Assignment IV- Individual Take Home Assignment

1. ANN regression model

```
In [30]:
```

```
#import libraries
import numpy as np
import pandas as pd
from sklearn.model selection import train test split
from sklearn.model_selection import cross val score
from sklearn.model selection import KFold
from sklearn.pipeline import Pipeline
from sklearn.preprocessing import MinMaxScaler
from sklearn.metrics import mean squared error
from tensorflow.python.keras.models import Sequential
from tensorflow.python.keras.layers import Dense
from tensorflow.python.keras.wrappers.scikit_learn import KerasRegressor
import matplotlib.pyplot as plt
import seaborn as sns
%matplotlib inline
import time
```

In [31]:

```
#Import Variables & standardize
dataset=np.loadtxt("data/school_grades.csv", delimiter=",", skiprows=1)
x=dataset[:,0:4]
y=dataset[:,4]
y=np.reshape(y, (-1,1))
scaler_x = MinMaxScaler()
scaler_y = MinMaxScaler()
print(scaler_x.fit(x))
xscale=scaler_x.transform(x)
print(scaler_y.fit(y))
yscale=scaler_y.transform(y)
MinMaxScaler(copy=True, feature_range=(0, 1))
MinMaxScaler(copy=True, feature_range=(0, 1))
```

In [32]:

```
#Split data into train & test
X_train, X_test, y_train, y_test = train_test_split(xscale, yscale)
```

In [33]:

```
#defining a 3 layer deep NN [12,8,1]
model = Sequential()
model.add(Dense(12, input_dim=4, kernel_initializer='normal', activation='relu'))
model.add(Dense(8, activation='relu'))
model.add(Dense(1, activation='linear'))
model.summary()
```

Model: "sequential 2"

Layer (type)	Output	Shape	Param #
dense_6 (Dense)	(None,	12)	60
dense_7 (Dense)	(None,	8)	104

```
dense_8 (Dense) (None, 1) 9

Total params: 173
Trainable params: 173
Non-trainable params: 0
```

In [34]:

#The mean_squared_error (mse) and mean_absolute_error (mae) are our loss functions - i.e. an estim
ate of how accurate the neural network is in predicting the test data.
model.compile(loss='mse', optimizer='adam', metrics=['mse', 'mae'])

