

# 1 Numerical Result

Table 1: Test for variable selection

Method	CFR (%)	CFR2 (%)	OFR (%)	AN	CFR (%)	CFR2 (%)	OFR (%)	AN
<b>Case A</b>					<b>Case B</b>			
PAWLS-AIC	0	0	80	87.6	0	0	100	97.2
PAWLS-BIC	0	20	100	18.8	0	20	100	13.2
APAWLS-AIC	80	100	20	10.2	80	80	0	8.2
APAWLS-BIC	80	100	20	10.2	80	80	0	8.2
<b>Case C</b>					<b>Case D</b>			
PAWLS-AIC	0	0	60	79	0	0	80	86
PAWLS-BIC	0	20	100	17.4	0	20	100	17.6
APAWLS-AIC	100	100	0	10	100	100	0	10
APAWLS-BIC	100	100	0	10	100	100	0	10
<b>Case E</b>								
PAWLS-AIC	0	0	40	76.4				
PAWLS-BIC	0	20	40	23				
APAWLS-AIC	20	20	0	7.4				
APAWLS-BIC	20	20	0	8				

Table 2: Test for outlier detection

		AIC			BIC		
	Model	M (%)	S (%)	JD(%)	M (%)	S (%)	JD(%)
PAWLS	Case A	0	0.1	1	0	0.01	1
	Case B	0	0	1	0	0.03	1
	Case C	0.08	0.1	0.6	0	0.01	1
	Case D	0.1	0.03	0.4	0	0.01	1
	Case E	0.46	0.18	0	0.3	0.02	0
APAWLS	Case A	0	0	1	0	0	1
	Case B	0	0.15	1	0	0.15	1
	Case C	0	0.01	1	0	0	1
	Case D	0	0.01	1	0	0	1
	Case E	0.24	0.11	0	0.3	0.02	0

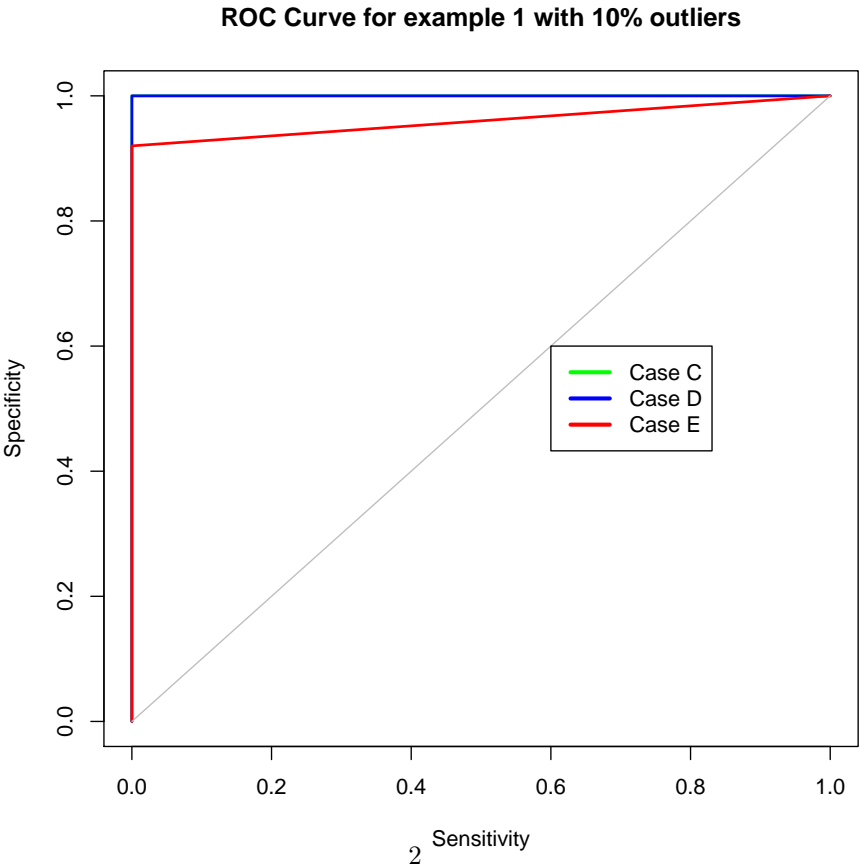


Table 3: Variable Selection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 10% outliers )

