

Step 1: → calculating the Reactions

$$\sum F_y = 0 \quad (\uparrow +ve)$$

$$\Rightarrow Ay + Dy - 10 = 0 \quad \text{--- (1)}$$

$$\sum F_x = 0 \quad (\rightarrow +ve)$$

$$-Ax + 25 = 0$$

$$\Rightarrow Ax = 25 \text{ kN}$$

$$\sum M_A = 0 \quad (\text{clockwise} +ve)$$

$$\Rightarrow 25 \times 2.5 + 10 \times 2 - Dy \times 4 = 0$$

$$\Rightarrow 4Dy = 62.5 + 20$$

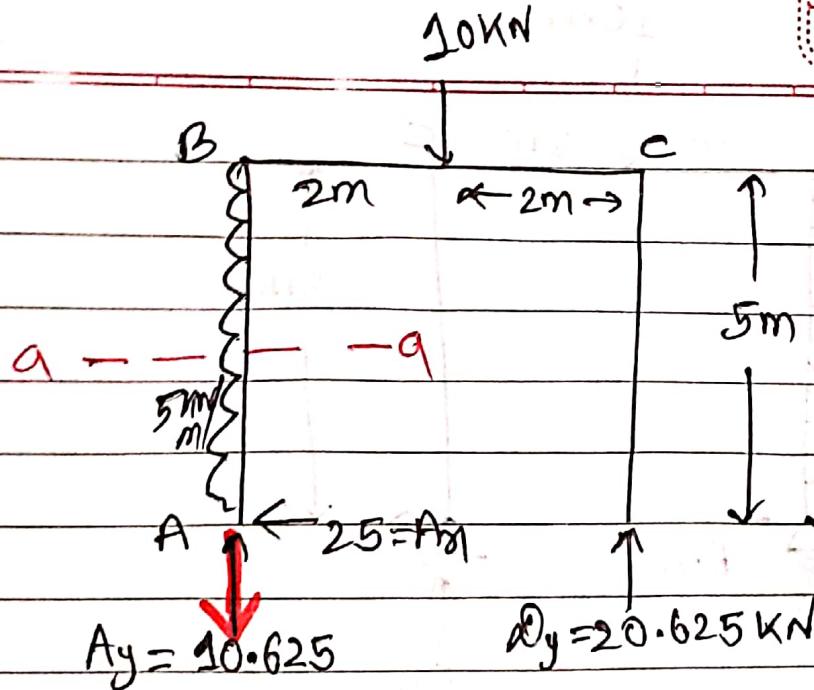
$$\Rightarrow Dy = 20.625 \text{ kN}$$

From eqn (1)

$$\Rightarrow Ay + 20.625 - 10 = 0$$

$$\Rightarrow Ay = -10.625 \text{ kN}$$

-ve sign represents that our assumed direction is not correct and now we have to change it.



Step 2:- Analysing Shear force and Bending moment of given frame.

For this isolate each member and find shear force, Bending moment, Axial force separately.

Note

For UDL

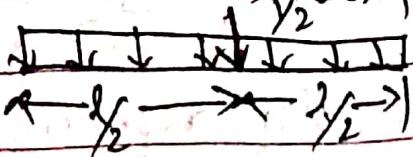
$R = \frac{w_0}{2} l$

Reaction of loading

intensity is given by

$\leftarrow l \text{ cm} \rightarrow$ the area under the

loading diagram, i.e. $R = \frac{1}{2} w_0 \times l$ and passes through CG of that rectangle
(i.e. $\frac{l}{2}$ mm from each end)



continued, Step 2

Century

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For member (AB) \rightarrow passing section a-a such that
 $(0 \leq x \leq 5m)$

(a) $V_n \rightarrow$ represent the shear force equation

and $M_n \rightarrow$ represent the bending moment equation.

