Note

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1 Signal

We consider a simple extension of the standard model (SM) [1], which includes a vectorlike dark fermion ($\overline{\chi}$, χ) and a complex singlet scalar S. A signature of CP violation could come from the Higgs-to-Higgs decays, $h_3 \to h_2 h_1$, where $h_3/h_2/h_1$ are the heaviest scalar, second heaviest scalar, and the SM-like 125 GeV Higgs, respectively.

The signal process is the triple production of 125 GeV Higgs bosons via the gluon fusion:

$$gg \rightarrow h_3 \rightarrow h_2 h_1 \rightarrow h_1 h_1 h_1$$

The Higgs boson h_1 would further decay to the $b\bar{b}$ pair. We consider the banchmark point 1 (BP1), where $m_{h_3}=450$ GeV, $m_{h_2}=280$ GeV, $m_{h_1}=125$ GeV. This process is generated at $\sqrt{s}=13$ TeV. Following are the MadGraph scripts for generating signal samples:

```
import model cxSM_VLF_EFT
generate g g > h h h
output MG5/gghhh_bsm
launch MG5/gghhh_bsm
```

```
shower=Pythia8
detector=Delphes
analysis=OFF
madspin=ON
done
```

```
set param_card mh1 125
set param_card mh2 280
set param_card mh3 420
set param_card theta12 0.73
```

```
set param card theta13 1.67079632679
set param_card theta23 -0.73
set param card vs 200
set param card delta2 0
set param card Rdelta3 0
set param card Idelta3 -3.5
set param card b2 0
set param_card Rc1 0
set param_card Ic1 0
set param_card Rc2 0
set param card Ic2 0
set param card Rd3 0
set param card Id3 0
set param card msq -5033.406281907266
set param card lam 0.13850082540690806
set param card Rdelta1 -47.561525227572744
set param card Idelta1 853.05384671134
set param card Rb1 -70476.6380004269
set param_card Ib1 -30486.140015405872
set param card Rd1 -2.562109886826132
set param card Id1 2.257859679994403
set param_card d2 6.340799300844676
set param_card gh1ggr -0.00005478952893059635
set param_card gh1gagar -0.00003270447254456052
set param_card gh1Zgar -0.00005871986046374793
set param card gh2ggr -1.4279972541632635e-7
set param_card gh2gagar -8.237715486808595e-8
set param card gh2Zgar -1.3984990232267825e-7
set param card gh3ggr -6.031835872118092e-6
set param card gh3gagar -1.1377279177203616e-6
set param card gh3Zgar -2.2999597941282603e-6
set param_card decay 102 auto
set param_card decay 103 auto
set run card nevents 100000
```

```
set run_card ebeam1 6500.0
set run_card ebeam2 6500.0
set run_card ptb 24
set run_card etab 2.6
set spinmode none
decay h > b b~
```

2 SPANet pairing

done

We employ the novel neural network structure SPA-NET [2, 3, 4] to identify the correct pairings among the jets in the final states.

2.1 Training dataset preparation

Preselection: ≥ 6 jets with transverse momentum $p_T \geq 25$ GeV in range $|\eta| < 2.5$.

The input features for the SPA-NET are a list of jets, each represented by its 4-component vector (p_T, η, ϕ, m) as well as a boolean b-tag. We only keep each event's 15 highest p_T jets. We define the correct jet assignments for each event by matching the jets to the simulated truth quarks within an angular distance of $\Delta R < 0.4$. Such an event will be dropped if a simulated truth quark is matched to more than one jet. Furthermore, some simulated truth quarks may not be matched to any jet, so the event will not be used in training either.

After the selection and matching, we could obtain the following results from 1M events:

• Total sample size: 522,899

• 1h sample size: 184,769

• 2h sample size: 161,476

• 3h sample size: 94,464

Here, the 1h sample is where we could define the correct jet assignments for 1 Higgs boson.

