

1 Numerical Result

Table 1: Test for variable selection

| Method | CFR (%) | CFR2 (%) | OFR (%) | AN | CFR (%) | CFR2 (%) | OFR (%) | AN |
|---------------|---------|----------|---------|------|---------------|----------|---------|------|
| Case A | | | | | Case B | | | |
| PAWLS-AIC | 0 | 0 | 80 | 87.6 | 0 | 0 | 100 | 97.2 |
| PAWLS-BIC | 60 | 100 | 40 | 10.4 | 100 | 100 | 0 | 10 |
| APAWLS-AIC | 80 | 100 | 20 | 10.2 | 80 | 80 | 0 | 8.2 |
| APAWLS-BIC | 80 | 100 | 20 | 10.2 | 80 | 80 | 0 | 8.2 |
| Case C | | | | | Case D | | | |
| PAWLS-AIC | 0 | 0 | 60 | 79 | 0 | 0 | 80 | 86 |
| PAWLS-BIC | 80 | 80 | 0 | 10 | 60 | 60 | 20 | 10.6 |
| APAWLS-AIC | 100 | 100 | 0 | 10 | 100 | 100 | 0 | 10 |
| APAWLS-BIC | 100 | 100 | 0 | 10 | 100 | 100 | 0 | 10 |
| Case E | | | | | | | | |
| PAWLS-AIC | 0 | 0 | 40 | 76.4 | | | | |
| PAWLS-BIC | 20 | 40 | 20 | 13.8 | | | | |
| APAWLS-AIC | 20 | 20 | 0 | 7.4 | | | | |
| APAWLS-BIC | 20 | 20 | 0 | 8 | | | | |

Table 2: Test for outlier detection

| | | AIC | | | BIC | | |
|---------------|--------|-------|-------|-------|-------|-------|-------|
| | Model | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| PAWLS | Case A | 0 | 0.1 | 1 | 0 | 0 | 1 |
| | Case B | 0 | 0 | 1 | 0 | 0.01 | 1 |
| | Case C | 0.08 | 0.1 | 0.6 | 0 | 0 | 1 |
| | Case D | 0.1 | 0.03 | 0.4 | 0.16 | 0 | 0.8 |
| | Case E | 0.46 | 0.18 | 0 | 0.44 | 0.01 | 0 |
| APAWLS | Case A | 0 | 0 | 1 | 0 | 0 | 1 |
| | Case B | 0 | 0.15 | 1 | 0 | 0.15 | 1 |
| | Case C | 0 | 0.01 | 1 | 0 | 0 | 1 |
| | Case D | 0 | 0.01 | 1 | 0 | 0 | 1 |
| | Case E | 0.24 | 0.11 | 0 | 0.3 | 0.02 | 0 |