$$V_n = 25 - 5x$$

~~$V_n = 25 - 5x$~~

$$@ x=0 \rightarrow V_A = 25 \text{ kN}$$

$$@ x=5, V_{B,L} = 0 \text{ kN}$$

\Rightarrow while moving beam left to right \rightarrow clockwise (+ve)

$$M_n = 25x - 5x^2 \times \frac{x}{2} = 25x - 2.5x^2$$

$$@ x=0 \rightarrow M_A = 0$$

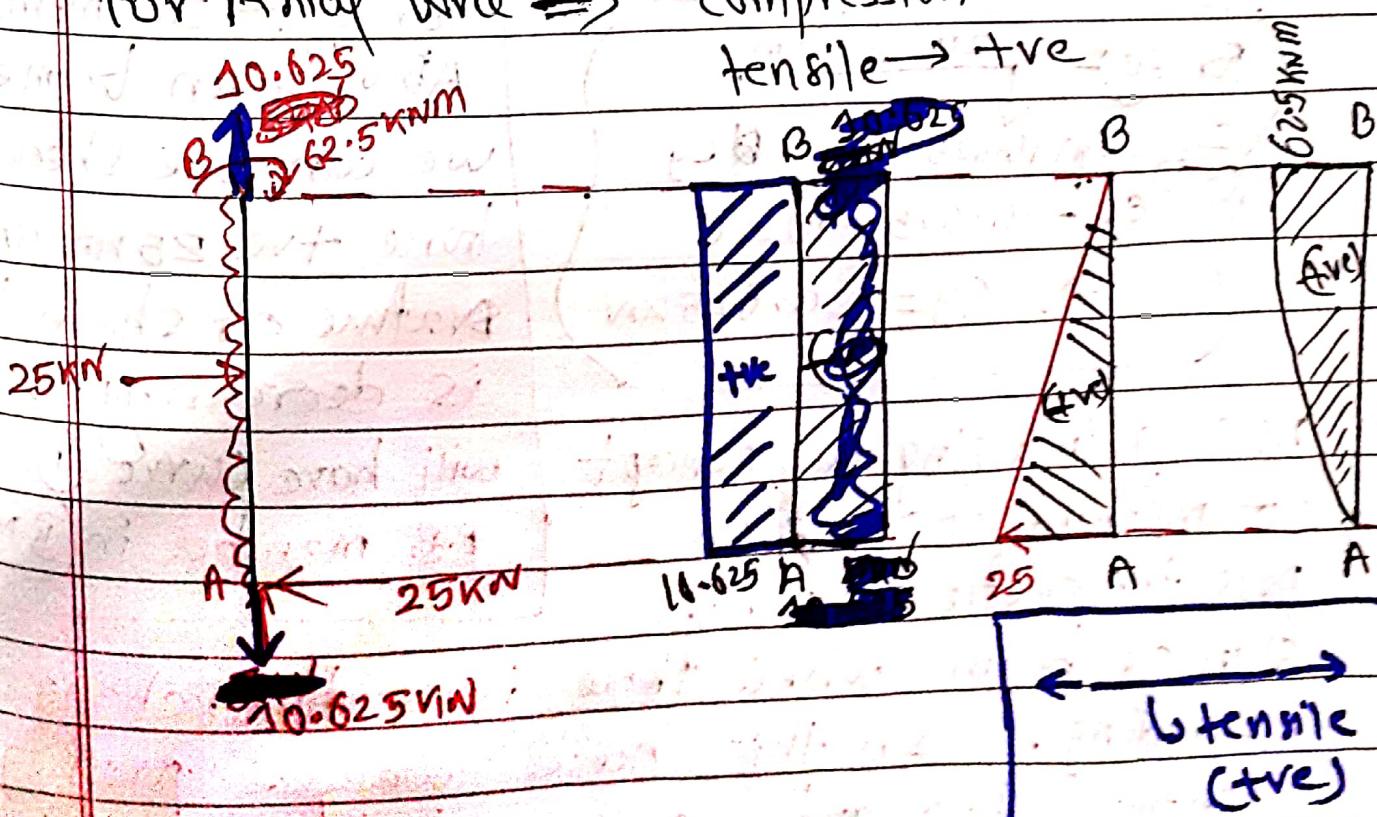
$$\Rightarrow M_n = 25x - 2.5x^2$$

$$@ x=5 \rightarrow M_{B,L} = 125 - 62.5$$

$$\Rightarrow M_{B,L} = 62.5 \text{ kNm}$$

For Axial force \Rightarrow compression \rightarrow -ve

tension \rightarrow +ve



Member BC (Balance the member BC by seeing the force in)

$$10 \text{ kN} \quad 2m \quad 2m \quad C \leftarrow \quad 10.625 \quad (10 + 10.625 = 20.625).$$

Balance the forces at joint C in member (AB) by simply providing the force (vertical) required to make it in equilibrium or simply consider member BC as beam and bind the reaction at C.

