

# CSIT881

## Programming and Data Structures

### Array and Linked List



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# Objectives

- Linear data structure
- Array
- Linked List

# Linear data structure

A linear data structure is a collection of items whose order is sequential. It means that each item (except the last item) has a unique next item, and that each item (except the first item) has a unique previous item.

This sequential order is a **logical order** and it may not be reflected in a real physical order in computer memory.

# Linear data structure

An Array is an abstract data type:

- a fixed-length sequence of items of the **same data type** that are stored contiguously in computer memory;
- items can be randomly accessed via its index;

7	3	8	5
---	---	---	---

# Linear data structure

7	3	8	5
---	---	---	---

An array contains a fixed number of items stored sequentially in a computer memory.

If we want to increase the length of an array to store more items, we may need to *allocate new memory* for the whole new array and *copy* each item from the old array to the new array. We also need to free the memory of the old array.

- In low level programming language, memory management is a tricky business;
- In high level programming language (such as Java and Python), memory management is handled automatically behind the scene.

# NumPy array

```
import numpy
```

```
help(numpy.ndarray)
```

Help on class ndarray in module numpy:

```
class ndarray(builtins.object)
|   ndarray(shape, dtype=float, buffer=None,
|           offset=0, strides=None, order=None)
|
|   An array object represents a multidimensional,
|   homogeneous array of fixed-size items.
```

# NumPy array

Creating a one-dimensional array:

```
import numpy

fibonacci = numpy.array([0, 1, 1, 2, 3, 5, 8, 13])

for i in range(0, len(fibonacci)):
    print(fibonacci[i])
```

# NumPy array

## Creating a one-dimensional array:

```
import numpy

arr1 = numpy.zeros(shape=5, dtype=numpy.int64)
print(arr1)

arr2 = numpy.ones(shape=7, dtype=numpy.int64)
print(arr2)
```

[0 0 0 0 0]

[1 1 1 1 1 1 1]

some other types

```
numpy.bool, numpy.str, numpy.byte,  
numpy.int32, numpy.int64, numpy.float32,  
numpy.float64, numpy.complex, numpy.object,  
...
```



# NumPy array

Creating a 2-dimensional array:

```
import numpy

magicSquare = numpy.array([[ 8,  1,  6], [ 3,  5,  7], [ 4,  9,  2]])

print(magicSquare)
```

```
[[ 8  1  6]
 [ 3  5  7]
 [ 4  9  2]]
```

# NumPy array

Creating a 2-dimensional array:

```
import numpy

arr3 = numpy.zeros(shape=(2, 3), dtype=bool)
print(arr3)
```

```
[[False False False]
 [False False False]]
```

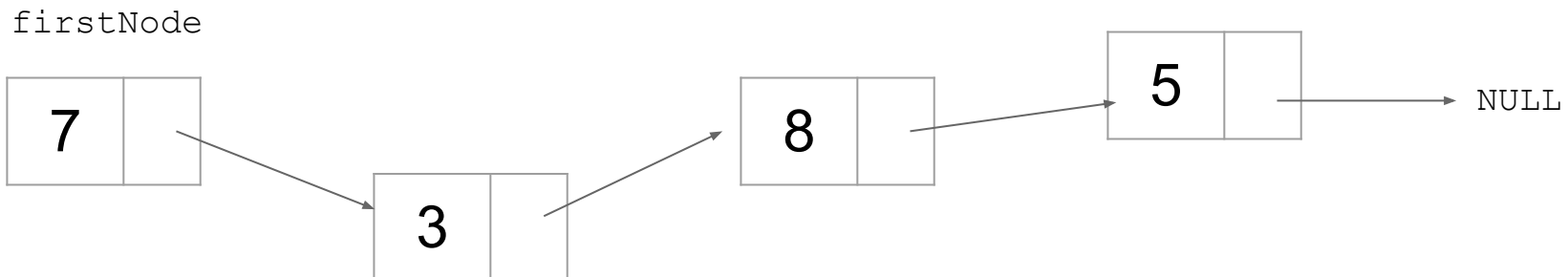
```
arr4 = numpy.ones(shape=(3, 2), dtype=numpy.int32)
print(arr4)
```

```
[[1 1]
 [1 1]
 [1 1]]
```

# (ADT) **Linked List**

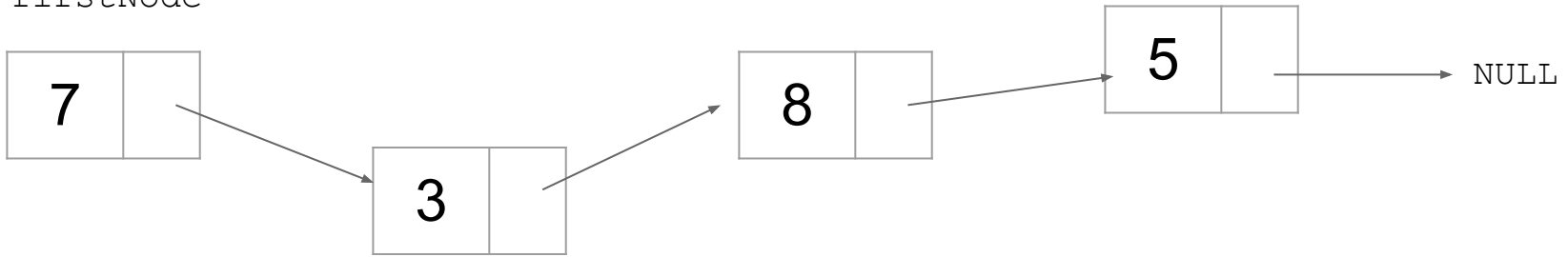
A linked list is an abstract data type:

- containing a sequence of data items whose **physical order** may not be sequential in computer memory;
- the data items may not be homogeneous, i.e. may have different sizes;
- its **logical order** is sequential by employing a collection of nodes where each node contains the data and **a reference to the next node**;



# (ADT) **Linked List**

firstNode



- each node contains the data and **a reference to the next node**;
- it is easy to add a new node in any position in the list and delete an old node, making the list grows dynamically;

