Predicting Pitcher DL

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Load libraries

```
setwd("F:/Capstone Workspace/predictDL/");
library('RODBC');
library('DBI');
library('plyr');
library('dplyr');
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:plyr':
##
##
       arrange, count, desc, failwith, id, mutate, rename, summarise,
##
       summarize
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library('stringi');
library('sqldf');
## Loading required package: gsubfn
## Loading required package: proto
## Loading required package: RSQLite
library('corrplot');
library('reshape2');
library('lattice');
library('ggplot2');
library('caret');
library('logistf');
library('klaR');
## Loading required package: MASS
```

```
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
library('pROC');
## Type 'citation("pROC")' for a citation.
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
library('pls');
##
## Attaching package: 'pls'
## The following object is masked from 'package:corrplot':
##
##
       corrplot
## The following object is masked from 'package:stats':
##
##
       loadings
library('ROSE');
## Loaded ROSE 0.0-3
library('randomForest')
## randomForest 4.6-12
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:ggplot2':
##
##
       margin
## The following object is masked from 'package:dplyr':
##
##
       combine
resetPar <- function() {</pre>
    dev.new()
```

```
op <- par(no.readonly = TRUE)
  dev.off()
  op
}
par(resetPar());</pre>
```

Prepare data

Load from Cache

Load the data from cache if the cache exists. This is will save time when re-running the analysis since the data will not change. It takes approximately 30 minutes to load the data from scratch.

```
need_load <- TRUE;
if (file.exists("pitches_dl_dataset.csv")){
  pitches_dl_dataset <- read.csv("pitches_dl_dataset.csv");
  pitches_dl_predict <- read.csv("pitches_dl_predict.csv");

  drops <- c("X");
  pitches_dl_dataset <- pitches_dl_dataset[ , !(names(pitches_dl_dataset) %in % drops)];
  pitches_dl_predict <- pitches_dl_predict[ , !(names(pitches_dl_predict) %in % drops)];
  need_load <- FALSE;
}</pre>
```

Load pitchFX data from Database

If there is data cached, load the data from the SQL Server database.

Impute missing values using the Median.

The median is used to measure the central tendency for each continuous variable for each pitcher. The count of the pitch types is also calculate for each pitcher in each year.

```
if (need_load) {
  years <- c(2010, 2011, 2012, 2013, 2014, 2015, 2016);

dbhandle <- odbcDriverConnect('driver={SQL Server}; server=localhost; databas
e=PitchFx; trusted_connection=true');

impute <- function(x, fun) {
  missing <- is.na(x)
  replace(x, missing, fun(x[!missing]))</pre>
```

```
}
  centroid_fun <- median;</pre>
  impute fun <- median;</pre>
  for (i in 2010:2016)
    query <-
   paste("SELECT ", i, " as season, m.rsID, p.id, p.atbatid, a.pitcher,
            p.x, p.y, p.start_speed, p.end_speed, p.sz_top, p.sz_bot,
            p.px, p.pz, p.x0, p.y0, p.z0, p.vx0, p.vy0, p.vz0, p.ax, p.ay, p.
az,
            p.break_y, p.break_length, p.spin_dir, p.spin_rate,
            1 as type ALL,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'AB' THEN 1 ELSE 0 END AS t
ype_AB,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'AS' THEN 1 ELSE 0 END AS t
ype_AS,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'CH' THEN 1 ELSE 0 END AS t
ype_CH,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'CU' THEN 1 ELSE 0 END AS t
ype_CU,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'EP' THEN 1 ELSE 0 END AS t
ype_EP,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'FA' THEN 1 ELSE 0 END AS t
ype_FA,
            CASE WHEN ISNULL(p.pitch_type,'UN') = 'FC' THEN 1 ELSE 0 END AS t
ype_FC,
            CASE WHEN ISNULL(p.pitch_type,'UN') = 'FF' THEN 1 ELSE 0 END AS t
ype_FF,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'FO' THEN 1 ELSE 0 END AS t
ype_F0,
            CASE WHEN ISNULL(p.pitch_type,'UN') = 'FS' THEN 1 ELSE 0 END AS t
ype_FS,
            CASE WHEN ISNULL(p.pitch_type,'UN') = 'FT' THEN 1 ELSE 0 END AS t
ype_FT,
            CASE WHEN ISNULL(p.pitch_type, 'UN') = 'IN' THEN 1 ELSE 0 END AS t
ype_IN,
            CASE WHEN ISNULL(p.pitch_type,'UN') = 'KC' THEN 1 ELSE 0 END AS t
ype_KC,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'KN' THEN 1 ELSE 0 END AS t
ype_KN,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'PO' THEN 1 ELSE 0 END AS t
ype_PO,
            CASE WHEN ISNULL(p.pitch_type, 'UN') = 'SC' THEN 1 ELSE 0 END AS t
ype_SC,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'SI' THEN 1 ELSE 0 END AS t
```

```
ype_SI,
            CASE WHEN ISNULL(p.pitch type, 'UN') = 'SL' THEN 1 ELSE 0 END AS t
ype_SL,
            CASE WHEN ISNULL(p.pitch_type,'UN') not in ('AS', 'CH', 'CU', 'EP
', 'FA', 'FC', 'FF', 'FO', 'FS', 'FT', 'IN', 'KC', 'KN', 'PO', 'SC', 'SI') TH
EN 1 ELSE 0 END as type UN
          FROM [PitchFx",i,"].[dbo].[Pitches] p
          INNER JOIN [PitchFx", i,"].[dbo].[AtBats] a on a.ID = p.AtBatID
          INNER JOIN [Mapping].[dbo].[RSID_MLBID_MAP] m on a.pitcher = m.mlbi
d
          INNER JOIN [Lahman].[dbo].[Master] ms on ms.retroID = m.rsID", sep=
"");
    pitches_raw <-sqlQuery(dbhandle, query);</pre>
    pitches_impute_centroid <- ddply(pitches_raw, ~rsID, transform,</pre>
                    x = impute(x, impute_fun),
                    y = impute(y, impute fun),
                    start speed = impute(start speed, impute fun),
                    end speed = impute(end speed, impute fun),
                    sz top = impute(sz top, impute fun),
                    sz_bot = impute(sz_bot, impute_fun),
                    px = impute(px, impute_fun),
                    pz = impute(pz, impute fun),
                    x0 = impute(x0, impute fun),
                    y0 = impute(y0, impute_fun),
                    z0 = impute(z0, impute fun),
                    vx0 = impute(vx0, impute_fun),
                    vy0 = impute(vy0, impute fun),
                    vz0 = impute(vz0, impute fun),
                    ax = impute(ax, impute fun),
                    ay = impute(ay, impute_fun),
                    az = impute(az, impute_fun),
                    break_y = impute(break_y, impute_fun),
                    break_length = impute(break_length, impute_fun),
                    spin dir = impute(spin dir, impute fun),
                    spin rate = impute(spin rate, impute fun)
                    );
   pitches_aggregate <- ddply(pitches_impute_centroid, ~rsID, summarise,</pre>
                    season = max(season),
                    x = centroid fun(x),
                    y = centroid fun(y),
                    start speed = centroid fun(start speed),
                    end_speed = centroid_fun(end_speed),
                    sz_top = centroid_fun(sz_top),
                    sz bot = centroid fun(sz bot),
                    px = centroid fun(px),
```

```
pz = centroid fun(pz),
                    x0 = centroid fun(x0),
                    y0 = centroid_fun(y0),
                    z0 = centroid_fun(z0),
                    vx0 = centroid_fun(vx0),
                    vy0 = centroid_fun(vy0),
                    vz0 = centroid fun(vz0),
                    ax = centroid_fun(ax),
                    ay = centroid_fun(ay),
                    az = centroid fun(az),
                    break_y = centroid_fun(break_y),
                    break length = centroid fun(break length),
                    spin dir = centroid fun(spin dir),
                    spin_rate = centroid_fun(spin_rate),
                    num_pitches = sum(type_ALL),
                    num\_AB = sum(type\_AB),
                    num_AS = sum(type_AS),
                    num CH = sum(type CH),
                    num CU = sum(type CU),
                    num_EP = sum(type_EP),
                    num_FA = sum(type_FA),
                    num_FC = sum(type_FC),
                    num_FF = sum(type_FF),
                    num FO = sum(type FO),
                    num_FS = sum(type_FS),
                    num_FT = sum(type_FT),
                    num IN = sum(type IN),
                    num_KC = sum(type_KC),
                    num_KN = sum(type_KN),
                    num PO = sum(type PO),
                    num_SC = sum(type_SC),
                    num_SI = sum(type_SI),
                    num_SL = sum(type_SL),
                    num UN = sum(type UN)
                    );
    assign(paste("pitches",i,sep=""), pitches_aggregate);
  };
  pitches <- rbind(pitches2010, pitches2011, pitches2012, pitches2013, pitche
s2014, pitches2015, pitches2016);
  pitches <- pitches[complete.cases(pitches),];</pre>
  close(dbhandle);
}
```

Load the disabled this

If there is no data cached, load the disable list data from the SQL Server database.

This data contains the list of pitchers on the disable list in each year. Define a new column for season_1 to denote the previous season. This is required since the pitching data from the previous season will be used to determine if the player will be on the disabled list in the current season.

```
if (need load) {
  dbhandle <- odbcDriverConnect('driver={SQL Server};server=localhost;databas</pre>
e=PitchFx;trusted connection=true');
  query <- "
  SELECT rsid, 2011 as season_dl, sum(days) as DLDays
    FROM [DisabledList].[dbo].[DL2011]
    WHERE Position in ('LHP', 'RHP', 'RP', 'SP', 'P')
    GROUP BY rsid
  UNION
  SELECT rsid, 2012 as season dl, sum(days) as DLDays
    FROM [DisabledList].[dbo].[DL2012]
    WHERE Pos in ('LHP', 'RHP', 'RP', 'SP', 'P')
    GROUP BY rsid
  UNION
  SELECT rsid, 2013 as season dl, sum(days) as DLDays
    FROM [DisabledList].[dbo].[DL2013]
    WHERE Position in ('LHP', 'RHP', 'RP', 'SP', 'P')
    GROUP BY rsid
  UNION
  SELECT rsid, 2014 as season dl, sum(days) as DLDays
    FROM [DisabledList].[dbo].[DL2014]
    WHERE Position in ('LHP', 'RHP', 'RP', 'SP', 'P')
    GROUP BY rsid
  UNION
  SELECT rsid, 2015 as season dl, sum(days) as DLDays
    FROM [DisabledList].[dbo].[DL2015]
    WHERE Position in ('LHP', 'RHP', 'RP', 'SP', 'P')
    GROUP BY rsid
  UNION
  SELECT rsid, 2016 as season dl, sum(days) as DLDays
    FROM [DisabledList].[dbo].[DL2016]
    WHERE Position in ('LHP', 'RHP', 'RP', 'SP', 'P')
    GROUP BY rsid
  ۳;
  dl <- sqlQuery(dbhandle, query);</pre>
  dl <- dl[complete.cases(dl),];</pre>
  dl$season 1 <- dl$season-1;</pre>
  close(dbhandle);
 }
```

Join the pitch and disabled list data

If there is no data cached, join the pitching data and disabled list data by season.

Define the response variable OnDL to be TRUE if the pitcher is was on the disabled list or FALSE otherwise.

The pitching data from seasons 2010 to 2015 will be used to build and test the model since the disabled list is only available up to the 2016 season.

The pitching data from 2016 will be used to predict which players are most likely be on the disable list in 2017.

```
if (need load) {
  #use previous season to predict DL in current season
  pitches_dl <- merge(x=pitches, y=dl, by.x=c("rsID", "season"), by.y=c("rsid")</pre>
", "season_1"), all.x = TRUE, all.y=FALSE)
  pitches_dl[pitches_dl==""] <- NA; #replace blanks with NA</pre>
  pitches dl$DLDays[is.na(pitches dl$DLDays)] <- 0; #no DL pitchers are on DL</pre>
for 0 days
  pitches dl$OnDL <- (ifelse(pitches dl$DLDays>0, 1, 0));
  drops <- c("season dl", "DLDays");</pre>
  pitches_dl <- pitches_dl[ , !(names(pitches_dl) %in% drops)];</pre>
  pitches dl <- pitches dl[complete.cases(pitches dl),];</pre>
  pitches dl dataset <- pitches dl[pitches dl$season < 2016,]; #for modeling</pre>
  pitches_dl_predict <- pitches_dl$season == 2016,]; #for 2017 pre</pre>
diction
  #pitches_dl_dataset$OnDL <- as.factor(ifelse(pitches_dl_dataset$DLDays>0, '
YES', 'NO'));
  drops <- c("season");</pre>
  pitches dl dataset <- pitches dl dataset[ , !(names(pitches dl dataset) %in</pre>
% drops)];
  pitches dl predict <- pitches dl predict[ , !(names(pitches dl predict) %in</pre>
% drops)];
  #write to csv to save time
  write.csv(pitches_dl_dataset, "pitches_dl_dataset.csv");
  write.csv(pitches_dl_predict, "pitches_dl_predict.csv");
}
```

Transform count variables

Apply Anscombe transformation to count variables

```
trf func <- function(x) {</pre>
  return ( 2*sqrt(x+3/8));
  #return ( log(x+1));
}
pitches_dl_dataset$trf_num_pitches <- trf_func(pitches_dl_dataset$num_pitches</pre>
pitches_dl_predict$trf_num_pitches <- trf_func(pitches_dl_predict$num_pitches</pre>
);
#
# for (t in c("AB", "AS", "CH", "CU", "EP", "FA", "FC", "FF", "FO", "FS", "FT
', "IN","KC", "KN", "PO", "SC", "SI", "SL", "UN"))
# {
#
    expression <- paste("pitches_dl_dataset$num_", t, sep="");</pre>
#
    eval_expression <- eval(parse(text=expression)) /pitches_dl_dataset$num_p</pre>
itches;
    assign_var = paste("pitches_dl_dataset$trf_num_", t, sep="");
#
#
    assign(assign var, eval expression)
#
#
    expression <- paste("pitches_dl_dataset$num_", t, sep="");</pre>
    eval expression <- eval(parse(text=expression))/pitches dl predict$num pi
#
tches;
    assign var = paste("pitches dl predict$trf num ", t, sep="");
#
#
    assign(assign_var, eval_expression)
#
# }
pitches_dl_dataset$trf_num_AB <- trf_func(pitches_dl_dataset$num_AB)</pre>
pitches_dl_dataset$trf_num_AS <- trf_func(pitches_dl_dataset$num_AS)</pre>
pitches_dl_dataset$trf_num_CH <- trf_func(pitches_dl_dataset$num_CH)</pre>
pitches_dl_dataset$trf_num_CU <- trf_func(pitches_dl_dataset$num_CU)</pre>
pitches dl dataset$trf num EP <- trf func(pitches dl dataset$num EP)</pre>
pitches_dl_dataset$trf_num_FA <- trf_func(pitches_dl_dataset$num_FA)</pre>
pitches_dl_dataset$trf_num_FC <- trf_func(pitches_dl_dataset$num_FC)</pre>
pitches_dl_dataset$trf_num_FF <- trf_func(pitches_dl_dataset$num_FF)</pre>
pitches_dl_dataset$trf_num_FO <- trf_func(pitches_dl_dataset$num_FO)</pre>
pitches_dl_dataset$trf_num_FS <- trf_func(pitches_dl_dataset$num_FS)</pre>
pitches_dl_dataset$trf_num_FT <- trf_func(pitches_dl_dataset$num_FT)</pre>
pitches_dl_dataset$trf_num_IN <- trf_func(pitches_dl_dataset$num_IN)</pre>
pitches_dl_dataset$trf_num_KC <- trf_func(pitches_dl_dataset$num_KC)</pre>
pitches dl dataset$trf num KN <- trf func(pitches dl dataset$num KN)</pre>
pitches_dl_dataset$trf_num_PO <- trf_func(pitches_dl_dataset$num_PO)</pre>
pitches dl dataset$trf num SC <- trf func(pitches dl dataset$num SC)</pre>
pitches_dl_dataset$trf_num_SI <- trf_func(pitches_dl_dataset$num_SI)</pre>
pitches_dl_dataset$trf_num_SL <- trf_func(pitches_dl_dataset$num_SL)</pre>
```

```
pitches dl dataset$trf num UN <- trf func(pitches dl dataset$num UN)</pre>
pitches_dl_predict$trf_num_AB <- trf_func(pitches_dl_predict$num_AB)</pre>
pitches dl predict$trf num AS <- trf func(pitches dl predict$num AS)</pre>
pitches_dl_predict$trf_num_CH <- trf_func(pitches_dl_predict$num_CH)</pre>
pitches dl predict$trf num CU <- trf func(pitches dl predict$num CU)</pre>
pitches_dl_predict$trf_num_EP <- trf_func(pitches_dl_predict$num_EP)</pre>
pitches_dl_predict$trf_num_FA <- trf_func(pitches_dl_predict$num_FA)</pre>
pitches dl predict$trf num FC <- trf func(pitches dl predict$num FC)</pre>
pitches_dl_predict$trf_num_FF <- trf_func(pitches_dl_predict$num_FF)</pre>
pitches_dl_predict$trf_num_FO <- trf_func(pitches_dl_predict$num_FO)</pre>
pitches_dl_predict$trf_num_FS <- trf_func(pitches_dl_predict$num_FS)</pre>
pitches dl predict$trf num FT <- trf func(pitches dl predict$num FT)</pre>
pitches_dl_predict$trf_num_IN <- trf_func(pitches_dl_predict$num_IN)</pre>
pitches dl predict$trf num KC <- trf func(pitches dl predict$num KC)</pre>
pitches_dl_predict$trf_num_KN <- trf_func(pitches_dl_predict$num_KN)</pre>
pitches_dl_predict$trf_num_PO <- trf_func(pitches_dl_predict$num_PO)</pre>
pitches_dl_predict$trf_num_SC <- trf_func(pitches_dl_predict$num_SC)</pre>
pitches_dl_predict$trf_num_SI <- trf_func(pitches_dl_predict$num_SI)</pre>
pitches_dl_predict$trf_num_SL <- trf_func(pitches_dl_predict$num_SL)</pre>
pitches dl predict$trf num UN <- trf func(pitches dl predict$num UN)</pre>
model dataset <- pitches_dl_dataset[,-grep( "^num_" , names( pitches_dl_datas</pre>
et ) )];
predict dataset <- pitches dl predict[,-grep( "^num " , names( pitches dl pre</pre>
dict ) )];
```

