

Handouts are in  
the back

# The Big Ideas of CS 233

An Introduction to CS233

Late Add FAQ:

<https://wiki.illinois.edu/wiki/display/cs233fa17/Registration+FAQ>

clickers  
are for  
practice  
today

Welcome!!

# Class Mechanics on one Slide

- **Lectures:** bring pen/pencil + iclicker
  - See wiki for video lectures
- **Section/Lab:** bring pen/pencil, short quiz, start on Lab
- **Piazza:** how to ask questions (use good etiquette, follow the template)
- **Web Homeworks:** after every lecture in the beginning
  - Done individually
  - Numbers match the lecture number
- **Labs:** due weekly on Sunday nights
  - Can be done in groups (up to 2). Don't share code across groups.
- **Exams:** See the wiki
  - Second chance testing (read course policy)
- **Office hours:** normal deal

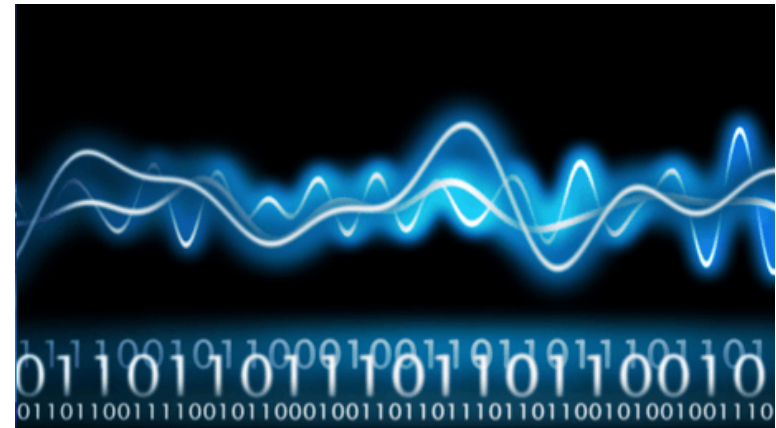
# Why I'm excited to be here



I will disappear for a couple weeks at some point this semester



iFoundry



# Why take CS 233?



# Why take CS 233? A warm-up i>clicker

Consider the following pieces of code that implement matrix multiplication, where A, B, and C, are all  $n \times n$  matrices and  $n$  is LARGE.

$$C = A * B$$

Which piece of code executes the matrix multiplication fastest?

Note: they all execute the algorithm correctly

a)

```
for (i=0; i<n; i++) {  
    for (j=0; j<n; j++) {  
        sum = 0.0;  
        for (k=0; k<n; k++)  
            sum += a[i][k] * b[k][j];  
        c[i][j] = sum;  
    }  
}
```

b)

```
for (k=0; k<n; k++) {  
    for (i=0; i<n; i++) {  
        r = a[i][k];  
        for (j=0; j<n; j++)  
            c[i][j] += r * b[k][j];  
    }  
}
```

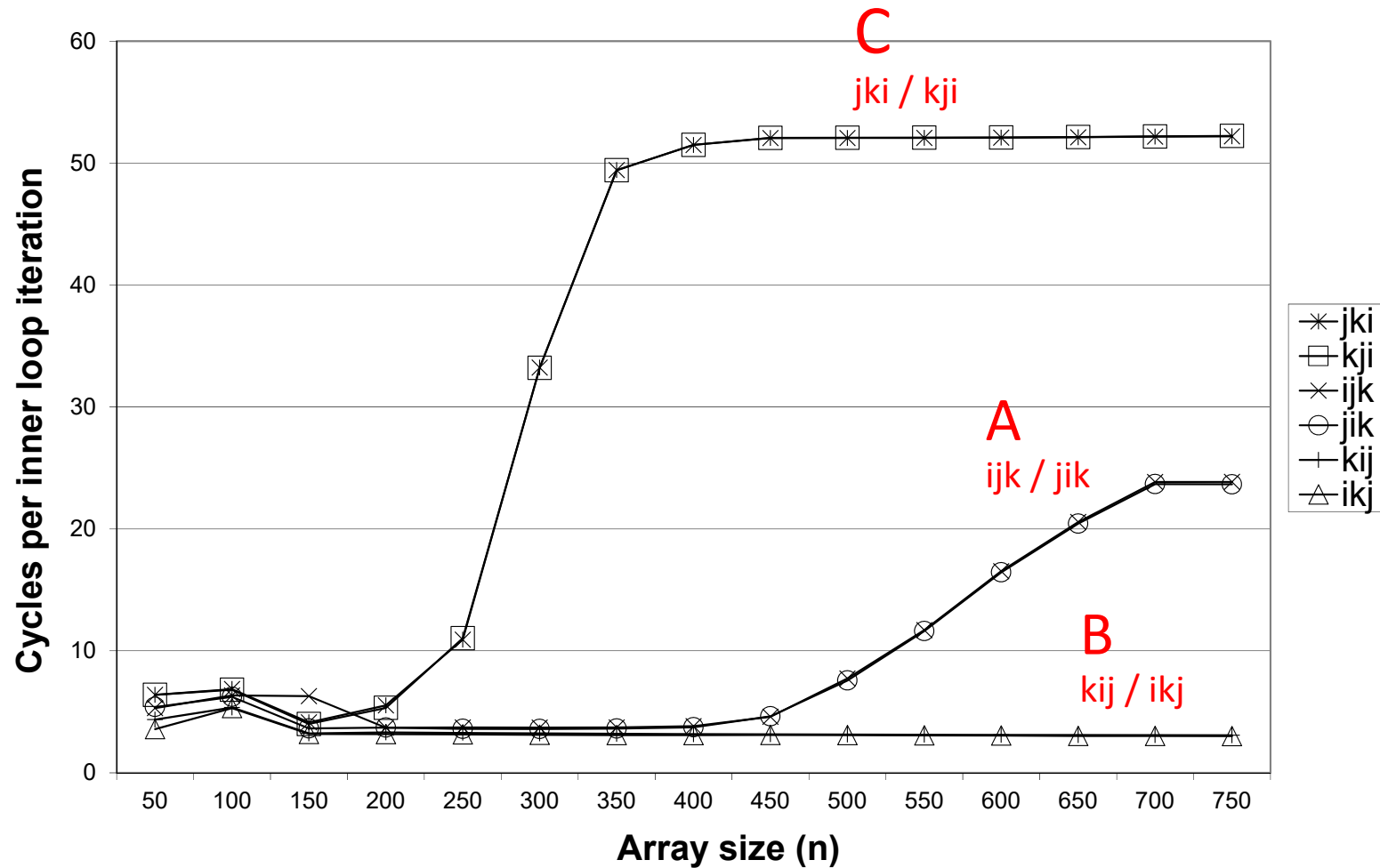
c)

```
for (j=0; j<n; j++) {  
    for (k=0; k<n; k++) {  
        r = b[k][j];  
        for (i=0; i<n; i++)  
            c[i][j] += a[i][k] * r;  
    }  
}
```

d) They are all approximately the same speed

e) (b) and (c) are faster than (a)

