Note

Feng-Yang Hsieh

1 Signal and background

Signal events are 3 Higgs events in BSM. I use MadGraph to generate by following commands:

```
import model cxSM_VLF_EFT
generate g g > h h h
```

then pass the events through the Pythia and Delphes. In Pythia, I set the branching ratio of Higgs so that it only decays to b quarks.

Background events are 6b events in SM. I use MadGraph to generate by following commands:

```
generate p p > b b b b~ b~ b~
```

then pass the events through the Pythia and Delphes.

2 Transverse momentum and pseudorapidity distribution

In each event, there are 6 b quarks. I order these b quarks by transverse momentum $p_{\rm T}$, then plot $p_{\rm T}$ and pseudorapidity η distributions.

Figure 1 is the $p_{\rm T}$ and η distributions of b quarks for background.

Figure 2 is the $p_{\rm T}$ and η distributions of b quarks for signal.

3 Delta R and transverse momentum distribution

For signal, I plot the $\Delta R(b,b)$ distribution of two b decays from the same Higgs. Then I plot $\Delta R(b,b)$ against $p_T(b,b)$. The result is in Figure 3. As can be seen from the plot, ΔR get smaller at higher $p_T(b,b)$.



Figure 1: $p_{\rm T}$ and η distributions of b partons for background events. They are ordered by $p_{\rm T}.$



Figure 2: $p_{\rm T}$ and η distributions of b partons for signal events. They are ordered by $p_{\rm T}$.



Figure 3: $\Delta R(b,b)$ distribution and $\Delta R(b,b)$ against $p_T(b,b)$ plot

4 Cutflow table

I apply the η and $p_{\rm T}$ cuts sequentially and count how many events can pass the cuts. The results are in Table 1 and Table 2.

Table 1: 1000 background events. Those background events is generated in $\sqrt{s}=13$ TeV with the cut b $p_{\rm T}>10$ GeV in MadGraph.

| Cut | number of events pass |
|--|-----------------------|
| 6 b-partons $ \eta < 2.5$ | 330 |
| 6 b-partons $p_{\rm T} < 25~{\rm GeV}$ | 11 |
| 4 b-partons $p_{\rm T} < 40~{\rm GeV}$ | 8 |

Table 2: 1000 signal events.

| Cut | number of events pass |
|--|-----------------------|
| 6 b-partons $ \eta < 2.5$ | 732 |
| 6 b-partons $p_{\rm T} < 25~{\rm GeV}$ | 534 |
| 4 b-partons $p_{\rm T} < 40~{\rm GeV}$ | 498 |

5 Construction of bb-pairs

To construct the bb-pairs from the same Higgs, the typical strategy is to try all combinatoric and find the minimal mass difference between all pairs, i.e. minimize this

$$\chi^2 = [M(b_1b_2) - M(b_3b_4)]^2 + [M(b_1b_2) - M(b_5b_6)]^2 + [M(b_3b_4) - M(b_5b_6)]^2$$

where $M(b_ib_j)$ means the invariant mass of b-parton i and b-parton j.

The other strategy is to minimize mass difference to the SM Higgs mass

$$\chi^2 = [M(b_1b_2) - M_H]^2 + [M(b_3b_4) - M_H]^2 + [M(b_5b_6) - M_H]^2$$

I implement these two methods to construct bb-pairs and test on the 10,000 signal events at the parton level. The result is as follows:

- Method 1 (mass difference between all pairs): accuracy = 0.863
- Method 2 (mass difference to the SM Higgs mass): accuracy = 0.875

Method 2 is better for identifying the true Higgs pair.

6 Absolute cross section

The absolute cross section is defined as follows

$$\sigma_{\rm abs} = \sigma \times \frac{\text{number of events pass the cut}}{\text{number of events}}$$

I have generated background events with different cuts in MadGraph, the detailed information of cuts is in Table 3. I calculate their absolute cross section and check if it is the same or not. The result is in Table 4.

From Table 4, if the number of events is large enough the absolute cross section will be similar.

7 The problem for generating pp \rightarrow 6b events

Failed to generate the requested number of events

Table 3: The cuts applied on the different runs. Where $p_{\rm T}$ means the minimum transverse momentum of b and $|\eta|$ means the range of b (-1 means no restriction).

| No. | $p_{\rm T}~({\rm GeV})$ | $ \eta $ |
|-----|-------------------------|----------|
| 1 | 0 | -1 |
| 2 | 10 | 5 |
| 3 | 10 | 3 |
| 4 | 20 | 3 |
| 5 | 0 | -1 |
| 6 | 10 | -1 |

Table 4: Absolute cross section. Where the selection cut is $p_{\rm T}>20$ GeV, $|\eta|<3$.

| No. | total event | cross section | events pass selection | absolute cross section |
|-----|-------------|---------------|-----------------------|------------------------|
| 1 | 339 | 2731.9362 | 0 | 0.0 |
| 2 | 4761 | 71.316651 | 190 | 2.846 |
| 3 | 9054 | 35.225852 | 694 | 2.700 |
| 4 | 4207 | 2.7698473 | 4183 | 2.754 |
| 5 | 1000 | 2531.9304 | 0 | 0.0 |
| 6 | 1000 | 70.158431 | 27 | 1.894 |

$8 \quad pp \rightarrow 4b$

I use MadGraph to generate 4b events by following commands:

In MadGraph, I apply the cuts: $p_T > 25 \text{ GeV}$, $|\eta| < 2.5 \text{ for b.}$ Pass those events through Pythia, then check how many events there are 6 b-hadrons final state.

In 100,000 events, 6,916 events are having greater than or equal to 6 b-hadrons. The distribution of number of b-hadrons is in Figure 4.



Figure 4: Number of b-hadrons in Pythia final state.

Pass events through Delphes. In Delphes the b-tagging efficiency is set to 1.

Figure 5 is the number of jets and number of b-jets distributions. In 100,000 events, 173 events are having greater than or equal to 6 b-jets.

9 Comparison for pp \rightarrow 4b and pp \rightarrow 6b event

To compare pp->4b and pp->6b events, I plot the $p_{\rm T}$, η and total invariant mass of 6 b-jets for both.

The number of events of 6 b-jets for pp->4b is 2051 and for pp->6b is 1408. I scaled the number of events for pp->4b to be the same as pp->6b.



Figure 5: Number of jets and number of b-jets.

Figure 6 is $p_{\rm T}$ and η distributions. Figure 7 is total invariant mass of 6 b-jets distributions. Their distributions look similar.

10 Cutflow table for b-jets

I apply the following cut sequentially and count how many events can pass these cuts. Table 5 is the result for pp->4b events. Table 6 is the result for pp->6b events. Table 7 is the result for signal events.

- Cut 1: There are greater than or equal to 6 b-jets.
- Cut 2: There are greater than or equal to 6 b-jets satisfy $|\eta| < 2.5$.
- Cut 3: There are greater than or equal to 6 b-jets satisfy $p_T > 25$ GeV.
- Cut 4: There are greater than or equal to 4 b-jets satisfy $p_T > 40$ GeV.

Table 5: 1,000,000 pp->4b events. Those events are generated in $\sqrt{s}=14$ TeV with the cuts: $p_T>25$ GeV, $|\eta|<2.5$ for b in MadGraph.

| Cut | number of event pass |
|-----|----------------------|
| 1 | 1783 |
| 2 | 1565 |
| 3 | 1059 |
| 4 | 735 |



Figure 6: $p_{\rm T}$ and η distributions of b-jets for pp->4b and pp->6b events. They are ordered by $p_{\rm T}$.



Figure 7: The distribution of total invariant mass of 6 b-jets for pp->4b and pp->6b events.

Table 6: 10,000 pp->6b events. Those events are generated in $\sqrt{s}=14$ TeV with the cuts: $p_{\rm T}>25$ GeV, $|\eta|<2.5$ for b in MadGraph.

| Cut | number of event pass |
|-----|----------------------|
| 1 | 1408 |
| 2 | 1322 |
| 3 | 1052 |
| 4 | 822 |

Table 7: 100,000 signal events. Those events are generated in $\sqrt{s}=14$ TeV.

| Cut | number of event pass |
|-----|----------------------|
| 1 | 21,814 |
| 2 | 21,254 |
| 3 | 17,130 |
| 4 | 14,142 |

11 Signal

Generate resonant channel gg->h3, h3->h2h, h2->hh in MadGraph by following commands:

```
import model cxSM_VLF_EFT
generate g g > h3, (h3 > h2 h, h2 > h h)
```

then check whether this channel is dominated in signal (gg->3h) or not.

I generate this channel and signal in $\sqrt{s} = 14$ TeV, the cross sections are 2.094 pb and 4.067 pb, respectively.

Figure 8 is the total invariant mass of 6 b-jets for signal events. Figure 9 is the total invariant mass of 6 b-jets for this resonant channel. From the results, there is a peak around 400 GeV, because the mass of h_3 is $m_3 = 420$ GeV.

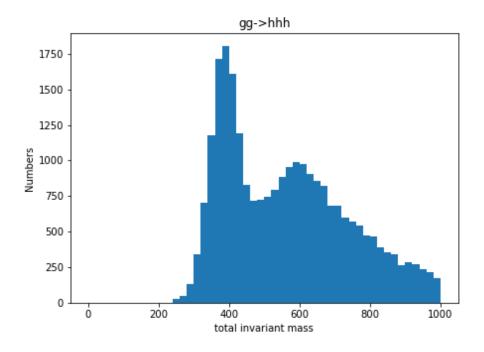


Figure 8: Total invariant mass of 6 b-jets for signal events.

