

CS & IT ENGINEERING



THEORY OF COMPUTATION

Regular Expressions

DPP - 02 Discussion Notes



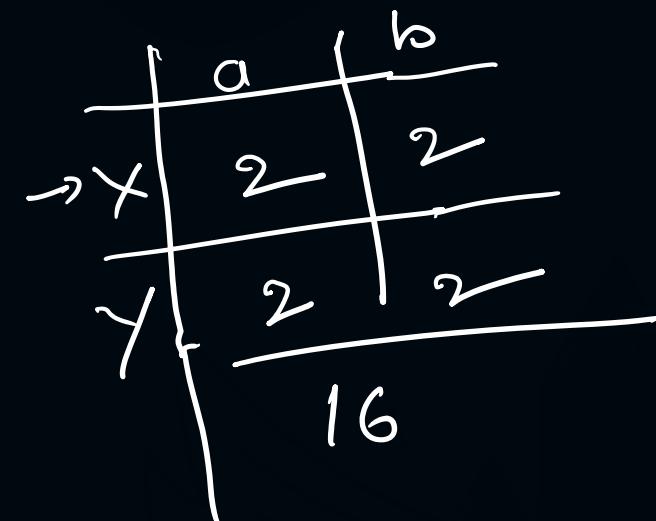
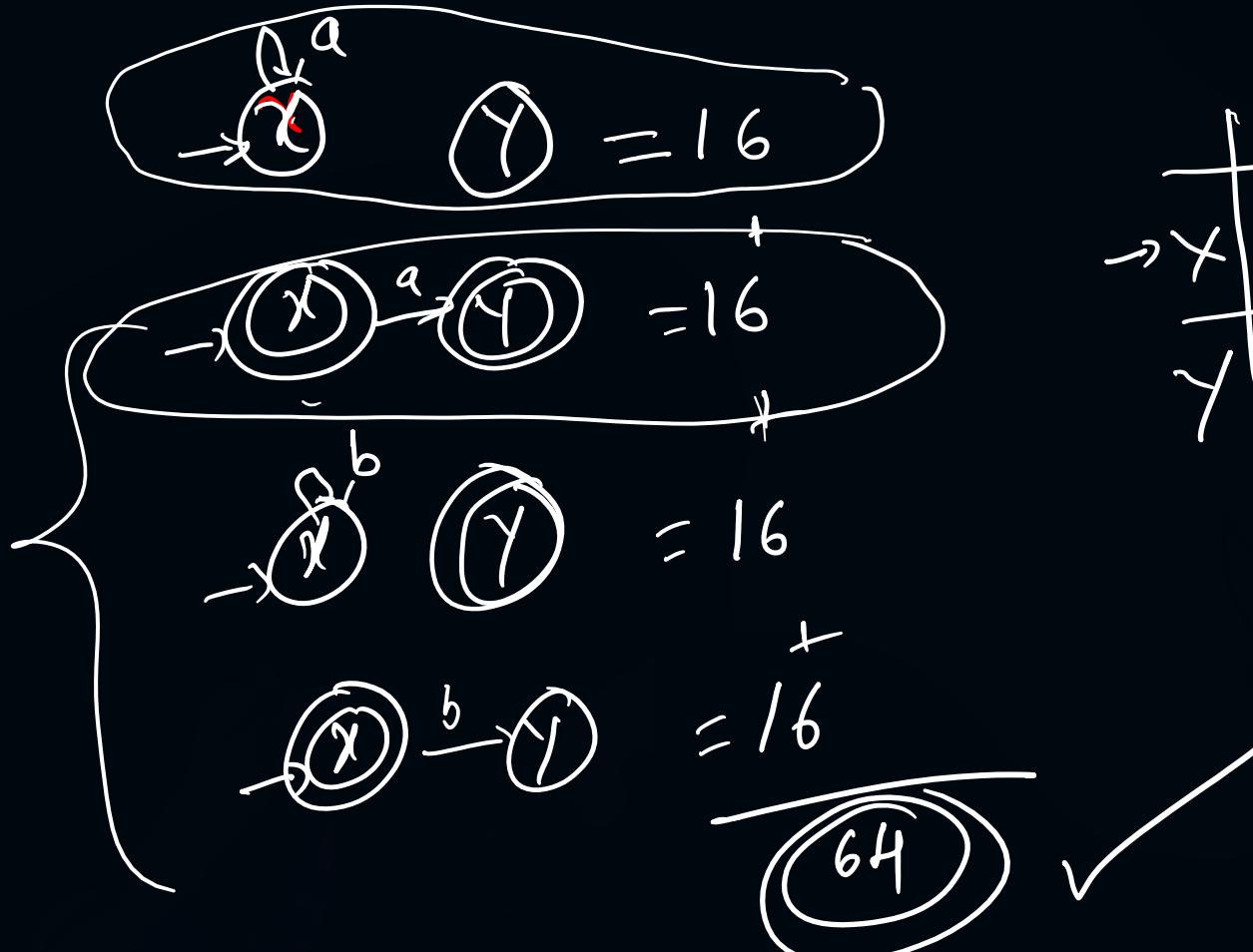
By- Venkat sir

