

CS & IT ENGINEERING



Theory of Computation

DFA

Lecture No.- 02



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Recap of Previous Lecture



Topic

TOC Introduction

Topic

Alphabet

Topic

String $\Rightarrow \epsilon$

Language \Rightarrow

- Empty Language
- Finite Language
- Infinite Language

DFA = $(Q, \Sigma, q_0, F, \delta)$ // F.A \Rightarrow DFA

Topics to be Covered



Topic

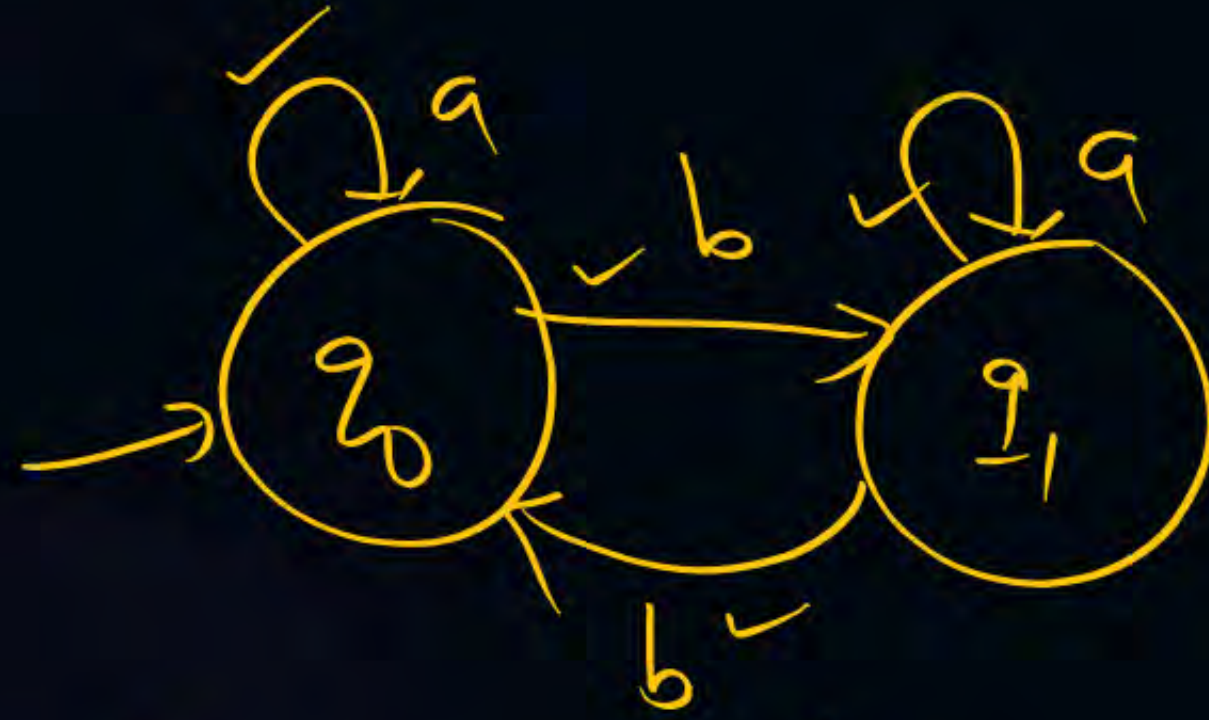
DFA Construction

Topic

??

Topic

??



DFA? $(Q, \Sigma, q_0, \underline{\underline{F}}, \delta)$

\checkmark \checkmark \checkmark \checkmark

F : set of final states

$n, m \geq 1$

$L_1 = \{a^n b^m \mid n > m\} \Rightarrow$ Dependency exist
DFA not possible

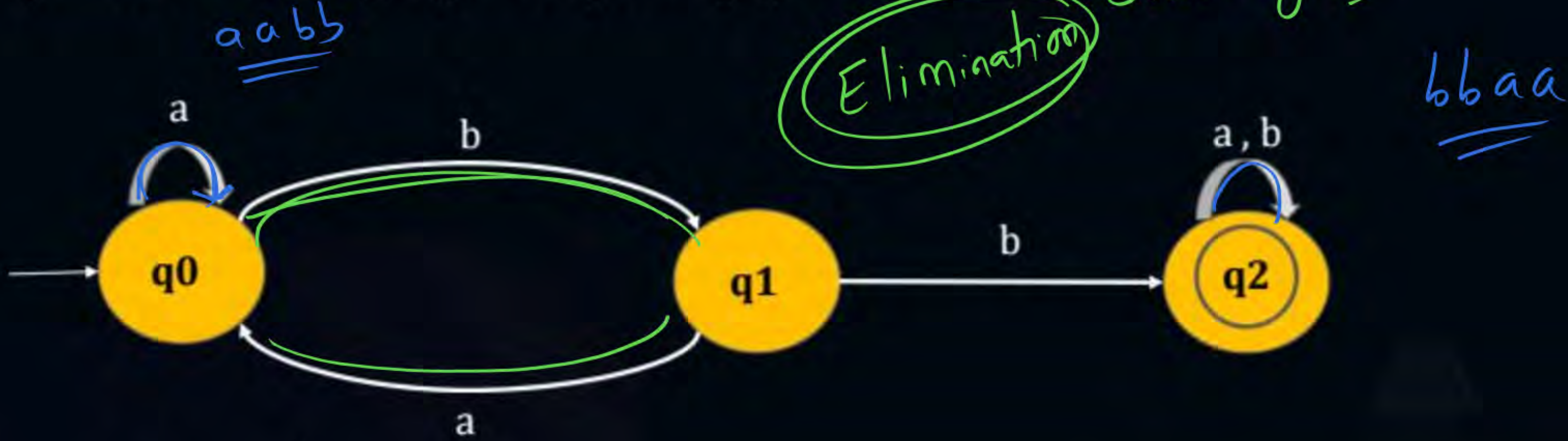
$L_2 = \{ \underline{a^n} \underline{(b^{2m})} \mid n, m \geq 1 \} \Rightarrow$ DFA possible

$a^n (bb)^m$

L_2 : Regular Language?

