

CS & IT ENGINEERING

Theory of Computation

DFA

Lecture No.- 02



By- Venkat-sir

Recap of Previous Lecture



Topic

Topic

Topic

TOC Introduction

Alphabet

String $\Rightarrow \epsilon$

Language \Rightarrow Empty Language
 \Rightarrow Finite Language
 \Rightarrow Infinite Language

$$DFA = (Q, \Sigma, \delta, Q_0, F) \quad || \quad F.A \Rightarrow DFA$$

Topics to be Covered



Topic

Topic

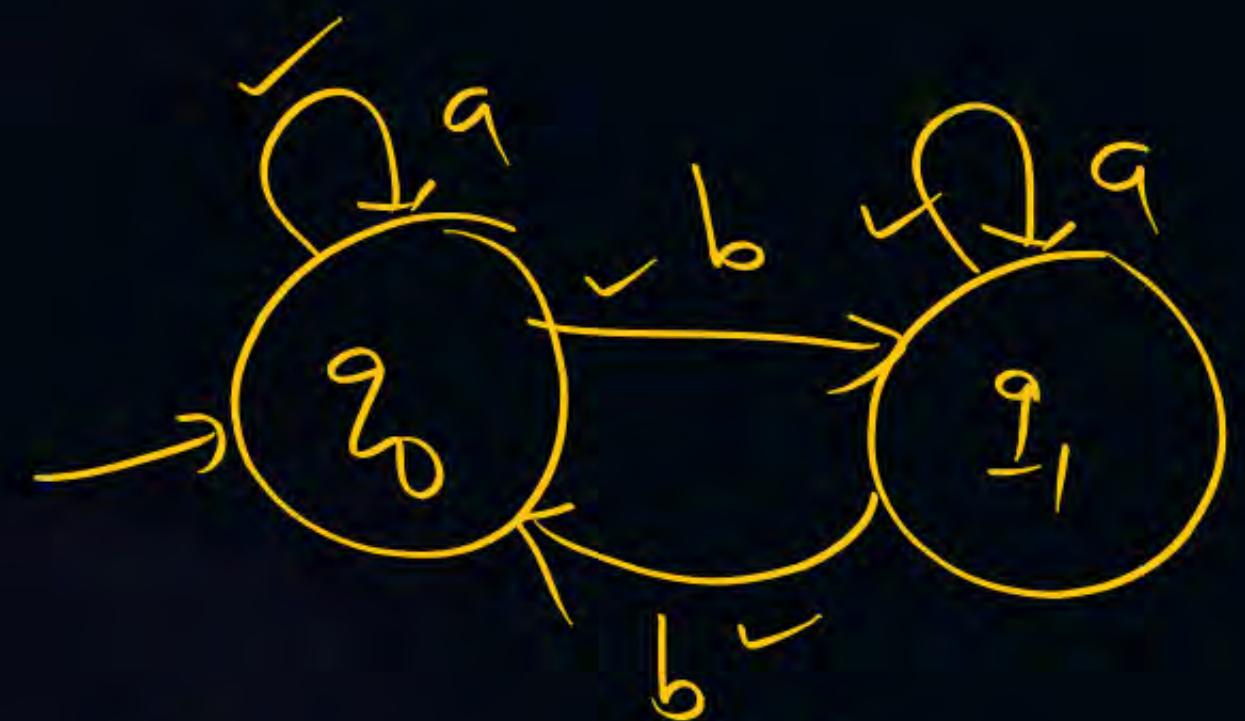
Topic

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DFA Construction





DFA? $(Q, \Sigma, q_0, \overline{F}, \delta)$

✓ ✓ ✓ ✓

F : set of final states

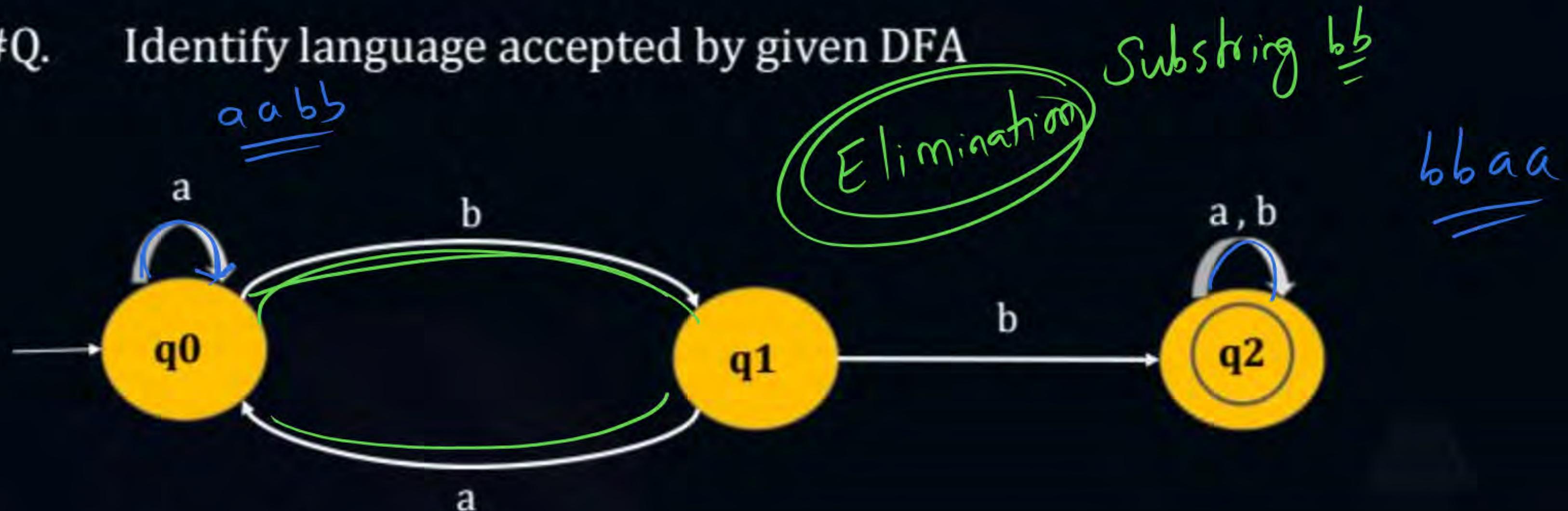
$L_1 = \{a^n b^m \mid n > m\}$ $\xrightarrow{n, m \geq 1}$ ~~Dependency exist~~
~~DFA not possible~~

$L_2 = \{a^n \underbrace{(b^m)}_{a^5 (bb)^m} \mid n, m \geq 1\}$ \Rightarrow ~~DFA possible~~

L_2 : Regular Language?
~~not~~

DFA \Rightarrow Language
= \emptyset

#Q. Identify language accepted by given DFA



- A** Starting with bb X
- B** Ending with bb X
- C** Contains atleast 2 b's X
- D** None ✓