Method	CFR (%)	OFR (%)	AN	TIME	CFR (%)	OFR (%)	AN	TIME
<b>Case A</b>				<b>Case B</b>				
ALasso	74	23	3.29	0.9	63	25	3.25	0.97
sLTS	10	89	4.89	4.3	24	76	4.21	4.1
MMNNG	68	25	3.25	691.33	88	12	3.13	682.07
SROS	19	78	4.34	49.36	30	70	4.12	53.2
PAWLS	50	50	3.5	1.5	60	40	3.5	1.47
APAWLS	80	20	3.2	3.09	100	0	3	3.1
<b>Case C</b>				<b>Case D</b>				
ALasso	3	2	1.94	0.85	0	19	2.52	1.19
sLTS	7	93	5.06	4.09	11	89	4.98	4.38
MMNNG	72	12	2.95	673.93	63	16	3.25	682.47
SROS	50	42	3.57	49.32	3	84	4.9	49.3
PAWLS	50	50	3.8	1.59	90	0	2.9	1.74
APAWLS	80	10	3	3.35	90	0	2.9	3.35
<b>Case E</b>								
ALasso	0	17	4.05	0.98				
sLTS	5	95	5.07	4.2				
MMNNG	79	12	3.08	484.67				
PAWLS	60	40	3.4	1.59				
APAWLS	100	0	3	3.24				

Table 4: Variable Selection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 20% outliers )

Method	CFR (%)	OFR (%)	AN	TIME	CFR (%)	OFR (%)	AN	TIME
<b>Case C</b>					<b>Case D</b>			
ALasso	1	2	1.22	1.03	1	4	1.68	1.57
sLTS	1	99	5.49	4.31	4	95	5.35	4.3
MMNNG	65	5	2.76	470.24	31	33	3.96	473.42
PAWLS	43	56	3.9	0.68	66	32	4.13	1.25
PAWLS	73	7	2.67	2.78	88	1	2.87	3.67
<b>Case E</b>								
ALasso	0	12	2.73	0.98				
sLTS	5	94	5.2	4.27				
MMNNG	56	6	2.72	457.01				
PAWLS	44	39	3.54	1.24				
APAWLS	49	3	2.2	2.5				

Table 5: Variable Selection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 30% outliers )

Method	CFR (%)	OFR (%)	AN	TIME	CFR (%)	OFR (%)	AN	TIME
<b>Case C</b>					<b>Case D</b>			
ALasso	2	0	0.68	1	0	3	0.96	1.75
sLTS	2	97	5.58	4.42	5	91	5.61	4.43
MMNNG	38	1	2.3	465.41	5	41	4.29	477.06
PAWLS	50	47	3.77	0.8	36	63	5.43	1.42
APAWLS	76	7	2.86	2.87	89	0	2.87	3.99
<b>Case E</b>								
ALasso	1	8	2.25	0.97				
sLTS	8	91	5.11	4.2				
MMNNG	26	8	2.43	459.79				
PAWLS	28	38	3.48	1.56				
PAWLS	32	3	2.07	2.74				

Table 6: Variable Selection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 10% outliers

Method	CFR (%)	OFR (%)	AN	TIME	CFR (%)	OFR (%)	AN	TIME
<b>Case A</b>					<b>Case B</b>			
ALasso	97	0	9.96	3.4	84	1	9.75	3.41
sLTS	0	78	31.9	1702.93	1	86	24.93	1630.7
PAWLS	2	98	30.83	38.38	12	88	18.12	36.85
APAWLS	92	0	9.84	113.76	96	0	9.96	109.8
<b>Case C</b>					<b>Case D</b>			
ALasso	0	0	6.25	4.07	0	1	6.89	4.07
sLTS	0	91	32.11	1942.99	0	92	31.98	1870.57
PAWLS	6	86	19.79	76.68	9	77	30.06	78.49
APAWLS	90	0	9.9	119.84	90	0	9.9	123.03
<b>Case E</b>								
ALasso	0	0	12.18	4.06				
sLTS	0	92	30.96	1830.16				
PAWLS	0	79	76.74	122.89				
APAWLS	16	0	10.32	143.43				

Table 7: Variable Selection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 20% outliers