$\begin{array}{l}
 \text{DFA} \Rightarrow \text{Language} \\
 = \quad \oplus
 \end{array}$

#Q. Identify language accepted by given DFA

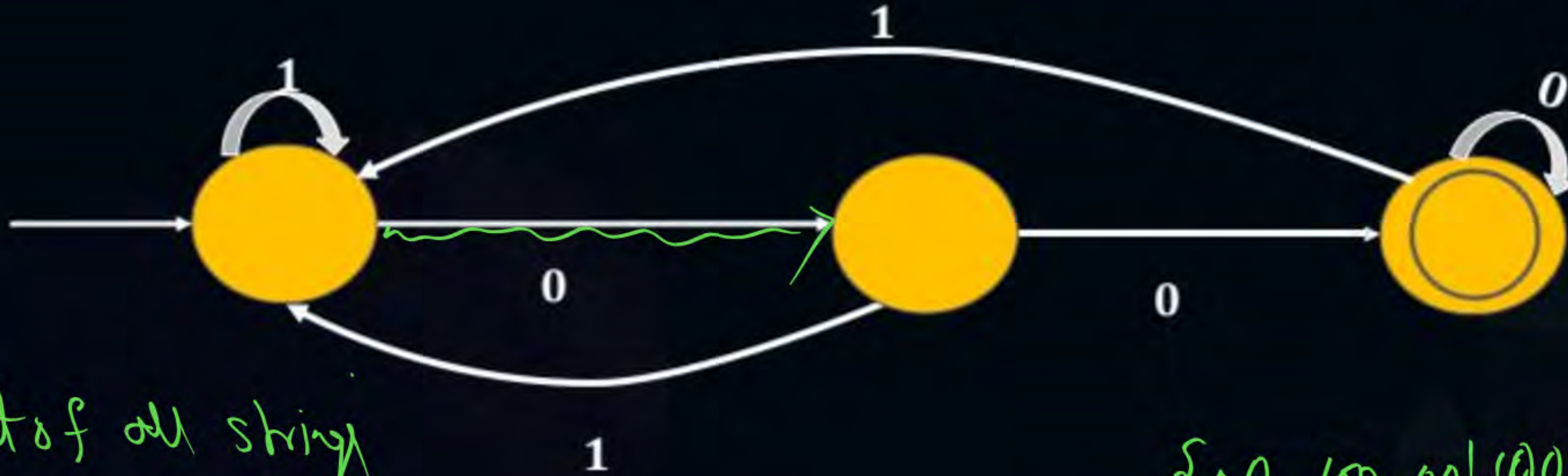


Set of all strings

- Options:
- A** ~~Starting with bb~~ = $\{bb, bab, bba, baba, \dots\}$
 - B** ~~Ending with bb~~
 - C** Contains at least 2 b's
 - D** None

