

# CS & IT ENGINEERING



## THEORY OF COMPUTATION

### REGULAR EXPRESSION



Lecture No.- 03



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# Recap of Previous Lecture



Topic

?????

Regular Expression Construction





# Topics to be Covered



Topic

Properties of Regular Expression

Topic

??

Topic

??

Finite Automata Regular Expression

Topic

??





## Topic : Properties of regular expression

① Associative Property  $\Rightarrow (r_1 + r_2) + r_3 = r_1 + (r_2 + r_3)$

② Commutative Property  $\Rightarrow (r_1 + r_2 = r_2 + r_1) \quad [r_1 \cdot r_2 \neq r_2 \cdot r_1]$

③ Distributive Property  $\Rightarrow r_1 \cdot (r_2 + r_3) = r_1 \cdot r_2 + r_1 \cdot r_3$

$$\underline{a}^* + \underline{a}^* = \underline{a}^*$$

$$a^* = (a^*)^* \Rightarrow a^*$$

$$(a^*)^+ \Rightarrow a^*$$

$$(a^+)^* = a^*$$



$$a \cdot a^* = a^+ = \underline{a^*} \cdot a$$

$$\underline{a} \cdot \{ \underline{1}, a, a^2, a^3, a^4, \dots \}$$

$$\{ a, a^2, a^3, \dots \}$$

$$2 \times 0 = 0$$

$$R = \text{Reg Expr}$$

$$0 \times 0 + 0 \times 0 = 0$$

$$(1) \quad R + \phi = \phi + R = R$$

$$(2) \quad R \cdot \phi = \phi \cdot R = \phi$$

$$(3) \quad R + \epsilon = \epsilon + R \neq R$$

$$(4) \quad R \cdot \epsilon = \epsilon \cdot R = R$$

$$(5) \quad (R^*)^* = (R^*)^+ = (R^+)^* = R^*$$

$$(6) \quad R \cdot R^* = R^+ = R^* R$$

$$(7) \quad \epsilon^* = \epsilon$$

$$(8) \quad \epsilon^+ = \epsilon$$

$$1 \times 1 = 1$$

$$(9) \quad \phi^* = \epsilon$$

$$(10) \quad \phi^+ = \phi$$

$$(11) \quad (a + b)^* \neq a^* b^*$$

$$(12) \quad (a + b)^* \neq (a \ b)^*$$

$$(13) \quad (a + b)^* \neq (a^*)^+ (b^*)^+$$

$$\phi^* = \epsilon$$

$$\phi^+ = \phi$$

$$(a + b)^* \neq a^* b^*$$

$$(a + b)^* \neq (a \ b)^*$$

$$(a + b)^* \neq (a^*)^+ (b^*)^+$$

$$\{\epsilon, \epsilon + \epsilon + \epsilon + \dots\}$$

$$\{ab, abab, \dots\}$$

$$ab$$

$$ab$$



\*\*\*

$$(14) \quad (a + b)^* = (a + b^*)^*$$

$$\begin{aligned} & \rightarrow (a^* + b)^* \\ & \rightarrow (a^* + b^*)^* \\ & \rightarrow (a^* b^*)^* \end{aligned}$$

$$(15) \quad (a^*) + (a^*) = a^* = a^* a^*$$

$\{a, b\}$

$\{b, a\}$

$$(16) \quad a + b = b + a \quad (\text{Commutative})$$

$$(17) \quad a \cdot b \neq ba$$

$$(a + b)^* = (a + b)^0 + (a + b)^1 + (a + b)^2 + (a + b)^3 + \dots$$

$$= \{ \epsilon, a, b, aa, ab, ba, bb, \dots \}$$

$$(r_1 + r_2)^* = (r_1^* \cdot r_2^*)^*$$



#Q. Identify language accepted by following regular expression

$$b^*(a^* \cdot \phi \cdot b + ab + a\phi^*b^*)(b + \phi)^*$$

$$b^*(\phi + ab + a\phi^*b^*)b^*$$

**A** Exactly one a

$$b^*(ab + ab^*)b^*$$

**B** At least one a

$$b^*(a(b + b^*))b^*$$

**C** At most one a

$$b^*(a \cdot b^*) \cdot b^*$$

**D** None

$$b^*ab^*$$

$$\left. \begin{aligned} b^* + b^* &= b^* \\ b^* \cdot b^* &= b^* \\ b^* + b &= b^* \end{aligned} \right\}$$



# [MCQ]

#Q. Which of the following regular expressions are equivalent?

- I.  $(00)^*(\epsilon+0)$   $\rightarrow$  all  
 II.  $(00)^*$   $\rightarrow$  even  
 III.  $0^*$   $\rightarrow$  all  
 IV.  $0(00)^*$   $\rightarrow$  odd

**A** (I) And (II)

**B** (ii) and (iii)

**C** (i) And (iii)

**D** (iii) and (iv)



# [MCQ]

$(a+b)^*$

#Q. Which of the following pair of regular expressions are not equal

**A**

$(r^*)^*$  and  $(r^+)^*$

**B**

$(r + \epsilon)^*$  and  $r^*$

$(\gamma + \epsilon)^* = \{\epsilon, \gamma, \gamma^2, \gamma^3, \dots\}$

**C**

$(rr + \epsilon)^*$  and  $r^*$

**D**

None of the above



(Q)  $\boxed{(a^*b^*)^* a^* b^*}$  is equivalent to  
 $(a+b)^* \underline{a^* b^*} = (a+b)^* + (a+b)^* a^2 b^2 + (a+b)^* a^3 b + (a+b)^*$

