \left(-\frac{\omega_1}{D} + \frac{\omega_2}{D} \right)$$

$$V_{x} = \frac{r}{l} \left(\omega_{l} + \omega_{L} \right)$$

$$\dot{\theta} = \frac{r}{2} \left(-\frac{\dot{\phi}_1}{D} + \frac{\dot{\phi}_2}{D} \right) \tag{3}$$

$$V_{x} : \frac{r}{l} \left(\dot{\phi}_{l} + \dot{\phi}_{l} \right) \tag{4}$$

Update Configuration:

$$\nabla d = \begin{bmatrix} \Omega & \sin \theta & \cos \theta \\ \Omega & \cos \theta & -\sin \theta \\ 1 & \Omega & \Omega \end{bmatrix} \begin{bmatrix} \nabla \theta^{\rho} \\ \nabla^{\lambda \rho} \\ \nabla^{\lambda \rho} \end{bmatrix}$$

QY

Compute Tub' = Tub Tbb'

Use (3) and (4) to get the twist and integrate that twist

Assign the x component to the x of the configuration

y that a