#Q. Identify language accepted by following DFA

elimination ending with 00



Set of all strings

A Starting with 00

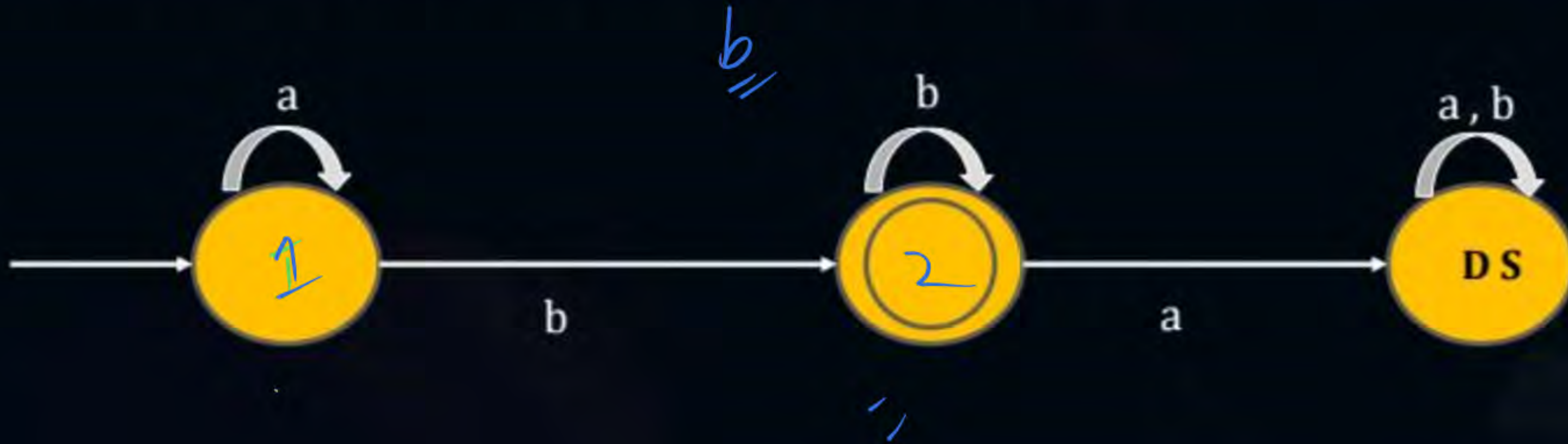
B Substring 00

C Ending with 0 = {0, 10, 00, ...}

D ✓ None

{00, 100, 001, 001, ...}

#Q. Identify language accepted by following DFA



A $L = \{a^n b^m \mid n, m \geq 1\}$ *of ab*

C $L = \{a^n b^m \mid n, m \geq 0\}$ *of*

B $L = \{a^n b^m \mid n \geq 1, m \geq 0\}$ *of a*

D None

#Q. Identify language accepted by following DFA



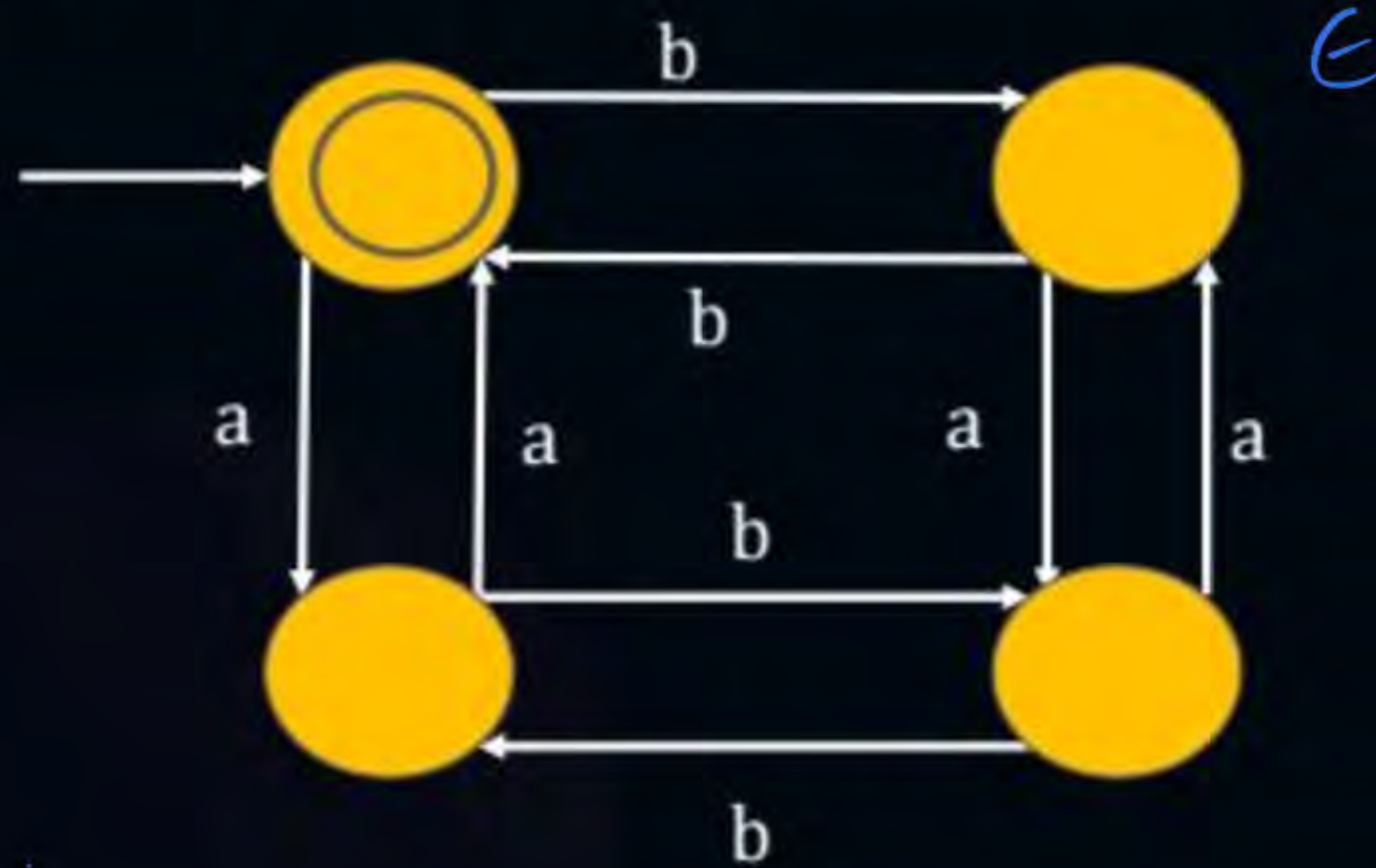
A $L = \{a^n b^m \mid n, m \geq 1\}$

B $L = \{a^n b^m \mid n \geq 1, m \geq 0\}$

C $L = \{a^n b^m \mid n, m \geq 0\}$

D None

#Q. Identify language accepted by following DFA



A ✓ # a's even and # b's even ✓

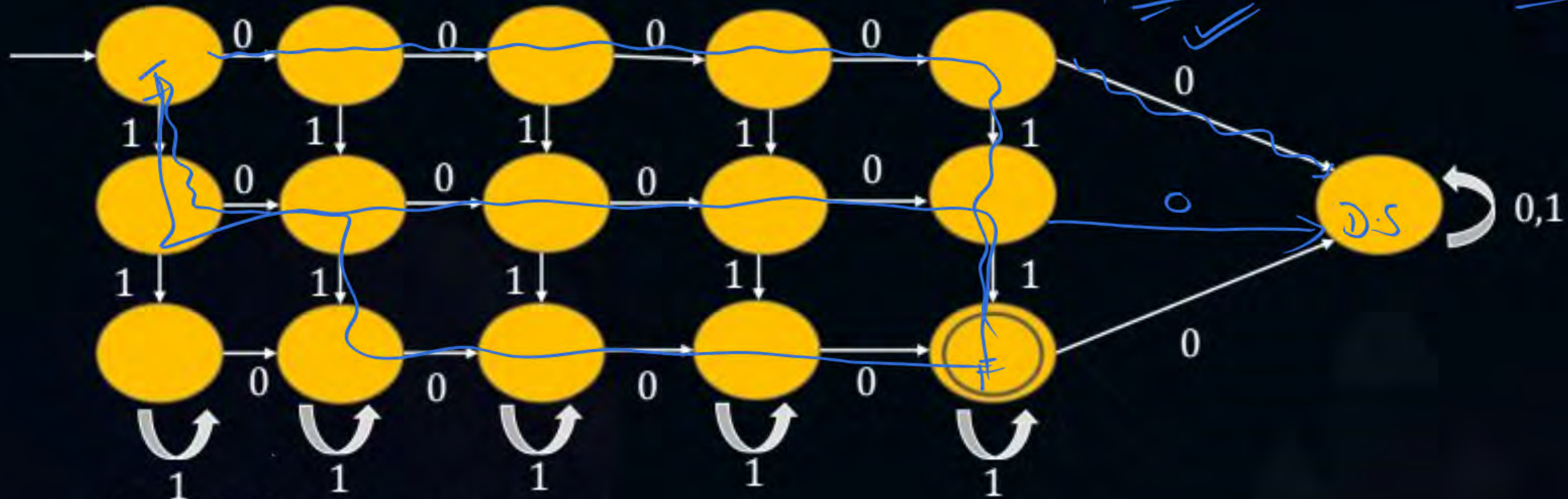
B ✗ # a's odd and # b's even

C ✗ # a's odd and # b's odd ✓

D ✗ # a's even and # b's odd

#Q. Identify language accepted by following DFA

#0's exactly 4 and #1's atleast 2



Set of all strings contains

- | | | | |
|----------|-------------------------------------|----------|-----------------------------------|
| A | Length of the string atleast 6 | B | # 0's exactly 4 and 1's atleast 3 |
| C | # 0's atleast 4 and # 1's exactly 2 | D | None |



Topic : DFA Construction



Dependency

If (comparision) exist between symbols of language then
DFA is not possible.