Exploratory Analysis

Summary of data set

List of variables

```
dependent_var <- colnames(model_dataset[,-grep( "^OnDL" , names( model_datase
t ) )])[-1];
original_var <- dependent_var[1:22];
count_var <- dependent_var[22:40];
response_var <- "OnDL";</pre>
```

Summary of continous variables

```
summary(model dataset[which(colnames(model dataset) %in% original var)]);
##
                                   start_speed
                                                  end_speed
         Х
## Min. : 75.54
                   Min.
                        : 97.7
                                  Min. :53.9
                                                Min. :49.80
## 1st Qu.: 97.86
                   1st Qu.:145.1
                                  1st Qu.:87.5
                                                1st Qu.:80.70
## Median :102.15
                   Median :148.5
                                  Median :89.8
                                                Median :82.70
## Mean :103.65
                   Mean :151.0
                                  Mean :89.4
                                                Mean :82.33
```

```
3rd Ou.:107.30
                                      3rd Ou.:91.9
                                                      3rd Ou.:84.50
                      3rd Ou.:152.8
##
    Max.
           :139.98
                     Max.
                             :195.7
                                      Max.
                                              :99.4
                                                      Max.
                                                             :91.10
##
                         sz_bot
        sz_top
                                           рх
                                                               pz
                                                         Min.
##
                                     Min.
                                            :-1.43400
   Min.
           :0.000
                            :0.000
                                                                :1.185
                    Min.
##
    1st Qu.:3.390
                    1st Qu.:1.550
                                     1st Qu.:-0.18875
                                                         1st Qu.:2.194
##
    Median :3.420
                    Median :1.580
                                     Median :-0.06750
                                                         Median :2.322
##
    Mean
                                            :-0.07214
           :3.416
                    Mean
                           :1.583
                                     Mean
                                                         Mean
                                                                :2.334
##
    3rd Qu.:3.450
                    3rd Qu.:1.610
                                     3rd Qu.: 0.05550
                                                         3rd Qu.:2.459
##
    Max.
           :3.750
                            :1.805
                                     Max.
                                            : 1.33350
                                                         Max.
                                                                :3.638
##
          x0
                            y0
                                         z0
                                                         VX0
                             :50
##
    Min.
           :-4.085
                     Min.
                                   Min.
                                          :1.960
                                                    Min.
                                                           :-15.965
                                   1st Qu.:5.643
##
    1st Qu.:-2.030
                     1st Qu.:50
                                                    1st Qu.: -4.080
##
    Median :-1.381
                     Median :50
                                   Median :5.894
                                                    Median : 4.511
##
    Mean
           :-0.717
                     Mean
                            :50
                                   Mean
                                          :5.854
                                                    Mean
                                                           : 2.084
##
    3rd Qu.: 1.047
                      3rd Qu.:50
                                   3rd Qu.:6.136
                                                    3rd Qu.: 6.216
##
    Max.
         : 5.229
                     Max.
                            :50
                                   Max.
                                          :7.306
                                                    Max.
                                                           : 11.441
##
         vy0
                            vz0
                                               ax
                                                                 ay
##
                      Min.
                              :-9.690
                                        Min.
                                                :-23.480
    Min.
           :-145.42
                                                           Min.
                                                                  :10.34
##
    1st Qu.:-134.48
                      1st Qu.:-5.546
                                        1st Qu.:-10.075
                                                           1st Qu.:25.43
                                        Median : -5.433
##
    Median :-131.43
                      Median :-4.654
                                                           Median :26.93
##
           :-130.83
                             :-4.445
                                              : -2.959
    Mean
                      Mean
                                        Mean
                                                           Mean
                                                                  :26.98
                       3rd Qu.:-3.641
                                        3rd Qu.: 4.211
##
    3rd Qu.:-128.08
                                                           3rd Qu.:28.60
##
                              :10.264
    Max.
           : -78.97
                      Max.
                                        Max.
                                                : 22.284
                                                           Max.
                                                                  :35.57
##
                          break_y
                                       break length
                                                           spin_dir
          az
##
                                      Min. : 2.600
    Min.
           :-44.314
                      Min.
                              :23.7
                                                        Min.
                                                               : 70.01
                                                        1st Qu.:161.16
##
    1st Qu.:-24.074
                      1st Qu.:23.8
                                      1st Qu.: 4.900
    Median :-20.948
##
                      Median :23.8
                                      Median : 5.800
                                                        Median :200.38
##
    Mean
           :-21.181
                      Mean
                              :23.8
                                      Mean
                                              : 5.884
                                                        Mean
                                                               :191.94
##
    3rd Qu.:-17.874
                       3rd Qu.:23.8
                                      3rd Qu.: 6.700
                                                        3rd Qu.:217.43
##
    Max.
          : -6.576
                      Max.
                              :23.9
                                      Max.
                                              :16.650
                                                        Max.
                                                               :325.10
##
      spin_rate
                     trf_num_pitches
##
    Min.
          : 445.4
                     Min. : 2.345
                     1st Qu.: 29.521
##
    1st Qu.:1663.2
##
    Median :1867.4
                     Median : 54.346
##
    Mean
           :1846.9
                     Mean
                             : 56.209
##
    3rd Qu.:2053.3
                      3rd Qu.: 72.811
##
    Max.
         :3000.0
                     Max. :133.287
```

Summary of count variables after transforming

```
summary(model_dataset[which(colnames(model_dataset) %in% count_var)]);
```

```
trf_num_pitches
                        trf_num_AB
                                        trf_num_AS
                                                        trf_num_CH
##
   Min. : 2.345
                      Min.
                            :1.225
                                      Min.
                                           :1.225
                                                      Min. : 1.225
   1st Qu.: 29.521
                      1st Qu.:1.225
                                      1st Qu.:1.225
                                                      1st Qu.: 3.674
##
   Median : 54.346
                      Median :1.225
                                      Median :1.225
                                                      Median :10.464
   Mean
           : 56.209
                      Mean
                             :1.227
                                      Mean
                                             :1.225
                                                      Mean
                                                             :14.888
##
    3rd Qu.: 72.811
                      3rd Qu.:1.225
                                      3rd Qu.:1.225
                                                      3rd Qu.:22.749
##
   Max.
           :133.287
                      Max.
                             :2.345
                                      Max.
                                             :2.345
                                                      Max.
                                                             :67.775
                                        trf_num_FA
##
      trf_num_CU
                       trf_num_EP
                                                         trf_num_FC
##
   Min. : 1.225
                     Min. : 1.225
                                      Min. : 1.225
                                                       Min. : 1.225
```

```
1st Qu.: 1.225
                     1st Qu.: 1.225
                                       1st Qu.: 1.225
                                                        1st Qu.: 1.225
##
   Median : 4.637
                     Median : 1.225
                                       Median : 1.225
                                                        Median : 1.225
##
   Mean
           :11.697
                     Mean
                            : 1.322
                                       Mean
                                              : 1.345
                                                        Mean
                                                                : 7.299
##
    3rd Qu.:19.532
                     3rd Qu.: 1.225
                                       3rd Qu.: 1.225
                                                        3rd Qu.: 5.431
##
   Max.
           :68.129
                     Max.
                             :27.009
                                       Max.
                                              :16.778
                                                        Max.
                                                                :87.416
      trf_num_FF
                       trf_num_F0
                                         trf_num_FS
                                                          trf_num_FT
##
##
          : 1.225
                     Min. : 1.225
                                            : 1.225
                                                        Min. : 1.225
   Min.
                                       Min.
    1st Qu.:11.380
                                       1st Qu.: 1.225
##
                     1st Qu.: 1.225
                                                        1st Qu.: 1.225
##
   Median :26.486
                     Median : 1.225
                                       Median : 1.225
                                                        Median : 6.124
##
   Mean
           :29.871
                     Mean
                             : 1.293
                                       Mean
                                             : 3.100
                                                        Mean
                                                                :13.998
                                       3rd Qu.: 1.225
                                                        3rd Qu.:21.852
##
    3rd Qu.:44.917
                     3rd Qu.: 1.225
##
   Max.
           :98.881
                     Max.
                             :35.405
                                       Max.
                                              :64.942
                                                        Max.
                                                                :86.357
##
      trf_num_IN
                       trf_num_KC
                                         trf_num_KN
                                                           trf_num_PO
##
   Min.
           : 1.225
                     Min.
                             : 1.225
                                       Min.
                                              : 1.225
                                                         Min.
                                                                 :1.225
##
    1st Qu.: 1.225
                     1st Qu.: 1.225
                                                 1.225
                                                          1st Qu.:1.225
                                       1st Qu.:
##
   Median : 3.674
                     Median : 1.225
                                       Median : 1.225
                                                          Median :1.225
##
   Mean
           : 3.744
                     Mean
                             : 3.060
                                       Mean
                                                 1.472
                                                         Mean
                                                                 :1.724
    3rd Qu.: 5.788
                     3rd Qu.: 1.225
##
                                                 1.225
                                                          3rd Qu.:2.345
                                       3rd Qu.:
##
   Max.
           :13.019
                     Max.
                             :67.420
                                       Max.
                                              :108.247
                                                         Max.
                                                                 :7.842
##
      trf_num_SC
                       trf_num_SI
                                         trf_num_SL
##
          : 1.225
                            : 1.225
                                             : 1.225
   Min.
                     Min.
                                       Min.
    1st Qu.: 1.225
##
                     1st Qu.: 1.225
                                       1st Qu.: 3.082
##
   Median : 1.225
                     Median : 1.225
                                       Median :14.748
##
          : 1.252
                            :10.211
                                              :18.245
   Mean
                     Mean
                                       Mean
##
    3rd Qu.: 1.225
                     3rd Qu.: 7.583
                                       3rd Qu.:29.521
##
   Max. :20.821
                     Max. :98.982
                                       Max. :78.521
```

Histogram of data

Continuous Variables

```
d <- melt(model_dataset[which(colnames(model_dataset) %in% original_var)]);
## No id variables; using all as measure variables

ggplot(d,aes(x = value)) + facet_wrap(~variable,scales = "free_x") + geom_hi
stogram();

## `stat bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```

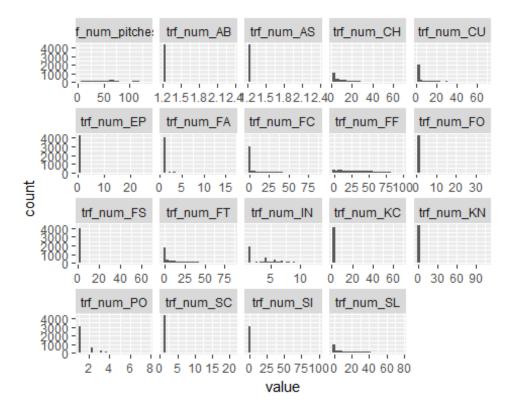


Variables

```
d <- melt(model_dataset[which(colnames(model_dataset) %in% count_var)]);
## No id variables; using all as measure variables

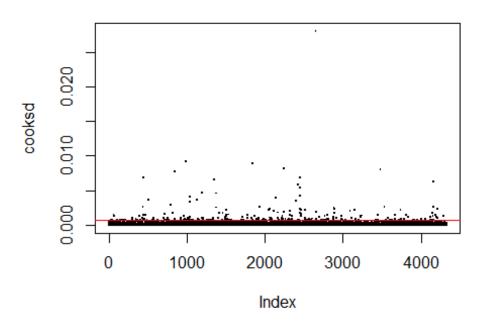
ggplot(d,aes(x = value)) + facet_wrap(~variable,scales = "free_x") + geom_hi
stogram();

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```



Outliers

Influential Obs by Cooks distance



text(x=1:length(cooksd)+1, y=cooksd, labels=ifelse(cooksd>10*mean(cooksd, n
a.rm=T),names(cooksd),""), col="red")

Remove outliers

```
influential <- as.numeric(names(cooksd)[(cooksd > 3*mean(cooksd, na.rm=T))]);
model_dataset_lessOutliers <- model_dataset[-(influential[!is.na(influential)]), ];</pre>
```

Summary of data after outliers removed

```
summary(model_dataset_lessOutliers);
##
          rsID
                                                        start speed
                           Х
                                            У
##
    abadf001:
                6
                    Min.
                           : 75.54
                                      Min.
                                            : 97.7
                                                       Min.
                                                               :53.90
##
    adamm001:
                    1st Qu.: 97.85
                                      1st Qu.:145.1
                                                       1st Qu.:87.60
                6
##
    affej001:
                6
                    Median :102.15
                                      Median :148.5
                                                       Median :89.85
    albem001:
                    Mean
                            :103.63
                                      Mean
                                              :150.9
                                                       Mean
##
                6
                                                               :89.47
##
    arrij001:
                    3rd Qu.:107.30
                                      3rd Qu.:152.8
                                                       3rd Qu.:91.90
    atchs001:
                    Max.
                            :139.98
                                              :195.7
                                                       Max.
                                                               :99.40
##
                                      Max.
    (Other) :4084
##
##
      end_speed
                         sz_top
                                          sz_bot
                                                             рх
           :49.80
                                                            :-1.43400
##
    Min.
                    Min.
                            :0.000
                                     Min.
                                             :0.000
                                                      Min.
##
    1st Qu.:80.70
                    1st Qu.:3.390
                                     1st Qu.:1.550
                                                      1st Qu.:-0.18862
##
   Median :82.70
                    Median :3.420
                                     Median :1.580
                                                      Median :-0.06750
           :82.39
                                                              :-0.07198
    Mean
                    Mean
                            :3.418
                                     Mean
                                             :1.584
    3rd Qu.:84.50
                    3rd Qu.:3.450
                                     3rd Qu.:1.610
                                                      3rd Qu.: 0.05563
```

```
##
    Max.
          :91.10
                            :3.750
                                     Max.
                                             :1.805
                    Max.
                                                      Max.
                                                             : 1.33350
##
##
                           x0
                                              y0
                                                           z0
          pz
##
                    Min.
                            :-4.0845
                                               :50
                                                            :1.960
   Min.
           :1.185
                                        Min.
                                                     Min.
##
    1st Qu.:2.197
                    1st Qu.:-2.0326
                                        1st Qu.:50
                                                     1st Qu.:5.649
##
    Median :2.323
                    Median :-1.3820
                                        Median :50
                                                     Median :5.897
##
    Mean
          :2.335
                    Mean
                            :-0.7262
                                        Mean
                                               :50
                                                     Mean
                                                            :5.860
##
    3rd Qu.:2.460
                    3rd Qu.: 1.0146
                                        3rd Qu.:50
                                                     3rd Qu.:6.137
##
    Max.
           :3.638
                    Max.
                            : 5.2295
                                       Max.
                                               :50
                                                     Max.
                                                            :7.306
##
##
         vx0
                            vy0
                                               vz0
                                                                  ax
##
    Min.
           :-15.965
                       Min.
                              :-145.42
                                         Min.
                                                 :-9.690
                                                           Min.
                                                                   :-23.480
    1st Qu.: -3.996
                                          1st Qu.:-5.558
##
                       1st Qu.:-134.50
                                                           1st Qu.:-10.087
    Median : 4.506
                       Median :-131.50
##
                                         Median :-4.671
                                                           Median : -5.486
##
    Mean
           : 2.113
                       Mean
                              :-130.93
                                          Mean
                                                 :-4.483
                                                           Mean
                                                                   : -3.003
##
    3rd Qu.: 6.231
                       3rd Qu.:-128.19
                                          3rd Qu.:-3.680
                                                           3rd Qu.: 4.138
##
    Max.
          : 11.441
                      Max.
                             : -78.97
                                         Max.
                                                 :10.264
                                                           Max.
                                                                   : 22.284
##
##
                                           break y
                                                        break length
          ay
                           az
##
    Min.
           :10.34
                    Min.
                            :-44.314
                                        Min.
                                              :23.7
                                                       Min. : 2.600
##
    1st Qu.:25.47
                    1st Qu.:-23.965
                                        1st Qu.:23.8
                                                       1st Qu.: 4.900
##
                                        Median :23.8
    Median :26.95
                    Median :-20.862
                                                       Median : 5.700
##
    Mean
                            :-21.074
           :27.00
                    Mean
                                        Mean
                                               :23.8
                                                       Mean
                                                               : 5.848
##
    3rd Qu.:28.62
                    3rd Ou.:-17.827
                                        3rd Qu.:23.8
                                                       3rd Qu.: 6.700
##
    Max.
           :35.44
                    Max.
                            : -8.132
                                        Max.
                                               :23.9
                                                       Max.
                                                              :16.650
##
##
       spin dir
                                            OnDL
                                                         trf num pitches
                        spin rate
##
           : 70.01
                            : 507.6
    Min.
                      Min.
                                       Min.
                                               :0.0000
                                                         Min.
                                                                : 2.345
##
    1st Qu.:161.79
                      1st Qu.:1668.6
                                        1st Qu.:0.0000
                                                         1st Qu.: 29.283
##
    Median :200.39
                      Median :1870.7
                                       Median :0.0000
                                                         Median : 53.568
##
           :192.05
                             :1850.2
                                                                 : 55.531
    Mean
                      Mean
                                       Mean
                                               :0.2371
                                                         Mean
##
    3rd Qu.:217.19
                      3rd Qu.:2055.2
                                        3rd Qu.:0.0000
                                                         3rd Qu.: 72.024
##
    Max.
           :325.10
                      Max.
                             :3000.0
                                       Max.
                                               :1.0000
                                                         Max.
                                                                 :133.287
##
##
      trf num AB
                       trf num AS
                                       trf num CH
                                                         trf num CU
                                             : 1.225
##
           :1.225
                            :1.225
                                                              : 1.225
    Min.
                    Min.
                                     Min.
                                                       Min.
##
    1st Qu.:1.225
                    1st Qu.:1.225
                                     1st Qu.: 3.674
                                                       1st Qu.: 1.225
##
    Median :1.225
                    Median :1.225
                                     Median :10.654
                                                       Median : 4.637
##
    Mean
           :1.225
                    Mean
                            :1.225
                                     Mean
                                             :14.780
                                                       Mean
                                                              :11.646
##
    3rd Qu.:1.225
                    3rd Qu.:1.225
                                     3rd Qu.:22.506
                                                       3rd Qu.:19.326
##
    Max.
           :1.225
                    Max.
                            :2.345
                                     Max.
                                             :67.775
                                                       Max.
                                                               :68.129
##
##
      trf num EP
                        trf num FA
                                         trf_num_FC
                                                           trf num FF
##
          : 1.225
                            : 1.225
                                             : 1.225
                                                               : 1.225
   Min.
                      Min.
                                       Min.
                                                         Min.
##
    1st Qu.: 1.225
                      1st Qu.: 1.225
                                       1st Qu.: 1.225
                                                         1st Qu.:11.554
##
    Median : 1.225
                      Median : 1.225
                                       Median : 1.225
                                                         Median :26.486
##
    Mean
          : 1.287
                      Mean
                             : 1.329
                                       Mean
                                             : 7.061
                                                         Mean
                                                                 :29.889
##
    3rd Qu.: 1.225
                      3rd Qu.: 1.225
                                        3rd Qu.: 5.050
                                                         3rd Qu.:44.805
##
    Max.
           :27.009
                      Max.
                             :16.778
                                       Max.
                                               :87.416
                                                         Max.
                                                                 :98.598
##
```

```
trf num FO
                       trf num FS
                                        trf_num_FT
                                                         trf num IN
   Min.
##
          : 1.225
                     Min. : 1.225
                                      Min. : 1.225
                                                       Min.
                                                             : 1.225
##
    1st Qu.: 1.225
                     1st Qu.: 1.225
                                      1st Qu.: 1.225
                                                       1st Qu.: 1.225
##
                     Median : 1.225
   Median : 1.225
                                      Median : 6.124
                                                       Median : 3.674
##
   Mean
         : 1.233
                     Mean
                            : 2.949
                                      Mean
                                             :14.025
                                                       Mean
                                                              : 3.717
    3rd Qu.: 1.225
                     3rd Qu.: 1.225
##
                                      3rd Qu.:22.125
                                                       3rd Qu.: 5.788
##
   Max.
          :11.023
                            :57.180
                                      Max.
                                             :86.357
                     Max.
                                                       Max.
                                                              :13.019
##
##
                                         trf_num_PO
      trf_num_KC
                       trf_num_KN
                                                         trf_num_SC
##
   Min.
          : 1.225
                               1.225
                                       Min.
                                              :1.225
                                                              : 1.225
                     Min.
                                                       Min.
    1st Qu.: 1.225
##
                     1st Qu.:
                               1.225
                                       1st Qu.:1.225
                                                       1st Qu.: 1.225
   Median : 1.225
                                       Median :1.225
##
                     Median :
                               1.225
                                                       Median : 1.225
##
           : 2.858
                               1.434
   Mean
                     Mean
                                       Mean
                                              :1.714
                                                       Mean
                                                              : 1.249
##
    3rd Qu.: 1.225
                     3rd Qu.:
                               1.225
                                       3rd Qu.:2.345
                                                       3rd Qu.: 1.225
##
           :65.920
                            :108.247
                                              :6.745
                                                               :20.821
   Max.
                     Max.
                                       Max.
                                                       Max.
##
##
      trf_num_SI
                       trf_num_SL
                                        trf_num_UN
##
           : 1.225
                            : 1.225
   Min.
                     Min.
                                      Min.
                                             : 1.225
##
    1st Qu.: 1.225
                     1st Qu.: 3.082
                                      1st Qu.:11.726
##
   Median : 1.225
                     Median :14.883
                                      Median :20.821
##
          : 9.778
                            :18.228
                                             :23.235
   Mean
                     Mean
                                      Mean
    3rd Qu.: 6.745
##
                     3rd Qu.:29.283
                                      3rd Qu.:32.535
##
           :92.030
   Max.
                     Max.
                            :78.521
                                      Max.
                                             :79.231
##
```