2.2 Training results

• Training sample:

- Total sample size: 470,609

- 1h sample size: 166,490

- 2h sample size: 145,309

- 3h sample size: 84,913

- 5% used on validation

• Testing sample:

- Total sample size: 52,290

- 1h sample size: 18,279

- 2h sample size: 16,167

- 3h sample size: 9,551

Some useful definitions for evaluating jet assignment performance:

• Event Efficiency

$$\epsilon^{\text{event}} \equiv \frac{\text{number of events with and all Higgs are correctly identified}}{\text{number of events}}$$
(1)

Higgs Efficiency

$$\epsilon^{\rm h} \equiv \frac{\text{number of correctly identified Higgs}}{\text{number of identifiable Higgs}}$$
(2)

The training results are shown in Table 1.

Table 1: Spa-Net pairing efficiencies on 3h events.

$N_{ m Jet}$	Event Fraction	Event Efficiency	Higgs Efficiency
= 6	0.077	0.532	0.650
=7	0.057	0.345	0.536
≥ 8	0.052	0.237	0.452
Total	0.186	0.375	0.548

3 χ^2 pairing

 χ^2 method considers all possible combinations of final jets and selects the configuration that minimizes the mass difference between Higgs candidates and SM Higgs, i.e., minimizes this:

$$\chi^2 = [m(j_1 j_2) - m_h]^2 + [m(j_3 j_4) - m_h]^2 + [m(j_5 j_6) - m_h]^2$$
(3)

where $m(j_i j_j)$ is the invariant mass of jet i, j and $m_h = 125$ GeV.

Table 2 is the performance of the χ^2 method.

Event Fraction Event Efficiency Higgs Efficiency 0.0770.4030.450=70.0570.1580.281 ≥ 8 0.0520.0000.077Total 0.1860.2150.294

Table 2: χ^2 pairing efficiencies on 3h events.

4 Estimate cross-section of background process

Besides the 6 b background, we need to consider the backgrounds that come from the mis-tagging of light jets or charm-jets to b-jets. We assume that the probability of a charm-jet being misidentified as b-jet is $\mathcal{P}_{c\to b} = 0.1$ and that of light jets is $\mathcal{P}_{j\to b} = 0.01$. The b-tagging efficiency is assumed to be $\mathcal{P}_{b\to b} = 0.7$.

Table 3 shows the cross-section computed from MadGraph and the cross-section times the mis-tagging probabilities $\mathcal{P}_{c\to b}$ and $\mathcal{P}_{j\to b}$. Table 4 shows the same results with kinetic cuts. We require the transverse momentum $p_{\rm T}$ of each jet greater than 24 GeV and in the range $|\eta| < 2.6$ at the MadGraph level. The 6b process contributes much more than the processes containing charm jets and light jets.

5 Compute pairing efficiency

To understand the pairing performance with different pairing methods, we compute how many events where 1h/2h/3h bosons are reconstructed correctly.

The pairing performance of SPA-NET are shown in Table 5. Table 6 is the performance of the χ^2 method. For both cases, we found the number of events where only two Higgs are

Table 3: The cross-sections of 6b and mis-tagging background processes. The cross-sections are computed from the MadGraph at $\sqrt{s} = 13$ TeV.

process	σ (pb)	$\sigma \times \mathcal{P}(\text{tagging efficiency}) \text{ (pb)}$
$(b\overline{b})(b\overline{b})(b\overline{b})$	2.53×10^3	2.97×10^{2}
$(b\overline{b})(b\overline{b})(c\overline{c})$	2.72×10^{2}	6.54×10^{-1}
$(b\overline{b})(c\overline{c})(c\overline{c})$	3.73×10^{1}	1.83×10^{-3}
$(b\overline{b})(b\overline{b})(jj)$	7.44×10^4	1.79

Table 4: The cross-sections of 6b and mis-tagging background processes. The cross-sections are computed from the MadGraph at $\sqrt{s} = 13$ TeV. We require the transverse momentum $p_{\rm T}$ of each jets greater than 24 GeV in range $|\eta| < 2.6$.