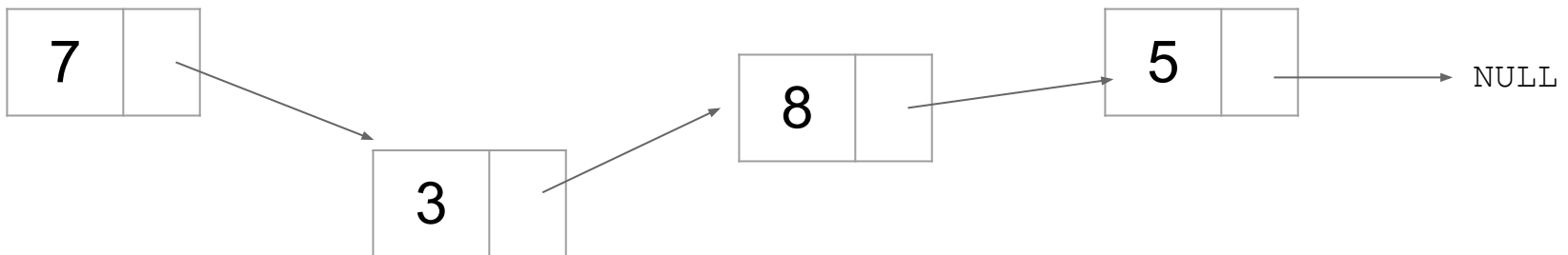
# (ADT) **Linked List**

## Comparison between Array and Linked List

7	3	8	5
---	---	---	---

- fixed length, homogeneous size, stored sequentially in memory;
- static structure, hard to extend memory to store more items.

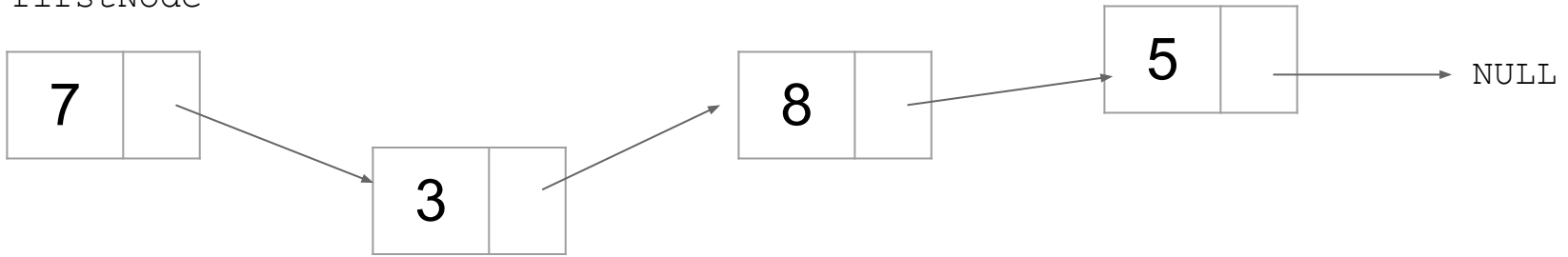
firstNode



- variable-length list, non-homogeneous size, items stored independently in memory;
- dynamic structure, easy to add and delete items.

# (ADT) **Linked List**

firstNode



Some common operations on linked list:

- Get first node
- Get last node
- Get the *i*th node
- Add an item to the start of the list
- Add an item to the end of the list
- Remove first node
- Search for an item...

# (ADT) **Linked List**

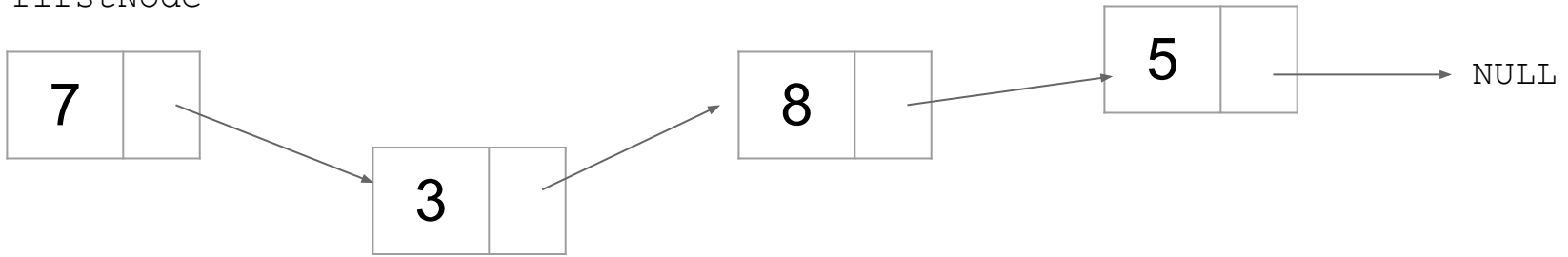
Some disadvantage:

- only the first node is readily accessible, access to other nodes need a linear travelling from the first node;
- easy to operate on the start of the list, but hard to operate at the end of the list because only reference to the first node is available;
- linear searching through a list.

Some programming language may add additional functionalities to their linked list implementation to have some of the above lacking behaviours.

# Implementation of (ADT) Linked List

firstNode



pseudocode

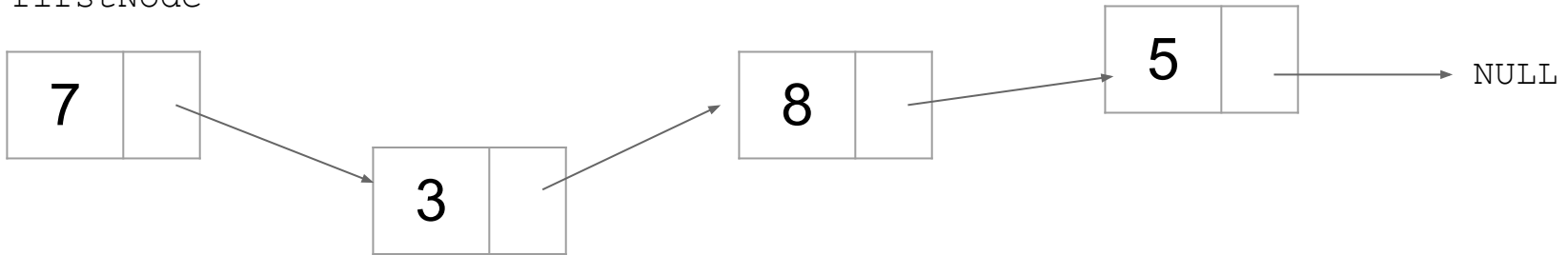
```
record Node
{
    datum           // the data being stored in the node
    Node next       // a reference to the next node
}
```

```
record LinkedList
{
    Node firstNode // first node of the list (null for empty list)
}
```