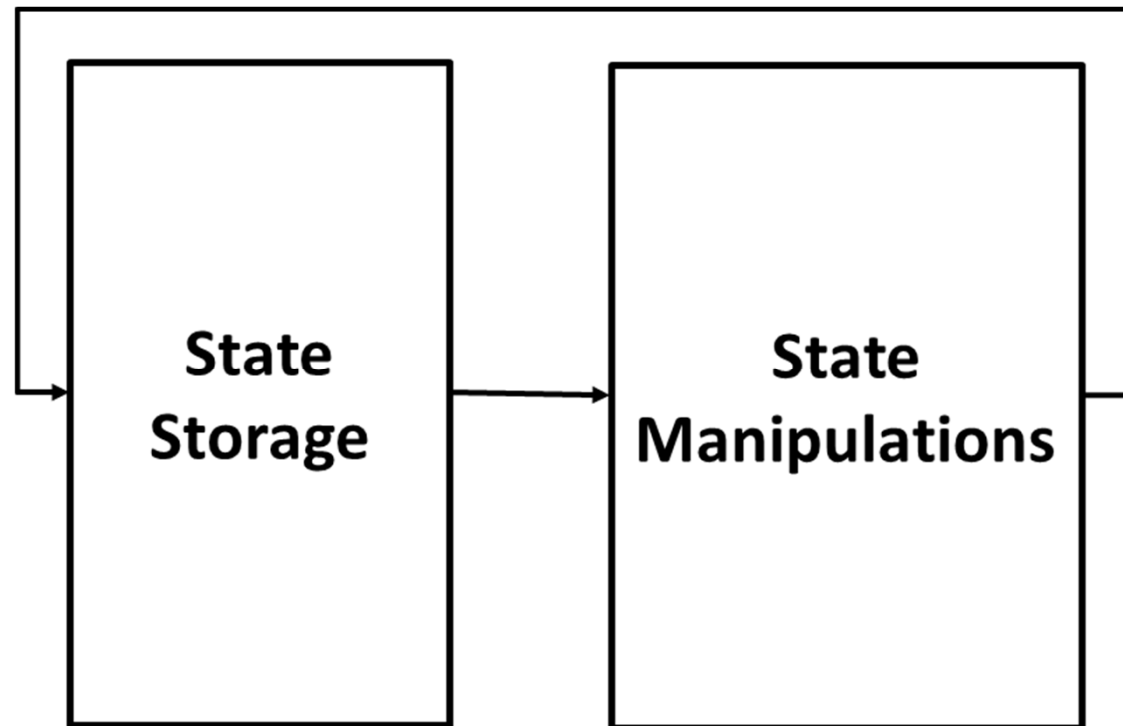
# Core i7 Matrix Multiply Performance



# 233 in one slide!

- The class consists roughly of 4 quarters: (Bolded words are the big ideas of the course, pay attention when you hear these words)
  1. You will build a simple computer processor  
Build and create **state** machines with **data**, **control**, and **indirection**
  2. You will learn how high-level language code executes on a processor  
Time limitations create **dependencies** in the **state** of the processor
  3. You will learn why computers perform the way they do  
Physical limitations require **locality** and **indirection** in how we access **state**
  4. You will learn about hardware mechanisms for parallelism  
**Locality**, **dependencies**, and **indirection** on performance enhancing drugs
- We will have a SPIMbot contest!

