

# CS & IT ENGINEERING

## Theory of Computation

Push Down Automata

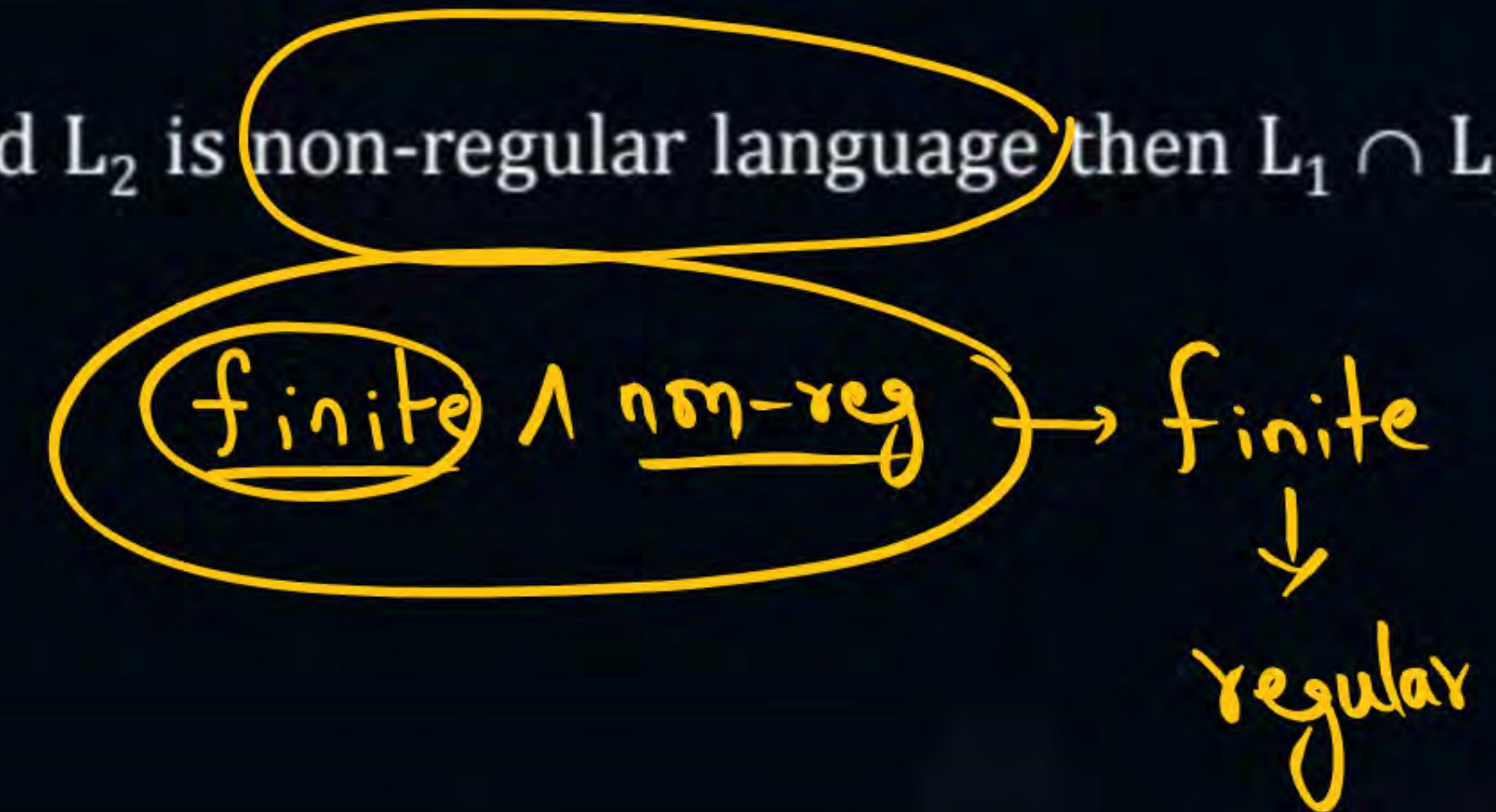
context-free Languages

DPP 01



By- Venkat sir

#Q. Suppose  $L_1$  is a finite language and  $L_2$  is non-regular language then  $L_1 \cap L_2$  will be:



- A Regular but infinite
- B Non-regular
- C / Finite and regular
- D None of these

#Q. Consider the following statements:

- (i) All finite language are context free language.
- (X) All regular language are finite.
- (X) All DCFL are finite.
- (✓) All regular language are DCFL
- (X) There exists some language which are finite and irregular.

