

CS & IT ENGINEERING



Algorithms

Greedy Method

Lecture No.- 04

By- Aditya Jain sir



Topics to be Covered



Topic

Topic

Topic

OMP

Huffman Encoding



About Aditya Jain sir



1. Appeared for GATE during BTech and secured AIR 60 in GATE in very first attempt - City topper
2. Represented college as the first Google DSC Ambassador.
3. The only student from the batch to secure an internship at Amazon. (9+ CGPA)
4. Had offer from IIT Bombay and IISc Bangalore to join the Masters program
5. Joined IIT Bombay for my 2 year Masters program, specialization in Data Science
6. Published multiple research papers in well known conferences along with the team
7. Received the prestigious excellence in Research award from IIT Bombay for my Masters thesis
8. Completed my Masters with an overall GPA of 9.36/10
9. Joined Dream11 as a Data Scientist
10. Have mentored 12,000+ students & working professionals in field of Data Science and Analytics
11. Have been mentoring & teaching GATE aspirants to secure a great rank in limited time
12. Have got around 27.5K followers on Linkedin where I share my insights and guide students and professionals.

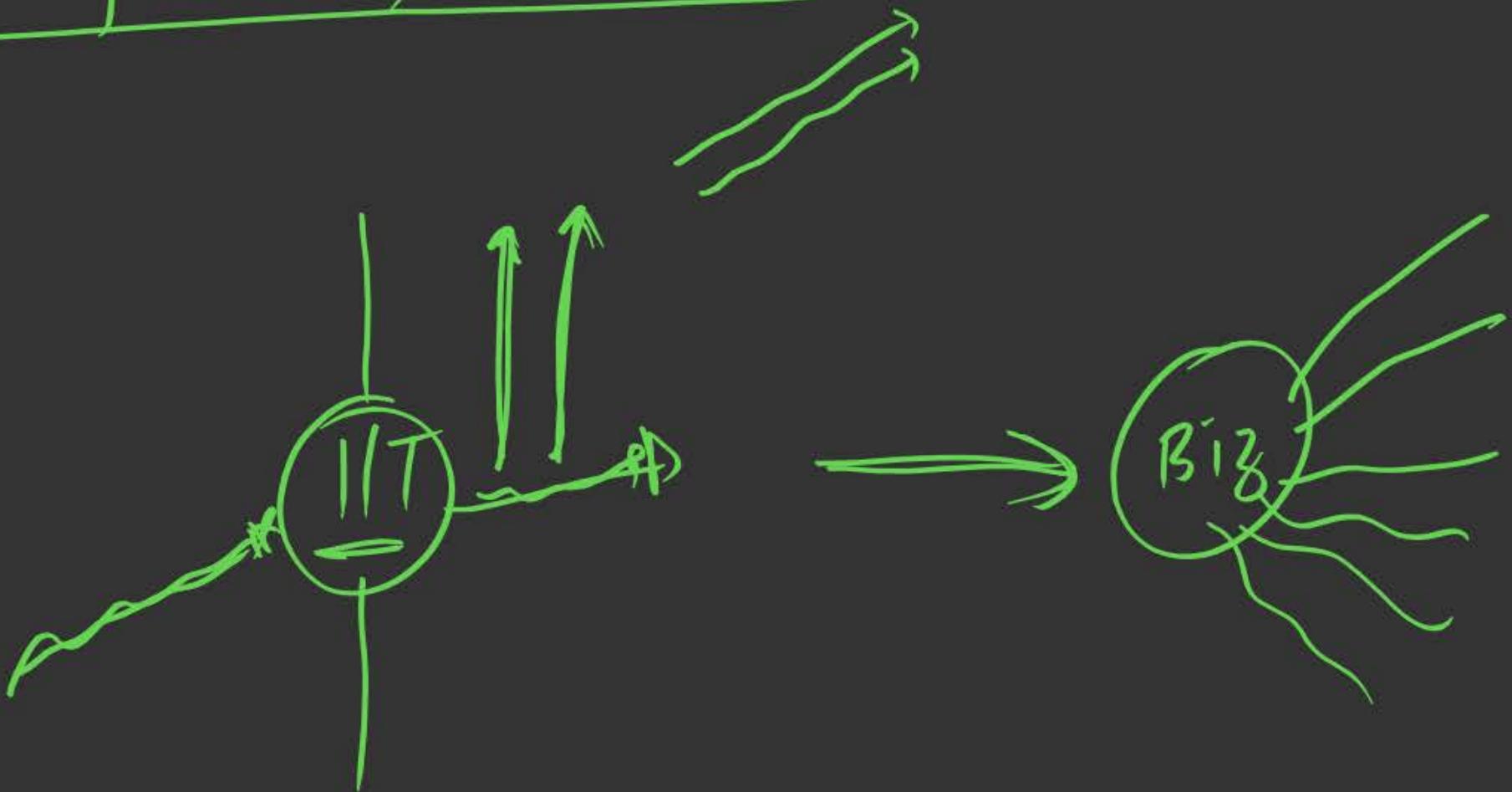


Telegram Link for Aditya Jain sir: https://t.me/AdityaSir_PW

OMP

Bnute force: $O(n!)$ $\approx O(n^n)$

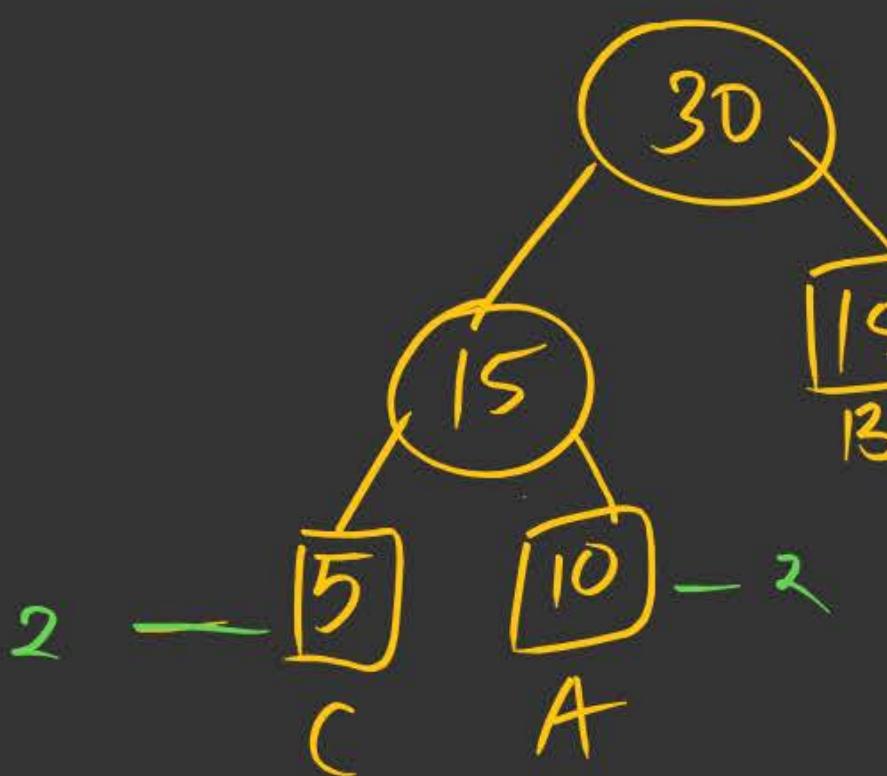
Optimal (Greedy based) Approach -



Optimal (Greedy based) Approach:

Optimal Binary Merge Tree

$$A = 10 \quad \cancel{\textcircled{2}}$$
$$B = 15 \quad \textcircled{3}$$
$$C = 5 \quad \cancel{\textcircled{4}}$$



1 TRM
= sum of all internal nodes

Appr 2 :-

$$TRM = \sum_{i=1}^{\infty} d_i q_i = 2 \times 5 + 2 \times 10 + 1 \times 15 \\ = 10 + 20 + 15 \\ = \textcircled{45} \quad \dots$$

d_i - depth (no. edges)

q_i - size



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Optimal merge pattern

Eg.1. A : 10(2)

B : 15(3)

C : 5(1)