In [35]:

```
#fitting model
start time = time.time()
history = model.fit(X_train, y_train, epochs=150, batch_size=50, verbose=1, validation_split=0.2)
end time = time.time()
ANN time = end time - start time
Train on 236 samples, validate on 60 samples
Epoch 1/150
399 - val loss: 0.3271 - val mse: 0.3271 - val mae: 0.5129
Epoch 2/150
53 - val loss: 0.3055 - val mse: 0.3055 - val mae: 0.4949
Epoch 3/150
27 - val loss: 0.2965 - val mse: 0.2965 - val mae: 0.4882
Epoch 4/150
68 - val loss: 0.2892 - val mse: 0.2892 - val mae: 0.4823
Epoch 5/150
03 - val loss: 0.2802 - val mse: 0.2802 - val mae: 0.4749
Epoch 6/150
14 - val_loss: 0.2688 - val_mse: 0.2688 - val_mae: 0.4653
Epoch 7/150
05 - val loss: 0.2558 - val mse: 0.2558 - val mae: 0.4542
Epoch 8/150
236/236 [=================== ] - Os 38us/sample - loss: 0.2488 - mse: 0.2488 - mae: 0.45
86 - val loss: 0.2428 - val_mse: 0.2428 - val_mae: 0.4427
Epoch 9/150
69 - val_loss: 0.2302 - val_mse: 0.2302 - val mae: 0.4313
Epoch 10/150
236/236 [============= ] - Os 47us/sample - loss: 0.2230 - mse: 0.2230 - mae: 0.43
45 - val loss: 0.2169 - val mse: 0.2169 - val mae: 0.4189
Epoch 11/150
236/236 [========================== ] - Os 42us/sample - loss: 0.2094 - mse: 0.2094 - mae: 0.42
13 - val_loss: 0.2036 - val_mse: 0.2036 - val_mae: 0.4060
Epoch 12/150
236/236 [========================= ] - Os 42us/sample - loss: 0.1958 - mse: 0.1958 - mae: 0.40
77 - val loss: 0.1901 - val mse: 0.1901 - val mae: 0.3923
Epoch 13/150
30 - val loss: 0.1763 - val mse: 0.1763 - val mae: 0.3776
Epoch 14/150
72 - val loss: 0.1624 - val mse: 0.1624 - val mae: 0.3620
Epoch 15/150
08 - val loss: 0.1485 - val mse: 0.1485 - val mae: 0.3456
Epoch 16/150
236/236 [================== ] - Os 38us/sample - loss: 0.1401 - mse: 0.1401 - mae: 0.34
36 - val loss: 0.1348 - val mse: 0.1348 - val mae: 0.3283
Epoch 17/150
236/236 [================== ] - Os 42us/sample - loss: 0.1260 - mse: 0.1260 - mae: 0.32
53 - val loss: 0.1216 - val mse: 0.1216 - val mae: 0.3103
Epoch 18/150
```

```
236/236 [============ ] - Os 42us/sample - loss: 0.1127 - mse: 0.1127 - mae: 0.30
67 - val loss: 0.1088 - val mse: 0.1088 - val mae: 0.2915
Epoch 19/150
71 - val loss: 0.0966 - val_mse: 0.0966 - val_mae: 0.2724
Epoch 20/150
69 - val loss: 0.0854 - val mse: 0.0854 - val mae: 0.2534
Epoch 21/150
70 - val loss: 0.0752 - val mse: 0.0752 - val mae: 0.2343
Epoch 22/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0669 - mse: 0.0669 - mae: 0.22
75 - val_loss: 0.0663 - val_mse: 0.0663 - val_mae: 0.2171
Epoch 23/150
92 - val_loss: 0.0588 - val_mse: 0.0588 - val_mae: 0.2015
Epoch 24/150
16 - val loss: 0.0525 - val mse: 0.0525 - val mae: 0.1864
Epoch 25/150
57 - val_loss: 0.0475 - val_mse: 0.0475 - val mae: 0.1744
Epoch 26/150
14 - val loss: 0.0436 - val mse: 0.0436 - val mae: 0.1642
Epoch 27/150
02 - val loss: 0.0406 - val mse: 0.0406 - val mae: 0.1565
Epoch 28/150
06 - val loss: 0.0385 - val mse: 0.0385 - val mae: 0.1511
Epoch 29/150
20 - val loss: 0.0369 - val mse: 0.0369 - val mae: 0.1476
Epoch 30/150
236/236 [============== ] - Os 42us/sample - loss: 0.0288 - mse: 0.0288 - mae: 0.12
56 - val loss: 0.0357 - val mse: 0.0357 - val mae: 0.1446
Epoch 31/150
08 - val loss: 0.0346 - val mse: 0.0346 - val mae: 0.1418
Epoch 32/150
236/236 [================== ] - Os 34us/sample - loss: 0.0266 - mse: 0.0266 - mae: 0.11
75 - val loss: 0.0337 - val mse: 0.0337 - val mae: 0.1392
Epoch 33/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0258 - mse: 0.0258 - mae: 0.11
46 - val_loss: 0.0328 - val_mse: 0.0328 - val_mae: 0.1367
Epoch 34/150
19 - val loss: 0.0319 - val mse: 0.0319 - val mae: 0.1342
Epoch 35/150
95 - val loss: 0.0311 - val mse: 0.0311 - val mae: 0.1317
74 - val_loss: 0.0302 - val_mse: 0.0302 - val mae: 0.1294
Epoch 37/150
54 - val loss: 0.0293 - val mse: 0.0293 - val mae: 0.1270
Epoch 38/150
36 - val loss: 0.0283 - val mse: 0.0283 - val mae: 0.1245
Epoch 39/150
15 - val loss: 0.0275 - val mse: 0.0275 - val mae: 0.1220
Epoch 40/150
94 - val loss: 0.0266 - val mse: 0.0266 - val mae: 0.1194
Epoch 41/150
71 - val_loss: 0.0258 - val_mse: 0.0258 - val_mae: 0.1168
Epoch 42/150
49 - val loss: 0.0250 - val mse: 0.0250 - val mae: 0.1144
Epoch 43/150
```