[NAT]

P
W

$\begin{matrix} 2 & 2 & x \\ Q, \Sigma, q_0, F, S \end{matrix}$

#Q. The possible number of DFA with 2 states X,Y over the alphabet {a, b} where X is always initial state ?

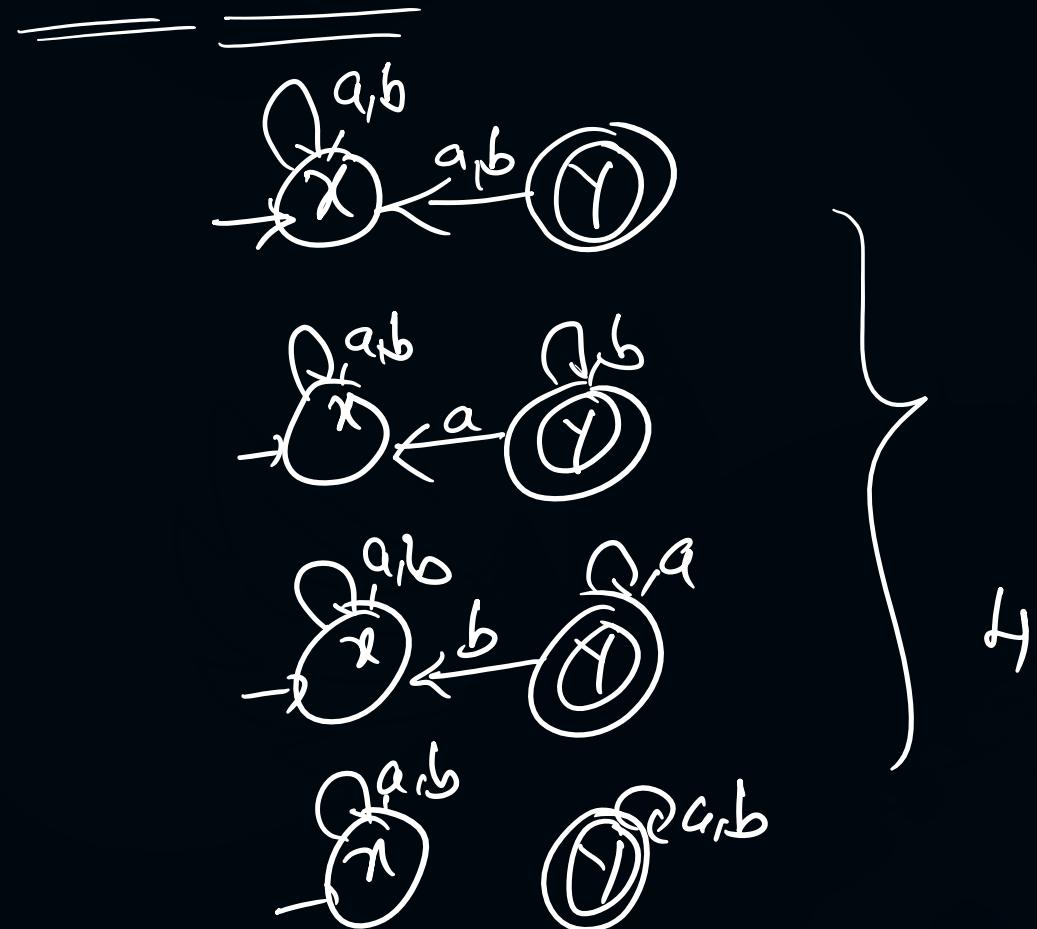
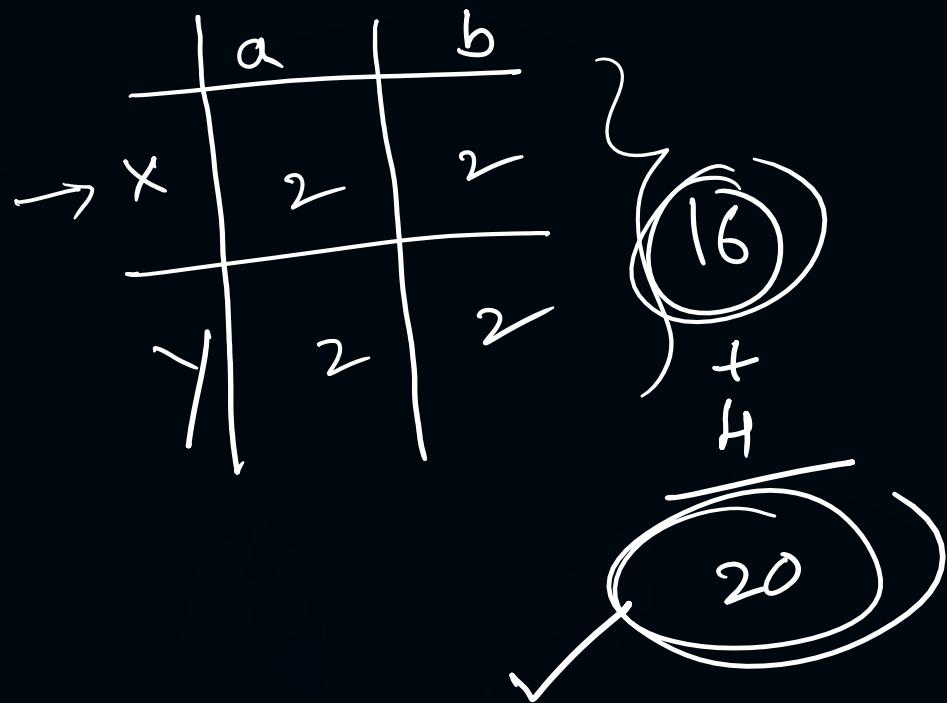


