

$4\hat{i} + 5\hat{j} + 6\hat{k}, \lambda\hat{i} + 8\hat{j} + 9\hat{k}$.

- (A) $\lambda = 3$
- (B) $\lambda = 7$
- (C) $\lambda \pm 7$
- (D) $\lambda = 0$

Q14 (a) Show that $(2, 1, 1)$ and $(1, -4, 2)$ are orthogonal.

(b) Determine which of the following vectors are orthogonal :

$$\begin{aligned} v_1 &= (-2, 6, 1), v_2 = (9, 2, 6), v_3 \\ &= (4, -15, -1). \end{aligned}$$

Q15 Among the following, the pair of the vector orthogonal to each other is

- (A) $[3, 4, 7], [3, 4, 7]$
- (B) $[0, 0, 0], [1, 1, 0]$
- (C) $[1, 0, 2], [0, 5, 0]$
- (D) $[1, 1, 1], [-, -1, 1]$

Q16 If $\bar{a} = 3\hat{i} - 2\hat{j} + \hat{k}$ and $\bar{b} = 4\hat{i} + 3\hat{j} - \lambda\hat{k}$ are orthogonal then $\lambda = ?$

- (A) 6
- (B) 12
- (C) -6
- (D) -12

Q17 The vector which is orthogonal to every column

vector of A = $\begin{bmatrix} 1 & 1 & 0 \\ 1 & -1 & 0 \\ 1 & 0 & 1 \\ 1 & 0 & -1 \end{bmatrix}$ will be ?

- (A) $\begin{bmatrix} 1 \\ -1 \\ 0 \\ 1 \end{bmatrix}$
- (B) $\begin{bmatrix} 1 \\ 1 \\ 0 \\ -1 \end{bmatrix}$
- (C) $\begin{bmatrix} 0 \\ -1 \\ 1 \\ 1 \end{bmatrix}$
- (D) $\begin{bmatrix} 1 \\ 1 \\ -1 \\ 0 \end{bmatrix}$

$$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Q18 Norm of vector $[8 \ 4 \ 1]^T$ is given as _____?

Q19

The normalized vector of $\begin{bmatrix} 2 \\ 1 \\ -4 \end{bmatrix}$ will be ?

Q20 For what values of α and β , the following simultaneous equations have an infinite number of solution?

$$\begin{aligned} x + y + z &= 5 \\ x + 3y + 3z &= 9 \\ x + 2y + az &= \beta \end{aligned}$$

$$\begin{array}{l} \alpha = 2 \\ \beta = 7 \end{array}$$

Q21 The following system of equations

$$\begin{aligned} x_1 + x_2 + 2x_3 &= 1 \\ x_1 + 2x_2 + 3x_3 &= 2 \\ x_1 + 4x_2 + ax_3 &= 4 \end{aligned}$$

has a unique solution. The only possible value of a is/are

- (A) 0
- (B) either 0 or 1
- (C) one of 0, 1 and -1
- (D) any real number other than 5

Q22 The solution(s) to the equations

$2x + 3y = 1, x - y = 4, 4x - y = \alpha$, will exist if α is equal to

- (A) -33
- (B) 0
- (C) 9
- (D) $\frac{59}{5}$

Q23 For the following set of simultaneous equations:

$$\begin{aligned} 1.5x - 0.5y &= 2 \\ 4x + 2y + 3z &= 9 \\ 7x + y + 5z &= 10 \end{aligned}$$

- (A) The solution is unique
- (B) Infinite many solutions exist
- (C) The equations are incompatible
- (D) Finite number of multiple solutions exist.

Q24 The condition for consistency of simultaneous equation $AX = B$ where $C = A : B$



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- (A) Rank A = Rank C
 (B) Rank A \neq Rank C
 (C) Rank A = Rank B
 (D) None of these

- Q25** In the system of equation AX = B and A, B = C
 (a) If the rank of A is not equal to rank of C
 (p) consistant with unique solution
 (b) If the rank of A is not equal to rank of C
 (q) Infinite solutions consistant with
 (c) If the rank A = rank of C < No. of unknowns
 (r) have a solution
 (d) The solution of AX = 0 is always
 (s) inconsistant

- (A) a->s,b->p,c->q,d->r
 (B) a->s,b->p,c->q,d->p
 (C) a->s,b->p,c->q,d->q
 (D) a->s,b->p,c->q,d->q



