

# 1 Numerical Result

Table 1: Variable Selection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 10% outliers )

| Method        | CFR (%) | OFR (%) | AN   | TIME          | CFR (%) | OFR (%) | AN   | TIME   |
|---------------|---------|---------|------|---------------|---------|---------|------|--------|
| <b>Case A</b> |         |         |      | <b>Case B</b> |         |         |      |        |
| ALasso        | 74      | 23      | 3.29 | 0.9           | 63      | 25      | 3.25 | 0.97   |
| sLTS          | 10      | 89      | 4.89 | 4.3           | 24      | 76      | 4.21 | 4.1    |
| MMNNG         | 68      | 25      | 3.25 | 691.33        | 88      | 12      | 3.13 | 682.07 |
| SROS          | 19      | 78      | 4.34 | 49.36         | 30      | 70      | 4.12 | 53.2   |
| PAWLS         | 39      | 60      | 3.96 | 0.82          | 44      | 56      | 3.95 | 0.78   |
| APAWLS        | 74      | 11      | 2.9  | 2.17          | 77      | 3       | 2.58 | 3.01   |
| <b>Case C</b> |         |         |      | <b>Case D</b> |         |         |      |        |
| ALasso        | 3       | 2       | 1.94 | 0.85          | 0       | 19      | 2.52 | 1.19   |
| sLTS          | 7       | 93      | 5.06 | 4.09          | 11      | 89      | 4.98 | 4.38   |
| MMNNG         | 72      | 12      | 2.95 | 673.93        | 63      | 16      | 3.25 | 682.47 |
| SROS          | 50      | 42      | 3.57 | 49.32         | 3       | 84      | 4.9  | 49.3   |
| PAWLS         | 52      | 48      | 3.83 | 0.68          | 87      | 12      | 3.35 | 1.07   |
| APAWLS        | 72      | 14      | 2.84 | 2.34          | 89      | 2       | 2.9  | 2.97   |
| <b>Case E</b> |         |         |      |               |         |         |      |        |
| ALasso        | 0       | 17      | 4.05 | 0.98          |         |         |      |        |
| sLTS          | 5       | 95      | 5.07 | 4.2           |         |         |      |        |
| MMNNG         | 79      | 12      | 3.08 | 484.67        |         |         |      |        |
| PAWLS         | 50      | 50      | 3.79 | 0.76          |         |         |      |        |
| APAWLS        | 63      | 7       | 2.45 | 2.23          |         |         |      |        |

Table 2: Variable Selection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 20% outliers )

| Method        | CFR (%) | OFR (%) | AN   | TIME   | CFR (%)       | OFR (%) | AN   | TIME   |
|---------------|---------|---------|------|--------|---------------|---------|------|--------|
| <b>Case C</b> |         |         |      |        | <b>Case D</b> |         |      |        |
| ALasso        | 1       | 2       | 1.22 | 1.03   | 1             | 4       | 1.68 | 1.57   |
| sLTS          | 1       | 99      | 5.49 | 4.31   | 4             | 95      | 5.35 | 4.3    |
| MMNNG         | 65      | 5       | 2.76 | 470.24 | 31            | 33      | 3.96 | 473.42 |
| PAWLS         | 43      | 56      | 3.9  | 0.68   | 66            | 32      | 4.13 | 1.25   |
| PAWLS         | 73      | 7       | 2.67 | 2.78   | 88            | 1       | 2.87 | 3.67   |
| <b>Case E</b> |         |         |      |        |               |         |      |        |
| ALasso        | 0       | 12      | 2.73 | 0.98   |               |         |      |        |
| sLTS          | 5       | 94      | 5.2  | 4.27   |               |         |      |        |
| MMNNG         | 56      | 6       | 2.72 | 457.01 |               |         |      |        |
| PAWLS         | 44      | 39      | 3.54 | 1.24   |               |         |      |        |
| APAWLS        | 49      | 3       | 2.2  | 2.5    |               |         |      |        |