$$2^4 = 16$$

64

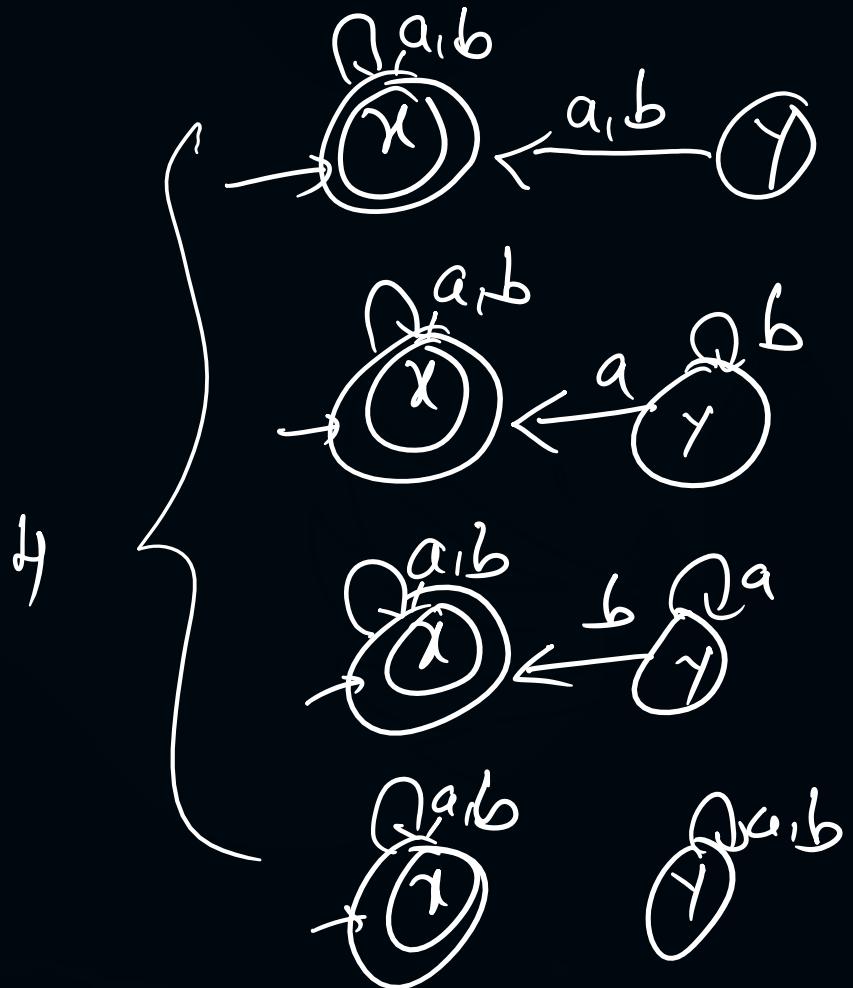


#Q. The possible number of DFA with 2 states X,Y over the alphabet {a, b} where X is always initial state , that accepts empty language?



#Q. The possible number of DFA with 2 states X,Y over the alphabet {a, b} where X is always initial state , that accepts complete language?

$$\begin{array}{c} 16 \\ + \\ 4 \\ \hline 20 \end{array}$$



[MCQ]

Consider the DFA ,M with states $Q=\{0,1,2,3,4\}$, input alphabet $\Sigma = \{0,1\}$ start state 0, final state 0 and transition function $\delta(q,i) = |q^2 - i| \text{ mod } 5$ $q \in Q$ input alphabets are $\{0,1\}$

#Q. The above DFA, M accepts all binary strings containing

- A even number of 1's
- B odd number of 1's
- C even number of 0's
- D odd number of 0's