#Q. Identify language accepted by following DFA



A ✓ Starting with 00

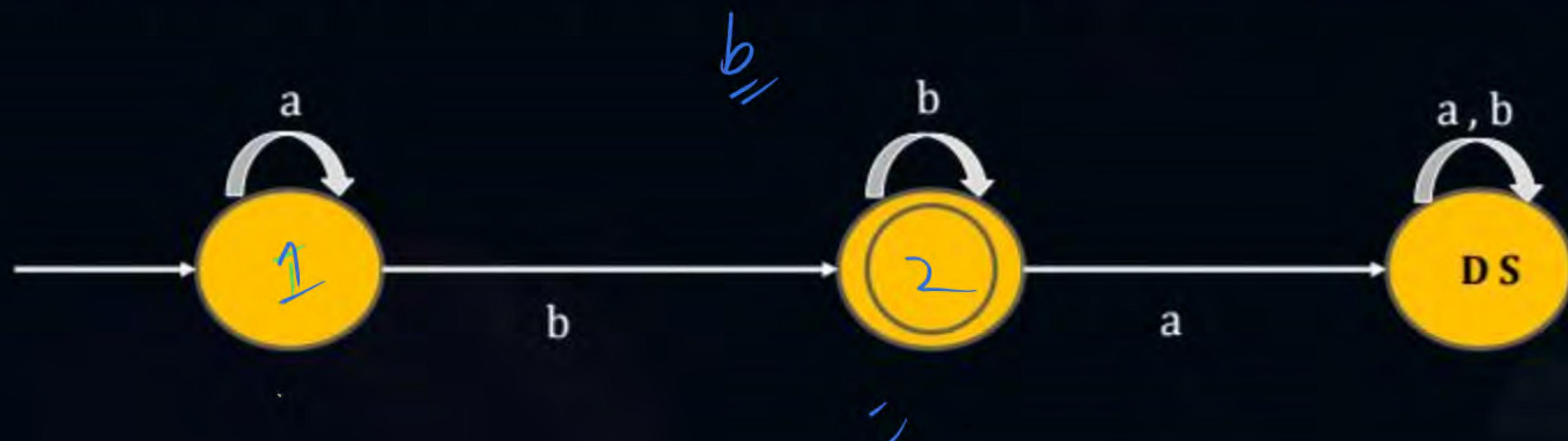
C ✓ Ending with 0 = $\{0, 10, 100, \dots\}$

B ✓ Substring 00

D ✓ None

$$\{00, 100, 00\underline{1}00\underline{1}, \dots\}$$

#Q. Identify language accepted by following DFA



- A** $L = \{a^n b^m \mid n, m \geq 1\}$ ✓
- C** $L = \{a^n b^m \mid n, m \geq 0\}$ ✗

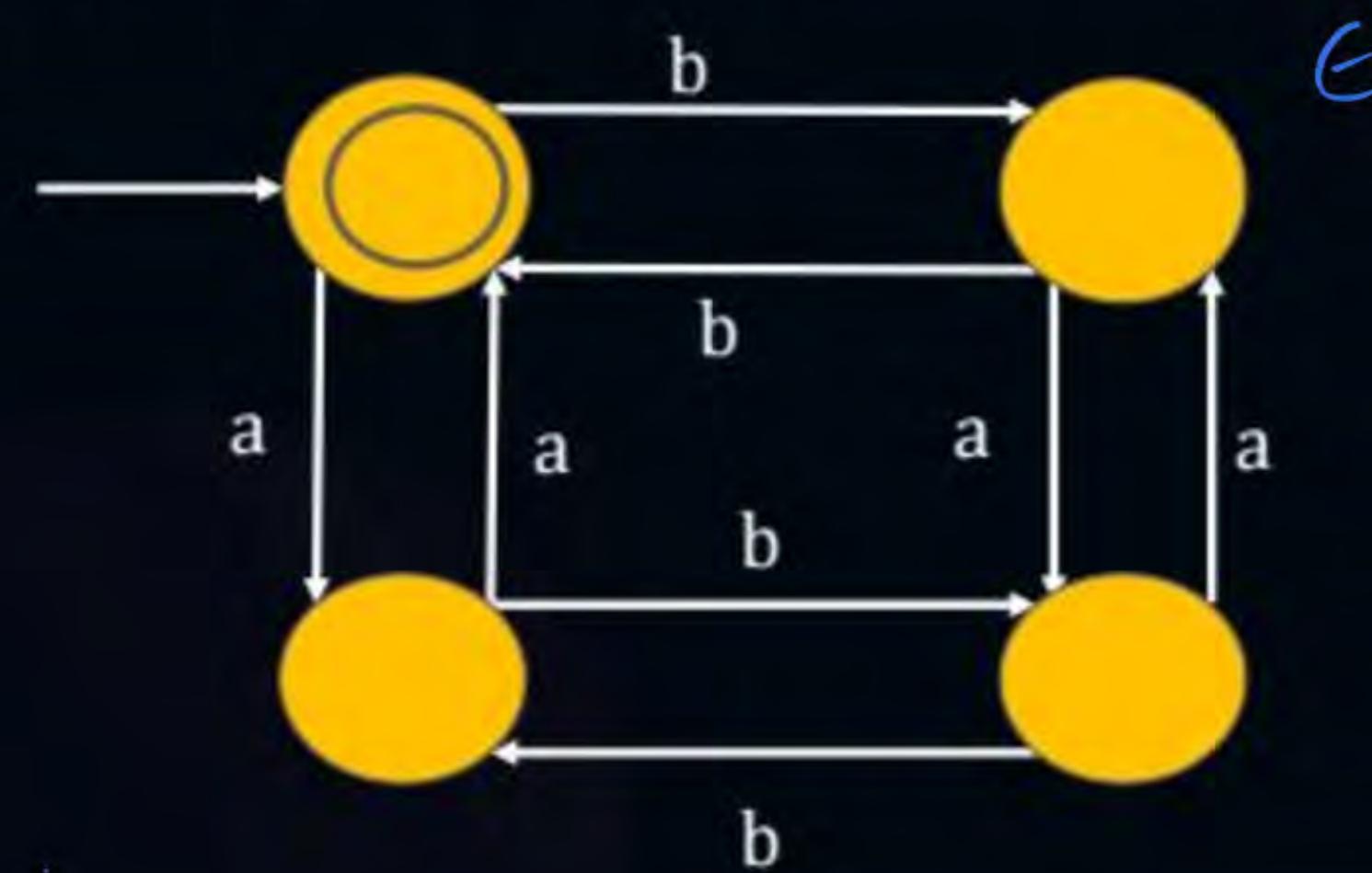
- B** $L = \{a^n b^m \mid n \geq 1, m \geq 0\}$ ✗
- D** None ✓

