## 1 Numerical Result

Table 1: Variable Selection and outliers detection Results for Example 1 ( $\beta=(3,2,1.5,0,0,0,0,0)'$  with 10% outliers )

| Variable Selection Outliers detection |         |      |         |      |      |                  |      |       |         |        |
|---------------------------------------|---------|------|---------|------|------|------------------|------|-------|---------|--------|
| Case                                  | Method  |      |         | AN   |      |                  |      |       |         |        |
| Case                                  | ALasso  | 72   | 25      | 99   | 7    | $\frac{1}{3.27}$ |      | -     | JD<br>- | 0.89   |
| A                                     | MMNNG   | 74.5 | 20.4    | 98.3 | 6.3  | 3.23             | _    | _     | _       | NA     |
|                                       | SROS    | 21   | 76      | 99   | 27.6 | 4.31             | _    | _     | _       | 56.67  |
|                                       | SROS-2  | 50   | 50      | 100  | 17.9 | 3.91             | 0    | 6.46  | 100     | 7.89   |
|                                       | ASROS-2 | 86   | 9       | 98.3 | 2.2  | 3.04             | 0    | 3.24  | 100     | 11.88  |
|                                       | SLTS    | 15   | 83      | 99.3 | 42.3 | 5.89             | 0    | 11.4  | 100     | 200.07 |
|                                       | PAWLS   | 30   | 68      | 99.3 | 23.1 | 4.07             | 0    | 9.1   | 100     | 6.6    |
|                                       | APAWLS  | 71   | 18      | 96   | 5.6  | 3.1              | 0    | 6.5   | 100     | 12.04  |
|                                       |         |      |         |      |      |                  |      |       |         |        |
|                                       | ALasso  | 70   | 15      | 94   | 5.9  | 3.07             | -    | -     | -       | 0.92   |
|                                       | MMNNG   | 86   | 14      | 100  | 3.9  | 3.17             | -    | -     | -       | 354.78 |
|                                       | SROS    | 31   | 69      | 100  | 24.6 | 4.24             | -    | -     | -       | 51.79  |
| В                                     | SROS-2  | 34   | 66      | 100  | 24.1 | 4.25             | 0    | 25.02 | 100     | 6.91   |
| _                                     | ASROS-2 | 95   | 5       | 100  | 1.3  | 3.05             | 0    | 9.48  | 100     | 10.29  |
|                                       | SLTS    | 13   | 87      | 100  | 43.8 | 5.97             | 0    | 13.62 | 100     | 216.52 |
|                                       | PAWLS   | 54   | 46<br>3 | 100  | 13.6 | 3.6              | 0    | 10.78 | 100     | 6.14   |
|                                       | APAWLS  | 97   | 3       | 100  | 0.7  | 3.03             | 0    | 8     | 100     | 11.73  |
|                                       | ALasso  | 0    | 2       | 44   | 10.3 | 1.61             | -    | -     | -       | 0.98   |
|                                       | MMNNG   | 74.7 | 12.1    | 95.6 | 3.3  | 3.01             | -    | -     | -       | NA     |
|                                       | SROS    | 41   | 50      | 97   | 17.5 | 3.7              | -    | -     | -       | 50.24  |
| $\mathbf{C}$                          | SROS-2  | 22   | 78      | 100  | 30.9 | 4.73             | 0    | 24.36 | 100     | 6.66   |
| C                                     | ASROS-2 | 76   | 16      | 97.3 | 4.6  | 3.11             | 0    | 0.11  | 100     | 11.69  |
|                                       | SLTS    | 23   | 76      | 99.7 | 36.9 | 5.42             | 0    | 4.87  | 100     | 313.05 |
|                                       | PAWLS   | 35   | 62      | 99   | 20   | 3.9              | 0    | 3.93  | 100     | 6.78   |
|                                       | APAWLS  | 79   | 15      | 98   | 4.4  | 3.12             | 0.2  | 1.8   | 99      | 12.61  |