$$\delta(\underline{0,0}) = \underline{10-0} \bmod 5 = 0 \checkmark$$

$$\delta(\underline{0,1}) = \underline{10-1} \bmod 5 = 1 \checkmark$$

$$\delta(\underline{1,0}) = \underline{11-0} \bmod 5 = 1 \checkmark$$

$$\delta(\underline{1,1}) = \underline{11-1} \bmod 5 = 0 \checkmark$$

$$\delta(\underline{2,0}) = \underline{14-0} \bmod 5 = 4 \checkmark$$

$$\delta(\underline{2,1}) = \underline{14-1} \bmod 5 = 3 \checkmark$$

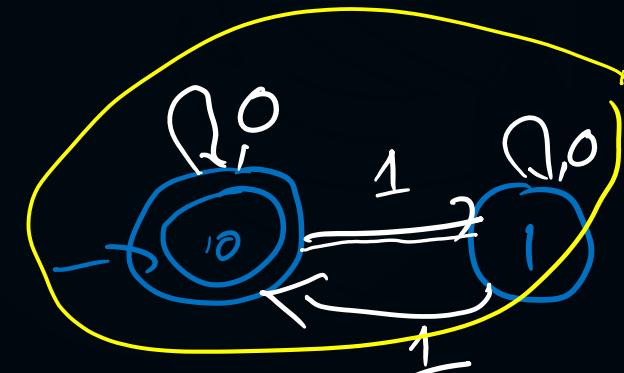
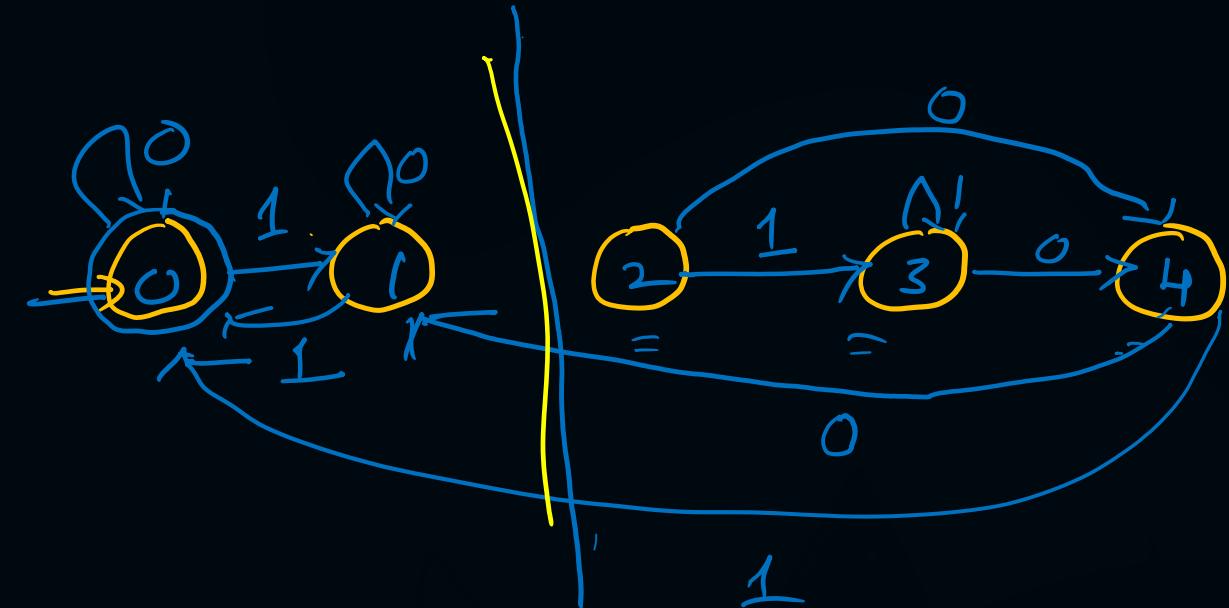
$$\delta(\underline{3,0}) = \underline{19-0} \bmod 5 = 4 \checkmark$$

$$\delta(\underline{3,1}) = \underline{19-1} \bmod 5 = 3 \checkmark$$

$$\delta(\underline{4,0}) = \underline{(16-0)} \bmod 5 = 1 \checkmark$$

$$\delta(\underline{4,1}) = \underline{(16-1)} \bmod 5 = 0 \checkmark$$

$$\delta(\underline{q_1,i}) = (q^2-i) \bmod 5$$



[MCQ] Consider the DFA ,M with states $Q=\{0,1,2,3,4\}$, input alphabet $\Sigma = \{0,1\}$ start state 0, final state 0 and transition function $\delta(q,i)=|q^2-i| \text{ mod } 5$ $q \in Q$, input alphabets are $\{0,1\}$