2. The total number of record movement = weighted external path length of the 2 - way binary merge tree.

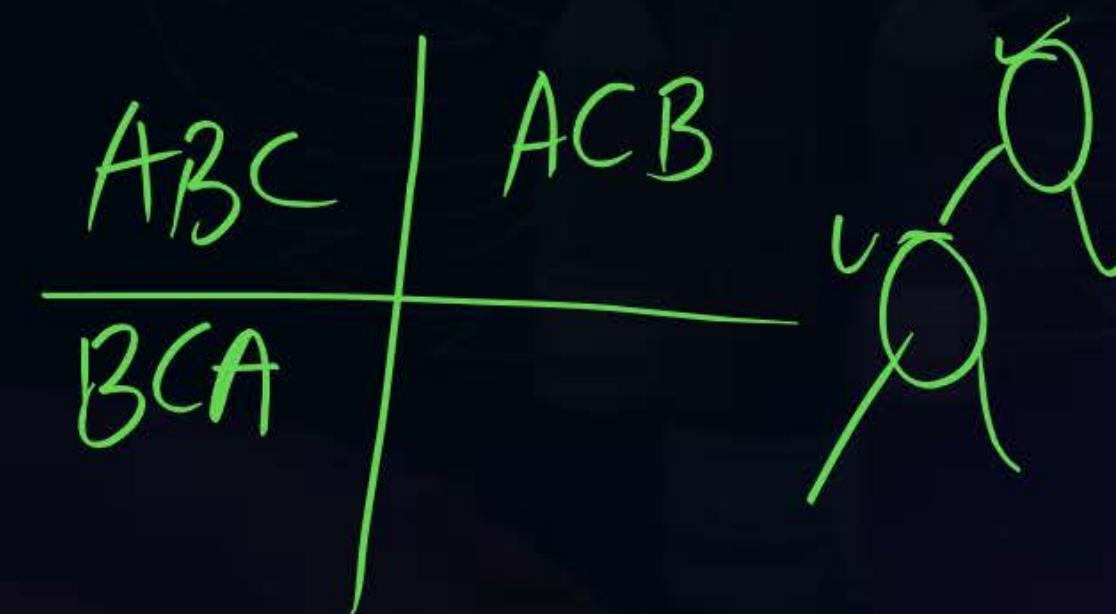
Minimum record movement

$$= \sum d_i * q_i$$

$$= 2 \times 10 + 1 \times 15 + 2 \times 5$$

$$= 20 + 15 + 10$$

$$= 45$$



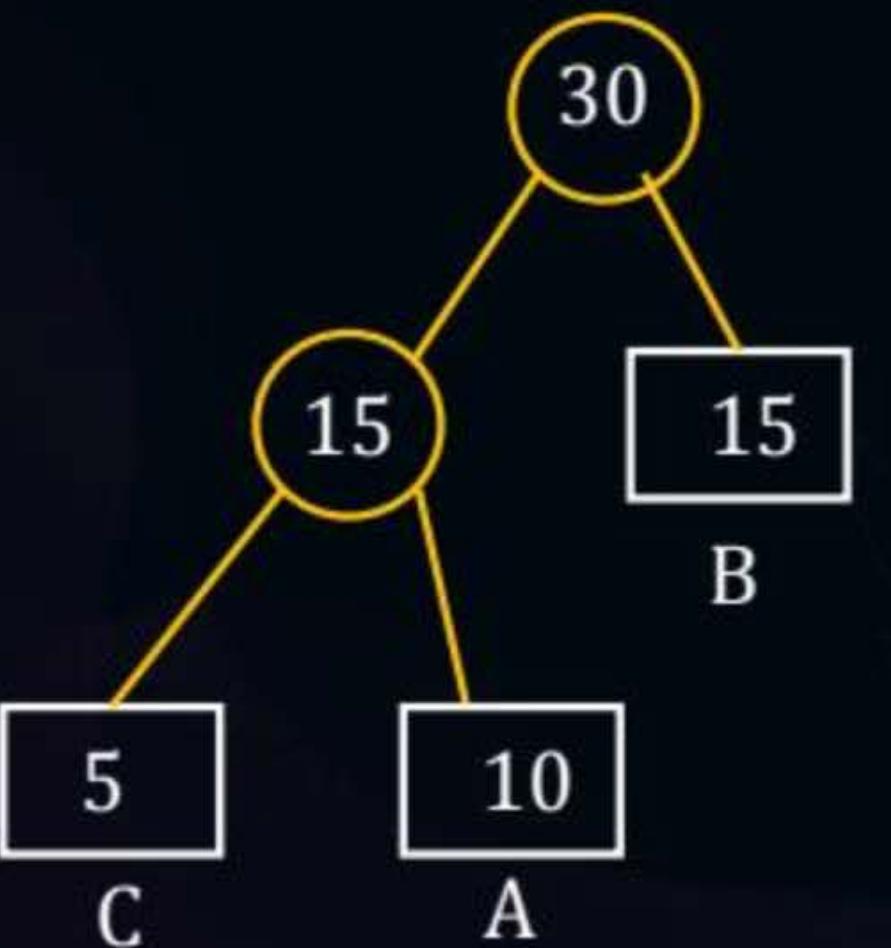


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Optimal 2-way Binary merge Tree

Min total record movement = $15 + 30 = 45$





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Greedy algo for optimal merge patterns

```
Struct tree_node  
{  
    tree_node * Lchild;  
    tree_nodes * Rchild ;  
    int weight;  
};
```



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Algo Tree (n)