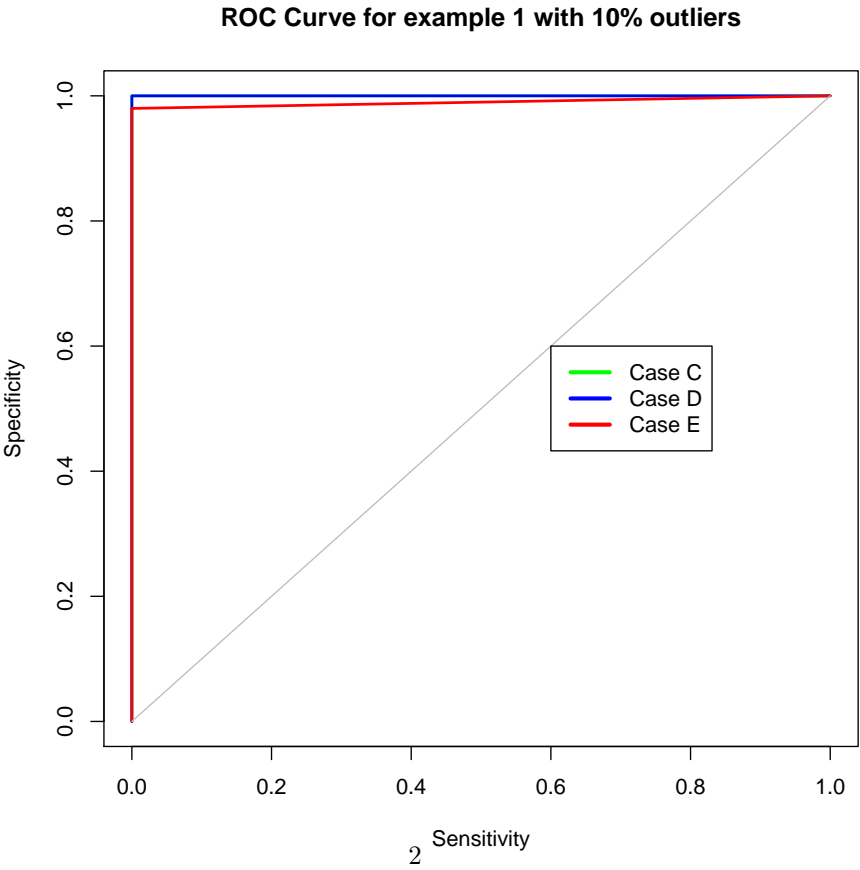


Table 3: Variable Selection Results for Example 1 ($\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$ with 10% outliers)

| Method | CFR (%) | OFR (%) | AN | TIME | CFR (%) | OFR (%) | AN | TIME |
|---------------|---------|---------|------|---------------|---------|---------|------|--------|
| Case A | | | | Case B | | | | |
| ALasso | 74 | 23 | 3.29 | 0.9 | 63 | 25 | 3.25 | 0.97 |
| sLTS | 10 | 89 | 4.89 | 4.3 | 24 | 76 | 4.21 | 4.1 |
| MMNNG | 68 | 25 | 3.25 | 691.33 | 88 | 12 | 3.13 | 682.07 |
| SROS | 19 | 78 | 4.34 | 49.36 | 30 | 70 | 4.12 | 53.2 |
| PAWLS | 100 | 0 | 3 | 1.66 | 100 | 0 | 3 | 1.48 |
| APAWLS | 40 | 0 | 2.3 | 3.12 | 40 | 0 | 2.3 | 3.04 |
| Case C | | | | Case D | | | | |
| ALasso | 3 | 2 | 1.94 | 0.85 | 0 | 19 | 2.52 | 1.19 |
| sLTS | 7 | 93 | 5.06 | 4.09 | 11 | 89 | 4.98 | 4.38 |
| MMNNG | 72 | 12 | 2.95 | 673.93 | 63 | 16 | 3.25 | 682.47 |
| SROS | 50 | 42 | 3.57 | 49.32 | 3 | 84 | 4.9 | 49.3 |
| PAWLS | 90 | 0 | 2.9 | 1.63 | 80 | 0 | 2.8 | 1.71 |
| APAWLS | 40 | 0 | 2.4 | 3.29 | 70 | 0 | 2.7 | 3.44 |
| Case E | | | | | | | | |
| ALasso | 0 | 17 | 4.05 | 0.98 | | | | |
| sLTS | 5 | 95 | 5.07 | 4.2 | | | | |
| MMNNG | 79 | 12 | 3.08 | 484.67 | | | | |
| PAWLS | 90 | 0 | 2.8 | 1.61 | | | | |
| APAWLS | 70 | 0 | 2.6 | 3.26 | | | | |

Table 4: Variable Selection Results for Example 1 ($\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$ with 20% outliers)

| Method | CFR (%) | OFR (%) | AN | TIME | CFR (%) | OFR (%) | AN | TIME |
|---------------|---------|---------|------|--------|---------------|---------|------|--------|
| Case C | | | | | Case D | | | |
| ALasso | 1 | 2 | 1.22 | 1.03 | 1 | 4 | 1.68 | 1.57 |
| sLTS | 1 | 99 | 5.49 | 4.31 | 4 | 95 | 5.35 | 4.3 |
| MMNNG | 65 | 5 | 2.76 | 470.24 | 31 | 33 | 3.96 | 473.42 |
| PAWLS | 43 | 56 | 3.9 | 0.68 | 66 | 32 | 4.13 | 1.25 |
| PAWLS | 73 | 7 | 2.67 | 2.78 | 88 | 1 | 2.87 | 3.67 |
| Case E | | | | | | | | |
| ALasso | 0 | 12 | 2.73 | 0.98 | | | | |
| sLTS | 5 | 94 | 5.2 | 4.27 | | | | |
| MMNNG | 56 | 6 | 2.72 | 457.01 | | | | |
| PAWLS | 44 | 39 | 3.54 | 1.24 | | | | |
| APAWLS | 49 | 3 | 2.2 | 2.5 | | | | |