**A computer can do 2 things: Store state...**

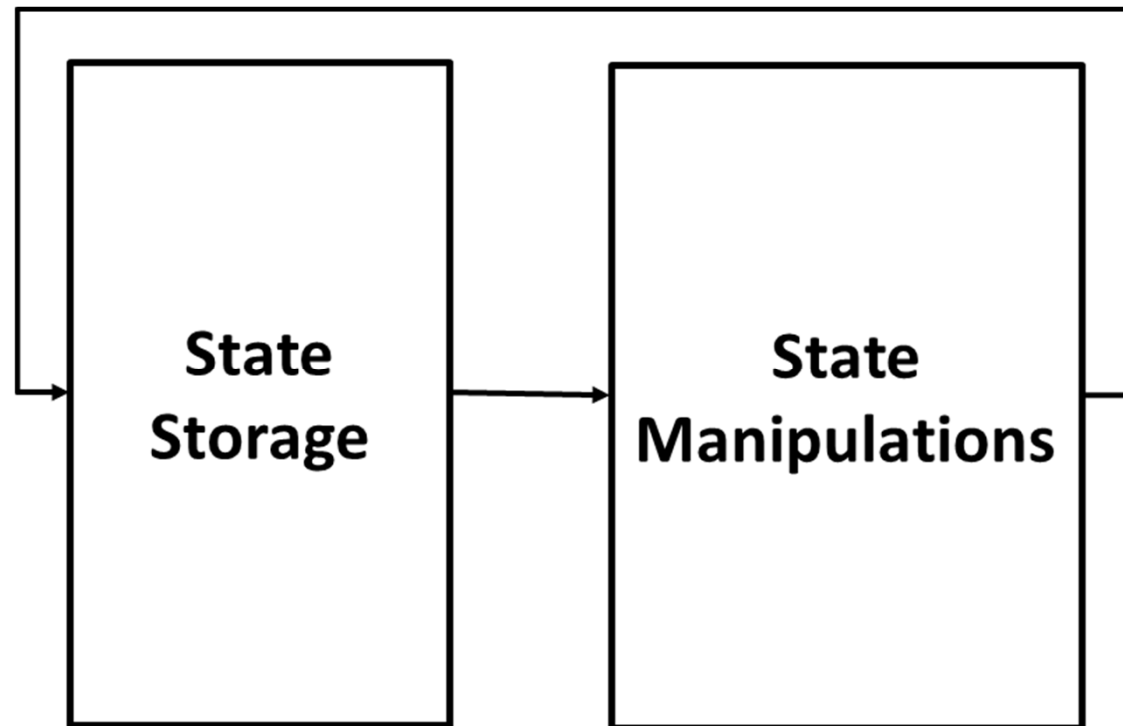




State is the relevant information about the progress of my system



**A computer can do 2 things: ...and manipulate state**

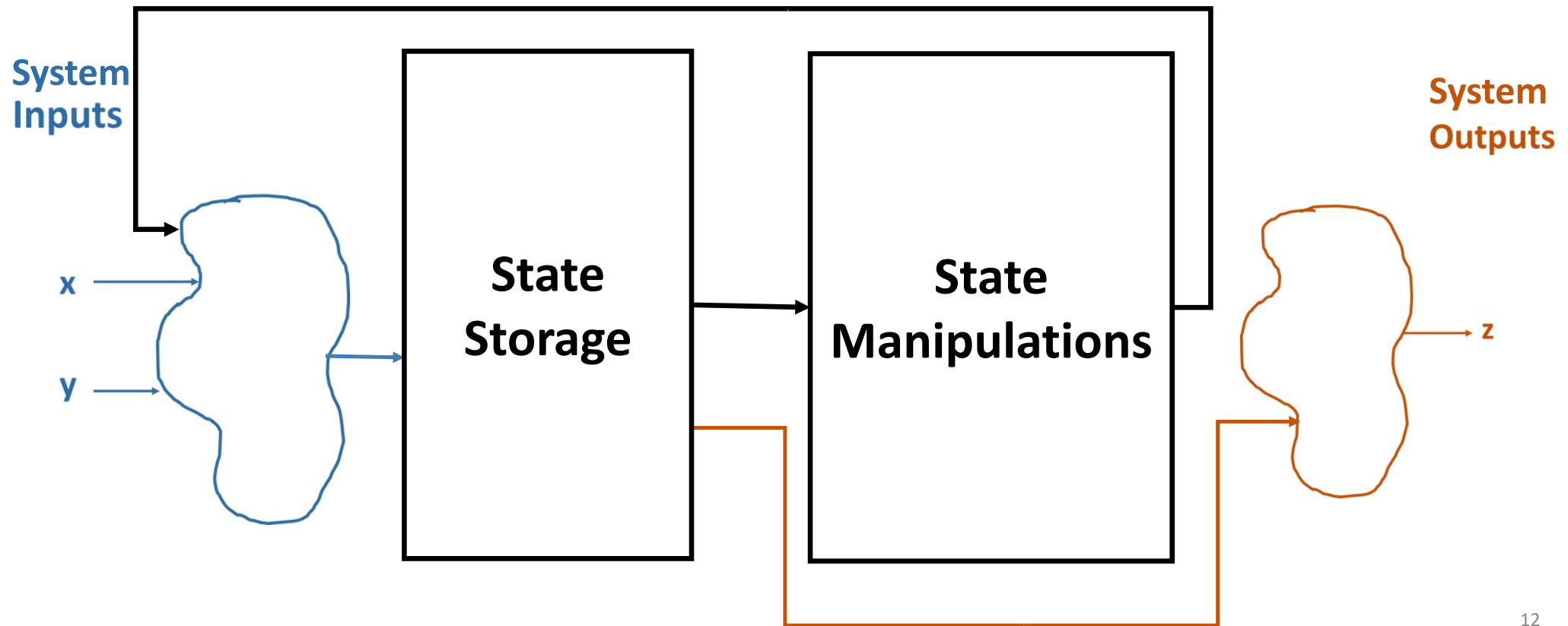




Computation  
changes my  
state in a  
limited  
number of  
ways



**State changes can respond to user (system) inputs**  
**State is used to compute a system output**



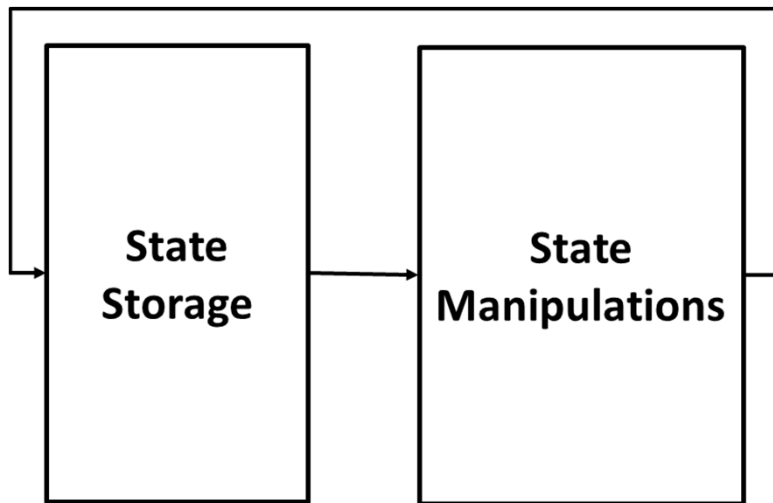


This game can be modeled with 3 system outputs: “game in progress,” “blue won,” “orange won”



# The state abstraction informs how we think about code tracing

- The system clock constrains when each line of code executes
- Code executes in series



```
z = x + y;  
x = 1;  
if(x == z){  
    y = 2;  
}  
.  
.  
.
```

# You have seen state in three forms in your coding: Data, control, and indirection

## Data

```
int add_numbers(int x, int y){  
    int z;  
  
    z = x + y;  
    return z;  
}
```

## Control

```
int find_greater(int x, int y){  
    if (x > y)  
        return x;  
    else  
        return y;  
}
```

