

# Computer Science & IT

## Database Management System



**Query Languages**

**Lecture No. 02**



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# Recap of Previous Lecture



✓ Topic

Query languages

✓ Topic

Relational Algebra

✓ Topic

Basic relational algebra operations



# Topics to be Covered



Topic

Join operations



Topic

Division operation





## Topic : Derived Relational Algebra operators

1. Intersection ( $\cap$ )  $\rightarrow$  It is a set op<sup>n</sup>, it can be performed only if relation are Union Compatible
2. Join Operations (" $\bowtie$ ")
3. Division Operation ( $\div$ )

$\Downarrow$   
Intersection is a derived relational algebra op<sup>n</sup>, it is derived using "Set difference"  
$$R \cap S = R - (R - S)$$





## Topic : Join Operations



Join operations are used to join relational tables based on some condition.

Using Cross Join each tuple of 1<sup>st</sup> table will be joined with each tuple of 2<sup>nd</sup> table



## Topic : Types Join Operations

- 1) Inner join
  - a. Theta join
  - b. Equi join
  - c. Natural join

{ Using inner join, we select only those tuples from both the relations that satisfy the join condition }

- 2) Outer join
  - a. Left outer join
  - b. Right outer join
  - c. Full outer join

{ In outer join we can also select the tuples from one or both the relations, that failed the join Cond<sup>n</sup> }



## Topic : Inner join



Inner join, includes only those tuples that satisfy the join condition.





## Topic : Theta join



(Also Known as Conditional Join)

The general case of JOIN operation is called a Theta join. It is denoted by symbol  $\theta$  . i.e.  $\bowtie_{\theta}$

it can be any condition

- Theta join can use any conditions in the selection criteria.

$<, \leq, >, \geq, =, <>$



Student (S)

Sid	Sname
2	A
3	B
4	A

Employee (E)

Eid	Ename
2	B
5	A
5	B

Student ⋈

(Student.Sid < Employee.Eid)

Employee

We can use any Cond<sup>n</sup> in theta join

it is the join Cond<sup>n</sup>

≡

$\sigma_{S.Sid < E.Eid}(\overset{\sim}{S} \times \overset{\sim}{E})$

∏:

S.Sid	S.Sname	E.Eid	E.Ename
2	A	4	A
2	A	5	A
3	B	5	B
4	A	5	B

No projection op<sup>n</sup> is used.  
 ∴ All attributes of "SxE" will be present in output.



## Topic : Equijoin



{ Equi-join is a type of theta join,  
where Cond<sup>n</sup> is Equality Cond<sup>n</sup> }

An equijoin is a theta join using the equality operator.

In equijoin the condition is always equality condition.

It is a type of theta join.

It need not be on  
the common attributes



Student (S)

Sid	Sname
2	A
3	B
4	A

Employee (E)

Eid	Ename
2	B
4	A
5	B

Student ⋈

(Student.Sid = Employee.Eid)

Attribute need not be  
Common attribute

Employee

Equality Cond<sup>n</sup>  
∴ It can be  
Called Equi-join %P =

$\equiv \left( \sigma_{S.Sid = E.Eid} (S \times E) \right)$

S.Sid	S.Sname	E.Eid	E.Ename
2	A	2	B
4	A	4	A

✓ Student (S)

Sid	Sname
2	A
3	B
4	A

✓ Enroll (E)

Sid	Cid
2	C <sub>1</sub>
4	C <sub>2</sub>
5	C <sub>3</sub>

Student ⋈ Enroll  
(Student.Sid = Enroll.Sid)

Attribut may be Common attribute as well

Equi-join

$\equiv \left( \sigma_{S.Sid = E.Sid} (S \times E) \right)$

Op =

S.Sid	S.Sname	E.Sid	E.Cid
2	A	2	C <sub>1</sub>
4	A	4	C <sub>2</sub>

It is not natural join.  
In Natural join  
We do not specify  
join Cond<sup>n</sup>.

If we perform  
Equi-join, then  
Common attributes  
from each relation  
will be present  
in output!