#Q. Identify language accepted by following DFA



- A** $L = \{a^n b^m \mid n, m \geq 1\}$
- B** $L = \{a^n b^m \mid n \geq 1, m \geq 0\}$
- C** $L = \{a^n b^m \mid n, m \geq 0\}$
- D** None

#Q. Identify language accepted by following DFA

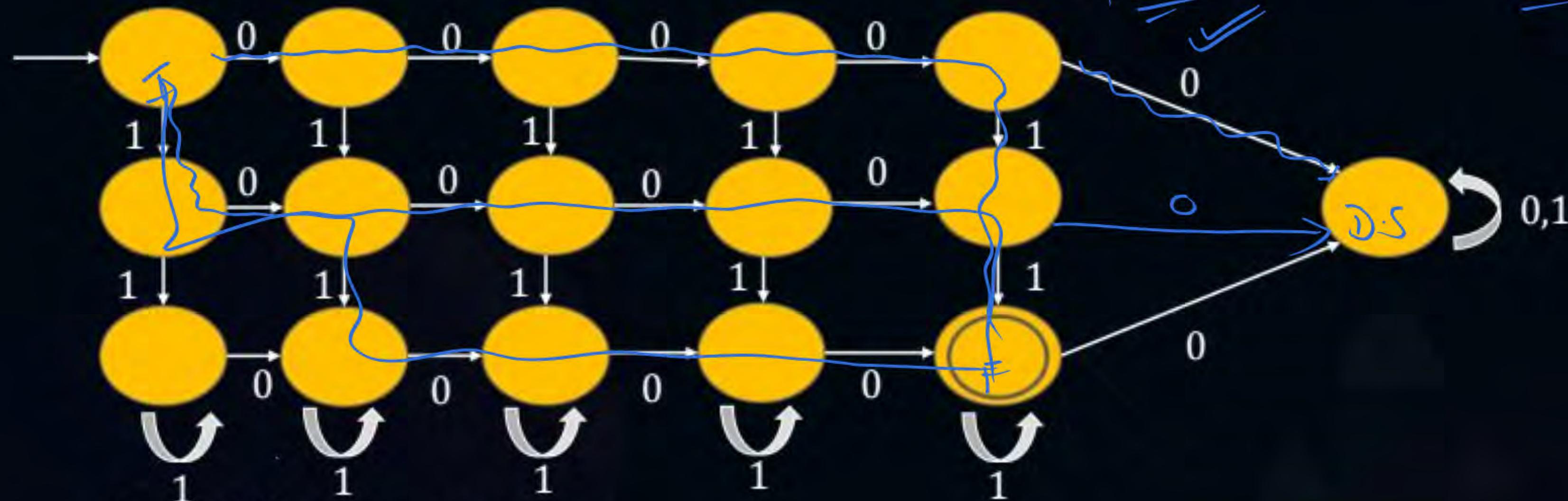


- A ✓ # a's even and # b's even
- C ✗ # a's odd and # b's odd

- B ✗ # a's odd and # b's even
- D ✗ # a's even and # b's odd

#Q. Identify language accepted by following DFA

0's exactly 4 and # 1's atleast 2



A

Length of the string atleast 6



B

0's exactly 4 and 1's atleast 3

D

None

C

0's atleast 4 and # 1's exactly 2





Topic : DFA Construction



Dependency

If (comparison) exist between symbols of language then
DFA is not possible.



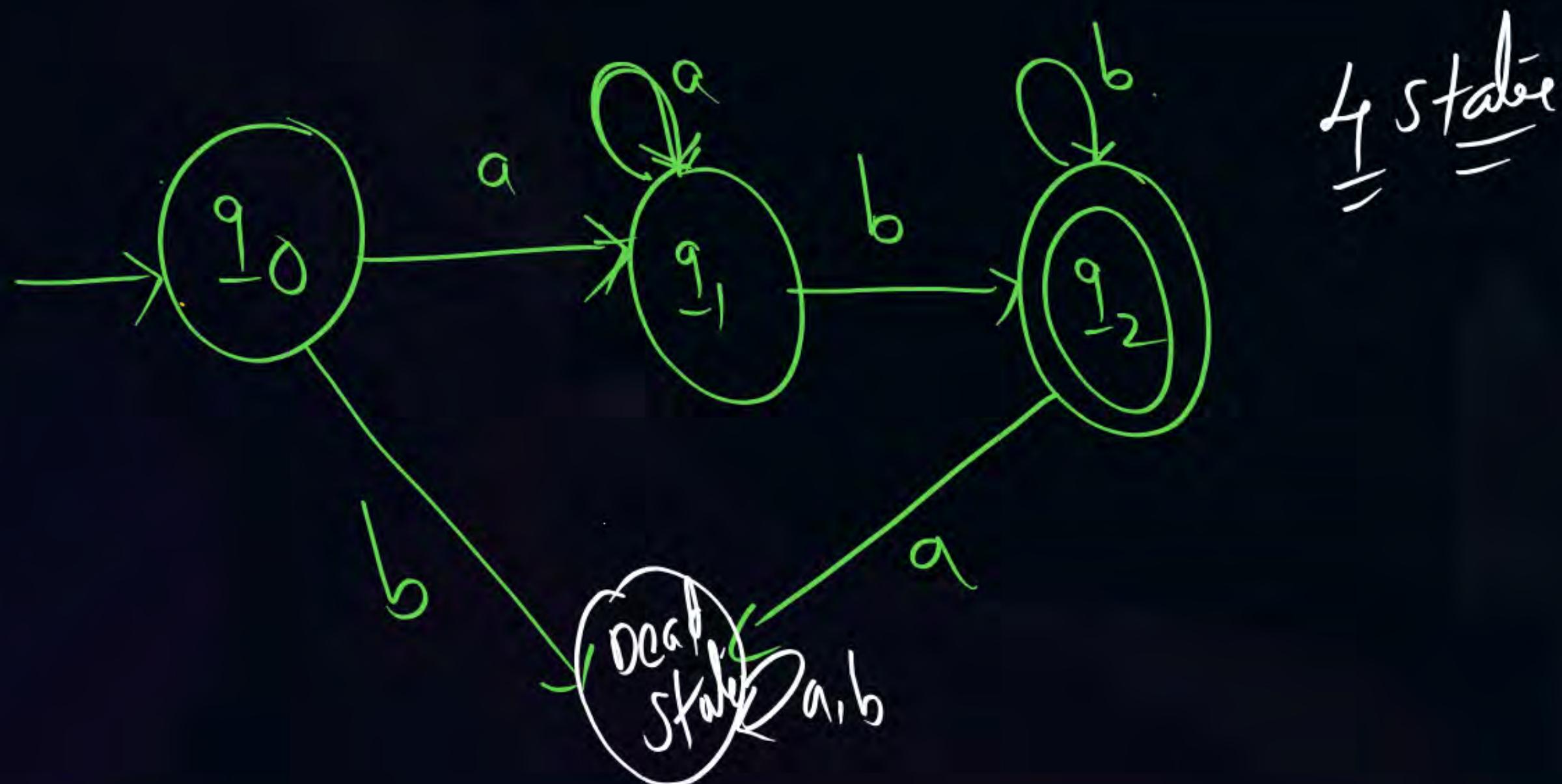
Topic : DFA Construction

$$L = \{ a^n b^m \mid n, m \geq 1 \}$$

Construct DFA for the following Language.