Table 3: Variable Selection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 30% outliers )

| Method        | CFR (%) | OFR (%) | AN   | TIME   | CFR (%)       | OFR (%) | AN   | TIME   |
|---------------|---------|---------|------|--------|---------------|---------|------|--------|
| <b>Case C</b> |         |         |      |        | <b>Case D</b> |         |      |        |
| ALasso        | 2       | 0       | 0.68 | 1      | 0             | 3       | 0.96 | 1.75   |
| sLTS          | 2       | 97      | 5.58 | 4.42   | 5             | 91      | 5.61 | 4.43   |
| MMNNG         | 38      | 1       | 2.3  | 465.41 | 5             | 41      | 4.29 | 477.06 |
| PAWLS         | 50      | 47      | 3.77 | 0.8    | 36            | 63      | 5.43 | 1.42   |
| APAWLS        | 76      | 7       | 2.86 | 2.87   | 89            | 0       | 2.87 | 3.99   |
| <b>Case E</b> |         |         |      |        |               |         |      |        |
| ALasso        | 1       | 8       | 2.25 | 0.97   |               |         |      |        |
| sLTS          | 8       | 91      | 5.11 | 4.2    |               |         |      |        |
| MMNNG         | 26      | 8       | 2.43 | 459.79 |               |         |      |        |
| PAWLS         | 28      | 38      | 3.48 | 1.56   |               |         |      |        |
| PAWLS         | 32      | 3       | 2.07 | 2.74   |               |         |      |        |

Table 4: Variable Selection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 10% outliers

| Method        | CFR (%) | OFR (%) | AN    | TIME    | CFR (%)       | OFR (%) | AN    | TIME    |
|---------------|---------|---------|-------|---------|---------------|---------|-------|---------|
| <b>Case A</b> |         |         |       |         | <b>Case B</b> |         |       |         |
| ALasso        | 97      | 0       | 9.96  | 3.4     | 84            | 1       | 9.75  | 3.41    |
| sLTS          | 0       | 78      | 31.9  | 1702.93 | 1             | 86      | 24.93 | 1630.7  |
| PAWLS         | 2       | 98      | 30.83 | 38.38   | 12            | 88      | 18.12 | 36.85   |
| APAWLS        | 71      | 19      | 9.52  | 197.74  | 76            | 3       | 8.15  | 215.55  |
| <b>Case C</b> |         |         |       |         | <b>Case D</b> |         |       |         |
| ALasso        | 0       | 0       | 6.25  | 4.07    | 0             | 1       | 6.89  | 4.07    |
| sLTS          | 0       | 91      | 32.11 | 1942.99 | 0             | 92      | 31.98 | 1870.57 |
| PAWLS         | 6       | 86      | 19.79 | 76.68   | 9             | 77      | 30.06 | 78.49   |
| APAWLS        | 62      | 16      | 8.54  | 231.28  | 65            | 14      | 8.67  | 240.65  |
| <b>Case E</b> |         |         |       |         |               |         |       |         |
| ALasso        | 0       | 0       | 12.18 | 4.06    |               |         |       |         |
| sLTS          | 0       | 92      | 30.96 | 1830.16 |               |         |       |         |
| PAWLS         | 0       | 79      | 76.74 | 122.89  |               |         |       |         |
| APAWLS        | 23      | 13      | 6.47  | 249.22  |               |         |       |         |

Table 5: Variable Selection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 20% outliers

| Method        | CFR (%) | OFR (%) | AN    | TIME    | CFR (%)       | OFR (%) | AN    | TIME    |
|---------------|---------|---------|-------|---------|---------------|---------|-------|---------|
| <b>Case C</b> |         |         |       |         | <b>Case D</b> |         |       |         |
| ALasso        | 0       | 0       | 5.7   | 6.45    | 0             | 0       | 6.15  | 6.89    |
| sLTS          | 0       | 98      | 32.24 | 3138.03 | 0             | 98      | 32.21 | 2997.23 |
| PAWLS         | 7       | 52      | 46.41 | 155.78  | 8             | 56      | 51.72 | 138.95  |
| APAWLS        | 60      | 6       | 7.56  | 257.45  | 53            | 8       | 7.29  | 267.92  |
| <b>Case E</b> |         |         |       |         |               |         |       |         |
| ALasso        | 0       | 0       | 17.41 | 6.3     |               |         |       |         |
| sLTS          | 0       | 76      | 34    | 2852.83 |               |         |       |         |
| PAWLS         | 0       | 39      | 87.43 | 132.7   |               |         |       |         |
| APAWLS        | 3       | 4       | 5.57  | 287.92  |               |         |       |         |