Table 5: Variable Selection Results for Example 1 ($\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$ with 30% outliers)

| Method | CFR (%) | OFR (%) | AN | TIME | CFR (%) | OFR (%) | AN | TIME |
|---------------|---------|---------|------|--------|---------------|---------|------|--------|
| Case C | | | | | Case D | | | |
| ALasso | 2 | 0 | 0.68 | 1 | 0 | 3 | 0.96 | 1.75 |
| sLTS | 2 | 97 | 5.58 | 4.42 | 5 | 91 | 5.61 | 4.43 |
| MMNNG | 38 | 1 | 2.3 | 465.41 | 5 | 41 | 4.29 | 477.06 |
| PAWLS | 50 | 47 | 3.77 | 0.8 | 36 | 63 | 5.43 | 1.42 |
| APAWLS | 76 | 7 | 2.86 | 2.87 | 89 | 0 | 2.87 | 3.99 |
| Case E | | | | | | | | |
| ALasso | 1 | 8 | 2.25 | 0.97 | | | | |
| sLTS | 8 | 91 | 5.11 | 4.2 | | | | |
| MMNNG | 26 | 8 | 2.43 | 459.79 | | | | |
| PAWLS | 28 | 38 | 3.48 | 1.56 | | | | |
| PAWLS | 32 | 3 | 2.07 | 2.74 | | | | |

Table 6: Variable Selection Results for Example 2 ($\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$ with 10% outliers

| Method | CFR (%) | OFR (%) | AN | TIME | CFR (%) | OFR (%) | AN | TIME |
|---------------|---------|---------|-------|---------|---------------|---------|-------|---------|
| Case A | | | | | Case B | | | |
| ALasso | 97 | 0 | 9.96 | 3.4 | 84 | 1 | 9.75 | 3.41 |
| sLTS | 0 | 78 | 31.9 | 1702.93 | 1 | 86 | 24.93 | 1630.7 |
| PAWLS | 2 | 98 | 30.83 | 38.38 | 12 | 88 | 18.12 | 36.85 |
| APAWLS | 92 | 0 | 9.84 | 113.76 | 96 | 0 | 9.96 | 109.8 |
| Case C | | | | | Case D | | | |
| ALasso | 0 | 0 | 6.25 | 4.07 | 0 | 1 | 6.89 | 4.07 |
| sLTS | 0 | 91 | 32.11 | 1942.99 | 0 | 92 | 31.98 | 1870.57 |
| PAWLS | 6 | 86 | 19.79 | 76.68 | 9 | 77 | 30.06 | 78.49 |
| APAWLS | 90 | 0 | 9.9 | 119.84 | 90 | 0 | 9.9 | 123.03 |
| Case E | | | | | | | | |
| ALasso | 0 | 0 | 12.18 | 4.06 | | | | |
| sLTS | 0 | 92 | 30.96 | 1830.16 | | | | |
| PAWLS | 0 | 79 | 76.74 | 122.89 | | | | |
| APAWLS | 16 | 0 | 10.32 | 143.43 | | | | |

Table 7: Variable Selection Results for Example 2 ($\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$ with 20% outliers

| Method | CFR (%) | OFR (%) | AN | TIME | CFR (%) | OFR (%) | AN | TIME |
|---------------|---------|---------|-------|---------|---------------|---------|-------|---------|
| Case C | | | | | Case D | | | |
| ALasso | 0 | 0 | 5.7 | 6.45 | 0 | 0 | 6.15 | 6.89 |
| sLTS | 0 | 98 | 32.24 | 3138.03 | 0 | 98 | 32.21 | 2997.23 |
| PAWLS | 7 | 52 | 46.41 | 155.78 | 8 | 56 | 51.72 | 138.95 |
| APAWLS | 60 | 6 | 7.56 | 257.45 | 53 | 8 | 7.29 | 267.92 |
| Case E | | | | | | | | |
| ALasso | 0 | 0 | 17.41 | 6.3 | | | | |
| sLTS | 0 | 76 | 34 | 2852.83 | | | | |
| PAWLS | 0 | 39 | 87.43 | 132.7 | | | | |
| APAWLS | 3 | 4 | 5.57 | 287.92 | | | | |