$$(Q, \Sigma, q_0, F, \delta)$$

$$\begin{matrix} a & a & a & b \\ \underline{a} & \underline{a} & \underline{a} & \underline{b} \end{matrix}$$



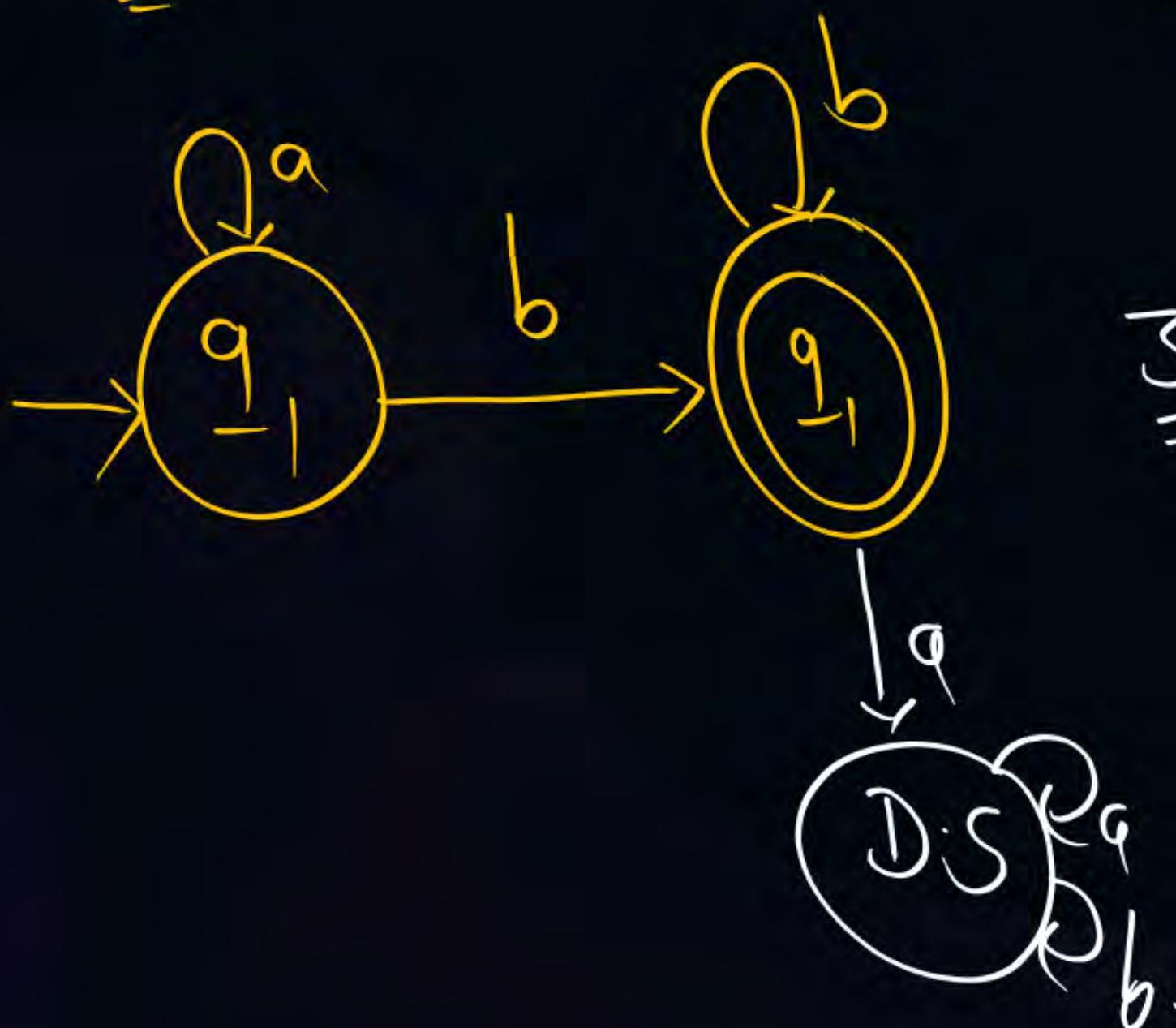


Topic : DFA Construction

$$L = \left\{ \underline{a}^n \underline{b}^m \mid n \geq 0, m \geq 1 \right\}$$

Construct DFA for the following Language.

ab



3 states

b b^2, b^3, \dots
ab, a^2b, ab^2, \dots



Topic : DFA Construction

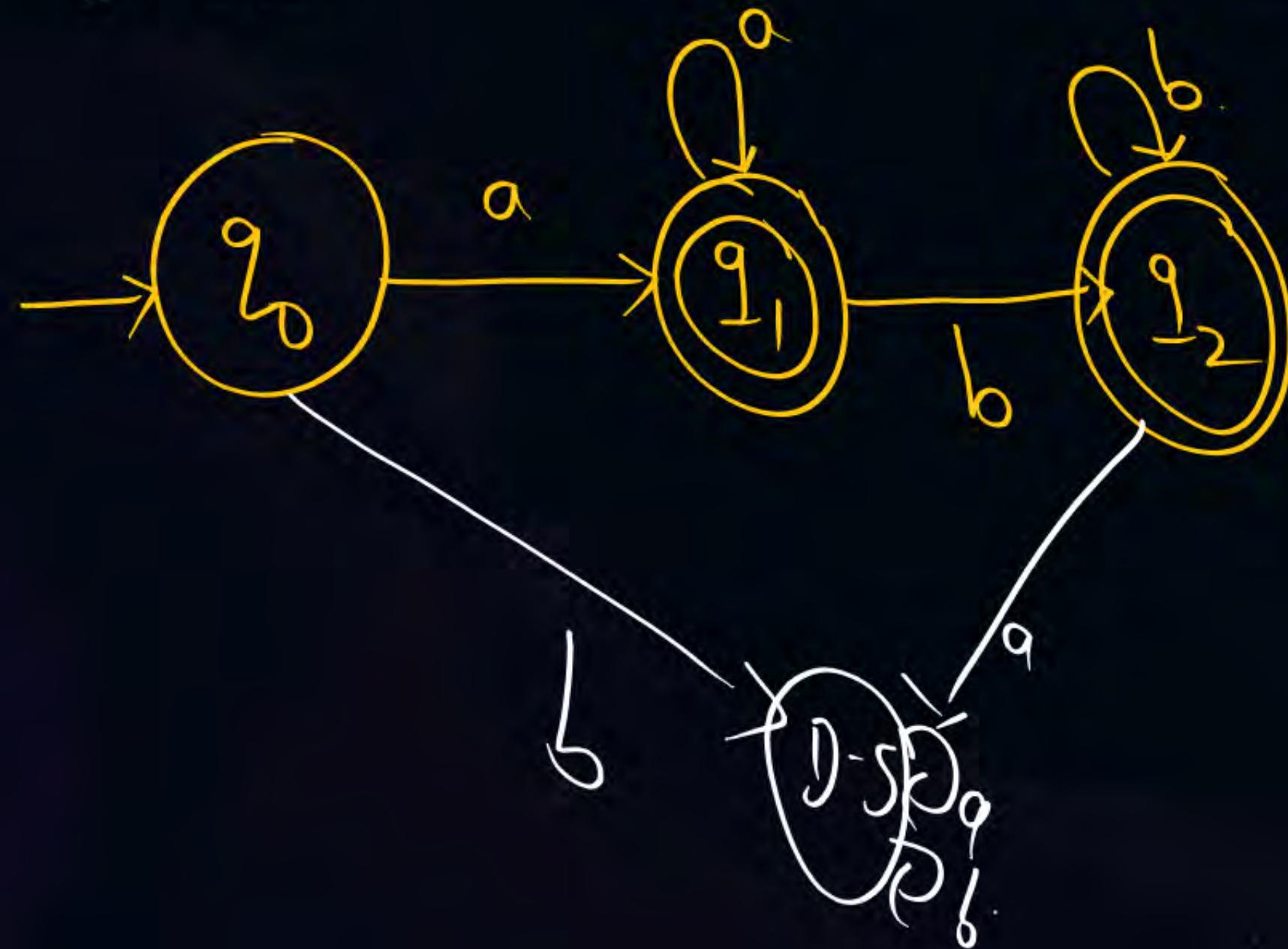
$$L = \{a^n b^m \mid n \geq 1, m \geq 0\}$$

