

# 1 Numerical Result

Table 1: Variable Selection and outliers detection Results for Example 1 ( $\beta = (3, 2, 1.5, 0, 0, 0, 0, 0)'$  with 10% outliers )

| Case     | Method  | Variable Selection |      |      |      |      | Outliers detection |      |     |        |
|----------|---------|--------------------|------|------|------|------|--------------------|------|-----|--------|
|          |         | CFR                | OFR  | PDR  | FDR  | AN   | M                  | S    | JD  | TIME   |
| <b>A</b> | ALasso  | 72                 | 25   | 99   | 7    | 3.27 | -                  | -    | -   | 0.89   |
|          | MMNNG   | 74.5               | 20.4 | 98.3 | 6.3  | 3.23 | -                  | -    | -   | NA     |
|          | SROS    | 21                 | 76   | 99   | 27.6 | 4.31 | -                  | -    | -   | 56.67  |
|          | SROS-2  | 50                 | 50   | 100  | 17.9 | 3.91 | 0                  | 6.46 | 100 | 7.89   |
|          | ASROS-2 | 86                 | 9    | 98.3 | 2.2  | 3.04 | 0                  | 3.24 | 100 | 11.88  |
|          | SLTS    | 15                 | 83   | 99.3 | 42.3 | 5.89 | 0                  | 11.4 | 100 | 200.07 |
|          | PAWLS   | 25                 | 73   | 99.3 | 27.8 | 4.45 | 0                  | 4.94 | 100 | 93.08  |
|          | APAWLS  | 76                 | 16   | 97.3 | 4.3  | 3.1  | 0                  | 2.86 | 100 | 196.75 |

Table 2: Variable Selection and outliers detection Results for Example 2 ( $\beta = (\mathbf{2}'_{10}, \mathbf{0}'_{p-10})'$  with 10% outliers )

| Case | Method  | Variable Selection |     |      |      |       | Outliers detection |       |     | TIME               |
|------|---------|--------------------|-----|------|------|-------|--------------------|-------|-----|--------------------|
|      |         | CFR                | OFR | PDR  | FDR  | AN    | M                  | S     | JD  |                    |
| A    | ALasso  | 97                 | 0   | 99.6 | 0    | 9.96  | -                  | -     | -   | 3.21               |
|      | SROS-2  | 2                  | 98  | 100  | 54.7 | 41.53 | 0                  | 4.45  | 100 | 603.94             |
|      | ASROS-2 | 85                 | 15  | 100  | 2    | 10.25 | 0                  | 0.42  | 100 | 723.54             |
|      | SLTS    | 0                  | 87  | 98.5 | 84   | 61.9  | 0                  | 24.91 | 100 | $1.89 \times 10^4$ |
|      | PAWLS   | 5                  | 95  | 100  | 32.9 | 17.02 | 0                  | 0.72  | 100 | 422.25             |
|      | APAWLS  | 91                 | 8   | 99.9 | 1.1  | 10.13 | 0                  | 0.36  | 100 | 911.97             |
| B    | ALasso  | 77                 | 1   | 94.3 | 0.5  | 9.47  | -                  | -     | -   | 3.23               |
|      | SROS-2  | 3                  | 97  | 100  | 52.6 | 32.94 | 0                  | 11.72 | 100 | 632.84             |
|      | ASROS-2 | 98                 | 2   | 100  | 0.2  | 10.02 | 0                  | 4.06  | 100 | 572.65             |
|      | SLTS    | 0                  | 93  | 98.7 | 82.7 | 57.6  | 0                  | 24.76 | 100 | $1.94 \times 10^4$ |
|      | PAWLS   | 6                  | 94  | 100  | 33.4 | 16.55 | 0                  | 2.71  | 100 | 442.9              |
|      | APAWLS  | 97                 | 3   | 100  | 0.3  | 10.03 | 0                  | 2.32  | 100 | 920.1              |
| C    | ALasso  | 0                  | 0   | 56.1 | 13.6 | 7.56  | -                  | -     | -   | 3.92               |
|      | SROS-2  | 1                  | 66  | 94.4 | 75   | 56.81 | 21.9               | 10.19 | 68  | 1214.61            |
|      | ASROS-2 | 56                 | 38  | 99.3 | 6.7  | 10.79 | 0                  | 0.16  | 100 | 650.33             |
|      | SLTS    | 0                  | 96  | 99.6 | 84   | 62.36 | 0                  | 16.47 | 100 | $2.24 \times 10^4$ |
|      | PAWLS   | 1                  | 99  | 100  | 39.6 | 18.21 | 0                  | 0.88  | 100 | 724.6              |
|      | APAWLS  | 82                 | 18  | 100  | 1.7  | 10.19 | 0                  | 0.18  | 100 | 1216.78            |
| D    | ALasso  | 0                  | 1   | 64.7 | 60.3 | 16.75 | -                  | -     | -   | 11.29              |
|      | SROS-2  | 0                  | 96  | 99.6 | 87.9 | 83.53 | 95.3               | 4.91  | 0   | 6152.51            |
|      | ASROS-2 | 0                  | 19  | 81.5 | 70.2 | 27.85 | 96.4               | 4.37  | 0   | 4328.89            |
|      | SLTS    | 0                  | 98  | 99.8 | 84.6 | 64.98 | 0                  | 16.57 | 100 | $2.72 \times 10^4$ |
|      | PAWLS   | 5                  | 92  | 99.5 | 38.7 | 21.25 | 7.2                | 0.5   | 90  | 1731               |
|      | APAWLS  | 74                 | 15  | 97.7 | 8.4  | 11.67 | 8.1                | 0.34  | 90  | 2536.55            |
| E    | ALasso  | 0                  | 0   | 31.8 | 70.8 | 10    | -                  | -     | -   | 6.78               |
|      | SROS-2  | 0                  | 55  | 92.2 | 84.6 | 61.26 | 85.5               | 15.8  | 0   | 4786.5             |
|      | ASROS-2 | 0                  | 0   | 49.1 | 75   | 17.57 | 98.9               | 0.91  | 0   | 2236.44            |
|      | SLTS    | 0                  | 96  | 99.6 | 84.6 | 65.06 | 0                  | 16.61 | 100 | $2.74 \times 10^4$ |
|      | PAWLS   | 33                 | 67  | 100  | 11.4 | 11.49 | 0                  | 0     | 100 | 1166.13            |
|      | APAWLS  | 80                 | 0   | 97.2 | 0    | 9.72  | 0                  | 0     | 100 | 1729.78            |