Topic : DFA Construction

$$L = \{ \underline{a}^n \underline{b}^m \mid n, m \geq 1 \}$$

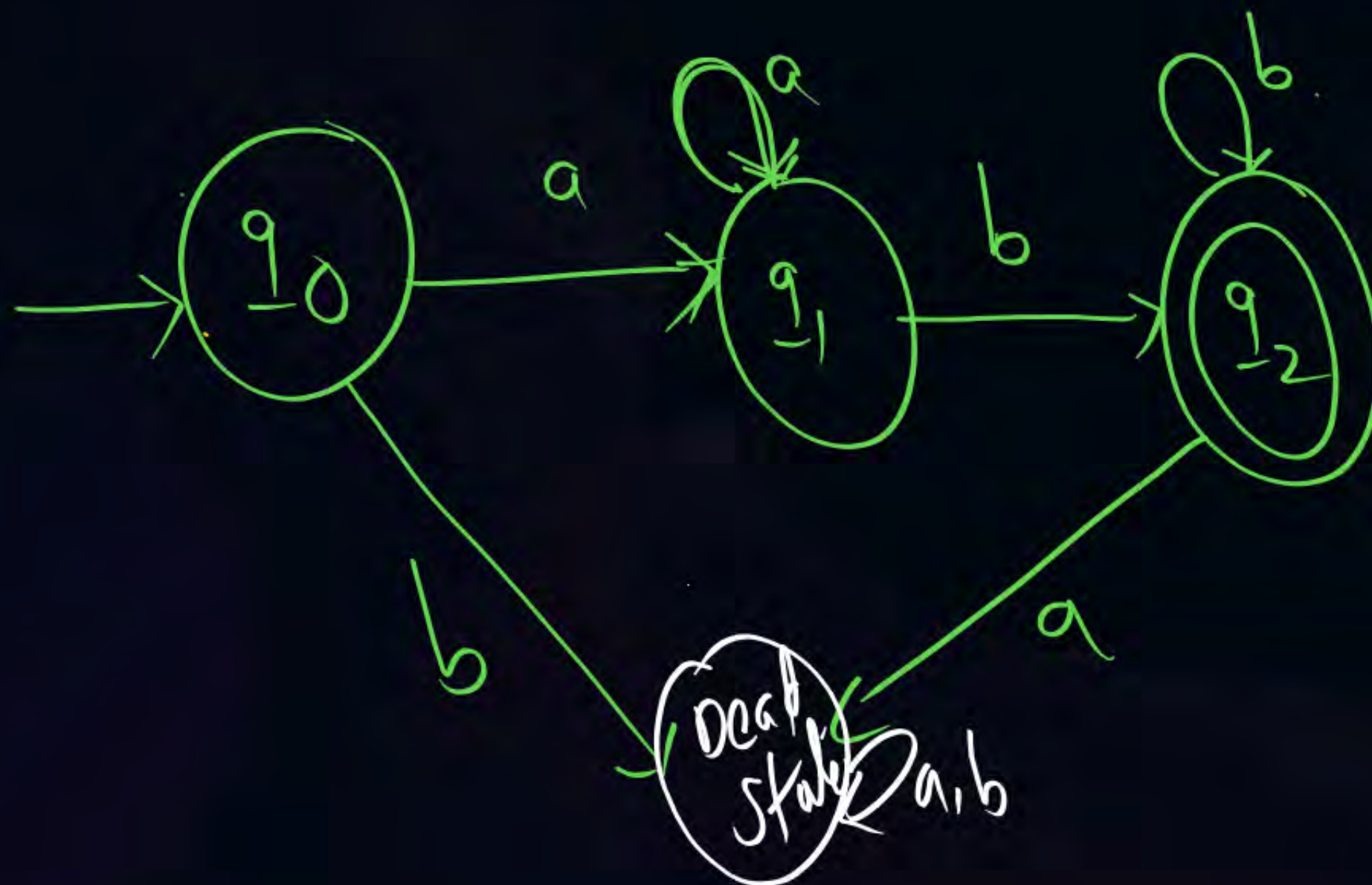
Construct DFA for the following Language.

$(Q, \Sigma, q_0, F, \delta)$

$\underline{a} \underline{a} \underline{a} \underline{b}$
 $\underline{a} \underline{a} \underline{b}$

$L = \{ \underline{ab}, \underline{a^2b}, \underline{ab^2}, \underline{a^2b^2}, \dots \}$

How many states?



4 states



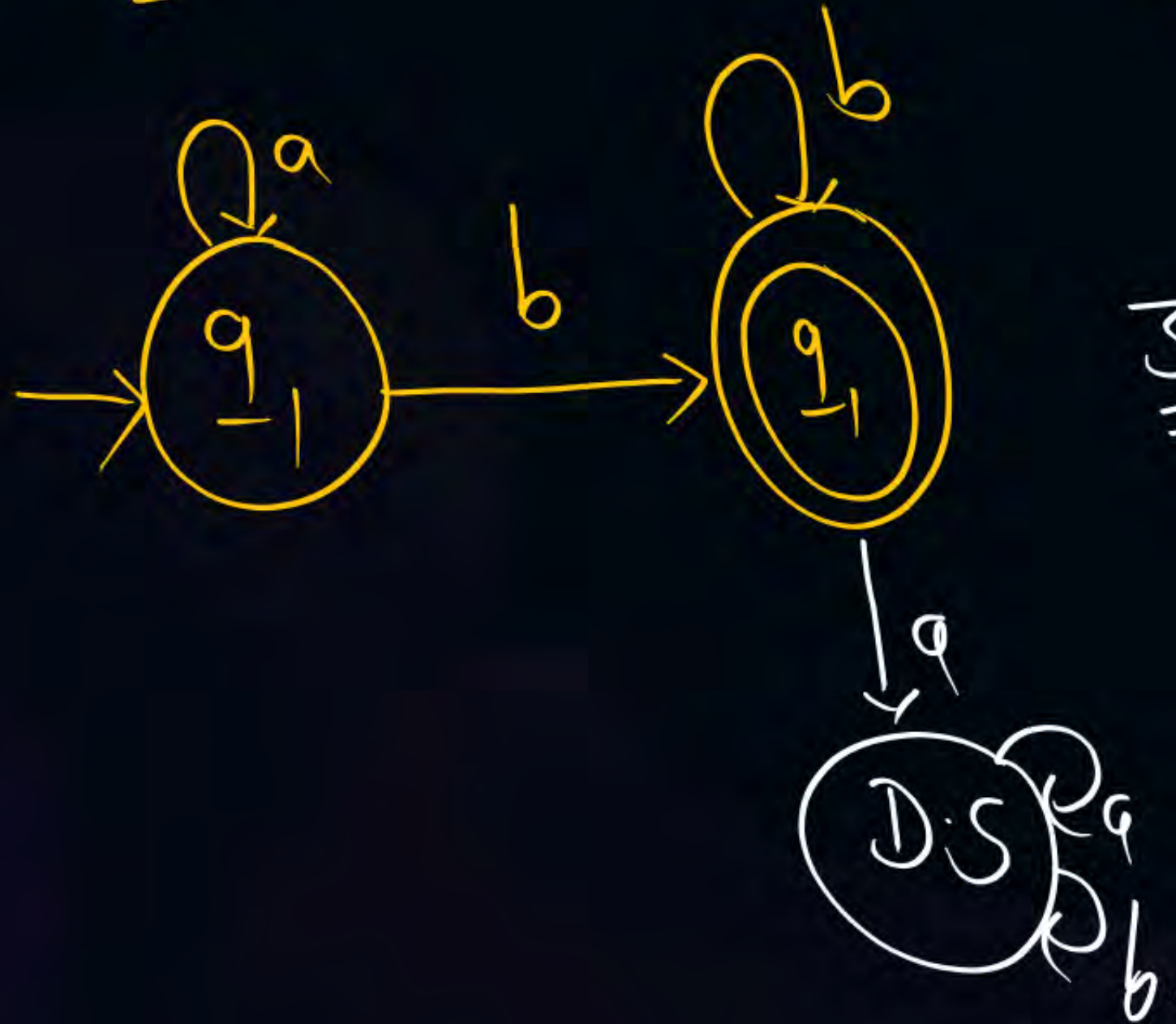
Topic : DFA Construction

$$L = \{ \underline{a}^n \underline{b}^m \mid n \geq 0, m \geq 1 \}$$

Construct DFA for the following Language.

