



CS & IT ENGINEERING

Theory of Computation

Push Down Automata
context-free Languages

DPP 01



By- Venkat sir

#Q. Suppose L_1 is a finite language and L_2 is non-regular language then $L_1 \cap L_2$ will be:

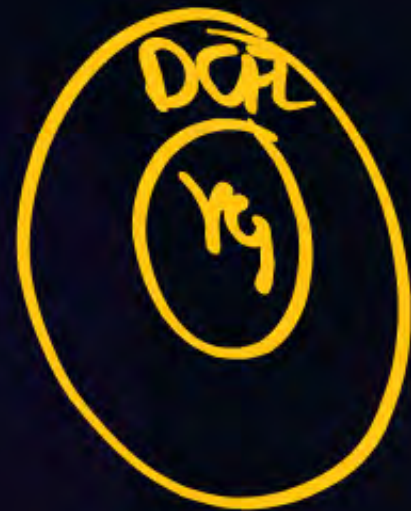
finite \cap non-reg \rightarrow finite
 \downarrow
regular

- A** Regular but infinite
- B** Non-regular
- C** ✓ Finite and regular
- D** None of these

#Q. Consider the following statements:

- ☒ (i) All finite language are context free language.
- ☒ (ii) All regular language are finite.
- ☒ (iii) All DCFL are finite.
- ☒ (iv) All regular language are DCFL
- ☒ (v) There exists some language which are finite and irregular.

The number of correct statements from the above statements are 2.



#Q. Consider the following languages.

$$L_1 = \{a^n b^n \mid n \geq 0\} \rightarrow \text{DCFL}$$

$$L_2 = \{a^n b^m c^k \mid n, m, k \geq 0 \wedge (n \neq m) \vee (m \neq k)\} \text{ CFL but not DCFL}$$

Which of the following statements is correct?

- | | | | |
|----------|--------------------------------|--|--------------------------------|
| A | L_1 is CFL and L_2 is DCFL | <input checked="" type="checkbox"/> B | L_1 is DCFL and L_2 is CFL |
| C | L_1 and L_2 both are DCFL | D | None of these. |

(A, B, C)

#Q. Which of the following grammar is/are generating DCFL but not regular language?

A ✓ $S \rightarrow \underline{aa} S \underline{bb} \mid \epsilon$
 $\{a^n b^n\}$

C ✓ $S \rightarrow aa S b \mid \epsilon$
 $\{a^n b^{2n}\}$

B ✓ $S \rightarrow a S bb \mid \epsilon$
 $\{a^n b^{2n}\}$

D $S \rightarrow \underline{ab} S \mid \epsilon$
 $(ab)^*$

#Q. Consider the following languages:

$$L_1 = \{a^m \overbrace{b^n c^k} \mid \text{if } (m = \text{even}) \text{ then } (n = k)\} \rightarrow \text{DCFL}$$

$$L_2 = \{a^n \underline{c} b^n\} \cup \{a^n \underline{d} b^n\} \rightarrow \text{DCFL}$$

Which of the following is correct statement?

A

Only L_1 is DCFL.

B

Only L_2 is DCFL.

C

Both L_1 and L_2 are CFL but not DCFL

D

Both L_1 and L_2 are DCFL but not regular.

$$xx^R yy^R$$

$$CFL \cdot CFL = CFL$$

#Q. Consider the following grammar:

$$S \rightarrow AB$$

$$A \rightarrow aAa \mid bAb \mid \epsilon \quad xx^R \rightarrow CFL$$

$$B \rightarrow aBa \mid bBb \mid \epsilon \quad yy^R \rightarrow CFL$$

Which of the following is correct regarding above grammar?

- ☒ **A** Language produced by S is $L = \{xx^R yy^R \mid x, y \in \{a, b\}^*\}$ and L is DCFL but not regular.
- ☒ **B** Language produced by S is $L = \{xx^R yy^R \mid x, y \in \{a, b\}^*\}$ and L is CFL but not DCFL.
- ☒ **C** Language produced by S is $L = \{xx^R yy^R \mid x, y \in \{a, b\}^*\}$ and L is DCFL.
- ☐ **D** None of the above.

#Q. The intersection of CFL and a regular language will be

- A** Always regular
- B** Always CFL ✓
- C** Always not regular
- D** None of these

$CFL \cap \text{regular}$ → always CFL.
may or may not regular

$$0^n \underline{1^n 1^m} 2^m = \underline{0^n 1^{n+m}} 2^m$$

#Q. Consider the following grammars G_1 , G_2 and G_3 :

G_1 : $S \rightarrow \underline{PQ} \mid \underline{P} \mid Q$
 $P \rightarrow 0P1 \mid \epsilon$
 $Q \rightarrow 1Q2 \mid \epsilon$

$$0^n 1^n 1^m 2^m$$

G_2 : $S \rightarrow 0S1 \mid Q$
 $P \rightarrow 1Q2 \mid \epsilon$

$$0^n (1^m 2^m) 1^n$$

G_3 : $S \rightarrow \underline{PQ} \mid Q \mid P$
 $P \rightarrow 0P1 \mid 01 \mid \epsilon$
 $Q \rightarrow 1Q2 \mid \epsilon$

$$0^n 1^n 1^m 2^m$$

A

G_1 and G_2 are equivalent

B

G_1 and G_3 are equivalent

C

G_2 and G_3 are equivalent

D

None of these

Here, $\{S, P, Q\}$ are variables where S is start symbol. $\{0, 1, 2\}$ are terminals.

Which of the following is true?

[MCQ]

$$\text{CSL} \wedge \text{CSL} \rightarrow \text{CSL}$$
$$\text{CSL} \wedge \text{CFL}$$



#Q. Consider the following language.