A bump around 600 GeV in Figure 8? In the run card, some parameters are not set correctly. After setting all parameters correctly and regenerating these event, the results are in Figure 10. There is no bump around 600 GeV.

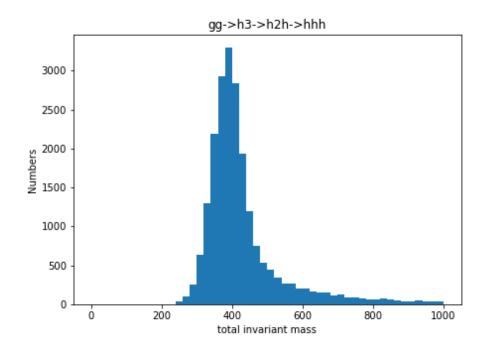


Figure 9: Total invariant mass of 6 b-jets for the resonant channel.

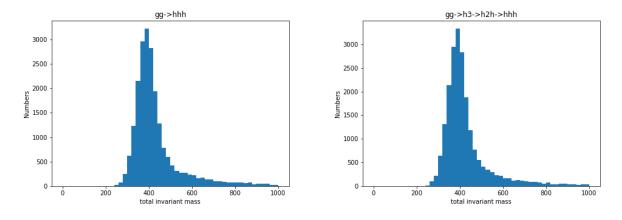


Figure 10: Total invariant mass of 6 b-jets for signal events and resonant channel (correct parameters).

12 The cross section in MadGraph

Table 8 is the cross sections calculated by MadGraph and in paper. They are different because in MadGraph we only consider LO. But in the paper, the numbers are quoted from the LHC Higgs Cross Section Working Group, and they have considered up to NNLO. The "k factor" is around 2.5, which accounts for the values in gg>h3.

Table 8: Cross section from MadGraph and paper

| Process | σ MadGraph (fb) | σ in paper (fb) |
|-----------------|------------------------|------------------------|
| g g > h3 | 21 | 55 |
| gg > h3 > h h h | 4.0 | 38.2 |

The problem of cross section: If we use the default run card to generate the decay process, the value of the cross section will be problematic.

Solution:

In madevent, use command compute_widths to compute decay widths of h_2 , h_3 , then replace the run_card_dat by run_card_default.dat.

Regenerate the signal and resonant event, the cross sections are 11.1 fb and 10.39 fb, respectively. This channel is indeed dominated in the signal.

13 Comparision for pp \rightarrow hhh and gg \rightarrow hhh

Generate pp->hhh in MadGraph by following commands:

```
import model cxSM_VLF_EFT
define p = p b b~
generate p p > h h h QCD<=8</pre>
```

Generate gg->hhh in MadGraph by following commands:

```
import model cxSM_VLF_EFT
generate g g > h h h
```

These events are generated in 14 TeV and the sample size is 100k. The cross section for pp->hhh and gg->hhh are 11.22 fb and 11.11 fb, respectively. They only differ by 1%.

14 Comparision for $gg \rightarrow hhh$ and resonant channel

To compare gg \rightarrow hhh and resonant channel, I plot the $p_{\rm T}$, η , and total invariant mass of 6 b-jets for both.

These events are generated in 14 TeV and the sample size is 100k. The cross section for gg->hhh and resonant channel are 11.11 fb and 10.38 fb, respectively.

The number of events of 6 b-jets for gg->hhh is 21,814 and for the resonant channel is 21,475. The numbers are very close. I scaled the number of events for gg->3h to be the same as the resonant channel.

Figure 11 is $p_{\rm T}$ and η distributions. Figure 12 is total invariant mass of 6 b-jets distributions. Their distributions look similar.

I apply the cuts same in Sec.10 and count how many events can pass these cuts. Table 9 is the result. The results for both events are similar.

Table 9: Number of events pass the selection cuts. The total number of events for gg->hhh and resonant channel are 100,000.

| Cut | gg->3h | resonant channel |
|-----|--------|------------------|
| 1 | 21,814 | 21,475 |
| 2 | 21,254 | 20,898 |
| 3 | 17,130 | 16,828 |
| 4 | 14,142 | 13,730 |

15 Branching ratios and decay widths

The branching ratios and decay widths are calculated by MadGraph and Mathematica notebook. Mathematica notebook does not include uu dd ss ee decay modes. Since the contribution of these modes is very small.

Table 10 is calculated by MadGraph. Table 11 is calculated by Mathematica notebook.

The exact values from both are slightly different because MG can not correctly expand the parameter ϵ in the model.

Set the ϵ to 0.001 and calculate again. The results are in Table 12 and Table 13.

This time, the decay widths and branching ratios calculated by MG and Mathematica notebook become close.



Figure 11: $p_{\rm T}$ and η distributions of b-jets for gg->3h and resonant channel. They are ordered by $p_{\rm T}$.

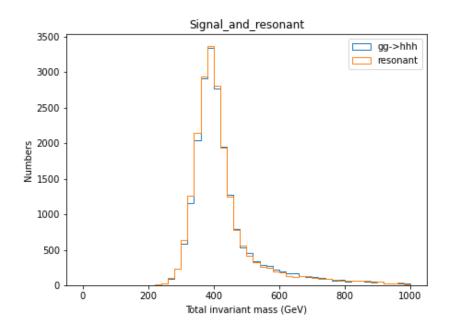


Figure 12: The distribution of total invariant mass of 6 b-jets for gg->3h and resonant channel.

Table 10: Decay widths and branching ratios calculated by MadGraph at BP1.

| | BR | Width (GeV) | | BR | Width (GeV) |
|-------------------------|------------|-------------|-------------------------|------------|-------------|
| $h_2 \to h_1 h_1$ | 0.7506 | 0.085616 | $h_3 \to h_1 h_2$ | 0.6795 | 0.8414 |
| $h_2 \to WW$ | 0.1734 | 0.019782 | $h_3 \to h_1 h_1$ | 0.1711 | 0.21183 |
| $h_2 \to ZZ$ | 0.07548 | 0.0086097 | $h_3 \to WW$ | 0.08756 | 0.10842 |
| $h_2 \to bb$ | 0.0004724 | 5.3887e-05 | $h_3 \to ZZ$ | 0.04102 | 0.050792 |
| $h_2 \to cc$ | 3.455 e-05 | 3.9407e-06 | $h_3 \to tt$ | 0.02065 | 0.025569 |
| $h_2 \to \tau\tau$ | 2.254e-05 | 2.5714e-06 | $h_3 \to gg$ | 8.662 e-05 | 0.00010725 |
| $h_2 \to ss$ | 2.185e-07 | 2.4927e-08 | $h_3 \to bb$ | 8.158e-05 | 0.00010102 |
| $h_2 \to gg$ | 1.561e-07 | 1.7811e-08 | $h_3 \to cc$ | 5.961e-06 | 7.3813e-06 |
| $h_2 \to \mu\mu$ | 7.972e-08 | 9.0933e-09 | $h_3 \to \tau \tau$ | 3.89e-06 | 4.8167e-06 |
| $h_2 \to \gamma \gamma$ | 6.495 e-09 | 7.409e-10 | $h_3 \to \gamma \gamma$ | 3.852e-07 | 4.7697e-07 |
| $h_2 \to \gamma Z$ | 9.447e-10 | 1.0776e-10 | $h_3 \to \gamma Z$ | 4.937e-08 | 6.1131e-08 |
| $h_2 \to dd$ | 5.441e-10 | 6.207e-11 | $h_3 \to ss$ | 3.77e-08 | 4.6686e-08 |
| $h_2 \to u u$ | 1.393e-10 | 1.5889e-11 | $h_3 \to \mu\mu$ | 1.375 e-08 | 1.7031e-08 |
| $h_2 \to ee$ | 1.865e-12 | 2.1269e-13 | $h_3 \to dd$ | 9.389e-11 | 1.1625 e-10 |
| | | | $h_3 \to uu$ | 2.403e-11 | 2.976e-11 |
| | | | $h_3 \rightarrow ee$ | 3.217e-13 | 3.9835e-13 |

Table 11: Decay widths and branching ratios calculated by Mathematica at BP1.