ab

$$\left\{ \boxed{\underline{b}}, \underline{b^2}, \underline{b^3}, \dots \right\}$$
$$\left\{ \underline{ab}, \underline{a^2b}, \underline{ab^2}, \dots \right\}$$



3 states



Topic : DFA Construction

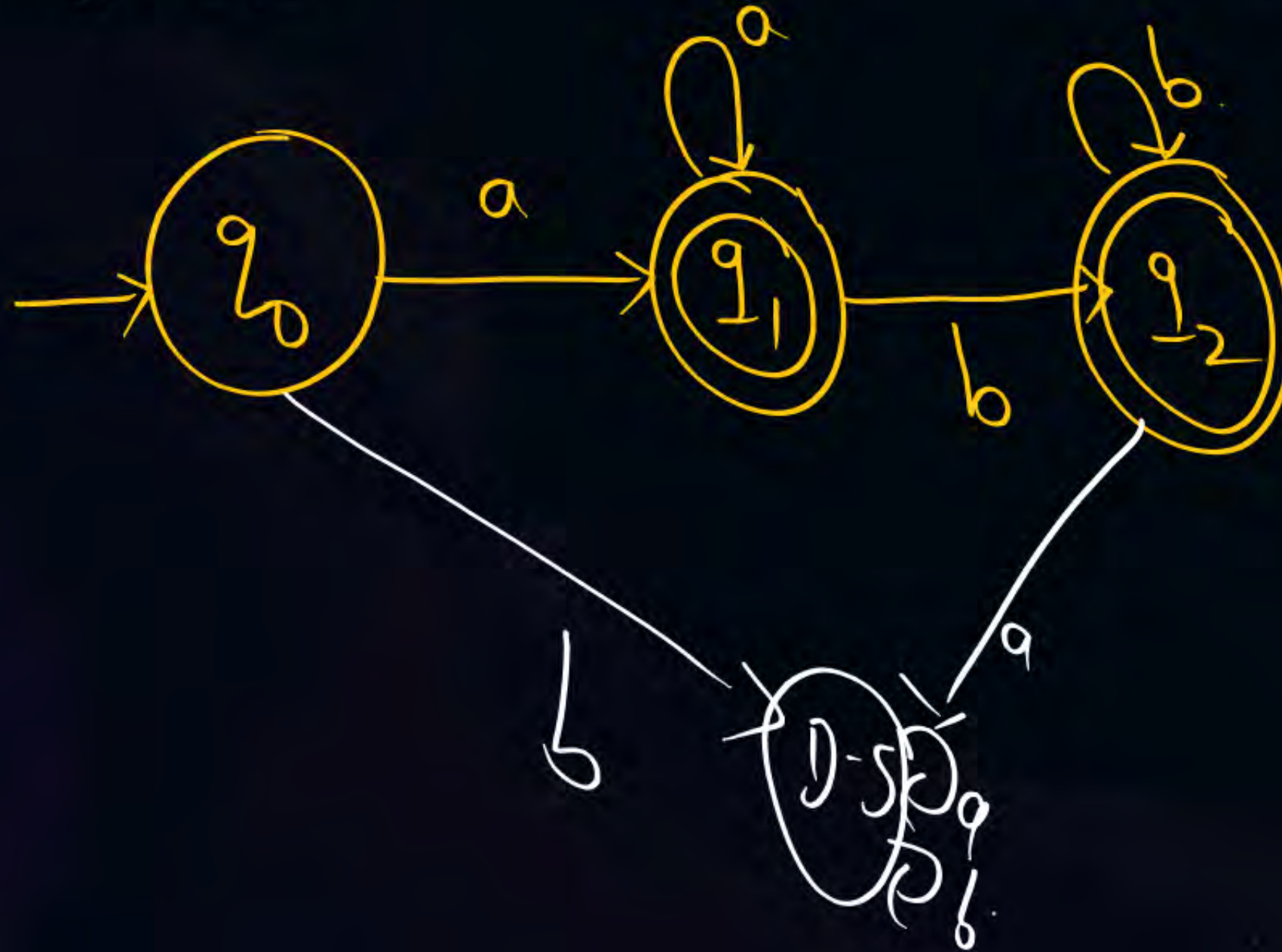
$$L = \{ a^n b^m \mid n \geq 1, m \geq 0 \}$$

Construct DFA for the following Language.

4 states

ab aba

$$\left\{ \begin{array}{l} \underline{a}, \underline{a^2}, \underline{a^3}, \underline{a^4}, \dots \\ \underline{ab}, \underline{a^2b}, \underline{ab^2}, \underline{a^2b^2}, \dots \end{array} \right\}$$



