algo.fit(the dense vectors of actor nodes) You can get the labels for corresponding actor nodes (algo.labels\_) Create a graph for every cluster(ie., if n\_clusters=3, create 3 graphs) (You can use ego\_graph to create subgraph from the actual graph) compute cost1, cost2 (if n\_cluster=3, cost1=cost1(graph1)+cost1(graph2)+cost1(graph3) # here we are doing summation cost2=cost2(graph1)+cost2(graph2)+cost2(graph3) computer the metric Cost = Cost1\*Cost2 return number\_of\_clusters which have maximum Cost #!pip install networkx==2.3 #!pip install stellargraph %matplotlib inline import networkx as nx from networkx.algorithms import bipartite import matplotlib.pyplot as plt from sklearn.cluster import KMeans import numpy as np import warnings warnings.filterwarnings("ignore") import pandas as pd # you need to have tensorflow from stellargraph.data import UniformRandomMetaPathWalk from stellargraph import StellarGraph #data=pd.read\_csv('movie\_actor\_network.csv', index\_col=False, names=['movie', 'actor']) In [100... For Google Colab In [101... from google.colab import drive drive.mount('/content/drive') Drive already mounted at /content/drive; to attempt to forcibly remount, call drive.mount("/content/drive", force\_remount=True). data=pd.read\_csv('/content/drive/MyDrive/14 Clustering on Graph Dataset/movie\_actor\_network.csv', index\_col=False, names=['movie', 'actor']) In [102... In [103... edges = [tuple(x) for x in data.values.tolist()] B = nx.Graph()In [104... B.add\_nodes\_from(data['movie'].unique(), bipartite=0, label='movie') B.add\_nodes\_from(data['actor'].unique(), bipartite=1, label='actor') B.add\_edges\_from(edges, label='acted') A = list(nx.connected\_component\_subgraphs(B))[0] In [105...  $\#A = (B.subgraph(c) for c in nx.connected\_components(B))$ #A = list(A)[0]print("number of nodes", A.number\_of\_nodes()) In [107... print("number of edges", A.number\_of\_edges()) number of nodes 4703 number of edges 9650 1, r = nx.bipartite.sets(A) $pos = \{\}$ pos.update((node, (1, index)) for index, node in enumerate(1)) pos.update((node, (2, index)) for index, node in enumerate(r)) nx.draw(A, pos=pos, with\_labels=True) plt.show() movies = [] In [109... actors = [] for i in A.nodes(): if 'm' in i: movies.append(i) if 'a' in i: actors.append(i) print('number of movies ', len(movies)) print('number of actors ', len(actors)) number of movies 1292 number of actors 3411 # Create the random walker In [110... rw = UniformRandomMetaPathWalk(StellarGraph(A)) # specify the metapath schemas as a list of lists of node types. metapaths = [ ["movie", "actor", "movie"], ["actor", "movie", "actor"] walks = rw.run(nodes=list(A.nodes()), # root nodes length=100, # maximum length of a random walk # number of random walks per root node metapaths=metapaths print("Number of random walks: {}".format(len(walks))) Number of random walks: 4703 from gensim.models import Word2Vec In [111... model = Word2Vec(walks, size=128, window=5) model.wv.vectors.shape # 128-dimensional vector for each node in the graph In [112.. Out[112... (4703, 128) In [113... # Retrieve node embeddings and corresponding subjects node\_ids = model.wv.index2word # list of node IDs node\_embeddings = model.wv.vectors # numpy.ndarray of size number of nodes times embeddings dimensionality node\_targets = [ A.node[node\_id]['label'] for node\_id in node\_ids] print(node\_ids[:15], end='') ['a973', 'a967', 'a964', 'a1731', 'a969', 'a970', 'a1028', 'a1057', 'a965', 'a1003', 'm1094', 'a966', 'm67', 'a988', 'm1111'] print(node\_targets[:15],end='') ['actor', 'actor', 'actor', 'actor', 'actor', 'actor', 'actor', 'actor', 