(a)  $(a+b)^*$

(b)  $a^* b^*$

(c)  $(a+b)^* ab$

(d) none



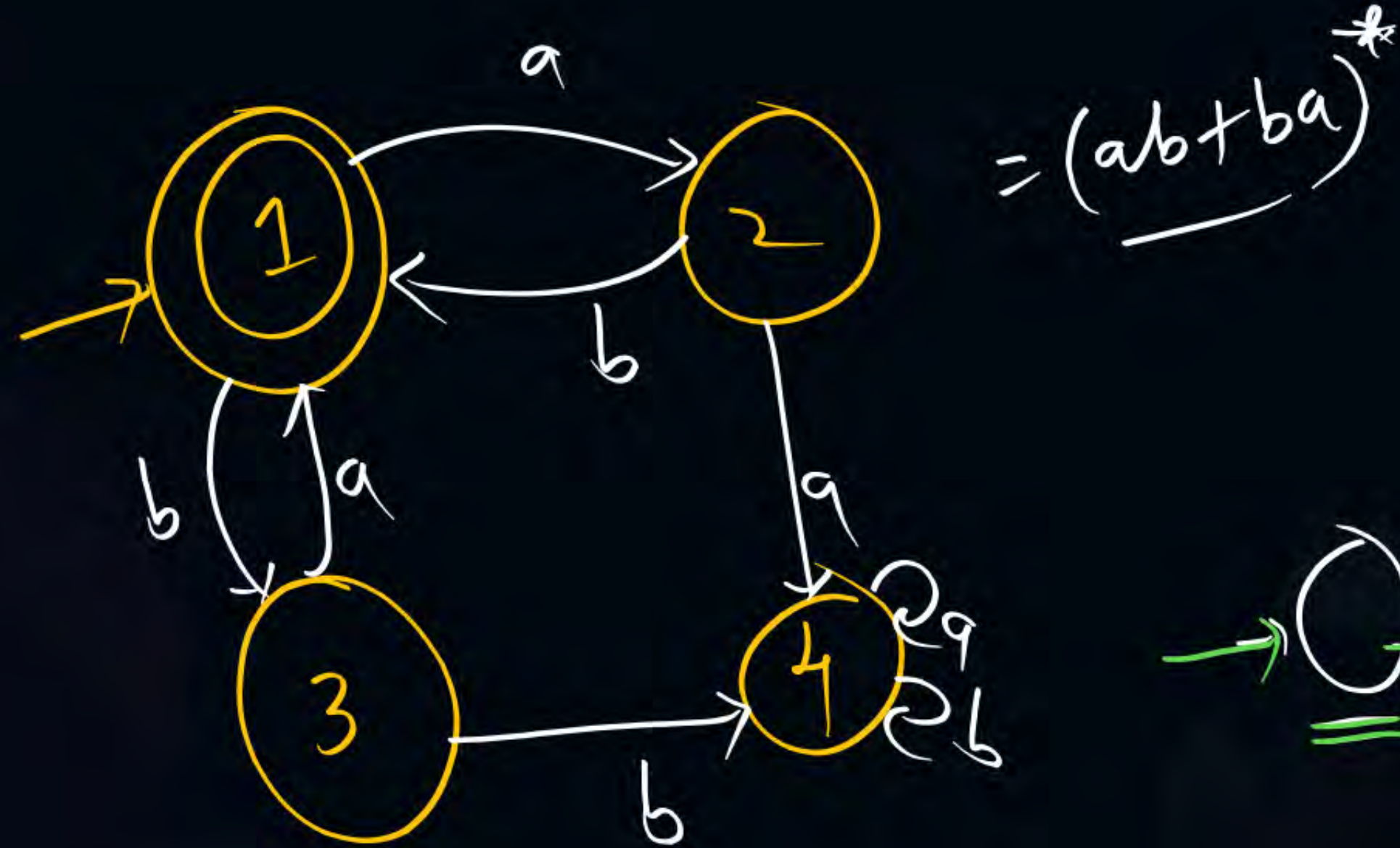
$\{ F.A \Rightarrow \text{Regular Expression} \}$