Note:- If we use theta join or Equi-join then we need to specify the join condition explicitly, which is not the case with natural join.

In natural join we do not specify any Cond<sup>n</sup>, because by default Cond<sup>n</sup> for natural join is Equality Condition on all common attributes.



## Topic : Natural join ( $\bowtie$ )

Natural join is performed based on the equality condition on all common attributes (column) between the relations. The name and type of common attributes must be same.

Additionally, a natural join removes the duplicate columns involved in the equality comparison so only one of each compared column remains

Student (Sid, Sname)  $\bowtie$  Enroll (Stu-id, Cid)  
There is no common attribute between Student &  
Enroll wrt. Natural join



## • Natural Join ( $\bowtie$ )

Natural join is a derived relational algebra op<sup>n</sup>.  
which can be derived using three basic relational algebra op<sup>n</sup>.  
ie; Cross product, Selection and Projection.

### Derivation of Natural join

$R \bowtie S =$

Step-1 : obtain  $R \times S$

Step-2 : Select the tuples from  $R \times S$  based on Equality Cond<sup>n</sup> on all common attributes of  $R$  and  $S$ .

Step-3 : From the output of Step-2 project distinct attributes

# Student (S)

Sid	Sname
2	A
3	B
4	A

# Enroll (E)

Sid	Cid
2	C <sub>1</sub>
4	C <sub>2</sub>
5	C <sub>3</sub>

$$\text{Student} \bowtie \text{Enroll} = \pi_{\text{Sid}, \text{Sname}, \text{Cid}} \left( \sigma_{\text{Student.Sid} = \text{Enroll.Sid}} (\text{Student} \times \text{Enroll}) \right)$$

\* No Cond<sup>n</sup> is specified  
 ↓  
 ∴ Natural join

O/p =

"Sid" will be present only once in the o/p

Sid	Sname	Cid
2	A	C <sub>1</sub>
4	A	C <sub>2</sub>



eg:  $R(A\ B\ C)$  &  $S(B\ C\ D)$

$$R \bowtie S = \pi_{A,B,C,D} \left( \sigma_{\substack{R.B = S.B \\ \wedge \\ R.C = S.C}} (R \times S) \right)$$

Equality Cond<sup>n</sup> ✓  
on all common  
attributes

eg.  $R(\overset{\sim}{A}, \overset{\sim}{B}, \overset{\sim}{C})$  &  $S(\overset{\sim}{D}, \overset{\sim}{E})$

$$R \bowtie S = \pi_{\overset{\sim}{A}, \overset{\sim}{B}, \overset{\sim}{C}, \overset{\sim}{D}, \overset{\sim}{E}} \left( \underbrace{\quad}_{\text{No Common attributes b/w R \& S}} (R \times S) \right) \equiv R \times S$$

No Common attributes b/w R & S  
∴ No Selection Cond<sup>n</sup>.

And hence all the tuples of  $R \times S$   
will get selected

And finally all attributes  
of  $R \times S$  will be projected.

∴ O/p will be exactly same as  $R \times S$

✓  
If there is no  
Common attribute  
between R and S,  
then Natural join  
of R and S will  
be equal to " $R \times S$ "




Student (S)

Sid	Sname
2	A
3	B
4	A

Employee (E)

Eid	Ename
2	B
4	A
5	B

$$\begin{matrix} (S) & (E) \\ \text{Student} & \bowtie \text{Employee} \end{matrix} \equiv S \times E$$

  
 No Common  
 attributes b/w  
 Student & Enroll



## Topic : Outer join



In an outer join, along with tuples that satisfy the join condition, we also include tuples that do not match the criteria either from left hand side relation, or from right hand side relation or both.





## Topic : Left Outer Join ( $\bowtie$ )

$R \bowtie S =$  All tuples of  $R \bowtie S$ , along with the tuples from left hand side relation { i.e.,  $R \in R$  } that failed the join Cond<sup>n</sup>



## Topic : Right Outer Join ( $\bowtie$ )

$R \bowtie S =$  All tuples of  $R \bowtie S$  along with the tuples of right hand side relation {i.e,  $R \bowtie S$ } that failed the join condition.