## Indirection(Address)

```
int find_data(int* x){  
    int y;  
  
    y = *x;  
    return y;  
}
```

# **Boolean Algebra and Its Relation to Gates**

Why you needed to take CS 173

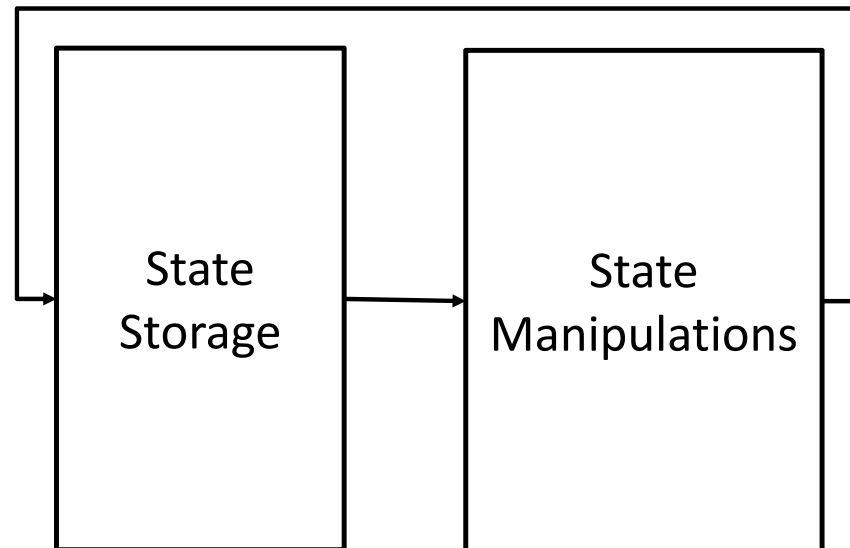


# We use Boolean algebra to manipulate the state of a system

Computer can do 2 things

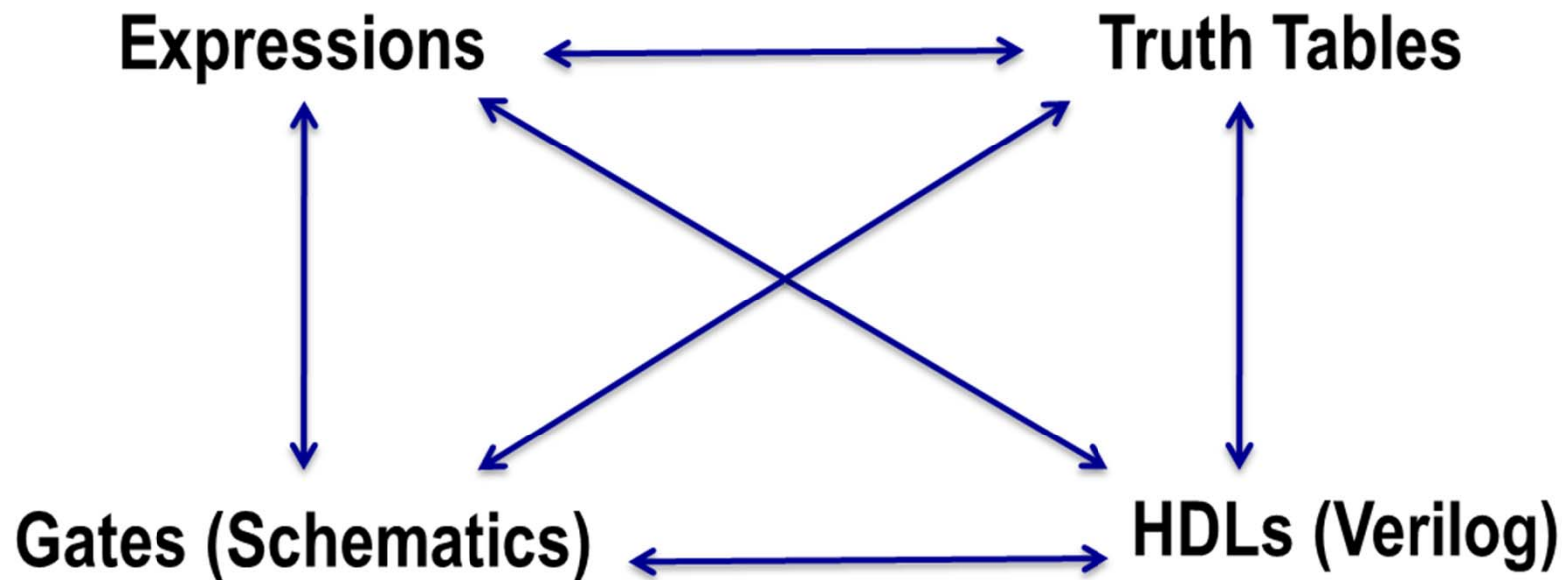
1) Store state

2) Manipulate state

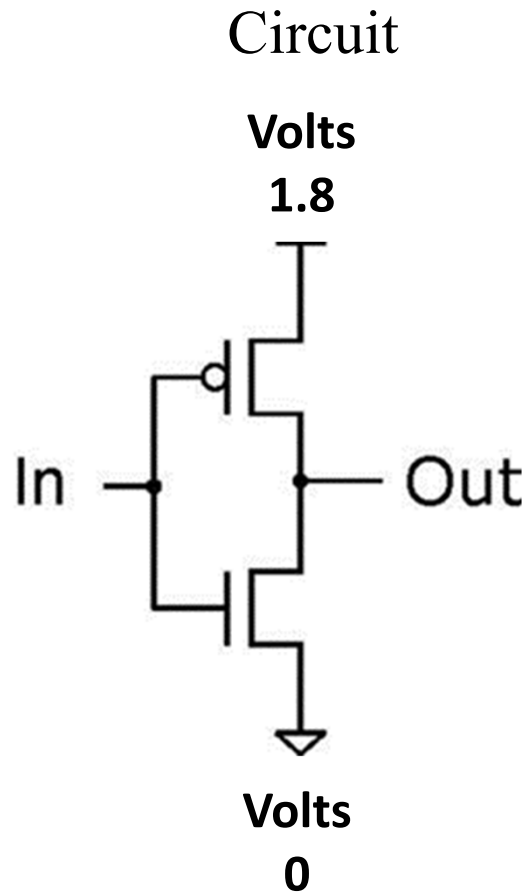


# Today's lecture

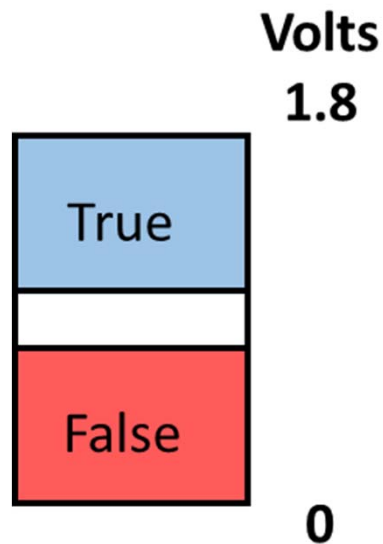
- Basic Boolean expressions
  - Booleans
  - AND, OR and NOT