The number of correct statements from the above statements are 2.



#Q. Consider the following languages.

$$L_1 = \{a^n b^n \mid n \geq 0\} \rightarrow \text{DCFL}$$

$$L_2 = \{a^n b^m c^k \mid n, m, k \geq 0 \wedge (n \neq m) \vee (m \neq k)\} \text{ CFL but not DCFL}$$

Which of the following statements is correct?

A

L<sub>1</sub> is CFL and L<sub>2</sub> is DCFL

C

L<sub>1</sub> and L<sub>2</sub> both are DCFL

B

L<sub>1</sub> is DCFL and L<sub>2</sub> is CFL

D

None of these.

(A, B, C)

#Q. Which of the following grammar is/are generating DCFL but not regular language?

$$\{a^n b^n\}$$

**A**  $S \rightarrow aa S bb | \epsilon$

**C**  $S \rightarrow aa S b | \epsilon$

$$\{a^{2n} b^n\}$$

$$\{a^n b^{2^n}\}$$

**B**  $S \rightarrow a S bb | \epsilon$

**D**  $S \rightarrow abS | \epsilon$

$$(ab)^k$$

#Q. Consider the following languages:

$$L_1 = \{a^m b^n c^k \mid \text{if } (m = \text{even}) \text{ then } (n = k)\} \rightarrow \text{DCFL}$$

$$L_2 = \{a^n c b^n\} \cup \{a^n d b^n\} \rightarrow \text{DCFL}$$

Which of the following is correct statement?

- A Only  $L_1$  is DCFL.
- B Only  $L_2$  is DCFL.
- C Both  $L_1$  and  $L_2$  are CFL but not DCFL
- D Both  $L_1$  and  $L_2$  are DCFL but not regular.

$xx^R yy^R$ 

$$\text{CFL} \cdot \text{CFL} = \text{CFL}$$

#Q. Consider the following grammar:

$$S \rightarrow AB$$

$$A \rightarrow aAa \mid bAb \mid \in \quad xx^R \rightarrow \text{CFL}$$

$$B \rightarrow aBa \mid bBb \mid \in \quad yy^R \rightarrow \text{CFL}$$

Which of the following is correct regarding above grammar?

- A** ✗ Language produced by S is  $L = \{xx^R yy^R \mid x, y \in \{a, b\}^*\}$  and L is DCFL but not regular.
- B** ✓ Language produced by S is  $L = \{xx^R yy^R \mid x, y \in \{a, b\}^*\}$  and L is CFL but not DCFL.
- C** ✗ Language produced by S is  $L = \{xx^R yy^R \mid x, y \in \{a, b\}^*\}$  and L is DCFL.
- D** None of the above.