'actor', 'movie', 'actor', 'movie', 'actor', 'movie'] def data\_split(node\_ids, node\_targets, node\_embeddings): In [114... '''In this function, we will split the node embeddings into actor\_embeddings , movie\_embeddings ''' actor\_nodes, movie\_nodes=[],[] actor\_embeddings, movie\_embeddings=[],[] # split the node\_embeddings into actor\_embeddings, movie\_embeddings based on node\_ids # By using node\_embedding and node\_targets, we can extract actor\_embedding and movie embedding # By using node\_ids and node\_targets, we can extract actor\_nodes and movie nodes actor\_nodes, movie\_nodes=[],[] actor\_embeddings, movie\_embeddings=[],[] actor\_target, movie\_target = [], [] for i in range(len(node\_targets)): if node\_targets[i] == 'actor': actor\_nodes.append(node\_ids[i]) actor\_embeddings.append(node\_embeddings[i]) actor\_target.append(node\_targets[i]) movie\_nodes.append(node\_ids[i]) movie\_embeddings.append(node\_embeddings[i]) movie\_target.append(node\_targets[i]) return actor\_nodes, movie\_nodes, actor\_embeddings, movie\_embeddings actor\_nodes, movie\_nodes, actor\_embeddings, movie\_embeddings = data\_split(node\_ids, node\_targets, node\_embeddings) Grader function - 1 def grader\_actors(data): In [116... assert(len(data)==3411) return True grader\_actors(actor\_nodes) Out[116... True Grader function - 2 def grader\_movies(data): assert(len(data)==1292) return True grader\_movies(movie\_nodes) Out[117... True Calculating cost1 (number of nodes in the largest connected component in the graph with the actor nodes and its movie neighbours in cluster i) where N= number of clusters  $Cost1 = \frac{1}{N} \sum_{\text{each cluster i}}$ (total number of nodes in that cluster i) import operator as op In [118... def cost1(graded\_graph,k): actor\_node\_list = [i for i in graded\_graph.node if 'a' in i] total\_nodes\_in\_cluster = len(set(list(graded\_graph.nodes()))) nodewise\_connected\_ele = [] for i in actor\_node\_list: selected\_node\_graph = nx.ego\_graph(graded\_graph, i) #print(selected\_node\_graph.nodes()) connected\_nodes = len(selected\_node\_graph.nodes()) nodewise\_connected\_ele.append(len(selected\_node\_graph.nodes())) nodewise\_connected\_ele #Now select node with max xonnected components #print(dict(zip(actor\_node\_list, nodewise\_connected\_ele))) cluster\_cost1 = op.truediv(max(nodewise\_connected\_ele),(total\_nodes\_in\_cluster)) cluster\_cost1 = op.truediv(cluster\_cost1 , k) return cluster\_cost1 import networkx as nx from networkx.algorithms import bipartite graded\_graph= nx.Graph() graded\_graph.add\_nodes\_from(['a1', 'a5', 'a10', 'a11'], bipartite=0) # Add the node attribute "bipartite" graded\_graph.add\_nodes\_from(['m1', 'm2', 'm4', 'm6', 'm5', 'm8'], bipartite=1) graded\_graph.add\_edges\_from([('a1', 'm1'), ('a1', 'm2'), ('a1', 'm4'), ('a11', 'm6'), ('a5', 'm5'), ('a10', 'm8')]) l={'a1', 'a5', 'a10', 'a11'};r={'m1', 'm2', 'm4', 'm6', 'm5', 'm8'} pos.update((node, (1, index)) for index, node in enumerate(1)) pos.update((node, (2, index)) for index, node in enumerate(r)) nx.draw\_networkx(graded\_graph, pos=pos, with\_labels=True, node\_color='lightblue', alpha=0.8, style='dotted', node\_size=500) m8 al a11 m6 a10 m1 a5 m2 Grader function - 3 graded\_cost1=cost1(graded\_graph, 3) def grader\_cost1(data): assert(data = ((1/3)\*(4/10))) # 1/3 is number of clustersreturn True grader\_cost1(graded\_cost1) Out[120... True Calculating cost2 In [121... def cost2(graded\_graph, k): '''In this function, we will calculate cost1''' #Select all the actor nodes from the actor data actor\_node\_list = [a for a in graded\_graph.node if 