| | BR | Width (GeV) | | BR | Width (GeV) |
|-------------------------|--------------|-------------|-------------------------|------------|-------------|
| $h_2 \to h_1 h_1$ | 0.8321 | 0.1407 | $h_3 \to h_1 h_2$ | 0.8219 | 2.158 |
| $h_2 \to WW$ | 0.1166 | 0.019721 | $h_3 \to h_1 h_1$ | 0.1049 | 0.27543 |
| $h_2 \to ZZ$ | 0.05108 | 0.0086386 | $h_3 \to WW$ | 0.04131 | 0.10846 |
| $h_2 \to gg$ | 0.0001204 | 2.0359e-05 | $h_3 \to ZZ$ | 0.01941 | 0.050962 |
| $h_2 \to bb$ | 9.91e-05 | 1.6758e-05 | $h_3 \to tt$ | 0.01242 | 0.032613 |
| $h_2 \to \tau\tau$ | 1.526 e - 05 | 2.5802 e-06 | $h_3 \to gg$ | 6.364 e-05 | 0.00016711 |
| $h_2 \to cc$ | 4.59e-06 | 7.7613e-07 | $h_3 \to bb$ | 1.195 e-05 | 3.1386e-05 |
| $h_2 \to \gamma \gamma$ | 3.161e-06 | 5.346e-07 | $h_3 \to \tau \tau$ | 1.841e-06 | 4.8326e-06 |
| $h_2 \to \gamma Z$ | 4.822e-07 | 8.154 e-08 | $h_3 \to cc$ | 5.536e-07 | 1.4536e-06 |
| $h_2 \to \mu\mu$ | 5.43e-08 | 9.1826e-09 | $h_3 \to \gamma \gamma$ | 1.823 e-07 | 4.7857e-07 |
| $h_2 \to t t$ | 4.355e-19 | 7.3649e-20 | $h_3 \to \gamma Z$ | 2.334e-08 | 6.1277e-08 |
| | | | $h_3 \to \mu\mu$ | 6.55 e-09 | 1.7198e-08 |
| | | | | | |

Table 12: Decay widths and branching ratios calculated by MadGraph at BP1 with $\epsilon=0.001$.

| | BR | Width (GeV) | | BR | Width (GeV) |
|-------------------------|--------------|-------------|-------------------------|------------|-------------|
| $h_2 \to h_1 h_1$ | 0.8311 | 1.4041 e-05 | $h_3 \to h_1 h_2$ | 1.0 | 2.1493 |
| $h_2 \to WW$ | 0.1174 | 1.9835 e-06 | $h_3 \to h_1 h_1 \\$ | 1.279 e-05 | 2.748e-05 |
| $h_2 \to ZZ$ | 0.0511 | 8.6329 e-07 | $h_3 \to WW$ | 5.058e-06 | 1.0871e-05 |
| $h_2 \to bb$ | 0.0003198 | 5.4032e-09 | $h_3 \to ZZ$ | 2.369e-06 | 5.0929 e-06 |
| $h_2 \to cc$ | 2.339e-05 | 3.9513e-10 | $h_3 \to t t$ | 1.193e-06 | 2.5638e-06 |
| $h_2 \to \tau\tau$ | 1.526 e - 05 | 2.5783e-10 | $h_3 \to gg$ | 5.007e-09 | 1.0761e-08 |
| $h_2 \to ss$ | 1.479 e - 07 | 2.4994e-12 | $h_3 \to bb$ | 4.713e-09 | 1.0129 e-08 |
| $h_2 \to \mu\mu$ | 5.397e-08 | 9.1178e-13 | $h_3 \to cc$ | 3.443e-10 | 7.4011e-10 |
| $h_2 \to dd$ | 3.684e-10 | 6.2237e-15 | $h_3 \to \tau\tau$ | 2.247e-10 | 4.8297e-10 |
| $h_2 \to uu$ | 9.431e-11 | 1.5932e-15 | $h_3 \to \gamma \gamma$ | 2.227e-11 | 4.7857e-11 |
| $h_2 \to gg$ | 1.056e-11 | 1.7841e-16 | $h_3 \to \gamma Z$ | 2.854e-12 | 6.1335e-12 |
| $h_2 \to ee$ | 1.262e-12 | 2.1326e-17 | $h_3 \to ss$ | 2.178e-12 | 4.6812e-12 |
| $h_2 \to \gamma \gamma$ | 4.393e-13 | 7.4213e-18 | $h_3 \to \mu\mu$ | 7.945e-13 | 1.7077e-12 |
| $h_2 \to \gamma Z$ | 6.389 e-14 | 1.0794e-18 | $h_3 \to dd$ | 5.423e-15 | 1.1657e-14 |
| | | | $h_3 \to uu$ | 1.388e-15 | 2.984e-15 |
| | | | $h_3 \to ee$ | 1.858e-17 | 3.9942e-17 |

Table 13: Decay widths and branching ratios calculated by Mathematica at BP1 with $\epsilon = 0.001$.

| | BR | Width (GeV) | | BR | Width (GeV) |
|-------------------------|--------------|-------------|-------------------------|--------------|---------------|
| $h_2 \to h_1 h_1$ | 0.8321 | 1.407e-05 | $h_3 \to h_1 h_2$ | 1.0 | 2.158 |
| $h_2 \to WW$ | 0.1166 | 1.9721e-06 | $h_3 \to h_1 h_1$ | 1.276 e-05 | 2.7543e-05 |
| $h_2 \to ZZ$ | 0.05108 | 8.6386e-07 | $h_3 \to WW$ | 5.026e-06 | 1.0846 e - 05 |
| $h_2 \to gg$ | 0.0001204 | 2.0359e-09 | $h_3 \to ZZ$ | 2.361e-06 | 5.0962e-06 |
| $h_2 \to bb$ | 9.91 e-05 | 1.6758e-09 | $h_3 \to tt$ | 1.511e-06 | 3.2613e-06 |
| $h_2 \to \tau\tau$ | 1.526 e - 05 | 2.5802e-10 | $h_3 \to gg$ | 7.743e-09 | 1.6711e-08 |
| $h_2 \to cc$ | 4.59 e - 06 | 7.7613e-11 | $h_3 \to bb$ | 1.454 e - 09 | 3.1386e-09 |
| $h_2 \to \gamma \gamma$ | 3.161e-06 | 5.346e-11 | $h_3 \to \tau\tau$ | 2.239e-10 | 4.8326e-10 |
| $h_2 \to \gamma Z$ | 4.822e-07 | 8.154e-12 | $h_3 \to cc$ | 6.736e-11 | 1.4536e-10 |
| $h_2 \to \mu\mu$ | 5.43e-08 | 9.1826e-13 | $h_3 \to \gamma \gamma$ | 2.218e-11 | 4.7857e-11 |
| $h_2 \to t t$ | 4.355e-15 | 7.3649e-20 | $h_3 \to \gamma Z$ | 2.839e-12 | 6.1277e-12 |
| | | | $h_3 \to \mu\mu$ | 7.969e-13 | 1.7198e-12 |

For color channels, still don't look the same. The reason is that in MadGraph only calculates to LO, but the numbers in the Mathematica notebook are calculated to NLO.

16 SPANet

Code: Symmetry Preserving Attention Networks

Symmetry Preserving Attention NETworks (Spa-Net) is used to do the jet assignment task. The jet assignment task is the identification of the original particle which leads to a reconstructed jet.

16.1 Prepare training data

1. Defining the event topology in .ini file. The structure of the .ini file follows this format:

```
[SOURCE]

FEATURE_1 = FEATURE_OPTION

FEATURE_2 = FEATURE_OPTION

FEATURE_3 = FEATURE_OPTION
```

```
[EVENT]
particles = (PARTICLE_1, PARTICLE_2, ...)
permutations = EVENT_SYMMETRY_GROUP

[PARTICLE_1]
jets = (JET_1, JET_2, ...)
permutations = JET_SYMMETRY_GROUP

[PARTICLE_2]
jets = (JET_1, JET_2, ...)
permutations = JET_SYMMETRY_GROUP
```

- 2. Create training dataset in HDF5 format.
- 3. Write option-file in JSON format.

16.2 Training

Training:

```
python train.py -of <OPTIONS_FILE> --log_dir <LOG_DIR> --name <NAME> --gpus 1
<OPTIONS_FILE>: JSON file with option overloads. <LOG_DIR>: output directory. <NAME>:
subdirectory for this run.
Evaluation:
```

```
python test.py <log_directory> --gpu
<log_directory>: directory containing the checkpoint and options file.
python test.py <log_directory> -tf <TEST_FILE> --gpu
<TEST_FILE> will replace the test file in option file.
```

17 SPANet for ttbar event

The training and testing datasets from here: Link For full ttbar event:

- Training sample:
 - Total sample size: 10,009,520
 - 2t sample size: 2,967,955
- Testing sample size:
 - Total sample size: 358,946
 - 2t sample size: 116,342

Figure 13 is the training results for full ttbar events. The results are the same as the numbers given in the SPANet paper.

18 SPANet for di-Higgs event

The .ini file for di-Higgs event (h > b b)

Generate di-Higgs events in MadGraph by following commands:

```
generate p p > h2 [QCD] QED<=99 QCD<=99 then use the MadSpin let h2 decay to h1h1 and h1 decay to b\overline{b}. The mass of h2 is 1000 GeV.
```

```
[SOURCE]
mass = log_normalize
pt = log_normalize
eta = normalize
phi = normalize

[EVENT]
particles = (h1, h2)
permutations = [(h1, h2)]
```

import model 2HDMtII NLO

[h1]

| | | | + | + |
|------------------------------|--|--|--|--|
| Event Type: *t | | · | + | ++- |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | T Purity |
| == 6 == 7 >= 8 Full | 0.812 0.851 0.881 0.850 | 0.308 0.341 0.351 1.000 | 0.640 0.597 0.523 0.583 | 0.694 0.665 0.610 0.652 |
| Event Type: 0t | | | · | · |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | T Purity |
| == 6 == 7 >= 8 Full | 0.188 0.149 0.119 0.150 | 0.308 0.341 0.351 1.000 | 1.000 1.000 1.000 1.000 | N/A N/A N/A N/A |
| Event Type: 1t | • | · | · | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | ++- T Purity |
| | 0.566 0.531 0.484 0.525 | 0.308 0.341 0.351 1.000 | 0.567 0.556 0.523 0.549 | 0.567 0.556 0.523 0.549 |
| Event Type: 2t Jet Limit | Event Proportion | Jet Proportion | + + Event Purity | |
| Jet Limit | Event Proportion 0.246 0.320 0.397 0.324 | Jet Proportion 0.308 0.341 0.351 1.000 | Event Purity | 0.841 |

Figure 13: The training result for full ttbar events.

```
jets = (b1, b2)
permutations = [(b1, b2)]

[h2]
jets = (b1, b2)
permutations = [(b1, b2)]
```

There are three types of events, 0h, 1h, and 2h. The number means how many identifiable Higgs is in an event.

