

# How the R-spatial evolution project affects spatial econometrics workflows

[SEA Plenary Session] Spatial Econometrics Software Roundtable, Friday 1:30 pm-3:30 pm, Santa Fe

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## Software round-table

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- Growth and change in software implementation: PySAL and friends: reflections on on boarding, growth, and change; How the R-spatial evolution project affects spatial econometrics workflows.
- Recent changes in modules/packages: PySAL/Spreg – The Module for Spatial Regression Models in Python; Recent developments in R packages sphet, spldv, and hspm.
- Max. 20 min per contribution, discussion after all contributions, but clarifications during contributions are fine.
- Possible (unimportant) points in discussion - where are Stata and SAS (or other closed-source implementations)? Who will be maintaining Matlab contributions?

## Outline

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# Introduction

- Spatial econometrics workflows using the R statistical language may be impacted as the representation of spatial data undergoes modernization.
- The **sp** package and the classes for spatial data there defined will continue to be supported.
- Infrastructure packages **maptools**, **rgdal** and **rgeos** were archived on the Comprehensive R Archive Network (CRAN) 16 October 2023.
- Archiving means that while the source packages are retained in the archive for manual download and installation, they are no longer available for direct installation for users or for other packages.
- These slides are online at [https://r-spatial.github.io/evolution/bivand\\_sandiego\\_2311.pdf](https://r-spatial.github.io/evolution/bivand_sandiego_2311.pdf).

- The functionality provided by the retiring packages, such as reading and writing data and handling geometries may largely be replaced by **sf** and **terra**.
- The **spdep** package providing functions for creating weights matrices and carrying out tests for spatial autocorrelation has already been adapted, as have spatial econometrics packages.
- The R-spatial evolution project tries to facilitate the mitigation of these changes for workflows using retiring packages, including uses in scripts underlying published papers, books, etc.
- This presentation will cover steps that can be taken to reduce impacts on existing workflows, and indicate how new workflows may be constructed to use available data representations in **sp**, **sf** and **terra** going forward.

## R-spatial evolution project

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- It became clear from about ten years ago that the representation of spatial data objects could not simply stay with the initial **sp** object definitions made ten years before that.
- The **sp** spatial vector objects were again based on simpler structures for ESRI Shapefiles in the **maptools** package.
- ESRI Shapefiles do not satisfy the OGC Simple Features standard, do not support modern representations of coordinate reference systems, nor do they properly support multi-byte string encodings.
- **sp** objects have twice been tweaked, once to smuggle some Simple Features structures into polygon representations (exterior/interior rings), later to add a concealed WKT2-2019 coordinate reference system representation.



## R-spatial evolution project

- Modernizing and replacing infrastructure packages in R-spatial workflows affects routines using **sp** (Pebesma and Bivand 2023a), **sf** (Pebesma 2023) and **raster** (Hijmans 2023a) and **terra** (Hijmans 2023b) taken together.
- **sf** (since 2017, Pebesma (2018)) and **terra** (since 2020) have interfaced OSGeo libraries **PROJ**, **GDAL** and **GEOS** directly, using the **Rcpp** (Eddelbuettel et al. 2023) framework.
- This means that they no longer need to use **rgdal** (Bivand, Keitt, and Rowlingson 2023), **maptools** (Bivand and Lewin-Koh 2023) or **rgeos** (Bivand and Rundel 2023) as **sp** and **raster** used to do.
- Using **Rcpp** is more efficient and easier to maintain. Rather than leaving **rgdal** and **rgeos** to decay, they were archived on CRAN 16 October 2023, as first announced in Edzer Pebesma's useR! plenary in July 2021.

- The **sf** package was based on the Simple Features standard, and consequently can interface directly with **GDAL** and **GEOS**, which use Simple Features internally.
- Of course, **GEOS** only works with planar geometries, so **sf** uses **s2** when coordinates are spherical/ellipsoidal for topological operations and predicates.
- **sf** does not provide class definitions for spatial rasters; **sf**-based **stars** (spatiotemporal arrays) does this, as does **terra**.
- **sf** uses unit metric definitions for measurement (Pebesma, Mailund, and Hiebert 2016; Pebesma et al. 2023).