# FINITE AUTOMATA TO REGULAR EXPRESSION

① State elimination method

x ② Ardens method

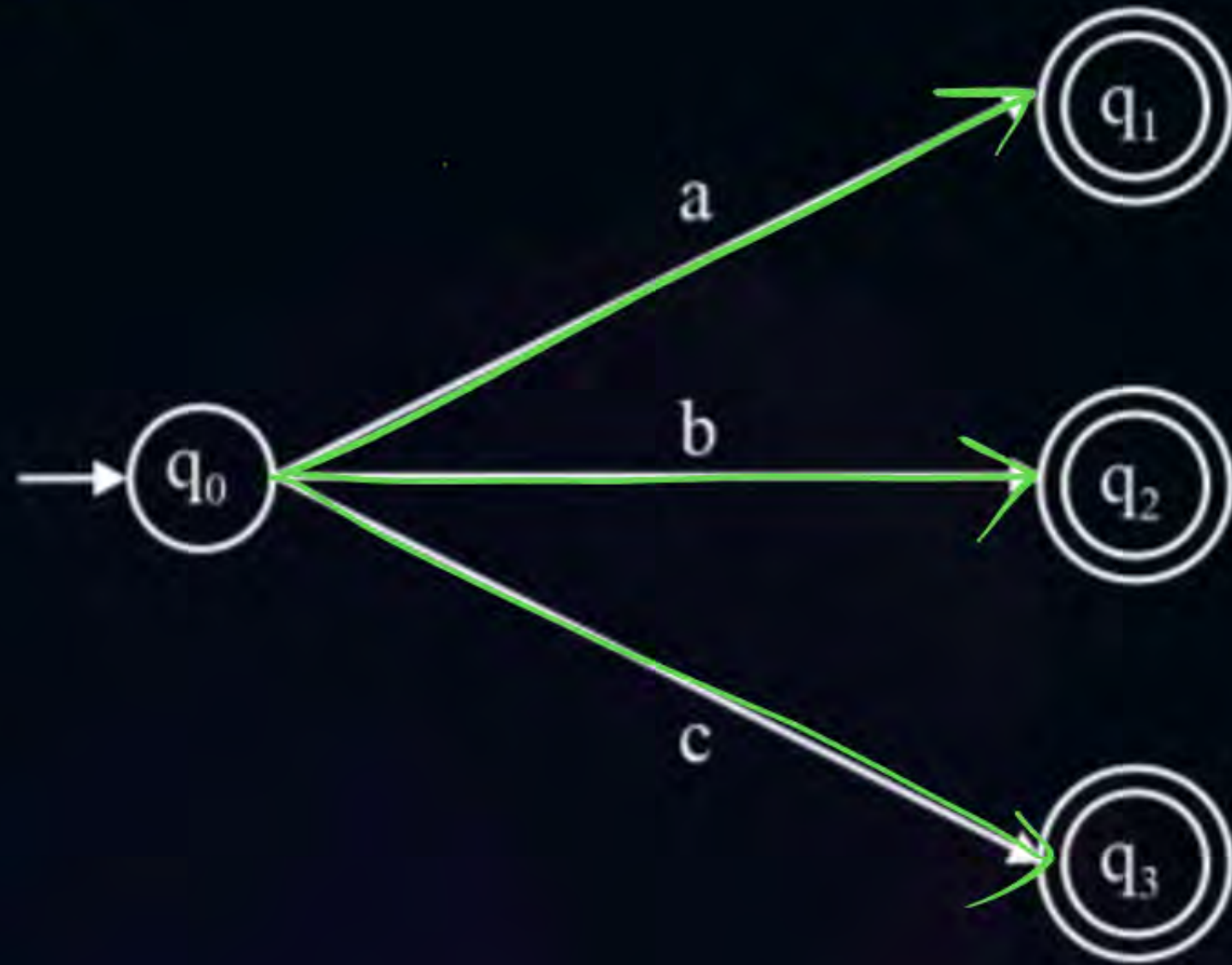






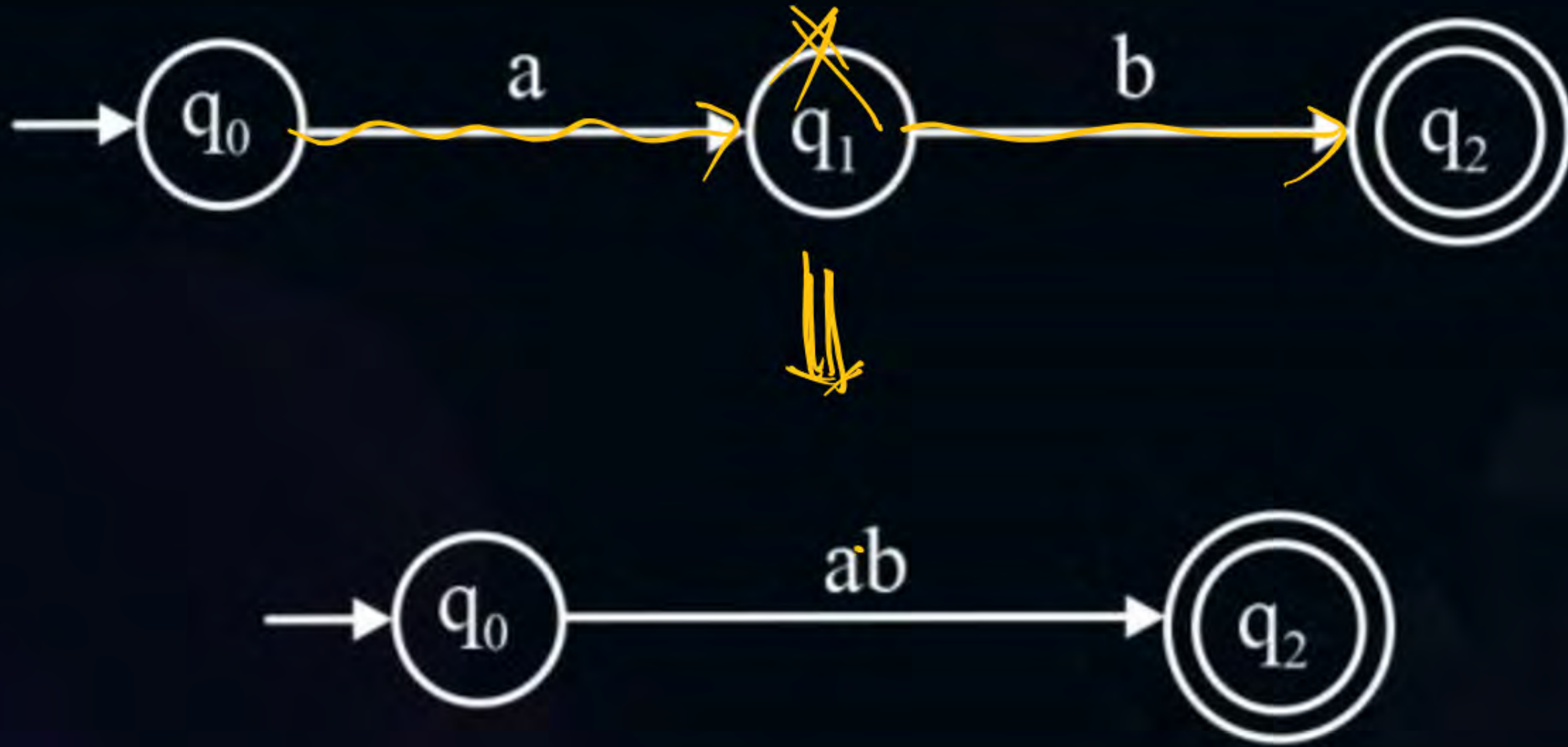
1.

multiple final states  $\Rightarrow$  one final state



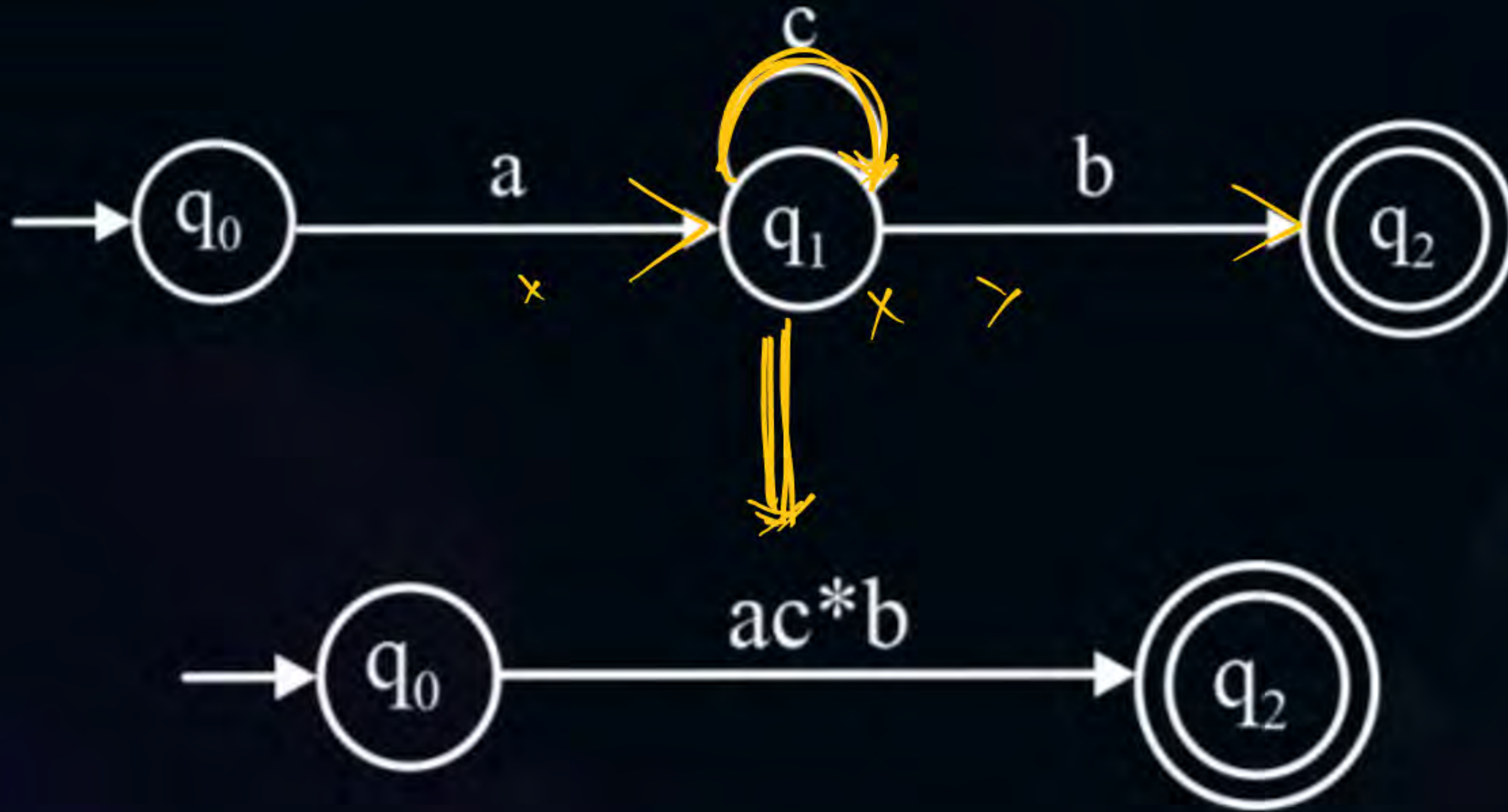


3.