For eg:-

$$\sum F_y = 0 \quad 10.625 + C_y - 10 - 10 = 0$$

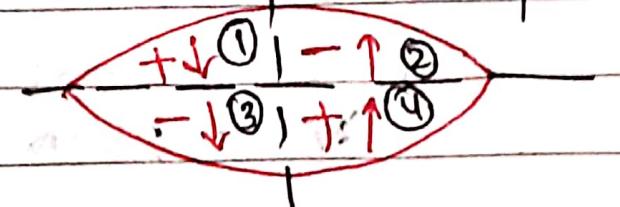
$$\Rightarrow C_y = 20.625 \text{ kN}$$

NOW again using the concept of method of section

pass the section along the

span of beam where there is sudden change in loading. In this case we are passing section b-b and c-c and formulating the Shear Force and Bending moment equation in term of x.

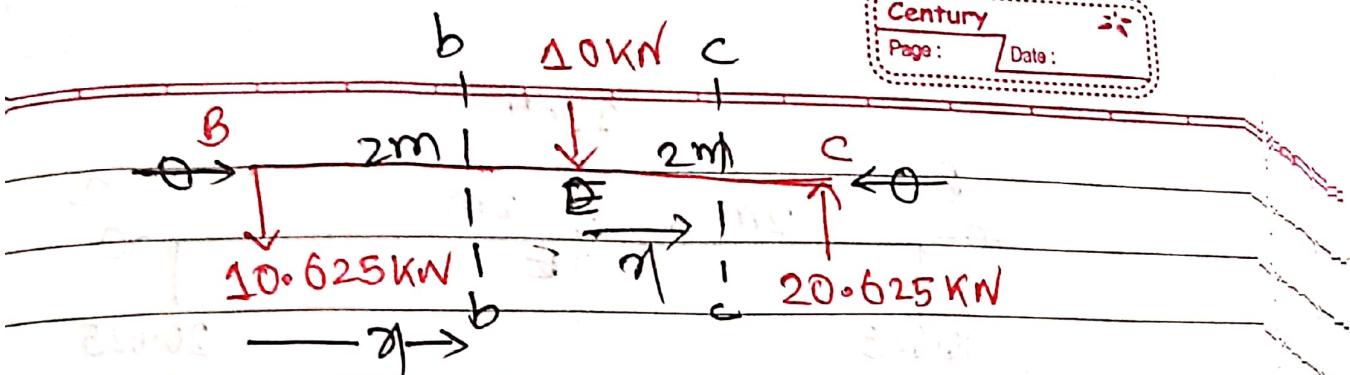
Trick: (Always see the shear Force diagram to draw curve for SFD/MFD)



+ \Rightarrow Represents the value of shear force.

For $\downarrow \Rightarrow$ increasing or decreasing represents the nature of shear force diagram.

For eg:- In member AB of given frame we can see shear force +ve 25kN and nature of shear force is decreasing, so we will have curve ① in AB member in (BMD)



For span $B\bar{D}E$ ($0 \leq x \leq 2m$)

$$\text{At } x=0 \rightarrow V_{B,R} = -10.625$$

$$V_x = -10.625$$

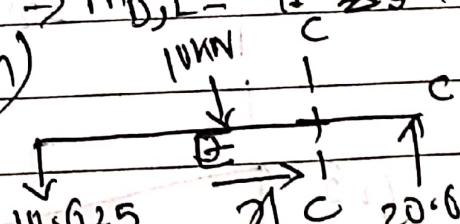
$$\text{At } x=2 \rightarrow V_{D,L} = -10.625$$

$$M_x = -10.625x + 62.5$$

$$\text{At } x=2 \rightarrow M_{D,L} = -21.25 + 62.5$$

$$M_{D,L} = 41.25 \text{ kNm}$$

For span $\bar{D}C$ ($0 \leq x \leq 2m$)



$$V_x = -10.625 \div 10$$

$$= -20.625$$

$$\text{At } x=0 \rightarrow V_{D,R} = -20.625$$

$$\text{At } x=2 \rightarrow V_{C,L} = -20.625$$

Always take x from the considered span.