- **sf** supports "**agr**" attributes (Stasch et al. 2014), related to field domains as used by the GeoPackage format <http://www.geopackage.org/guidance/extensions/schema.html>, see also <https://r-spatial.org/book/05-Attributes.html#sec-extensiveintensive>.
- The next step is to work with spatial and spatiotemporal data in the cloud without downloading input data ... so plenty to do going forward, and maintaing outdated packages could not be a priority

## Foundations for archiving retiring packages

- `sf` was well-established on CRAN in 2018, `s2` and `terra` in 2020, `sf` used WKT2-2019 from 2020, followed by `terra` in 2021, and 2022 for updating the GDAL RRASTER driver for WKT2-2019.
- Edzer Pebesma announced that `maptools`, `rgdal` and `rgeos` will be retiring in his online useR! July 2021 plenary 23:42 - 31:20.
- Edzer and I were funded by R Consortium in late 2021 to execute a project to archive the retiring packages minimizing disruption to CRAN packages depending on the retiring packages

## Dependencies on retiring packages

- Dependencies between packages can be represented as a directed graph, so dependencies on retiring packages are edges from other packages to the retiring packages.
- Strong dependencies are those packages that must be installed for the packages depending on them to function.
- All dependencies add weak to strong dependencies; weak dependencies are not required to be present for the package to perform its core functions, but the package should not fail checks when the packages it weakly depends on are absent.

## Process timeline

- From over 550 dependencies in early 2022, we eroded the count down to under 180 on archiving day 2023-10-16.
- Many downstream package maintainers were alerted in December 2022 that **raster** no longer used **rgdal** or **rgeos**, using **terra** in their place; of some 250 packages, only about 30 have not updated.
- Guides and blogs were published on <https://r-spatial.github.io/evolution/>
- The evolution project successfully asked/nudged maintainers of packages depending on retiring packages to update their packages:

##	Sep 2019	Aug 2020	Aug 2021	Jan 2022	Dec 2022	Aug 2023	Oct 2023	Nov 2023
## All	487	519	561	563	497	284	175	36
## Strong	301	314	327	324	265	149	80	0

## Pageranks of R-spatial packages

While dependency graph-based pagerank scores sum to unity over the graph of included packages (and these vary), changes over time show success in suppressing usage (all reverse dependencies) of retiring packages:

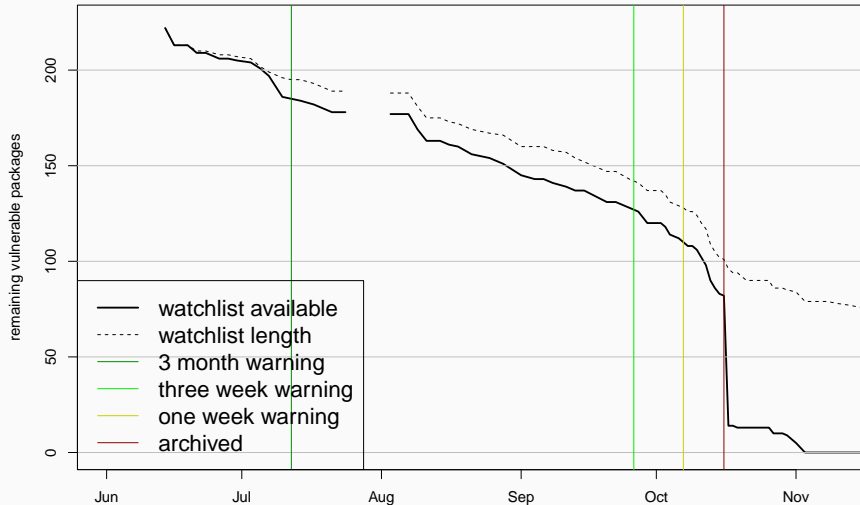
##	Sep 2019	Aug 2020	Aug 2021	Jan 2022	Dec 2022	Aug 2023	Oct 2023	Nov 2023
## sf	0.00078	0.00097	0.00109	0.00115	0.00133	0.00154	0.00168	0.00171
## sp	0.00237	0.00220	0.00190	0.00183	0.00159	0.00141	0.00128	0.00110
## terra	0.00000	0.00002	0.00008	0.00011	0.00029	0.00051	0.00063	0.00067
## raster	0.00149	0.00148	0.00142	0.00139	0.00126	0.00107	0.00097	0.00086
## rgdal	0.00109	0.00105	0.00099	0.00096	0.00079	0.00043	0.00026	0.00005
## rgeos	0.00076	0.00070	0.00061	0.00059	0.00046	0.00027	0.00014	0.00003
## maptools	0.00073	0.00062	0.00055	0.00052	0.00041	0.00022	0.00017	0.00003

## Last five months of process

- After a further extensive round of emails and where possible github issues in April 2023, a watchlist of still vulnerable packages was started in June 2023 and more nudges sent.
- From June 2023, `sp` began to use `sf` in place of `rgdal`; from October 2023, `sp` dropped use of retiring packages.
- If a package on the watchlist is updated on CRAN, it is checked without retiring packages on the library path; if it passes checks, it is removed from the checklist; if no longer available on CRAN it is retained.
- Further warnings were sent to still-vulnerable package maintainers three months, three weeks and one week before archiving.