Construct DFA for the following Language.

4 states

$$\begin{array}{c} ab \\ \underline{ab} \\ ab \\ \underline{a} \end{array}$$

$$\left\{ \begin{array}{l} a, a^2, a^3, a^4, \dots \\ ab, a^2b, a^3b, a^4b, \dots \end{array} \right\}$$

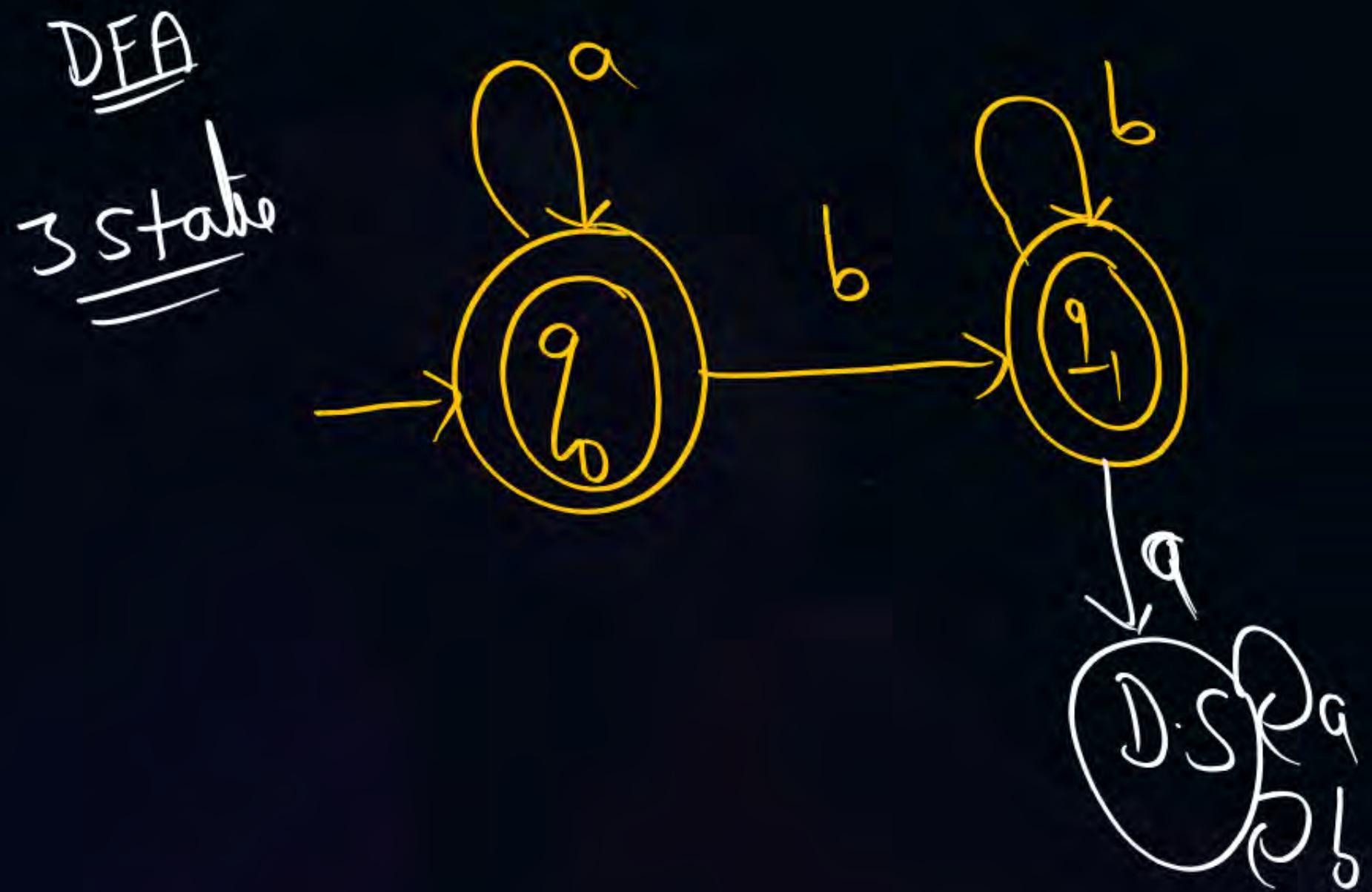




Topic : DFA Construction

$$L = \{a^n b^m \mid n, m \geq 0\}$$

Construct DFA for the following Language.



$$\begin{cases} \epsilon \\ a, a^2, \dots \\ b, b^2, \dots \\ ab, ab^2, \dots \end{cases}$$