4.



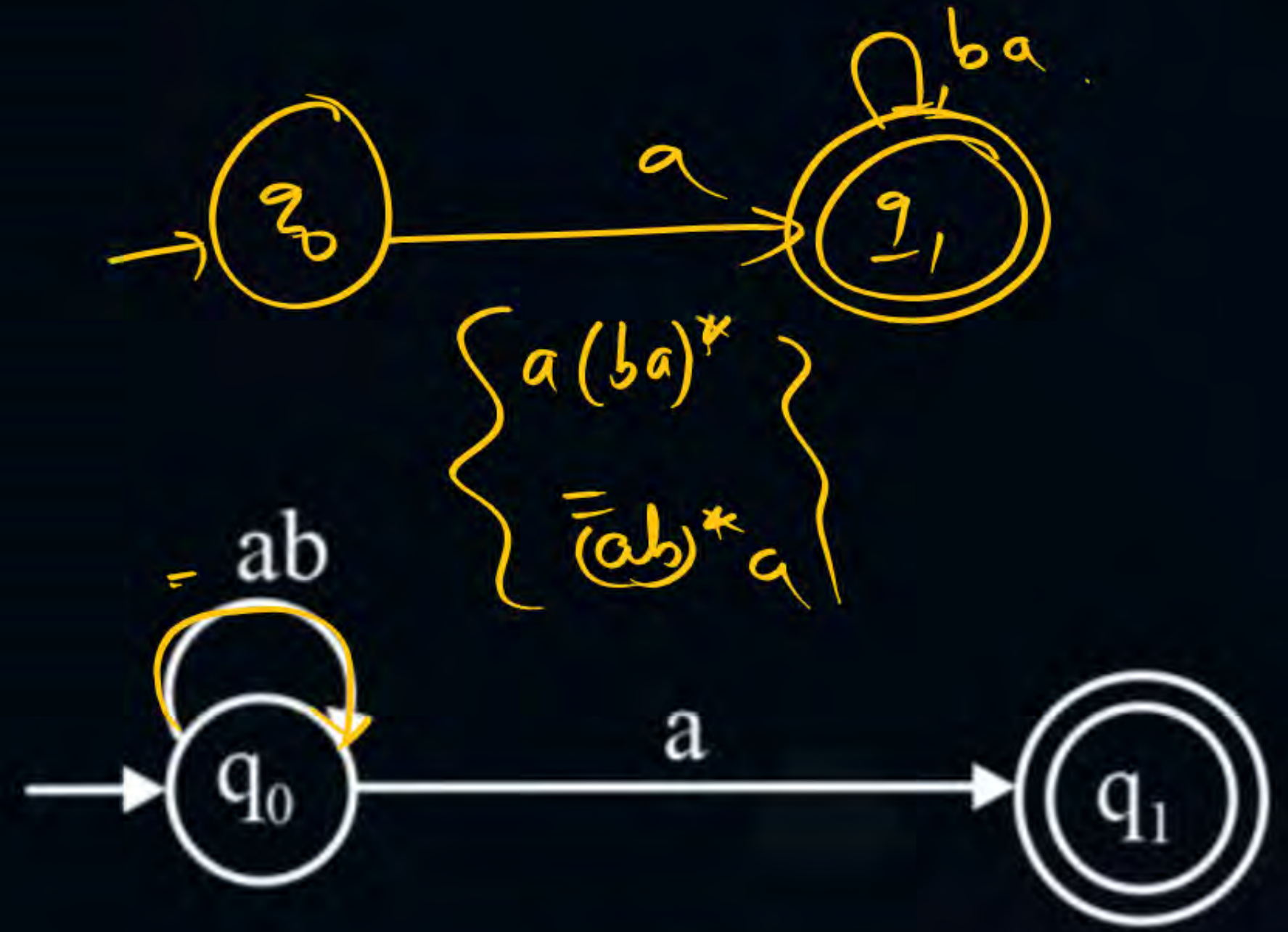
$Q^{\gamma_1}$   
 $Q^{\gamma_2}$   
 $= (\gamma_1 + \gamma_2)^*$

$Q^a$   
 $\rightarrow Q^b$

$= (a+b)^*$



5.)

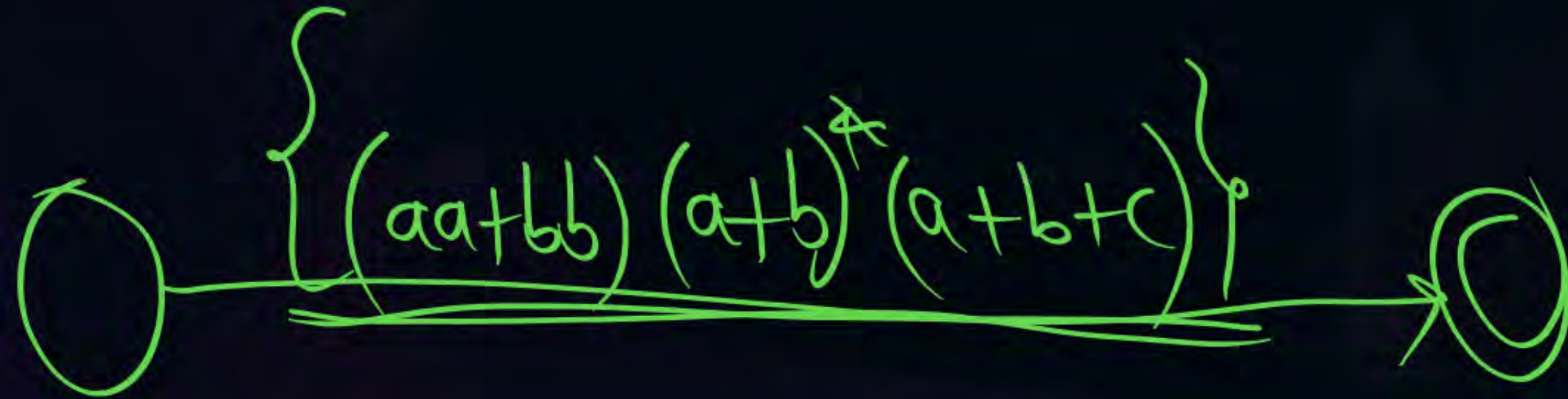
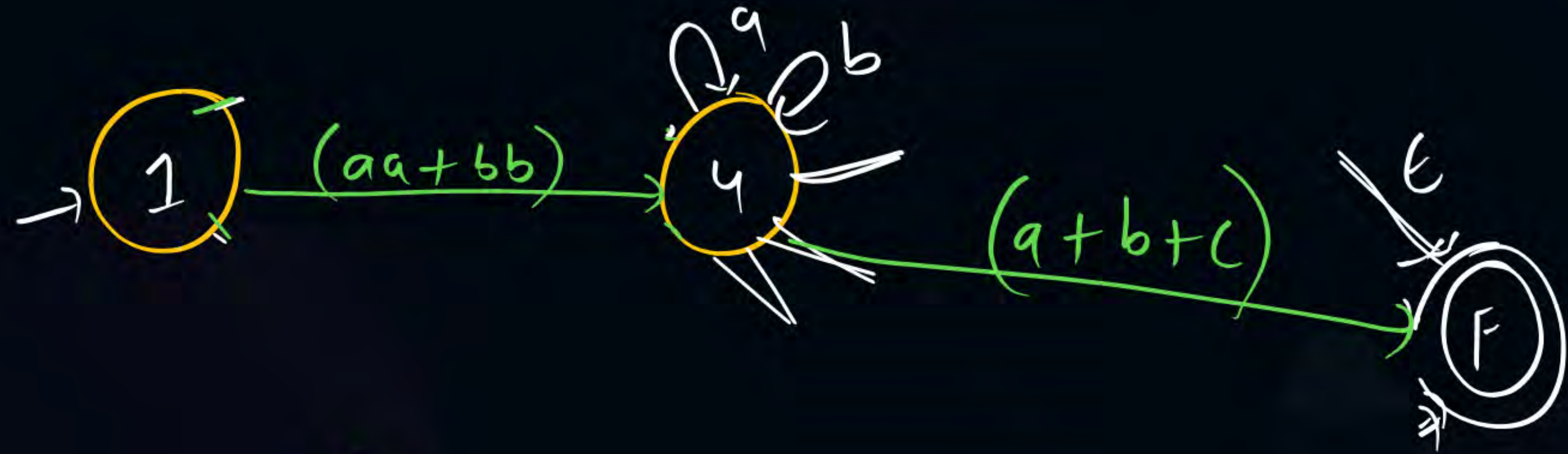