# Implementation of (ADT) Linked List

firstNode

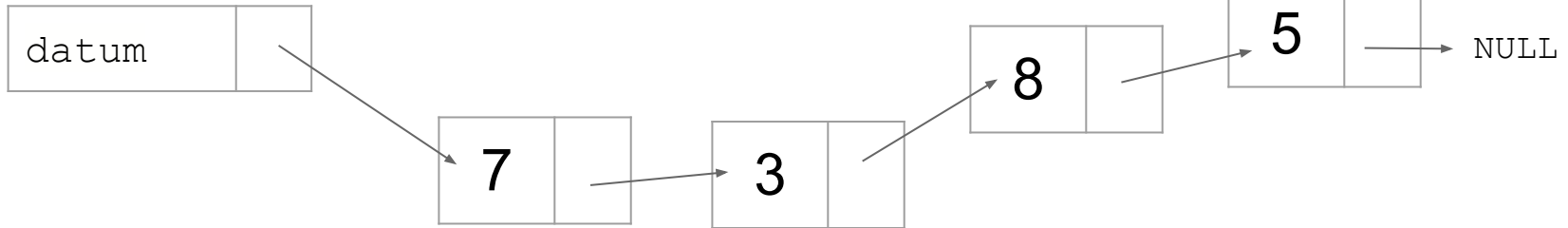


pseudocode

```
Function constructor()  
// Construct an empty linked list  
{  
    firstNode = NULL  
}  
  
Function getFirstNode()  
// Returns the first node of the linked list.  
// If the linked list is empty then returns NULL  
{  
    RETURN firstNode  
}
```

# Implementation of (ADT) Linked List

firstNode



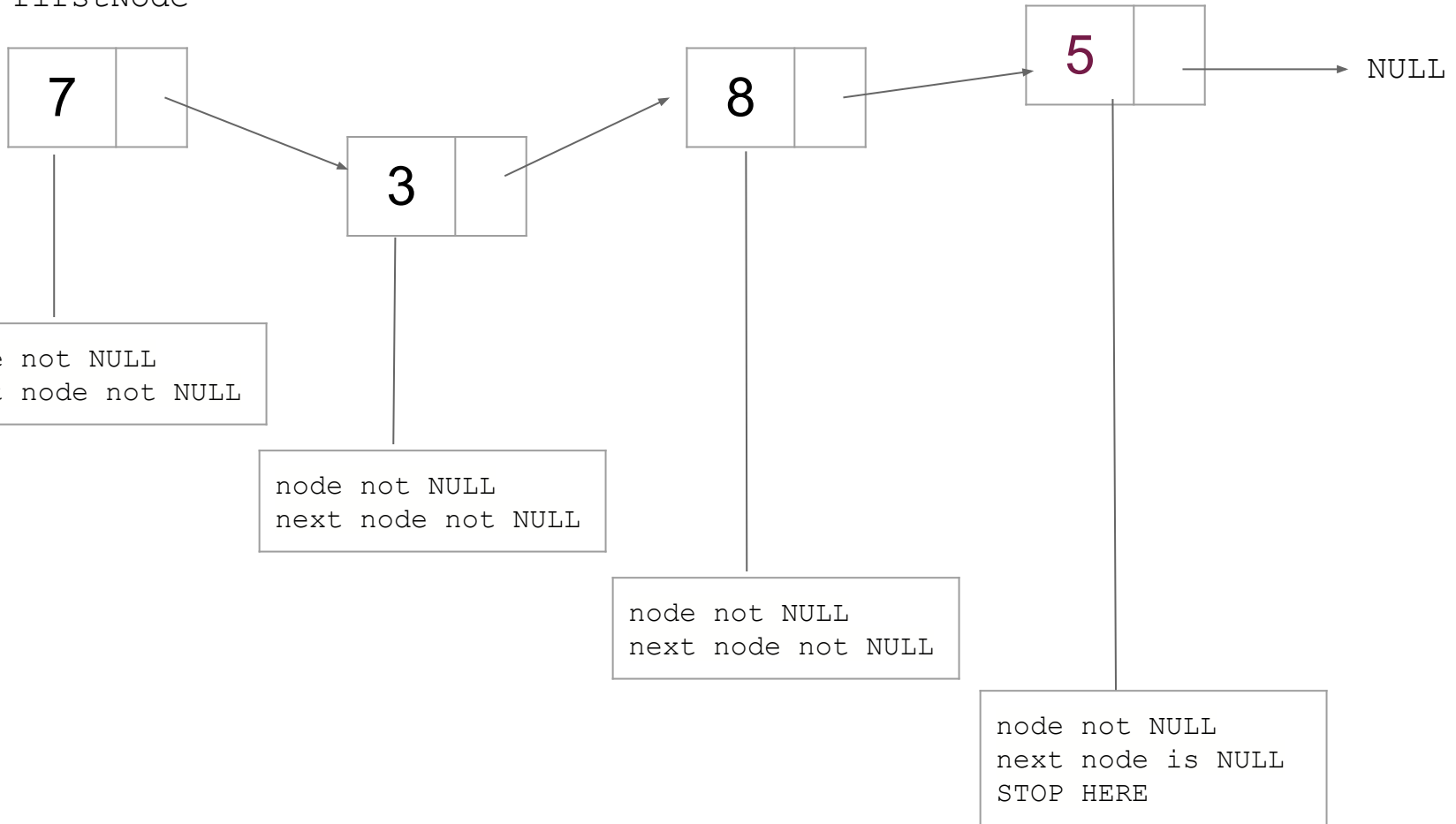
pseudocode

```
Function insertFirst(datum)
// Inserts a node holding the datum at the beginning of this list
{
    // Create a new node
    Node newNode = create Node
    newNode.datum = datum
    newNode.next = firstNode

    // Set the new node to be the first node of the list
    firstNode = newNode
}
```