Method	CFR (%)	OFR (%)	AN	TIME	CFR (%)	OFR (%)	AN	TIME
<b>Case C</b>					<b>Case D</b>			
ALasso	0	0	5.7	6.45	0	0	6.15	6.89
sLTS	0	98	32.24	3138.03	0	98	32.21	2997.23
PAWLS	7	52	46.41	155.78	8	56	51.72	138.95
APAWLS	60	6	7.56	257.45	53	8	7.29	267.92
<b>Case E</b>								
ALasso	0	0	17.41	6.3				
sLTS	0	76	34	2852.83				
PAWLS	0	39	87.43	132.7				
APAWLS	3	4	5.57	287.92				

Table 8: Variable Selection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 30% outliers

Method	CFR (%)	OFR (%)	AN	TIME	CFR (%)	OFR (%)	AN	TIME
<b>Case C</b>					<b>Case D</b>			
ALasso	0	0	6.26	7.26	0	0	7.03	7.28
sLTS	0	2	56.47	3177.43	0	69	40.49	3135
PAWLS	0	8	89.68	210.68	0	29	80.26	196.42
APAWLS	23	3	5.28	290.77	21	14	6.65	301.11
<b>Case E</b>								
ALasso	0	0	17.89	6.67				
sLTS	0	17	42.75	2960.74				
PAWLS	0	12	89.01	155.62				
APAWLS	0	0	3.33	291.39				

Table 9: Outlier Detection Evaluation in Example 1 and 2 with 10% outliers

		sLTS			PAWLS		
	Model	M (%)	S (%)	JD(%)	M (%)	S (%)	JD(%)
<b>Example 1</b>	Case A	0	0.05	1	0	0.05	1
	Case B	0	0.08	1	0	0.06	1
	Case C	0	0	1	0	0	1
	Case D	0	0	1	0	0	1
	Case E	0.03	0	0.87	0.08	0	0.8
<b>Example 2</b>	Case A	0	0.21	1	0	0.01	1
	Case B	0	0.16	1	0	0.01	1
	Case C	0	0.13	0.99	0	0	1
	Case D	0	0.14	0.99	0	0	1
	Case E	0.08	0.12	0.42	0.54	0	0

Table 10: Outlier Detection Evaluation in Example 1 and 2 with 20% outliers

	Model	sLTS			PAWLS		
		M (%)	S (%)	JD(%)	M (%)	S (%)	JD(%)
<b>Example 1</b>	Case C	0	$5 \times 10^{-4}$	1	0	0.01	1
	Case D	0.02	0	0.95	0	$7.5 \times 10^{-4}$	0.99
	Case E	0.02	0	0.81	0.08	0.02	0.45
<b>Example 2</b>	Case C	0	0.05	1	0.04	0.07	0.67
	Case D	0	0.05	0.99	0.07	0.08	0.57
	Case E	0.18	0.07	0	0.35	0.12	0

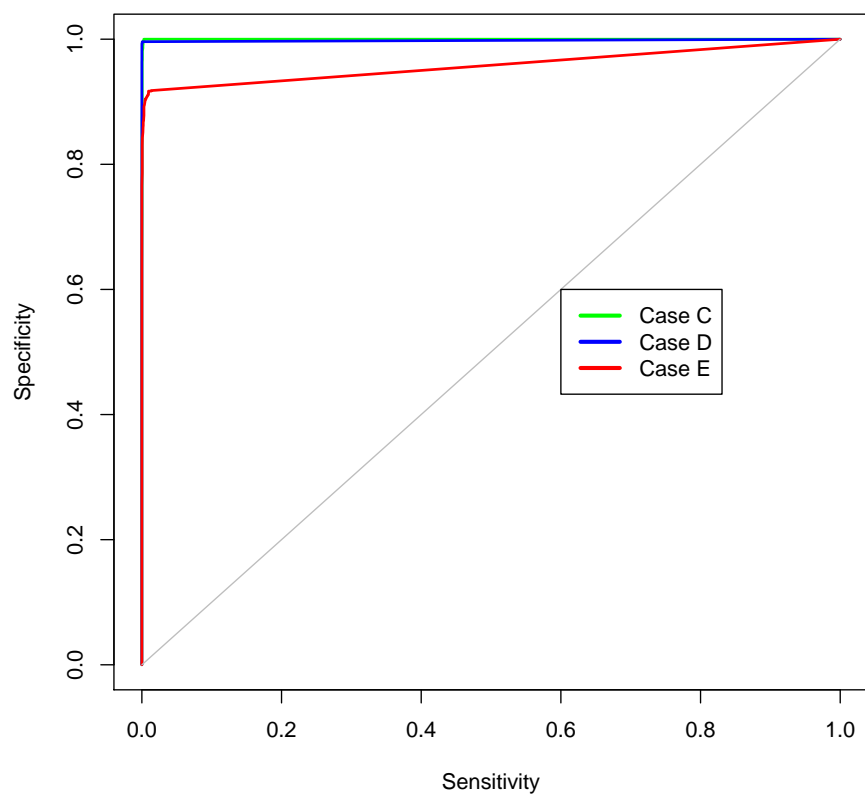
Table 11: Outlier Detection Evaluation in Example 1 and 2 with 30% outliers