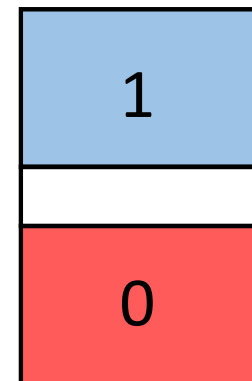
# State information is encoded with 1s and 0s



Boolean

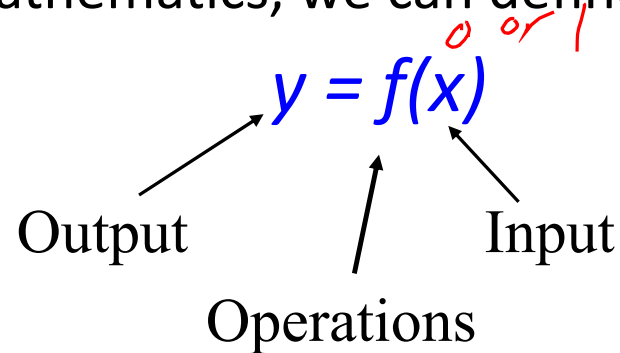


Binary



# Boolean functions

- Just like in other mathematics, we can define functions:



- Because there are a finite number (2) of boolean values...
  - There are a finite number of boolean functions
  - Let's discuss with an example

# A 1-input Boolean function has 4 unique output functions

$$y = f(x)$$

- A 1-input Boolean function has  $2^1 = 2$  possible input combinations:
- There are  $2^{(\text{\# of input combinations})}$  possible unique functions
  - For each input value, there are 2 possible output values (0 or 1)
  - The value of each output is independent from the value of each input
- The 4 possible 1-input Boolean functions

x	f(x)
0	f(0)
1	f(1)

x	$f_0(x)$
0	<u>0</u>
1	<u>0</u>

x	$f_1(x)$
0	<u>0</u>
1	<u>1</u>

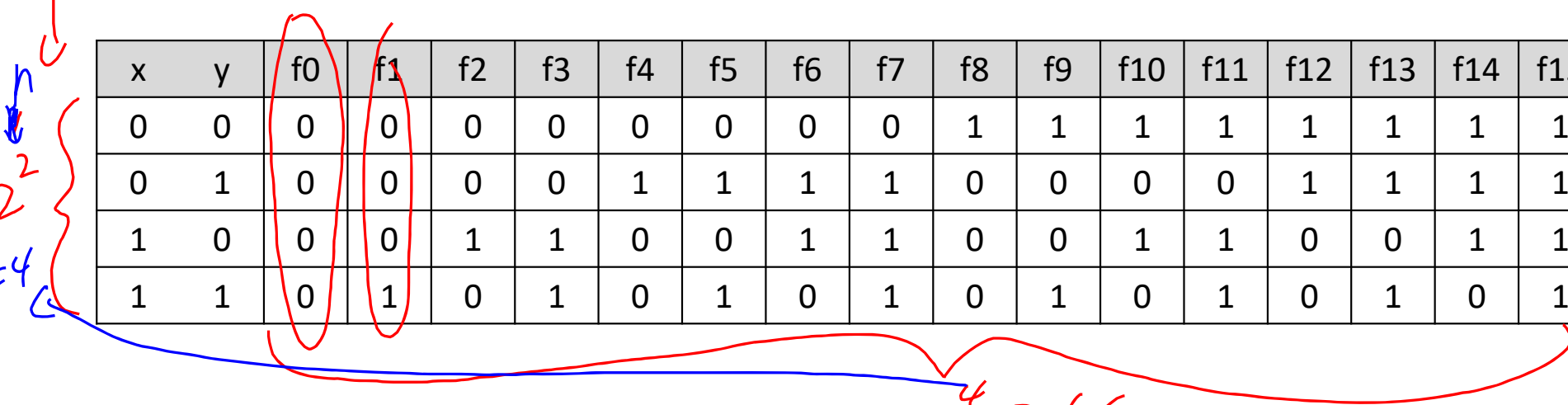
x	$f_2(x)$
0	<u>1</u>
1	<u>0</u>

x	$f_3(x)$
0	<u>1</u>
1	<u>1</u>

# A 2-input Boolean function has 16 unique output functions

$$z = f(x, y)$$

- 4 possible input combinations, 16 possible functions:



x	y	f0	f1	f2	f3	f4	f5	f6	f7	f8	f9	f10	f11	f12	f13	f14	f15
0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
0	1	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
1	0	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
1	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1

- We'll focus on 2 functions for now

$$2^4 = 16$$

## i>clicker question

If there are  $n$  inputs to a Boolean function, how many unique output functions could there be (i.e., how many unique columns would be created in the truth table)?

*a)*  $2 * 2 * n$

*b)*  $2 * n^2$

*c)*  $2^{n^2}$

*d)*  $2 * 2^n$

*e)*  $2^{2^n}$

# We use three basic logical operations: AND, OR, and NOT

Operation:

Expression

Notation:

Truth table:

AND (product)  
of two inputs

$xy$ , or  $x \bullet y$

x	y	f(x)
0	0	0
0	1	0
1	0	0
1	1	1

OR (sum) of  
two inputs

$x + y$

x	y	f(x)
0	0	0
0	1	1
1	0	1
1	1	1

NOT  
(complement)  
on one input

$x'$  or  $\bar{x}$

x	f(x)
0	1
1	0

These are sufficient to implement any Boolean function



# Boolean expressions (formally)

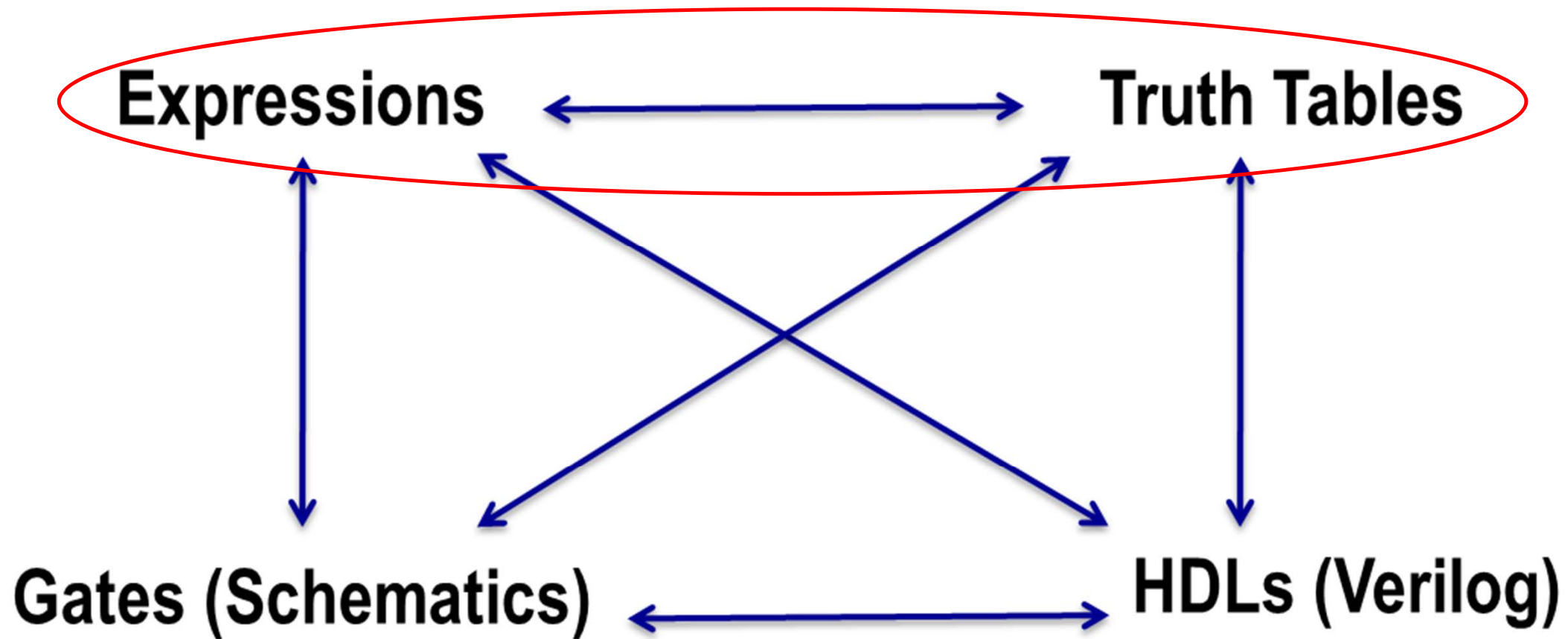
- Use these basic operations to form more complex expressions:

$$f(x,y,z) = (x + y')z + x'$$

- Some terminology and notation:
  - $f$  is the name of the function.
  - $(x,y,z)$  are the **input variables**, each representing 1 or 0. Listing the inputs is optional, but sometimes helpful.
  - A **literal** is any occurrence of an input variable or complement. The function above has four literals:  $x$ ,  $y'$ ,  $z$ , and  $x'$ .
- Precedences are similar to what you learned from algebra
  - NOT has the highest precedence, followed by AND, and then OR.
  - Fully parenthesized, the function above would be kind of messy:

$$f(x,y,z) = (((x + (y'))z) + x')$$

## A quick reminder



# Boolean expressions → Truth tables

- To compute a truth table given a Boolean expression:
  - Evaluate the function for every combination of inputs.

$$f(x,y,z) = (x + y')z + x'$$

$$\begin{aligned} f(0,0,0) &= (\underline{0} + \underline{1}) \underline{0} + \underline{1} = \underline{\quad} \\ &= (1) \cdot 0 + 1 \\ &= 0 + 1 \\ &= 1 \end{aligned}$$

$$f(1,0,1) = (\underline{\quad} + \underline{\quad}) \underline{\quad} + \underline{\quad} = \underline{\quad}$$

x	y	z	f(x,y,z)
0	0	0	1
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	1
1	1	0	
1	1	1	

a)	0
b)	1

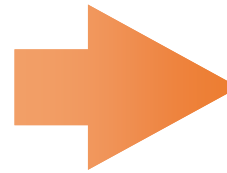
# Boolean expressions → Truth tables

- To compute a truth table given a Boolean expression:
  - Evaluate the function for every combination of inputs.