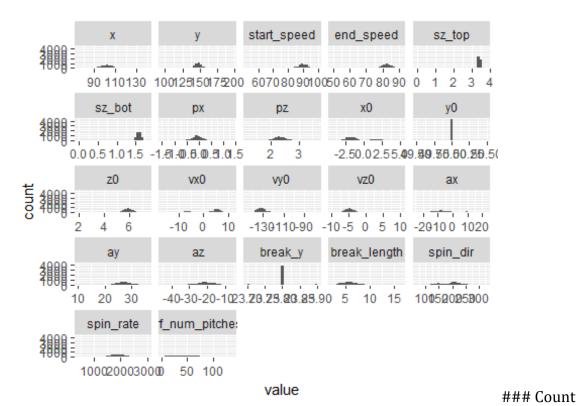
Histogram of data

Continuous Variables with outliers

```
d <- melt(model_dataset[which(colnames(model_dataset) %in% original_var)]);
## No id variables; using all as measure variables

ggplot(d,aes(x = value)) + facet_wrap(~variable,scales = "free_x") + geom_hi
stogram();

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```

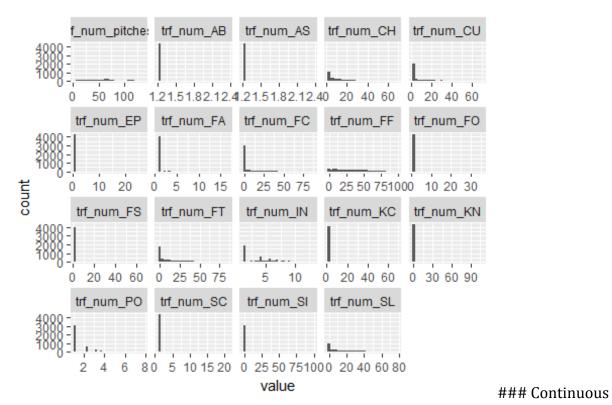


Variables with outliers

```
d <- melt(model_dataset[which(colnames(model_dataset) %in% count_var)]);
## No id variables; using all as measure variables

ggplot(d,aes(x = value)) + facet_wrap(~variable,scales = "free_x") + geom_hi
stogram();

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```



Variables without outliers

```
d <- melt(model_dataset_lessOutliers[which(colnames(model_dataset_lessOutlier
s) %in% original_var)]);
## No id variables; using all as measure variables

ggplot(d,aes(x = value)) + facet_wrap(~variable,scales = "free_x") + geom_hi
stogram();

## `stat bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```

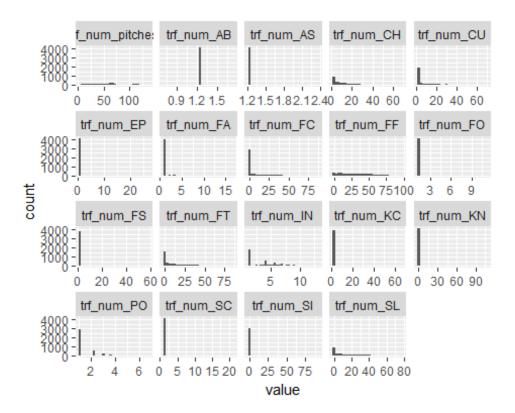


Variables without outlisers

```
d <- melt(model_dataset_lessOutliers[which(colnames(model_dataset_lessOutlier
s) %in% count_var)]);
## No id variables; using all as measure variables

ggplot(d,aes(x = value)) + facet_wrap(~variable,scales = "free_x") + geom_hi
stogram();

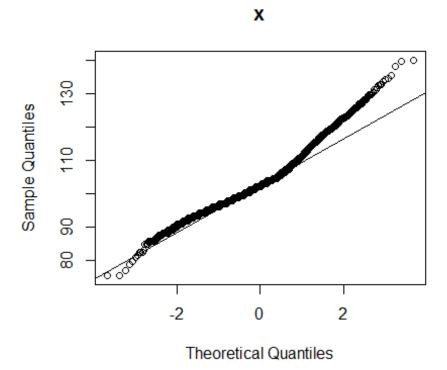
## `stat bin()` using `bins = 30`. Pick better value with `binwidth`.</pre>
```

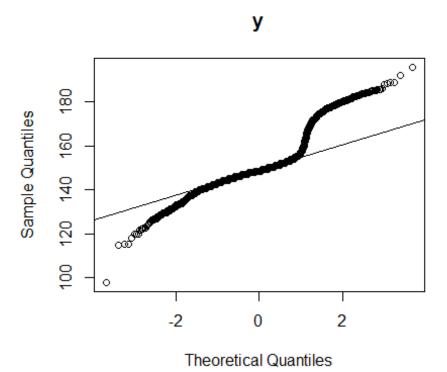


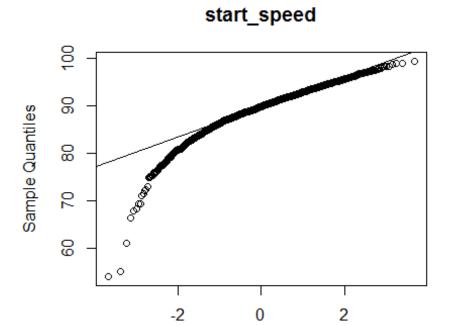
Check normality using QQ plot without outliers

```
par(mar=c(4,4,4,4))