'a' in a] #create Empty Graph cluster\_graph=nx.Graph() #For each node in actor nodes, create ego graph and add node+edge info to cluster graph for i in actor\_node\_list: selected\_node\_graph = nx.ego\_graph(graded\_graph, i) cluster\_graph.add\_nodes\_from(selected\_node\_graph.nodes()) cluster\_graph.add\_edges\_from(selected\_node\_graph.edges()) #nx.draw(cluster\_graph, with\_labels = True) actor\_node\_list = [a for a in cluster\_graph.node if 'a' in a] #print(actor\_node\_list) movie\_node\_list = [m for m in cluster\_graph.node if 'm' in m] #print(movie\_node\_list) cluster\_cost2 = op.truediv(len(list(cluster\_graph.edges)),len(movie\_node\_list)) cluster\_cost2 = op.truediv(cluster\_cost2 , k) return cluster\_cost2 Grader function - 4 In [122... graded\_cost2=cost2(graded\_graph, 3) def grader\_cost2(data): assert(data==((1/3)\*(6/6))) # 1/3 is number of clustersreturn True grader\_cost2(graded\_cost2) Out[122... True Grouping similar actors from tqdm import tqdm In [123...  $k_{list} = [3, 5, 10, 30, 50, 100, 200, 500]$ final\_cost\_list = [] #Selecting each value of k for k in tqdm(k\_list): K\_means = KMeans(n\_clusters=k, random\_state=1, n\_jobs=-1) K\_means.fit(actor\_embeddings) actor\_df = pd.DataFrame(data=[actor\_nodes] ) actor\_df = pd.DataFrame(actor\_df.T) actor\_df['actor\_embeddings'] = actor\_embeddings actor\_df['cluster\_no'] = list(K\_means.labels\_) actor\_df.columns = ['actor\_nodes', 'actor\_embeddings', 'cluster\_no'] #HERE need to select all clusters one-by-one cluster\_names = [] for i in range(k): cluster\_names.append(str('cluster\_')+str(i)) #cluster\_names clusters\_list = [] for i in range(k): cluster\_names[i] = pd.DataFrame(actor\_df.cluster\_no==i]) clusters\_list.append(cluster\_names[i]) #select each cluster for all k for selected\_cluster in clusters\_list: cost1\_list, cost2\_list = [],[] #create Empty Graph selected\_cluster\_graph=nx.Graph() actor\_node\_list = list(selected\_cluster.actor\_nodes) #For each node in actor nodes, create ego graph and add node+edge info to cluster graph for i in actor\_node\_list: selected\_node\_graph = nx.ego\_graph(A, i) selected\_cluster\_graph.add\_nodes\_from(selected\_node\_graph.nodes()) selected\_cluster\_graph.add\_edges\_from(selected\_node\_graph.edges()) **#Visualizing Graph** #nx.draw(selected\_cluster\_graph, with\_labels=True) selected\_cluster\_cost1 = cost1(selected\_cluster\_graph, k) cost1\_list.append(selected\_cluster\_cost1) selected\_cluster\_cost2 = cost2(selected\_cluster\_graph, k) cost2\_list.append(selected\_cluster\_cost2) final\_cost = sum(cost1\_list) \* sum(cost2\_list) final\_cost\_list.append(final\_cost) k\_cost = (dict(zip(k\_list, final\_cost\_list))) best\_k = k\_list[final\_cost\_list.index(max(final\_cost\_list))] print("k = {0} gives max cost i.e. {1} ".format(best\_k, max(final\_cost\_list))) print(k\_cost) print("Best Value of k :", best\_k) 100%| 8/8 [00:41<00:00, 5.13s/it] k = 3 gives max cost i.e. 0.0935115093996007 {3: 0.0935115093996007, 5: 0.009967576515859552, 10: 0.015126085543119864, 30: 0.0005366789347756835, 50: 0.0004, 100: 0.0001, 200: 2.5e-05, 500: 2.6538461538 46154e-06} Best Value of k : 3Now train model with best K. K\_means = KMeans(n\_clusters=best\_k, random\_state=1, n\_jobs=-1) In [124... K\_means.fit(actor\_embeddings) actor\_df = pd.DataFrame(data=[actor\_nodes] ) actor\_df = pd.DataFrame(actor\_df.T) #actor\_df['actor\_embeddings'] = actor\_embeddings actor\_df['cluster\_no'] = list(K\_means.labels\_) actor\_df.columns = ['actor\_nodes', 'cluster\_no'] actor\_df Out[124... actor\_nodes cluster\_no 0 a973 2 a967 a964 2