## Last five months of process



Using ASSE (Kopczewska 2021) as an  
example

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## Using ASSE (Kopczewska 2021) as an example

- Although ASSE (Kopczewska 2021) was largely written five years ago, **sf** is only used in chapters 3 and 10, **terra** is not used, **raster** is used in chapters 2-4 and 9-10, **maptools** is used in chapters 2-6 and 8-9, **rgeos** in chapters 2, 7 and 10, and **rgdal** in chapters 2-6 and 8-10 (thankfully, the code is available); this contrasts with Lovelace, Nowosad, and Muenchow (2019), which does not use retiring packages.
- Packages **spdep** (chapters 2 and 4-5) and **spatialreg** (chapter 5) were a single package until early 2019, so book code post-dates that split; **sf** was added as a strong dependency of **spdep** and a weak dependency of **spatialreg** in early 2019.
- **sphet** is not used, and **pspatreg**, **spsur**, **spldv**, **hspm** post-date the publication of the book.
- We can use a project blog to indicate how the code in ASSE chapters 2, 4-5 might be updated.

- On the evolution project website the code of ASDAR (Bivand, Pebesma, and Gomez-Rubio 2013) is shown as by-chapter diffs between the original code, and code that works without the retiring packages.
- The updated code is available from [https://github.com/rsbivand/sf\\_asdar2ed](https://github.com/rsbivand/sf_asdar2ed).
- Because the ASDAR first and second edition code is executed nightly, problems emerging from changes in packages used are detectable quite quickly.
- For example, a transient problem in **stars** (spatio-temporal arrays) turned up this week in line 118 of `cm2_mod.R`, and was addressed by updating **stars** to the development version (and raising a github issue).

- The ASSE code is not run regularly, and was provided as-is, with no aim to be runnable.
- So first a number of changes had to be made to permit it to run to completion, including the commenting out of **SDMTools** that is archived on CRAN and was not on my desktop machine.
- Other changes included adding those data files that could be located (thanks to Krzysztof Dyba [https://github.com/kkopczewska/spatial\\_book/issues/5](https://github.com/kkopczewska/spatial_book/issues/5)), and corrections of obvious typos.
- Calls to interactive functions were commented out, and code added to record warnings and dump output from running the scripts to file.

## Updating ASSE code to current R

- From R 4.0.0 (April 2020), `stringsAsFactors = FALSE`, but the ASSE code pre-dated that change; adding `stringsAsFactors = TRUE` to all file-reading functions was necessary.
- R on macOS and Linux (`unix` systems) have handled multibyte **UTF-8** characters natively for a long time.
- **UTF-8** was also supported on Windows systems if declared as the preferred encoding, but until R 4.2.0 this was not general; R 4.2.0 for Windows and later are based on Microsoft's universal C runtime (UCRT), rather than many differing CRT versions, and provides system-wide **UTF-8** support.
- Data provided for ASSE is encoded as **CP1250**, so needed conversion where string comparisons or graphics output encountered non-ASCII characters.

## Updating ASSE code to absence of retiring packages

- Minimal updating means keeping to **sp** object representations as far as possible; proper updating would move to **sf** objects.
- Using [https://r-spatial.org/r/2023/04/10/evolution3.html#splitting-r\\_libs](https://r-spatial.org/r/2023/04/10/evolution3.html#splitting-r_libs), the scripts running successfully with retiring packages on the library path were next re-run without retiring packages on the library path to detect failures.
- Because **GISTools** both was itself archived last year for unconnected maintenance oversights and it strongly depends on retiring packages, it had to be dropped; possibly if others use it, a new maintainer could adopt and update it.
- My fork is at [https://github.com/rsbivand/kk\\_spatial\\_book](https://github.com/rsbivand/kk_spatial_book), with diffs of the scripts and their output at [https://rsbivand.github.io/kk\\_spatial\\_book/](https://rsbivand.github.io/kk_spatial_book/)