|                                       | ALasso  | 0    | 14      | 61   | 51.7 | 4.02             | _    | _     | _       | 1.21   |
|                                       | MMNNG   | 71.7 | 11.1    | 93.9 | 4.1  | 2.97             | _    | _     | _       | NA     |
|                                       | SROS    | 8    | 80      | 96   | 37.1 | 4.76             | -    | -     | -       | 50.31  |
| D                                     | SROS-2  | 0    | 34      | 73.7 | 55.4 | 5.27             | 89.8 | 9.31  | 0       | 25.16  |
| D                                     | ASROS-2 | 0    | 14      | 60   | 51.7 | 3.91             | 92.8 | 5.89  | 0       | 25.1   |
|                                       | SLTS    | 10   | 89      | 99.7 | 43.1 | 5.77             | 0    | 5.62  | 100     | 309.51 |
|                                       | PAWLS   | 46   | 53      | 99.7 | 17.7 | 3.83             | 2    | 1.07  | 98      | 8.91   |
|                                       | APAWLS  | 76   | 18      | 98   | 5.7  | 3.18             | 2    | 0.44  | 98      | 15     |
| E                                     | ALasso  | 0    | 3       | 23   | 81.9 | 2.72             | _    | _     | _       | 1.42   |
|                                       | MMNNG   | 79   | 11      | 96.7 | 3.4  | 3.03             | _    | _     | _       | 342.83 |
|                                       | SROS    | 26   | 61      | 95.7 | 30.2 | 4.45             | _    | _     | _       | 50.08  |
|                                       | SROS-2  | 0    | 6       | 32.7 | 75.3 | 3.89             | 87   | 5.56  | 5       | 16.76  |
|                                       | ASROS-2 | 0    | 0       | 13.7 | 84.2 | 2.16             | 91.8 | 2.64  | 3       | 14.29  |
|                                       | SLTS    | 16   | 82      | 99.3 | 38.4 | 5.39             | 0    | 4     | 100     | 385.66 |
|                                       | PAWLS   | 44   | 55      | 99.7 | 17.9 | 3.82             | 0    | 1.42  | 100     | 8.05   |
|                                       | APAWLS  | 77   | 12      | 96.3 | 4    | 3.05             | 2.2  | 0.56  | 94      | 14.1   |

Table 2: Variable Selection and outliers detection Results for Example 2 ( $\beta=({\bf 2}'_{10},{\bf 0}'_{p-10})'$  with 10% outliers )

| ~            | 3.5 .1 .1 | CED | Variable Selection |      |      |       |           | Outliers detection   |          |                      |  |  |
|--------------|-----------|-----|--------------------|------|------|-------|-----------|----------------------|----------|----------------------|--|--|
| Case         | Method    | CFR | OFR                | PDR  | FDR  | AN    | M         | S                    | JD       | TIME                 |  |  |
| A            | ALasso    | 97  | 0                  | 99.6 | 0    | 9.96  | -         | _                    | <u>-</u> | 3.21                 |  |  |
|              | SROS-2    | 2   | 98                 | 100  | 54.7 | 41.53 | 0         | 4.45                 | 100      | 603.94               |  |  |
|              | ASROS-2   | 85  | 15                 | 100  | 2    | 10.25 | 0         | 0.42                 | 100      | 723.54               |  |  |
|              | SLTS      | 0   | 87                 | 98.5 | 84   | 61.9  | 0         | 24.91                | 100      | $1.89 \times 10^{4}$ |  |  |
|              | PAWLS     | 4   | 96                 | 100  | 32.5 | 16.13 | 0         | 0.9                  | 100      | 439.93               |  |  |
|              | APAWLS    | 90  | 10                 | 100  | 1.1  | 10.13 | 0         | 0.35                 | 100      | 924.47               |  |  |
|              | ALasso    | 77  | 1                  | 94.3 | 0.5  | 9.47  |           |                      |          | 3.23                 |  |  |