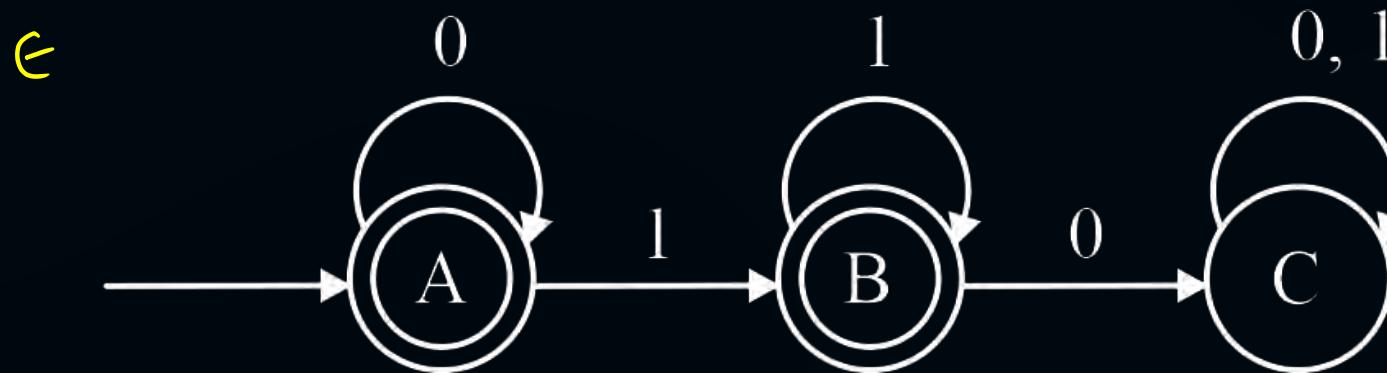
#Q. The number of states in the minimal finite automata ,which is equivalent to M is

- A 1
- B 2
- C 3
- D 4

2



#Q. The regular expression for the language recognized by the following finite automata is?



A ¹⁰
 $(0 + 1)^*$ X

C 0^*1^* ✓

B $0(0 + 1)^*1$ X

D $0^*(0 + 1)^*1^*$ X

[MCQ]



#Q. Choose the regular language from the following

A $L = \{x/x \in (a + b)^*\}$ and is even length palindrome



B $L = \{a^n / n \geq 1\}$ → Regular

C $L = \{a^n b^{2n} / n \geq 1\}$ → non Regular

D दवदम

[MCQ]



#Q. Which of the following regular expression represents all strings of a's and b's where the length of the string is at most 'n' is

A

$$(a + b)^n \rightarrow \text{exactly}$$

$\in, 1, 2, \dots, n$

B

$$(a+b)^n(a+b)^* \rightarrow \text{at least } n$$

C

$$(a + b + \epsilon)^n$$

at most n

C

D

None of the above

[MCQ]



#Q. Which of the following pair of regular expressions are not equal

- A $(r^*)^*$ and $(r^*)^*$ → equal
- B $(r + \epsilon)^*$ and r^* → equal
- C $((r + \epsilon)^*)^*$ and $r^* = \{\epsilon, rr, r^2, r^3\}$ → not equal
- D None of the above

[MCQ]

#Q. Consider the language S^* where S is all strings of a's and b's with odd length. The other description of this language is.

A

All strings of a's and b's

B

All even length strings of a's and b's

C

All odd length strings of a's and b's

D

None of the above

$$\begin{aligned}S^* &= \left[(a+b) \overline{[(a+b)(a+b)]^*} \right]^* \\&= [(a+b) \in]^* = (a+b)^*\end{aligned}$$

[MCQ]

#Q. Let $r = (1 + 0)^*$, $s = 11^*0$ and $t = 1^*0$ be three regular expressions. Which one of the following is true?

A

$L(s) \subset L(r)$ and $L(s) \subset L(t)$

B

$L(r) \subset L(s)$ and $L(s) \subset L(t)$

C

$L(t) \subset L(s)$ and $L(s) \subset L(r)$

D

None of the above

$$t = \{0, 10, 110, 1110, \dots\}$$

$$s = \{10, 110, 1110, \dots\}$$



THANK - YOU