# Implementation of (ADT) Linked List

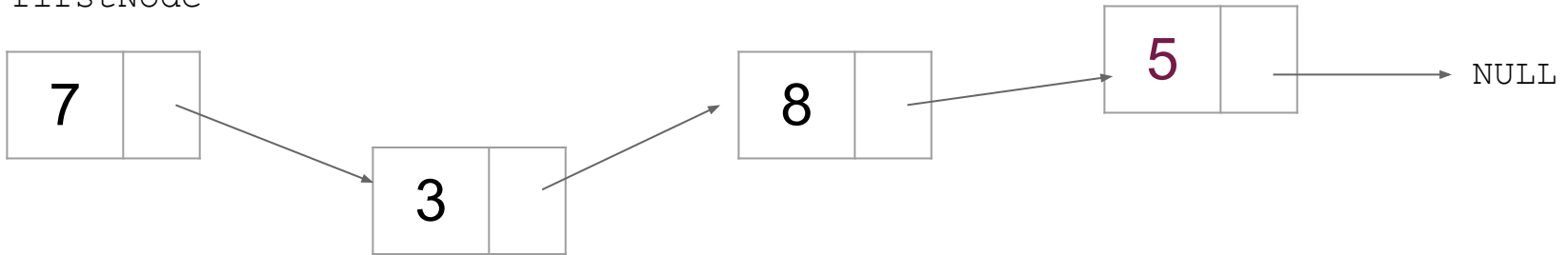
firstNode



```
Function getLastNode()  
// Returns the last node of the linked list.  
// If the list is empty then returns NULL
```

# Implementation of (ADT) Linked List

firstNode

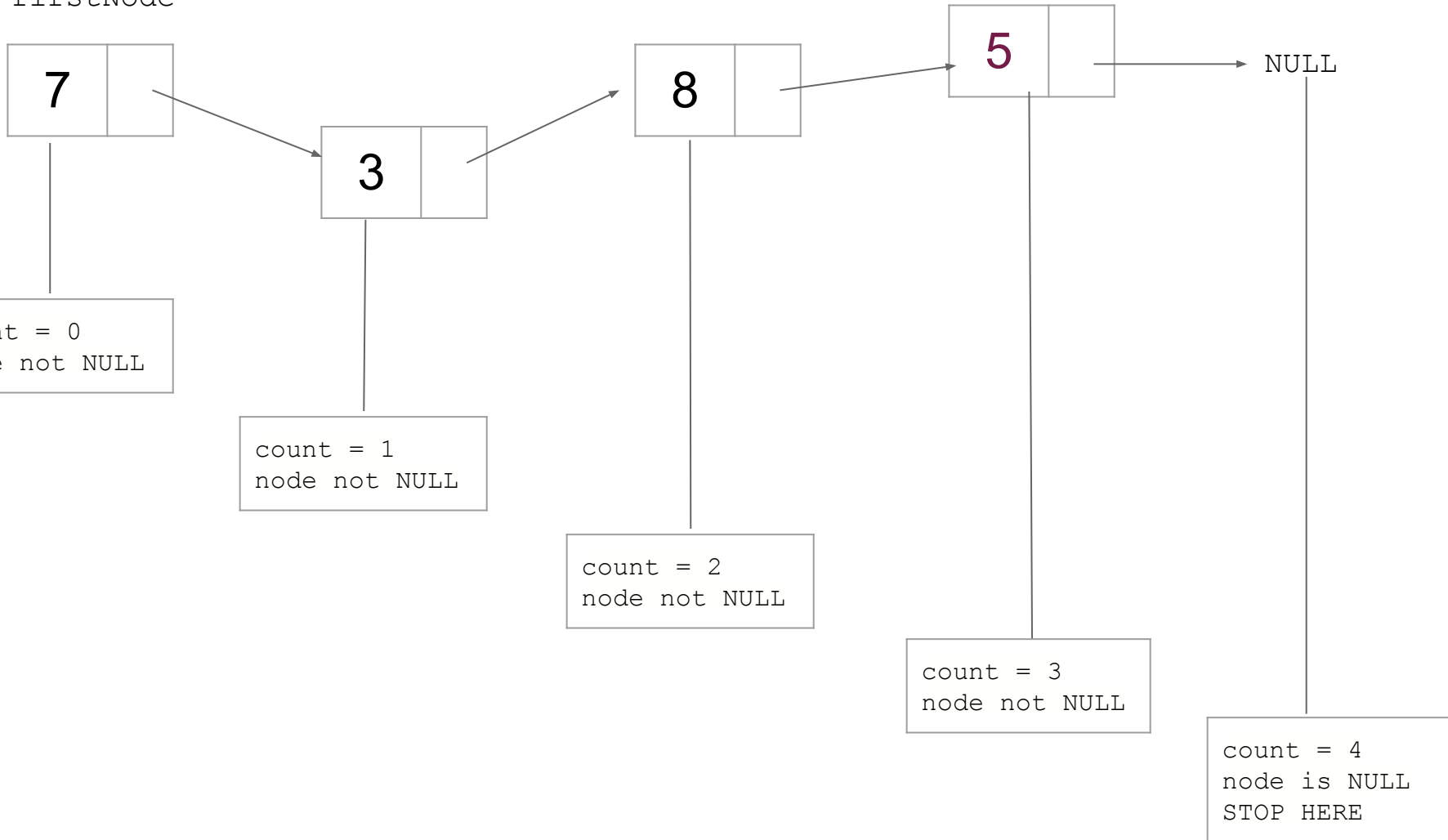


pseudocode

```
Function getLastNode()  
// Returns the last node of the linked list.  
// If the list is empty then returns NULL  
{  
    // start at the first node  
    node = firstNode  
  
    // travel down the list  
    WHILE node != NULL and node.next != NULL  
        node = node.next  
    END WHILE  
  
    RETURN node  
}
```