$$f(x,y,z) = (x + y')z + x'$$

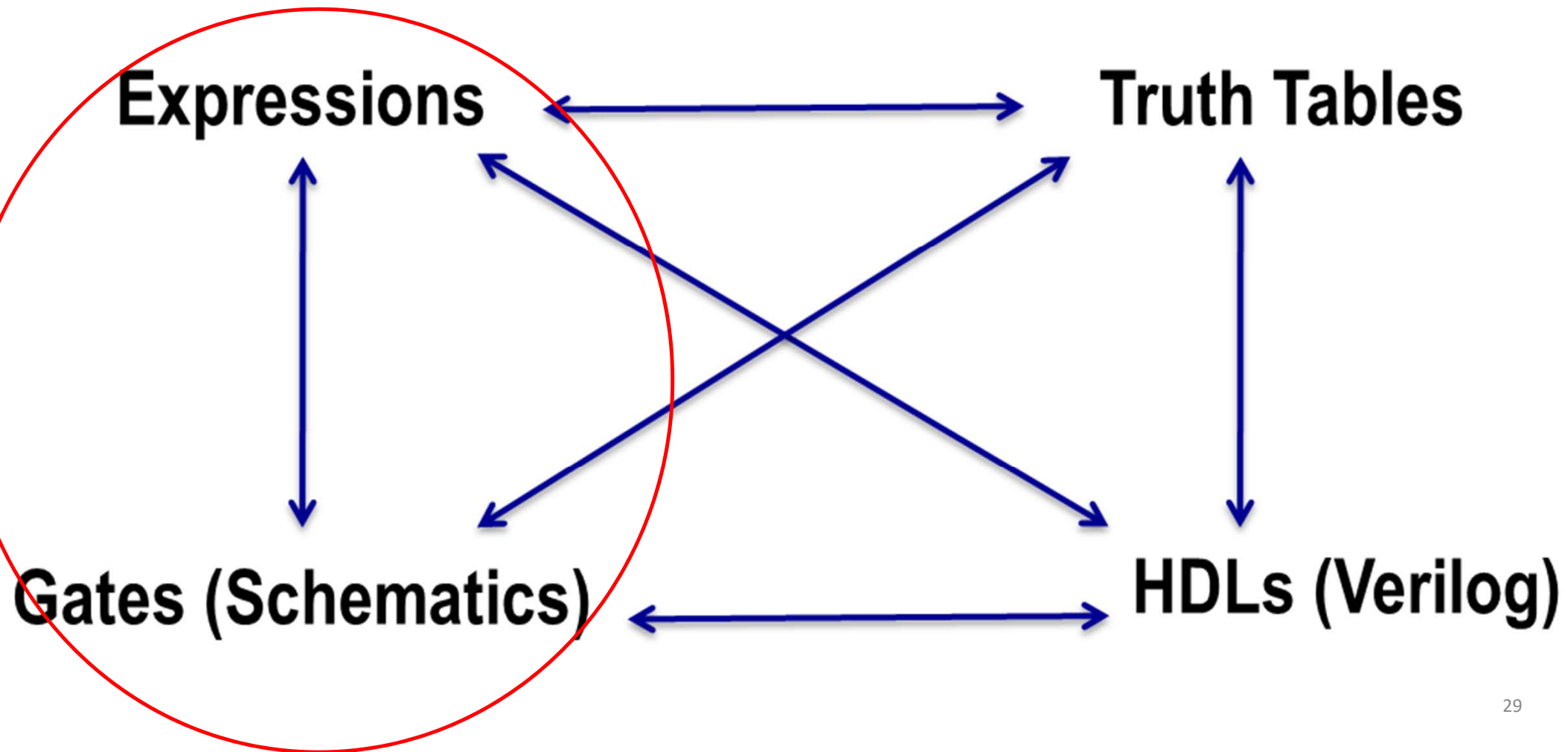


$f(0,0,0)$	$= (0 + 1)0 + 1$	$= 1$
$f(0,0,1)$	$= (0 + 1)1 + 1$	$= 1$
$f(0,1,0)$	$= (0 + 0)0 + 1$	$= 1$
$f(0,1,1)$	$= (0 + 0)1 + 1$	$= 1$
$f(1,0,0)$	$= (1 + 1)0 + 0$	$= 0$
$f(1,0,1)$	$= (1 + 1)1 + 0$	$= 1$
$f(1,1,0)$	$= (1 + 0)0 + 0$	$= 0$
$f(1,1,1)$	$= (1 + 0)1 + 0$	$= 1$


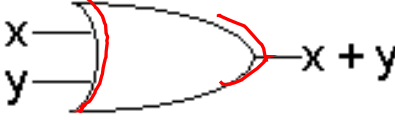
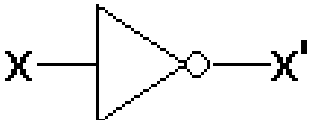


x	y	z	$f(x,y,z)$
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

## A quick reminder



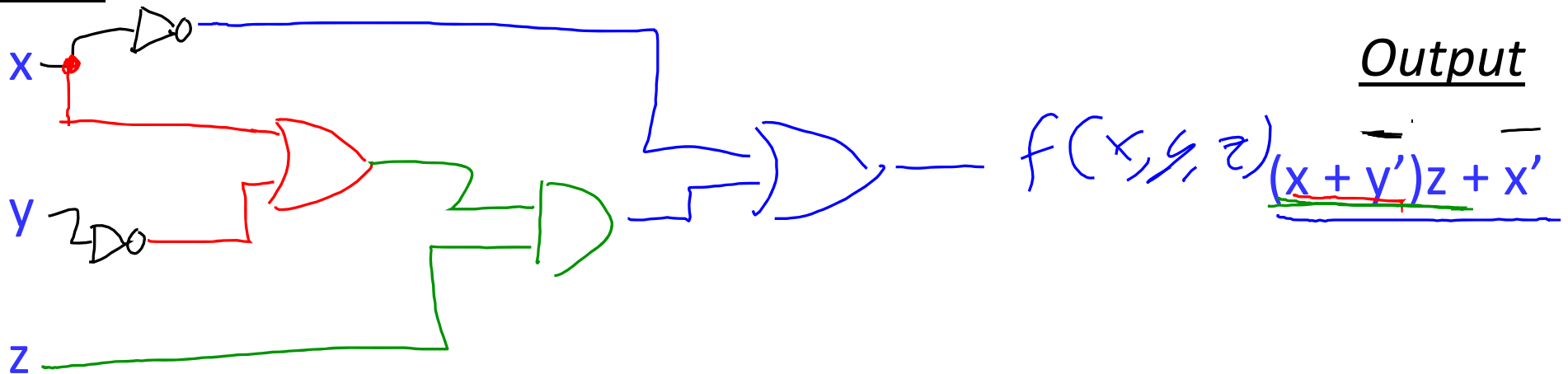
# The Boolean operators map to three primitive logic gates

Operation:	AND (product) of two inputs	OR (sum) of two inputs	NOT (complement) on one input
Expression:	$xy$ , or $x \bullet y$	$x + y$	$x'$
Logic gate:			

# Boolean expressions $\rightarrow$ circuits

- Any Boolean expression can be converted into a **circuit** in a straightforward way.
  - Write a gate for each operation in the expression in precedence order.
  - We typically draw circuits with inputs on left and outputs on right.