## Topic : Full Outer Join ( $\bowtie$ )

$R \bowtie S$  : All tuples of  $R \bowtie S$  along with the tuples from both side relation that failed the join condition

✓ R:

A	B	C
1	2	3
1	4	5

RMS=

A	B	C	D
1	2	3	4

✓ S:

B	C	D
2	3	5
5	6	7
5	7	9

RMS=

A	B	C	D
1	2	3	4
1	4	5	NULL

RMS=

A	B	C	D
1	2	3	4
NULL	5	6	7
NULL	4	7	9

RMS=

A	B	C	D
1	2	3	4
1	4	5	NULL
NULL	5	6	7
NULL	4	7	9



Division



## Topic : Division ( $\div$ )



Division operation is used whenever the query is with respect to every or all.



eg. Consider following three relations.

Student (S)

<u>Sid</u>	Sname
S <sub>1</sub>	A
S <sub>2</sub>	A
S <sub>3</sub>	B
S <sub>4</sub>	C

Enroll (E)

<u>Sid</u>	<u>Cid</u>	fee
S <sub>1</sub>	C <sub>1</sub>	-
S <sub>1</sub>	C <sub>2</sub>	-
S <sub>2</sub>	C <sub>2</sub>	-
S <sub>1</sub>	C <sub>3</sub>	-
S <sub>2</sub>	C <sub>3</sub>	-
S <sub>3</sub>	C <sub>3</sub>	-

Course (C)

<u>Cid</u>	Cname
C <sub>1</sub>	OS
C <sub>2</sub>	COA
C <sub>3</sub>	DBMS

Query:-

Retrieve Sids of the students who have  
Enrolled for all Courses.





Student (S)

Sid	Sname
S <sub>1</sub>	A
S <sub>2</sub>	A
S <sub>3</sub>	B
S <sub>4</sub>	C

Enroll (E)

Sid	Cid	fee
S <sub>1</sub>	C <sub>1</sub>	
S <sub>1</sub>	C <sub>2</sub>	
S <sub>2</sub>	C <sub>2</sub>	
S <sub>1</sub>	C <sub>3</sub>	
S <sub>2</sub>	C <sub>3</sub>	
S <sub>3</sub>	C <sub>3</sub>	

Course (C)

Cid	Cname
C <sub>1</sub>	OS
C <sub>2</sub>	COA
C <sub>3</sub>	DBMS

\* Retrieve Sids of the students who have Enrolled for all Courses.

↳ We are actually looking for the Sids in the Enroll table that are associated with all 'Cids' of Course table


Desired result can be produced by the following relational algebra Expression

$$\pi_{sid, cid}(E) \div \pi_{cid}(C) \Rightarrow o/p$$

Sid
S <sub>1</sub>

It will produce the Sids that are associated with all Cid of Course table

Enroll (E)	
Sid	Cid
S <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>
S <sub>2</sub>	C <sub>2</sub>
S <sub>1</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>3</sub>
S <sub>3</sub>	C <sub>3</sub>

$\pi_{\text{Sid}} (E) \Rightarrow \text{o/p} =$   
  
 This R.A. Expression  
 Will produce the  
 Sids of the Students  
 who have enroll for  
 some Course  
 ↓  
 {at least 1}

Sid
S <sub>1</sub>
S <sub>2</sub>
S <sub>3</sub>



Course(C)	
Cid	Cname
C <sub>1</sub>	OS
C <sub>2</sub>	COA
C <sub>3</sub>	DBMS

$\pi_{Cid}(C) \Rightarrow \text{o/p} =$

Cid
C <sub>1</sub>
C <sub>2</sub>
C <sub>3</sub>

This R.A. Expression  
will produce  
Cids of all  
Courses.

$$\pi_{\text{Sid}}(E) = \begin{array}{|c|} \hline \text{Sid} \\ \hline S_1 \\ S_2 \\ S_3 \\ \hline \end{array} \quad \checkmark$$

$$\pi_{\text{Cid}}(C) = \begin{array}{|c|} \hline \text{Cid} \\ \hline C_1 \\ C_2 \\ C_3 \\ \hline \end{array} \quad \checkmark$$

$$\pi_{\text{Sid}}(E) \times \pi_{\text{Cid}}(C) \Rightarrow \text{o/p} = \begin{array}{|c|c|} \hline E.\text{Sid} & C.\text{Cid} \\ \hline \end{array}$$

This R.A. Expression will produce a universal relation, in which Every student who has Enrolled for some Courses is Combined with all Courses.