for (i in 2:(ncol(model_dataset_lessOutliers)-1)){
   tmp <- model_dataset_lessOutliers[, i];
   qqnorm(tmp, main = colnames(model_dataset_lessOutliers[i]));
   qqline(tmp);
}</pre>
```

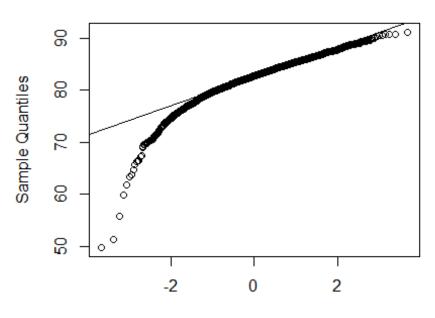




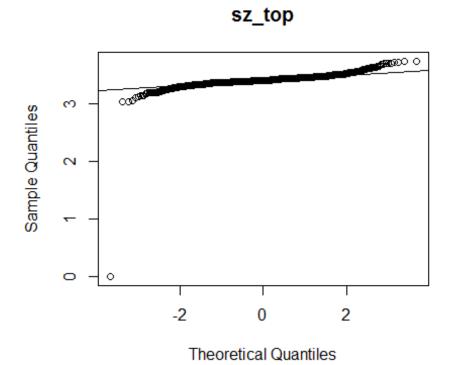


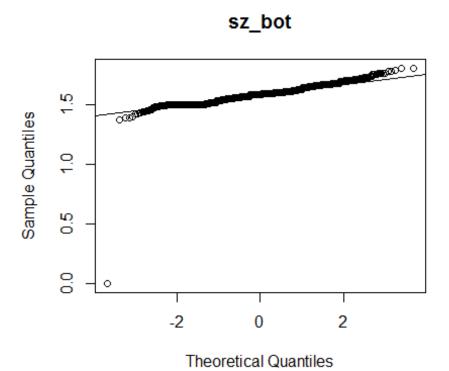
Theoretical Quantiles

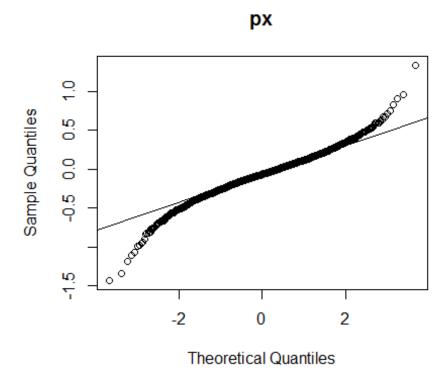
end_speed

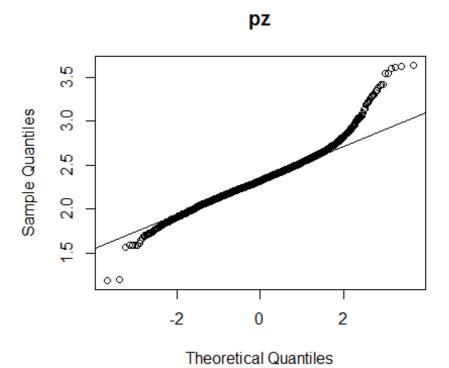


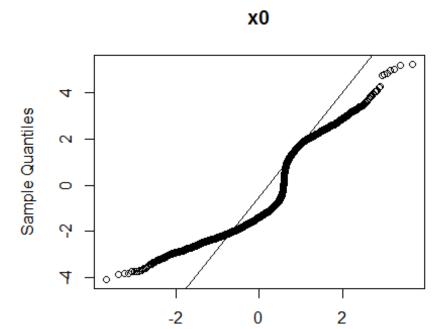
Theoretical Quantiles



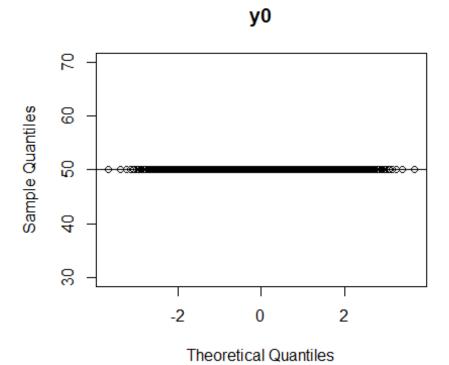




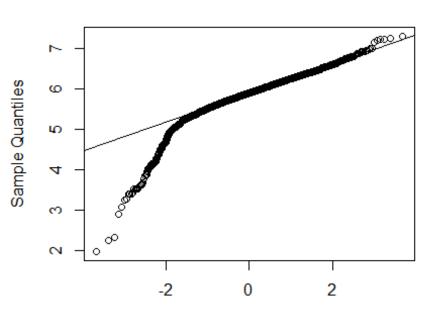




Theoretical Quantiles

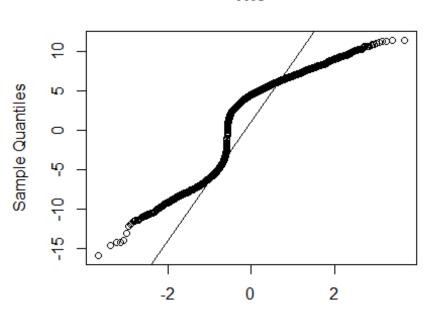




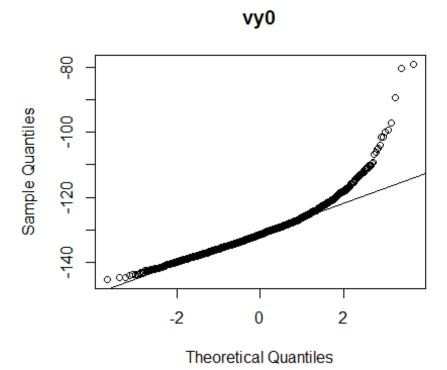


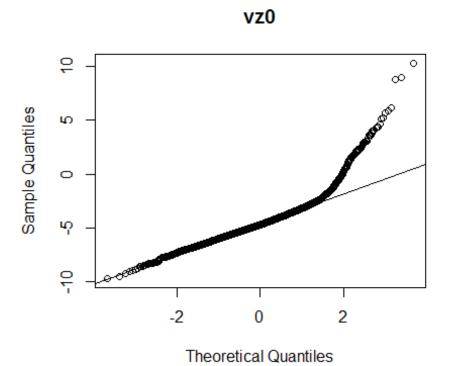
Theoretical Quantiles

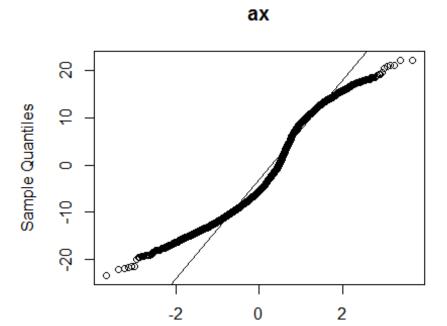
vx0



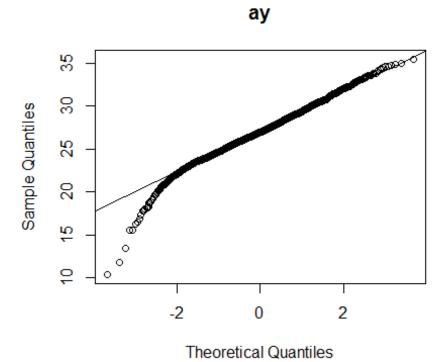
Theoretical Quantiles



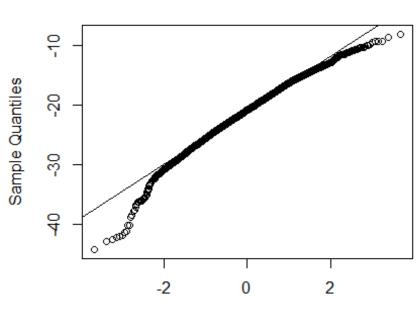




Theoretical Quantiles

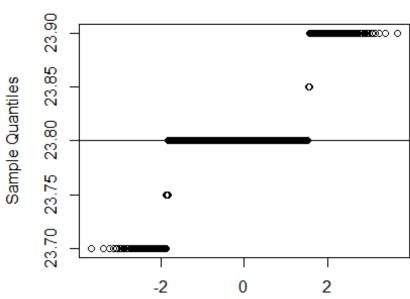






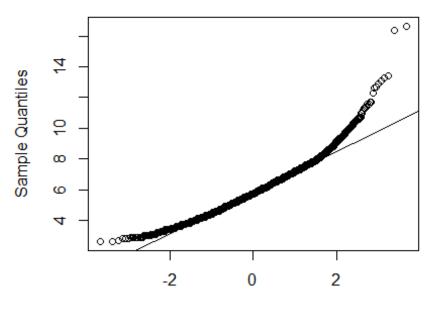
Theoretical Quantiles

break_y



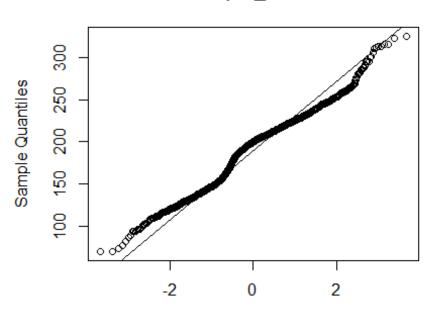
Theoretical Quantiles

break_length



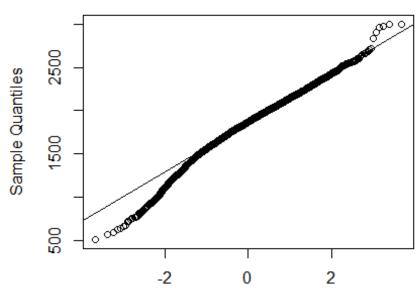
Theoretical Quantiles

spin_dir



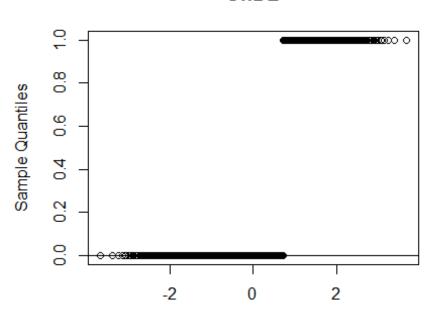
Theoretical Quantiles





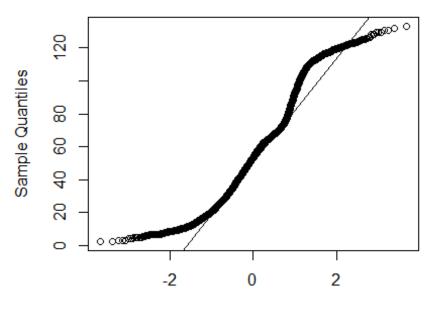
Theoretical Quantiles

OnDL



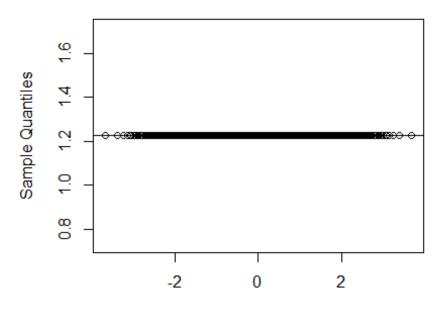
Theoretical Quantiles

trf_num_pitches

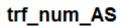


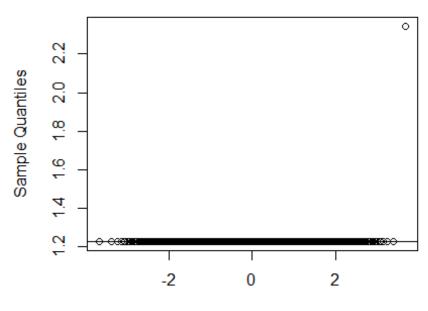
Theoretical Quantiles

trf_num_AB



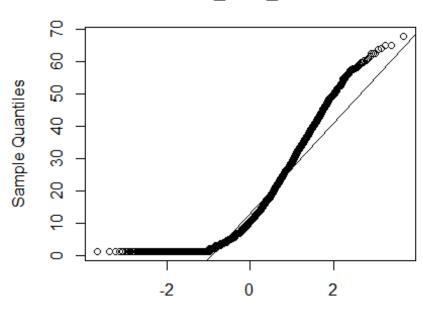
Theoretical Quantiles



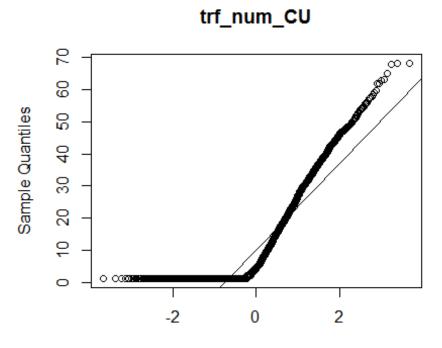


Theoretical Quantiles

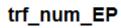
trf_num_CH

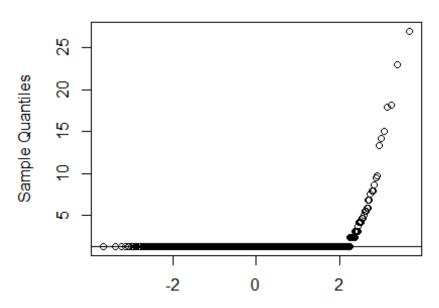


Theoretical Quantiles

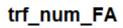


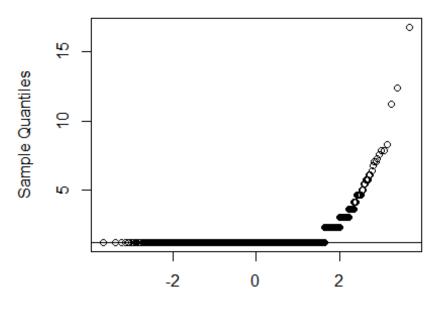
Theoretical Quantiles





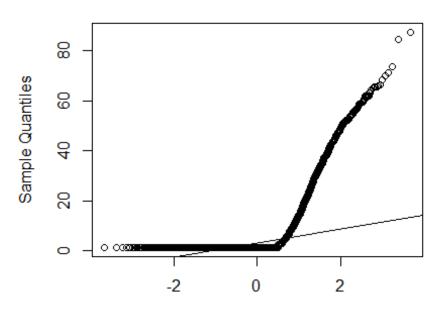
Theoretical Quantiles



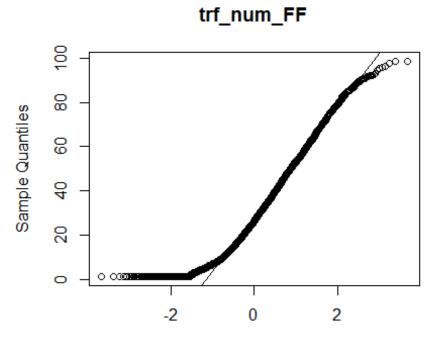


Theoretical Quantiles

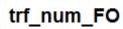
trf_num_FC

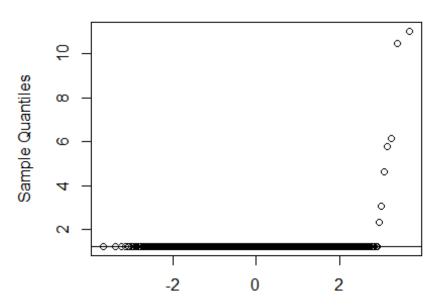


Theoretical Quantiles

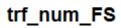


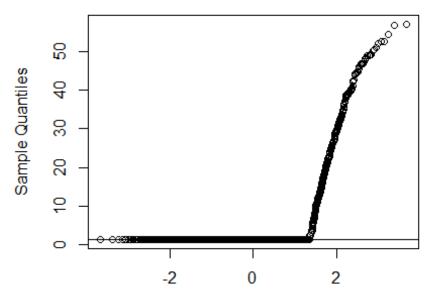
Theoretical Quantiles





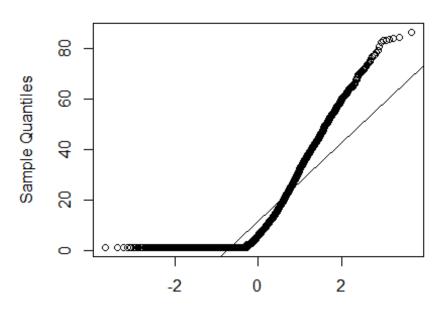
Theoretical Quantiles





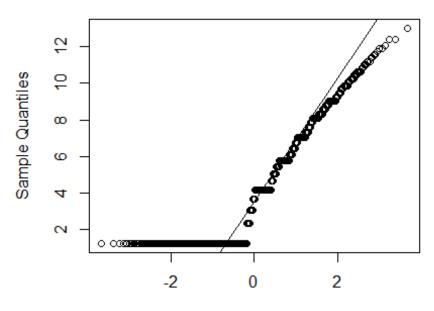
Theoretical Quantiles

trf_num_FT



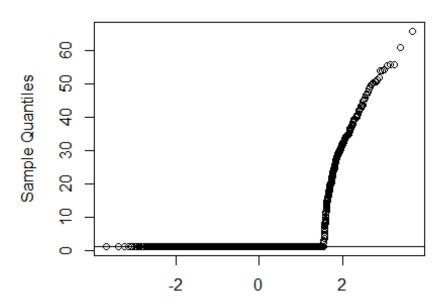
Theoretical Quantiles

trf_num_IN



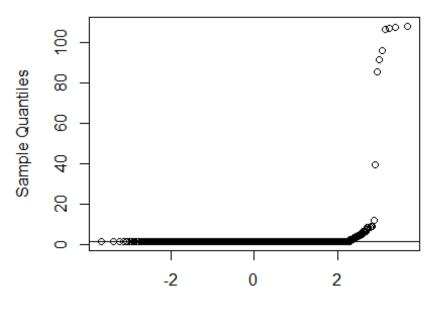
Theoretical Quantiles

trf_num_KC



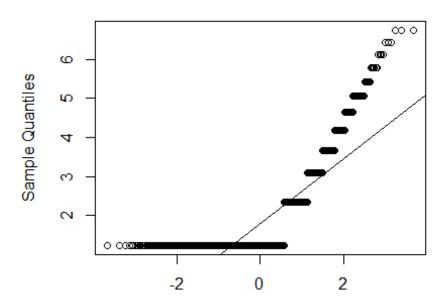
Theoretical Quantiles

trf_num_KN



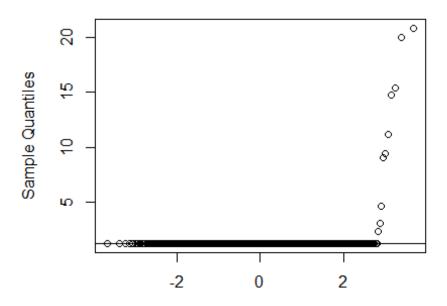
Theoretical Quantiles

trf_num_PO



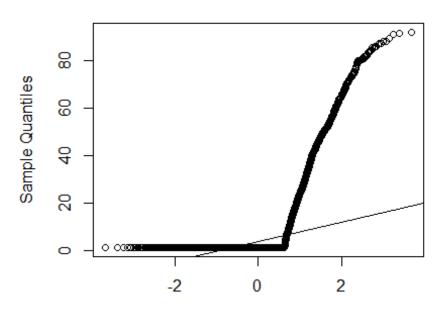
Theoretical Quantiles

trf_num_SC



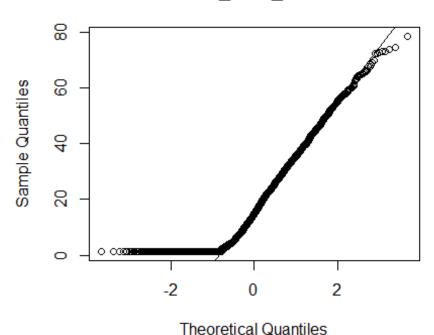
Theoretical Quantiles

trf_num_SI



Theoretical Quantiles

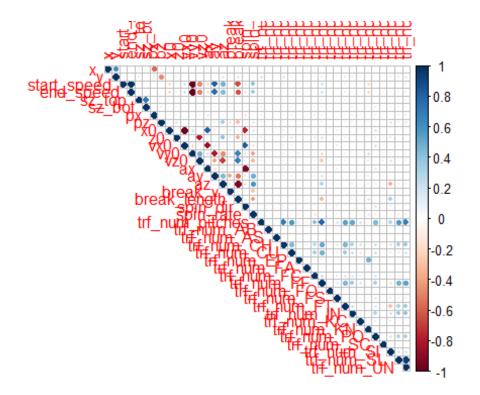
trf_num_SL



Display correlation

All variables

```
numeric_dataset <- model_dataset[sapply(model_dataset, is.numeric)];
#ignore column y0 since there is 0 variance
numeric_dataset <- numeric_dataset[ , !(names(numeric_dataset) %in% c("y0", "OnDL"))];
#numeric_dataset <- numeric_dataset[1:(ncol(numeric_dataset))];
m <- cor(numeric_dataset);
corrplot::corrplot(m, type="upper");</pre>
```



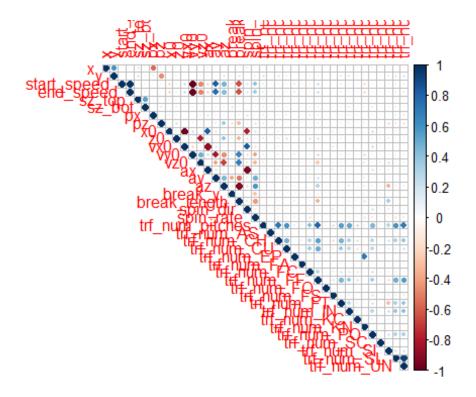
#corrplot::corrplot.mixed(m);

All variables without outliers

```
numeric_dataset_lessOutliers <- model_dataset_lessOutliers[sapply(model_datas
et_lessOutliers, is.numeric)];

#ignore column y0 since there is 0 variance
numeric_dataset_lessOutliers <- numeric_dataset_lessOutliers[, !(names(numeric_dataset_lessOutliers) %in% c("y0", "trf_num_AB", "OnDL"))];

#numeric_dataset <- numeric_dataset[1:(ncol(numeric_dataset))];
m_lessOutliers <- cor(numeric_dataset_lessOutliers);
corrplot::corrplot(m_lessOutliers, type="upper");</pre>
```



#corrplot::corrplot.mixed(m_lessOutliers);

Model Building with all data

Model 1 All variables

```
Create training and testing set using 75% training and 25% testing
set.seed(123)

train <- createDataPartition(model_dataset$OnDL, p=0.75, list=FALSE);

training <- model_dataset[train,];
write.csv(training, "training.csv");

testing <- model_dataset[-train,];

threshold <- 0.4;</pre>
```

Construct Model

```
selected_variables <- dependent_var;
selected_i <- which(colnames(training) %in% selected_variables);</pre>
```

Summary

The summary shows that variables which have some significance to the outcomes are: end_speed, sz_bot, pz, z0, vz0, break_y, break_length, trf_num_pitches, trf_num_CH, trf_num_FT, trf_num_SI, trf_num_UN

```
summary(mod 1);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training)
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                          Max
                                  3Q
## -1.6157 -0.7642 -0.5675
                                       2.4404
                              0.8835
##
## Coefficients: (1 not defined because of singularities)
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   4.791e+01 4.331e+03
                                          0.011
                                                 0.99117
## X
                   -1.438e-02
                              1.621e-02 -0.887
                                                 0.37498
## y
                   1.796e-02 1.062e-02
                                          1.691
                                                 0.09086 .
## start_speed
                  -3.305e-01
                              5.816e-01 -0.568
                                                 0.56982
## end speed
                   1.305e-01 1.581e-01
                                          0.825
                                                 0.40922
## sz top
                                          0.829
                                                 0.40712
                   8.380e-01 1.011e+00
## sz bot
                   3.676e-01 1.052e+00
                                          0.350
                                                 0.72666
                  -3.698e-01
                              5.575e-01 -0.663
                                                 0.50714
## px
                   5.774e-01 4.710e-01
## pz
                                          1.226
                                                 0.22027
## x0
                                                 0.45061
                   2.618e-01
                              3.470e-01
                                          0.754
## y0
                          NA
                                     NA
                                             NA
                                                      NA
                  -2.719e-01
                              3.982e-01
                                         -0.683
## z0
                                                 0.49480
## vx0
                   1.136e-01
                              1.381e-01
                                          0.823
                                                 0.41072
## vy0
                  -2.127e-01 4.071e-01
                                         -0.522
                                                 0.60140
                  -1.967e-01 1.473e-01
                                         -1.335
## vz0
                                                 0.18183
## ax
                   3.755e-02 3.098e-02
                                          1.212
                                                 0.22551
## ay
                  -2.311e-02
                              5.081e-02
                                         -0.455
                                                 0.64918
                                         -0.050
                              6.215e-02
## az
                  -3.089e-03
                                                 0.96035
## break_y
                  -3.087e+00
                              1.952e+00
                                         -1.582
                                                 0.11366
## break length
                   2.243e-01
                              1.959e-01
                                          1.145
                                                 0.25221
## spin dir
                   2.884e-03 4.366e-03
                                          0.660
                                                 0.50894
## spin rate
                  -1.923e-05
                              3.034e-04
                                         -0.063
                                                 0.94947
## trf num pitches 2.782e-02 9.278e-03
                                          2.999
                                                 0.00271 **
## trf num AB
                   3.076e-01 7.137e-01
                                          0.431
                                                 0.66642
## trf_num_AS
                   1.708e+01
                              3.531e+03
                                          0.005
                                                 0.99614
## trf_num_CH
                  -1.502e-02 5.985e-03 -2.510
                                                 0.01206 *
```

```
0.713
## trf num CU
                    3.915e-03
                                5.493e-03
                                                    0.47598
## trf num EP
                    -8.667e-03
                                3.930e-02
                                            -0.221
                                                    0.82547
## trf_num_FA
                    4.091e-02
                                5.976e-02
                                             0.685
                                                    0.49366
## trf num FC
                    -3.243e-03
                                4.874e-03
                                            -0.665
                                                    0.50578
## trf_num_FF
                    2.446e-04
                                6.576e-03
                                            0.037
                                                    0.97034
## trf_num_F0
                    -1.027e-02
                                3.799e-02
                                            -0.270
                                                    0.78703
## trf num FS
                    -7.668e-03
                                6.925e-03
                                            -1.107
                                                    0.26814
## trf_num_FT
                    -4.951e-03
                                5.041e-03
                                            -0.982
                                                    0.32606
## trf_num_IN
                    -4.556e-02
                                1.895e-02
                                            -2.404
                                                    0.01621 *
## trf num KC
                                6.919e-03
                                            -0.268
                                                    0.78867
                    -1.855e-03
## trf_num_KN
                    -1.538e-02
                                1.501e-02
                                            -1.025
                                                    0.30532
## trf num PO
                    2.985e-02
                                4.956e-02
                                            0.602
                                                    0.54695
                                1.908e+02
## trf num SC
                    -1.106e+01
                                            -0.058
                                                    0.95379
## trf_num_SI
                    -8.891e-03
                                5.803e-03
                                            -1.532
                                                    0.12550
## trf_num_SL
                    -1.868e-03
                                9.015e-03
                                            -0.207
                                                    0.83583
## trf num UN
                    6.808e-04
                                1.120e-02
                                             0.061
                                                    0.95154
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3667.1 on 3245
                                        degrees of freedom
## Residual deviance: 3322.1
                              on 3205
                                        degrees of freedom
## AIC: 3404.1
##
## Number of Fisher Scoring iterations: 16
```

COefficients