{

// list is a global list of n single nodes binary tree, as described before

for i : 1 to (n-1) ; $\rightarrow O(n)$

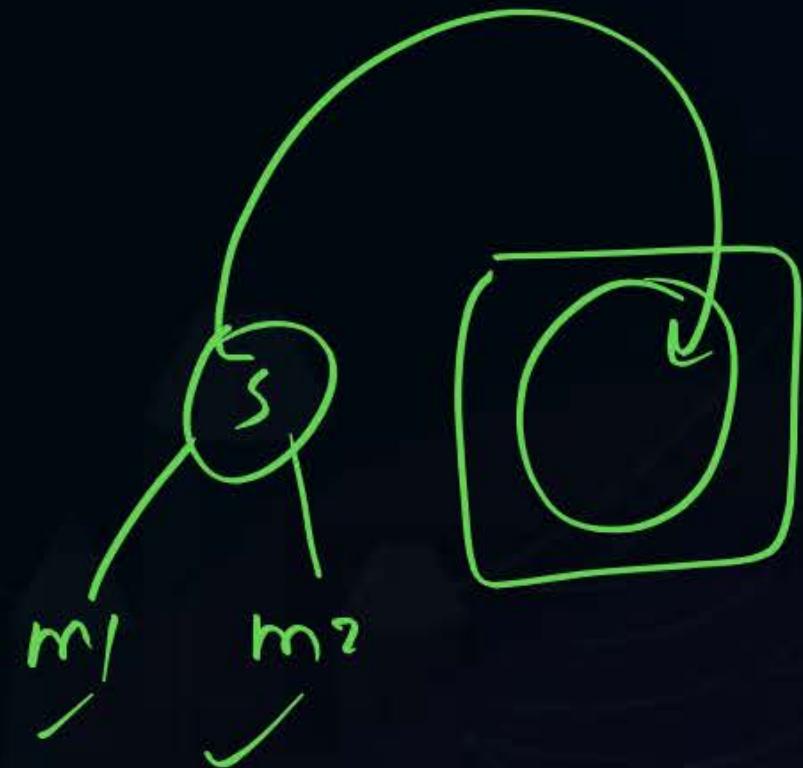
{

1. Pt = new (tree_node);
2. Pt \rightarrow Lchild = minimum (list);
3. Pt \rightarrow Rchild = minimum (list);
4. Pt \rightarrow weight = ((Pt \rightarrow Lchild) \rightarrow weight)
((Pt \rightarrow Rchild) \rightarrow weight)

5. insert (list, Pt);
}

return minimum(list);

}





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Time complexity: (for 'n' files)

1. Linear linked list:

('n' elements)

Insert $\rightarrow O(1)$

Minimum $\rightarrow O(n)$

Overall TC $\rightarrow O(n*n) = O(n^2)$



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Implementation of list

2. Heap (non-linear)

(‘n’ elements)