E.Sid	C.Cid
S <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>
S <sub>1</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>1</sub>
S <sub>2</sub>	C <sub>2</sub>
S <sub>2</sub>	C <sub>3</sub>
S <sub>3</sub>	C <sub>1</sub>
S <sub>3</sub>	C <sub>2</sub>
S <sub>3</sub>	C <sub>3</sub>



$$\pi_{\text{sid, cid}}(E) \Rightarrow \text{o/p} =$$

Sid.	Cid.
S <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>
S <sub>2</sub>	C <sub>2</sub>
S <sub>2</sub>	C <sub>2</sub>
S <sub>1</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>3</sub>
S <sub>3</sub>	C <sub>3</sub>

$$(\pi_{sid}(E) \times \pi_{cid}(C)) - \pi_{sid,cid}(E) = \text{o/p} =$$

$\Rightarrow \text{o/p} =$

E.Sid	C.Cid
S <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>
S <sub>1</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>1</sub>
S <sub>2</sub>	C <sub>2</sub>
S <sub>2</sub>	C <sub>3</sub>
S <sub>3</sub>	C <sub>1</sub>
S <sub>3</sub>	C <sub>2</sub>
S <sub>3</sub>	C <sub>3</sub>

Sid	Cid
S <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>
S <sub>2</sub>	C <sub>2</sub>
S <sub>1</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>3</sub>
S <sub>3</sub>	C <sub>3</sub>

Sid	Sid
S <sub>2</sub>	C <sub>1</sub>
S <sub>3</sub>	C <sub>1</sub>
S <sub>3</sub>	C <sub>2</sub>



\* Retrieve Sids of the students who have Enrolled for all Courses.

Ans:  $\pi_{sid, cid}(E) \div \pi_{cid}(C)$

$$= \left[ \pi_{sid}(E) - \pi_{sid} \left[ \left( \pi_{sid}(E) \times \pi_{cid}(C) \right) - \pi_{sid, cid}(E) \right] \right]$$

Sids of Students who enrolled for at least one course

Sid
S <sub>1</sub>
S <sub>2</sub>
S <sub>3</sub>

Sids of the students who enrolled for all Courses.

Sid
S <sub>1</sub>

o/p will be Sids of the students who did not enroll for all Courses.

Sid
S <sub>2</sub>
S <sub>3</sub>

In the o/p we will get the Sids of students who did not enroll for all Courses along with the Cids of the Courses for which they did not enroll.

Sid	Cid
S <sub>2</sub>	C <sub>1</sub>
S <sub>3</sub>	C <sub>1</sub>
S <sub>3</sub>	C <sub>2</sub>

\* Retrieve Sids of the students who have  
Enrolled for all Courses.

Ans:  $\pi_{sid, cid}(E) \div \pi_{cid}(C)$

$$= \left[ \pi_{sid}(E) - \pi_{sid} \left[ \left( \pi_{sid}(E) \times \pi_{cid}(C) \right) - \pi_{sid, cid}(E) \right] \right]$$

Order of  
Execution  $\Rightarrow$

①

⑧

⑦

②

④

③


⑥

⑤




Note ∴

①  $\pi_{A,B,C}(R) \div \pi_C(S) \Rightarrow$



O/p will contain the value (A,B) from relation R, that are associated with all values of attribute 'C' in relation S.

②  $\pi_{A,B,C}(R) \div \pi_{B,C}(S) \Rightarrow$



O/p will contain values of attribute 'A' from relation R, that are associated with all values of (B,C) in relation S.





## 2 mins Summary



✓ **Topic**

Join operations

✓ **Topic**

Division operation

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**THANK - YOU**