process	σ (fb)	$\sigma \times \mathcal{P}(\text{tagging efficiency}) \text{ (fb)}$
$(b\overline{b})(b\overline{b})(b\overline{b})$	9.63×10^{2}	113.35
$(b\overline{b})(b\overline{b})(c\overline{c})$	1.67×10^{3}	4.02
$(b\overline{b})(c\overline{c})(c\overline{c})$	1.06×10^{3}	5.19×10^{-2}
$(b\overline{b})(b\overline{b})(jj)$	4.16×10^{5}	9.98
$(b\overline{b})(jj)(jj)$	1.50×10^{7}	7.73×10^{-2}

paired correctly is tiny, which means if we can pair two Higgs bosons correctly, then we have a high chance to pair the final Higgs correctly.

Note that Higgs Efficiencies of SPA-NET are inconsistent with Table 1. This issue needs more checking.

Table 5: Spa-Net pairing efficiencies on different categories.

	Correc	etly reco			
$N_{ m Jet}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.532	0.000	0.119	0.348	0.572
=7	0.345	0.021	0.166	0.469	0.414
≥ 8	0.237	0.022	0.186	0.554	0.314
Total	0.375	0.014	0.156	0.455	0.436

Table 6: χ^2 pairing efficiencies on different categories.

	Correc	etly reco			
$\overline{N_{ m Jet}}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.403	0.000	0.143	0.455	0.450
=7	0.158	0.070	0.228	0.544	0.281
≥ 8	0.000	0.000	0.231	0.769	0.077
Total	0.215	0.022	0.194	0.570	0.294

6 SPANet pairing and classification

We train a SPA-NET to identify the correct pairings and perform the signal/background classification at the same time.

6.1 Training dataset

The selection and matching process for the jet pairing is the same as Section 2.1. We prepare the signal and background samples of the same size for classification.

For the jet assignment part,

• Training sample:

- Total sample size: 1,800,000

- 1h sample size: 318,053

- 2h sample size: 277,876

- 3h sample size: 162,444

- 5% used on validation

• Testing sample:

- Total sample size: 200,000

- 1h sample size: 35,372

- 2h sample size: 30,853

- 3h sample size: 18,004

For event classification,

• Training sample:

- Total sample size: 1,800,000

- Signal sample size: 900,000

- Background sample size: 900,000

- 5% used on validation

• Testing sample:

- Total sample size: 200,000

- Signal sample size: 100,000

- Background sample size: 100,000

This training takes around 10 hours on our server.

6.2 Training results

The training results are presented in Table 7. This result is better than Table 5 since we use larger training datasets.

Table 7: Spa-Net training results on the tri-Higgs samples. Spa-Net is trained on jet pairing and event classification tasks at the same time.

	Correc	etly reco			
$N_{ m Jet}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.656	0.000	0.082	0.262	0.684
=7	0.436	0.017	0.168	0.379	0.504
≥ 8	0.341	0.018	0.173	0.468	0.411
Total	0.478	0.012	0.142	0.368	0.533

Table 8 presents the classification training results. We use the accuracy (ACC) and the area under the Receiver Operating Characteristic (ROC) curve (AUC) as two metrics.

Table 8: The Spa-Net classification training results with tri-Higgs sample.

6.3 3h training dataset

We only consider 3h events in pairing tasks in this subsection. We prepare the signal and background samples of the same size for classification.

For the jet assignment part,

- Training sample:
 - Total sample size: 1,800,000
 - 1h sample size: 0
 - 2h sample size: 0
 - 3h sample size: 900,000
 - 5% used on validation
- Testing sample:
 - Total sample size: 200,000
 - 1h sample size: 0
 - 2h sample size: 0
 - 3h sample size: 100,000

For event classification,

- Training sample:
 - Total sample size: 1,800,000
 - Signal sample size: 900,000
 - Background sample size: 900,000
 - 5% used on validation
- Testing sample:
 - Total sample size: 200,000
 - Signal sample size: 100,000
 - Background sample size: 100,000

The training results are presented in Table 9. This result is similar to Table 7.