Definition of some parameters:

• Event proportion:

Event proportion
$$\equiv \frac{\text{number of some type events with } i \text{ jets}}{\text{number of events with } i \text{ jets}}$$
 (1)

• Jet proportion:

Jet proportion
$$\equiv \frac{\text{number of events with } i \text{ jets}}{\text{total number of events}}$$
 (2)

• Event purity:

$$\epsilon^{\text{event}} \equiv \frac{\text{number of some type events with and all Higgs are correctly identified}}{\text{number of some type events}}$$
 (3)

• H purity:

$$\epsilon^{\rm h} \equiv \frac{\text{number of correctly identified Higgs in some type events}}{\text{number of identifiable Higgs in some type events}}$$
(4)

18.1 Training sample for di-Higgs events

Di-Higgs events pp->h2, h2->hh, h->bb was generated at $\sqrt{s}=14$ TeV using Mad-Graph. Then pass these events to Pythia8 for showering and hadronization. Then pass to Delphes for detector simulation.

Jets are reconstructed by the anti-kT algorithm with radius R=0.5 and are required to have $p_{\rm T} \geq 20$ GeV.

Preselection requirements: ≥ 4 jets in $|\eta| < 2.5$.

Define the correct jet assignments by matching them to the simulated truth quarks within an angular distance of $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} < 0.4$.

18.2 Training result for di-Higgs event

For 100k di-Higgs event with $m_{\rm h_2}=1000$ GeV:

• Training sample:

 $-\,$ Total sample size: $78{,}785$

- 2h sample size: 36,765

- 5% used on validation

• Testing sample:

- Total sample size: 8,753

- 2h sample size: 4,130

| Event Type: *h | + | | | ++- |
|------------------------------|--|--|--|--|
| Jet Limit | + Event Proportion | + Jet Proportion | + Event Purity | ++- H Purity |
| == 4 == 5 >= 6 Full | 0.887 0.925 0.947 0.922 | 0.291 0.331 0.378 1.000 | 0.945 0.908 0.792 0.874 | 0.960 0.940 0.865 0.914 |
| Event Type: 0h | + | · | · | · |
| Jet Limit | + Event Proportion | Jet Proportion | Event Purity | |
| == 4 == 5 >= 6 Full | 0.113 0.075 0.053 0.078 | 0.291 0.331 0.378 1.000 | 1.000 1.000 1.000 1.000 | N/A |
| | | | | |
| Event Type: 1h | | | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.545 0.442 0.385 0.450 | 0.291 0.331 0.378 1.000 | 0.911 0.888 0.827 0.876 | 0.911 0.888 0.827 0.876 |
| Event Type: 2h | + | · | · | ++- |
| Jet Limit | + Event Proportion | Jet Proportion | Event Purity | ++- H Purity |
| | 0.342 0.483 0.562 0.472 | 0.291 0.331 0.378 1.000 | 1.000 0.926 0.769 0.871 | 1.000 |

Figure 14: The training result for 100k di-Higgs events.

Figure 14 is the training results for 100k di-Higgs events. For 2h events, $\epsilon^{\text{event}} = 0.871, \epsilon^{\text{h}} = 0.933$.

For 1M di-Higgs event with $m_{\rm h_2} = 1000$ GeV:

- Training sample:
 - Total sample size: 788,160
 - 2h sample size: 364,773
 - 5% used on validation
- Testing sample:
 - Total sample size: 87,702
 - 2h sample size: 40,695

Figure 15 is the training results for 1M di-Higgs events. For 2h events, $\epsilon^{\text{event}} = 0.914, \epsilon^{\text{h}} = 0.955$.

For di-Higgs event with $m_{\rm h_2} = 500$ GeV:

- Training sample:
 - Total sample size: 764,676
 - 2h sample size: 396,588
 - -5% used on validation
- Testing sample:
 - Total sample size: 84,687
 - 2h sample size: 43,818

Figure 16 is the training results for 500 GeV di-Higgs events. For 2h events, $\epsilon^{\text{event}} = 0.779, \epsilon^{\text{h}} = 0.871.$

18.3 Apply the pre-trained model on different m_{h_2} sample

The SPANet models in Sec.18.2 are trained on $m_{\rm h_2} = 500$ GeV and $m_{\rm h_2} = 1000$ GeV. Test these models on samples with $m_{\rm h_2} = 500$ GeV, 750 GeV, 1000 GeV.

The results are summarized in Table 14.

| Event Type: *h | · | · | | · |
|------------------------------|--|----------------------------------|----------------------------------|--|
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.877 0.920 0.944 0.916 | 0.301 0.326 0.372 1.000 | 0.950 0.919 0.831 0.894 | 0.964 0.946 0.891 0.928 |
| Event Type: 0h | I | | | · |
| Jet Limit | + Event Proportion | Jet Proportion | Event Purity | |
| == 4 == 5 >= 6 Full | 0.123 0.080 0.056 0.084 | 0.301 0.326 0.372 1.000 | 1.000 1.000 1.000 1.000 | N/A |
| | | | | |
| Event Type: 1h | | | | · |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.533 0.445 0.394 0.452 | 0.301 0.326 0.372 1.000 | 0.917 0.885 0.813 0.873 | 0.917 0.885 0.813 0.873 |
| Event Type: 2h | · | · | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | |
| == 4 == 5 >= 6 Full | 0.345 0.475 0.551 0.464 | 0.301 0.326 0.372 1.000 | 1.000 0.950 0.844 0.914 | 1.000 0.975 0.918 |

Figure 15: The training result for 1M di-Higgs events.

Table 14: SPANet models test on different $m_{\rm h_2}$ samples.

| Training $m_{\rm h_2}$ (GeV) | Testing $m_{\rm h_2}$ (GeV) | Event purity | H purity |
|------------------------------|-----------------------------|--------------|----------|
| 500 | 500 | 0.779 | 0.871 |
| 500 | 750 | 0.408 | 0.672 |
| 500 | 1000 | 0.390 | 0.665 |
| 1000 | 500 | 0.383 | 0.638 |
| 1000 | 750 | 0.731 | 0.860 |
| 1000 | 1000 | 0.914 | 0.955 |

| | + <u>-</u> | + <u></u> | + <u>-</u> | + <u>+-</u> |
|------------------------------|--|--|--|--|
| Event Type: *h | | | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.872 0.923 0.944 0.914 | 0.319 0.325 0.356 1.000 | 0.879 0.802 0.633 0.763 | 0.914 0.868 0.753 0.836 |
| | | | | |
| Event Type: 0h | | | | ++- |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.128 0.077 0.056 0.086 | 0.319 0.325 0.356 1.000 | 1.000 1.000 1.000 1.000 | N/A N/A N/A N/A |
| | | | | |
| Event Type: 1h | | | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.497 0.391 0.312 0.397 | 0.319 0.325 0.356 1.000 | 0.793 0.748 0.666 0.743 | 0.793 0.748 0.666 0.743 |
| Event Type: 2h | | · | +································ | · |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 4 == 5 >= 6 Full | 0.375 0.532 0.632 0.517 | 0.319 0.325 0.356 1.000 | 0.994 0.841 0.617 0.779 | 0.994 0.912 0.775 0.871 |

Figure 16: The training result for di-Higgs events with $m_{\rm h_2}=500$ GeV.

19 SPANet for tri-Higgs event

The tri-Higgs events are signal events (gg->hhh) generated in the previous.

19.1 Training sample for tri-Higgs event

Tri-Higgs events gg->hhh was generated at $\sqrt{s} = 14$ TeV using MadGraph. Then pass these events to Pythia8 for showering and hadronization. In Pythia8, the Higgs is forced to decay to $b\bar{b}$. Then pass to Delphes for detector simulation.

Jets are reconstructed by the anti-kT algorithm with radius R=0.5 and are required to have $p_{\rm T} \geq 20$ GeV.

Preselection requirements: ≥ 6 jets in $|\eta| < 2.5$.

Define the correct jet assignments by matching them to the simulated truth quarks within an angular distance of $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} < 0.4$.