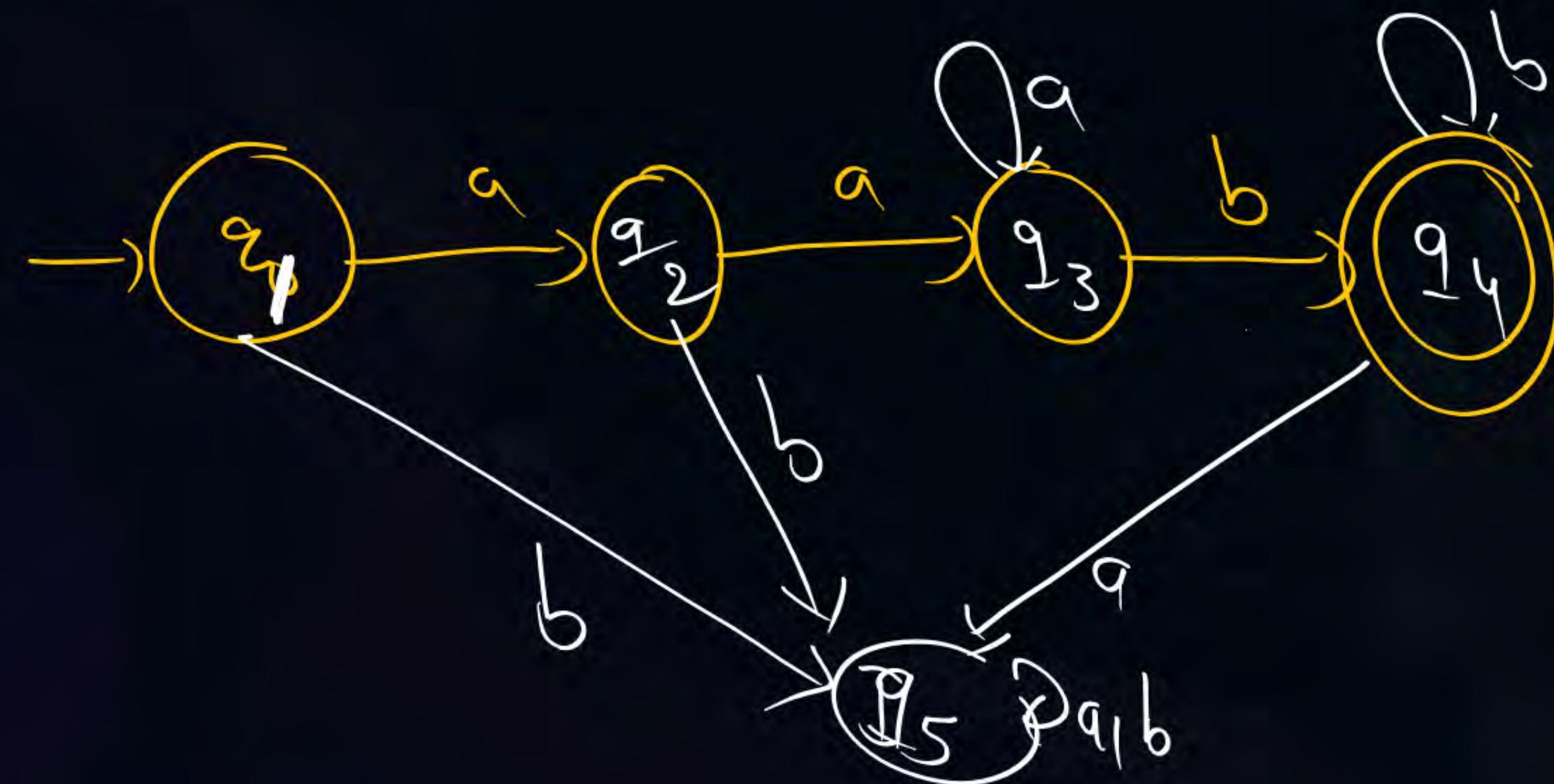
Topic : DFA Construction



Construct DFA for the following Language.

DFA = 5 states

$$L = \{a^n b^m \mid n \geq 2, m \geq 1\} = \{a^2 b, \dots\}$$

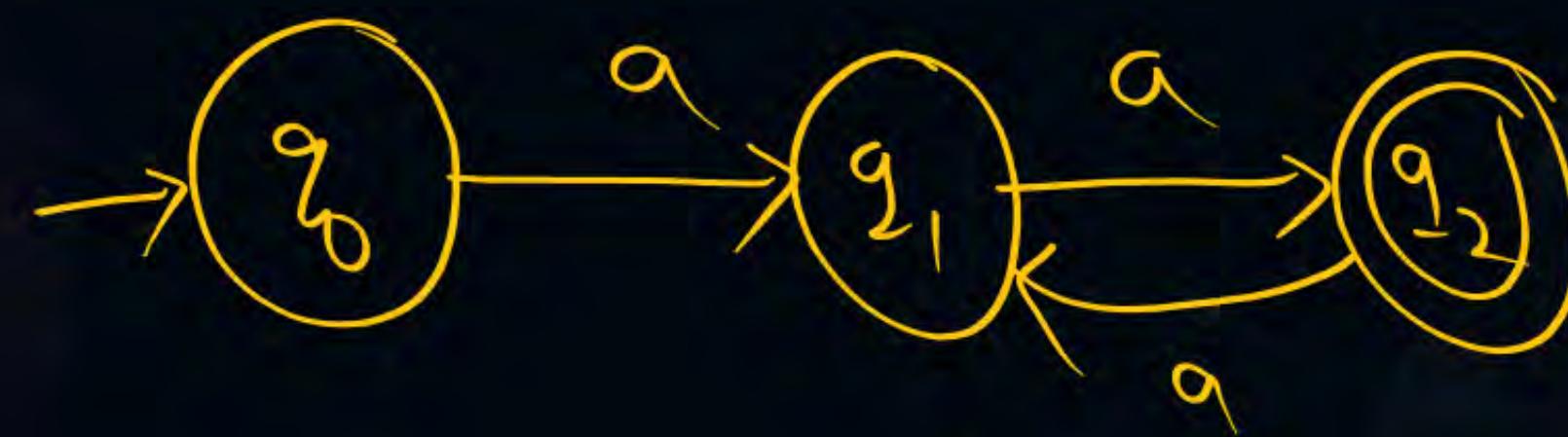




Topic : DFA Construction

Construct DFA for the following Language.

$$L = \left\{ \underbrace{aa}_{2^n} \mid n \geq 1 \right\} = \left\{ a^2, a^4, a^6, \dots \right\}$$



3 states



Topic : DFA Construction

Construct DFA for the following Language.