However, some issues should be resolved when we try to use all 3h events for combining training. The loss values are not reasonable.

Table 9: Spa-Net training results on the tri-Higgs samples, where we only consider 3h events. Spa-Net is trained on jet pairing and event classification tasks at the same time.

	Correc	etly reco			
$N_{ m Jet}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.680	0.000	0.084	0.236	0.708
=7	0.477	0.014	0.150	0.359	0.536
≥ 8	0.311	0.027	0.184	0.477	0.391
Total	0.491	0.014	0.139	0.356	0.547

7 Review the pairing methods

In Refs. [5, 6]: We select the 6 b-tagged jets with the highest transverse momentum. The requirements for the transverse momentum and pseudo-rapidity are applied. We subsequently make use of the observable:

$$\chi^{2,(6)} = \sum_{qr \in J} (m_{qr} - m_h)^2 \tag{4}$$

where $J = \{j_1j_2, j_3j_4, j_5j_6\}$ is the set of all possible 15 pairings of 6 b-tagged jets. Out of all the possible combinations we pick the one with the smallest value $\chi_{\min}^{2,(6)}$. The pairing of b-jets defining $\chi_{\min}^{2,(6)}$ is our best candidate for the reconstruction of the three Higgs bosons, h. No pairing efficiency is provided.

In Ref. [7]: We select the 6 b-tagged jets with the highest transverse momentum and form pairs in different combinations, with the aim of first reconstructing individual SM-like Higgs bosons, h_1 , and subsequently the two scalars h_2 and h_3 . To this end, we introduce two observables:

$$\chi^{2,(4)} = \sum_{qr \in I} (m_{qr} - m_h)^2 \tag{5}$$

$$\chi^{2,(6)} = \sum_{qr \in J} (m_{qr} - m_h)^2 \tag{6}$$

where we have defined the sets $I = \{i_1i_2, i_3i_4\}$ and $J = \{j_1j_2, j_3j_4, j_5j_6\}$, constructed from different pairings of 4 and 6 b-tagged jets, respectively, and where m_{qr} denotes the invariant mass of the respective pairing, qr. Note that the set I that defines $\chi_{\min}^{2,(4)}$ should be a subset of the arrangement J.

We select the combinations of b-tagged jets entering in I and J based on the minimization of the sum

$$\chi^{2,(4)} + \chi^{2,(6)} \tag{7}$$

We then "identify" candidates for the scalars h_2 and h_3 with the pairing configurations I_{\min} and J_{\min} which minimise $\chi^{2,(4)}$ and $\chi^{2,(6)}$ respectively. Note that this procedure does not guarantee that I_{\min} indeed reconstructs to h_2 ; in fact, we found this to be the case in about 40% on average for all benchmark samples, being slightly higher than a "blind guess" that would lead to a probability of 1/3.

8 6b requirement

They could utilize stronger kinetic and b-tagging requirements in experiments. However, we do not use the b-tag information for the previous χ^2 method. Thus, we change the preselection condition to make a fair comparison.

For testing samples, we only consider the event that contains at least 6 b-tagged jets. The Higgs Bosons are reconstructed by pairing the 6 leading b-jets for the χ^2 method. Thus, the best one is chosen from 15 possible pairing combinations.

Table 10 and Table 11 are the pairing performance on 6 b-tagged samples. The χ^2 method performs better than the previous results (Table 6) but still performs worse than the SPA-NET pairing.

Table 10: χ^2 pairing efficiencies on different categories. The χ^2 method only considers the 6 leading b-jets.

	Correc	etly reco			
$N_{ m Jet}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.500	0.000	0.124	0.376	0.541
=7	0.322	0.072	0.185	0.486	0.389
≥ 8	0.238	0.026	0.156	0.579	0.308
Total	0.329	0.013	0.159	0.499	0.391

9 Another pairing method

The pairing algorithm is defined to minimize

$$|m_{h_1} - 120| + |m_{h_2} - 115| + |m_{h_3} - 110| \tag{8}$$

where m_{h_i} is the mass of the *i*-th Higgs boson candidate (sorted by $p_{\rm T}$) in units of GeV. The numbers in this definition are chosen based on the peaks of the m_{h_i} distributions in simulated signal events.