## Coordinate reference system definitions

- `rgeos` always assumed that geometries were planar (as does `GEOS`), but `sf` uses `s2` for spherical coordinates; for whatever reason, ASSE code transforms from `"ETRS89 / Poland CS92"` to `"NAD83"`, which I corrected to `"OGC:CRS84"` as used by `geojson`; `NAD83` is strictly only for North America, but with spherical coordinates, `s2` will be in play for most topological operations and predicates.
- The provided WKT1 CRS definition in the ESRI Shapefile formatted data is out of date (Bivand 2021), but also note that the more recent definition is in northing-easting axis order; respecting data source axis order is becoming much more important, as are correct datum definitions and their representation.



## Coordinate reference system: OGC:CRS84 i

```
sf::st_crs("OGC:CRS84")

## Coordinate Reference System:
##   User input: OGC:CRS84
##   wkt:
##   GEOGCRS["WGS 84 (CRS84)",
##     DATUM["World Geodetic System 1984",
##       ELLIPSOID["WGS 84",6378137,298.257223563,
##         LENGTHUNIT["metre",1]]],
##     PRIMEM["Greenwich",0,
##       ANGLEUNIT["degree",0.0174532925199433]],
##     CS[ellipsoidal,2],
##       AXIS["geodetic longitude (Lon)",east,
##         ORDER[1],
##         ANGLEUNIT["degree",0.0174532925199433]],
##       AXIS["geodetic latitude (Lat)",north,
##         ORDER[2],
##         ANGLEUNIT["degree",0.0174532925199433]],
##     USAGE[
##       SCOPE["unknown"],
##       AREA["World"],
##       BBOX[-90,-180,90,180]],
##     ID["OGC","CRS84"]]
```

## Coordinate reference system: legacy EPSG:2180 i

```
sf::st_crs(sf::st_read("../kk_spatial_book/Panstwo.shp", quiet=TRUE))
```

```
## Coordinate Reference System:
```

```
##   User input: ETRS89 / Poland CS92
```

```
##   wkt:
```

```
## BOUNDCRS[
```

```
##     SOURCECRS[
```

```
##         PROJCRS["ETRS89 / Poland CS92",
```

```
##             BASEGEOGCRS["ETRS89",
```

```
##                 DATUM["European Terrestrial Reference System 1989",
```

```
##                     ELLIPSOID["GRS 1980",6378137,298.257222101,
```

```
##                         LENGTHUNIT["metre",1]]],
```

```
##                 PRIMEM["Greenwich",0,
```

```
##                     ANGLEUNIT["Decimal Degree",0.0174532925199433]]],
```

```
##             CONVERSION["unnamed",
```

```
##                 METHOD["Transverse Mercator",
```

```
##                     ID["EPSG",9807]],
```

```
##                 PARAMETER["Latitude of natural origin",0,
```

```
##                     ANGLEUNIT["Decimal Degree",0.0174532925199433],
```

```
##                     ID["EPSG",8801]],
```

```
##                 PARAMETER["Longitude of natural origin",19,
```

```
##                     ANGLEUNIT["Decimal Degree",0.0174532925199433],
```

```
##                     ID["EPSG",8802]],
```

## Coordinate reference system: legacy EPSG:2180 ii

```
##          PARAMETER["Scale factor at natural origin",0.9993,
##          SCALEUNIT["unity",1],
##          ID["EPSG",8805]],
##          PARAMETER["False easting",500000,
##          LENGTHUNIT["Meter",1],
##          ID["EPSG",8806]],
##          PARAMETER["False northing",-5300000,
##          LENGTHUNIT["Meter",1],
##          ID["EPSG",8807]]],
##      CS[Cartesian,2],
##          AXIS["(E)",east,
##          ORDER[1],
##          LENGTHUNIT["Meter",1]],
##          AXIS["(N)",north,
##          ORDER[2],
##          LENGTHUNIT["Meter",1]],
##      ID["EPSG",2180]]],
##      TARGETCRS[
##          GEOGCRS["WGS 84",
##          DATUM["World Geodetic System 1984",
##          ELLIPSOID["WGS 84",6378137,298.257223563,
##          LENGTHUNIT["metre",1]]],
##          PRIMEM["Greenwich",0,
```