Insert ✓

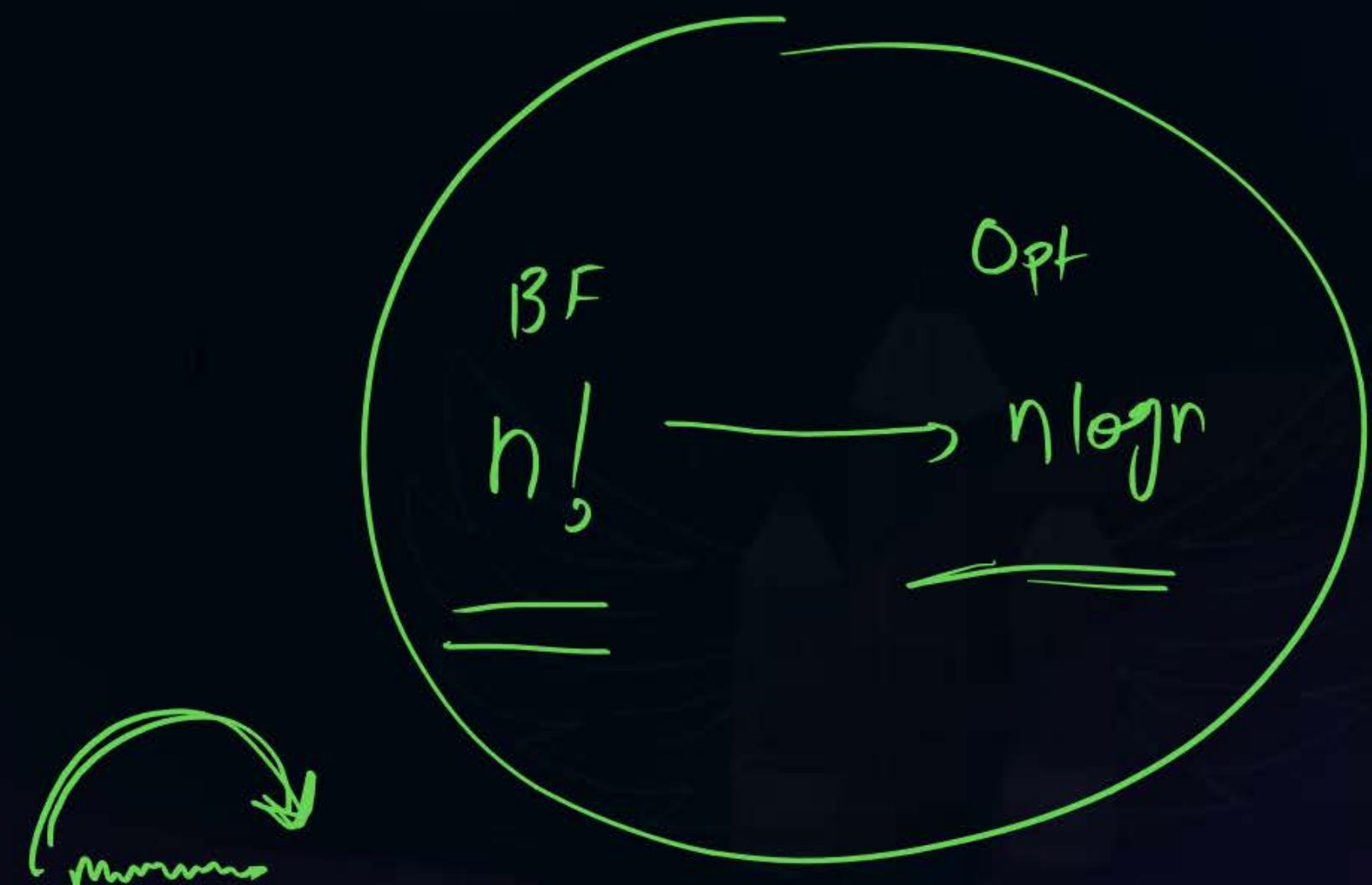
Delete ✓

Dec./Inc. ✓

$O(\log n)$

Min Heap: Minimum $\rightarrow O(1)$

Overall TC: $O(n \log n)$

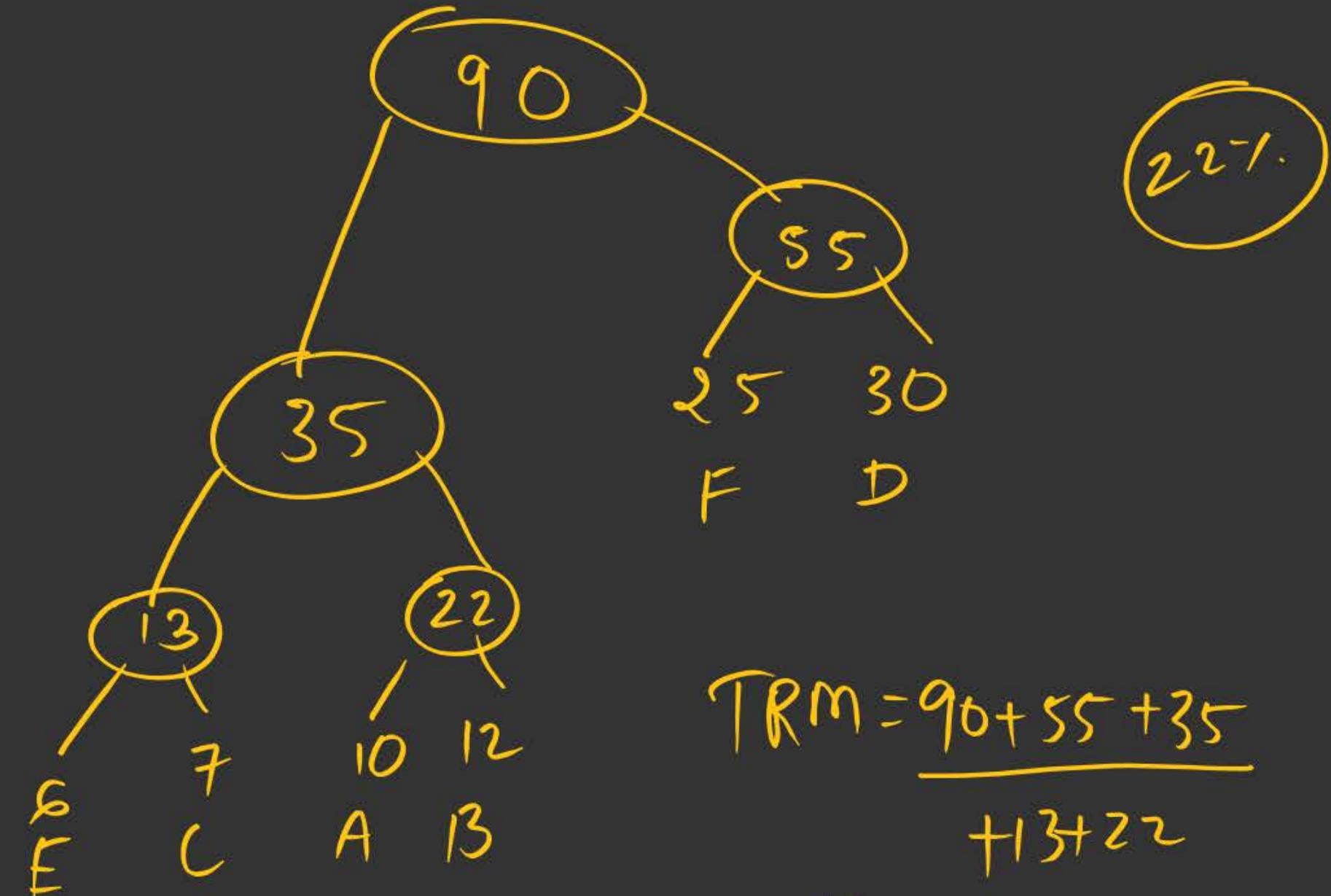


min TRM?

(Q)

A - 10 - 3 /
B - 12 - 4 /
C - 7 - 2 /
D - 30 - 6 /
E - 6 - 1 /
F - 25 - 5 /

13, 22, 35, 55



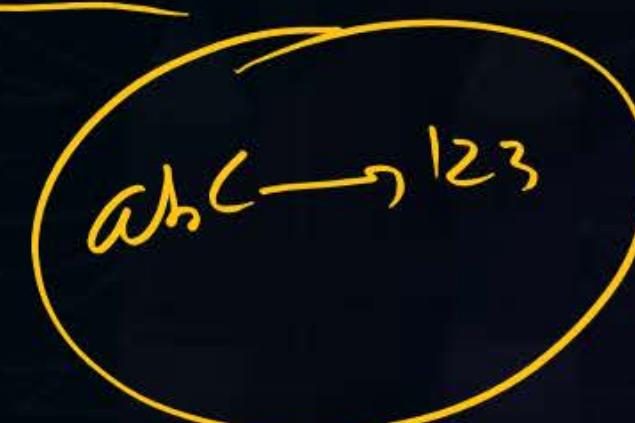


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3. Huffman Encoding

- Application of optimal merge pattern
- Data encoding and data compression Technique
- Representing some elements with a unique code
- Compression → Reduce size of data without data loss





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Eg.1.