- Q26** The values of k for which equations $x + y + z = 1$, $x + 2y + 4z = k$, $x + 4y + 10z = k^2$ have a solution
 (A) 1 or 2
 (B) 3 or 4
 (C) 5 or 6
 (D) any values

- Q27** For what value of b the following system of equations has non-trivial solution?

$$\begin{aligned} 2x + y + 2z &= 0 \\ x + y + 3z &= 0 \\ 4x + 3y + bz &= 0 \end{aligned}$$



- Q28** Let AX = B be a system of linear equations where A is an $m \times n$ matrix and B is an $n \times 1$ column matrix which of the following is false?
 (A) The system has a solution, if $\rho(A) = r(A/B)$
 (B) If $m = n$ and B is non-zero vector then the system has a unique solution
 (C) If $m < n$ and B is a zero vector then the system has infinitely many solutions
 (D) The system will have a trivial solution when $m = n$, B is the zero vector and rank of A is n.

- Q29** Let A be a square matrix of order n, then nullity of A is
 (A) $n - \text{rank } A$
 (B) $\text{rank } A - n$
 (C) $n + \text{rank } A$

- (D) None of these

- Q30** An $n \times n$ homogenous system of equations AX = 0 is given. The rank of A is $r < n$. Then the system has
 (A) $n - r$ independent solutions
 (B) r independent solutions
 (C) no solution
 (D) $n - 2r$ independent solutions

- Q31** The simultaneous equation

$$a_1x + b_2y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

$$(i) \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} \quad (p)$$

no solution

$$(ii) \frac{a_1}{a_2} \neq \frac{b_1}{b_2} = \frac{c_1}{c_2} \quad (q)$$

unique solution

$$(iii) \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

(r) infinitely many solutions

$$(iv) \frac{a_1}{a_2} \neq \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \quad (s) \text{None}$$

of these

- (A) a->r

b->q

c->p

d->q

- (B) a->p

b->s

c->q

d->r

- (C) a->s

b->p

c->r

d->q

- (D) None of these

- Q32** If $x + 2y - 2u = 0$, $2x - y - u = 0$, $x = 2z - u = 0$, $4x - y + 3z - u = 0$ is a system of equations, then it is
 (A) consistant with trivial solution
 (B) consistant without trivial solution
 (C) inconsistant with trivial solution
 (D) inconsistant without trivial solution



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Q33 The equations $kx + y + z = 0$, $-x + ky + z = 0$, $-x - y + kz = 0$ will have non-zero solution, when real k is

Q34 For the given set of equations:

$$x + y = 1$$

$$y + z = 1$$

$$x + z = 1,$$

Which one of the following statements is correct?

- (A) Equations are inconsistent
 - (B) Equations are consistent and a single non-trivial solution exists
 - (C) Equations are consistent and many solutions
 - (D) Equations are consistent and only a trivial solution exists



Answer Key

- Q1 2
Q2 3
Q3 1
Q4 (C)
Q5 (B)
Q6 (C)
Q7 (A)
Q8 (A)
Q9 The vectors are linearly independent if they cannot be expressed as the linear combination of each others.
Q10 (B)
Q11 (A)
Q12 (B)
Q13 (B)
Q14 v1 and v2 are orthogonal and v2 and v3 are orthogonal.
Q15 (C)
Q16 (A)
Q17 (C, D)

- Q18 9
Q19 $\frac{1}{\sqrt{21}} \begin{bmatrix} 2 \\ 1 \\ -4 \end{bmatrix}$
Q20 $\alpha = 2, \beta = 7$
Q21 (D)
Q22 (D)
Q23 (A)
Q24 (A)
Q25 (A)
Q26 (A)
Q27 8
Q28 (B)
Q29 (A)
Q30 (A)
Q31 (A)
Q32 (A)
Q33 (B)
Q34 (B)



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Hints & Solutions

Q1 Text Solution:

We have, $A = \begin{bmatrix} 4 & 2 & 1 & 3 \\ 6 & 3 & 4 & 7 \\ 2 & 1 & 0 & 1 \end{bmatrix}$

Performing $R_1 \rightarrow R_1 \div 4$

$$A = \begin{bmatrix} 1 & 1/2 & 1/4 & 3/4 \\ 6 & 3 & 4 & 7 \\ 2 & 1 & 0 & 1 \end{bmatrix}$$

Performing $R_2 \rightarrow R_2 - 6R_1$, $R_3 \rightarrow R_3 - 2R_1$

$$\text{and } A = \begin{bmatrix} 1 & 1/2 & 1/4 & 3/4 \\ 0 & 0 & 5/2 & 5/2 \\ 0 & 0 & -1/2 & -1/2 \end{bmatrix}$$

Now, performing $R_2 \rightarrow R_2 \times (\frac{2}{5})$, We get

$$A = \begin{bmatrix} 1 & 1/2 & 1/4 & 3/4 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & -1/2 & -1/2 \end{bmatrix}$$

Performing $R_3 \rightarrow R_3 + \frac{1}{2}R_2$, we get

$$A = \begin{bmatrix} 1 & 1/2 & 1/4 & 3/4 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Hence, number of non-zero rows = 2.

