

CS & IT ENGINEERING



THEORY OF COMPUTATION

Regular Expressions

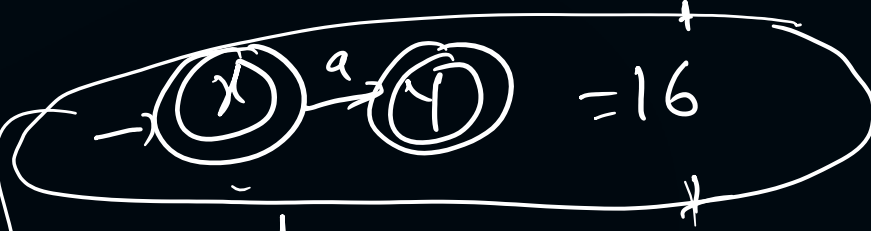
DPP – 02 Discussion Notes



By- Venkat sir

$$(Q, \Sigma, q_0, F, \delta)$$

#Q. The possible number of DFA with 2 states X, Y over the alphabet {a, b} where X is always initial state ?

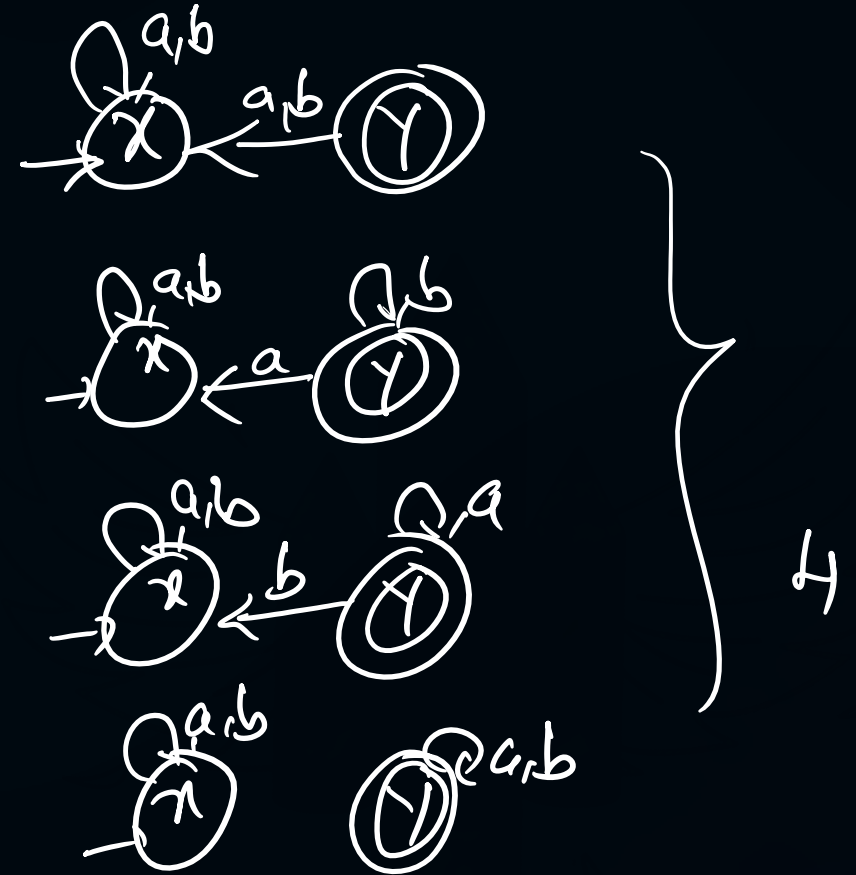
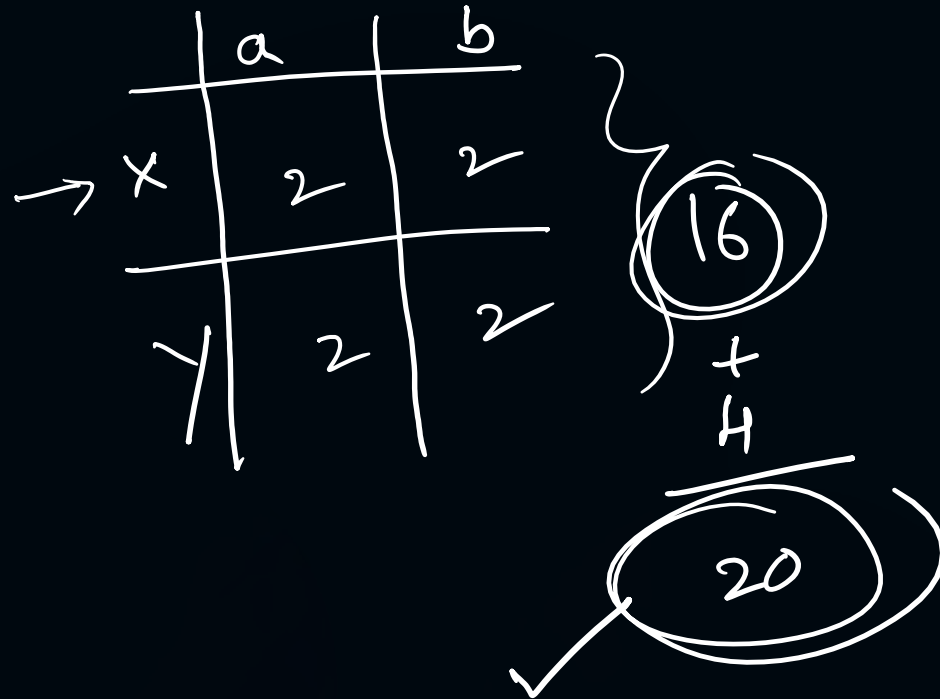