```
mod_1$coefficients;
##
                                                           start speed
       (Intercept)
                                   Х
                                                    У
##
      4.790750e+01
                      -1.438374e-02
                                         1.795870e-02
                                                         -3.305324e-01
##
         end_speed
                              sz_top
                                               sz_bot
                                                                     рх
##
      1.305043e-01
                       8.380272e-01
                                         3.676150e-01
                                                         -3.698234e-01
                                                   y0
##
                                  х0
                                                                     z0
                 pz
##
      5.773934e-01
                       2.617837e-01
                                                   NA
                                                         -2.718682e-01
##
                vx0
                                                  vz0
                                 vy0
                                                                     ax
##
      1.136216e-01
                      -2.126678e-01
                                        -1.967318e-01
                                                          3.754882e-02
##
                                              break_y
                                                          break_length
                 ay
##
                      -3.089469e-03
     -2.311265e-02
                                        -3.087421e+00
                                                          2.243344e-01
##
          spin dir
                           spin_rate trf_num_pitches
                                                            trf num AB
                                         2.782237e-02
##
      2.883562e-03
                      -1.922527e-05
                                                          3.076493e-01
##
        trf_num_AS
                         trf_num_CH
                                           trf_num_CU
                                                            trf_num_EP
##
      1.707741e+01
                      -1.502439e-02
                                         3.915119e-03
                                                         -8.666885e-03
        trf_num_FA
                         trf_num_FC
                                           trf_num_FF
##
                                                            trf_num_F0
##
      4.090886e-02
                      -3.243093e-03
                                         2.445568e-04
                                                         -1.026509e-02
##
        trf_num_FS
                         trf_num_FT
                                           trf_num_IN
                                                            trf num KC
##
                      -4.951131e-03
                                                         -1.854666e-03
     -7.668036e-03
                                        -4.555533e-02
##
        trf_num_KN
                         trf_num_PO
                                           trf_num_SC
                                                            trf_num_SI
##
     -1.538422e-02
                       2.985496e-02
                                        -1.105629e+01
                                                         -8.890802e-03
```

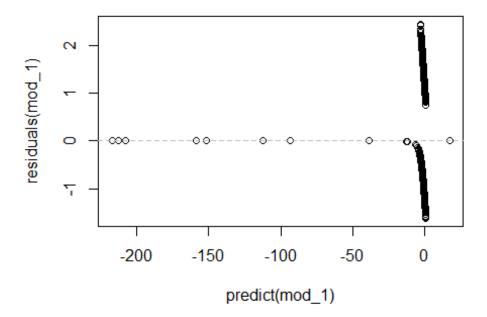
```
## trf_num_SL trf_num_UN
## -1.868304e-03 6.808348e-04
```

Odds Ratio

```
exp(mod_1$coefficients);
##
                                                          start speed
       (Intercept)
                                   Χ
                                                    У
##
      6.396778e+20
                       9.857192e-01
                                        1.018121e+00
                                                         7.185411e-01
##
         end_speed
                              sz_top
                                               sz_bot
                                                                    рх
##
      1.139403e+00
                       2.311802e+00
                                        1.444286e+00
                                                         6.908563e-01
##
                                                   y0
                 pz
##
      1.781389e+00
                       1.299246e+00
                                                   NA
                                                         7.619547e-01
##
                vx0
                                 vy0
                                                  vz0
                                                                    ax
##
                                                         1.038263e+00
      1.120328e+00
                       8.084246e-01
                                        8.214109e-01
##
                                              break_y
                                                         break_length
                 ay
                                  az
##
      9.771524e-01
                       9.969153e-01
                                        4.561945e-02
                                                         1.251489e+00
##
          spin_dir
                          spin_rate trf_num_pitches
                                                           trf_num_AB
##
      1.002888e+00
                       9.999808e-01
                                        1.028213e+00
                                                         1.360224e+00
##
        trf num AS
                         trf_num_CH
                                          trf_num_CU
                                                           trf num EP
##
      2.609906e+07
                       9.850879e-01
                                        1.003923e+00
                                                         9.913706e-01
##
        trf_num_FA
                         trf_num_FC
                                          trf_num_FF
                                                           trf_num_F0
##
      1.041757e+00
                       9.967622e-01
                                        1.000245e+00
                                                         9.897874e-01
##
                         trf_num_FT
                                                            trf_num_KC
        trf_num_FS
                                          trf_num_IN
##
      9.923613e-01
                       9.950611e-01
                                        9.554667e-01
                                                         9.981471e-01
##
        trf num KN
                         trf num PO
                                          trf num SC
                                                           trf_num_SI
##
      9.847335e-01
                       1.030305e+00
                                        1.578746e-05
                                                         9.911486e-01
##
        trf_num_SL
                         trf_num_UN
##
      9.981334e-01
                       1.000681e+00
```

Residual

```
plot(predict(mod_1),residuals(mod_1));
abline(h=0,lty=2,col="grey");
```



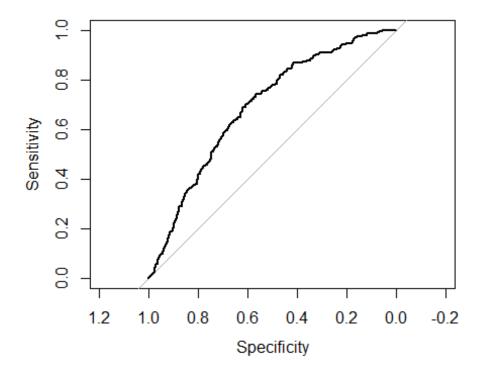
Performance

```
pred <- ifelse(predict(mod_1, testing, type='response') > threshold, 1, 0)
confusionMatrix(data=pred, reference=testing$OnDL, positive='1');
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
                    1
##
            0 673 244
              85
##
                  79
##
                  Accuracy : 0.6957
##
##
                    95% CI: (0.6673, 0.723)
       No Information Rate: 0.7012
##
       P-Value [Acc > NIR] : 0.6684
##
##
##
                     Kappa: 0.1542
##
    Mcnemar's Test P-Value : <2e-16
##
               Sensitivity: 0.24458
##
##
               Specificity: 0.88786
##
            Pos Pred Value: 0.48171
            Neg Pred Value: 0.73391
##
##
                Prevalence: 0.29880
##
            Detection Rate: 0.07308
##
      Detection Prevalence: 0.15171
```

```
## Balanced Accuracy : 0.56622
##
## 'Positive' Class : 1
##
```

ROC curve

```
prob <- predict(mod_1, testing, type='response');
g1 <- roc(OnDL ~ prob, data = testing);
roc.curve(testing$OnDL, prob, plotit =F)
## Area under the curve (AUC): 0.690
plot(g1)</pre>
```



Model Building without outliers

Model 1(b) All variables

```
Create training and testing set using 75% training and 25% testing
train_lessOutliers <- createDataPartition(model_dataset_lessOutliers$0nDL, p=
0.75, list=FALSE);
training_lessOutliers <- model_dataset_lessOutliers[train_lessOutliers,];
testing_lessOutliers <- model_dataset_lessOutliers[-train_lessOutliers,];</pre>
```

Construct Model

Summary

The summary shows that variables which have some significance to the outcomes are: end_speed, break_length, trf_num_pitches, trf_num_FA, trf_num_FT, trf_num_KN

```
summary(mod 1b);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training_lessOutli
ers)
##
## Deviance Residuals:
      Min
                10
                     Median
                                  3Q
                                          Max
## -1.6558 -0.7240 -0.5000 -0.1471
                                       2.4884
##
## Coefficients: (2 not defined because of singularities)
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   8.745e+01 1.941e+04
                                          0.005 0.996406
## X
                  -1.927e-02 2.064e-02 -0.934 0.350411
## y
                   2.512e-02 1.334e-02 1.883 0.059667
## start speed
                  -1.310e+00 6.491e-01 -2.018 0.043632 *
## end speed
                  -2.380e-02 1.773e-01 -0.134 0.893222
## sz_top
                  -2.253e-01 1.090e+00 -0.207 0.836265
## sz_bot
                   1.255e+00 1.144e+00 1.097 0.272603
## px
                   6.341e-02
                              6.925e-01 0.092 0.927040
## pz
                   1.608e+00 5.581e-01
                                          2.881 0.003964 **
## x0
                  -6.459e-02
                              3.913e-01 -0.165 0.868904
## y0
                          NA
                                     NA
                                             NA
                                                      NA
## z0
                  -1.352e+00 4.603e-01 -2.937 0.003316 **
## vx0
                   1.400e-02 1.543e-01
                                         0.091 0.927698
## vv0
                  -1.025e+00 4.554e-01 -2.251 0.024390 *
## vz0
                  -6.471e-01
                              1.709e-01 -3.786 0.000153 ***
                  3.611e-02 3.505e-02
## ax
                                         1.030 0.302869
## ay
                  -1.395e-01
                              5.681e-02 -2.455 0.014090 *
## az
                  -6.398e-02 7.528e-02 -0.850 0.395350
                  -4.295e+00 2.111e+00 -2.035 0.041877 *
## break y
```

```
## break length
                                            1.349 0.177276
                    3.159e-01
                                2.342e-01
## spin dir
                    1.688e-03
                                5.564e-03
                                            0.303 0.761585
## spin_rate
                    2.461e-04
                                3.632e-04
                                             0.677 0.498137
## trf num pitches
                    1.804e-02
                                1.058e-02
                                            1.705 0.088223 .
## trf_num_AB
                            NA
                                       NA
                                               NA
                                                         NA
## trf_num_AS
                    1.991e+01
                                1.582e+04
                                            0.001 0.998996
                                6.584e-03
                                            -1.001 0.316856
## trf num CH
                    -6.590e-03
## trf_num_CU
                    5.427e-03
                                5.989e-03
                                            0.906 0.364896
## trf_num_EP
                    -2.044e-01
                                1.251e-01
                                            -1.634 0.102317
## trf num FA
                                           -3.044 0.002336 **
                   -3.213e-01
                                1.056e-01
## trf_num_FC
                    4.582e-04
                                5.381e-03
                                            0.085 0.932137
## trf_num_FF
                    1.002e-02
                                7.739e-03
                                             1.295 0.195475
## trf num FO
                   -7.047e-02
                                2.939e-01
                                           -0.240 0.810492
## trf_num_FS
                    3.050e-03
                                7.829e-03
                                            0.390 0.696827
## trf_num_FT
                    2.912e-03
                                5.675e-03
                                            0.513 0.607871
## trf_num_IN
                    -7.009e-02
                                2.049e-02
                                           -3.421 0.000623 ***
## trf_num_KC
                   -2.082e-03
                                7.514e-03
                                           -0.277 0.781735
## trf num KN
                   -9.878e+00
                                2.335e+02
                                           -0.042 0.966259
## trf num PO
                                5.354e-02
                                            0.605 0.545362
                    3.238e-02
## trf_num_SC
                                8.855e+02
                                           -0.015 0.988097
                   -1.321e+01
                                           -0.549 0.583337
## trf num SI
                   -3.658e-03
                                6.668e-03
## trf_num_SL
                    8.721e-03
                                1.002e-02
                                            0.870 0.384217
## trf_num_UN
                   -7.347e-03
                                1.242e-02
                                           -0.592 0.554040
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3345.5
                              on 3089
                                        degrees of freedom
## Residual deviance: 2897.1
                              on 3050
                                        degrees of freedom
## AIC: 2977.1
## Number of Fisher Scoring iterations: 19
```

COefficients

```
mod 1b$coefficients;
                                                           start_speed
##
       (Intercept)
                                   Х
                                                     У
##
                       -1.927374e-02
                                         2.512222e-02
                                                         -1.309720e+00
      8.744651e+01
##
         end speed
                              sz_top
                                               sz bot
##
     -2.379882e-02
                       -2.252678e-01
                                         1.255197e+00
                                                          6.340907e-02
##
                                                   y0
                                                                     z0
                 pz
                                  х0
##
      1.607753e+00
                       -6.459042e-02
                                                   NA
                                                         -1.351931e+00
##
                vx0
                                 vy0
                                                  vz0
                                                                     ax
##
      1.399884e-02
                       -1.025046e+00
                                        -6.470604e-01
                                                          3.611276e-02
##
                                                          break length
                 ay
                                  az
                                              break y
##
     -1.394579e-01
                       -6.398053e-02
                                        -4.295483e+00
                                                          3.159281e-01
##
                                                            trf num AB
                           spin rate trf num pitches
           spin dir
##
                       2.460692e-04
                                         1.804388e-02
                                                                     NA
      1.688166e-03
##
        trf_num_AS
                         trf_num_CH
                                           trf_num_CU
                                                            trf_num_EP
```

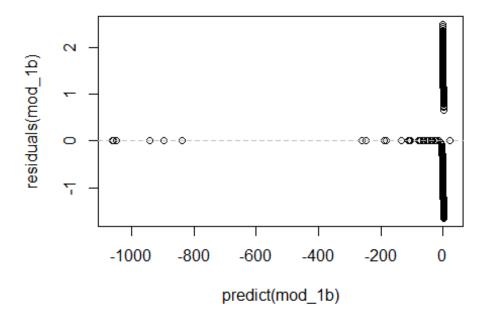
```
##
      1.990627e+01
                      -6.589889e-03
                                        5.426562e-03
                                                        -2.044280e-01
##
        trf num FA
                         trf num FC
                                          trf num FF
                                                           trf num FO
                                        1.001870e-02
##
     -3.212850e-01
                       4.582021e-04
                                                        -7.047383e-02
##
        trf_num_FS
                         trf_num_FT
                                          trf num IN
                                                           trf_num_KC
##
      3.050274e-03
                       2.911716e-03
                                       -7.008995e-02
                                                        -2.081670e-03
##
        trf_num_KN
                         trf_num_P0
                                          trf_num_SC
                                                           trf_num_SI
##
     -9.878404e+00
                       3.237507e-02
                                       -1.321116e+01
                                                        -3.657734e-03
##
                         trf_num_UN
        trf_num_SL
##
                      -7.346978e-03
      8.720584e-03
```

Odds Ratio

```
exp(mod_1b$coefficients);
##
                                                           start speed
       (Intercept)
                                   Х
                                                    У
##
      9.495889e+37
                       9.809108e-01
                                         1.025440e+00
                                                          2.698956e-01
##
         end speed
                                               sz bot
                              sz top
                                                                    рх
##
      9.764821e-01
                       7.983024e-01
                                         3.508529e+00
                                                          1.065463e+00
##
                                  x0
                                                   y0
                                                                    z0
                 pz
##
      4.991581e+00
                       9.374513e-01
                                                   NA
                                                          2.587402e-01
##
                vx0
                                 vy0
                                                  vz0
##
      1.014097e+00
                       3.587801e-01
                                         5.235827e-01
                                                          1.036773e+00
##
                                                          break length
                                              break y
                 ay
##
      8.698297e-01
                       9.380233e-01
                                         1.362999e-02
                                                          1.371532e+00
##
                           spin_rate trf_num_pitches
                                                            trf_num_AB
           spin dir
##
      1.001690e+00
                       1.000246e+00
                                        1.018208e+00
                                                                    NA
##
        trf_num_AS
                         trf_num_CH
                                          trf_num_CU
                                                            trf_num_EP
##
      4.417553e+08
                       9.934318e-01
                                         1.005441e+00
                                                          8.151135e-01
##
        trf num FA
                         trf num FC
                                          trf num FF
                                                            trf_num_F0
##
      7.252165e-01
                       1.000458e+00
                                         1.010069e+00
                                                          9.319521e-01
##
        trf num FS
                         trf num FT
                                          trf num IN
                                                            trf num KC
##
      1.003055e+00
                       1.002916e+00
                                        9.323100e-01
                                                          9.979205e-01
##
        trf_num_KN
                         trf_num_P0
                                           trf_num_SC
                                                            trf_num_SI
##
      5.127003e-05
                       1.032905e+00
                                         1.830061e-06
                                                          9.963489e-01
##
        trf_num_SL
                         trf_num_UN
##
      1.008759e+00
                       9.926799e-01
```

Residual

```
plot(predict(mod_1b), residuals(mod_1b));
abline(h=0,lty=2,col="grey");
```



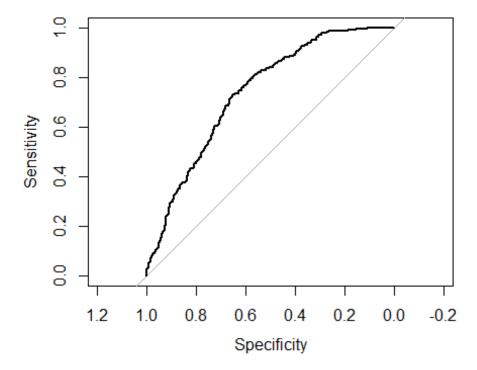
Performance

```
pred <- ifelse(predict(mod_1b, testing_lessOutliers, type='response') > thres
hold, 1, 0)
confusionMatrix(data=pred, reference=testing_lessOutliers$OnDL, positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
##
            0 678 174
            1 91 87
##
##
##
                  Accuracy : 0.7427
                    95% CI: (0.7149, 0.7692)
##
##
       No Information Rate : 0.7466
       P-Value [Acc > NIR] : 0.6284
##
##
##
                     Kappa: 0.2402
##
    Mcnemar's Test P-Value: 4.723e-07
##
##
               Sensitivity: 0.33333
##
               Specificity: 0.88166
##
            Pos Pred Value: 0.48876
##
            Neg Pred Value: 0.79577
##
                Prevalence: 0.25340
```

```
## Detection Rate : 0.08447
## Detection Prevalence : 0.17282
## Balanced Accuracy : 0.60750
##
## 'Positive' Class : 1
##
```

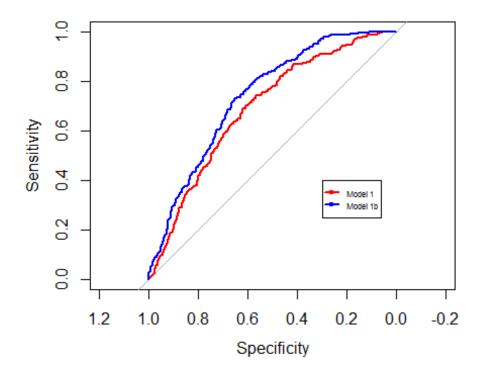
ROC curve