$\left\{ \begin{array}{l} a(ba)^* \\ (ab)^*a \end{array} \right\}$

$\Downarrow$   
 $(ab)^*a$   
 $\underline{\underline{=}}$



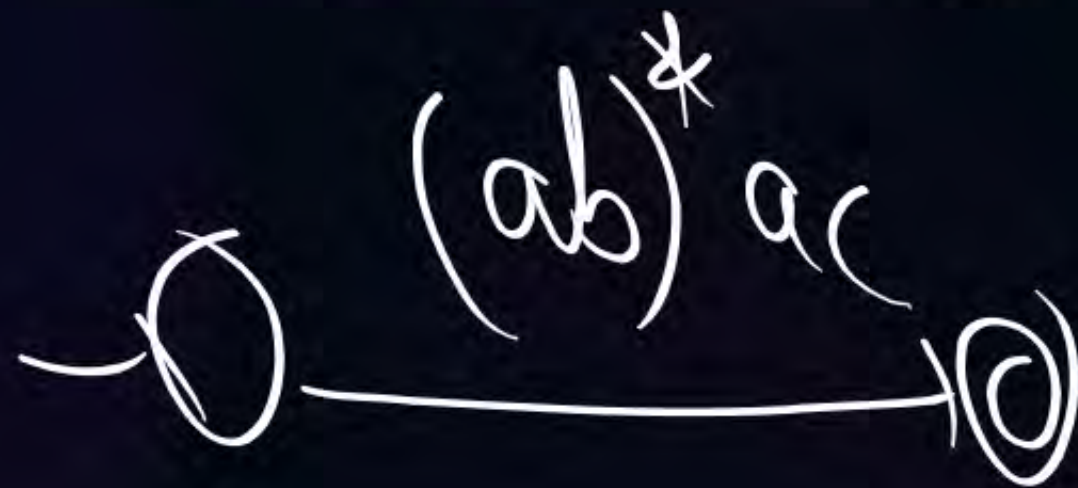
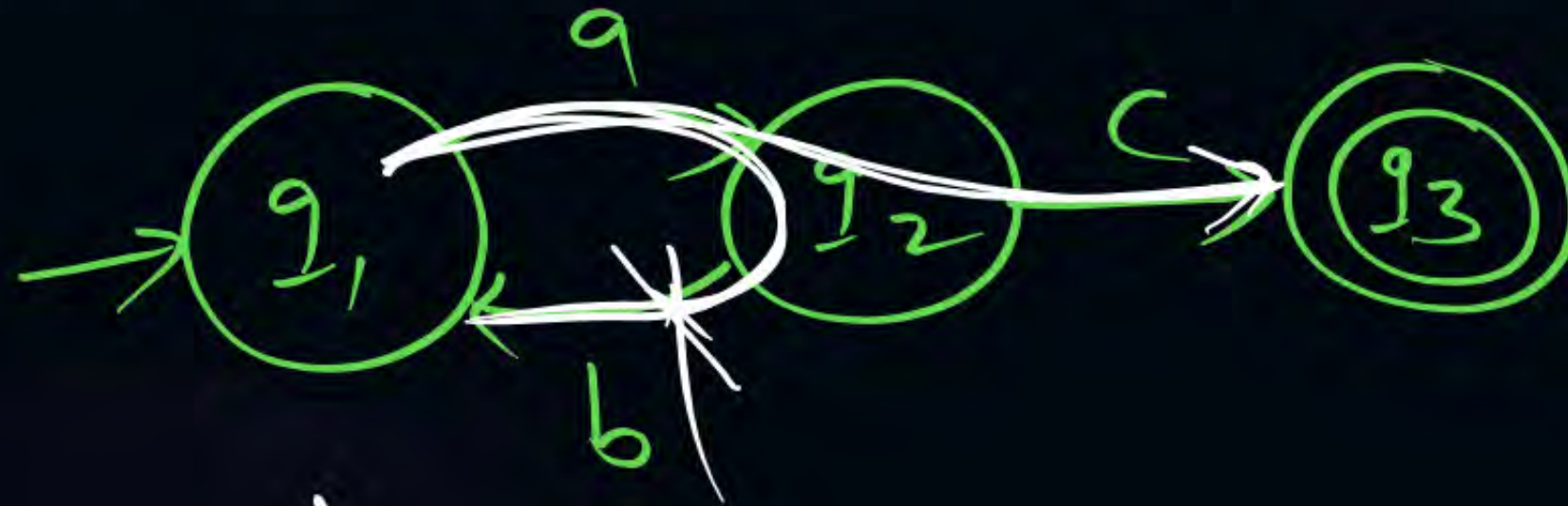
#Q. Construct Regular Expression for the following Finite Automata.





#Q. Construct Regular Expression for the following Finite Automata.