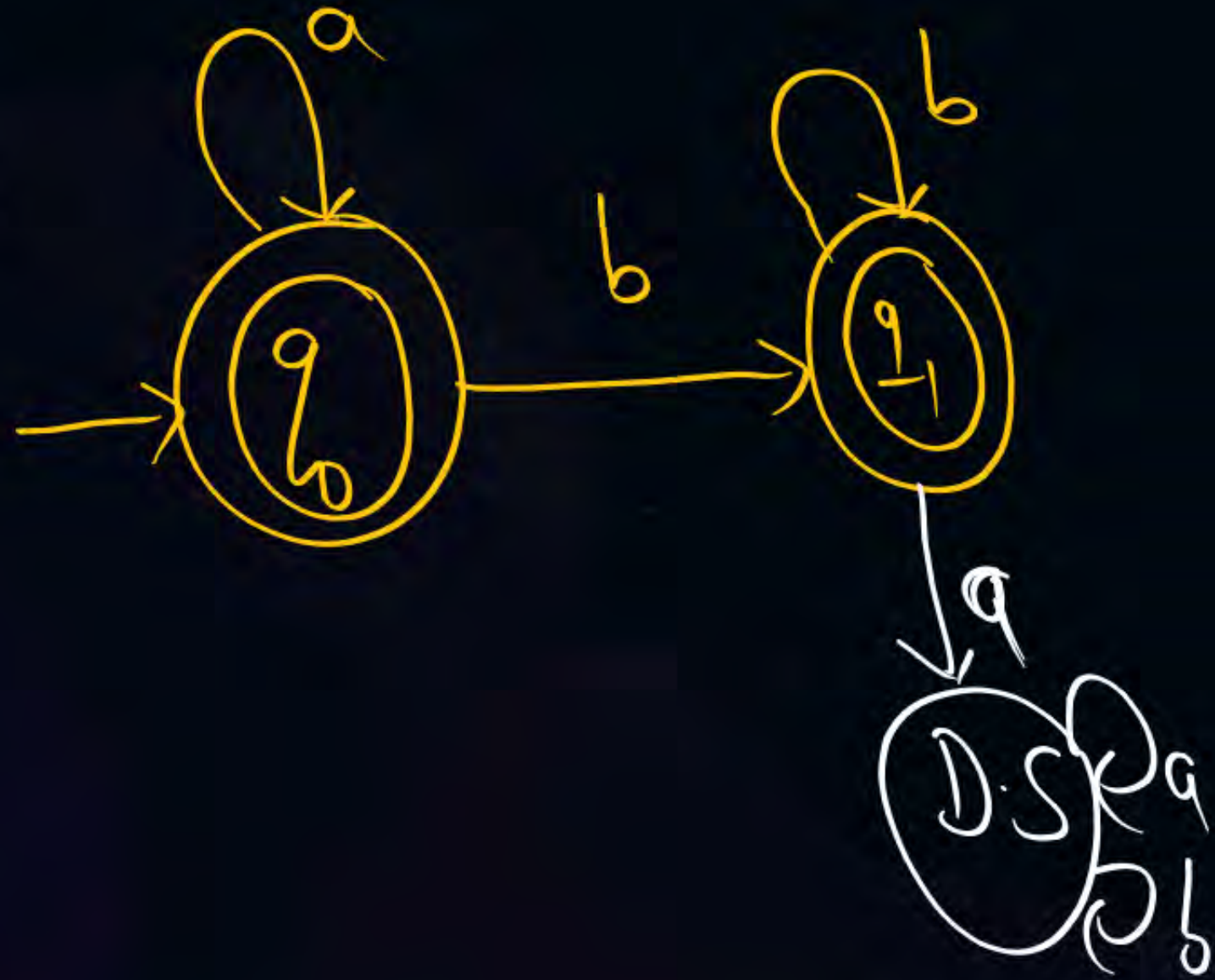


Topic : DFA Construction

$$L = \{a^n b^m \mid n, m \geq 0\}$$

Construct DFA for the following Language.

DFA
3 state



$\{ \epsilon, a, a^2, \dots, b, b^2, \dots, ab, ab^2, \dots \}$

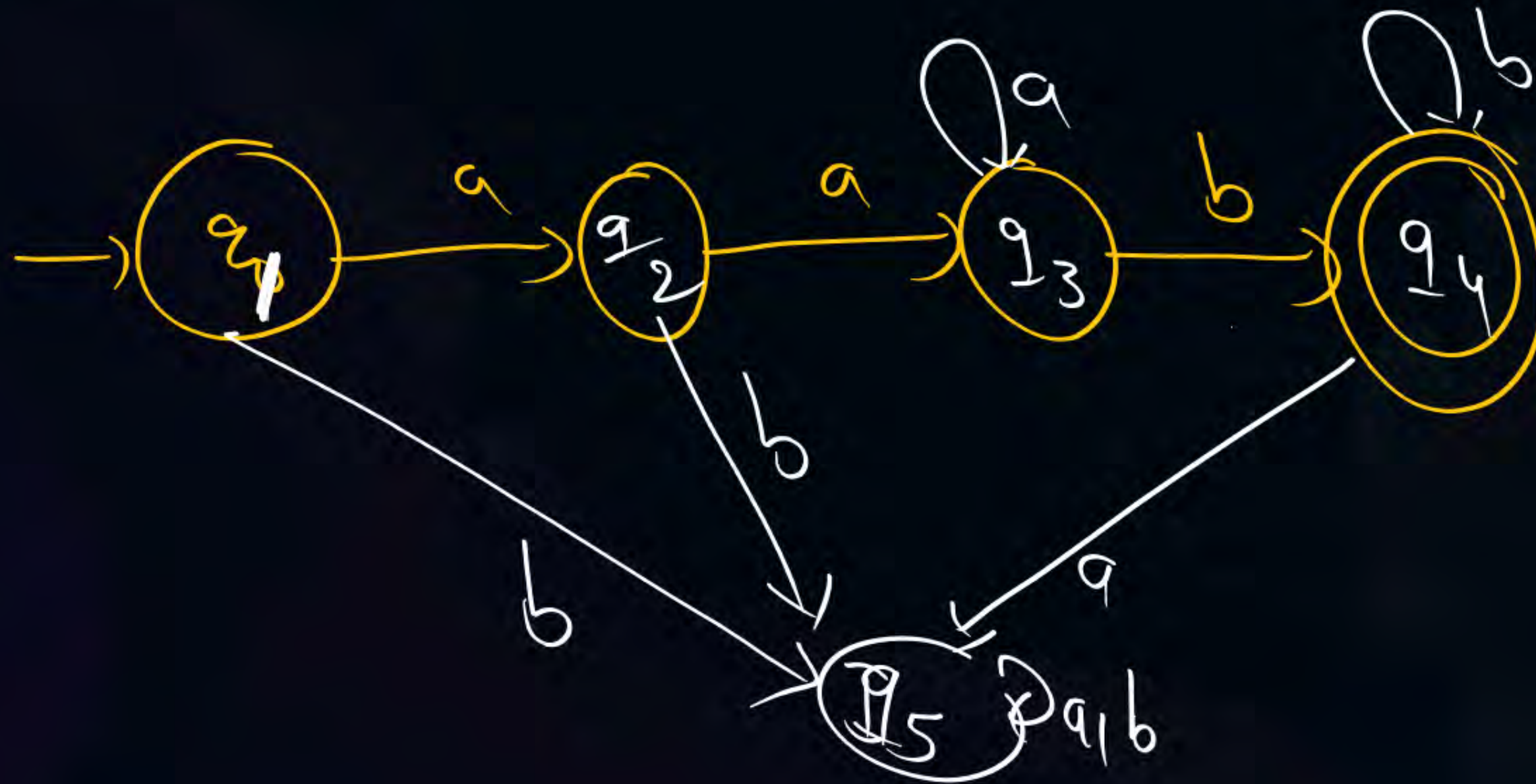


Topic : DFA Construction

Construct DFA for the following Language.