Table 6: Variable Selection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 30% outliers

| Method        | CFR (%) | OFR (%) | AN    | TIME          | CFR (%) | OFR (%) | AN    | TIME   |
|---------------|---------|---------|-------|---------------|---------|---------|-------|--------|
| <b>Case C</b> |         |         |       | <b>Case D</b> |         |         |       |        |
| ALasso        | 0       | 0       | 6.26  | 7.26          | 0       | 0       | 7.03  | 7.28   |
| sLTS          | 0       | 2       | 56.47 | 3177.43       | 0       | 69      | 40.49 | 3135   |
| PAWLS         | 0       | 8       | 89.68 | 210.68        | 0       | 29      | 80.26 | 196.42 |
| APAWLS        | 23      | 3       | 5.28  | 290.77        | 21      | 14      | 6.65  | 301.11 |
| <b>Case E</b> |         |         |       |               |         |         |       |        |
| ALasso        | 0       | 0       | 17.89 | 6.67          |         |         |       |        |
| sLTS          | 0       | 17      | 42.75 | 2960.74       |         |         |       |        |
| PAWLS         | 0       | 12      | 89.01 | 155.62        |         |         |       |        |
| APAWLS        | 0       | 0       | 3.33  | 291.39        |         |         |       |        |

Table 7: Outlier Detection Evaluation in Example 1 and 2 with 10% outliers

|                  |        | sLTS  |       |       | PAWLS |       |       |
|------------------|--------|-------|-------|-------|-------|-------|-------|
|                  | Model  | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| <b>Example 1</b> | Case A | 0     | 0.05  | 1     | 0     | 0.06  | 1     |
|                  | Case B | 0     | 0.08  | 1     | 0     | 0.06  | 1     |
|                  | Case C | 0     | 0     | 1     | 0.01  | 0.01  | 0.99  |
|                  | Case D | 0     | 0     | 1     | 0.01  | 0     | 0.97  |
|                  | Case E | 0.03  | 0     | 0.87  | 0.05  | 0.01  | 0.79  |
| <b>Example 2</b> | Case A | 0     | 0.21  | 1     | 0     | 0.04  | 1     |
|                  | Case B | 0     | 0.16  | 1     | 0     | 0.09  | 1     |
|                  | Case C | 0     | 0.13  | 0.99  | 0.02  | 0.05  | 0.88  |
|                  | Case D | 0     | 0.14  | 0.99  | 0.02  | 0.05  | 0.88  |
|                  | Case E | 0.08  | 0.12  | 0.42  | 0.29  | 0.12  | 0.07  |

Table 8: Outlier Detection Evaluation in Example 1 and 2 with 20% outliers

|                  | Model  | sLTS  |                    |       | PAWLS |                      |       |
|------------------|--------|-------|--------------------|-------|-------|----------------------|-------|
|                  |        | M (%) | S (%)              | JD(%) | M (%) | S (%)                | JD(%) |
| <b>Example 1</b> | Case C | 0     | $5 \times 10^{-4}$ | 1     | 0     | 0.01                 | 1     |
|                  | Case D | 0.02  | 0                  | 0.95  | 0     | $7.5 \times 10^{-4}$ | 0.99  |
|                  | Case E | 0.02  | 0                  | 0.81  | 0.08  | 0.02                 | 0.45  |
| <b>Example 2</b> | Case C | 0     | 0.05               | 1     | 0.04  | 0.07                 | 0.67  |
|                  | Case D | 0     | 0.05               | 0.99  | 0.07  | 0.08                 | 0.57  |
|                  | Case E | 0.18  | 0.07               | 0     | 0.35  | 0.12                 | 0     |