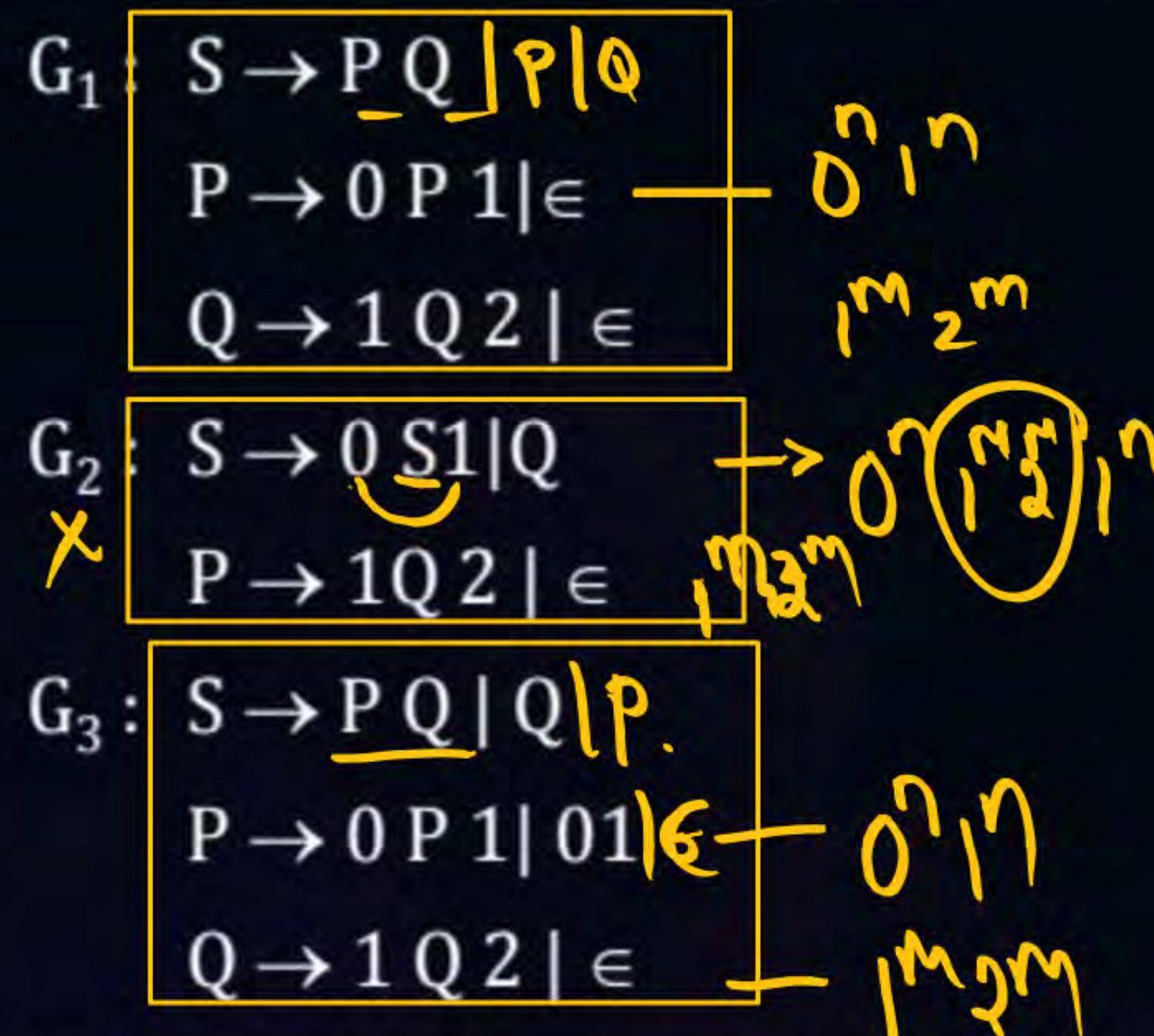
#Q. The intersection of CFL and a regular language will be

- A Always regular
- B Always CFL
- C Always not regular
- D None of these

$\text{CFL} \wedge \text{regular}$  → always CFL.  
may (or) may not regular

$$0^n \underline{1^n} 1^m 2^m = \underline{0^n 1^{n+m}} 2^m$$

#Q. Consider the following grammars  $G_1$ ,  $G_2$  and  $G_3$ :



- A  $G_1$  and  $G_2$  are equivalent
- B  $G_1$  and  $G_3$  are equivalent
- C  $G_2$  and  $G_3$  are equivalent
- D None of these

Here,  $\{S, P, Q\}$  are variables where  $S$  is start symbol.  $\{0, 1, 2\}$  are terminals.

Which of the following is true?

[MCQ]

$$\begin{array}{c} \text{CSL} \wedge \text{CSL} \xrightarrow{\quad} \underline{\text{CSL}} \\ \text{CSL} \wedge \text{CFL} \end{array}$$

P  
W

#Q. Consider the following language.

L<sub>1</sub> = Context free language. ✓

L<sub>2</sub> = Deterministic context free language.

L<sub>3</sub> = Context sensitive language.

L<sub>4</sub> = Regular

Which of the following is incorrect?

A

L<sub>2</sub> . L<sub>4</sub> is always DCFL. → false

C

$\Sigma^*$  - L<sub>3</sub> is CSL. → true

B

L<sub>1</sub> ∩ L<sub>3</sub> is CSL. → true

D

None of the above.

DCFL . regular

DCFL . DCFL

#Q. Consider the following push down automata.

$$PDA = \{Q, \Sigma, \delta, \Gamma, q_0, Z_0, q_f\}$$

$$a^* \cup \underline{a^n b^m} \underline{c^{n+m}}$$

Which of the following language is accepted by above PDA?

