

Pure Shear Strain:  $\gamma = \tan \theta$

$\gamma = \text{strain}$   $\theta$  is the angle

## Stress and strain:

### “Types of Loading”

- 1) Tension
- 2) Compression
- 3) Shear
- 4) Torsion

Stress and strain are positive for tensile loads, negative for compressive loads.

## Mechanicals properties

**Engineering Stress:** Pressure due to applied load.

Units for stress: Newtons/m<sup>2</sup>

megapascal = 10<sup>6</sup> ,

1.  $\sigma = F/A_0$  tensile<sup>1</sup> or compressive<sup>2</sup> stress.

$A_0$ =Original cross section area.

$F$ =Applied force.

- In tension and compression tests, the relevant area is that perpendicular to the force
- In shear or torsion tests, the area is perpendicular to the axis of rotation.
- Force divided by area is called stress.

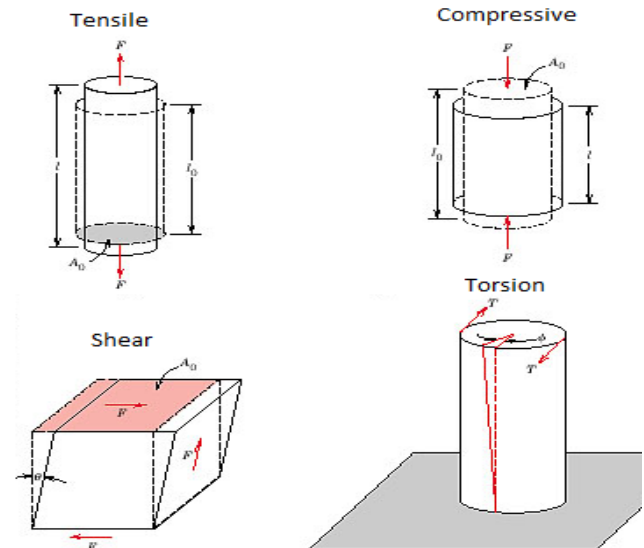
2.  $\tau = F/A_0$  shear<sup>3</sup> or torsion<sup>4</sup> stress
- $\tau$  is the stress. This symbol is more used to describe shear and torsion stress.

**Engineering Strain:** Response of the material to stress (i.e. physical deformation), degree of deformation.

Strain is unit less .

$$\epsilon = (L_i - L_o) / L_o$$

$L_i$ = instantaneous length,  $L_o$ =Original length



### True Stress :

$$\sigma = F/A_i$$

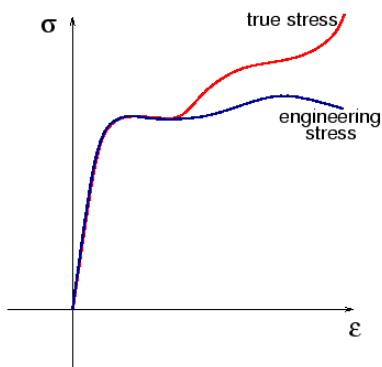
$A_i$  = Instantaneous Cross sectional area.

### True Strain:

$$\epsilon = \ln (L_i/L_o)$$

$L_i$  = instantaneous length

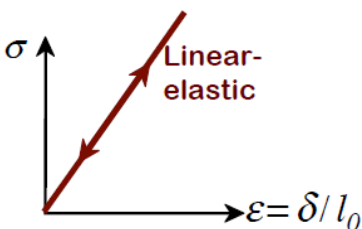
$L_o$  = Original length



## Stress-Strain Behavior

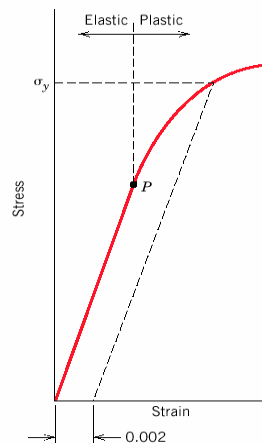
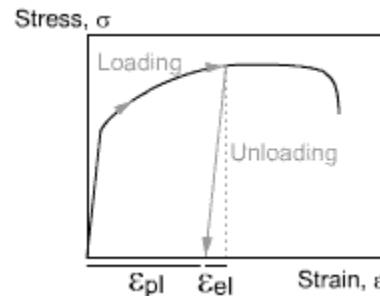
### Elastic deformation

**Reversible:** When the stress is removed, the material regains its original dimensions before the loading. Usually strains are small (except for some plastics and rubber).