64 ✓

| | a | b |
|---|----|---|
| X | 2 | 2 |
| Y | 2 | 2 |
| | 16 | |

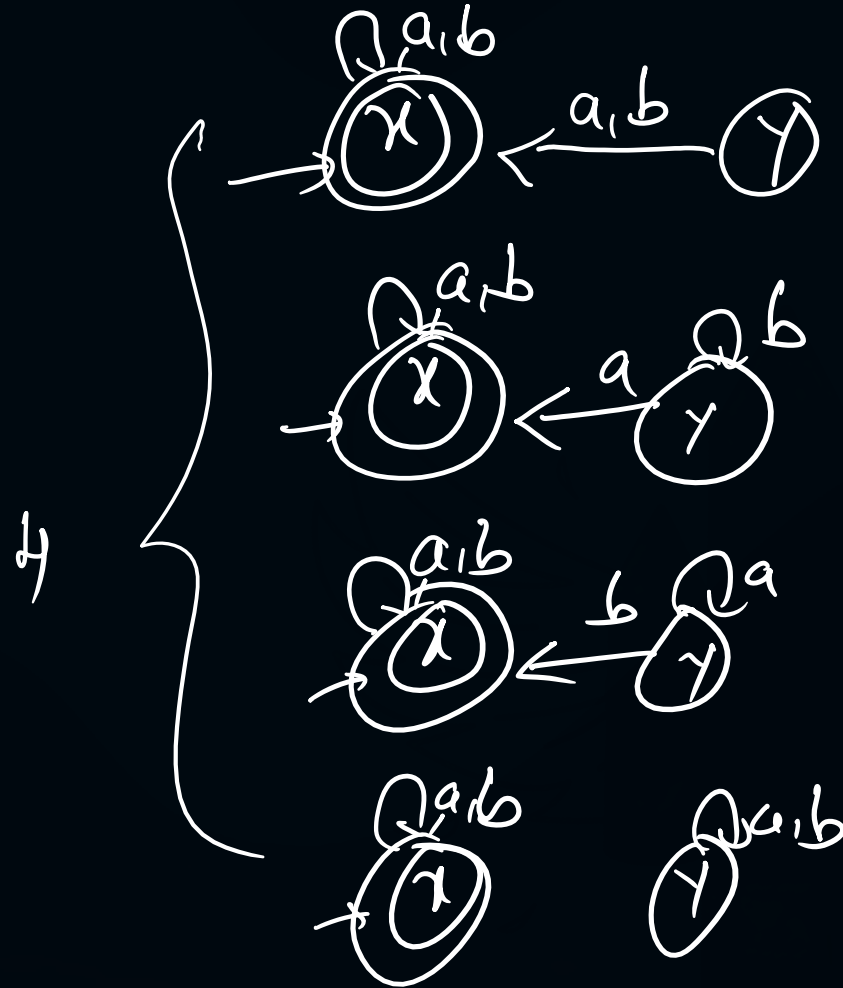
$2^4 = 16$

#Q. The possible number of DFA with 2 states X,Y over the alphabet {a, b} where X is always initial state, that accepts empty language?