19.2 Training result for tri-Higgs event

For 1M tri-Higgs event:

- Training sample:
 - Total sample size: 542,681
 - 3h sample size: 104,467
 - 5% used on validation
- Testing sample:
 - Total sample size: 60,173
 - 3h sample size: 11,598

Figure 17 is the training results for 1M tri-Higgs events. For 3h events, $\epsilon^{\text{event}} = 0.344, \epsilon^{\text{h}} = 0.538.$

| | + | | + <u></u> | + <u>+-</u> |
|------------------------------|--|--|--|--|
| Event Type: 0h | | | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 6 == 7 >= 8 Full | 0.186 0.147 0.119 0.157 | 0.439 0.313 0.248 1.000 | 1.000 1.000 1.000 1.000 | N/A |
| | · | · | · | · |
| Event Type: 1h | | | · | · |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 6 == 7 >= 8 Full | 0.386 0.337 0.312 0.353 | 0.439 0.313 0.248 1.000 | 0.452 0.405 0.334 0.412 | 0.452 0.405 0.334 0.412 |
| | | | · | · |
| Event Type: 2h | | | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 6 == 7 >= 8 Full | 0.303 0.298 0.285 0.297 | 0.439 0.313 0.248 1.000 | 0.293 0.228 0.152 0.239 | 0.489 0.429 0.343 0.435 |
| | • | · | · | · |
| Event Type: 3h | | | | |
| Jet Limit | Event Proportion | Jet Proportion | Event Purity | H Purity |
| == 6 == 7 >= 8 Full | 0.124 0.218 0.283 0.193 | 0.439 0.313 0.248 1.000 | 0.603 0.336 0.152 0.344 | 0.705 |

Figure 17: The training result for 1M tri-Higgs events.

20 χ^2 method

20.1 Di-Higgs

Try all possible combinations of final jets and find the minimal mass difference between SM Higgs mass, i.e. minimize this

$$\chi^2 = [M(j_1 j_2) - M_{\rm H}]^2 + [M(j_3 j_4) - M_{\rm H}]^2$$
(5)

where $M(j_i j_j)$ means the invariant mass of jet i and jet j.

The results are presented in Table 15.

Table 15: Performance comparison for di-Higgs events.

| | Event | SPANet Efficiency | | χ^2 Effi | ciency |
|--------------|----------|-------------------|-------|---------------|--------|
| $N_{ m Jet}$ | Fraction | Event | Higgs | Event | Higgs |
| = 4 | 0.224 | 1.000 | 1.000 | 1.000 | 1.000 |
| =5 | 0.334 | 0.950 | 0.975 | 0.675 | 0.737 |
| ≥ 6 | 0.442 | 0.844 | 0.918 | 0.313 | 0.441 |
| Total | 1.000 | 0.914 | 0.955 | 0.582 | 0.665 |

20.2 Di-Higgs with b-tag

Similarly, try to minimize (5), but only try all possible permutations of b-tagged jets. Here, we only consider the events with ≥ 4 b-jets.

The results are presented in Table 16 and Table 17.

Table 16: Performance comparison for di-Higgs events with ≥ 4 b-jets (b-tagging efficiency = 100%).

| | Event | SPANet Efficiency | | χ^2 Efficiency | |
|--------------|----------|-------------------|-------|---------------------|-------|
| $N_{ m Jet}$ | Fraction | Event | Higgs | Event | Higgs |
| = 4 | 0.224 | 1.000 | 1.000 | 1.000 | 1.000 |
| =5 | 0.334 | 0.980 | 0.990 | 0.974 | 0.979 |
| ≥ 6 | 0.442 | 0.946 | 0.972 | 0.916 | 0.933 |
| Total | 1.000 | 0.969 | 0.984 | 0.954 | 0.963 |

Table 17: Performance comparison for di-Higgs events with ≥ 4 b-jets (b-tagging efficiency = default).

| | Event | SPANet Efficiency | | χ^2 Efficiency | |
|--------------|----------|-------------------|-------|---------------------|-------|
| $N_{ m Jet}$ | Fraction | Event | Higgs | Event | Higgs |
| =4 | 0.200 | 1.000 | 1.000 | 1.000 | 1.000 |
| =5 | 0.318 | 0.950 | 0.975 | 0.892 | 0.914 |
| ≥ 6 | 0.482 | 0.865 | 0.930 | 0.725 | 0.776 |
| Total | 1.000 | 0.919 | 0.958 | 0.833 | 0.865 |

20.3 Tri-Higgs

Try all possible combinations of final jets and find the minimal mass difference between SM Higgs mass, i.e. minimize this

$$\chi^2 = [M(j_1 j_2) - M_{\rm H}]^2 + [M(j_3 j_4) - M_{\rm H}]^2 + [M(j_5 j_6) - M_{\rm H}]^2$$
(6)

where $M(j_i j_j)$ means the invariant mass of jet i and jet j.

Testing samples are required with ≥ 0 b-jets and b-tagging efficiency: default. The results are presented in Table 18.

Table 18: Performance comparison for tri-Higgs events. The results are for complete events (3 Higgs).

| | Event | SPANet Efficiency | | χ^2 Efficiency | |
|--------------|----------|-------------------|-------|---------------------|-------|
| $N_{ m Jet}$ | Fraction | Event | Higgs | Event | Higgs |
| =6 | 0.062 | 0.580 | 0.689 | 0.515 | 0.559 |
| =7 | 0.076 | 0.382 | 0.596 | 0.178 | 0.228 |
| ≥ 8 | 0.081 | 0.238 | 0.465 | 0.043 | 0.133 |
| Total | 0.291 | 0.384 | 0.564 | 0.223 | 0.303 |

Below, only consider the permutation of b-tagged jets. Testing events are required with ≥ 6 b-jets. The results are presented in Table 19 and Table 20.

21 SPANet for di-Higgs events with b-tag

In this section, SPANet will take the b-tagging information.

The .ini file for the di-Higgs event

Table 19: Performance comparison for tri-Higgs events with ≥ 6 b-jets (b-tagging efficiency = 100%). The results are for complete events (3 Higgs).

| | Event | SPANet Efficiency | | χ^2 Efficiency | |
|--------------|----------|-------------------|-------|---------------------|-------|
| $N_{ m Jet}$ | Fraction | Event | Higgs | Event | Higgs |
| =6 | 0.150 | 0.633 | 0.729 | 0.517 | 0.560 |
| =7 | 0.183 | 0.550 | 0.675 | 0.459 | 0.512 |
| ≥ 8 | 0.196 | 0.443 | 0.597 | 0.363 | 0.425 |
| Total | 0.529 | 0.534 | 0.662 | 0.440 | 0.494 |

Table 20: Performance comparison for tri-Higgs events with ≥ 6 b-jets (b-tagging efficiency = default). The results are for complete events (3 Higgs).

| | Event | SPANet Efficiency | | χ^2 Efficiency | |
|--------------|----------|-------------------|-------|---------------------|-------|
| $N_{ m Jet}$ | Fraction | Event | Higgs | Event | Higgs |
| = 6 | 0.100 | 0.488 | 0.613 | 0.484 | 0.535 |
| =7 | 0.175 | 0.329 | 0.502 | 0.347 | 0.413 |
| ≥ 8 | 0.257 | 0.185 | 0.394 | 0.173 | 0.254 |
| Total | 0.532 | 0.290 | 0.417 | 0.289 | 0.359 |

[SOURCE]

```
mass = log_normalize
pt = log_normalize
eta = normalize
phi = normalize
btag = none
```

[EVENT]

```
particles = (h1, h2)
permutations = [(h1, h2)]
```

[h1]

[h2] jets = (b1, b2)

permutations = [(b1, b2)]

For training data preparation is almost the same in Sec.18.1. 2 b-tagged jets or 4 b-tagged jets will be required in the following training data. The default b-tagging efficiency in Delphes is

eff. =
$$0.85 \tanh(0.0025p_{\rm T}) \frac{25.0}{1 + 0.063p_{\rm T}}$$
 (7)

21.1 Training result for di-Higgs event

Case 1: ≥ 0 b-tagged jets, b-tagging efficiency: 100%

- Training sample:
 - Total sample size: 788,108
 - 1h sample size: 357,082
 - 2h sample size: 364,717
 - -5% used on validation
- Testing sample:
 - Total sample size: 87,748
 - 1h sample size: 39,816
 - 2h sample size: 40,635

The training results for Case 1 is presented in Table 21.

Table 21: SPA-NET results on di-Higgs with at least 0 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| =4 | 0.224 | 1.000 | 1.000 |
| =5 | 0.333 | 0.981 | 0.990 |
| ≥ 6 | 0.443 | 0.948 | 0.973 |
| Total | 1.000 | 0.970 | 0.985 |

Case 2: ≥ 2 b-tagged jets, b-tagging efficiency: 100%

• Training sample:

- Total sample size: 787,097

- 1h sample size: 357,078

- 2h sample size: 364,717

- 5% used on validation

• Testing sample:

- Total sample size: 87,641

- 1h sample size: 39,816

- 2h sample size: 40,635

The training results for Case 2 is presented in Table 22.

Table 22: SPA-NET results on di-Higgs with at least 2 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 4 | 0.224 | 1.000 | 1.000 |
| =5 | 0.333 | 0.984 | 0.992 |
| ≥ 6 | 0.443 | 0.953 | 0.976 |
| Total | 1.000 | 0.974 | 0.987 |

Case 3: ≥ 4 b-tagged jets, b-tagging efficiency: 100%

• Training sample:

- Total sample size: 454,768

- 1h sample size: 85,074

- 2h sample size: 363,904

- 5% used on validation

• Testing sample:

- Total sample size: 50,735

- 1h sample size: 9,547

- 2h sample size: 40,541

The training results for Case 3 is presented in Table 23.