Inputs

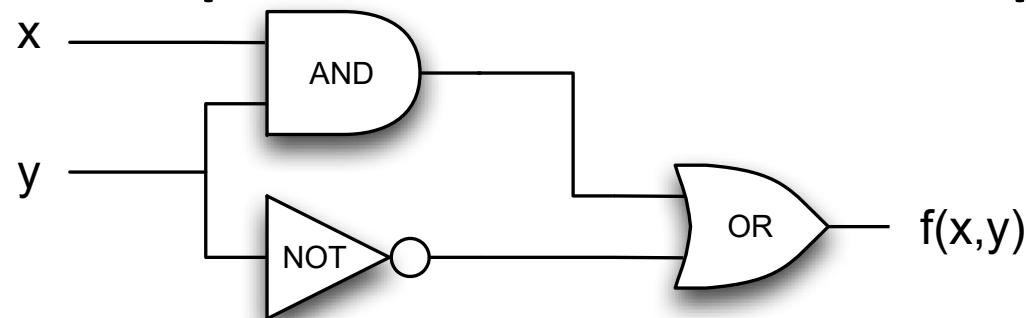


Output

$$f(x, y, z) \underline{(x + y')z + x'}$$

# Circuits $\rightarrow$ expressions

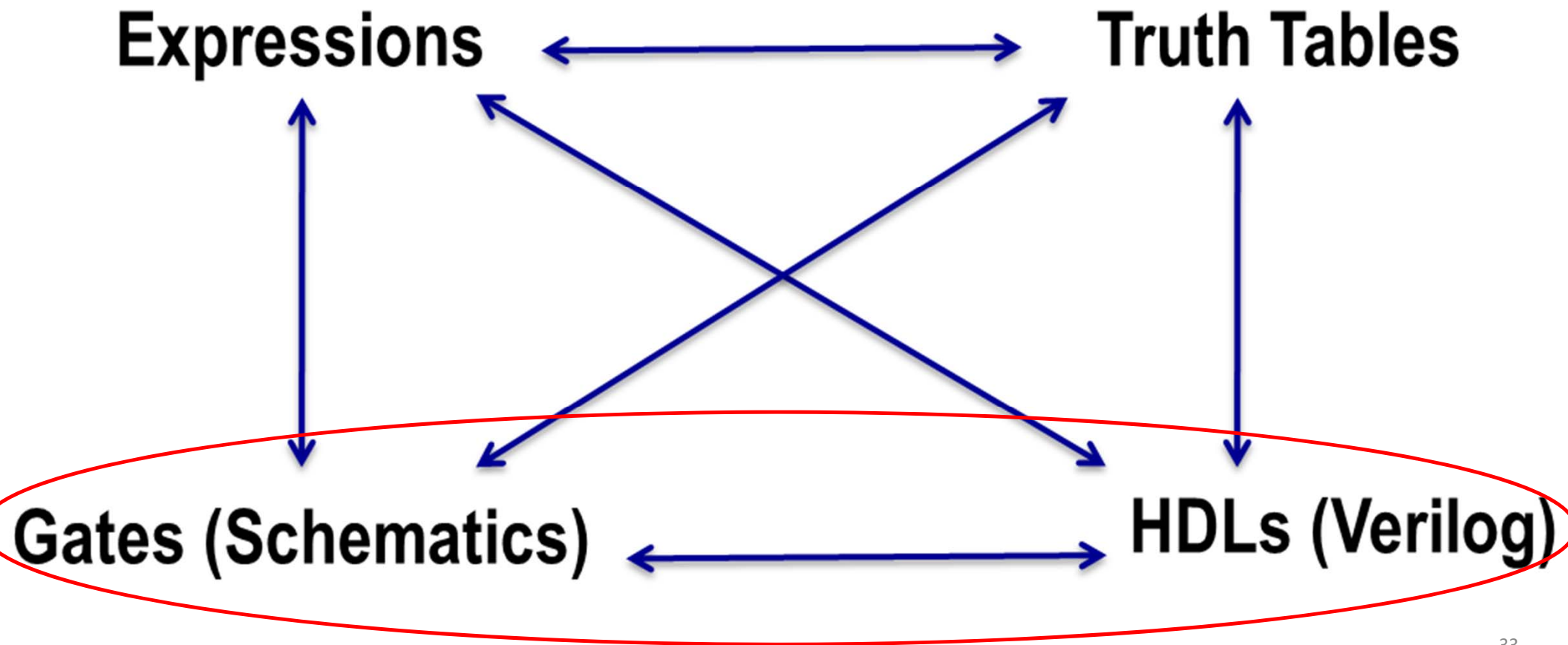
■ What Boolean expression does this circuit implement?



- a)  $(x + y)y'$
- b)  $x + y + y'$
- c)  $xy' + y$
- d)  $(xy) + y'$
- e)  $(x+y)(x+y')$



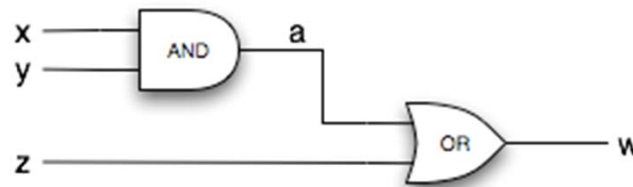
## A quick reminder



# Hardware Description Languages (HDL)

- Textual descriptions of circuits
  - (We're very good at manipulating text...)

A Circuit:

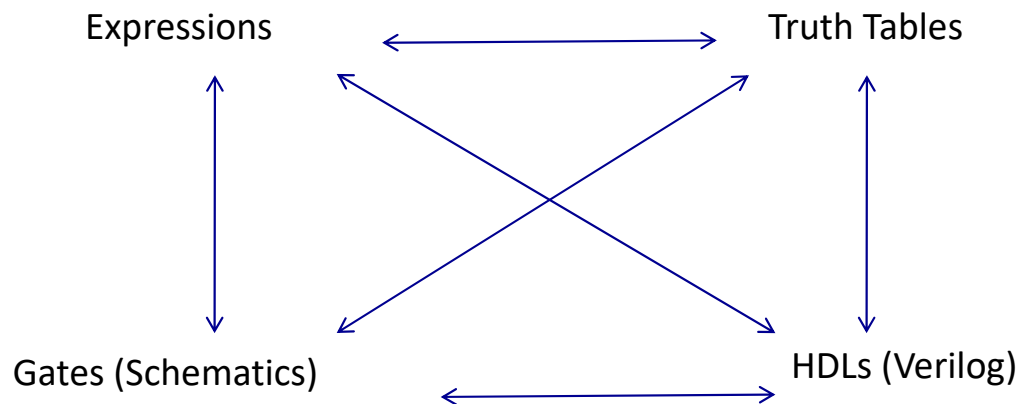


Verilog  
HDL Code:      `wire x, y, z, a, w;`  
                 `and a1(a, x, y);`      `// gatetype name(out, in1, in2);`  
                 `or o1(w, a, z);`

- **Not like a normal programming language**
  - Each statement describes one or more gates and/or wires.

# Summary of what we discussed today

- We can interpret high and low voltages as true and false.
- A Boolean variable can be either 1 or 0.
- AND, OR, and NOT are the basic Boolean operations.
- We can express Boolean functions in many ways:
  - Expressions, truth tables, circuits, and HDL code
  - These are different representations for equivalent things



# Things to do before next lecture

- Get on Piazza for CS 233
- Watch the Introduction to Verilog video
  - We'll send details by email and post on Piazza
- Do your Web Homework problems
  - <https://prairielearn.engr.illinois.edu/> There is something due each night before a lecture.

Late Add FAQ:

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# Discussion Section starts this week!

- We'll introduce you to the tools designing, testing, and debugging digital logic circuits
  - Verilog
  - Waveform Viewers

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