```
prob <- predict(mod_1b, testing_lessOutliers, type='response');
g1b <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit =F)
## Area under the curve (AUC): 0.738
plot(g1b)</pre>
```



Compare ROC of model with outliers vs model without outliers

The comparison of the ROC curve between the model with outliers (red) and one without outliers (blue) shows that the model has better performance once outliers are removed.



Model 2 Only low correlation variables (less than 0.25)

Low correlation variables

Construct Model

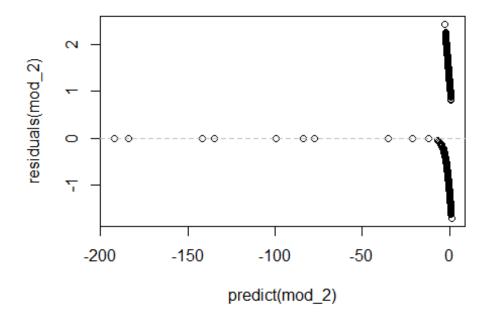
```
mod_2 = glm(formula = formula , family=binomial(logit), data=training_lessOut
liers);
```

Summary

```
summary(mod_2);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training_lessOutli
ers)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
          -0.7253
                    -0.5435
                             -0.3083
                                       2.4255
## -1.6961
##
## Coefficients: (1 not defined because of singularities)
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 65.165651 249.595378
                                      0.261 0.79403
                                      0.239
                                            0.81131
## X
                0.001452
                           0.006082
## sz_top
                0.720973
                           0.904091
                                      0.797
                                            0.42519
## pz
               -0.467048
                           0.239939 -1.947 0.05159
## x0
               -0.024572
                           0.027743 -0.886 0.37578
                           0.032356 -4.702 2.58e-06 ***
               -0.152128
## vz0
## break_y
               -2.395364
                           1.647853 -1.454 0.14605
## trf num AB
                      NA
                                 NA
                                         NA
                                                  NA
                           0.003773
## trf_num_CU
                0.006271
                                      1.662 0.09649
## trf_num_EP
               -0.224243
                           0.116947 -1.917 0.05518
                           0.100639 -2.813 0.00490 **
## trf_num_FA
              -0.283122
## trf num FF
                0.019190
                           0.003042
                                     6.308 2.82e-10 ***
## trf num FO
               -0.131495
                           0.277602 -0.474 0.63573
## trf num FT
                                     4.225 2.39e-05 ***
                0.011969
                           0.002833
## trf_num_IN
              -0.029048
                           0.019056 -1.524 0.12742
## trf_num_PO
                                    0.814 0.41549
              0.041881
                           0.051433
## trf_num_SC
               -9.763217 201.230702 -0.049 0.96130
## trf_num_UN
                0.012164
                           0.003798
                                      3.203 0.00136 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 3345.5
                             on 3089
                                      degrees of freedom
## Residual deviance: 3018.0 on 3073
                                      degrees of freedom
## AIC: 3052
## Number of Fisher Scoring iterations: 16
```

Residual

```
plot(predict(mod_2),residuals(mod_2));
abline(h=0,lty=2,col="grey");
```



COefficients

```
mod 2$coefficients;
   (Intercept)
                                   sz_top
                                                                  x0
                                                     pz
## 65.165650877
                              0.720972800 -0.467047727 -0.024571987
                 0.001451894
##
            vz0
                     break y
                               trf_num_AB
                                             trf num CU
                                                          trf num EP
## -0.152127964 -2.395363802
                                            0.006271082 -0.224243237
                                        NA
    trf_num_FA
                  trf_num_FF
                                            trf_num_FT
                                                          trf_num_IN
##
                               trf_num_F0
## -0.283122269 0.019189752 -0.131495281
                                            0.011968967 -0.029048234
    trf_num_PO
                 trf_num_SC
                               trf_num_UN
##
    0.041880740 -9.763217477 0.012163559
```

Odds ratio

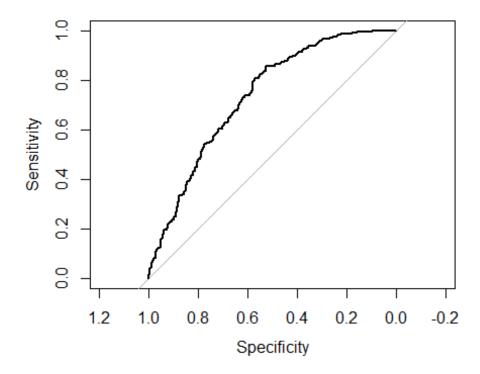
```
exp(mod_2$coefficients);
  (Intercept)
                                                                  x0
                           Х
                                   sz_top
                                                     pz
## 2.000242e+28 1.001453e+00 2.056433e+00 6.268502e-01 9.757274e-01
##
            vz0
                     break y
                               trf num AB
                                             trf num CU
                                                          trf num EP
## 8.588784e-01 9.113952e-02
                                        NA 1.006291e+00 7.991207e-01
                               trf_num_F0
                  trf num FF
                                             trf_num_FT
    trf_num_FA
                                                          trf_num_IN
## 7.534277e-01 1.019375e+00 8.767834e-01 1.012041e+00 9.713696e-01
     trf num PO
                  trf_num_SC
                               trf_num_UN
## 1.042770e+00 5.752923e-05 1.012238e+00
```

Performance

```
pred <- ifelse(predict(mod_2, testing_lessOutliers, type='response') > thresh
old, 1, 0);
confusionMatrix(data=pred, reference=testing lessOutliers$OnDL, positive='1')
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                0
                    1
##
            0 688 196
            1 81 65
##
##
##
                  Accuracy : 0.7311
##
                    95% CI: (0.7029, 0.7579)
       No Information Rate : 0.7466
##
##
       P-Value [Acc > NIR] : 0.881
##
##
                     Kappa : 0.1682
##
   Mcnemar's Test P-Value : 7.406e-12
##
               Sensitivity: 0.24904
##
               Specificity: 0.89467
##
##
            Pos Pred Value : 0.44521
##
            Neg Pred Value: 0.77828
##
                Prevalence: 0.25340
##
            Detection Rate: 0.06311
##
      Detection Prevalence: 0.14175
##
         Balanced Accuracy: 0.57186
##
          'Positive' Class : 1
##
##
```

ROC curve

```
prob <- predict(mod_2, testing_lessOutliers, type='response');
g2 <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit = F);
## Area under the curve (AUC): 0.734
plot(g2)</pre>
```



Model 2(b) Only low correlation variables (less than 0.5)

Low correlation variables

```
highlyCorDescr <- findCorrelation(m_lessOutliers, cutoff = .5)

lowCorColNames<- colnames(numeric_dataset[,-highlyCorDescr]);

print(lowCorColNames);

## [1] "sz_top" "px" "pz" "x0" "z0"

## [6] "ay" "break_y" "spin_rate" "trf_num_AB" "trf_num_AS"

## [11] "trf_num_CH" "trf_num_EP" "trf_num_FA" "trf_num_FF" "trf_num_FO"

## [16] "trf_num_FS" "trf_num_FT" "trf_num_IN" "trf_num_KC" "trf_num_KN"

## [21] "trf_num_PO" "trf_num_SC" "trf_num_SI" "trf_num_UN"
```

Construct Model

```
mod_2b = glm(formula = formula , family=binomial(logit), data=training_lessOu
tliers);
```

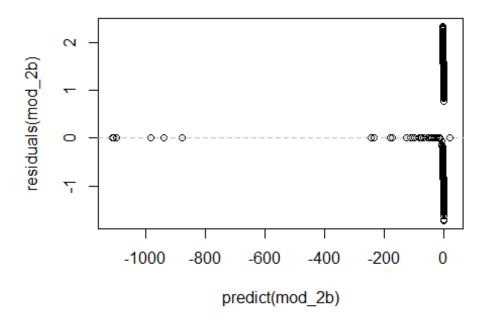
Summary

```
summary(mod_2b);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training_lessOutli
ers)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
           -0.7251
                    -0.5341
                             -0.2341
## -1.7172
                                       2.3303
##
## Coefficients: (1 not defined because of singularities)
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -2.013e+01
                         1.941e+04 -0.001 0.999172
               5.412e-01 8.885e-01
## sz top
                                      0.609 0.542424
## px
               7.273e-01 2.483e-01
                                      2.929 0.003402 **
                                     -2.662 0.007778 **
## pz
               -6.711e-01
                         2.522e-01
## x0
               -8.171e-03 2.957e-02 -0.276 0.782308
                                      2.475 0.013319 *
## z0
               2.890e-01 1.168e-01
## ay
               9.663e-02 2.728e-02
                                      3.542 0.000397 ***
## break y
               7.546e-01 1.877e+00
                                      0.402 0.687755
## spin_rate
               3.942e-05 1.956e-04
                                      0.202 0.840266
## trf_num_AB
                      NA
                                 NA
                                         NA
                                                  NA
## trf num AS
               1.948e+01 1.582e+04
                                      0.001 0.999018
## trf num CH
               -6.219e-03 5.001e-03
                                     -1.244 0.213621
## trf num EP
               -2.006e-01 1.198e-01
                                     -1.675 0.094014
## trf num FA
              -2.956e-01 1.036e-01 -2.853 0.004329 **
                                     7.873 3.45e-15 ***
## trf_num_FF
               2.764e-02 3.511e-03
## trf_num_FO
              -1.471e-01 3.005e-01 -0.490 0.624463
## trf_num_FS
               4.882e-03 6.628e-03
                                      0.737 0.461358
               2.047e-02 3.412e-03
                                      5.999 1.99e-09 ***
## trf_num_FT
## trf_num_IN
              -5.681e-02 1.956e-02 -2.905 0.003670 **
## trf num KC
               -4.111e-03 5.666e-03 -0.725 0.468177
## trf num KN
              -1.036e+01
                          2.377e+02
                                     -0.044 0.965251
## trf_num_PO
               9.465e-03 5.221e-02
                                      0.181 0.856149
## trf_num_SC
              -1.244e+01 8.730e+02 -0.014 0.988627
## trf num SI
               1.504e-02 3.443e-03
                                      4.368 1.25e-05 ***
## trf_num_UN
               4.738e-03 3.990e-03
                                      1.188 0.234980
## ---
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3345.5
                                      degrees of freedom
                             on 3089
## Residual deviance: 2976.2 on 3066 degrees of freedom
## AIC: 3024.2
```

```
##
## Number of Fisher Scoring iterations: 19
```

Residual

```
plot(predict(mod_2b), residuals(mod_2b));
abline(h=0,lty=2,col="grey");
```



COefficients

```
mod 2b$coefficients;
##
     (Intercept)
                                                                        x0
                        sz top
                                           рх
                                                          pz
## -2.013386e+01
                  5.412250e-01
                                 7.272884e-01 -6.711160e-01 -8.170812e-03
##
                                                                trf_num_AB
              z0
                                      break y
                                                  spin rate
                             ay
##
    2.890383e-01
                  9.663075e-02
                                7.545614e-01
                                               3.941815e-05
                                                                        NA
##
      trf_num_AS
                    trf_num_CH
                                   trf_num_EP
                                                 trf_num_FA
                                                                trf_num_FF
    1.948419e+01 -6.219403e-03 -2.005616e-01 -2.955782e-01
                                                              2.764281e-02
##
##
      trf num FO
                    trf num FS
                                   trf num FT
                                                 trf_num_IN
                                                                trf num KC
## -1.470926e-01
                  4.882289e-03
                                 2.046642e-02 -5.681122e-02 -4.110602e-03
##
      trf num KN
                    trf num PO
                                   trf num SC
                                                 trf num SI
                                                                trf num UN
## -1.035637e+01
                  9.464679e-03 -1.244472e+01 1.503747e-02 4.738141e-03
```

Odds ratio

```
exp(mod_2b$coefficients);
## (Intercept) sz_top px pz x0
## 1.802916e-09 1.718110e+00 2.069461e+00 5.111378e-01 9.918625e-01
## z0 ay break_y spin_rate trf_num_AB
```

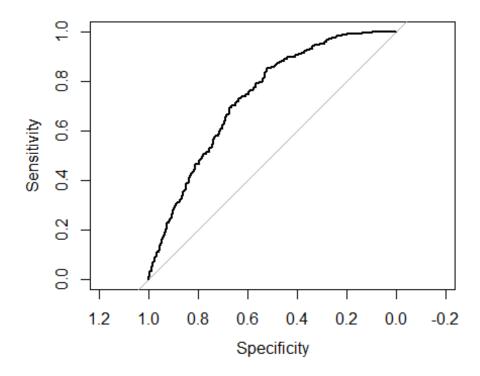
```
## 1.335143e+00 1.101454e+00 2.126679e+00 1.000039e+00
                 trf num CH
                              trf num EP
    trf num AS
                                           trf num FA
                                                        trf num FF
## 2.896521e+08 9.937999e-01 8.182710e-01 7.441013e-01 1.028028e+00
                 trf num FS
    trf num FO
                              trf num FT
                                           trf num IN
                                                        trf num KC
## 8.632140e-01 1.004894e+00 1.020677e+00 9.447724e-01 9.958978e-01
    trf num KN
                 trf_num_PO
                              trf_num_SC
                                           trf_num_SI
                                                        trf_num_UN
## 3.178965e-05 1.009510e+00 3.938474e-06 1.015151e+00 1.004749e+00
```

Performance

```
pred <- ifelse(predict(mod_2b, testing_lessOutliers, type='response') > thres
hold, 1, 0);
confusionMatrix(data=pred, reference=testing lessOutliers$OnDL, positive='1')
;
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
            0 688 184
##
            1 81 77
##
##
                  Accuracy : 0.7427
                    95% CI: (0.7149, 0.7692)
##
##
       No Information Rate: 0.7466
##
       P-Value [Acc > NIR] : 0.6284
##
##
                     Kappa : 0.2181
   Mcnemar's Test P-Value : 3.709e-10
##
##
##
               Sensitivity: 0.29502
               Specificity: 0.89467
##
            Pos Pred Value: 0.48734
##
            Neg Pred Value: 0.78899
##
##
                Prevalence: 0.25340
##
            Detection Rate: 0.07476
##
      Detection Prevalence: 0.15340
##
         Balanced Accuracy: 0.59484
##
##
          'Positive' Class : 1
##
```

ROC curve

```
prob <- predict(mod_2b, testing_lessOutliers, type='response');
g2b <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit = F);
## Area under the curve (AUC): 0.735
plot(g2b)</pre>
```



Model 2(c) Only low correlation variables (less than 0.75)

Low correlation variables

```
highlyCorDescr <- findCorrelation(m_lessOutliers, cutoff = .75);</pre>
lowCorColNames <- colnames(numeric_dataset_lessOutliers[,-highlyCorDescr]);</pre>
#filter_pitches_dl_dataset <- filteredDescr[,-highlyCorDescr]</pre>
#all_variables <- colnames(numeric_dataset);</pre>
print(lowCorColNames);
   [1] "x"
                                    "sz top"
                                                 "sz_bot"
                                                               "px"
##
##
   [6] "pz"
                      "z0"
                                    "vx0"
                                                               "az"
                      "spin_rate" "trf_num_AS" "trf_num_CH" "trf_num_CU"
## [11] "break_y"
## [16] "trf_num_EP" "trf_num_FA" "trf_num_FC" "trf_num_FF" "trf_num_FO"
## [21] "trf_num_FS" "trf_num_FT" "trf_num_IN" "trf_num_KC" "trf_num_KN"
## [26] "trf_num_PO" "trf_num_SC" "trf_num_SI" "trf_num_SL"
```

Construct Model

```
selected_variables <- lowCorColNames;
selected_i <- which(colnames(training) %in% selected_variables);
formula_text <- paste(response_var, "~",</pre>
```

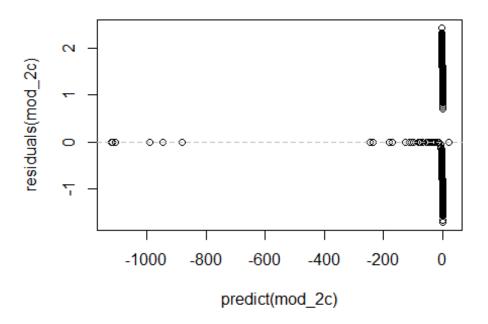
```
paste(names(training lessOutliers)[selected i], collaps
e="+"));
formula <- as.formula(formula_text);</pre>
mod_2c = glm(formula = formula , family=binomial(logit), data=training_lessOu
tliers);
Summary
summary(mod 2c);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training_lessOutli
ers)
##
## Deviance Residuals:
      Min
                1Q
                     Median
                                  3Q
                                          Max
                    -0.5256 -0.2240
## -1.7091
           -0.7280
                                       2.4339
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
                         1.941e+04 -0.001 0.998844
## (Intercept) -2.813e+01
## X
              -2.709e-02 2.024e-02 -1.338 0.180755
## y
               3.107e-02 1.307e-02
                                      2.377 0.017431 *
## sz top
               -2.171e-01 8.399e-01 -0.259 0.796017
## sz bot
               2.763e-01 1.050e+00
                                      0.263 0.792530
               -7.305e-02 6.004e-01 -0.122 0.903156
## px
               6.976e-02 3.797e-01
## pz
                                      0.184 0.854236
## z0
               3.181e-01 1.280e-01
                                      2.485 0.012949 *
## vx0
              -1.930e-04 9.099e-03 -0.021 0.983078
               1.082e-01 2.900e-02 3.731 0.000191 ***
## ay
## az
               -1.993e-02 1.916e-02 -1.040 0.298275
## break y
               9.775e-01 1.908e+00
                                      0.512 0.608425
## spin rate
               2.693e-04 2.436e-04
                                      1.105 0.268963
## trf_num_AS
               1.949e+01 1.582e+04
                                      0.001 0.999017
## trf_num_CH
              -6.668e-03 5.034e-03 -1.325 0.185325
## trf num CU
               2.059e-03 4.711e-03
                                      0.437 0.662108
## trf_num_EP
               -2.198e-01 1.236e-01 -1.778 0.075402
              -3.088e-01 1.046e-01 -2.952 0.003162 **
## trf_num_FA
               8.043e-03 4.013e-03
                                      2.004 0.045063 *
## trf_num_FC
                                      6.081 1.19e-09 ***
## trf_num_FF
               2.571e-02 4.227e-03
## trf num FO
              -1.258e-01
                          2.958e-01 -0.425 0.670727
## trf num FS
               4.370e-03 6.745e-03
                                      0.648 0.517059
## trf_num_FT
               1.729e-02 3.812e-03
                                      4.535 5.77e-06 ***
              -6.094e-02 1.972e-02 -3.090 0.002003 **
## trf num IN
## trf_num_KC
               -3.521e-03 6.457e-03 -0.545 0.585570
## trf_num_KN
              -1.041e+01 2.354e+02 -0.044 0.964725
## trf num PO
               1.520e-02 5.289e-02
                                      0.287 0.773757
## trf num SC
              -1.247e+01 8.749e+02 -0.014 0.988629
```

trf num SI 1.128e-02 4.006e-03 2.815 0.004878 **