Table 23: SPA-NET results on di-Higgs with at least 4 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 4 | 0.224 | 1.000 | 1.000 |
| =5 | 0.333 | 0.980 | 0.990 |
| ≥ 6 | 0.443 | 0.946 | 0.972 |
| Total | 1.000 | 0.969 | 0.984 |

Case 4: ≥ 0 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 788,160

- 1h sample size: 357,137

- 2h sample size: 364,773

- 5% used on validation

• Testing sample:

- Total sample size: 87,702

- 1h sample size: 39,659

- 2h sample size: 40,695

The training results for Case 4 is presented in Table 24.

Case 5: ≥ 2 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 633,726

- 1h sample size: 270,325

- 2h sample size: 328,427

Table 24: SPA-NET results on di-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default)

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 4 | 0.224 | 1.000 | 1.000 |
| =5 | 0.334 | 0.961 | 0.981 |
| ≥ 6 | 0.442 | 0.887 | 0.941 |
| Total | 1.000 | 0.937 | 0.968 |

-5% used on validation

• Testing sample:

- Total sample size: 70,436

- 1h sample size: 29,847

- 2h sample size: 36,742

The training results for Case 5 is presented in Table 25.

Table 25: SPA-NET results on di-Higgs with at least 2 b-tagged jets (b-tagging efficiency: default)

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 4 | 0.223 | 1.000 | 1.000 |
| =5 | 0.332 | 0.964 | 0.982 |
| ≥ 6 | 0.445 | 0.891 | 0.943 |
| Total | 1.000 | 0.939 | 0.969 |

Case 6: ≥ 4 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 108,266

- 1h sample size: 19,808

- 2h sample size: 87,196

- 5% used on validation

• Testing sample:

- Total sample size: 11,992

- 1h sample size: 2,205

- 2h sample size: 9,643

The training results for Case 6 is presented in Table 26.

Table 26: SPA-NET results on di-Higgs with at least 4 b-tagged jets (b-tagging efficiency: default)

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 4 | 0.200 | 1.000 | 1.000 |
| =5 | 0.318 | 0.950 | 0.975 |
| ≥ 6 | 0.482 | 0.865 | 0.930 |
| Total | 1.000 | 0.919 | 0.958 |

Table 27 is the summary for b-tag training results.

Table 27: Summary for b-tag training results. 2b means at least 2 b-tagged jets. 100% and default are the b-tagging efficiency in Delphes.

| Case | Event Efficiency | Higgs Efficiency | Testing sample |
|--------------------|--------------------|--------------------|----------------|
| no b-tag | 0.914 ± 0.0014 | 0.955 ± 0.0007 | 40,695 |
| ≥ 0 b 100% | 0.970 ± 0.0008 | 0.985 ± 0.0004 | 40,635 |
| ≥ 2 b 100% | 0.974 ± 0.0008 | 0.987 ± 0.0004 | 40,635 |
| ≥ 4 b 100% | 0.969 ± 0.0009 | 0.984 ± 0.0004 | 40,541 |
| ≥ 0 b default | 0.937 ± 0.0012 | 0.968 ± 0.0006 | 40,695 |
| ≥ 2 b default | 0.939 ± 0.0012 | 0.969 ± 0.0006 | 36,742 |
| ≥ 4 b default | 0.919 ± 0.0028 | 0.958 ± 0.0014 | 9,643 |

22 SPANet for tri-Higgs events with b-tag

The .ini file for the tri-Higgs event

[SOURCE]

mass = log normalize

pt = log_normalize

eta = normalize

```
phi = normalize
btag = none

[EVENT]
particles = (h1, h2, h3)
permutations = [(h1, h2, h3)]

[h1]
jets = (b1, b2)
permutations = [(b1, b2)]

[h2]
jets = (b1, b2)
permutations = [(b1, b2)]

[h3]
jets = (b1, b2)
permutations = [(b1, b2)]
```

22.1 Training sample preparation for tri-Higgs events

Tri-Higgs events gg->hhh was generated at $\sqrt{s} = 14$ TeV using MadGraph. Then pass these events to Pythia8 for showering and hadronization. In Pythia8, the Higgs is forced to decay to $b\bar{b}$. Then pass to Delphes for detector simulation.

Jets are reconstructed by the anti-kT algorithm with radius R=0.4 and are required to have $p_{\rm T}\geq 20$ GeV.

Preselection requirements: ≥ 6 jets in $|\eta| < 2.5$.

Define the correct jet assignments by matching them to the simulated truth quarks within an angular distance of $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} < 0.4$.

22.2 Trainging result for tri-Higgs events

In all cases, partial event training is set to true.

Case 1: ≥ 0 b-tagged jets, b-tagging efficiency: 100%

• Training sample:

- Total sample size: 519,372

- 1h sample size: 168,385

- 2h sample size: 175,616

- 3h sample size: 112,770

- 5% used on validation

• Testing sample:

- Total sample size: 57,652

- 1h sample size: 18,639

- 2h sample size: 19,456

- 3h sample size: 12,679

The training results for Case 1 is presented in Table 28.

Table 28: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.062 | 0.608 | 0.711 |
| =7 | 0.076 | 0.519 | 0.652 |
| ≥ 8 | 0.081 | 0.426 | 0.584 |
| Total | 0.220 | 0.510 | 0.644 |

Case 2: ≥ 2 b-tagged jets, b-tagging efficiency: 100%

• Training sample:

- Total sample size: 519,318

- 1h sample size: 168,385

- 2h sample size: 175,616

- 3h sample size: 112,770

- 5% used on validation

• Testing sample:

- Total sample size: 57,646

- 1h sample size: 18,639

- 2h sample size: 19,456

- 3h sample size: 12,679

The training results for Case 2 is presented in Table 29.

Table 29: SPA-NET results on tri-Higgs with at least 2 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.063 | 0.637 | 0.732 |
| =7 | 0.076 | 0.556 | 0.679 |
| ≥ 8 | 0.081 | 0.442 | 0.601 |
| Total | 0.220 | 0.537 | 0.665 |

Case 3: ≥ 4 b-tagged jets, b-tagging efficiency: 100%

• Training sample:

- Total sample size: 503,404

- 1h sample size: 164,104

- 2h sample size: 175,572

- 3h sample size: 112,770

- 5% used on validation

• Testing sample:

- Total sample size: 55,989

- 1h sample size: 18,197

- 2h sample size: 19,454

- 3h sample size: 12,679

The training results for Case 3 is presented in Table 30.

Table 30: SPA-NET results on tri-Higgs with at least 4 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.064 | 0.635 | 0.732 |
| =7 | 0.079 | 0.563 | 0.684 |
| ≥ 8 | 0.084 | 0.443 | 0.602 |
| Total | 0.226 | 0.539 | 0.668 |

Case 4: ≥ 6 b-tagged jets, b-tagging efficiency: 100%

- Total sample size: 212,885

- 1h sample size: 5,349

- 2h sample size: 33,675

- 3h sample size: 112,330

- 5% used on validation

• Testing sample:

- Total sample size: 23,886

- 1h sample size: 3,853

- 2h sample size: 6,804

- 3h sample size: 12,639

The training results for Case 4 is presented in Table 31.

Table 31: SPA-NET results on tri-Higgs with at least 6 b-tagged jets (b-tagging efficiency: 100%).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.150 | 0.633 | 0.729 |
| =7 | 0.183 | 0.550 | 0.675 |
| ≥ 8 | 0.196 | 0.443 | 0.597 |
| Total | 0.529 | 0.534 | 0.662 |

Case 5: ≥ 0 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 519,404

- 1h sample size: 168,781

- 2h sample size: 175,235

- 3h sample size: 112,740

- 5% used on validation

• Testing sample:

- Total sample size: 57,744

- 1h sample size: 18,447

- 2h sample size: 19,572

- 3h sample size: 12,655

The training results for Case 5 is presented in Table 32.

Table 32: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.062 | 0.580 | 0.689 |
| =7 | 0.076 | 0.382 | 0.569 |
| ≥ 8 | 0.081 | 0.238 | 0.465 |
| Total | 0.219 | 0.384 | 0.564 |

Case 6: ≥ 2 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 486,815

- 1h sample size: 155,932

- 2h sample size: 166,234

- 3h sample size: 109,947

- 5% used on validation

• Testing sample:

- Total sample size: 54,132

- 1h sample size: 17,102

- 2h sample size: 18,522

- 3h sample size: 12,321

The training results for Case 6 is presented in Table 33.

Table 33: SPA-NET results on tri-Higgs with at least 2 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.064 | 0.575 | 0.683 |
| =7 | 0.079 | 0.386 | 0.573 |
| ≥ 8 | 0.085 | 0.236 | 0.460 |
| Total | 0.228 | 0.383 | 0.562 |

Case 7: ≥ 4 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 238,155

- 1h sample size: 16,272

- 2h sample size: 65,770

- 3h sample size: 72,441

- 5% used on validation

• Testing sample:

- Total sample size: 26,561

- 1h sample size: 7,261

- 2h sample size: 9,300

- 3h sample size: 8,124

The training results for Case 7 is presented in Table 34.

Table 34: SPA-NET results on tri-Higgs with at least 4 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.081 | 0.553 | 0.668 |
| =7 | 0.105 | 0.373 | 0.559 |
| ≥ 8 | 0.120 | 0.236 | 0.460 |
| Total | 0.306 | 0.367 | 0.549 |

Case 8: ≥ 6 b-tagged jets, b-tagging efficiency: default

- Total sample size: 20,335

- 1h sample size: 3,300

- 2h sample size: 5,639

- 3h sample size: 10,840

- 5% used on validation

• Testing sample:

- Total sample size: 2,166

- 1h sample size: 357

- 2h sample size: 592

- 3h sample size: 1,153

The training results for Case 8 is presented in Table 35.