Table 8: Variable Selection Results for Example 2 ($\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$ with 30% outliers

| Method | CFR (%) | OFR (%) | AN | TIME | CFR (%) | OFR (%) | AN | TIME |
|---------------|---------|---------|-------|---------------|---------|---------|-------|--------|
| Case C | | | | Case D | | | | |
| ALasso | 0 | 0 | 6.26 | 7.26 | 0 | 0 | 7.03 | 7.28 |
| sLTS | 0 | 2 | 56.47 | 3177.43 | 0 | 69 | 40.49 | 3135 |
| PAWLS | 0 | 8 | 89.68 | 210.68 | 0 | 29 | 80.26 | 196.42 |
| APAWLS | 23 | 3 | 5.28 | 290.77 | 21 | 14 | 6.65 | 301.11 |
| Case E | | | | | | | | |
| ALasso | 0 | 0 | 17.89 | 6.67 | | | | |
| sLTS | 0 | 17 | 42.75 | 2960.74 | | | | |
| PAWLS | 0 | 12 | 89.01 | 155.62 | | | | |
| APAWLS | 0 | 0 | 3.33 | 291.39 | | | | |

Table 9: Outlier Detection Evaluation in Example 1 and 2 with 10% outliers

| | Model | sLTS | | | PAWLS | | |
|------------------|--------|-------|-------|-------|-------|-------|-------|
| | | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| Example 1 | Case A | 0 | 0.05 | 1 | 0 | 0 | 1 |
| | Case B | 0 | 0.08 | 1 | 0 | 0.05 | 1 |
| | Case C | 0 | 0 | 1 | 0 | 0.01 | 1 |
| | Case D | 0 | 0 | 1 | 0 | 0.02 | 1 |
| | Case E | 0.03 | 0 | 0.87 | 0.02 | 0.01 | 0.9 |
| Example 2 | Case A | 0 | 0.21 | 1 | 0 | 0.01 | 1 |
| | Case B | 0 | 0.16 | 1 | 0 | 0.01 | 1 |
| | Case C | 0 | 0.13 | 0.99 | 0 | 0 | 1 |
| | Case D | 0 | 0.14 | 0.99 | 0 | 0 | 1 |
| | Case E | 0.08 | 0.12 | 0.42 | 0.54 | 0 | 0 |

Table 10: Outlier Detection Evaluation in Example 1 and 2 with 20% outliers

| | Model | sLTS | | | PAWLS | | |
|------------------|--------|-------|--------------------|-------|-------|----------------------|-------|
| | | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| Example 1 | Case C | 0 | 5×10^{-4} | 1 | 0 | 0.01 | 1 |
| | Case D | 0.02 | 0 | 0.95 | 0 | 7.5×10^{-4} | 0.99 |
| | Case E | 0.02 | 0 | 0.81 | 0.08 | 0.02 | 0.45 |
| Example 2 | Case C | 0 | 0.05 | 1 | 0.04 | 0.07 | 0.67 |
| | Case D | 0 | 0.05 | 0.99 | 0.07 | 0.08 | 0.57 |
| | Case E | 0.18 | 0.07 | 0 | 0.35 | 0.12 | 0 |

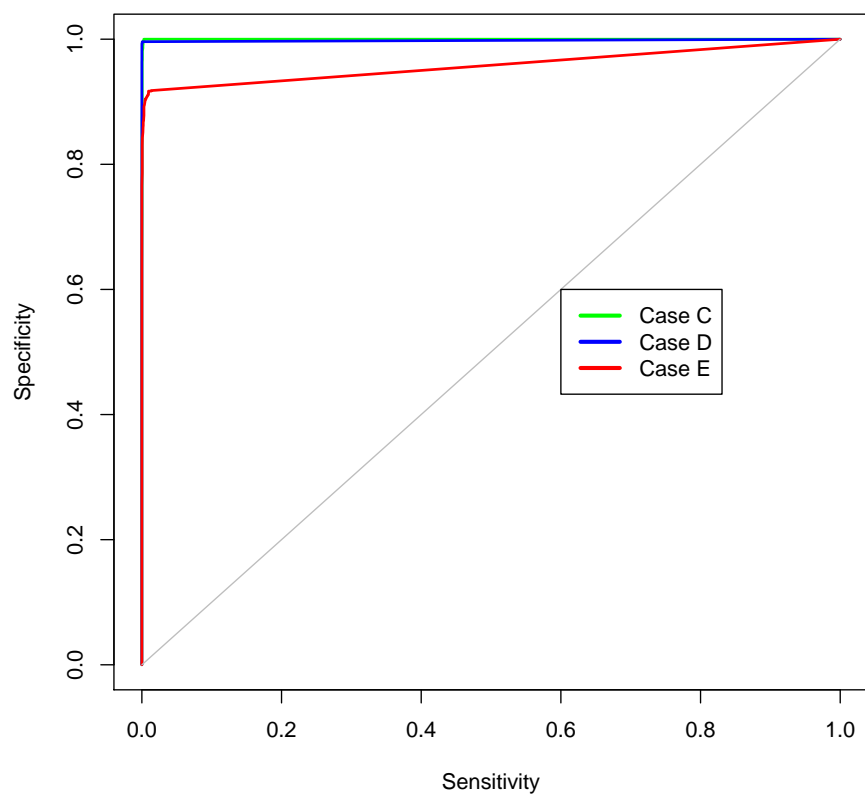
Table 11: Outlier Detection Evaluation in Example 1 and 2 with 30% outliers