# Implementation of (ADT) Linked List

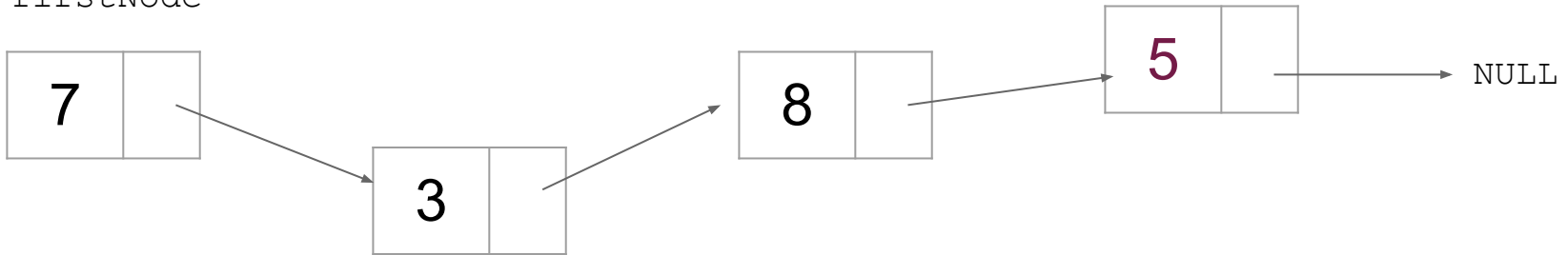
firstNode



```
Function getLength()  
// Returns the length of the linked list
```

# Implementation of (ADT) Linked List

firstNode



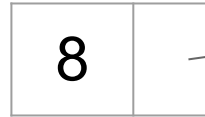
pseudocode

```
Function getLength()  
// Returns the length of the linked list  
{  
    // counting number of nodes  
    count = 0  
  
    // start at the first node  
    node = firstNode  
  
    // travel down the list and increase the count  
    WHILE node != NULL  
        node = node.next  
        count = count + 1  
    END WHILE  
  
    RETURN count  
}
```

# Implementation of (ADT) Linked List

firstNode

index = 2



NULL

i = 0  
i < index  
node not NULL

i = 1  
i < index  
node not NULL

i = 2  
i = index  
STOP HERE

Function **getNode**(index)

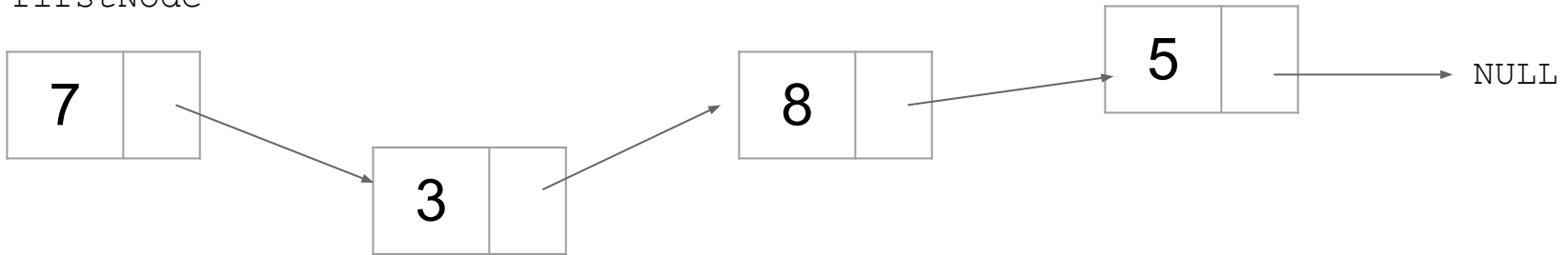
// Returns the node at the specified index in this list.

// Returns NULL if there is no node at that position.

// Index 0 refers to the first node.

# Implementation of (ADT) Linked List

firstNode



pseudocode

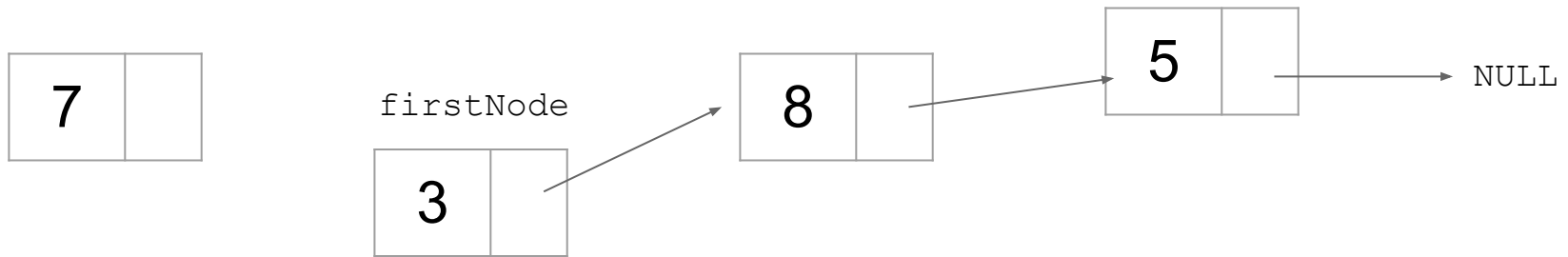
```
Function getNode(index)
// Returns the node at the specified index in this list.
// Returns NULL if there is no node at that position.
// Index 0 refers to the first node.
{
    // start at the first node
    node = firstNode
    i = 0

    // travel down the list until the index
    WHILE i < index and node != NULL
        node = node.next
        i = i + 1
    END WHILE

    RETURN node
}
```



# Implementation of (ADT) Linked List

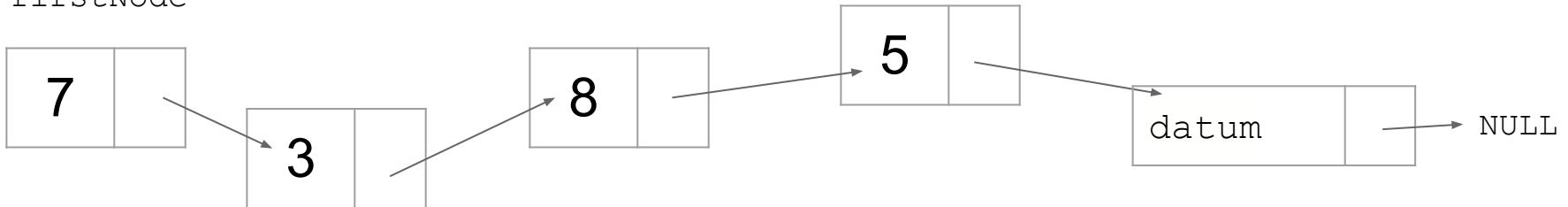


pseudocode

```
Function removeFirst()  
// Removes the first node and returns its datum.  
// Returns NULL if the list is empty.  
{  
    // check empty list  
    IF firstNode is NULL  
        RETURN NULL  
  
    // get the first datum  
    firstDatum = firstNode.datum  
  
    // reset the first node of the list  
    firstNode = firstNode.next  
  
    RETURN firstDatum  
}
```