31 - val loss: 0.0241 - val mse: 0.0241 - val mae: 0.1120

```
Epoch 44/150
236/236 [============= ] - Os 34us/sample - loss: 0.0180 - mse: 0.0180 - mae: 0.09
17 - val loss: 0.0231 - val mse: 0.0231 - val mae: 0.1097
Epoch 45/150
98 - val loss: 0.0221 - val mse: 0.0221 - val mae: 0.1062
Epoch 46/150
71 - val_loss: 0.0208 - val_mse: 0.0208 - val mae: 0.1021
Epoch 47/150
47 - val_loss: 0.0198 - val_mse: 0.0198 - val_mae: 0.0998
Epoch 48/150
34 - val_loss: 0.0191 - val_mse: 0.0191 - val_mae: 0.0976
Epoch 49/150
236/236 [============= ] - Os 34us/sample - loss: 0.0144 - mse: 0.0144 - mae: 0.08
17 - val loss: 0.0184 - val mse: 0.0184 - val mae: 0.0954
Epoch 50/150
236/236 [============= ] - Os 38us/sample - loss: 0.0139 - mse: 0.0139 - mae: 0.07
96 - val_loss: 0.0178 - val mse: 0.0178 - val mae: 0.0927
Epoch 51/150
76 - val loss: 0.0172 - val mse: 0.0172 - val mae: 0.0904
Epoch 52/150
59 - val loss: 0.0167 - val mse: 0.0167 - val mae: 0.0885
Epoch 53/150
45 - val loss: 0.0161 - val mse: 0.0161 - val mae: 0.0871
Epoch 54/150
35 - val loss: 0.0156 - val_mse: 0.0156 - val_mae: 0.0861
Epoch 55/150
27 - val_loss: 0.0151 - val_mse: 0.0151 - val mae: 0.0855
Epoch 56/150
18 - val loss: 0.0147 - val mse: 0.0147 - val mae: 0.0840
Epoch 57/150
236/236 [============= ] - Os 38us/sample - loss: 0.0113 - mse: 0.0113 - mae: 0.07
05 - val_loss: 0.0143 - val_mse: 0.0143 - val_mae: 0.0827
Epoch 58/150
91 - val_loss: 0.0140 - val_mse: 0.0140 - val_mae: 0.0812
Epoch 59/150
76 - val_loss: 0.0137 - val_mse: 0.0137 - val_mae: 0.0802
Epoch 60/150
70 - val loss: 0.0133 - val mse: 0.0133 - val mae: 0.0797
Epoch 61/150
66 - val loss: 0.0130 - val mse: 0.0130 - val mae: 0.0785
Epoch 62/150
54 - val loss: 0.0127 - val mse: 0.0127 - val mae: 0.0771
Epoch 63/150
49 - val loss: 0.0124 - val mse: 0.0124 - val mae: 0.0766
Epoch 64/150
41 - val loss: 0.0122 - val mse: 0.0122 - val mae: 0.0754
Epoch 65/150
36 - val loss: 0.0120 - val_mse: 0.0120 - val_mae: 0.0749
Epoch 66/150
236/236 [============= ] - Os 38us/sample - loss: 0.0097 - mse: 0.0097 - mae: 0.06
32 - val loss: 0.0119 - val mse: 0.0119 - val mae: 0.0743
Epoch 67/150
26 - val_loss: 0.0118 - val_mse: 0.0118 - val_mae: 0.0739
Epoch 68/150
24 - val_loss: 0.0116 - val_mse: 0.0116 - val_mae: 0.0741
```