**A**

$$L = \{a^*\} \cup \{a^p b^q c^r \mid p, q, r \geq 1, p + q = r\}$$

**B**

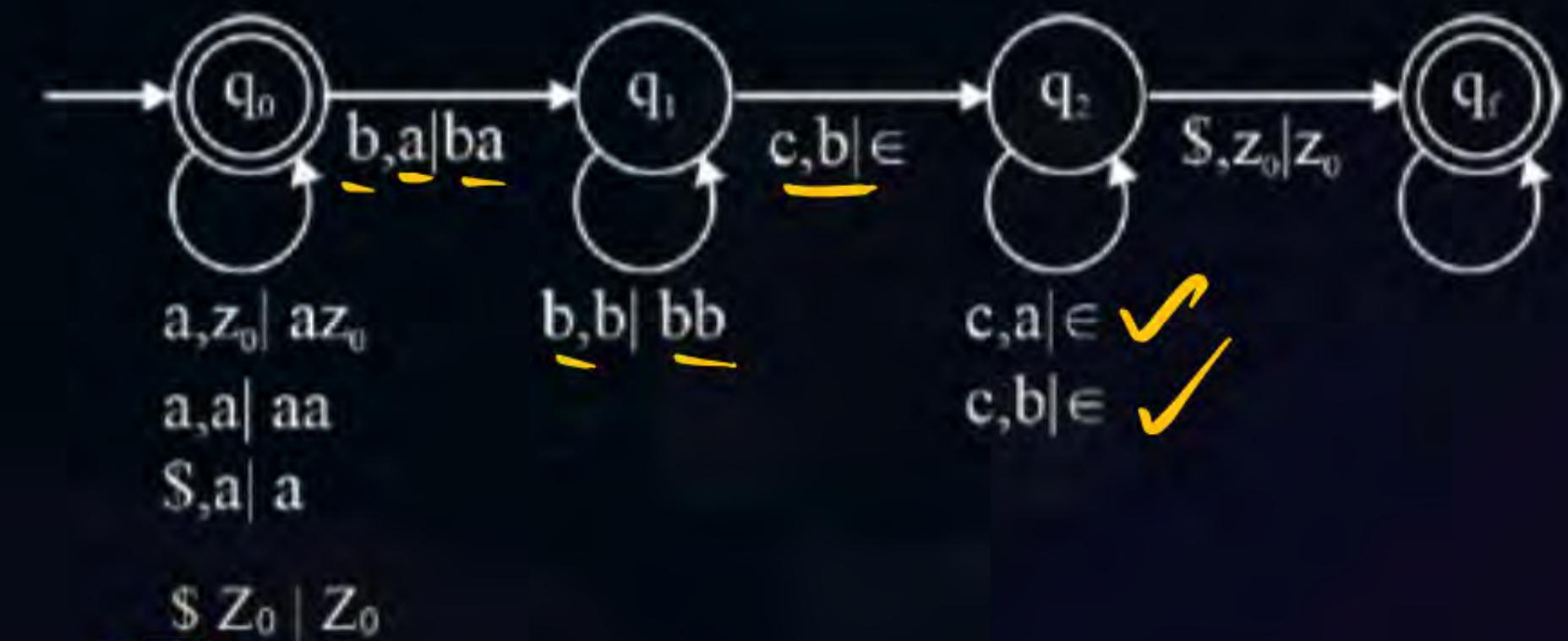
$$L = \{a^{p+q} b^{q+r} \mid p, q, r \geq 0\}$$

**C**

$$L = \{a^p b^q c^r \mid p, q, r \geq 1\}$$

**D**

None of the above





#Q. Consider the following language:

$$L_1 = \{ab^n a^{2n} \mid n \geq 1\} \rightarrow \text{DCFL}$$

$$L_2 = \{aab^n a^{3n} \mid n \geq 1\} \rightarrow \text{DCFL}$$

(A, D)

Which of the following is correct?

- A** ✓  $L_1 \cup L_2$  is DCFL but not regular.
- B**  $L_1 \cup L_2$  is CFL but not DCFL.
- C**  $L_1 \cup L_2$  is CSL but not CFL.
- D** ✓  $L_1 \cup L_2$  is DCFL and also CFL.

#Q. Suppose, L is any CFL language on alphabet

$\Sigma = \{a, b\}$ , and the following language:

$$L_1 = L - \underbrace{\{w x w^R \mid w, x \in \{a,b\}^*\}}_{(a+b)^*} - \emptyset$$

$$L_2 = L_1 \cdot L - \emptyset$$

$$L_3 = \bar{L}_1 \cup L = \Sigma^*$$

Which of the following is/are correct?

(A, B, C)

A

$L_1$  is regular

B

$L_2$  is CFL.

C

$L_3$  is regular.

D

None of these



THANK - YOU