So, rank of given matrix = 2

Q2 Text Solution:

$$A = \begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 4 \end{bmatrix}$$

Rearranging the rows we get –

$$A = \begin{bmatrix} -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 4 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

So the number of non-zero rows is 3

Q3 Text Solution:

$$A = \begin{bmatrix} 1 & 1 & 1 \\ a & a & a \\ a^3 & a^3 & a^3 \end{bmatrix}$$

multiplying R_1 with a and subtracting with R_2 and then multiplying R_1 with a^3 and subtracting with R_3 we get –

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Thus the rank is 1

Q4 Text Solution:

We need to find the rank of the matrix,

$$M = \begin{bmatrix} 1 & 1 & 0 \\ -1 & 1 & 2 \\ 2 & 2 & 0 \\ -1 & 0 & 1 \end{bmatrix}$$

Reduce the matrix to echelon form using the operations

" $R_2 \rightarrow R_2 + R_1$ ", $R_3 \rightarrow R_3 - 2R_1$ and $R_4 \rightarrow R_4 + R_1$.

Thus we get–

$$M = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 2 & 2 \\ 0 & 0 & 0 \\ 0 & 1 & 1 \end{bmatrix}$$



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and also applying $R_4 \rightarrow 2R_4 - R_2$, we have-

$$M = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 2 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

So, rank of M = 2.

Q5 Text Solution:

Rank (PMQ) = Rank M, as P and Q are non singular matrices.

Q6 Text Solution:

So basically, the matrix is of order 4×4 . Now as it is a singular matrix so the rank can never be 4, but if we have to explain for at most number which can be the rank, it will be 3 only.

Q7 Text Solution:

A is any matrix of order $m \times n$ then rank of A $\leq \min\{m, n\}$

rank of A $\leq m$

\therefore rank of A $\leq m$ ($\because m < n$)

Q8 Text Solution:

Given that both rows and columns are equal.

So let us consider $A_{n \times n}$

Also given that $\rho(A)$ = number of rows of A = number of column of A.

So, $\rho(A) = n$

$\Rightarrow |A| \neq 0$

Q9 Text Solution:

The vectors are linearly independent if they cannot be expressed as the linear combination of each others. Thus after making linear combinations and having the system of solutions we have a trivial solution then the vectors will be independent of each other.

Q10 Text Solution:

The vectors are linearly independent if they cannot be expressed as the linear combination of each others. Thus after making linear combinations and having the system of solutions we have a trivial solution then the vectors will be independent of each other.

Q11 Text Solution:

If A is matrix of order $n \times m$ such that A is singular then column vectors are linearly dependent.

As the matrix is singular thus the determinant will be 0, hence the columns are LD.

Q12 Text Solution:

If there exist no relationship between the column vectors of $A_{m \times n}$ then they all are independent of each other thus the rank will be n.

Q13 Text Solution:

So we have 3 vectors as -

$$\hat{i} + 2\hat{j} + 3\hat{k}, 4\hat{i} + 5\hat{j} + 6\hat{k}, \lambda\hat{i} + 8\hat{j} + 9\hat{k}$$

We have to express them as linear combination thus-

$$\alpha(\hat{i} + 2\hat{j} + 3\hat{k}) + \beta(4\hat{i} + 5\hat{j} + 6\hat{k}) = \lambda\hat{i} + 8\hat{j} + 9\hat{k}$$

$$\alpha + 4\beta = \lambda \quad \dots \quad (1)$$

$$2\alpha + 5\beta = 8 \quad \dots \quad (2)$$

$$3\alpha + 6\beta = 9 \quad \dots \quad (3)$$

solving 3 and 4 we get -

$$\alpha = -1, \beta = 2$$

thus putting it in eqn 1 we get

$$\lambda = -1 + 8 = 7$$

Q14 Text Solution:

a) The two vectors are said to be orthogonal if the dot product of two vectors are 0.