> a1731 a970

> a1990

a1624

a2152

a1263

a2023

Displaying similar actor clusters

transform = TSNE #PCA

trial.columns = ['x', 'y']

X

o -59.311085 15.375273
1 -58.056496 21.319038
2 -59.733837 15.557880
3 0.578625 64.590424
4 -59.396622 17.393166

**3406** -22.048473 -3.789406

**3408** -22.616083 -3.582985

**3410** -12.539353 1.889613

3411 rows × 3 columns

3407

3409

60

40

-60

In [128...

In [128..

In [129...

-7.183355 25.884834

-7.055651 28.220812

trial.plot.scatter(x='x',

from sklearn.manifold import TSNE

trans = transform(n\_components=2)

3411 rows × 2 columns

4

3406

3407

3408

3409

3410

In [125...

In [126...

Out[126...

2

1

1

1

Now the task is to display each cluster with different color.

trial = pd.DataFrame(actor\_embeddings\_2d)

trial['cluster\_no'] = list(K\_means.labels\_)

y cluster\_no

actor\_embeddings\_2d = trans.fit\_transform(actor\_embeddings)

1

c='cluster\_no',
colormap='Accent\_r')

actor\_embeddings\_3d = trans.fit\_transform(actor\_embeddings)

K\_means = KMeans(n\_clusters=k, random\_state=1, n\_jobs=-1)

movie\_df.columns = ['movie\_nodes', 'movie\_embeddings', 'cluster\_no']

cluster\_names[i] = pd.DataFrame(movie\_df[movie\_df.cluster\_no==i])

selected\_cluster\_graph.add\_nodes\_from(selected\_node\_graph.nodes())
selected\_cluster\_graph.add\_edges\_from(selected\_node\_graph.edges())

print("k = {0} gives max cost i.e. {1} ".format(best\_k, max(final\_cost\_list)))

#For each node in actor nodes, create ego graph and add node+edge info to cluster graph

1.75

1.50

1.25

1.00 b

0.75

0.50

0.25

"trans = transform(n\_components=3)\nactor\_embeddings\_3d = trans.fit\_transform(actor\_embeddings)\n\ntrial\_3D = pd.DataFrame(actor\_embeddings\_3d)\ntrial\_3D.colu mns = ['D1', 'D2', 'D3']\ntrial\_3D['cluster\_no'] = list(K\_means.labels\_)\n\nfrom google.colab import files\ntrial\_3D.to\_csv('actors\_3D.csv') \nfiles.downloa

 $\{3:\ 0.045617869313972444,\ 5:\ 0.0437973116192195,\ 10:\ 0.001646831028749848,\ 30:\ 0.0014784205693296603,\ 50:\ 0.0007854545454545455,\ 100:\ 0.00019,\ 200:\ 4.61538461\}$ 

Out[127... <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb38c52d90>

#Generating dataset for 3D Scatter Plot

trial\_3D = pd.DataFrame(actor\_embeddings\_3d)

k\_list = [3, 5, 10, 30, 50, 100, 200, 500]

movie\_df = pd.DataFrame(data=[movie\_nodes] )

#HERE need to select all clusters one-by-one

clusters\_list.append(cluster\_names[i])

for selected\_cluster in clusters\_list:
 cost1\_list, cost2\_list = [],[]

selected\_cluster\_graph=nx.Graph()

#select each cluster for all k

for i in actor\_node\_list:

#create Empty Graph

**#Visualizing Graph** 

print(k\_cost)

Best Value of k:3

movie\_df

0

2

4

1287

1288

1289

1290 1291

trial

1287

1288

1289

1290 1291

30

20

10

-10

-20

-30

In [130...