#Q. The possible number of DFA with 2 states X,Y over the alphabet {a, b} where X is always initial state, that accepts complete language?

$$\begin{array}{r}
 16 \\
 + 4 \\
 \hline
 20
 \end{array}$$



[MCQ]



Consider the DFA, M with states $Q = \{0, 1, 2, 3, 4\}$, input alphabet $\Sigma = \{0, 1\}$ start state 0, final state 0 and transition function $\delta(q, i) = |q^2 - i| \bmod 5$ $q \in Q$, input alphabets are $\{0, 1\}$ ✓

#Q. The above DFA, M accepts all binary strings containing

A even number of 1's ✓

B odd number of 1's

C even number of 0's

D odd number of 0's

$$s(\underline{0}, \underline{0}) = \underline{10-0} \bmod 5 = 0 \checkmark$$

$$s(\underline{0}, \underline{1}) = \underline{10-1} \bmod 5 = 1 \checkmark$$

$$s(\underline{1}, \underline{0}) = \underline{11-0} \bmod 5 = 1 \checkmark$$

$$s(\underline{1}, \underline{1}) = \underline{(1-1)} \bmod 5 = 0 \checkmark$$

$$s(\underline{2}, \underline{0}) = \underline{14-0} \bmod 5 = 4 \checkmark$$

$$s(\underline{2}, \underline{1}) = \underline{14-1} \bmod 5 = 3 \checkmark$$

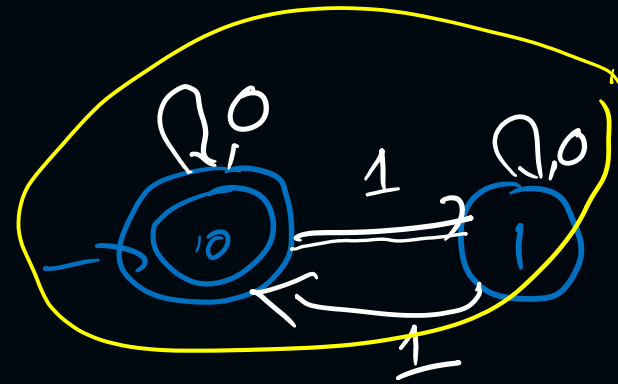
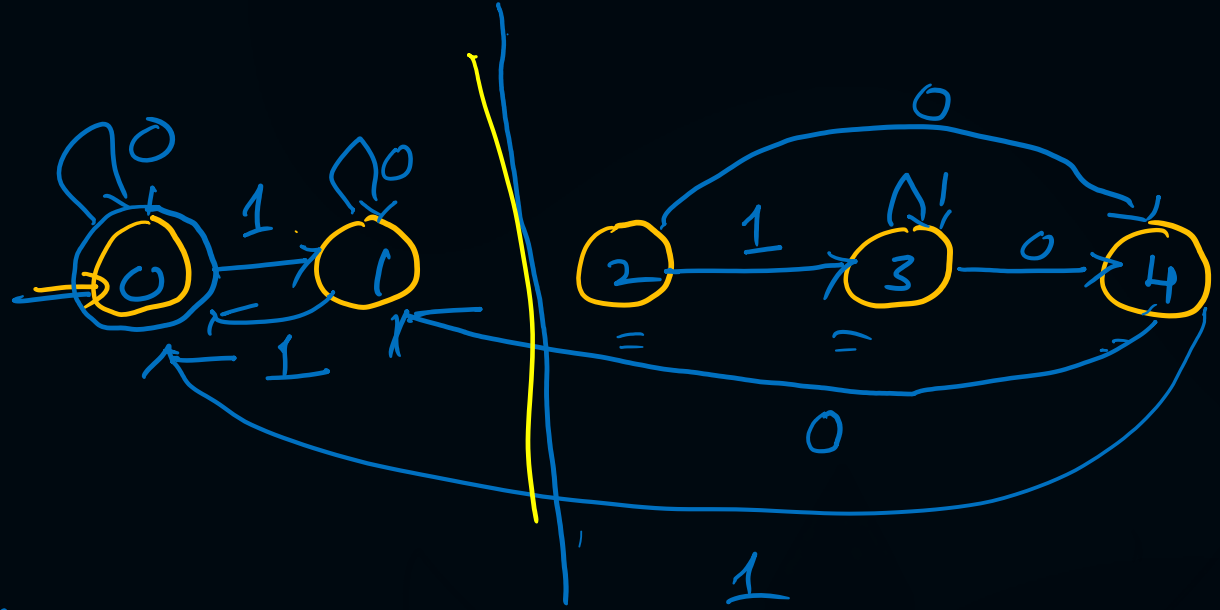
$$s(\underline{3}, \underline{0}) = \underline{19-0} \bmod 5 = 4 \checkmark$$

$$s(\underline{3}, \underline{1}) = \underline{19-1} \bmod 5 = 3 \checkmark$$

$$s(\underline{4}, \underline{0}) = \underline{(16-0)} \bmod 5 = 1 \checkmark$$

$$s(\underline{4}, \underline{1}) = \underline{(16-1)} \bmod 5 = 0 \checkmark$$

$$s(q, i) = 19^q - i \bmod 5$$



[MCQ] Consider the DFA ,M with states $Q=\{0,1,2,3,4\}$, input alphabet $\Sigma = \{0,1\}$ start state 0, final state 0 and transition function $\delta(q,i)=|q^2 - i| \bmod 5$ $q \in Q$, input alphabets are $\{0,1\}$