Table 35: SPA-NET results on tri-Higgs with at least 6 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.100 | 0.488 | 0.613 |
| =7 | 0.175 | 0.329 | 0.502 |
| ≥ 8 | 0.257 | 0.185 | 0.394 |
| Total | 0.532 | 0.290 | 0.417 |

Case 9: Without b-tagging information.

• Training sample:

- Total sample size: 519,404

- 1h sample size: 168,781

- 2h sample size: 175,235

- 3h sample size: 112,740

- 5% used on validation

• Testing sample:

- Total sample size: 57,744

- 1h sample size: 18,447

- 2h sample size: 19,572

- 3h sample size: 12,655

The training results for Case 9 is presented in Table 36.

Table 36: SPA-NET results on tri-Higgs without b-tagging information.

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.062 | 0.600 | 0.703 |
| =7 | 0.076 | 0.343 | 0.557 |
| ≥ 8 | 0.081 | 0.172 | 0.415 |
| Total | 0.219 | 0.351 | 0.545 |

Case 10: ≥ 6 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 200,020

- 1h sample size: 32,269

- 2h sample size: 55,500

- 3h sample size: 106,820

- 5% used on validation

• Testing sample:

- Total sample size: 22,351

- 1h sample size: 3,639

- 2h sample size: 6,161

- 3h sample size: 11,908

The training results for Case 10 is presented in Table 37.

Table 37: SPA-NET results on tri-Higgs with at least 6 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.099 | 0.631 | 0.729 |
| =7 | 0.164 | 0.435 | 0.604 |
| ≥ 8 | 0.269 | 0.272 | 0.481 |
| Total | 0.533 | 0.389 | 0.565 |

Case 11: ≥ 0 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 2,597,986

- 1h sample size: 842,297

- 2h sample size: 877,590

- 3h sample size: 564,989

- 5% used on validation

• Testing sample:

- Total sample size: 289,131

- 1h sample size: 93,303

- 2h sample size: 98,004

- 3h sample size: 62,944

The training results for Case 11 is presented in Table 38.

Table 38: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.060 | 0.642 | 0.735 |
| =7 | 0.075 | 0.445 | 0.619 |
| ≥ 8 | 0.081 | 0.293 | 0.511 |
| Total | 0.218 | 0.443 | 0.611 |

Case 12: ≥ 0 b-tagged jets, b-tagging efficiency: default

- Total sample size: $5{,}194{,}850$

- 1h sample size: 1,681,832

- 2h sample size: 1,754,176

- 3h sample size: 1,132,044

- 5% used on validation

• Testing sample:

- Total sample size: 578,248

- 1h sample size: 186,731

- 2h sample size: 195,461

- 3h sample size: 126,154

The training results for Case 12 is presented in Table 39.

Table 39: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.061 | 0.669 | 0.755 |
| =7 | 0.075 | 0.478 | 0.643 |
| ≥ 8 | 0.082 | 0.322 | 0.531 |
| Total | 0.218 | 0.473 | 0.632 |

Case 13: ≥ 0 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 1,558,455

- 1h sample size: 505,734

- 2h sample size: 525,989

- 3h sample size: 339,012

- 5% used on validation

• Testing sample:

- Total sample size: 173,474

- 1h sample size: 55,738

- 2h sample size: 58,879

- 3h sample size: 37,864

The training results for Case 13 is presented in Table 40.

Table 40: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.061 | 0.660 | 0.750 |
| =7 | 0.075 | 0.447 | 0.620 |
| ≥ 8 | 0.082 | 0.281 | 0.500 |
| Total | 0.218 | 0.444 | 0.611 |

Case 14: ≥ 0 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 3,636,395

- 1h sample size: 1,178,817

- 2h sample size: 1,227,899

- 3h sample size: 791,457

- 5% used on validation

• Testing sample:

- Total sample size: 404,773

- 1h sample size: 130,462

- 2h sample size: 136,786

- 3h sample size: 88,466

The training results for Case 14 is presented in Table 41.

Table 41: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| =6 | 0.061 | 0.685 | 0.767 |
| =7 | 0.075 | 0.462 | 0.634 |
| ≥ 8 | 0.082 | 0.301 | 0.516 |
| Total | 0.218 | 0.464 | 0.627 |

Case 15: ≥ 0 b-tagged jets, b-tagging efficiency: default

• Training sample:

- Total sample size: 7,791,375

- 1h sample size: 2,523,958

- 2h sample size: 2,629,911

- 3h sample size: 1,697,675

- 5% used on validation

• Testing sample:

- Total sample size: 866,656

- 1h sample size: 280,093

- 2h sample size: 293,008

- 3h sample size: 188,956

The training results for Case 15 is presented in Table 42.

Table 42: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.061 | 0.711 | 0.785 |
| =7 | 0.075 | 0.501 | 0.662 |
| ≥ 8 | 0.082 | 0.337 | 0.545 |
| Total | 0.218 | 0.497 | 0.652 |

Case 16: ≥ 0 b-tagged jets, b-tagging efficiency: default

- Total sample size: 10,388,500

- 1h sample size: 3,364,562

- 2h sample size: 3,507,744

- 3h sample size: 2,263,437

- 5% used on validation

• Testing sample:

- Total sample size: 1,155,542

- 1h sample size: 374,000

- 2h sample size: 390,507

- 3h sample size: 251,870

The training results for Case 16 is presented in Table 43.

Table 43: SPA-NET results on tri-Higgs with at least 0 b-tagged jets (b-tagging efficiency: default).

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.061 | 0.718 | 0.790 |
| =7 | 0.075 | 0.510 | 0.666 |
| ≥ 8 | 0.082 | 0.344 | 0.550 |
| Total | 0.218 | 0.505 | 0.656 |

Table 44 is the summary for tri-Higgs training results.

Figure 18 is the accuracy against 3h training sample size for 0b default case.

Table 44: Summary for tri-Higgs training results. Tagging eff. is the b-tagging efficiency in Delphes.

| Case | $N_{ m bjet}$ | Tagging eff. | Event Efficiency | Higgs Efficiency | Testing sample |
|------|---------------|--------------|--------------------|--------------------|----------------|
| 1 | ≥ 0 | 100% | 0.510 ± 0.0044 | 0.644 ± 0.0025 | 12,679 |
| 2 | ≥ 2 | 100% | 0.537 ± 0.0044 | 0.665 ± 0.0024 | 12,679 |
| 3 | ≥ 4 | 100% | 0.539 ± 0.0044 | 0.668 ± 0.0024 | 12,679 |
| 4 | ≥ 6 | 100% | 0.534 ± 0.0044 | 0.662 ± 0.0024 | 12,639 |
| 5 | ≥ 0 | default | 0.384 ± 0.0043 | 0.564 ± 0.0025 | 12,655 |
| 6 | ≥ 2 | default | 0.383 ± 0.0044 | 0.562 ± 0.0026 | 12,321 |
| 7 | ≥ 4 | default | 0.367 ± 0.0053 | 0.549 ± 0.0032 | 8,124 |
| 8 | ≥ 6 | default | 0.290 ± 0.0134 | 0.417 ± 0.0084 | 1,153 |
| 9 | N | lo b-tag | 0.351 ± 0.0042 | 0.545 ± 0.0026 | 12,655 |
| 10 | ≥ 6 | default | 0.389 ± 0.0045 | 0.565 ± 0.0026 | 11,908 |
| 11 | ≥ 0 | default | 0.443 ± 0.0020 | 0.611 ± 0.0011 | 62,944 |
| 12 | ≥ 0 | default | 0.473 ± 0.0014 | 0.632 ± 0.0008 | 126,154 |
| 13 | ≥ 0 | default | 0.444 ± 0.0026 | 0.611 ± 0.0014 | 37,864 |
| 14 | ≥ 0 | default | 0.464 ± 0.0017 | 0.627 ± 0.0009 | 88,466 |
| 15 | ≥ 0 | default | 0.497 ± 0.0012 | 0.652 ± 0.0006 | 188,956 |
| 16 | ≥ 0 | default | 0.505 ± 0.0010 | 0.656 ± 0.0005 | 251,870 |
| 17 | ≥ 0 | default | 0.508 ± 0.0008 | 0.660 ± 0.0004 | 377,960 |

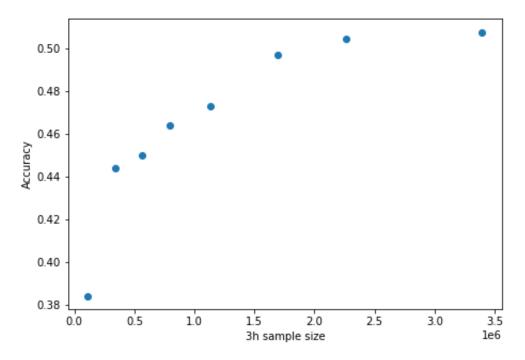


Figure 18: The accuracy against 3h training sample size.

22.3 Training curve

Figure 19 and 20 are the training curves for Case 9. After 50 epochs, the validation accuracy has not improved much.