## Coordinate reference system: legacy EPSG:2180 iii

```
##          ANGLEUNIT["degree",0.0174532925199433]],
##          CS[ellipsoidal,2],
##          AXIS["latitude",north,
##              ORDER[1],
##              ANGLEUNIT["degree",0.0174532925199433]],
##          AXIS["longitude",east,
##              ORDER[2],
##              ANGLEUNIT["degree",0.0174532925199433]],
##          ID["EPSG",4326]]],
## ABRIDGEDTRANSFORMATION["Transformation from ETRS89 to WGS84",
##     METHOD["Position Vector transformation (geog2D domain)",
##         ID["EPSG",9606]],
##     PARAMETER["X-axis translation",0,
##         ID["EPSG",8605]],
##     PARAMETER["Y-axis translation",0,
##         ID["EPSG",8606]],
##     PARAMETER["Z-axis translation",0,
##         ID["EPSG",8607]],
##     PARAMETER["X-axis rotation",0,
##         ID["EPSG",8608]],
##     PARAMETER["Y-axis rotation",0,
##         ID["EPSG",8609]],
##     PARAMETER["Z-axis rotation",0,
```

## Coordinate reference system: legacy EPSG:2180 iv

```
##          ID["EPSG",8610]],  
##    PARAMETER["Scale difference",1,  
##          ID["EPSG",8611]]]]
```

## Coordinate reference system: current EPSG:2180 i

```
sf::st_crs("EPSG:2180")

## Coordinate Reference System:
##   User input: EPSG:2180
##   wkt:
## PROJCRS["ETRF2000-PL / CS92",
##     BASEGEOGCRS["ETRF2000-PL",
##       DATUM["ETRF2000 Poland",
##         ELLIPSOID["GRS 1980",6378137,298.257222101,
##           LENGTHUNIT["metre",1]]],
##       PRIMEM["Greenwich",0,
##         ANGLEUNIT["degree",0.0174532925199433]],
##       ID["EPSG",9702]],
##     CONVERSION["Poland CS92",
##       METHOD["Transverse Mercator",
##         ID["EPSG",9807]],
##       PARAMETER["Latitude of natural origin",0,
##         ANGLEUNIT["degree",0.0174532925199433],
##         ID["EPSG",8801]],
##       PARAMETER["Longitude of natural origin",19,
##         ANGLEUNIT["degree",0.0174532925199433],
##         ID["EPSG",8802]],
##       PARAMETER["Scale factor at natural origin",0.9993,
```

## Coordinate reference system: current EPSG:2180 ii

```
##          SCALEUNIT["unity",1],
##          ID["EPSG",8805]],
##    PARAMETER["False easting",500000,
##          LENGTHUNIT["metre",1],
##          ID["EPSG",8806]],
##    PARAMETER["False northing",-5300000,
##          LENGTHUNIT["metre",1],
##          ID["EPSG",8807]]],
##    CS[Cartesian,2],
##      AXIS["northing (x)",north,
##        ORDER[1],
##        LENGTHUNIT["metre",1]],
##      AXIS["easting (y)",east,
##        ORDER[2],
##        LENGTHUNIT["metre",1]],
##    USAGE[
##      SCOPE["Topographic mapping (medium and small scale)."],
##      AREA["Poland - onshore and offshore."],
##      BBOX[49,14.14,55.93,24.15]],
##    ID["EPSG",2180]]
```

## Main updating points i

- Obviously `rgdal::readOGR()` has to be replaced by `as(sf::st_read(), "Spatial")` for reading spatial vector files.
- ASSE scripts make extensive use of `sp::over()`, which in some input combinations used `rgeos`; in those cases, `sf` has to be used instead.
- `maptools::unionSpatialPolygons` using `rgeos` can sometimes be replaced by the `sf::aggregate` method for `sf` objects, sometimes by `sf::st_union`.
- `rgeos` binary predicates can be replaced by equivalent `sf` predicates, note that returned objects from `sf` by default are sparse not dense logical matrices.
- `maptools::pointLabel` is now `car::pointLabel`.



- `rgeos::gDelaunayTriangulation` can be replaced by `deldir::deldir`.
- `rgeos::gArea` can be replaced by `sf::st_area`, but the area units will be given correctly by `sf` rather than wrongly for spherical coordinates by `rgeos`.
- Coercion to classes defined in `spatstat` was in `maptools` but is now in `sf`; tessellations could be coerced by stepping through lists of tiles.
- Upgrading spatial vector files from `ESRI Shapefile` to `GPKG` (GeoPackage) would permit proper storage of `UTF-8` characters and `WKT2-2019` coordinate reference system declarations.
- The `jpt_powier` field of `powiaty.dbf` appears to be corrupted in the upstream data source.