#Q. The number of states in the minimal finite automata ,which is equivalent to M is

A 1

B 2 ✓

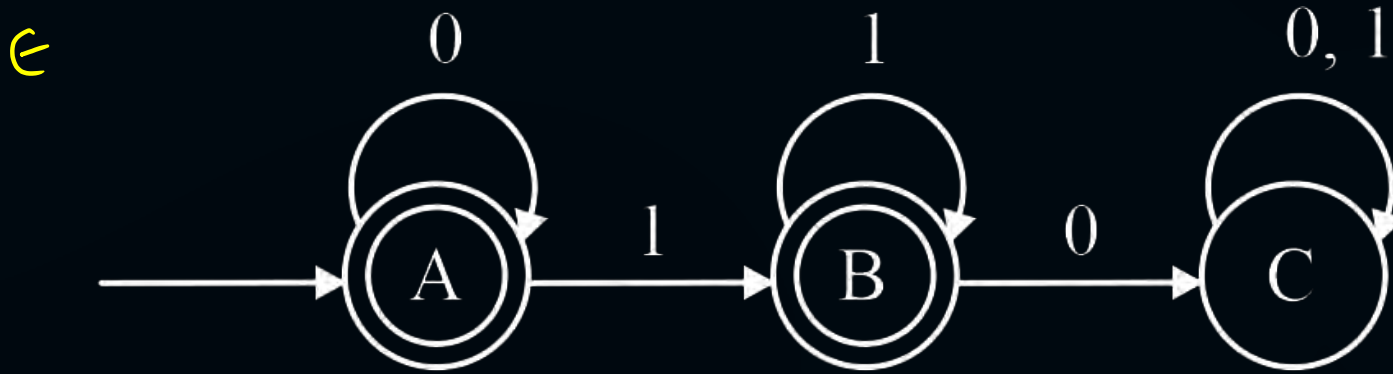
C 3

D 4

[MCQ]



#Q. The regular expression for the language recognized by the following finite automata is?



A $(0 + 1)^*$ ✗

B $0(0 + 1)^*1$ ✗

C 0^*1^* ✓

D $0^*(0 + 1)^*1^*$ ✗

[MCQ]



#Q. Choose the regular language from the following

MOM
Dad

A $L = \{x/x \in (a + b)^*\}$ and is even length palindrome

B $L = \{a^n / n \geq 1\} \rightarrow \text{Regular}$

C $L = \{a^n b^{2n} / n \geq 1\} \rightarrow \text{non Regular}$

D दवदम

[MCQ]



#Q. Which of the following regular expression represents all strings of a's and b's where the length of the string is at most 'n' is

- A** $(a + b)^n$ \rightarrow exactly $\in, 1, 2, \dots, n$
- B** $(a+b)^n(a+b)^*$ \rightarrow at least n
- C** $(a + b + \epsilon)^n$ $\checkmark \rightarrow$ at most n \checkmark
- D** None of the above

[MCQ]



#Q. Which of the following pair of regular expressions are not equal

- A** $(r^*)^*$ and $(r^*)^*$ \rightarrow equal
- B** $(r + \epsilon)^*$ and r^* \rightarrow equal
- C** $(r + \epsilon)^*$ and r^* $= \{\epsilon, r, r^2, r^3\} \rightarrow$ not equal
- D** None of the above

[MCQ]



#Q. Consider the language S^* where S is all strings of a's and b's with odd length. The other description of this language is.

$$S^* = \left[(a+b) \left[(a+b)(a+b) \right]^* \right]^*$$
$$= \left[(a+b) \epsilon \right]^* = (a+b)^*$$

A

All strings of a's and b's

B

All even length strings of a's and b's

C

All odd length strings of a's and b's

D

None of the above

[MCQ]



#Q. Let $r = (1 + 0)^*$, $s = 11^*0$ and $t = 1^*0$ be three regular expressions. Which one of the following is true?

- A** $L(s) \subset L(r)$ and $L(s) \subset L(t)$ ✓
- B** $L(r) \subset L(s)$ and $L(s) \subset L(t)$ ✗
- C** $L(t) \subset L(s)$ and $L(s) \subset L(r)$ ✗
- D** None of the above

$$t = \{0, 10, 110, 1110, \dots\}$$

$$s = \{10, 110, 1110, \dots\}$$



THANK - YOU