### Plastic deformation

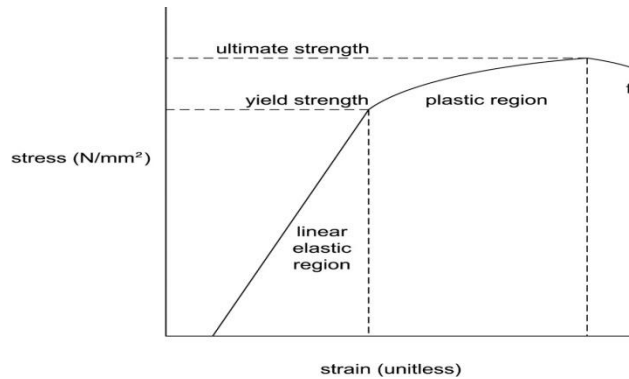
**Irreversible:** When the stress is removed, the material does not regain its original dimensions.



**-Yielding strength:** the point when a material “yields”.

- 1) Start at 0.002 (for almost all metals)
- 2) Draw a line parallel to the linear region

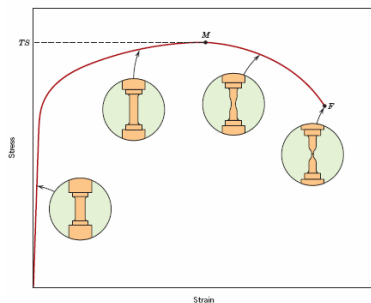
- 3)  $\sigma_y$  Is where the dotted line cross the stress-strain curve
- Mixed Elastic-Plastic Behaviour beyond P



## Poisson's ratio

The Poisson's ratio of a stable, isotropic, linear elastic material cannot be less than  $-1.0$  nor greater than  $0.5$  due to the requirement that Young's modulus, the shear modulus and bulk modulus have positive values.

- Ultimate Tensile Strength ( $\sigma_u$ ) indicates the strength of material and is a Maximum Engineering stress a material can sustain.
- However, it is only suitable for ductile materials.
- Metals:  $\sigma_u$  depend on the average size of flaw. (material property)
- Ceramics:  $\sigma_u$  depend on largest flaw (Not a material property)



- Beyond UTS necking starts and eventually material breaks at the fracture point

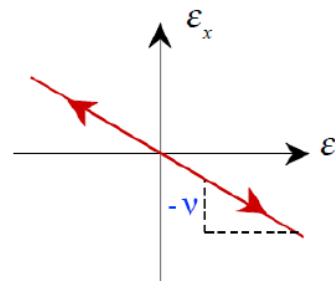
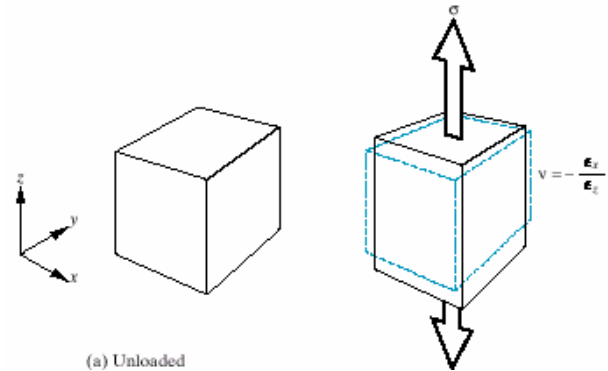
The stress-strain relationship is called **Hooke's law**:

$$\sigma = E \epsilon$$

$E$  = Young Modulus

(Slope of Stress to Strain graph)

It is material resistance to elastic deformation.



$$\nu = -\epsilon_x / \epsilon_z = -\epsilon_y / \epsilon_z$$

Range of  $\nu$  :-

$$-1 < \nu < 0.5$$

$-\nu$  is dimensionless.