	Model	sLTS			PAWLS		
		M (%)	S (%)	JD(%)	M (%)	S (%)	JD(%)
<b>Example 1</b>	Case C	0	0	1	$6.67 \times 10^{-4}$	0	0.99
	Case D	0.07	0.01	0.81	0	$5.71 \times 10^{-4}$	1
	Case E	0.04	$2.86 \times 10^{-4}$	0.63	0.11	0.01	0.31
<b>Example 2</b>	Case C	0.25	0.04	0	0.09	0.1	0.36
	Case D	0.32	0.06	0	0.15	0.08	0.33
	Case E	0.35	0.06	0	0.32	0.14	0

Table 12: Outlier Detection Evaluation in Example 1

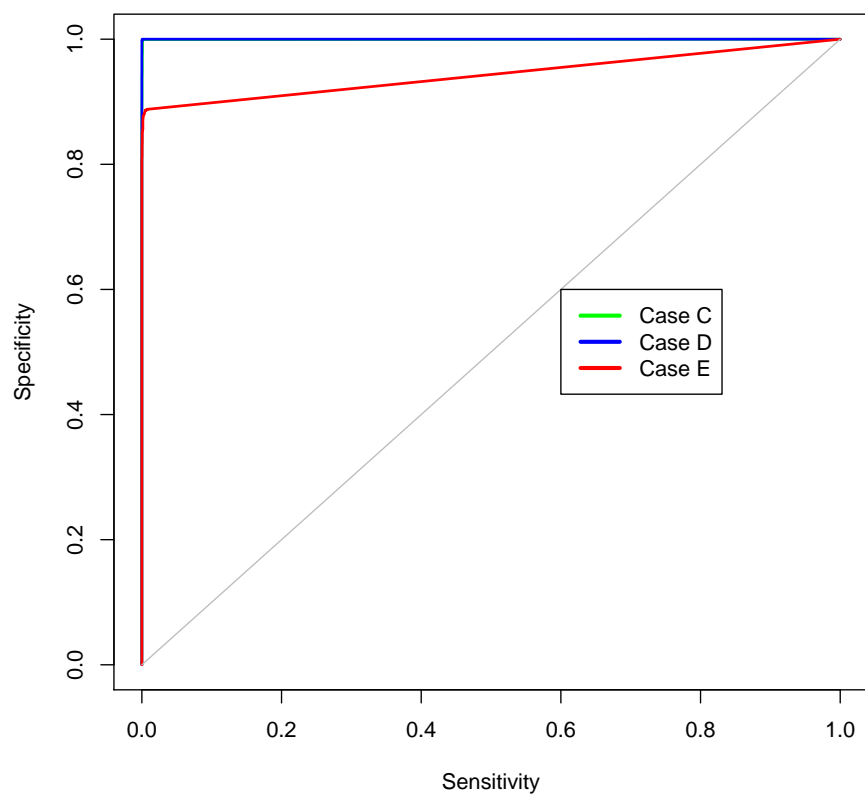
	Model	IPOD			PAWLS		
		M (%)	S (%)	JD(%)	M (%)	S (%)	JD(%)
<b>Example 1</b>	Case A	0	0	1	0	0.05	1
	Case B	0	0.1	1	0	0.06	1
	Case C	0	0.08	1	0	0	1
	Case D	0.49	0.02	0.07	0	0	1
	Case E	0.22	0.05	0.31	0.08	0	0.8

ROC Curve for example 1 with 20% outliers





ROC Curve for example 1 with 30% outliers



ROC Curve for example 2 with 10% outliers