# Implementation of (ADT) Linked List

firstNode

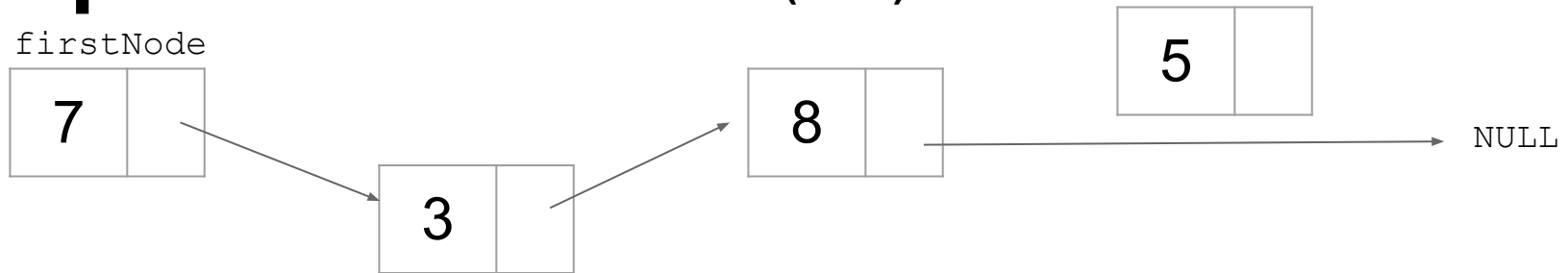


pseudocode

```
Function insertLast(datum)
// Inserts a node holding the datum at the end of the list
{
    lastNode = getLastNode()

    IF lastNode is NULL
        // list is currently empty
        insertFirst(datum)
    ELSE
        // create a new node
        Node newNode = create Node
        newNode.datum = datum
        newNode.next = NULL
        // link the current last node to this new node
        lastNode.next = newNode
}
```

# Implementation of (ADT) Linked List

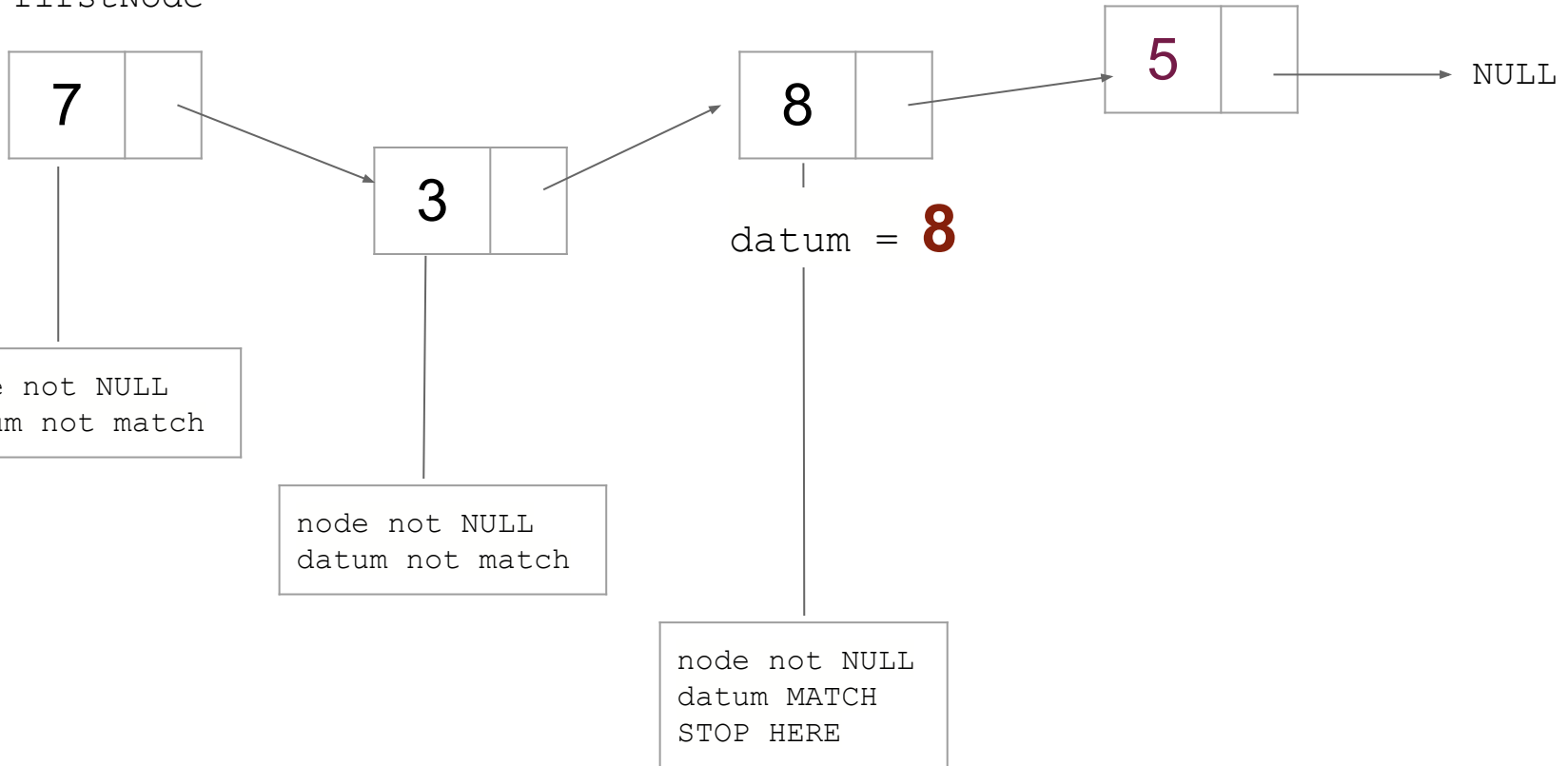


pseudocode

```
Function removeLast()  
// Removes the last node of this list and returns its datum.  
// Returns NULL if the list is empty.  
{  
    IF firstNode is NULL // empty list case  
        RETURN NULL  
    END IF  
  
    // find the last node and its previous node  
    prevNode = NULL  
    lastNode = firstNode  
    WHILE lastNode != NULL and lastNode.next != NULL  
        prevNode = lastNode  
        lastNode = lastNode.next  
    END WHILE  
  
    IF prevNode is NULL  
        // this list currently has one item  
        firstNode = NULL  
    ELSE  
        prevNode.next = NULL  
    END IF  
  
    RETURN lastNode.datum  
}
```