Table 11: SPA-NET training results on the tri-Higgs samples, where we only consider 3h events. SPA-NET is trained on $\geq 0b$ datasets and tested on $\geq 6b$ datasets.

	Correc	etly reco			
$N_{ m Jet}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.679	0.000	0.074	0.246	0.704
=7	0.522	0.013	0.127	0.337	0.574
≥ 8	0.354	0.019	0.180	0.447	0.427
Total	0.492	0.013	0.136	0.359	0.546

Figure 1 is the Higgs boson invariant mass m_h distributions. The peaks of the m_h distributions in our simulation are 121, 119, 116 GeV. Based on these values we modify the numbers in Equation 8. Table 12 is the pairing performance on 6 b-tagged samples. The



Figure 1: The Higgs boson mass distributions. Here, we only consider the event containing at least 6 b-tagged jets.

absolute value method performs worse than the χ^2 method (Table 10).

Table 12: χ^2 pairing efficiencies on different categories. The χ^2 method only considers the 6 leading b-jets.

	Correc	etly reco			
$\overline{N_{ m Jet}}$	3h	2h	1h	0h	Higgs Efficiency
= 6	0.476	0.000	0.135	0.388	0.522
=7	0.293	0.011	0.185	0.511	0.362
≥ 8	0.215	0.026	0.168	0.589	0.289
Total	0.303	0.015	0.167	0.515	0.367

10 New simulation setting

We apply the new setting to the event generation to make a fair comparison. Following are the notes about the latest simulation setting.

The 6b analysis uses R = 0.4 anti- $k_{\rm T}$ jets. All jets are required to have $p_{\rm T} > 20$ GeV and $|\eta| < 2.5$, to be within the tracker acceptance for b-tagging.

All events must pass the Preselection. They must have at least six jets, defined by the earlier selection criteria. Of these 6 jets, at least 4 jets must have $p_T > 40$ GeV and at least 4 jets must be b-tagged.

Pairing is performed on all events passing the Preselection. In the case of 4b or 5b events, the 6 jets considered for pairing into Higgs candidates are the b-tagged jets and the extra jets are selected as the highest $p_{\rm T}$ of the remaining light-flavour jets. In the case of 6b events, the 6 jets are the 6 leading $p_{\rm T}$ b-tagged jets.

11 Pairing for new simulated samples

We modified the **Delphes** card to apply the anti- $k_{\rm T}$ clustering algorithm with R=0.4 and change the b-tagging efficiency to the ATLAS DL1r 77% working point. At this working point, the light-jet (charm-jet) rejection is about 130 (4.9).

Figure 2 is the Higgs boson invariant mass m_h distributions for new simulated samples. All events passing the Preselection and matching are used to generate this plot. The peaks of the m_h distributions in our simulation are 119, 115, 111 GeV. Based on these values we modify the numbers in Equation 8.

Table 13, 14 and 15 are the pairing performance on new simulated samples. The SPA-NET performs the best.

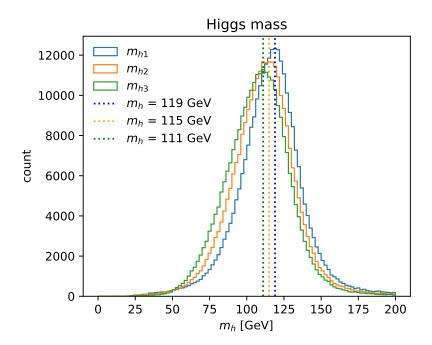


Figure 2: The Higgs boson mass distributions. Here, we consider all events passing the Preselection and the correct pairing can be obtained.

Table 13: χ^2 pairing efficiencies on different categories. We minimize the quantity defined in Equation 3. The χ^2 method considers the possible combinations of 6 jets.