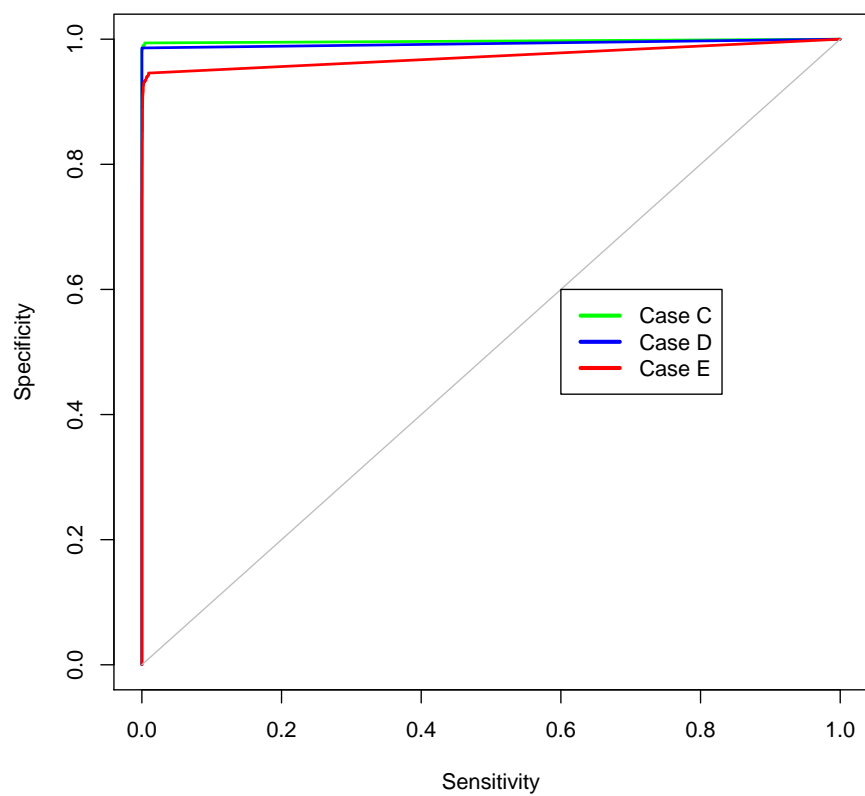
Table 9: Outlier Detection Evaluation in Example 1 and 2 with 30% outliers

|                  | Model  | sLTS  |                       |       | PAWLS                 |                       |       |
|------------------|--------|-------|-----------------------|-------|-----------------------|-----------------------|-------|
|                  |        | M (%) | S (%)                 | JD(%) | M (%)                 | S (%)                 | JD(%) |
| <b>Example 1</b> | Case C | 0     | 0                     | 1     | $6.67 \times 10^{-4}$ | 0                     | 0.99  |
|                  | Case D | 0.07  | 0.01                  | 0.81  | 0                     | $5.71 \times 10^{-4}$ | 1     |
|                  | Case E | 0.04  | $2.86 \times 10^{-4}$ | 0.63  | 0.11                  | 0.01                  | 0.31  |
| <b>Example 2</b> | Case C | 0.25  | 0.04                  | 0     | 0.09                  | 0.1                   | 0.36  |
|                  | Case D | 0.32  | 0.06                  | 0     | 0.15                  | 0.08                  | 0.33  |
|                  | Case E | 0.35  | 0.06                  | 0     | 0.32                  | 0.14                  | 0     |

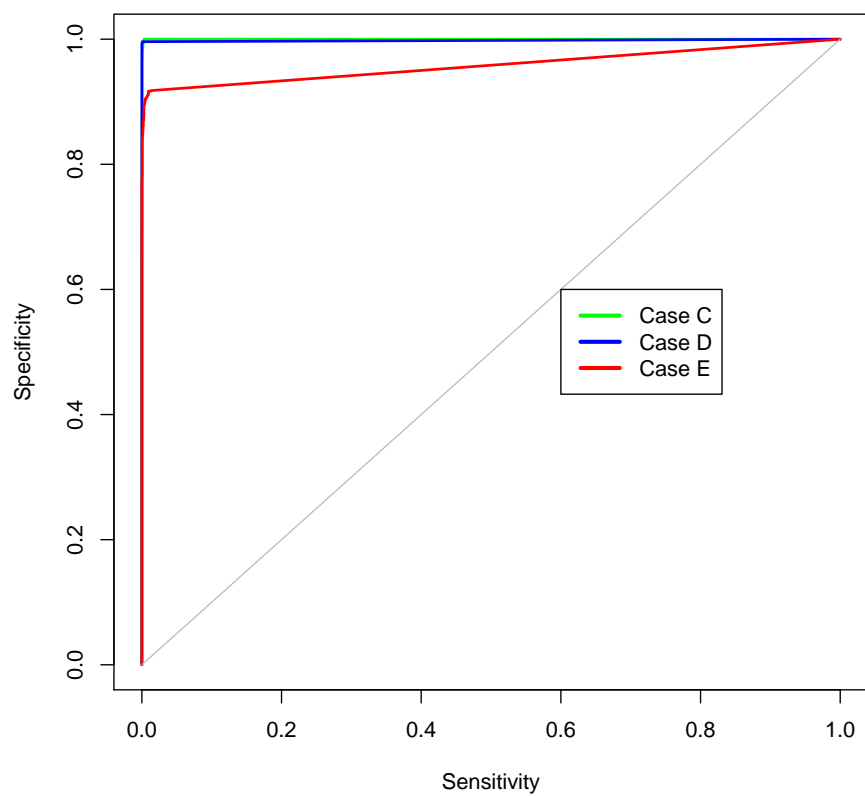
Table 10: Outlier Detection Evaluation in Example 1