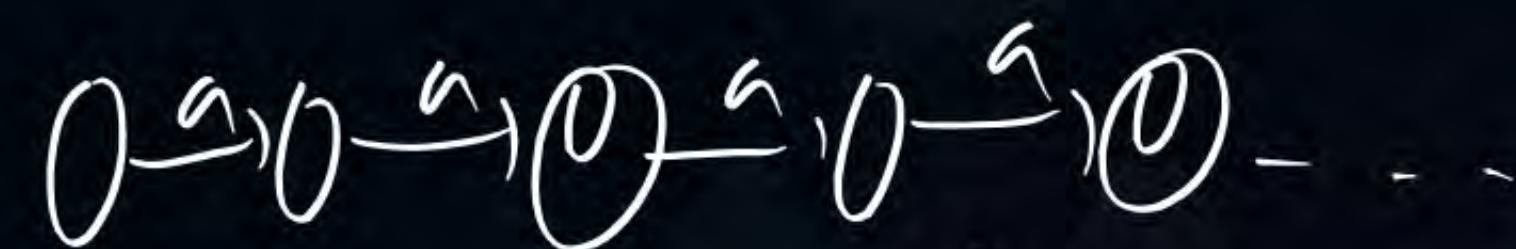
$$L = \left\{ a^{\frac{2^n}{n}} \mid n \geq 1 \right\} = \left\{ a^2, a^4, a^8, a^{16}, \dots \right\}$$

Ⓐ 3

Ⓑ 5

Ⓒ 8

Ⓓ none



DFA not possible

X



Topic : DFA Construction



Construct DFA for the following Language.



NOTE

If a language formed over 1 symbol

then common difference should exist

between string to construct DFA

Otherwise DFA not possible.

Q Which of the following is Regular Language?

a) $L = \{a^{n^n} \mid n \geq 1\} = \{a^1, a^4, a^{27}, \dots\} \times$

b) $L = \{a^p \mid p \text{ is prime number}\} = \{a^2, a^3, a^5, a^7, a^{11}, \dots\}$

Crossed out: $L = \{a^K \mid K \text{ is odd number}\} = \{a^1 \cup a^3 \cup a^5 \cup a^7 \cup \dots\}$

D) none

(Q) Construct DFA over $\Sigma = \{0, 1\}$ where each string is having substring 01

$$L = \{ \underline{01}, 101, 010, 011, 1010, 0\underline{01}1, \dots \}$$

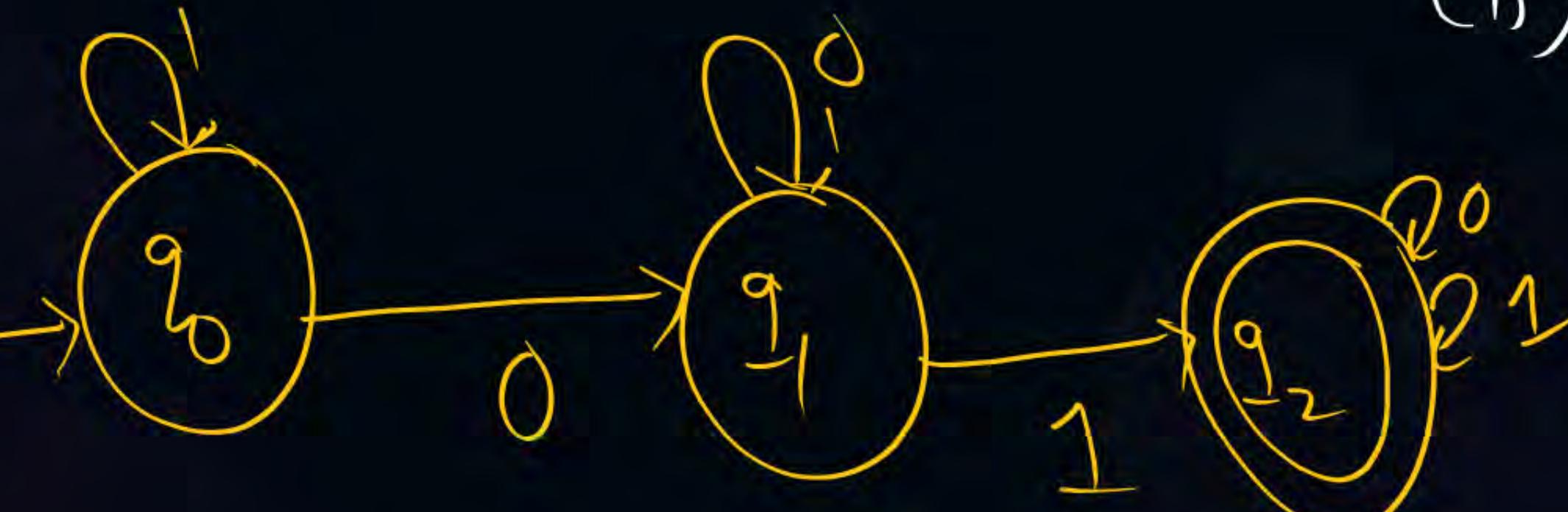
001

 $\begin{pmatrix} 0 \\ 1 \end{pmatrix} \underline{01} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$

11

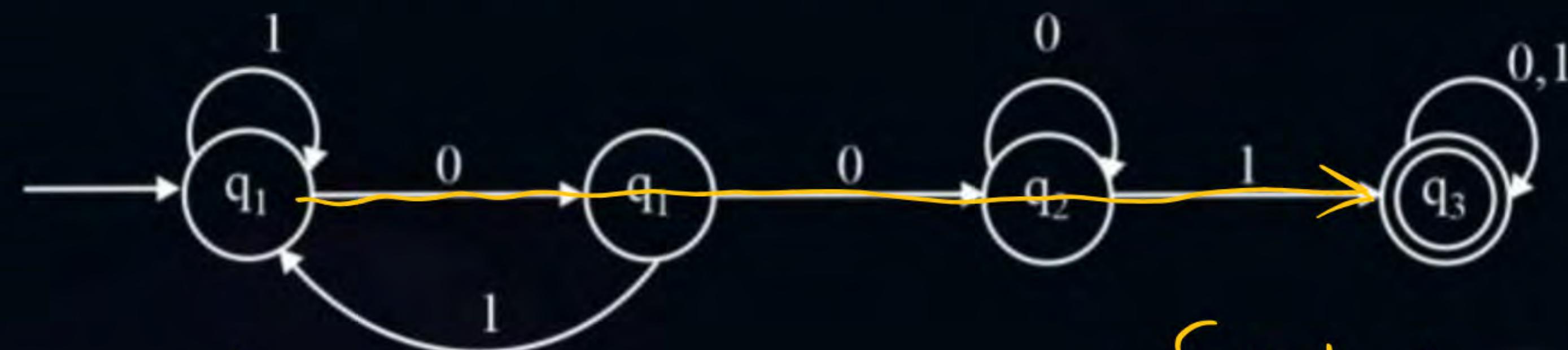
n length substring

11

 $(n+1)$ state

0001

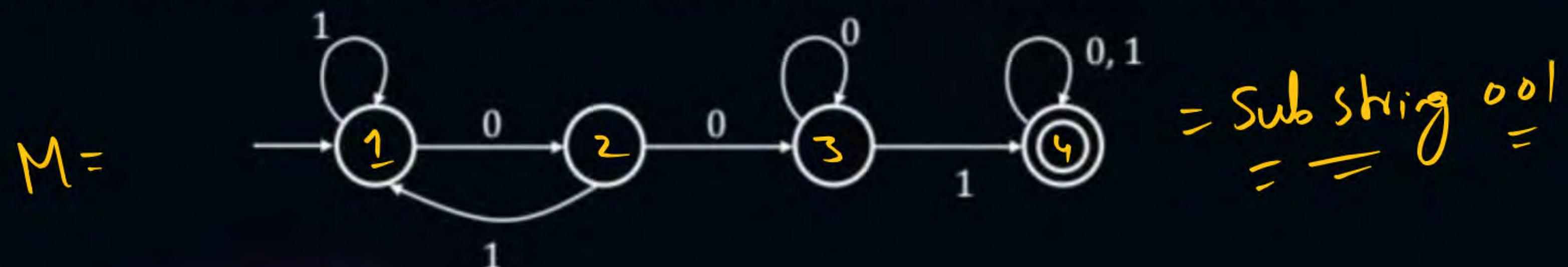
#Q. Consider the following deterministic finite automata m.