236/236 [============] - Os 34us/sample - loss: 0.0094 - mse: 0.0094 - mae: 0.06

```
25 - val loss: 0.0115 - val mse: 0.0115 - val mae: 0.0739
Epoch 70/150
22 - val loss: 0.0114 - val mse: 0.0114 - val mae: 0.0734
Epoch 71/150
16 - val loss: 0.0114 - val mse: 0.0114 - val mae: 0.0729
Epoch 72/150
236/236 [============] - ETA: Os - loss: 0.0095 - mse: 0.0095 - mae: 0.060 - Os
38us/sample - loss: 0.0093 - mse: 0.0093 - mae: 0.0618 - val loss: 0.0113 - val mse: 0.0113 - val
mae: 0.0734
Epoch 73/150
19 - val loss: 0.0112 - val mse: 0.0112 - val mae: 0.0730
Epoch 74/150
14 - val loss: 0.0112 - val mse: 0.0112 - val mae: 0.0725
Epoch 75/150
11 - val loss: 0.0112 - val mse: 0.0112 - val mae: 0.0724
Epoch 76/150
08 - val loss: 0.0112 - val mse: 0.0112 - val mae: 0.0720
Epoch 77/150
236/236 [============= ] - 0s 34us/sample - loss: 0.0091 - mse: 0.0091 - mae: 0.06
07 - val loss: 0.0111 - val mse: 0.0111 - val mae: 0.0722
Epoch 78/150
09 - val_loss: 0.0110 - val_mse: 0.0110 - val_mae: 0.0723
Epoch 79/150
08 - val_loss: 0.0110 - val_mse: 0.0110 - val_mae: 0.0721
Epoch 80/150
236/236 [============ ] - Os 38us/sample - loss: 0.0090 - mse: 0.0090 - mae: 0.06
06 - val loss: 0.0109 - val mse: 0.0109 - val mae: 0.0721
Epoch 81/150
05 - val_loss: 0.0109 - val_mse: 0.0109 - val mae: 0.0718
Epoch 82/150
07 - val loss: 0.0108 - val mse: 0.0108 - val mae: 0.0719
Epoch 83/150
06 - val loss: 0.0108 - val mse: 0.0108 - val mae: 0.0716
Epoch 84/150
05 - val loss: 0.0107 - val mse: 0.0107 - val mae: 0.0716
Epoch 85/150
03 - val loss: 0.0108 - val mse: 0.0108 - val mae: 0.0712
Epoch 86/150
02 - val loss: 0.0107 - val mse: 0.0107 - val mae: 0.0712
Epoch 87/150
00 - val_loss: 0.0107 - val_mse: 0.0107 - val_mae: 0.0710
Epoch 88/150
98 - val_loss: 0.0107 - val_mse: 0.0107 - val_mae: 0.0708
Epoch 89/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0088 - mse: 0.0088 - mae: 0.05
97 - val_loss: 0.0107 - val_mse: 0.0107 - val_mae: 0.0708
Epoch 90/150
00 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0710
Epoch 91/150
02 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0709
Epoch 92/150
99 - val loss: 0.0107 - val mse: 0.0107 - val mae: 0.0704
Epoch 93/150
96 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0703
Epoch 94/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0088 - mse: 0.0088 - mae: 0.05
```