# Implementation of (ADT) Linked List

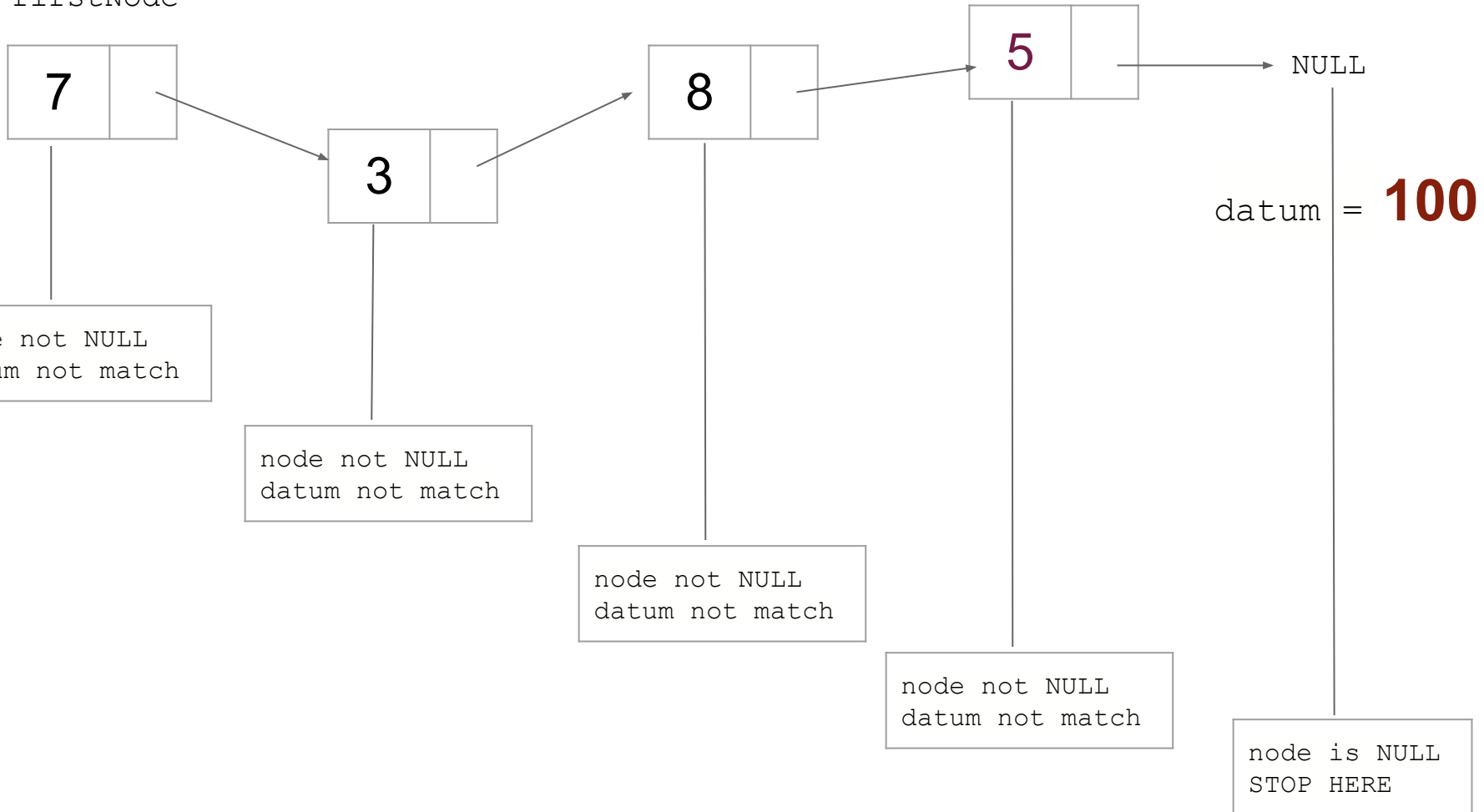
firstNode



```
Function search(datum)
// Returns the node that has the datum matched
// Returns NULL if there is no match.
```

# Implementation of (ADT) Linked List

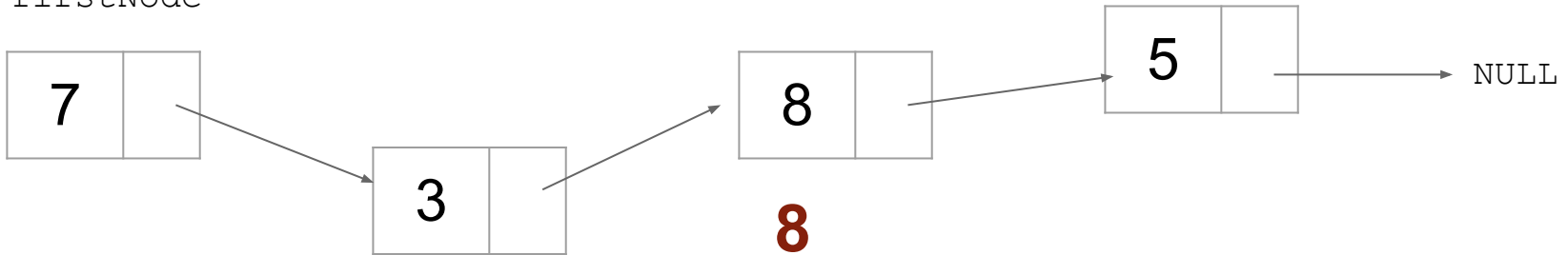
firstNode



```
Function search(datum)
// Returns the node that has the datum matched
// Returns NULL if there is no match.
```

# Implementation of (ADT) Linked List

firstNode



pseudocode

```
Function search(datum)
// Returns the node that has the datum matched
// Returns NULL if there is no match.
{
    // start at the first node
    node = firstNode

    // travel down the list until datum found
    WHILE node != NULL
        IF node.datum matches datum
            RETURN node
        END IF
        node = node.next
    END WHILE

    RETURN NULL
}
```