```
## trf num SL 7.549e-03 4.098e-03
                                      1.842 0.065428 .
## ---
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3345.5
                             on 3089
                                      degrees of freedom
## Residual deviance: 2959.9 on 3060
                                       degrees of freedom
## AIC: 3019.9
##
## Number of Fisher Scoring iterations: 19
```

Residual

```
plot(predict(mod_2c),residuals(mod_2c));
abline(h=0,lty=2,col="grey");
```



COefficients

```
mod 2c$coefficients;
     (Intercept)
##
                                                                    sz_bot
                              Х
                                                      sz_top
## -2.813061e+01 -2.708802e-02
                                3.106750e-02 -2.171255e-01
                                                              2.762835e-01
##
                                           z0
                                                         vx0
              рх
                             pz
                                                                         ay
## -7.304863e-02
                  6.976023e-02
                                3.181179e-01 -1.929885e-04
                                                              1.081875e-01
                       break_y
##
                                    spin_rate
                                                 trf_num_AS
                                                                trf_num_CH
              az
## -1.993275e-02
                  9.774508e-01
                                 2.692993e-04
                                               1.948753e+01 -6.667687e-03
                    trf_num_EP
                                                 trf_num_FC
      trf_num_CU
                                   trf_num_FA
                                                                trf_num_FF
```

```
2.058678e-03 -2.198445e-01 -3.087691e-01 8.043021e-03
                                                           2.570561e-02
##
     trf num FO
                   trf num FS
                                 trf num FT
                                               trf num IN
                                                             trf num KC
## -1.257593e-01 4.369897e-03 1.728698e-02 -6.093793e-02 -3.521058e-03
                                               trf num SI
     trf num KN
                 trf num PO
                                 trf num SC
                                                             trf num SL
## -1.041132e+01 1.520469e-02 -1.246918e+01 1.127814e-02 7.549246e-03
Performance
pred <- ifelse(predict(mod_2c, testing_lessOutliers, type='response') > thres
hold, 1, 0);
confusionMatrix(data=pred, reference=testing_lessOutliers$OnDL, positive='1')
## Confusion Matrix and Statistics
##
            Reference
##
               0
## Prediction
                   1
##
           0 680 189
##
           1 89 72
##
##
                 Accuracy : 0.7301
##
                   95% CI: (0.7019, 0.757)
##
       No Information Rate: 0.7466
      P-Value [Acc > NIR] : 0.8944
##
```

Kappa : 0.1833

Sensitivity: 0.2759

Specificity: 0.8843

Pos Pred Value: 0.4472

Neg Pred Value : 0.7825 Prevalence : 0.2534

Detection Rate: 0.0699

Detection Prevalence: 0.1563

'Positive' Class : 1

Balanced Accuracy: 0.5801

Mcnemar's Test P-Value : 2.892e-09

ROC curve

##

##

##

##

##

##

##

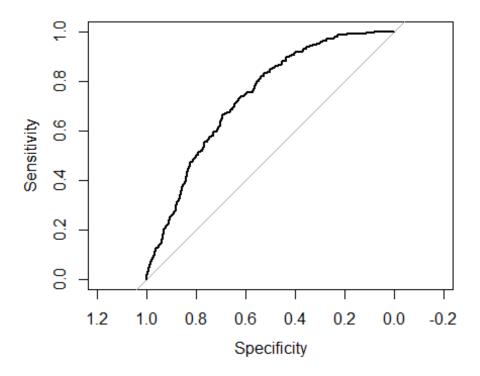
##

##

##

##

```
prob <- predict(mod_2c, testing_lessOutliers, type='response');
g2c <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit = F)
## Area under the curve (AUC): 0.736
plot(g2c)</pre>
```



Model 2(d) Only low correlation variables (less than 0.85)

Low correlation variables

```
highlyCorDescr <- findCorrelation(m_lessOutliers, cutoff =0.85);</pre>
lowCorColNames <- colnames(numeric_dataset_lessOutliers[,-highlyCorDescr]);</pre>
#filter_pitches_dl_dataset <- filteredDescr[,-highlyCorDescr]</pre>
#all_variables <- colnames(numeric_dataset);</pre>
print(lowCorColNames);
                            "y"
    [1] "x"
##
                                               "end_speed"
    [4]
        "sz_top"
                            "sz_bot"
                                               "px"
##
    [7] "pz"
                            "z0"
                                               "vx0"
##
## [10] "vz0"
                            "ay"
                                               "az"
## [13] "break_y"
                            "spin_rate"
                                               "trf_num_pitches"
## [16] "trf_num_AS"
                            "trf_num_CH"
                                               "trf_num_CU"
## [19] "trf_num_EP"
                            "trf_num_FA"
                                               "trf num FC"
                                               "trf_num_FS"
## [22] "trf_num_FF"
                            "trf num FO"
                            "trf_num_IN"
                                               "trf_num_KC"
## [25] "trf_num_FT"
## [28] "trf_num_KN"
                            "trf_num_PO"
                                               "trf_num_SC"
## [31] "trf num SI"
                            "trf num SL"
```

Construct Model

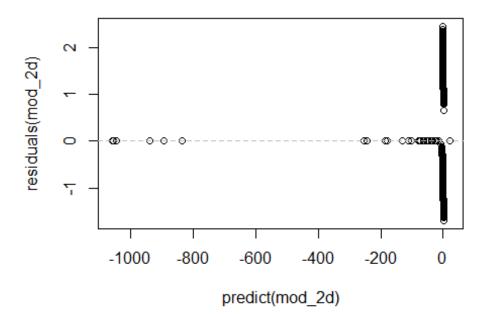
Summary

```
summary(mod_2d);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training lessOutli
##
## Deviance Residuals:
                1Q
                    Median
                                 3Q
      Min
                                         Max
## -1.6953 -0.7265 -0.5076 -0.1613
                                      2.4513
##
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
                   8.086e+01 1.941e+04
                                         0.004 0.996676
## (Intercept)
## X
                  -2.148e-02 2.028e-02 -1.059 0.289458
                   2.628e-02 1.308e-02 2.008 0.044595 *
## y
                   1.271e-01 3.646e-02 3.485 0.000492 ***
## end_speed
## sz_top
                  -2.695e-01 1.062e+00 -0.254 0.799664
## sz bot
                   1.269e+00 1.088e+00 1.166 0.243416
## px
                   8.385e-02 5.972e-01 0.140 0.888343
                   1.437e+00 5.271e-01 2.726 0.006401 **
## pz
## z0
                  -1.137e+00 4.344e-01 -2.616 0.008885 **
## vx0
                  -1.161e-02 9.446e-03 -1.229 0.219073
                  -5.541e-01 1.569e-01 -3.532 0.000412 ***
## vz0
                  -8.587e-02 4.104e-02 -2.092 0.036427 *
## ay
## az
                  -1.236e-01 3.085e-02 -4.005
                                                6.2e-05 ***
## break y
                  -3.890e+00 2.094e+00 -1.857 0.063249 .
## spin_rate
                   3.544e-04 2.459e-04 1.441 0.149553
## trf_num_pitches 1.397e-02 9.447e-03 1.479 0.139142
                   1.998e+01 1.582e+04
## trf num AS
                                         0.001 0.998993
## trf num CH
                  -5.264e-03 6.314e-03 -0.834 0.404403
## trf num CU
                  5.516e-03 5.821e-03
                                        0.948 0.343335
## trf num EP
                  -2.093e-01 1.241e-01 -1.687 0.091592 .
## trf_num_FA
                  -3.115e-01 1.056e-01 -2.949 0.003185 **
## trf_num_FC
               2.916e-03 5.205e-03 0.560 0.575280
```

```
## trf num FF
                    1.153e-02
                               7.379e-03
                                           1.563 0.118078
## trf num FO
                   -5.915e-02 2.892e-01
                                          -0.205 0.837960
## trf_num_FS
                    3.038e-03
                               7.642e-03
                                           0.398 0.690997
## trf_num_FT
                               5.361e-03
                    5.631e-03
                                           1.050 0.293493
## trf_num_IN
                   -6.793e-02
                               2.034e-02
                                          -3.340 0.000838 ***
## trf_num_KC
                   -9.364e-04
                               7.354e-03
                                          -0.127 0.898675
## trf num KN
                   -9.848e+00
                               2.302e+02
                                          -0.043 0.965874
## trf_num_PO
                    2.881e-02
                               5.343e-02
                                           0.539 0.589717
## trf_num_SC
                   -1.291e+01
                               8.653e+02
                                          -0.015 0.988094
## trf num SI
                   -1.352e-03
                               6.268e-03
                                          -0.216 0.829158
## trf_num_SL
                    4.945e-03 5.532e-03
                                           0.894 0.371385
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3345.5
                              on 3089
                                       degrees of freedom
## Residual deviance: 2910.1
                             on 3057
                                       degrees of freedom
## AIC: 2976.1
##
## Number of Fisher Scoring iterations: 19
```

Residual

```
plot(predict(mod_2d),residuals(mod_2d));
abline(h=0,lty=2,col="grey");
```



COefficients

```
exp(mod_2d$coefficients);
##
       (Intercept)
                                   Х
                                                    У
                                                            end speed
##
      1.309692e+35
                       9.787465e-01
                                        1.026627e+00
                                                         1.135513e+00
##
            sz top
                             sz bot
                                                   рх
                                                                    pz
##
      7.637463e-01
                       3.558145e+00
                                        1.087466e+00
                                                         4.208748e+00
##
                 z0
                                 vx0
                                                  vz0
                                                                    ay
##
      3.209218e-01
                       9.884575e-01
                                        5.745706e-01
                                                         9.177123e-01
##
                 az
                            break_y
                                           spin_rate trf_num_pitches
##
      8.837658e-01
                       2.044149e-02
                                        1.000354e+00
                                                         1.014070e+00
##
        trf_num_AS
                         trf_num_CH
                                          trf_num_CU
                                                           trf_num_EP
##
                       9.947494e-01
                                                         8.111271e-01
      4.738614e+08
                                        1.005531e+00
##
        trf_num_FA
                         trf_num_FC
                                                           trf_num_F0
                                          trf num FF
##
                       1.002920e+00
      7.323249e-01
                                        1.011600e+00
                                                         9.425663e-01
##
        trf_num_FS
                         trf_num_FT
                                          trf_num_IN
                                                           trf_num_KC
##
      1.003043e+00
                       1.005647e+00
                                        9.343268e-01
                                                         9.990641e-01
##
        trf num KN
                         trf num PO
                                          trf num SC
                                                           trf num SI
##
      5.284055e-05
                       1.029233e+00
                                        2.464992e-06
                                                         9.986484e-01
##
        trf_num_SL
##
      1.004957e+00
```

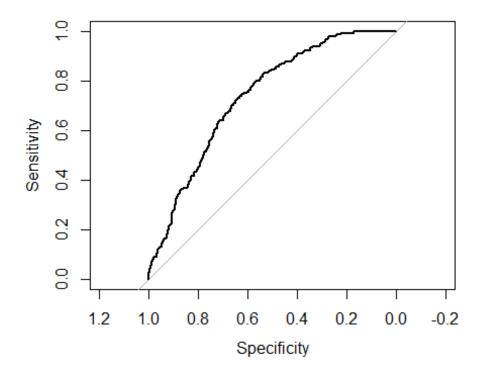
Performance

```
pred <- ifelse(predict(mod_2d, testing_lessOutliers, type='response') > thres
confusionMatrix(data=pred, reference=testing lessOutliers$OnDL, positive='1')
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                0
##
            0 677 174
##
            1 92 87
##
##
                  Accuracy : 0.7417
##
                    95% CI: (0.7139, 0.7682)
##
       No Information Rate: 0.7466
##
       P-Value [Acc > NIR] : 0.655
##
##
                     Kappa : 0.2384
##
    Mcnemar's Test P-Value : 6.82e-07
##
##
               Sensitivity: 0.33333
##
               Specificity: 0.88036
            Pos Pred Value: 0.48603
##
##
            Neg Pred Value: 0.79553
##
                Prevalence: 0.25340
##
            Detection Rate: 0.08447
      Detection Prevalence: 0.17379
##
```

```
## Balanced Accuracy : 0.60685
##
## 'Positive' Class : 1
##
```

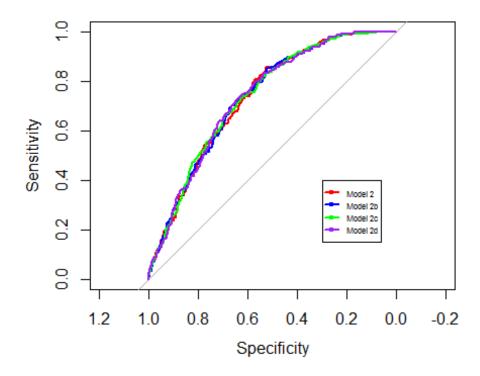
ROC curve

```
prob <- predict(mod_2d, testing_lessOutliers, type='response');
g2d <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit = F)
## Area under the curve (AUC): 0.736
plot(g2d)</pre>
```



Compare ROC Curve of model by correlation

```
plot(g2, col='red'); #cutoff 0.25
plot(g2b, add=TRUE, col='blue') #cutoff 0.5
plot(g2c, add=TRUE, col='green') #cutoff 0.75
plot(g2d, add=TRUE, col='purple') #cutoff 0.85
legend(0.3,0.4, c("Model 2","Model 2b","Model 2c", "Model 2d"), lty=c(1,1), lwd=c(2.5,2.5),col=c("red","blue","green", "purple"), pch=1, cex=0.5);
```



Model 3 Original continuous variables

Construct Model

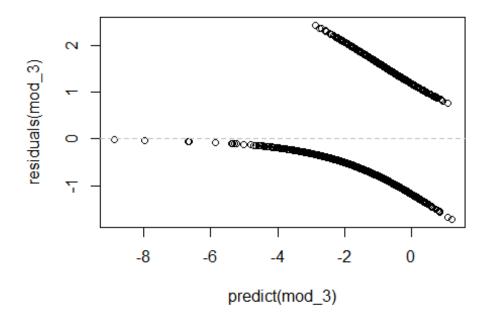
Summary

```
summary(mod_3);
##
## Call:
## glm(formula = formula, family = binomial(logit), data = training_lessOutli
ers)
##
## Deviance Residuals:
## Min    1Q    Median    3Q    Max
## -1.7124   -0.7388   -0.5148   -0.2044    2.4239
##
```

```
## Coefficients: (1 not defined because of singularities)
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   8.951e+01
                              4.913e+01
                                         1.822
                                                0.06846
                  -2.057e-02 2.072e-02 -0.992
## X
                                                0.32097
                   2.459e-02 1.340e-02
## y
                                        1.834
                                                0.06660 .
## start_speed
                  -1.166e+00 6.382e-01 -1.827
                                                0.06765 .
## end_speed
                  -6.360e-03 1.722e-01 -0.037
                                                0.97054
## sz_top
                  -3.317e-01
                              1.036e+00 -0.320
                                                0.74880
## sz_bot
                  1.298e+00 1.077e+00
                                        1.205
                                                0.22827
                                         0.286
                                                0.77463
## px
                   1.987e-01
                              6.938e-01
                                                0.00192 **
## pz
                   1.652e+00 5.323e-01
                                         3.103
## x0
                  -2.991e-01
                              3.855e-01 -0.776
                                                0.43785
## y0
                          NA
                                    NA
                                            NA
                                                     NA
## z0
                  -1.370e+00 4.224e-01
                                        -3.243
                                                0.00118 **
                  -7.884e-02 1.518e-01
                                        -0.519
## vx0
                                                0.60356
## vy0
                  -9.135e-01 4.475e-01 -2.041
                                                0.04120 *
## vz0
                  -6.350e-01
                              1.575e-01 -4.031 5.54e-05 ***
## ax
                  6.168e-03 3.448e-02
                                        0.179
                                                0.85803
                              5.504e-02 -2.674
## ay
                  -1.472e-01
                                                0.00749 **
## az
                 -5.634e-02 7.168e-02 -0.786
                                                0.43180
                 -4.462e+00 2.074e+00 -2.151
## break y
                                                0.03147 *
## break_length
                  2.084e-01 2.174e-01
                                         0.959
                                                0.33760
## spin dir
                  -2.112e-03 5.579e-03 -0.379
                                                0.70501
## spin rate
                   7.839e-05
                              3.400e-04
                                        0.231
                                                0.81766
## trf_num_pitches 2.083e-02 1.542e-03 13.507 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 3345.5 on 3089
                                     degrees of freedom
##
## Residual deviance: 2954.9
                            on 3068
                                     degrees of freedom
## AIC: 2998.9
## Number of Fisher Scoring iterations: 5
```

Residual

```
plot(predict(mod_3),residuals(mod_3));
abline(h=0,lty=2,col="grey");
```



COefficients

```
mod 3$coefficients;
##
       (Intercept)
                                                           start_speed
                                                    У
                                         2.458839e-02
##
      8.951037e+01
                       -2.056870e-02
                                                         -1.166118e+00
##
         end_speed
                              sz_top
                                               sz_bot
                                                                     рх
##
     -6.360043e-03
                       -3.317224e-01
                                         1.298170e+00
                                                          1.986510e-01
##
                 pz
                                  x0
                                                   y0
##
      1.651737e+00
                       -2.990770e-01
                                                   NA
                                                         -1.369666e+00
##
                vx0
                                                  vz0
                                 vy0
##
     -7.884158e-02
                       -9.135098e-01
                                        -6.349508e-01
                                                          6.167722e-03
                                                          break_length
##
                                              break_y
                 ay
##
                                        -4.461766e+00
     -1.471963e-01
                       -5.634498e-02
                                                          2.084452e-01
##
                           spin_rate trf_num_pitches
          spin_dir
                       7.839036e-05
                                        2.083002e-02
##
     -2.111879e-03
```

Odds Raio