|              | SROS-2    | 3   | 97                 | 100  | 52.6 | 32.94 | 0         | 11.72                | 100      | 632.84               |  |  |
|              | ASROS-2   | 98  | 2                  | 100  | 0.2  | 10.02 | 0         | 4.06                 | 100      | 572.65               |  |  |
|              | SLTS      | 98  | 93                 | 98.7 | 82.7 | 57.6  | 0         | $\frac{4.06}{24.76}$ | 100      | $1.94 \times 10^4$   |  |  |
| $\mathbf{B}$ | PAWLS     | 4   |                    |      |      |       |           |                      |          |                      |  |  |
|              |           | _   | 96                 | 100  | 34.9 | 16.67 | 0         | 2.84                 | 100      | 454.22               |  |  |
|              | APAWLS    | 98  | 2                  | 100  | 0.2  | 10.02 | 0         | 2.31                 | 100      | 936.15               |  |  |
|              | ALasso    | 0   | 0                  | 56.1 | 13.6 | 7.56  | _         | _                    | _        | 3.92                 |  |  |
|              | SROS-2    | 1   | 66                 | 94.4 | 75   | 56.81 | 21.9      | 10.19                | 68       | 1214.61              |  |  |
|              | ASROS-2   | 56  | 38                 | 99.3 | 6.7  | 10.79 | 0         | 0.16                 | 100      | 650.33               |  |  |
| ~            | SLTS      | 0   | 96                 | 99.6 | 84   | 62.36 | 0         | 16.47                | 100      | $2.24 \times 10^{4}$ |  |  |
| $\mathbf{C}$ | PAWLS     | 4   | 96                 | 100  | 38.8 | 17.88 | 0         | 0.98                 | 100      | 729.23               |  |  |
|              | APAWLS    | 86  | 14                 | 100  | 1.3  | 10.15 | 0         | 0.19                 | 100      | 1227.51              |  |  |
|              |           |     |                    |      |      |       |           |                      |          |                      |  |  |
|              | ALasso    | 0   | 1                  | 64.7 | 60.3 | 16.75 | -         | -                    | -        | 11.29                |  |  |
|              | SROS-2    | 0   | 96                 | 99.6 | 87.9 | 83.53 | 95.3      | 4.91                 | 0        | 6152.51              |  |  |
|              | ASROS-2   | 0   | 19                 | 81.5 | 70.2 | 27.85 | 96.4      | 4.37                 | 0        | 4328.89              |  |  |
| D            | SLTS      | 0   | 98                 | 99.8 | 84.6 | 64.98 | 0         | 16.57                | 100      | $2.72 \times 10^{4}$ |  |  |
| D            | PAWLS     | 8   | 88                 | 99.3 | 37.7 | 17.83 | 5.1       | 0.01                 | 94       | 1421.83              |  |  |
|              | APAWLS    | 88  | 6                  | 98.5 | 2.5  | 10.16 | 5.8       | 0                    | 94       | 2138.42              |  |  |
|              | A I одда  | 0   | 0                  | 31.8 | 70.8 | 10    |           |                      |          | 6.78                 |  |  |
|              | ALasso    | -   |                    |      |      |       | -<br>07 7 | 150                  | -        |                      |  |  |
|              | SROS-2    | 0   | 55                 | 92.2 | 84.6 | 61.26 | 85.5      | 15.8                 | 0        | 4786.5               |  |  |
|              | ASROS-2   | 0   | 0                  | 49.1 | 75   | 17.57 | 98.9      | 0.91                 | 0        | 2236.44              |  |  |
| ${f E}$      | SLTS      | 0   | 96                 | 99.6 | 84.6 | 65.06 | 0         | 16.61                | 100      | $2.74 \times 10^4$   |  |  |
|              | PAWLS     | 4   | 96                 | 100  | 33.8 | 16.61 | 0.3       | 0.27                 | 99       | 1173.68              |  |  |
|              | APAWLS    | 88  | 9                  | 99.7 | 1.4  | 10.15 | 1.1       | 0.01                 | 93       | 1790.1               |  |  |