Considering the first vector and multiplying the consecutive elements we get-

$$2*1-4*1+2*1=0$$

Thus they are orthogonal.

b) Similarly moving to the next question we get-
 $v_1 \cdot v_2 = -2 * 9 + 6 * 2 + 6 * 1 = 0$, thus
orthogonal

$v_2 \cdot v_3 = 9 * 4 - 15 * 2 - 1 * 6 = 0$, thus
orthogonal



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Q15 Text Solution:

The two vectors X_1 & X_2 are said to be orthogonal if $X_1 \cdot X_2 = 0$

Let $X_1 = [1 \ 0 \ 2]^T$ and $X_2 = [0 \ 5 \ 0]^T$

So, $X_1 \cdot X_2 =$

$$\begin{bmatrix} 1 \\ 0 \\ 2 \end{bmatrix} \cdot \begin{bmatrix} 0 \\ 5 \\ 0 \end{bmatrix} = 1 \times 0 + 0 \times 5 + 2 \times 0 = 0$$

Method II:

For orthogonal vector: $\vec{a} \cdot \vec{b} = 0$

i.e. if $\vec{a} = x_1 i + y_1 j + z_1 k$

& $\vec{b} = x_2 i + y_2 j + z_2 k$

Then: $x_1 x_2 + y_1 y_2 + z_1 z_2 = 0$

Option 'c' satisfies the condition.

Q16 Text Solution:

$$\bar{a} = 3\hat{i} - 2\hat{j} + \hat{k}, \bar{b} = 4\hat{i} + 3\hat{j} - \lambda\hat{k}$$

Here as they are orthogonal thus, the dot product will be 0.

$$\bar{a} \cdot \bar{b} = 12 - 6 - \lambda = 0$$

$$\lambda = 6$$

Q17 Text Solution:

$$A = \begin{bmatrix} 1 & 1 & 0 \\ 1 & -1 & 0 \\ 1 & 0 & 1 \\ 1 & 0 & -1 \end{bmatrix}$$

So we have the column vectors as –
 $(1, 1, 1, 1)^T, (1, -1, 0, 0)^T, (0, 0, 1, -1)^T$

Lets take the option $\begin{pmatrix} c \end{pmatrix}$

If they are orthogonal ; then the dot product will turn out to be 0.

$$\begin{pmatrix} -1, -1, 1, 1 \end{pmatrix} \cdot \begin{pmatrix} 1, 1, 1, 1 \end{pmatrix} = 0$$

$$\begin{pmatrix} -1, -1, 1, 1 \end{pmatrix} \cdot \begin{pmatrix} 1, -1, 0, 0 \end{pmatrix} = 0$$

$$\begin{pmatrix} -1, -1, 1, 1 \end{pmatrix} \cdot \begin{pmatrix} 0, 0, 1, -1 \end{pmatrix} = 0$$

Lets take the option $\begin{pmatrix} d \end{pmatrix}$

$$\begin{pmatrix} 0, 0, 0, 0 \end{pmatrix} \cdot \begin{pmatrix} 1, 1, 1, 1 \end{pmatrix} = 0$$

$$\begin{pmatrix} 0, 0, 0, 0 \end{pmatrix} \cdot \begin{pmatrix} 1, -1, 0, 0 \end{pmatrix} = 0$$

$$\begin{pmatrix} 0, 0, 0, 0 \end{pmatrix} \cdot \begin{pmatrix} 0, 0, 1, -1 \end{pmatrix} = 0$$

Q18 Text Solution:

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Norm is defined as –

lets say we have a vector $x_1 \hat{i} + y_1 \hat{i} + z_1 \hat{i}$

then norm is $= \sqrt{x_1^2 + y_1^2 + z_1^2}$

Thus here –

$$\sqrt{64 + 16 + 1} = \sqrt{81} = 9$$

Q19 Text Solution:

The vector given is $\begin{bmatrix} 2 \\ 1 \\ -4 \end{bmatrix}$

Norm is defined as –

lets say we have a vector $x_1 \hat{i} + y_1 \hat{i} + z_1 \hat{i}$

then norm is $= \sqrt{x_1^2 + y_1^2 + z_1^2}$

Thus here –

$$\sqrt{4 + 1 + 16} = \sqrt{21}$$

Thus the normalised vector will be –

$$\frac{1}{\sqrt{21}} \begin{bmatrix} 2 \\ 1 \\ -4 \end{bmatrix}$$

Q20 Text Solution:

Putting the system of simultaneous equations in the form

$$AX = B$$

We get,

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 3 & 3 \\ 1 & 2 & \alpha \end{bmatrix}, X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, B = \begin{bmatrix} 5 \\ 9 \\ \beta \end{bmatrix}$$

So, the augmented matrix

$$\tilde{A} = [A : B] = \begin{bmatrix} 1 & 1 & 1 & : & 5 \\ 1 & 3 & 3 & : & 9 \\ 1 & 2 & \alpha & : & \beta \end{bmatrix}$$

Operating $R_2 \rightarrow R_2 - R_1$ and $R_3 \rightarrow R_3 - R_1$,

$$\text{We get } \sim \begin{bmatrix} 1 & 1 & 1 & : & 5 \\ 0 & 2 & 2 & : & 4 \\ 0 & 1 & \alpha - 1 & : & \beta - 5 \end{bmatrix}$$

Operating $R_2 \rightarrow R_2 \div 2$, we get

$$\sim \begin{bmatrix} 1 & 1 & 1 & : & 5 \\ 0 & 1 & 1 & : & 2 \\ 0 & 1 & \alpha - 1 & : & \beta - 5 \end{bmatrix}$$

Operating $R_3 \rightarrow R_3 - R_2$, we get

$$\sim \begin{bmatrix} 1 & 1 & 1 & : & 5 \\ 0 & 1 & 1 & : & 2 \\ 0 & 1 & \alpha - 2 & : & \beta - 7 \end{bmatrix}$$

Now, for infinite solution the last row must be zero.

Therefore, $\alpha - 2 = 0$ implies $\alpha = 2$

$\beta - 7 = 0$ implies $\beta = 7$

Q21 Text Solution:

Putting the given linear equations in $AX = B$ form

$$A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 1 & 4 & \alpha \end{bmatrix}, X = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 \\ 2 \\ 4 \end{bmatrix}$$

Now, augmented matrix

$$[A : B] = \begin{bmatrix} 1 & 1 & 2 & : & 1 \\ 1 & 2 & 3 & : & 2 \\ 1 & 4 & \alpha & : & 4 \end{bmatrix}$$

Operation $R_2 \rightarrow R_2 - R_1$ and $R_3 \rightarrow R_3 - R_1$, we get

$$= \begin{bmatrix} 1 & 1 & 2 & : & 1 \\ 0 & 1 & 1 & : & 1 \\ 0 & 3 & \alpha - 2 & : & 3 \end{bmatrix}$$

Operating $R_3 \rightarrow R_3 - 3R_2$, we get

$$= \begin{bmatrix} 1 & 1 & 2 & : & 1 \\ 0 & 1 & 1 & : & 1 \\ 0 & 0 & \alpha - 5 & : & 0 \end{bmatrix}$$

If $\alpha - 5 \neq 0 \Rightarrow \alpha \neq 5$

Then, rank of $[A] = \text{rank of } [A : B] = 3$

Hence, α can take any value except 5

Q22 Text Solution:

$$2x + 3y = 1 \dots \text{(i)}$$

$$x - y = 4 \dots \text{(ii)}$$

$$4x - y = \alpha \dots \text{(iii)}$$

Form equation (i) and equation (ii)

$$x = \frac{13}{5}, y = -\frac{7}{5}$$

The solution of equations exists

$$\Rightarrow \alpha = 4 \left(\frac{13}{5} \right) - \left(-\frac{7}{5} \right)$$

$$\alpha = \frac{59}{5}$$

Q23 Text Solution:

$|A| = \text{Determinant of }$

$$\begin{bmatrix} 1.5 & -0.5 & 0 \\ 4 & 2 & 3 \\ 7 & 1 & 5 \end{bmatrix}$$

$$= (1.5)(10 - 3) + (0.5)(20 - 21)$$



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$$= 10.5 - 0.5 = 10 \neq 0$$

Q24 Text Solution:

We have to find the condition for consistency of simultaneous equation $AX = B$ where $C=A:B$

That C is equal to A augmented B , no in order for the consistency of equations means that the solutions must exist either unique or infinite thus for this the rank of A must be equal to rank of C .