95 - val loss: 0.0107 - val mse: 0.0107 - val mae: 0.0701

```
Epoch 95/150
97 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0706
97 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0701
Epoch 97/150
96 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0701
Epoch 98/150
94 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0699
Epoch 99/150
95 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0700
Epoch 100/150
96 - val_loss: 0.0105 - val_mse: 0.0105 - val_mae: 0.0699
Epoch 101/150
95 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0695
Epoch 102/150
89 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0693
Epoch 103/150
87 - val_loss: 0.0106 - val_mse: 0.0106 - val_mae: 0.0693
Epoch 104/150
236/236 [============= ] - Os 42us/sample - loss: 0.0087 - mse: 0.0087 - mae: 0.05
89 - val_loss: 0.0104 - val_mse: 0.0104 - val_mae: 0.0698
Epoch 105/150
01 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0699
98 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0693
Epoch 107/150
92 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0692
Epoch 108/150
86 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0690
Epoch 109/150
236/236 [=========== 0.087 - mse: 0.0087 - m
86 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0691
Epoch 110/150
84 - val loss: 0.0106 - val mse: 0.0106 - val mae: 0.0688
Epoch 111/150
86 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0692
Epoch 112/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0086 - mse: 0.0086 - mae: 0.05
89 - val_loss: 0.0105 - val_mse: 0.0105 - val mae: 0.0691
Epoch 113/150
86 - val_loss: 0.0105 - val_mse: 0.0105 - val mae: 0.0689
Epoch 114/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0086 - mse: 0.0086 - mae: 0.05
83 - val_loss: 0.0105 - val_mse: 0.0105 - val_mae: 0.0688
Epoch 115/150
87 - val_loss: 0.0104 - val_mse: 0.0104 - val_mae: 0.0690
Epoch 116/150
236/236 [============= ] - Os 38us/sample - loss: 0.0086 - mse: 0.0086 - mae: 0.05
88 - val_loss: 0.0105 - val mse: 0.0105 - val mae: 0.0689
Epoch 117/150
84 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0687
Epoch 118/150
84 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0688
Epoch 119/150
236/236 [============ ] - 0s 38us/sample - loss: 0.0086 - mse: 0.0086 - mae: 0.05
86 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0688
Epoch 120/150
```

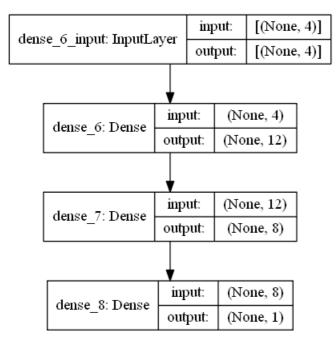
```
83 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0686
Epoch 121/150
83 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0687
Epoch 122/150
86 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0688
Epoch 123/150
83 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0686
Epoch 124/150
80 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0686
Epoch 125/150
82 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0686
Epoch 126/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0086 - mse: 0.0086 - mae: 0.05
85 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0687
Epoch 127/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0086 - mse: 0.0086 - mae: 0.05
85 - val_loss: 0.0104 - val mse: 0.0104 - val mae: 0.0685
Epoch 128/150
79 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0684
Epoch 129/150
76 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0682
Epoch 130/150
79 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0684
Epoch 131/150
80 - val_loss: 0.0104 - val_mse: 0.0104 - val mae: 0.0683
Epoch 132/150
236/236 [============= ] - Os 34us/sample - loss: 0.0085 - mse: 0.0085 - mae: 0.05
77 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0682
Epoch 133/150
79 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0682
Epoch 134/150
236/236 [============= ] - Os 38us/sample - loss: 0.0085 - mse: 0.0085 - mae: 0.05
80 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0682
Epoch 135/150
78 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0681
Epoch 136/150
236/236 [=================== ] - Os 38us/sample - loss: 0.0085 - mse: 0.0085 - mae: 0.05
74 - val loss: 0.0105 - val mse: 0.0105 - val mae: 0.0680
Epoch 137/150
236/236 [=================== ] - Os 34us/sample - loss: 0.0085 - mse: 0.0085 - mae: 0.05
72 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0680
Epoch 138/150
236/236 [============== ] - Os 34us/sample - loss: 0.0085 - mse: 0.0085 - mae: 0.05
78 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0681
Epoch 139/150
77 - val_loss: 0.0103 - val_mse: 0.0103 - val_mae: 0.0680
Epoch 140/150
78 - val_loss: 0.0103 - val_mse: 0.0103 - val_mae: 0.0679
Epoch 141/150
76 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0680
Epoch 142/150
74 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0679
Epoch 143/150
77 - val loss: 0.0103 - val mse: 0.0103 - val mae: 0.0681
Epoch 144/150
82 - val_loss: 0.0103 - val_mse: 0.0103 - val_mae: 0.0680
Epoch 145/150
76 - val loss: 0.0104 - val mse: 0.0104 - val mae: 0.0677
```