L_1 = Context free language. ✓

L_2 = Deterministic context free language.

L_3 = Context sensitive language.

L_4 = Regular

Which of the following is incorrect?

A

$L_2 \cdot L_4$ is always DCFL.

→ false

B

$L_1 \cap L_3$ is CSL. — true

C

$\Sigma^* - L_3$ is CSL. — true

D

None of the above.

DCFL. regular

DCFL. DCFL

#Q. Consider the following push down automata.

PDA = $\{Q, \Sigma, \delta, \Gamma, q_0, Z_0, q_f\}$

Which of the following language is accepted by above PDA?

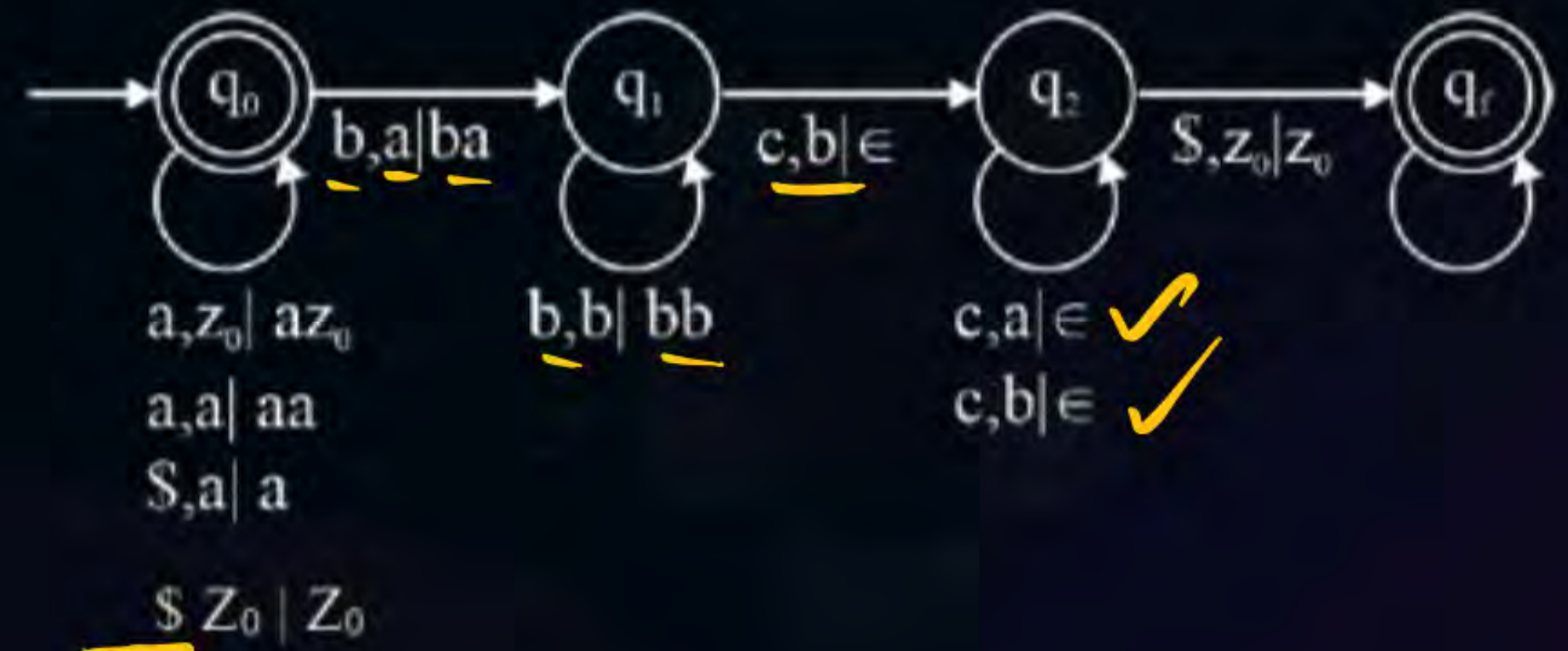
$a^* \cup \underbrace{a^n b^m c^{n+m}}$

A $L = \{a^*\} \cup \{a^p b^q c^r \mid p, q, r \geq 1, p + q = r\}$

B $L = \{a^{p+q} b^{q+r} \mid p, q, r \geq 0\}$

C $L = \{a^p b^q c^r \mid p, q, r \geq 1\}$

D None of the above



[MSQ]



#Q. Consider the following language: L_2

$$L_1 = \{ab^n a^{2n} \mid n \geq 1\} \rightarrow \text{DCFL}$$

$$L_2 = \{aab^n a^{3n} \mid n \geq 1\} \rightarrow \text{DCFL}$$

Which of the following is correct?

A ✓ $L_1 \cup L_2$ is DCFL but not regular.

B $L_1 \cup L_2$ is CFL but not DCFL.

C $L_1 \cup L_2$ is CSL but not CFL.

D ✓ $L_1 \cup L_2$ is DCFL and also CFL.

(A, D)

#Q. Suppose, L is any CFL language on alphabet

$\Sigma = \{a, b\}$, and the following language:

$$L_1 = L - \underbrace{\{w x w^R \mid w, x \in \{a, b\}^*\}}_{(a+b)^*} - \emptyset$$

$$L_2 = L_1 \cdot L - \emptyset$$

$$L_3 = \bar{L}_1 \cup L = \Sigma^* \cup L = \Sigma^*$$

Which of the following is/are correct?

(A, B, C)

A

L_1 is regular ✓

B

L_2 is CFL. ✓

C

L_3 is regular. ✓

D

None of these



THANK - YOU