②

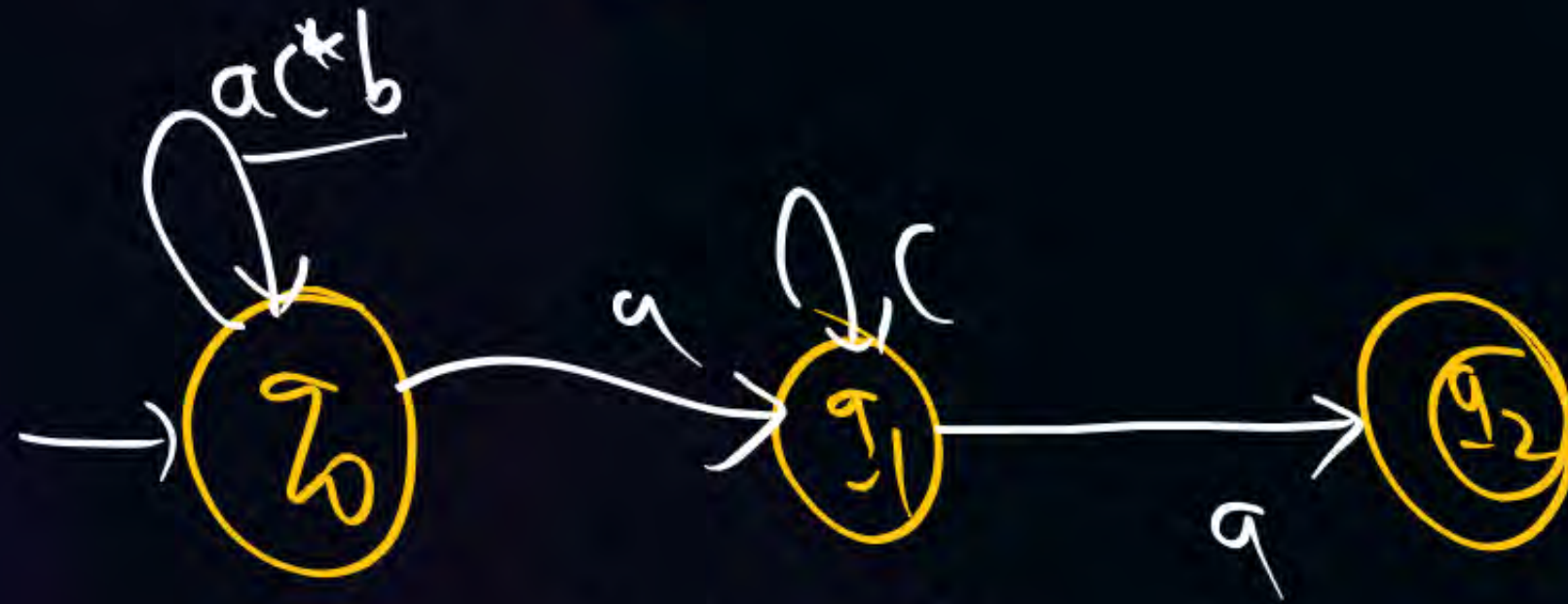




$(ab)^*$   $a \rightarrow b$

#Q. Construct Regular Expression for the following Finite Automata.