```
exp(mod_3$coefficients);
##
       (Intercept)
                                                           start_speed
                                   Х
                                         1.024893e+00
##
      7.479279e+38
                       9.796414e-01
                                                          3.115742e-01
         end_speed
##
                              sz_top
                                               sz_bot
                                                                     рх
##
      9.936601e-01
                                         3.662588e+00
                       7.176866e-01
                                                          1.219756e+00
##
                                  x0
                                                    y0
                 pz
##
      5.216030e+00
                       7.415023e-01
                                                    NA
                                                          2.541918e-01
##
                vx0
                                                   vz0
                                 vy0
                                                                     ax
```

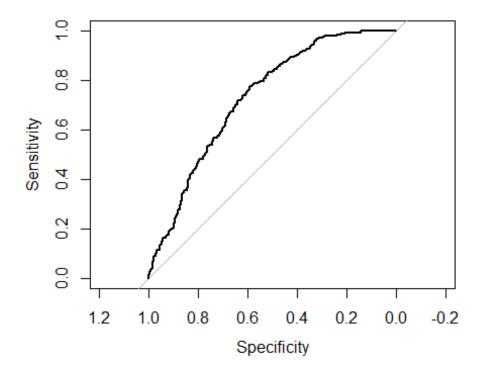
```
##
      9.241863e-01
                     4.011139e-01
                                      5.299615e-01
                                                     1.006187e+00
##
                                                     break length
                ay
                                az
                                          break y
      8.631246e-01
                                                     1.231761e+00
##
                     9.452130e-01
                                      1.154196e-02
##
                         spin rate trf num pitches
          spin dir
##
      9.978903e-01
                                     1.021048e+00
                     1.000078e+00
```

Performance

```
pred <- ifelse(predict(mod_3, testing_lessOutliers, type='response') > thresh
old, 1, 0);
confusionMatrix(data=pred, reference=testing_lessOutliers$OnDL, positive='1')
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                0
                    1
            0 668 180
##
##
            1 101 81
##
##
                  Accuracy : 0.7272
##
                    95% CI: (0.6989, 0.7542)
       No Information Rate: 0.7466
##
##
       P-Value [Acc > NIR] : 0.9281
##
##
                     Kappa : 0.1989
##
   Mcnemar's Test P-Value : 3.27e-06
##
               Sensitivity: 0.31034
##
##
               Specificity: 0.86866
##
            Pos Pred Value : 0.44505
##
            Neg Pred Value : 0.78774
                Prevalence: 0.25340
##
            Detection Rate: 0.07864
##
##
      Detection Prevalence: 0.17670
##
         Balanced Accuracy: 0.58950
##
##
          'Positive' Class : 1
##
```

ROC curve

```
prob <- predict(mod_3, testing_lessOutliers, type='response');
g3 <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit = F)
## Area under the curve (AUC): 0.729
plot(g3)</pre>
```



Model 3(b) Siginificant Continuous Variables + num pitches

Construct Model

Summary

```
summary(mod_3b);

##

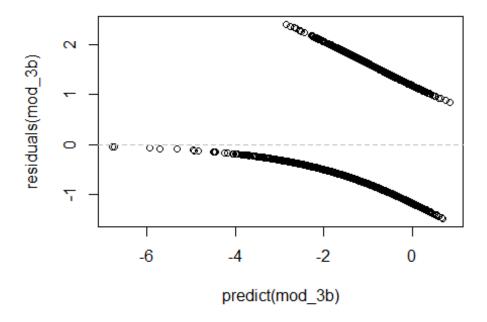
## Call:
## glm(formula = formula, family = binomial(logit), data = training_lessOutli
ers)
##

## Deviance Residuals:
## Min 1Q Median 3Q Max
## -1.4861 -0.7449 -0.5293 -0.2556 2.4066
```

```
##
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                    5.580861 39.454286
                                          0.141 0.88751
## start_speed
                   -0.609483
                               0.579532 -1.052 0.29295
## vy0
                   -0.486067
                               0.397291 -1.223
                                                 0.22116
## vz0
                   -0.110262
                               0.034178 -3.226
                                                 0.00125 **
                   -0.746877
                               1.650973
                                        -0.452
## break_y
                                                 0.65099
                                        14.793 < 2e-16 ***
## trf_num_pitches 0.021762
                               0.001471
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3345.5
                              on 3089
                                       degrees of freedom
## Residual deviance: 3005.3
                            on 3084
                                      degrees of freedom
## AIC: 3017.3
##
## Number of Fisher Scoring iterations: 5
```

Residual

```
plot(predict(mod_3b), residuals(mod_3b));
abline(h=0,lty=2,col="grey");
```



COefficients

mod_3b\$coefficients

```
##
       (Intercept)
                        start speed
                                                 vv0
                                                                  vz0
        5.58086102
##
                        -0.60948285
                                         -0.48606728
                                                          -0.11026238
##
           break_y trf_num_pitches
##
       -0.74687689
                         0.02176217
exp(mod 3b$coefficients);
##
       (Intercept)
                        start_speed
                                                 vy0
                                                                  vz0
       265.2999366
                                           0.6150404
##
                          0.5436319
                                                           0.8955991
##
           break_y trf_num_pitches
##
         0.4738441
                          1.0220007
```

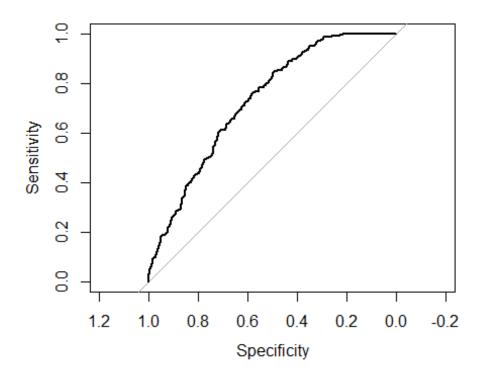
Performance

```
pred <- ifelse(predict(mod_3b, testing_lessOutliers, type='response') > thres
hold, 1, 0);
confusionMatrix(data=pred, reference=testing_lessOutliers$OnDL, positive='1')
;
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                0
                    1
##
            0 678 187
##
            1 91 74
##
##
                  Accuracy : 0.7301
                    95% CI: (0.7019, 0.757)
##
##
       No Information Rate: 0.7466
##
       P-Value [Acc > NIR] : 0.8944
##
##
                     Kappa: 0.188
   Mcnemar's Test P-Value : 1.214e-08
##
##
##
               Sensitivity: 0.28352
##
               Specificity: 0.88166
            Pos Pred Value: 0.44848
##
##
            Neg Pred Value: 0.78382
##
                Prevalence: 0.25340
##
            Detection Rate: 0.07184
      Detection Prevalence: 0.16019
##
##
         Balanced Accuracy: 0.58259
##
##
          'Positive' Class : 1
##
```

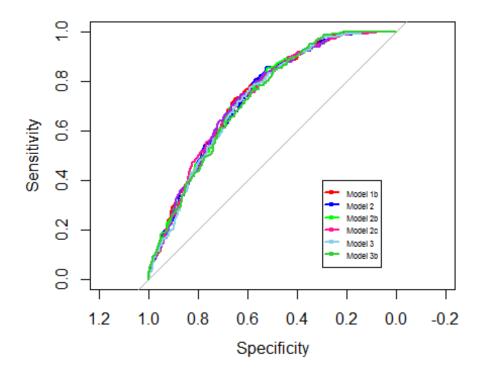
ROC curve

```
prob <- predict(mod_3b, testing_lessOutliers, type='response');
g3b <- roc(OnDL ~ prob, data = testing_lessOutliers);
roc.curve(testing_lessOutliers$OnDL, prob, plotit = F)</pre>
```

```
## Area under the curve (AUC): 0.729
plot(g3b)
```



Compare all models by ROC curve



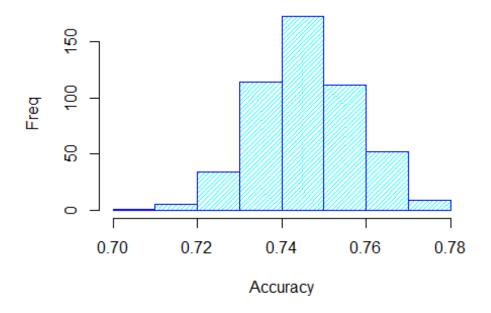
Cross Validation on significant variables

```
# highlyCorDescr <- findCorrelation(m_lessOutliers, cutoff = .85);</pre>
#
# lowCorColNames <- colnames(numeric_dataset_lessOutliers[,-highlyCorDescr]);</pre>
#
# #filter_pitches_dl_dataset <- filteredDescr[,-highlyCorDescr]</pre>
# #all_variables <- colnames(numeric_dataset);</pre>
# print(lowCorColNames);
selected_variables <- c("y","z0", "ay", "trf_num_FA", "trf_num_FC", "trf_num_</pre>
FF", "trf_num_FT", "trf_num_IN", "trf_num_SI");
selected_i <- which(colnames(training) %in% selected_variables);</pre>
formula_text <- paste(response_var, "~",</pre>
                        paste(names(training_lessOutliers)[selected_i], collaps
e="+"));
formula <- as.formula(formula_text);</pre>
# False positive rate
fpr <- NULL
```

```
# False negative rate
fnr <- NULL
# True positive rate
tpr <- NULL
# True negative rate
tnr <- NULL
auc <- NULL
# Number of iterations
k <- 500
# # Initialize progress bar
# pbar <- create_progress_bar('text')</pre>
# pbar$init(k)
# Accuracy
acc <- NULL
set.seed(123)
for(i in 1:k)
    # Train-test splitting
    # 95% of samples -> fitting
    # 5% of samples -> testing
    smp_size <- floor(0.75 * nrow(model_dataset_lessOutliers))</pre>
    index <- sample(seq_len(nrow(model_dataset_lessOutliers)), size=smp_size)</pre>
    train <- model_dataset_lessOutliers[index, ]</pre>
    test <- model dataset lessOutliers[-index, ]</pre>
    # Fitting
    model <- glm(formula=formula,family=binomial,data=model_dataset_lessOutli</pre>
ers)
    # Predict results
    results_prob <- predict(model,test,type='response')</pre>
    # If prob > 0.4 then 1, else 0
    results <- ifelse(results_prob > 0.4,1,0)
    # Actual answers
    answers <- test$OnDL;</pre>
```

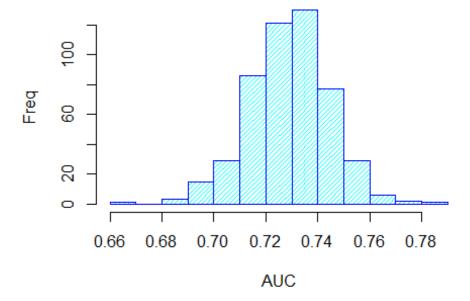
```
# Accuracy calculation
    misClasificError <- mean(answers != results)</pre>
    # Collecting results
    acc[i] <- 1-misClasificError</pre>
    # Confusion matrix
    cm <- confusionMatrix(data=results, reference=answers, positive='1')</pre>
    tnr[i] <- cm$table[1]/(cm$table[1]+cm$table[2])</pre>
    tpr[i] <- cm$table[4]/(cm$table[3]+cm$table[4])</pre>
    fpr[i] <- cm$table[2]/(cm$table[1]+cm$table[2])</pre>
    fnr[i] <- cm$table[3]/(cm$table[3]+cm$table[4])</pre>
    auc[i] <- roc.curve(test$OnDL, results_prob, plotit = F)$auc</pre>
    # pbar$step()
}
# Average accuracy of the model
mean(acc)
## [1] 0.7458835
# Average auc of the model
mean(auc)
## [1] 0.7289232
# Histogram of accuracy
hist(acc,xlab='Accuracy',ylab='Freq', col='cyan',border='blue',density=30)
```

Histogram of acc



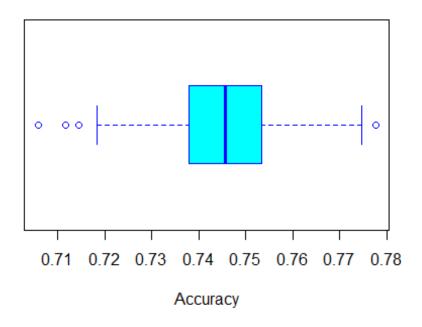
Histogram of auc
hist(auc,xlab='AUC',ylab='Freq', col='cyan',border='blue',density=30)

Histogram of auc



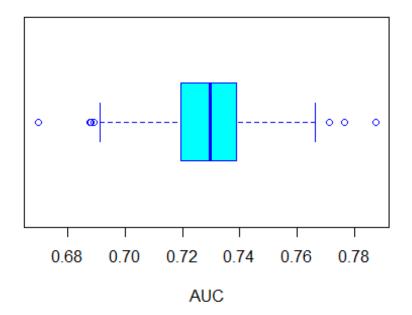
```
# Boxplot of accuracy
boxplot(acc,col='cyan',border='blue',horizontal=T,xlab='Accuracy', main='Accu
racy CV')
```

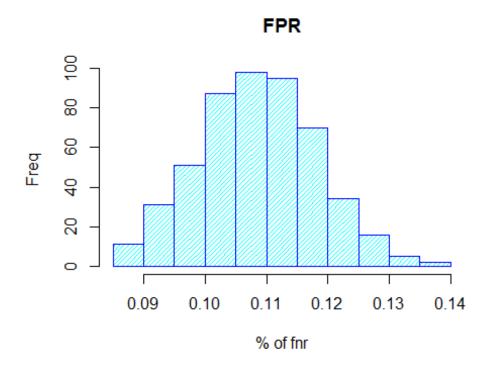
Accuracy CV

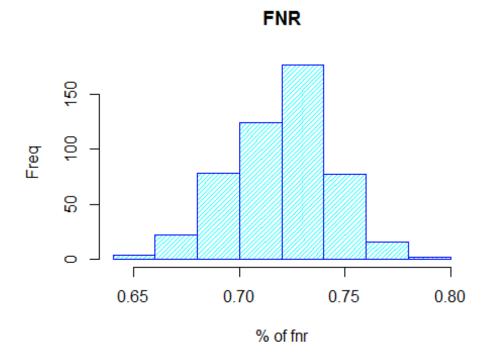


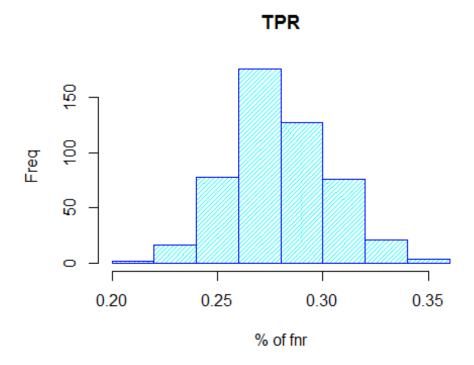
```
# Boxplot of auc
boxplot(auc,col='cyan',border='blue',horizontal=T,xlab='AUC', main='AUC CV')
```

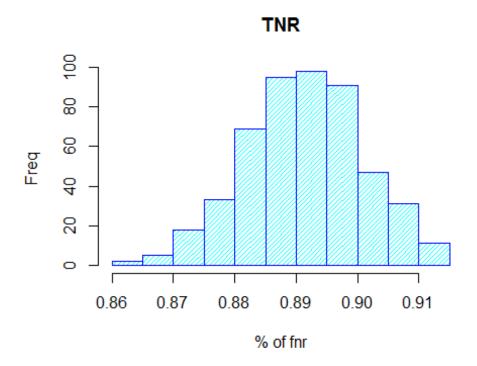
AUC CV











Predictions for 2017

Model 2b has the highest accuracry rate.

```
pred <- (predict(mod_2b, pitches_dl_predict, type='response'))*100;</pre>
predictions <- data.frame(rsid=pitches_dl_predict$rsID, probabilty=pred);</pre>
dbhandle <- odbcDriverConnect('driver={SQL Server};server=localhost;database=</pre>
Lahman; trusted connection=true');
query <- "SELECT retroID as rsid, nameFirst, nameLast FROM Master";</pre>
players <-sqlQuery(dbhandle, query);</pre>
predictions_players <- merge(x=predictions, y=players, by="rsid", all.x=TRUE)</pre>
head(predictions players[rev(order(predictions players$probabilty)),], 20);
##
           rsid probabilty nameFirst nameLast
## 201 happj001
                   78.69762
                                 J. A.
                                           Happ
## 170 gausk001
                   74.92285
                                 Kevin Gausman
## 437 sanca006
                   73.32695
                                 Aaron Sanchez
## 348 odorj001
                   72.10956
                                  Jake Odorizzi
```

341	nolar001	70.83420	Ricky	Nolasco
398	ray-r002	69.88841	Robbie	Ray
387	quinj001	66.97850	Jose	Quintana
241	jimeu001	65.75076	Ubaldo	Jimenez
276	lestj001	65.68297	Jon	Lester
371	perem004	65.51329	Martin	Perez
379	pinem001	65.34702	Michael	Pineda
370	peraw001	64.67090	Wily	Peralta
381	porcr001	64.59890	Rick	Porcello
15	arrij001	64.59393	Jake	Arrieta
199	hammj002	64.19380	Jason	Hammel
509	walkt004	64.17469	Taijuan	Walker
81	chatt001	63.70163	Tyler	Chatwood
252	kenni001	62.88287	Ian	Kennedy
472	strom001	62.70291	Marcus	Stroman
266	lackj001	61.72387	John	Lackey
	398 387 241 276 371 379 370 381 15 199 509 81 252 472	341 nolar001 398 ray-r002 387 quinj001 241 jimeu001 276 lestj001 371 perem004 379 pinem001 370 peraw001 381 porcr001 15 arrij001 199 hammj002 509 walkt004 81 chatt001 252 kenni001 472 strom001 266 lackj001	398 ray-r002 69.88841 387 quinj001 66.97850 241 jimeu001 65.75076 276 lestj001 65.68297 371 perem004 65.51329 379 pinem001 65.34702 370 peraw001 64.67090 381 porcr001 64.59890 15 arrij001 64.59393 199 hammj002 64.19380 509 walkt004 64.17469 81 chatt001 63.70163 252 kenni001 62.88287 472 strom001 66.97850	398 ray-r002 69.88841 Robbie 387 quinj001 66.97850 Jose 241 jimeu001 65.75076 Ubaldo 276 lestj001 65.68297 Jon 371 perem004 65.51329 Martin 379 pinem001 65.34702 Michael 370 peraw001 64.67090 Wily 381 porcr001 64.59890 Rick 15 arrij001 64.59393 Jake 15 hammj002 64.19380 Jason 509 walkt004 64.17469 Taijuan 81 chatt001 63.70163 Tyler 252 kenni001 62.88287 Ian 472 strom001 62.70291 Marcus