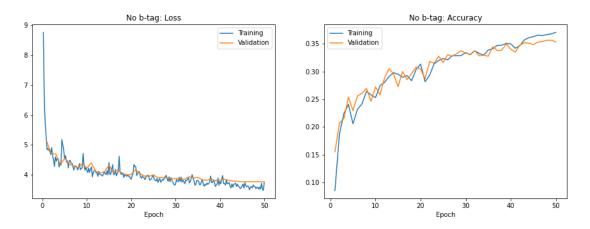


Figure 19: The 50 epoch training curves for Case 9.

Figure 21 is the training curves for Case 10.

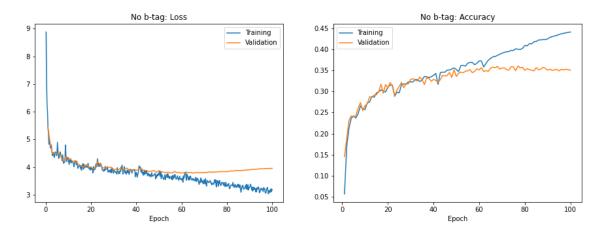


Figure 20: The 100 epoch training curves for Case 9.

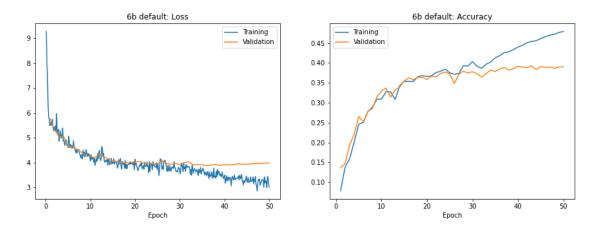


Figure 21: The training curves for Case 10 (6b default).

22.4 Test on different dataset

For example, use Case 5 samples for training and test on Case 5, 6, 7, and 8 samples. The results are presented in Table 45.

| Table 45: 0b SPANet test on different samp | ples. |
|--|-------|
|--|-------|

| Training samples | Testing samples | Event efficiency | Higgs efficiency |
|------------------|-----------------|------------------|------------------|
| 0b default | 0b default | 0.386 | 0.567 |
| 0b default | 2b default | 0.387 | 0.568 |
| 0b default | 4b default | 0.391 | 0.571 |
| 0b default | 6b default | 0.366 | 0.550 |

Use Case 6 samples for training and test on Case 5, 6, 7, and 8 samples. The results are presented in Table 46.

Table 46: 2b SPANet test on different samples.

| Training samples | Testing samples | Event efficiency | Higgs efficiency |
|------------------|-----------------|------------------|------------------|
| 2b default | 0b default | 0.383 | 0.562 |
| 2b default | 2b default | 0.383 | 0.562 |
| 2b default | 4b default | 0.388 | 0.565 |
| 2b default | 6b default | 0.363 | 0.548 |

Use Case 7 samples for training and test on Case 5, 6, 7, and 8 samples. The results are presented in Table 47.

Table 47: 4b SPANet test on different samples.

| Training samples | Testing samples | Event efficiency | Higgs efficiency |
|------------------|-----------------|------------------|------------------|
| 4b default | 0b default | 0.356 | 0.540 |
| 4b default | 2b default | 0.358 | 0.542 |
| 4b default | 4b default | 0.367 | 0.549 |
| 4b default | 6b default | 0.355 | 0.536 |

Use Case 10 samples for training and test on Case 5, 6, 7, and 8 samples. The results are presented in Table 48.

Use Case 12 samples for training and test on Case 6, 7, 10, and 12 samples. The results are presented in Table 49.

Table 48: 6b SPANet test on different samples.

| Training samples | Testing samples | Event efficiency | Higgs efficiency |
|------------------|-----------------|------------------|------------------|
| 6b default | 0b default | 0.230 | 0.412 |
| 6b default | 2b default | 0.234 | 0.417 |
| 6b default | 4b default | 0.290 | 0.476 |
| 6b default | 6b default | 0.385 | 0.559 |

Table 49: 0b SPANet test on different samples.

| Training samples | Testing samples | Event efficiency | Higgs efficiency |
|------------------|-----------------|------------------|------------------|
| 0b default | 0b default | 0.473 | 0.632 |
| 0b default | 2b default | 0.475 | 0.634 |
| 0b default | 4b default | 0.479 | 0.636 |
| 0b default | 6b default | 0.457 | 0.623 |

Table 50: SPANet trained on 0b test on 6b.

| $N_{ m Jet}$ | Event Fraction | Event Efficiency | Higgs Efficiency |
|--------------|----------------|------------------|------------------|
| = 6 | 0.099 | 0.713 | 0.788 |
| =7 | 0.164 | 0.508 | 0.663 |
| ≥ 8 | 0.269 | 0.331 | 0.538 |
| Total | 0.533 | 0.457 | 0.623 |

23 Hyperparameters

Some hyperparameters of SPANet:

• Learning rate: 0.0004

• Central encoder count: 6

• Branch encoder count: 3

• Dropout percentage: 0.0

• L2 weight normalization: 0.0002

• L2 gradient clipping: 0.0

the above values are used in Sec.22.

23.1 Scan hyperparameters

In below, use the 0b default samples (Sec. 22.2, Case 5) for hyperparameter scan.

Learning rate Range: [0.0003, 0.0030]. Step size: 0.0003. Figure 22 is the scanning results. When the learning rate is greater than 0.0006 the model can not be trained.

Central encoder count Range: [2,6]. Step size: 1. Figure 23 is the scanning results. When central encoder layers are equal to 2 or 4, the model will get the best performance at the first 10 epochs.

Branch encoder count Range: [2,7]. Step size: 1. Figure 24 is the scanning results. When branch encoder layers equal 2 or 4, the model will get the best performance at the first 10 epochs.

23.2 Training results for different hyperparamers

In this section, use the 0b default samples (Sec.22.2, Case 5) for training. Train 50 epochs. Table 51 is the training results for different hyperparameters.

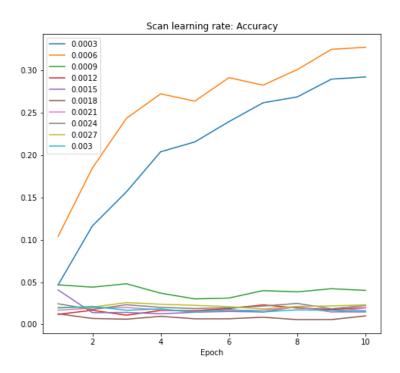


Figure 22: SPANet training results for different learning rates.

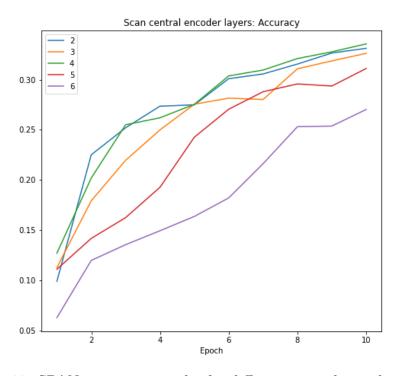


Figure 23: SPANet training results for different central encoder layers.

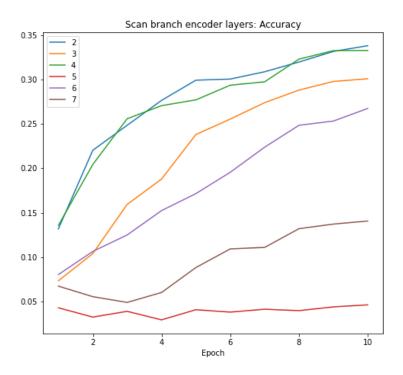


Figure 24: SPANet training results for different branch encoder layers.

Table 51: SPANet training results for different hyperparameters.

| Central encoder | Branch encoder | learning rate | Event efficiency | Higgs efficiency |
|-----------------|----------------|---------------|------------------|------------------|
| 6 | 3 | 0.0004 | 0.386 | 0.567 |
| 2 | 2 | 0.0006 | 0.395 | 0.571 |
| 4 | 4 | 0.0006 | 0.362 | 0.547 |
| 4 | 2 | 0.0006 | 0.386 | 0.567 |

24 Signal and background

To separate the signal and background events, defined the cuts as follows:

- Eta PT cut: In $|\eta| < 2.5$ there are ≥ 6 jets. The p_T of jets are required over 25 GeV.
- bTag cut: ≥ 6 b-jets.
- PT cut: Require 4 jets over 40 GeV.
- inv mass cut: The total invariant mass of 6 b-jets ≤ 500 GeV.

The result is in Table 52.

Table 52: The cross sections for the signal and background processes at different cuts. $\mathcal{L} = 139 \text{ fb}^{-1}$ is provided.

| | Cross section (pb) | | | |
|--------------|--------------------|------------|----------|--------------|
| | Signal | Background | S/B | S/\sqrt{B} |
| No cut | 0.0118 | 7.18e + 02 | 1.64e-05 | 0.164 |
| Eta PT cut | 0.00619 | 29.6 | 0.000209 | 0.424 |
| bTag cut | 0.00199 | 0.711 | 0.0028 | 0.881 |
| PT cut | 0.00164 | 0.503 | 0.00326 | 0.86 |
| inv mass cut | 0.0013 | 0.129 | 0.01 | 1.34 |