

**Information Security, Fall 2016****Homework #2: Part 1 Symmetric Ciphers, Part 2 Asymmetric Ciphers**

Graded out of 10 points. Due: 11/3 (Thursday)(End of the class)

**1.** How many bytes in **State** are affected by ShiftRows?**2.** Given the plaintext {000102030405060708090A0B0C0D0E0F} and the key {01010101010101010101010101010101}:a. Show the original contents of **State**, displayed as a 4 \* 4 matrix.b. Show the value of **State** after initial AddRoundKey.c. Show the value of **State** after SubBytes.d. Show the value of **State** after ShiftRows.e. Show the value of **State** after MixColumns. [Just report the diagonal elements here, i.e.  $S_{0,0}$ ,  $S_{1,1}$ ,  $S_{2,2}$ ,  $S_{3,3}$ ]**3.** What is a meet-in-the-middle attack?**4.** If a bit error occurs in the transmission of a ciphertext character in 8-bit CFB mode, how far does the error propagate?**5.** What is the difference between a one-time pad and a stream cipher?**6.** Alice and Bob agree to communicate privately via email using a scheme based on RC4, but they want to avoid using a new secret key for each transmission. Alice and Bob privately agree on a 128-bit key  $k$ . To encrypt a message  $m$ , consisting of a string of bits, the following procedure is used.1. Choose a random 80-bit value  $v$ 2. Generate the ciphertext  $c = RC4(v || k) \oplus m$ 3. Send the bit string  $(v || c)$ Suppose Alice uses this procedure to send a message  $m$  to Bob. Describe how Bob can recover the message  $m$  from  $(v || c)$  using  $k$ .**7.** What is a prime number?**8.** Use **Fermat's theorem** to find a number  $x$  between 0 and 28 with  $x^{85}$  congruent to 6 modulo 29. (You should not need to use any brute-force searching. Must answer with Fermat's theorem)**9.** What requirements must a public-key cryptosystems fulfill to be a secure algorithm?**10.** In a public-key cryptosystem using RSA, given the ciphertext  $C = 61$  and the public key  $e = 11$ ,  $n = 91$ , find the plaintext  $M$ .