# Implementation of (ADT) Linked List

Python implementation

```
class Node:
    """
    Representing a node consisting of
    - datum: the datum stored at the node
    - next: reference to the next node
    """

    def __init__(self, datum, next):
        #{
            self.datum = datum
            self.next = next
        #}
```

# Implementation of (ADT) Linked List

Python implementation

```
class MyLinkedList:
    """
    Implementation of a linked list
    that connect firstNode -> node -> node -> ... -> NULL
    """

    def __init__(self):
        #{
            """
            Constructs an empty linked list
            """
            self.firstNode = None
        #}
```



# Implementation of (ADT) Linked List

Python implementation

```
class MyLinkedList:

    def insertFirst(self, datum):
        #{
            """
            Inserts a node holding the datum at the beginning of this list.
            """

            # create a new node
            newNode = Node(datum=datum, next= self.firstNode)

            # set the new node to be the first node of the list
            self.firstNode = newNode
        #}
```

# Implementation of (ADT) Linked List

Python implementation

```
class MyLinkedList:

    def getLastNode(self):
        #{
            """
            Returns the last node of this list.
            If the list is empty then returns None
            """

            # start at the first node
            node = self.firstNode

            # travel down the list
            while (node != None) and (node.next != None):
                node = node.next

            return node

        #}
```

# Implementation of (ADT) Linked List

Python implementation

```
class MyLinkedList:

    def getLength(self):
        #{
            """
            Returns the length of the list.
            If the list is empty then returns 0.
            """

            # counting number of nodes
            count = 0

            # start at the first node
            node = self.firstNode

            # travel down the list and increase count
            while node != None:
                #{
                    node = node.next
                    count = count + 1
                #}

            return count
        #}
```

# Implementation of (ADT) Linked List

Python implementation

```
class MyLinkedList:

    def getNode(self, index):
        #{
            """
            Returns the node at the specified index in this list.
            Returns None if there is no node at that position.
            Index 0 refers to the first node.
            """

            # start at the first node
            node = self.firstNode
            i = 0

            # travel down the list until the index
            while (i < index) and (node != None):
                #{
                    node = node.next
                    i = i + 1
                #}

            return node

        #}
```

# Implementation of (ADT) Linked List

Python implementation

```
class MyLinkedList:

    def removeFirst(self):
        #{
            """
            Removes the first node of this list and return its datum.
            Returns None if the list is empty.
            """

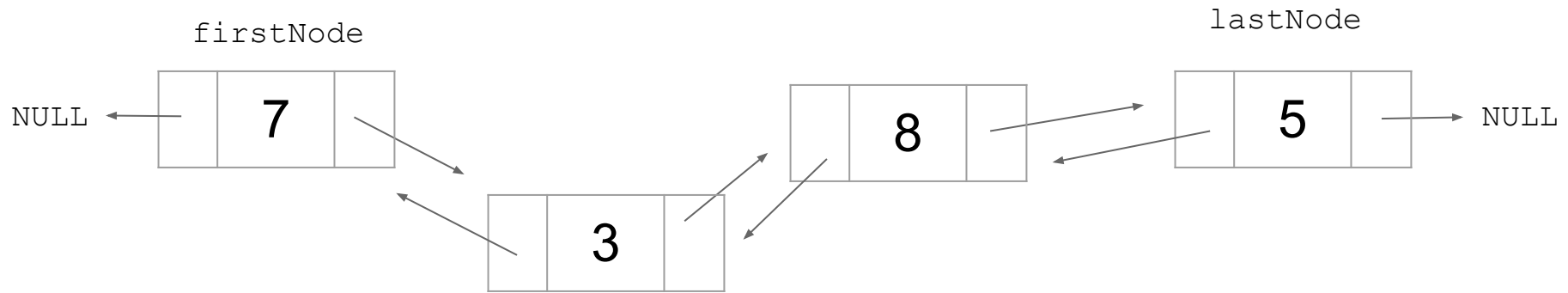
            # if the list is empty
            if (self.firstNode == None):
                return None

            # get the first datum
            firstDatum = self.firstNode.datum

            # reset the first node of this list
            self.firstNode = self.firstNode.next

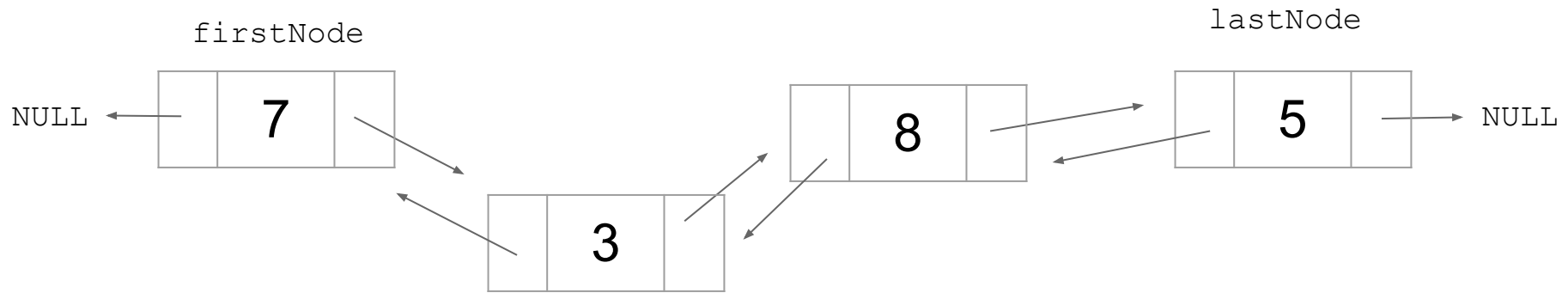
            return firstDatum
        #}
```

# (ADT) Doubly Linked List



- each node contains the data and two node references:
  - one reference to the **next node**;
  - one reference to the **previous node**;
- a doubly linked list has two references: one to its **first node** and one to its **last node**.

# (ADT) Doubly Linked List



pseudocode

```
record Node
{
    datum           // the data being stored in the node
    Node prev       // a reference to the previous node
    Node next        // a reference to the next node
}
```

```
record DoublyLinkedList
{
    Node firstNode // first node of the list (null for empty list)
    Node lastNode  // last node of the list (null for empty list)
}
```

# References

- Python 3 documentation  
<https://docs.python.org/3/>
- NumPy Reference  
<https://numpy.org/doc/stable/reference/>