|                  | Model  | IPOD  |       |       | PAWLS |       |       |
|------------------|--------|-------|-------|-------|-------|-------|-------|
|                  |        | M (%) | S (%) | JD(%) | M (%) | S (%) | JD(%) |
| <b>Example 1</b> | Case A | 0     | 0     | 1     | 0     | 0.06  | 1     |
|                  | Case B | 0     | 0.1   | 1     | 0     | 0.06  | 1     |
|                  | Case C | 0     | 0.08  | 1     | 0.01  | 0.01  | 0.99  |
|                  | Case D | 0.49  | 0.02  | 0.07  | 0.01  | 0     | 0.97  |
|                  | Case E | 0.22  | 0.05  | 0.31  | 0.05  | 0.01  | 0.79  |

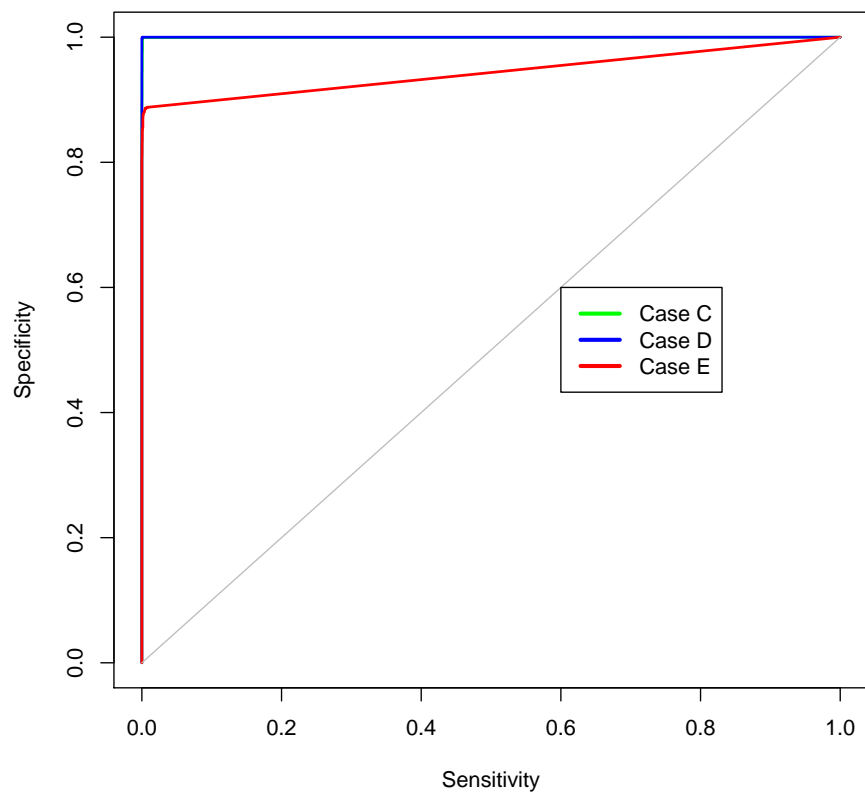
ROC Curve for example 1 with 10% outliers



ROC Curve for example 1 with 20% outliers



ROC Curve for example 1 with 30% outliers





ROC Curve for example 2 with 10% outliers