Out[130...

In [131...

In [132...

Out[132...

In [133.

In [134...

Out[134...

cluster\_names.append(str('cluster\_')+str(i))

actor\_node\_list = list(selected\_cluster.movie\_nodes)

#nx.draw(selected\_cluster\_graph, with\_labels=True)

selected\_cluster\_cost1 = cost1(selected\_cluster\_graph, k)

selected\_cluster\_cost2 = cost2(selected\_cluster\_graph, k)

best\_k = k\_list[final\_cost\_list.index(max(final\_cost\_list))]

K\_means = KMeans(n\_clusters=best\_k, random\_state=1, n\_jobs=-1)

selected\_node\_graph = nx.ego\_graph(A, i)

cost1\_list.append(selected\_cluster\_cost1)

cost2\_list.append(selected\_cluster\_cost2)

final\_cost = sum(cost1\_list) \* sum(cost2\_list)

k\_cost = (dict(zip(k\_list, final\_cost\_list)))

100%| 8/8 [00:22<00:00, 2.84s/it] k = 3 gives max cost i.e. 0.045617869313972444

movie\_df = pd.DataFrame(data=[movie\_nodes] )

#movie\_df['movie\_embeddings'] = movie\_embeddings
movie\_df['cluster\_no'] = list(K\_means.labels\_)
movie\_df.columns = ['movie\_nodes', 'cluster\_no']

5384615e-05, 500: 7.384615384615385e-06}

final\_cost\_list.append(final\_cost)

print("Best Value of k :", best\_k)

K\_means.fit(movie\_embeddings)

movie\_nodes cluster\_no

m1094 m1111

m1100

m67

m48

m33

m251 m1371

m541

transform = TSNE #PCA

trial.columns = ['x', 'y']

**0** -11.821812 32.679317

**1** -27.674002 17.675865 **2** -10.882120 28.317831

3 -20.846407 22.1082484 -11.287133 29.356508

-7.151497 -2.217743

-3.274102 -0.734553

-5.543108 -1.544203

-4.023222 0.307190

Displaying similar movie clusters

trial.plot.scatter(x='x',

2.189119

-8.996601

1292 rows × 3 columns

from sklearn.manifold import TSNE

trans = transform(n\_components=2)

trial = pd.DataFrame(movie\_embeddings\_2d)

trial['cluster\_no'] = list(K\_means.labels\_)

y cluster\_no

1292 rows × 2 columns

1

movie\_embeddings\_2d = trans.fit\_transform(movie\_embeddings)

0

0

1

1

c='cluster\_no',
colormap='Accent\_r')

movie\_embeddings\_3d = trans.fit\_transform(movie\_embeddings)

2.00

1.75

1.50

-1.00 apsilon -0.75

0.50

0.25

"trans = transform(n\_components=3)\nmovie\_embeddings\_3d = trans.fit\_transform(movie\_embeddings)\n\nmovie\_3D = pd.DataFrame(movie\_embeddings\_3d)\nmovie\_3D.colu

mns = ['D1', 'D2', 'D3']\nmovie\_3D['cluster\_no'] = list(K\_means.labels\_)\n\nmovie\_3D.to\_csv('movie\_3D.csv')\nfiles.download('movie\_3D.csv')"

Out[133... <matplotlib.axes.\_subplots.AxesSubplot at 0x7fdb3a6e9cd0>

#Generating dataset for 3D Scatter Plot

movie\_3D = pd.DataFrame(movie\_embeddings\_3d)

movie\_3D['cluster\_no'] = list(K\_means.labels\_)