- `sf::st_read` does not use the **FID** component of vector layers as a **row.name**.
- **sp** is no longer attached by **spdep**, so may need to be attached explicitly.

## Further steps

- It should be obvious (and expected) that there were no impacts on **spdep** for creating spatial weights or carrying out tests for spatial autocorrelation, or on **spatialreg**.
- Indeed, packages for spatial econometrics generally have been pro-actively adapting to the archiving of the retiring packages.
- Chapters 14-17 of Pebesma and Bivand (2023b) were written without the retiring packages, and adaptations of code for creating spatial weights in **spdep** have tracked **s2** and **sf** closely.
- In some cases, **spdep** converts input **sp** objects to **sf** to benefit from its more efficient approaches.
- The forthcoming second edition of ASSE, updating the text and converting the **sp** workflows to **sf**, is in progress.

- The mitigations applied here use **sf**, but **terra** could have been employed as it also links to **GDAL**, **GEOS** and **PROJ**, and remains closer to the **sp** legacy GIS position of pretending that most coordinates are planar for topological predicates and operations.
- Data should no longer be shared in ESRI Shapefile format, but the GeoPackage format should be used; recent and impending changes in GDAL drivers will make GPKG even more efficient (column-based access more generally in vector drivers, SOzip).
- Increasingly, data are accessed through APIs (ASSE chapter 3), but both the data and the API definitions are seldom stable; computing in the cloud is now realistic for earth observation data.

- Workflow impacts on spatial econometrics from the archiving of retiring R-spatial packages are not difficult to mitigate, but older workflows, courses, tutorials, etc., would benefit from active maintenance.
- Both R itself and key programming infrastructure components are evolving, native pipes came in R 4.1.0.
- S7 is a forward-looking proof-of-concept class/object system hoping to combine S3 (as used by `sf`) and S4 (as used by `sp`), see <https://cran.r-project.org/package=S7>.
- Changes in class representations will also affect how we organise model output, like methods such as `impacts`, `summary`, `predict`, etc.

# sessionInfo i

```
sessionInfo()

## R version 4.3.2 (2023-10-31)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: Fedora Linux 39 (Workstation Edition)
##
## Matrix products: default
## BLAS:   /home/rsb/topics/R/R432-share/lib64/R/lib/libRblas.so
## LAPACK: /home/rsb/topics/R/R432-share/lib64/R/lib/libRlapack.so; LAPACK version 3.11.0
##
## locale:
##  [1] LC_CTYPE=en_GB.UTF-8      LC_NUMERIC=C              LC_TIME=en_GB.UTF-8
##  [4] LC_COLLATE=en_GB.UTF-8   LC_MONETARY=en_GB.UTF-8  LC_MESSAGES=en_GB.UTF-8
##  [7] LC_PAPER=en_GB.UTF-8     LC_NAME=C                LC_ADDRESS=C
## [10] LC_TELEPHONE=C          LC_MEASUREMENT=en_GB.UTF-8 LC_IDENTIFICATION=C
##
## time zone: America/Los_Angeles
## tzcode source: system (glibc)
##
## attached base packages:
## [1] stats      graphics  grDevices  utils      datasets  methods   base
##
## loaded via a namespace (and not attached):
```

```
## [1] vctrs_0.6.4      cli_3.6.1      knitr_1.45     rlang_1.1.2
## [5] xfun_0.41        DBI_1.1.3      KernSmooth_2.23-22 generics_0.1.3
## [9] sf_1.0-15        glue_1.6.2     htmltools_0.5.7 e1071_1.7-13
## [13] fansi_1.0.5      rmarkdown_2.25 grid_4.3.2     tibble_3.2.1
## [17] evaluate_0.23    classInt_0.4-10 fastmap_1.1.1  yaml_2.3.7
## [21] lifecycle_1.0.4  compiler_4.3.2 dplyr_1.1.3    pkgconfig_2.0.3
## [25] Rcpp_1.0.11      rstudioapi_0.15.0 digest_0.6.33  R6_2.5.1
## [29] tidyselect_1.2.0 utf8_1.2.4     class_7.3-22  pillar_1.9.0
## [33] magrittr_2.0.3   tools_4.3.2   proxy_0.4-27  units_0.8-4
```

## Aftermatter

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