{ Sub String 001 }

The language accepted by finite automata?

#Q. Consider the following deterministic finite state automaton M.



Let S denote the set of seven-bit binary strings in which the first, the fourth, and the last bits are 1. The number of strings in S that are accepted by M is

$$S: \frac{1}{11} \frac{00}{00} \frac{1}{10} \frac{00}{00} \frac{1}{11} \} 16$$

A 1
C 7

B 5
D 8

| 0 0 | 0 0 | } 5

| 0 0 | 0 | |

| 0 0 | 1 0 |

| 0 0 | 1 1 | }

| 0 | 0 0 | }

| 0 | 0 | |

| 0 | 1 0 |

| 0 | 1 1 | }

| 1 0 | 0 0 | } 6

| 1 0 | 0 | |

| 1 0 | 1 0 |

| 1 0 | " | "

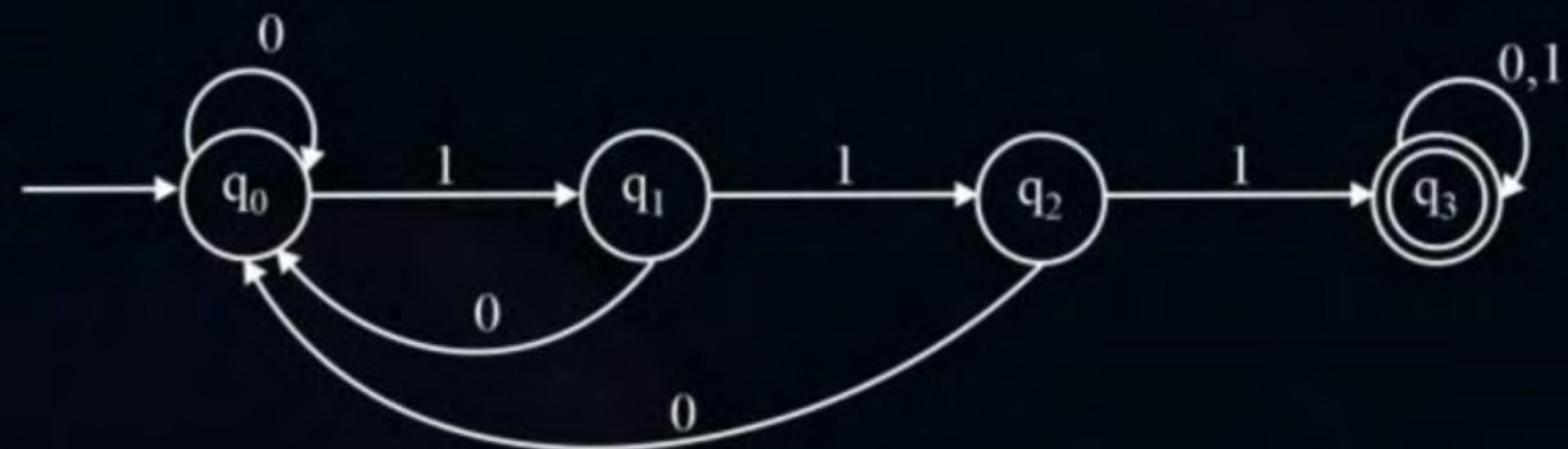
| 1 1 | 0 0 | } 7

| 1 1 | 0 | |

| 1 1 | 1 0 |

| 1 1 | 1 1 | }

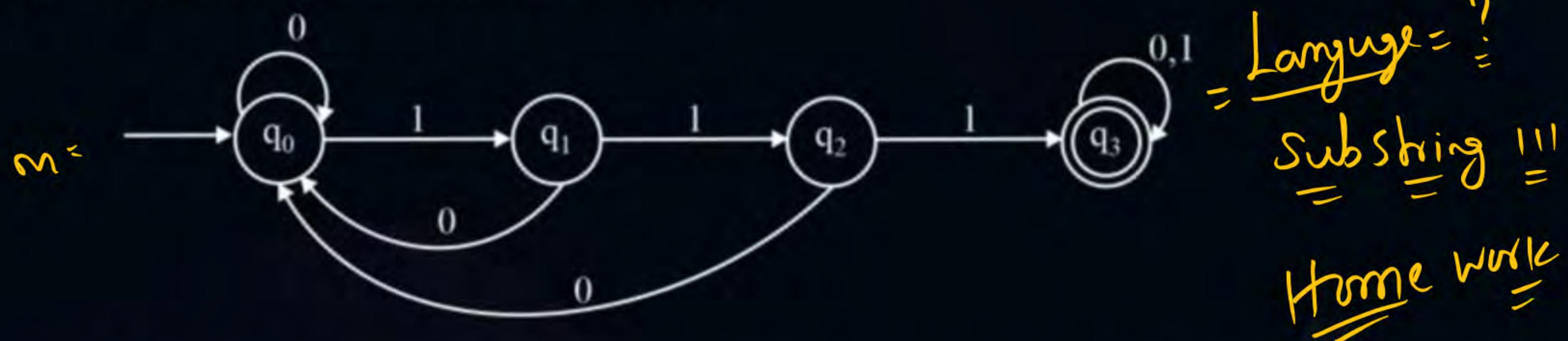
#Q. Consider the finite automata m.



The language accepted by m is, over the alphabet $\{0,1\}$

- A** The set of all strings containing three consecutive I's
- B** The set of all strings not containing three consecutive I's
- C** The set of all strings beginnigs with three consecutive I's
- D** The set of all strings ending with three consecutive I's

#Q. Consider the finite automata m.



Let S denotes the set of all six bit binary strings in which first and fourth bits are 1. The number of strings in S that are accepted by m is-

- S: $\underline{1} \underline{1} \underline{0} \underline{1} \underline{1} \underline{1}$
- $4+1+2+1$
- A** 1 **B** 4
C 7 ✓ **D** 8



THANK - YOU