Epoch 146/150

In [36]:

```
from tensorflow.keras.utils import plot_model
#Vizualize Model
plot_model(model, to_file='ANN_model.png', show_shapes=True, show_layer_names=True, expand_nested=True)
```

Out[36]:



In [37]:

```
print(history.history.keys())
# plotting loss function with epoch
plt.plot(history.history['loss'])
plt.plot(history.history['val_loss'])
plt.title('model loss')
plt.ylabel('loss')
plt.xlabel('epoch')
plt.legend(['train', 'validation'], loc='upper left')
plt.show()
```

```
dict_keys(['loss', 'mse', 'mae', 'val_loss', 'val_mse', 'val_mae'])
```



```
0.05 - 0.00 - 0 20 40 60 80 100 120 140 epoch
```

In [38]:

```
y_pred = model.predict(X_test)

MSE_scaled = mean_squared_error(y_test, y_pred)

MSE = mean_squared_error(scaler_y.inverse_transform(y_test), scaler_y.inverse_transform(y_pred))

print("Scaled MSE:", MSE_scaled)
print("MSE:", MSE)
print("Runtime: %s seconds"%ANN_time)
```

Scaled MSE: 0.009582817080292176 MSE: 3.8331268356480934

Runtime: 2.195000648498535 seconds

2. Multiple Linear Regression Model

In [39]:

```
#import libraries
%matplotlib inline
from statsmodels.compat import lzip
import numpy as np
import pandas as pd
import statsmodels.formula.api as smf
import statsmodels.api as sm
import statsmodels.stats.api as sms
import matplotlib.pyplot as plt
```

In [40]:

```
#importing data
df = pd.read_csv('data/school_grades.csv')

#making copy to work with
df_copy = df.copy()

X = df_copy.drop(['G3'], axis=1)
y = df_copy["G3"]

#splitting training and testing sets
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3) # 70% training and 30% test
```

In [41]:

```
# Fit regression model
start_time = time.time()
results = smf.ols('G3 ~ age + absences + G1 + G2', data=pd.concat([X_train,y_train], axis=1)).fit()
end_time = time.time()
MLR_time = end_time - start_time
# Inspect the results
print(results.summary())
```

```
OLS Regression Results
```

```
Dep. Variable: G3 R-squared: 0.783 Model: OLS Adj. R-squared: 0.780
```

<pre>Metnod: Date: Time: No. Observat Df Residuals Df Model: Covariance T</pre>	ions: :		020 Prob :04 Log-I 276 AIC: 271 BIC:	tistic: (F-statistic ikelihood:):	245.1 9.94e-89 -600.71 1211. 1230.
	coef	std err	t	P> t	[0.025	0.975]
Intercept						
_				0.075		
absences				0.002		
G1	0.1962	0.080	2.445	0.015	0.038	0.354
G2	0.9641	0.073	13.160	0.000	0.820	1.108
Omnibus: 132.410		 410 Durbi	Durbin-Watson:		1.965	
Prob(Omnibus): 0.00		000 Jarqu	Jarque-Bera (JB):			
Skew: -2.095		095 Prob(Prob(JB):			
Kurtosis:		8.	170 Cond.	No.		346.

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

In [42]:

```
y_pred = results.predict(X_test)

MSE = mean_squared_error(y_test, y_pred)

print("MSE:",MSE)
print("Runtime: %s seconds"%MLR_time)
```

MSE: 1.4293875205069166

Runtime: 0.01698923110961914 seconds