4 Characters /elements

w, x, y, z

Straight forward Binary encoding

Normal Encoding

or

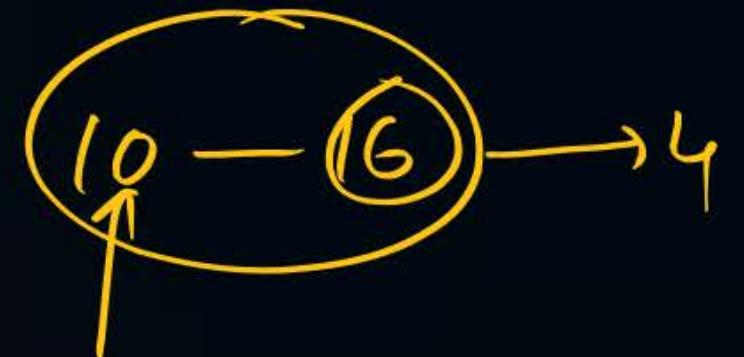
Uniform Encoding

$$\begin{aligned} W &\rightarrow 0\ 0 \\ X &\rightarrow 0\ 1 \\ Y &\rightarrow 1\ 0 \\ Z &\rightarrow 1\ 1 \end{aligned}$$

4



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If we use uniform encoding:

1. 6 elements \rightarrow 3 bits
2. 10 elements \rightarrow 4 bit $\rightarrow \log_2 10 \rightarrow \lceil 3. x \rceil$

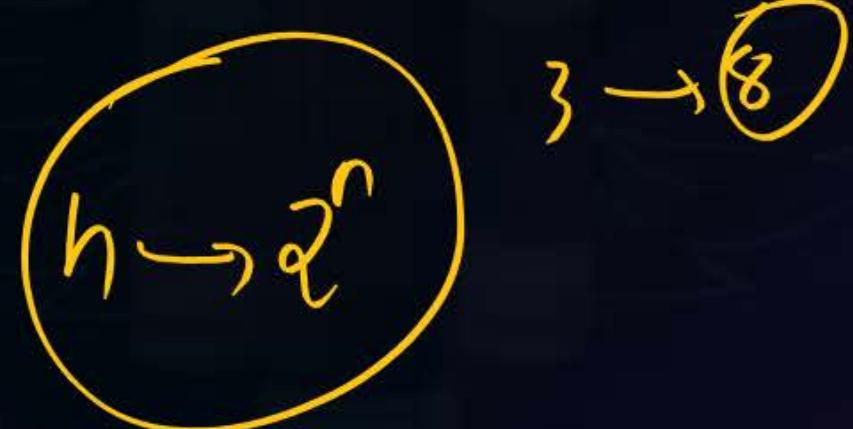
$\rightarrow 4$

$2 \rightarrow 4$
 $3 \leftarrow 6$

4 bits \rightarrow max $2^4 = \underbrace{16 \text{ elements}}$ can be uniquely encoded

6 elem

3. 17 element \rightarrow 5 bits.....
4. 100 elements \rightarrow 7 bits/ elements or characters.





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In general

To represent N elements using uniform encoding

we need $\lceil \log_2 (N) \rceil$ bit/character.

$$\lceil \log_2 10 \rceil = 4 \quad \lceil \log_2 8 \rceil = 3$$

Imp. Observations:

1. Using uniform encoding, data compression is not possible.
2. Hence, for data compression we need non-uniform encoding.



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V.V.'imp

Huffman Encoding (non-uniform encoding)

Idea:- Encoding/code → assigned based on the frequency of that character or elements.

Logic:- (no. of bits to encode) ~~×~~ $\frac{1}{(\text{freq.of character})}$

1. Assign more bits to low frequently occurring elements.
2. Assign less bits to high frequently occurring elements.
3. No 2 elements/characters will have the same encoding (as it needs to be unique).



