

Quiz4

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1. Data compression is often used in data storage and transmission. Suppose you want to use data compression in conjunction with encryption. Does it make more sense to:

A) Compress then encrypt

壓縮的基本原理是將文件中重複出現的位元(文字)，以新的代碼表示，並將這些代碼和原本的位元編成 dictionary，以此達到壓縮文件的效果，但若是先進行加密，可能會讓編碼相比於加密前更加無序混亂，使得壓縮時，無法找到夠多重複出現的位元，讓壓縮得效果不好。而先壓縮後，並不會對加密造成太大的影響。

因此，先進行加密再壓縮是較為合理的作法。

2. Let $G: \{0,1\}^n \rightarrow \{0,1\}^n$ be a secure PRG. Which of the following is a secure PRG (there is more than one correct answer):

D) $G'(k) = G(k \oplus 1^n)$ 把 keyword 先 inverse 不會影響安全性

E) $G'(k) = G(k) \oplus 1^n$ 把結果 inverse 不會影響安全性

F) $G'(k) = \text{reverse}(G(k))$ 把 keyword 相反不會影響安全性

Secure PRG 必須要是不可預測的，因為原本的 $G(k)$ 是 secure PRG，所以以上三個也都會是不可預測的 secure PRG。

而下面三個則是有規律而非隨機，因此可以被預測，所以不是 secure PRG。

A) $G'(k) = G(k) || 0$ 如果 LSB 被攻擊者得知，它們可以選擇一個 receiver 來解密

B) $G'(k) = G(k) || G(k)$ 重複出現不符合 secure PRG 的規則

C) $G'(k) = G(0)$ keyword = 0 可以被攻擊者得知，因此並不安全

- 3.** Let b a secure PRG. Define where \wedge is the bit-wise AND function. Consider the following statistical test A on n outputs $\text{LSB}(x)$, the last significant bit of x . What is $\text{Adv PRG}[A, G']$? You may assume that $\text{LSB}[G(k)]$ is 0 for exactly half the seeds k in K .

Ans: 0.25

Since $\text{LSB}[G(k)] = 0$ is 0.5 $\rightarrow \text{LSB}[G(K)] = 1$ is $1 - 0.5 = 0.5$.
 $\text{LSB}[G(k_1)]$ and $\text{LSB}[G(k_2)]$ both be 1 is $0.5 * 0.5 = 0.25$

- 4.** Ans: C) $p_1 = (k_1, k_2)$, $p_2 = (k_1', k_2)$, $p_3 = (k_2')$
 p_1 and p_2 can use k_1 and k_1' to derive k to decrypt
 p_2 and p_3 can use k_2 and k_2' to derive k to decrypt
 p_1 and p_3 can use k_2 and k_2' to derive k to decrypt
other 4 can't be the solution since:
A) Can't derive k with $p_2 = (k_1')$ and $p_3 = (k_2')$
B) $P_2 = (k_2, k_2')$ p_2 can derive k by itself
D) Can't derive k with $p_2 = (k_1', k_2')$ and $p_3 = (k_2')$
E) Can't derive k with $p_1 = (k_1, k_2)$ $p_2 = (k_1, k_2)$