DFA = 5 states

$$L = \{ \underline{a^n b^m} \mid n \geq 2, m \geq 1 \} = \{ a^2 b, \dots \}$$





Topic : DFA Construction

Construct DFA for the following Language.

$$L = \{ \underline{a^{2^n}} \mid n \geq 1 \} = \{ \overset{3}{\cancel{x}} a^2 \cup \overset{5}{\cancel{x}} a^4 \cup \overset{7}{\cancel{x}} a^6 \dots \}$$



3 states



Topic : DFA Construction

Construct DFA for the following Language.

$$L = \{ a^{2^n} \mid n \geq 1 \} = \{ \underbrace{a^2}_2, \underbrace{a^4}_4, \underbrace{a^8}_8, a^{16}, \dots \}$$

(a) 3

(b) 5

(c) 8

(d) none

$$0 \xrightarrow{a} 0 \xrightarrow{a} 0 \xrightarrow{a} 0 \xrightarrow{a} 0 \dots$$

X

DFA not possible



Topic : DFA Construction



Construct DFA for the following Language.



NOTE

If a language formed over 1 symbol
then common difference should exist
between string to construct DFA
otherwise DFA not possible.

Q which of the following is Regular Language?

(a) $L = \{a^n \mid n \geq 1\} = \{a^1, a^4, a^{27} \dots\}$ X

(b) $L = \{a^p \mid p \text{ is prime number}\} = \{a^2, a^3, a^5, a^7, a^{11} \dots\}$ X

(c) $L = \{a^k \mid k \text{ is odd number}\} = \{a^1, a^3, a^5, a^7 \dots\}$

(d) none

(Q) Construct DFA over $\Sigma = \{0, 1\}$ where each string is having substring 01

$$L = \{ \underline{01}, 101, 010, 011, 1010, 0\underline{01}1, \dots \}$$

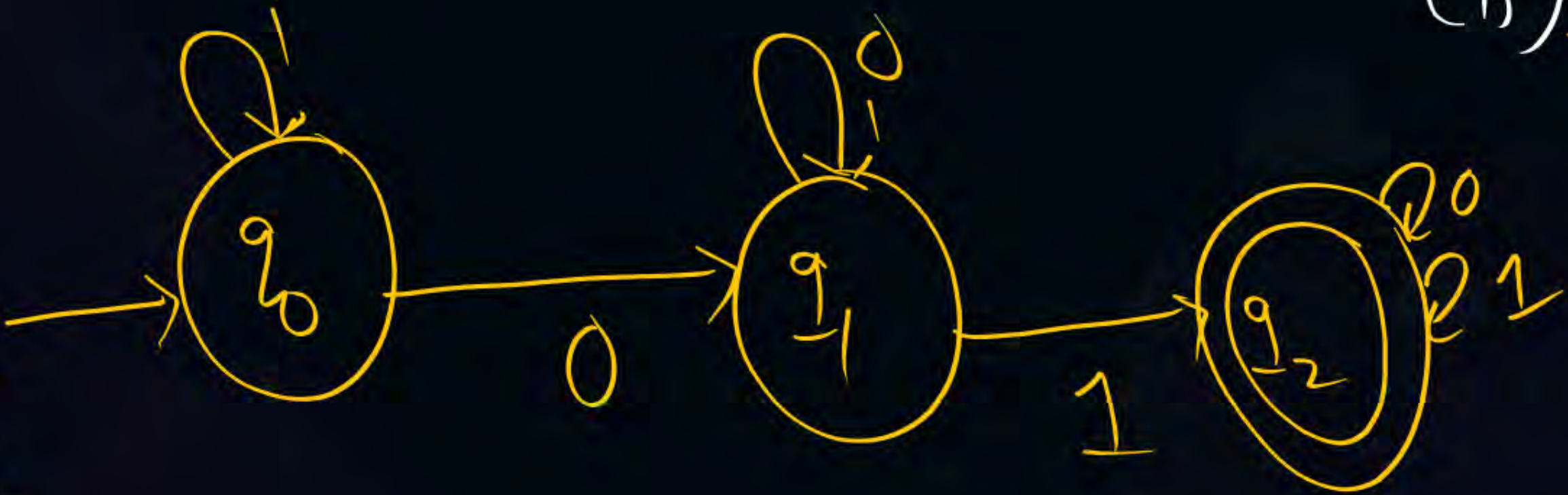
001

||

n length substring

||

(n+1) state

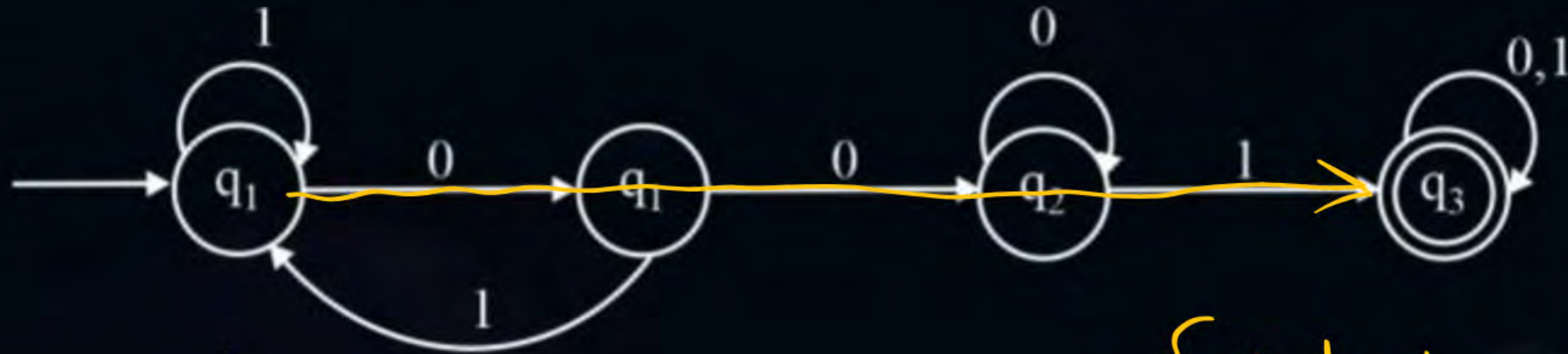


0001

MCQ



#Q. Consider the following deterministic finite automata m.



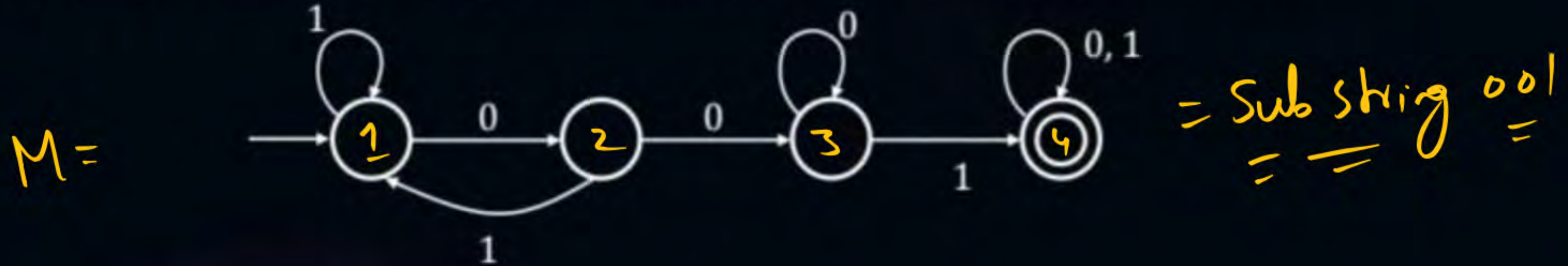
$\{ \underline{\text{Sub strings } 001} \}$

The language accepted by finite automata,?