		Correc	tly reco			
$N_{ m Jet}$	Fraction	3h	2h	1h	0h	Higgs Efficiency
= 6	0.241	0.519	0.000	0.112	0.368	0.557
=7	0.335	0.272	0.010	0.186	0.532	0.341
≥ 8	0.424	0.147	0.008	0.196	0.649	0.218
Total	1.000	0.279	0.007	0.172	0.542	0.341

Table 14: Absolute value pairing efficiencies on different categories. We minimize the quantity defined in Equation 8. The absolute value method considers the possible combination of 6 jets.

		Correc	etly reco			
$N_{ m Jet}$	Fraction	3h	2h	1h	0h	Higgs Efficiency
= 6	0.241	0.457	0.000	0.131	0.412	0.500
=7	0.335	0.239	0.009	0.184	0.568	0.306
≥ 8	0.424	0.136	0.007	0.197	0.661	0.206
Total	1.000	0.248	0.006	0.176	0.570	0.311

Table 15: SPA-NET training results on the tri-Higgs samples, where we only consider 3h events. The SPA-NET method considers all jets in the final state.

		Correc	etly reco			
$N_{ m Jet}$	Fraction	3h	2h	1h	0h	Higgs Efficiency
= 6	0.241	0.619	0.000	0.097	0.283	0.652
=7	0.335	0.481	0.008	0.150	0.361	0.536
≥ 8	0.424	0.350	0.011	0.171	0.469	0.414
Total	1.000	0.459	0.007	0.146	0.388	0.512

12 Modify the matching strategy

For the previous exercise, we define the correct jet assignments for each event by matching the jets to the simulated truth quarks within an angular distance of $\Delta R < 0.4$. Such an event will be dropped if a simulated truth quark is matched to more than one jet. Furthermore, some simulated truth quarks may not be matched to any jet, so the event will not be used in training either.

We modify our strategy for more than one jet case. If there are more than one jet can be matched to a simulated truth quark in the $\Delta R = 0.4$ cone, we choose the nearest one by the ΔR distance. This method is the same as the di-Higgs analysis [8].

Table 16 is the cutflow number at different selection cuts.

Table 16: The number of passing events, efficiencies, and passing rates for signal processes at different selection cuts.

	Count	Efficiency	Pass rate
Total	100000	1.00	1.00
$\geq 6 \text{ jets}$	61454	0.61	0.61
≥ 4 jets with $p_{\rm T} > 40$ GeV	50341	0.82	0.50
≥ 4 b-jets	32337	0.64	0.32
Matching 3h	9944	0.31	0.10
Matching 2h	11341	0.35	0.11
Matching 1h	8941	0.28	0.09

Table 17 and 18 are the pairing performance with the new matching strategy. The results are similar to the previous one (Table 13 and 14).

Table 17: χ^2 pairing efficiencies on different categories. We minimize the quantity defined in Equation 3. The χ^2 method considers the possible combinations of 6 jets.

		Correc	etly reco			
$N_{ m Jet}$	Fraction	3h	2h	1h	0h	Higgs Efficiency
= 6	0.242	0.520	0.000	0.112	0.368	0.557
=7	0.335	0.277	0.007	0.182	0.534	0.343
≥ 8	0.422	0.161	0.008	0.190	0.641	0.229
Total	1.000	0.287	0.006	0.168	0.539	0.347

Table 18: Absolute value pairing efficiencies on different categories. We minimize the quantity defined in Equation 8. The absolute value method considers the possible combination of 6 jets.

		Correc	etly reco			
$N_{ m Jet}$	Fraction	3h	2h	1h	0h	Higgs Efficiency
= 6	0.242	0.450	0.000	0.132	0.418	0.494
=7	0.335	0.249	0.007	0.177	0.566	0.313
≥ 8	0.422	0.145	0.009	0.194	0.653	0.215
Total	1.000	0.254	0.006	0.173	0.567	0.316

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