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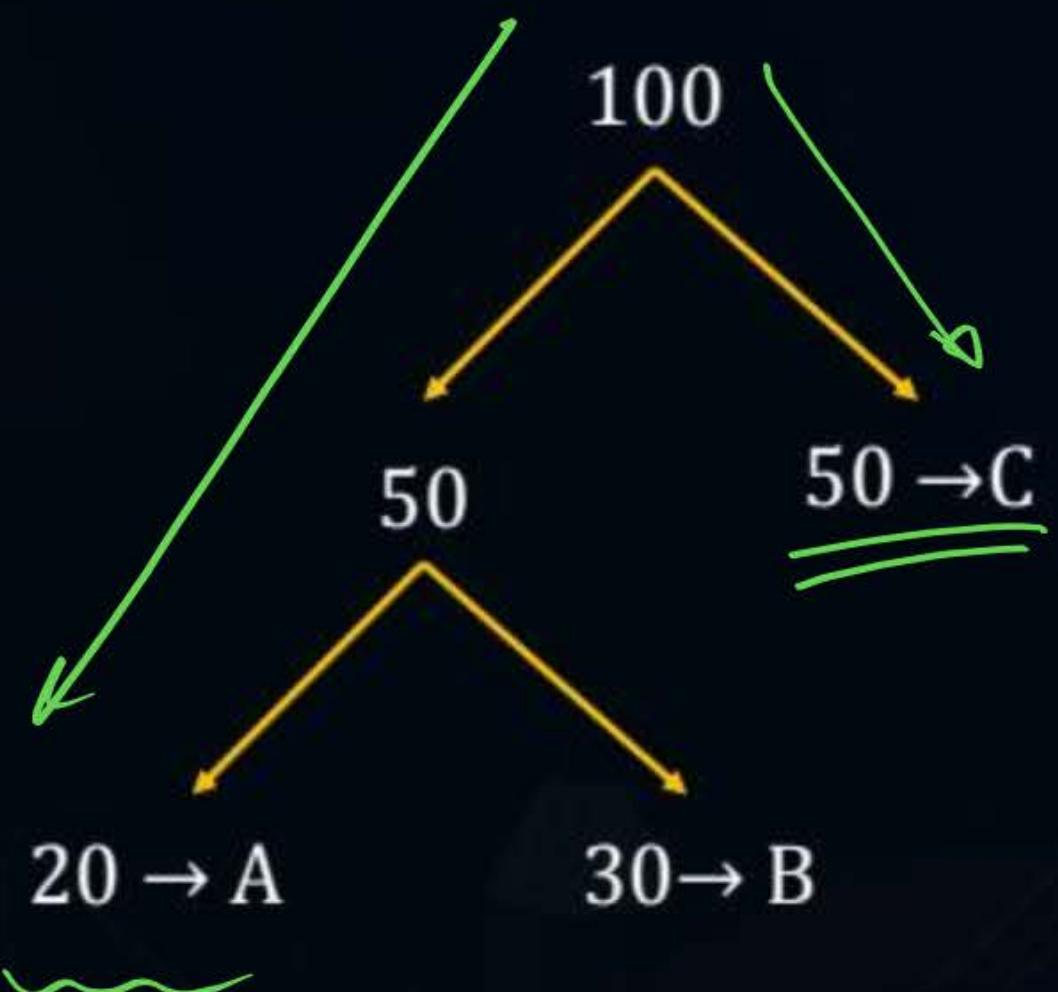


Eg.1. $A \rightarrow 20$

$B \rightarrow 30$

$C \rightarrow 50$

"A B C B C C"
 (| |



Overall total bits compression



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Note:- Start from lowest level.

Char	freq/prob
A	$\rightarrow 0.23 \dots (4)$
B	$\rightarrow 0.05 \dots (1)$
C	$\rightarrow 0.48 \dots (5)$
D	$\rightarrow 0.15 \dots (3)$
E	$\rightarrow 0.09 \dots (2)$

Priority (low to high)

Avg bits/char

$$\left\lceil \frac{n=5}{\log_2 5} \right\rceil = 3$$



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Eg..

Given: Language/ Elements $\Rightarrow \{A, B, C, D, E\} \rightarrow 5$ character

If uniform encoding: $\lceil \log_2 N \rceil$ bits / character

$$= \lceil \log_2 5 \rceil$$

$$= 3 \text{ bit / character}$$



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P
W

2-way Optimal Binary merge tree:

Left Branch → 0

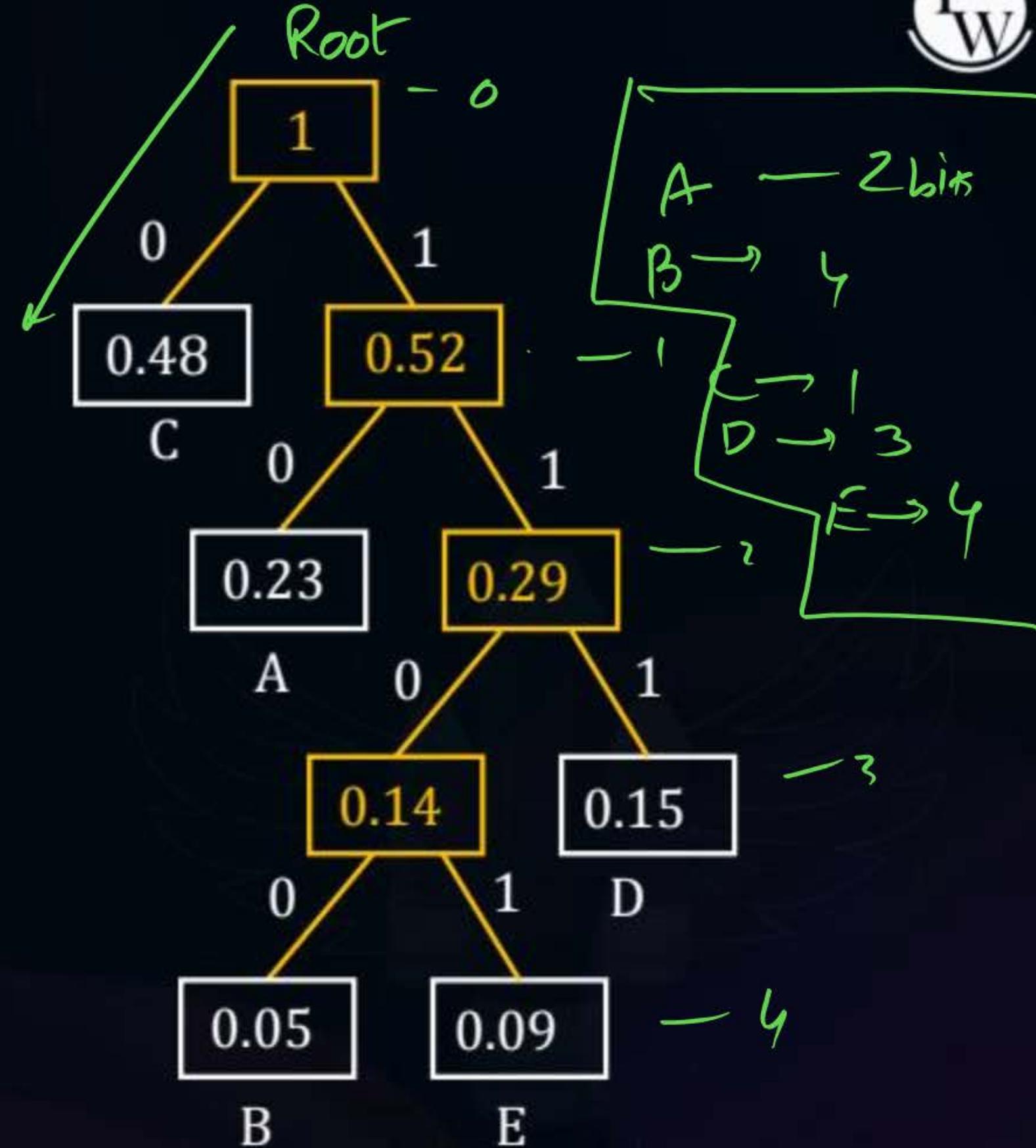
Right Branch → 1

Standard

Left → Smaller

Right → Larger

A
B
C
D
E



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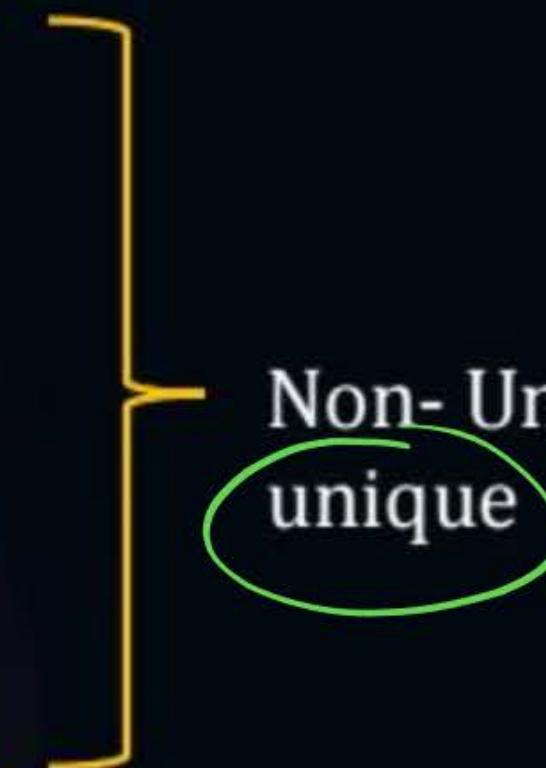
A → 10 → 2 bits

B → 1100 → 4 bits

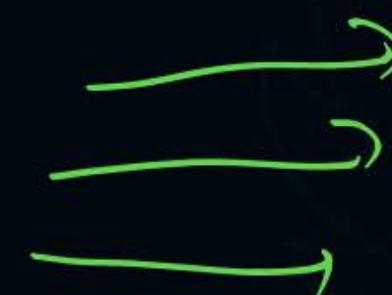
C → 0 → 1 bits

D → 111 → 3 bits

E → 1101 → 4 bits



Non- Uniform encoding & all are
unique





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#Q. Average number of bit required using Huffman encoding?

= Weighted external path length: (Sum of internal nodes)

$$= \sum_{i=1}^n d_i * q_i$$

$$\approx \underline{\underline{1.95}} \text{ bits/char}$$



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(extension of prev)

#Q. "CCACCCABC"

How many bit required to represent the above text :-

1. Uniform Encoding: $\rightarrow 3 \times 10 = 30 \text{ bits}$

2. Huffman Encoding:

(Non-uniform)

17 bits



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2. Using Huffman Encoding:

Text: C C A C C C A B D C

0 0 10 0 0 0 101100111 0

Final Encoding:

00100001011001110

Total = 17 bit (compressions)

A → 2
B → 1
C → 6
D → 1
E → 0

$$\begin{aligned} \text{Total bits} &= 2 \times 2 + 1 \times 4 \\ &\quad + 6 \times 1 + 1 \times 3 \\ &\quad + 0 \times 4 \\ &= \underline{17 \text{ bits}} \end{aligned}$$



2 mins Summary

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THANK - YOU