'''trans = transform(n\_components=3)

movie\_3D.columns = ['D1', 'D2', 'D3']

movie\_3D.to\_csv('movie\_3D.csv')
files.download('movie\_3D.csv')'''

m1095

movie\_df = pd.DataFrame(movie\_df.T)

movie\_df['movie\_embeddings'] = movie\_embeddings
movie\_df['cluster\_no'] = list(K\_means.labels\_)

trial\_3D['cluster\_no'] = list(K\_means.labels\_)

'''trans = transform(n\_components=3)

trial\_3D.columns = ['D1', 'D2', 'D3']

from google.colab import files
trial\_3D.to\_csv('actors\_3D.csv')
files.download('actors\_3D.csv')'''

d('actors\_3D.csv')"

Grouping similar movies

from tqdm import tqdm

final\_cost\_list = []

cluster\_names = []
for i in range(k):

clusters\_list = []
for i in range(k):

#cluster\_names

#Selecting each value of k
for k in tqdm(k\_list):

K\_means.fit(movie\_embeddings)

movie\_df = pd.DataFrame(movie\_df.T)

**Clustering Assignment** 

**Every Grader function has to return True.** 

For this task consider only the actor nodes
 Apply any clustering algorithm of your choice

4. Cost1 =  $\frac{1}{N} \sum_{\text{each cluster i}}$ 

(Write your code in def cost1())

(Write your code in def cost2())

1. For this task consider only the movie nodes

(Write your code in def cost1())

(Write your code in def cost2())

Algorithm for actor nodes

Refer: https://scikit-learn.org/stable/modules/clustering.html

Please check clustering assignment helper functions notebook before attempting this assignment.

Split the dense representation into actor nodes, movies nodes.(Write you code in def data split())

Task 1: Apply clustering algorithm to group similar actors

6. Fit the clustering algorithm with the opimal number of clusters and get the cluster number for each node

for number\_of\_clusters in [3, 5, 10, 30, 50, 100, 200, 500]:
 algo = clustering\_algorith(clusters=number\_of\_clusters)

Task 2: Apply clustering algorithm to group similar movies

• Read graph from the given movie\_actor\_network.csv (note that the graph is bipartite graph.)

3. Choose the number of clusters for which you have maximum score of Cost1\*Cost2

There will be some functions that start with the word "grader" ex: grader\_actors(), grader\_movies(), grader\_cost1() etc, you should not change those function definition.

Using stellergaph and gensim packages, get the dense representation(128dimensional vector) of every node in the graph. [Refer Clustering Assignment Reference.ipynb]

(total number of nodes in that cluster i)

 $Cost1 = \frac{1}{N} \sum_{each \ cluster \ i} \frac{\text{(number of nodes in the largest connected component in the graph with the movie nodes and its actor neighbours in cluster \ i)}{\text{(total number of nodes in that cluster \ i)}} \text{ where N= number of clusters}$ 

# you will be passing a matrix of size N\*d where N number of actor nodes and d is dimension from gensim

5. Cost2 =  $\frac{1}{N} \sum_{\text{each cluster i}} \frac{\text{(sum of degress of actor nodes in the graph with the actor nodes and its movie neighbours in cluster i)}{\text{(number of unique movie nodes in the graph with the actor nodes and its movie neighbours in cluster i)}}$  where N= number of clusters

7. Convert the d-dimensional dense vectors of nodes into 2-dimensional using dimensionality reduction techniques (preferably TSNE) 8. Plot the 2d scatter plot, with the node vectors after step e and give colors to nodes such that same cluster nodes will have same color

2. Apply any clustering algorithm of your choice 3. Choose the number of clusters for which you have maximum score of Cost1\*Cost2

3. Cost2 =  $\frac{1}{N}$   $\sum_{\text{each cluster i}} \frac{\text{(sum of degress of movie nodes in the graph with the movie nodes and its actor neighbours in cluster i)}{\text{(number of unique actor nodes in the graph with the movie nodes and its actor neighbours in cluster i)}}$ 

(number of nodes in the largest connected component in the graph with the actor nodes and its movie neighbours in cluster i)

Where N= number of clusters