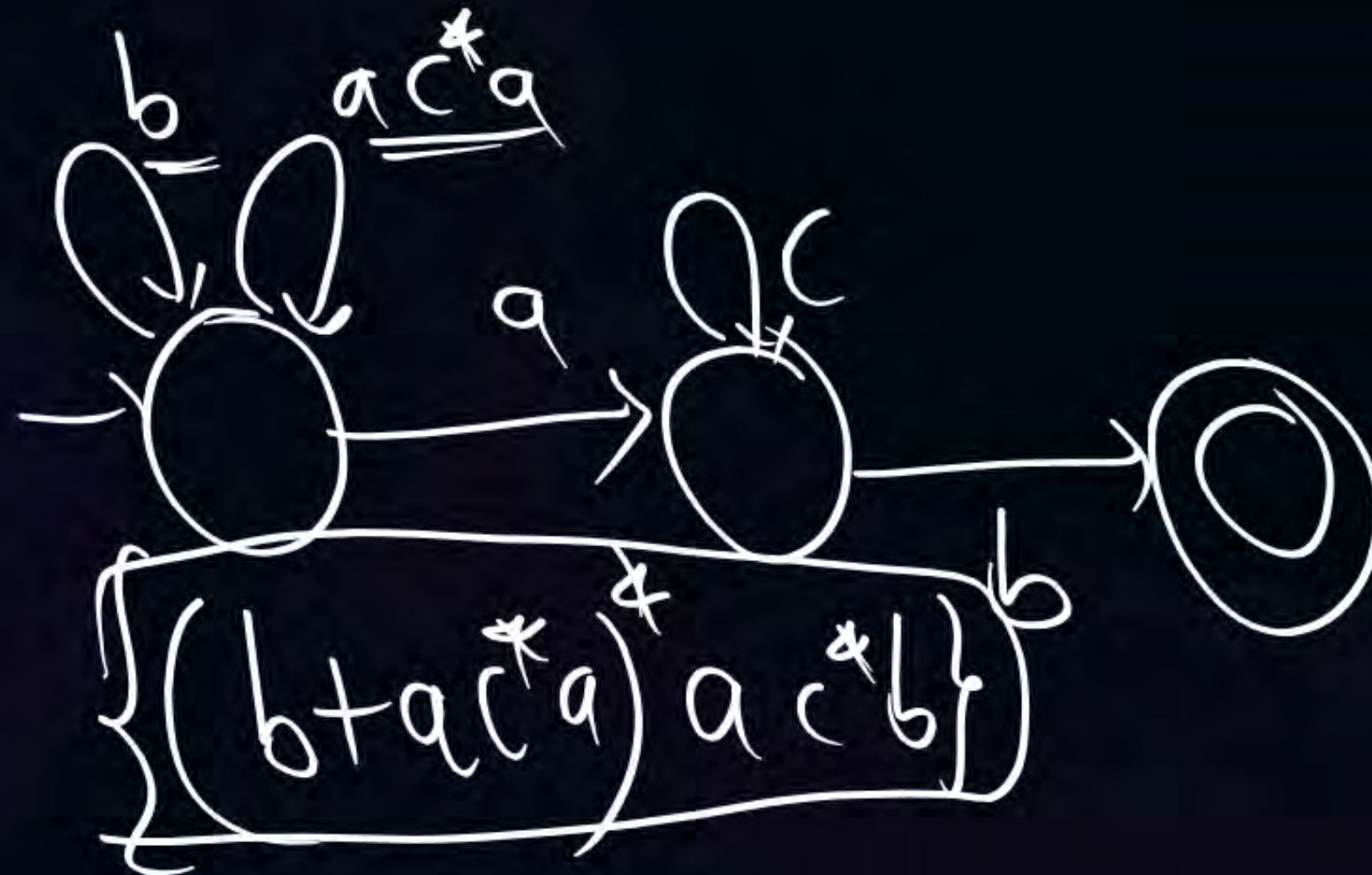
③



$(ac^*b)^* ac^*a$

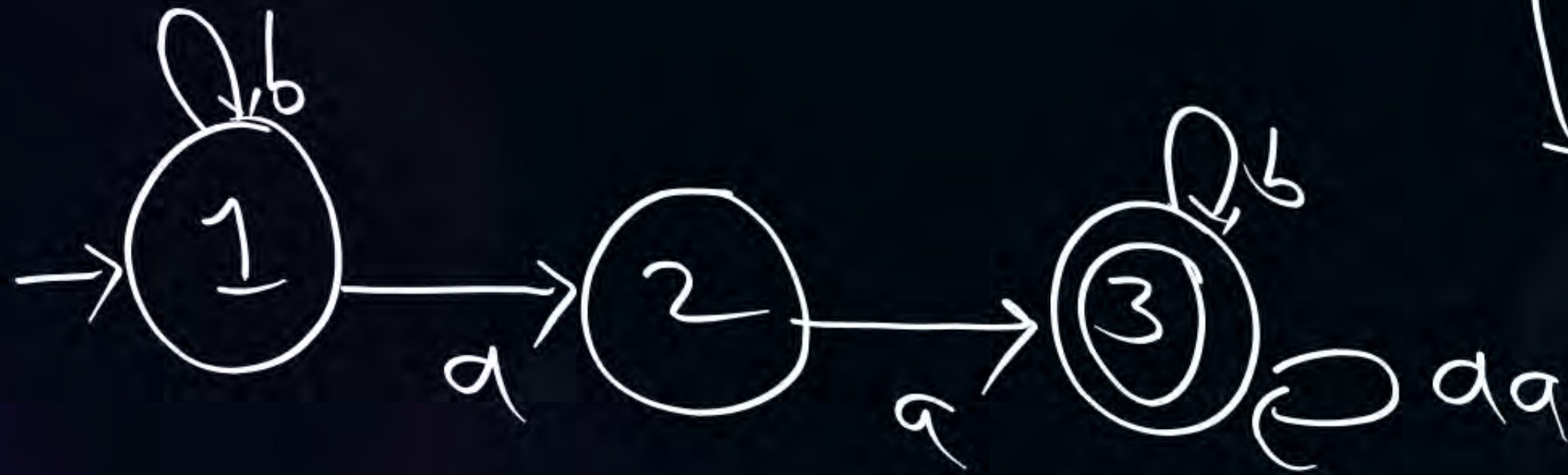
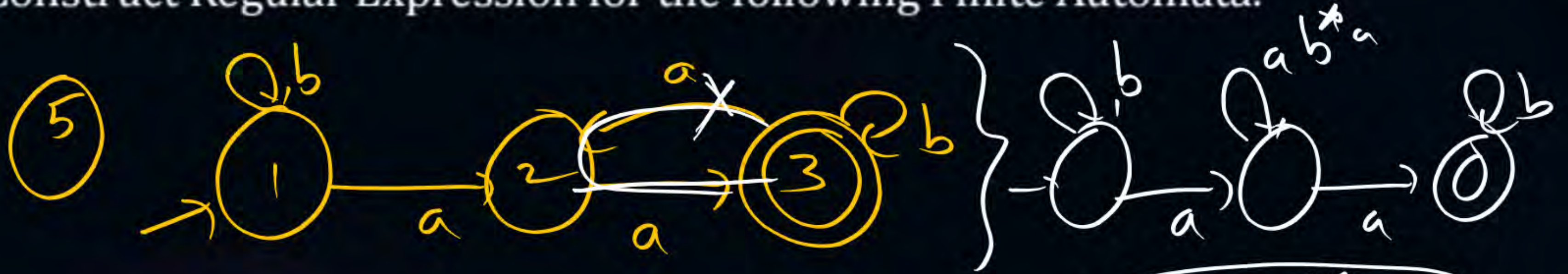


#Q. Construct Regular Expression for the following Finite Automata.





#Q. Construct Regular Expression for the following Finite Automata.

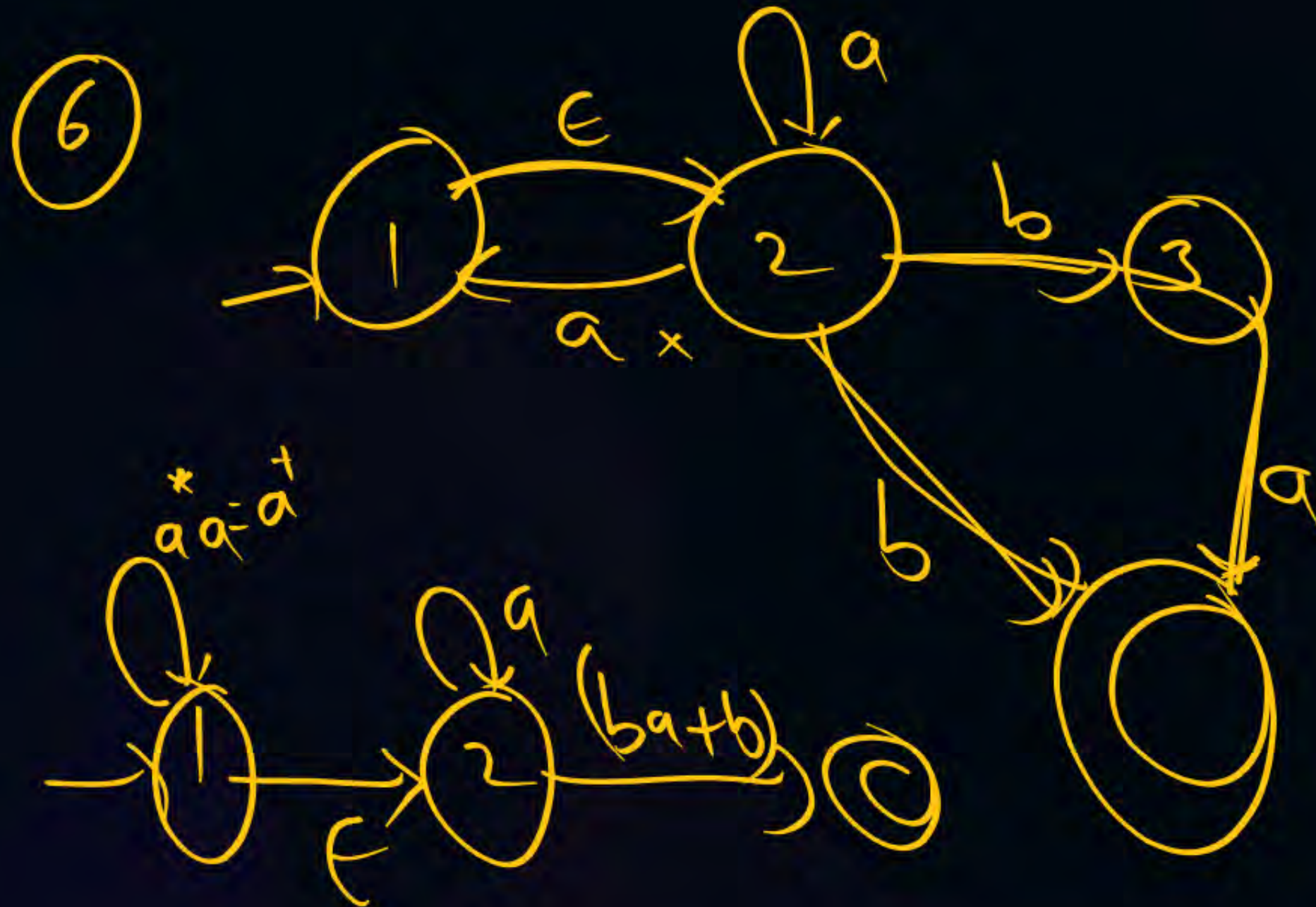


$$b^* a (a b^* a)^* a b^*$$

$$b^* a a (b + a a)^*$$



#Q. Construct Regular Expression for the following Finite Automata.