| | Model | sLTS | | | PAWLS | | |
|------------------|--------|-------|-----------------------|-------|-----------------------|-----------------------|-------|
| | | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| Example 1 | Case C | 0 | 0 | 1 | 6.67×10^{-4} | 0 | 0.99 |
| | Case D | 0.07 | 0.01 | 0.81 | 0 | 5.71×10^{-4} | 1 |
| | Case E | 0.04 | 2.86×10^{-4} | 0.63 | 0.11 | 0.01 | 0.31 |
| Example 2 | Case C | 0.25 | 0.04 | 0 | 0.09 | 0.1 | 0.36 |
| | Case D | 0.32 | 0.06 | 0 | 0.15 | 0.08 | 0.33 |
| | Case E | 0.35 | 0.06 | 0 | 0.32 | 0.14 | 0 |

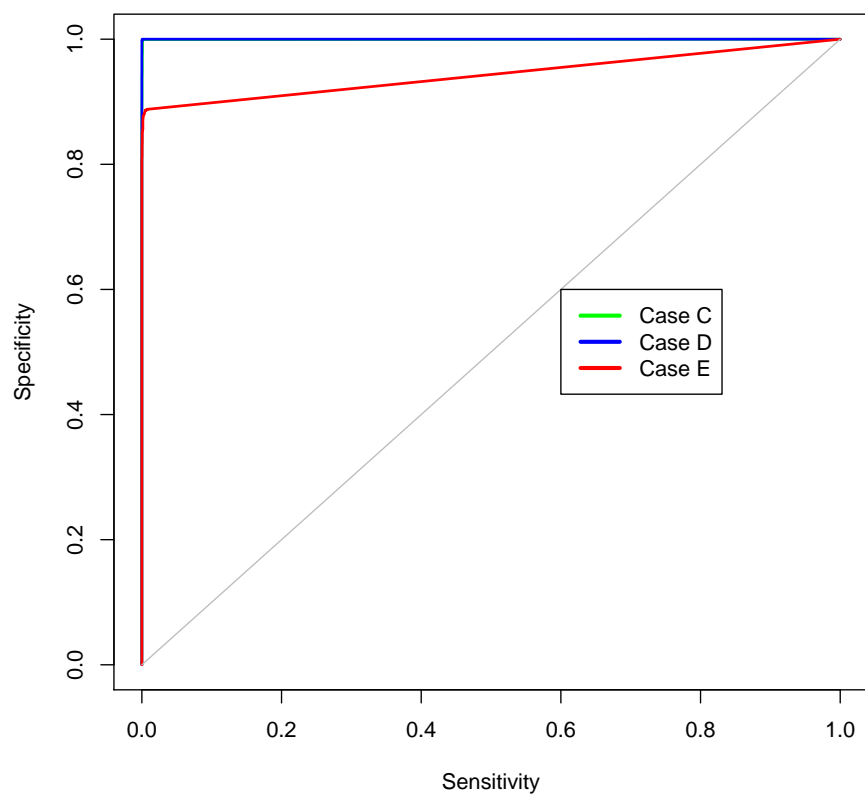
Table 12: Outlier Detection Evaluation in Example 1

| | Model | IPOD | | | PAWLS | | |
|------------------|--------|-------|-------|-------|-------|-------|-------|
| | | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| Example 1 | Case A | 0 | 0 | 1 | 0 | 0 | 1 |
| | Case B | 0 | 0.1 | 1 | 0 | 0.05 | 1 |
| | Case C | 0 | 0.08 | 1 | 0 | 0.01 | 1 |
| | Case D | 0.49 | 0.02 | 0.07 | 0 | 0.02 | 1 |
| | Case E | 0.22 | 0.05 | 0.31 | 0.02 | 0.01 | 0.9 |

ROC Curve for example 1 with 20% outliers



ROC Curve for example 1 with 30% outliers



ROC Curve for example 2 with 10% outliers

