



BINARY SEARCH

CS A250 – C++ Programming II

SEARCH ALGORITHMS

- Search algorithms are very common
 - They search a list
 - Look at each item in the list and compare to the search item
- We will consider two ways to search:
 - **Linear**
 - Also called **sequential** search
 - Can be done in an **ordered/unordered** list
 - **Binary**
 - Can be done *only* in an *ordered* list

LINEAR SEARCH

- **Linear Search** searches through the elements of an arbitrary sequence (in this case, a **vector v**) until
 - The match is found **OR**
 - It reaches the end of the sequence

```
int count = 0;
bool found = false;
int size = static_cast<int>(v.size());
while (!found && count < size)
{
    if (v[count] == value)
        found = true;
    else
        ++count;
}
```

Assumption: All elements in the list are *unique*.

HOW MANY COMPARISONS?

- You always look at the worst case:
 - Assuming your list has 20 elements
 - You compare each element at most once with the given element
 - If the element you are searching for happens to be the last element in the list:
 - You have made **20 comparisons**
 - **Generalize:** 20 is denoted by n (a list of n elements)
- Therefore, the worst case in a **sequential search** is **n comparisons**.

BINARY SEARCH

○ Binary search

- Is faster than **linear search**
 - **BUT** assumes **array is sorted**
- Breaks the list in **half**
 - Determines if item in 1st or 2nd half
 - Then searches again just that half
 - Can be done **recursively**.

EXECUTION OF BINARY SEARCH

- A **sorted** array of 10 elements
 - Search for **63**

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90

EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Find the **middle** $\rightarrow (0 + 9) / 2 = 4$

Since indices are type **int**
result will be truncated

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90



EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Find the **middle** $\rightarrow (0 + 9) / 2 = 4$

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90

↑
mid

Is [4] equal to **63**? No
Is **63** > or < than [4]? >
Check between [5] and [9]

EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Find the **middle** $\rightarrow (5 + 9) / 2 = 7$

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90



EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Find the **middle** $\rightarrow (5 + 9) / 2 = 7$

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90

↑
mid

Is [7] equal to 63?	No
Is 63 > or < than [7]?	<
Check between [5] and [6]	

EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Find the **middle** $\rightarrow (5 + 6) / 2 = \mathbf{5}$

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90

Diagram illustrating the middle element calculation. A blue box labeled "mid" points to the element 63 at index [5] in the sorted array.

EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Find the **middle** $\rightarrow (5 + 6) / 2 = \mathbf{5}$

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90

↑
mid


Is **[5]** equal to **63**? Yes
Stopping case \rightarrow **63** found
Location = **mid**

EXECUTION OF BINARY SEARCH (CONT.)

- A **sorted** array of 10 elements
 - Search for **63**

Number of **comparisons** → **3**

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
15	20	35	41	57	63	75	80	85	90



A blue box labeled 'mid' with an upward-pointing arrow indicating the current middle element of the array, which is 63 at index 5.

IMPLEMENTATION

- **Binary search** can be implemented
 - **Iteratively**
 - Using a **while** loop
 - **Recursively**
 - **IF/ELSE** statement and **call to itself**
 - **Stopping case** for both implementations:
 - **if (first > last)** → no elements between them, so **key** cannot be there!
 - **if (key == a[mid])** → found!

EFFICIENCY OF BINARY SEARCH

- **Binary search** is *very efficient*
 - Extremely *fast*, compared to **sequential search**
- Half of array eliminated at start!
 - Then a quarter, then 1/8, etc.
 - Essentially eliminate half with each call
- Example: Array of 100 elements
 - In this case, a binary search never needs more than 7 compares!

RECURSIVE SOLUTIONS

- If done **recursively**, then the **binary search** algorithm actually solves "more general" problem
 - Original goal:
 - Design function to search an entire list
 - **BUT** you can search any *interval of the list*
 - By specifying bounds *first* and *last*
 - Very common when designing recursive functions



BINARY SEARCH (END)