MCQ



#Q. Consider the following deterministic finite state automaton M.



Let S denote the set of seven-bit binary strings in which the first, the fourth, and the last bits are 1. The number of strings in S that are accepted by M is

$$S: \underline{1} \underline{\begin{smallmatrix} 0 & 0 \\ 1 & 1 \end{smallmatrix}} \underline{1} \underline{\begin{smallmatrix} 0 & 0 \\ 1 & 0 \end{smallmatrix}} \underline{1} \underline{\begin{smallmatrix} 0 & 0 \\ 1 & 1 \end{smallmatrix}} \underline{1} \} \underline{16}$$

A 1

B 5

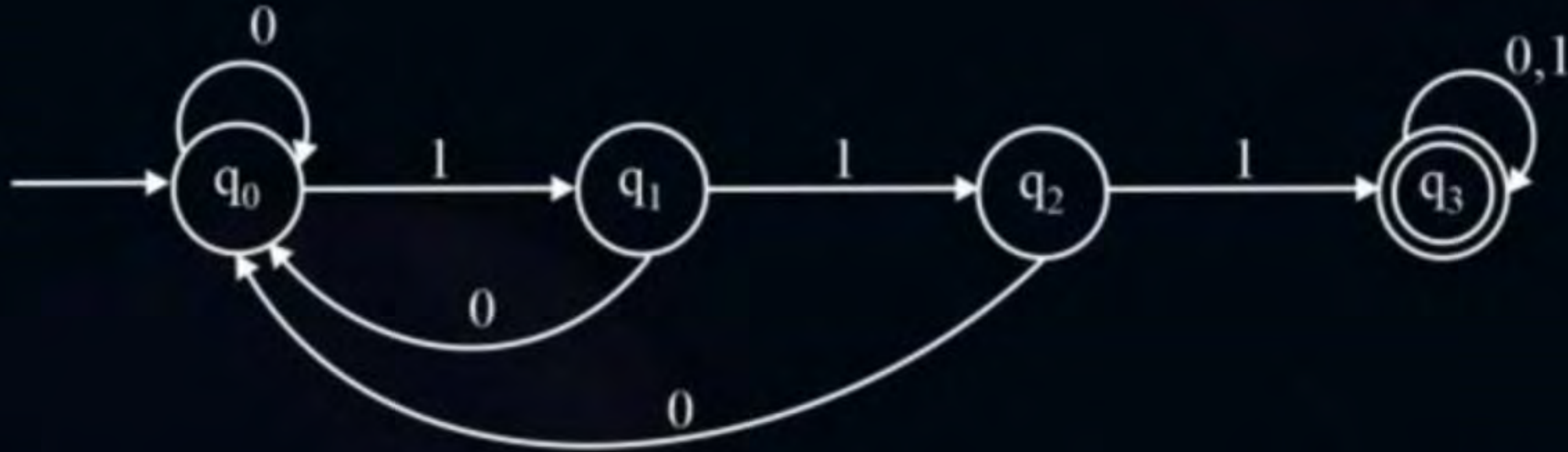
☒ **C** 7

D 8

	0	0		0	0		}	5
	0	0		0	1			
	0	0		1	0			
	0	0		1	1			
	0	1		0	0			
	0	1		0	1			
	0	1		1	0			
	0	1		1	1			

	1	0		0	0		}	6
	1	0		0	1			
	1	0		1	0			
	1	0		1	1			
	1	1		0	0		}	7
	1	1		0	1			
	1	1		1	0			
	1	1		1	1			

#Q. Consider the finite automata m.



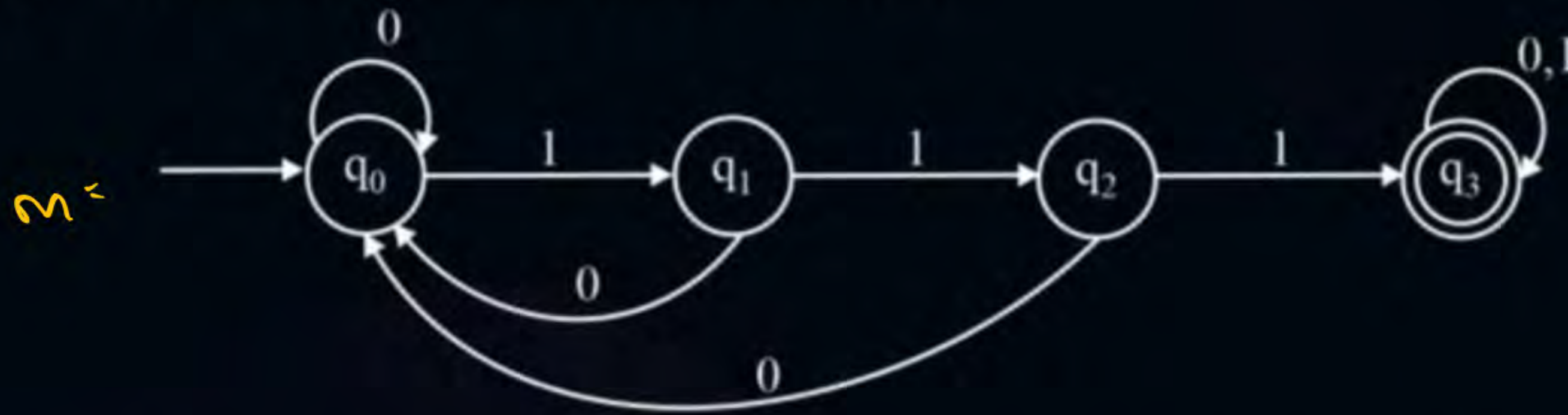
The language accepted by m is, over the alphabet $\{0,1\}$

- A** The set of all strings containing three consecutive I's
- B** The set of all strings not containing three consecutive I's
- C** The set of all strings beginning with three consecutive I's
- D** The set of all strings ending with three consecutive I's

MCQ



#Q. Consider the finite automata m.



Language = ?
Substring !!!
Home work

Let S denotes the set of all six bit binary strings in which first and fourth bits are 1. The number of strings in S that are accepted by m is-

A 1

C 7

S: 1 1 0 1 1 1
4+1+2+1
8

B 4

✓ **D** 8



THANK - YOU