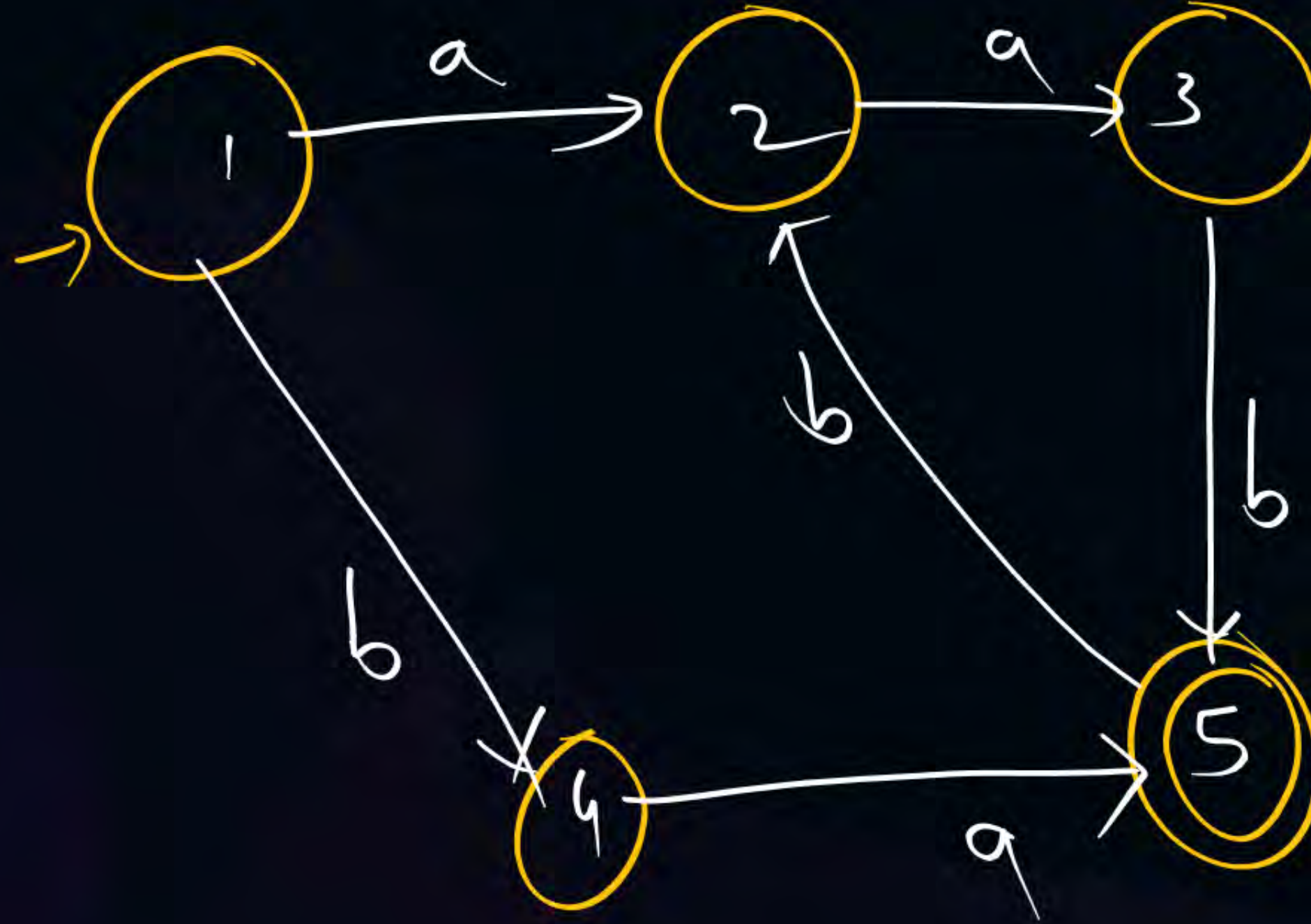


$$\begin{aligned}
 (a^+)^* a^* (ba+ab) &= a^* (ba+ab) \\
 a^+ \cdot a^* (ba+ab)
 \end{aligned}$$



#Q. Construct Regular Expression for the following Finite Automata.

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Regular Expr?

Home Work



## Question



$$\frac{a^*b^*}{\epsilon}$$

#Q. Consider the following regular expressions:

- (I)  $a^*b^* + a^*$   $\equiv a^*b^*$
- (II)  $(\epsilon + aa^*)(bb^* + \epsilon) = a^*b^*$   
 $(\epsilon + a^+)a^*(b^+ + \epsilon)$
- ~~(III)  $b^*a^* + a^*b^* + b^*$~~
- ~~(IV)  $aa^+bb^+$~~

Which the following is equivalent to  $a^*b^*$

**A** (I) and (II) only

**B** (I) only

**C** (II) and (III) only

**D** (I) and (IV) only



## Question



#Q. Which of the following is not correct?

⊂

**A**  $a^*b^+ = a^*b^+$

**B**  $a^*a^+ = a^+$

$\in \{a, a^2, a^3, \dots\}$

**C**  $a^+a^+ = a^+$

**D**  $\phi^* = \epsilon$



## Question



#Q. Consider following regular expressions:

[I]  $(ab)^*a \neq a(ab)^*$

[II]  $(bb)^*b^* = b^*$

[III]  $(b + \epsilon)^+ = b^*$

Which of the following is correct?

**A** II and III only

**B** I and II only

**C** All are correct

**D** None of these are correct



## Question



#Q. Let  $L_1 = \phi$ ,  $L_2 = \{\epsilon\}$ ,  $L_3 = \{a, \epsilon\}$ .

$L_1, L_2, L_3$  are languages defined over  $\Sigma = \{a\}$  then,

$$L_1 \cdot L_2^* + L_3 \cdot L_1 + L_1^* \cdot L_2 \cdot L_3 = ?$$
$$\underline{\phi \cdot \epsilon} + \{a, \epsilon\} \cdot \phi + \phi^* \cdot \epsilon \cdot \{a, \epsilon\}$$
$$\phi + \phi + \epsilon \cdot \epsilon \cdot \{a, \epsilon\} = \{a, \epsilon\}$$

**A**  $\phi$

**B**  $\{a\}$

**C**  $\{a, \epsilon\}$  ✓

**D**  $\{a^n \mid n \geq 2\}$





**THANK - YOU**