Q25 Text Solution:

- (a) If the rank A rank of C
(r) have a solution
- (c) If the rank $A = \text{rank of } C < \text{No. of unknowns}$
(p) consistent with unique solution
- (c) If the rank $A = \text{rank of } C < \text{No. of unknowns}$
(q) Infinite solutions consistent with
- (d) The solution of $AX = 0$ is always
(r) have a solution

The correct solutions is a->s,b->p,c->q,d->r

Q26 Text Solution:

The values of k for which equations $x + y + z = 1$, $x + 2y + 4z = k$, $x + 4y + 10z = k^2$ have a solution

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 1 & 2 & 4 & k \\ 1 & 4 & 10 & k^2 \end{array} \right]$$

$$R_2 \rightarrow R_2 - R_1$$

$$R_3 \rightarrow R_3 - R_1$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & 1 & 3 & k-1 \\ 0 & 3 & 9 & k^2-1 \end{array} \right]$$

$$R_3 \rightarrow R_3 - 3R_2$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & 1 & 3 & k-1 \\ 0 & 0 & 0 & k^2-1-3k+3 \end{array} \right]$$

$$K^2 - 3K + 2 = 0$$

$$K - 2 = 0, K - 1 = 0$$

$$K = 1, 2$$

Q27 Text Solution:

Since the system of homogeneous equations has non-trivial solution

Hence, $|A| = 0$

$$\Rightarrow \begin{vmatrix} 2 & 1 & 2 \\ 1 & 1 & 3 \\ 4 & 3 & b \end{vmatrix} = 0$$

$$\Rightarrow 2 \begin{vmatrix} 1 & 3 \\ 3 & b \end{vmatrix} - 1 \begin{vmatrix} 1 & 3 \\ 4 & b \end{vmatrix} + 2 \begin{vmatrix} 1 & 1 \\ 4 & 3 \end{vmatrix} = 0$$

$$\Rightarrow 2(b-9) - 1(b-12) + 2(3-4) = 0$$

$$\Rightarrow b - 8 = 0$$

$$\Rightarrow b = 8$$

Q28 Text Solution:

Given, that $A_{m \times n} X_{n \times 1} = B_{m \times 1}$

According to option (b)

We can take $m = n$ & $B = 0$

So (1) $= A_{m \times n} X_{n \times 1} = O_{m \times 1}$

If $|A|$ is not equal to 0, system have unique solution if $|A|=0$ system have infinite solution.

Hence, option (b) is wrong because condition of unique solution is not mentioned.

Q29 Text Solution:

Let A be a square matrix of order n , then nullity of A is

then the nullity is defined as $n-r$,

The nullity of a matrix is **the dimension of the null space of A , also called the kernel of A .**

Q30 Text Solution:

An $n \times n$ homogenous system of equations $AX = 0$ is given. The rank of A is $r < n$. Then the system will have $n-r$ independent solutions

Q31 Text Solution:

a) $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ (r) Infinity many solutions

b) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2} = \frac{c_1}{c_2}$ (q) unique solution

c) $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ (p) No solution

d) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ (s) None of these

The correct solutions will be-

a->r

b->q

c->p

d->q



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Q32 Text Solution:

If $x + 2y - 2u = 0$, $2x - y - u = 0$, $x + 2z - u = 0$, $4x - y + 3z - u = 0$

Thus $AX = O$

$$\begin{bmatrix} 1 & 2 & -2 & 0 \\ 2 & -1 & -1 & 0 \\ 1 & 0 & -1 & 2 \\ 4 & -1 & -1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \\ u \\ z \end{bmatrix} = O$$

If we will calculate the determinant of A its coming out to be non-zero, thus consistent with trivial solution.

Q33 Text Solution:

The equations are $kx + y + z = 0$, $-x + ky + z = 0$, $-x - y + kz = 0$

$$\left[\begin{array}{ccc|c} k & 1 & 1 & 0 \\ -1 & k & 1 & 0 \\ -1 & -1 & k & 0 \end{array} \right]$$

Thus the determinant should be equal to 0

$$\left[\begin{array}{ccc|c} k & 1 & 1 & 0 \\ -1 & k & 1 & 0 \\ -1 & -1 & k & 0 \end{array} \right] = A$$

$$|A| = 0$$

$$k \left(k^2 + 1 \right) - 1 \left(-k + 1 \right) + 1 \left(1 + k \right) \\ = 0$$

$$k^3 + k + k - 1 + 1 + k = 0$$

$$k^3 + 3k = 0$$

$$k = 0$$

Q34 Text Solution:

Lets make the augmented matrix for the system of equations –

$$\left[\begin{array}{ccc|c} 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \end{array} \right]$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \end{array} \right]$$

As the determinant of A is not 0 and thus the rank of A = 3 thus the system of equations will have a unique solution.



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