$$M_x = -10.625(2+x) - 10x + 62.5$$

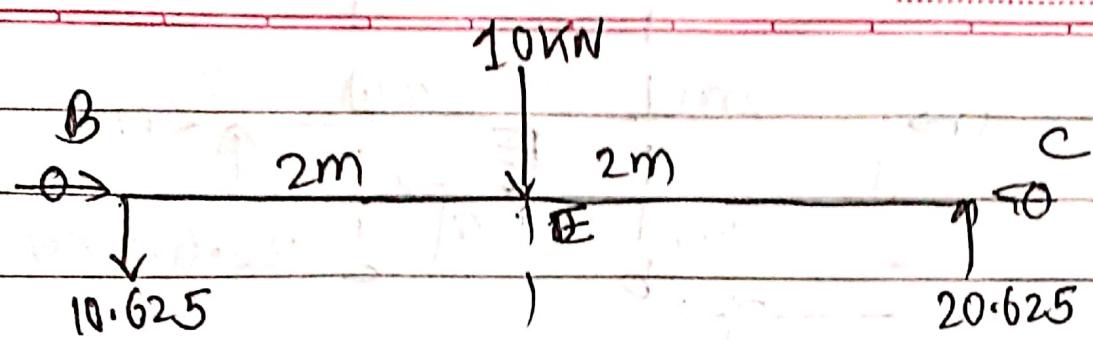
$$= -21.25 - 10.625x - 10x + 62.5$$

$$= -21.25 - 20.625x + 62.5$$

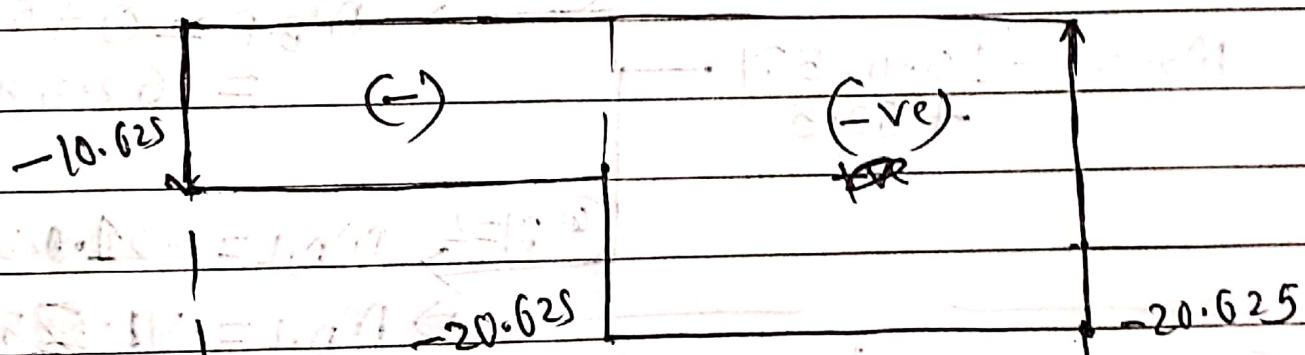
$$\text{At } x=0 \rightarrow M_{D,R} = -21.25$$

$$\text{At } x=2 \rightarrow M_{C,L} = -41.25 - 21.25 + 62.5$$

$$= 0$$



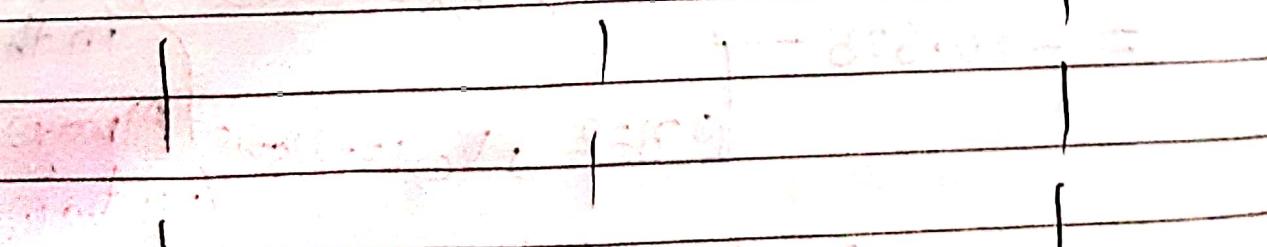
AFD



62.5

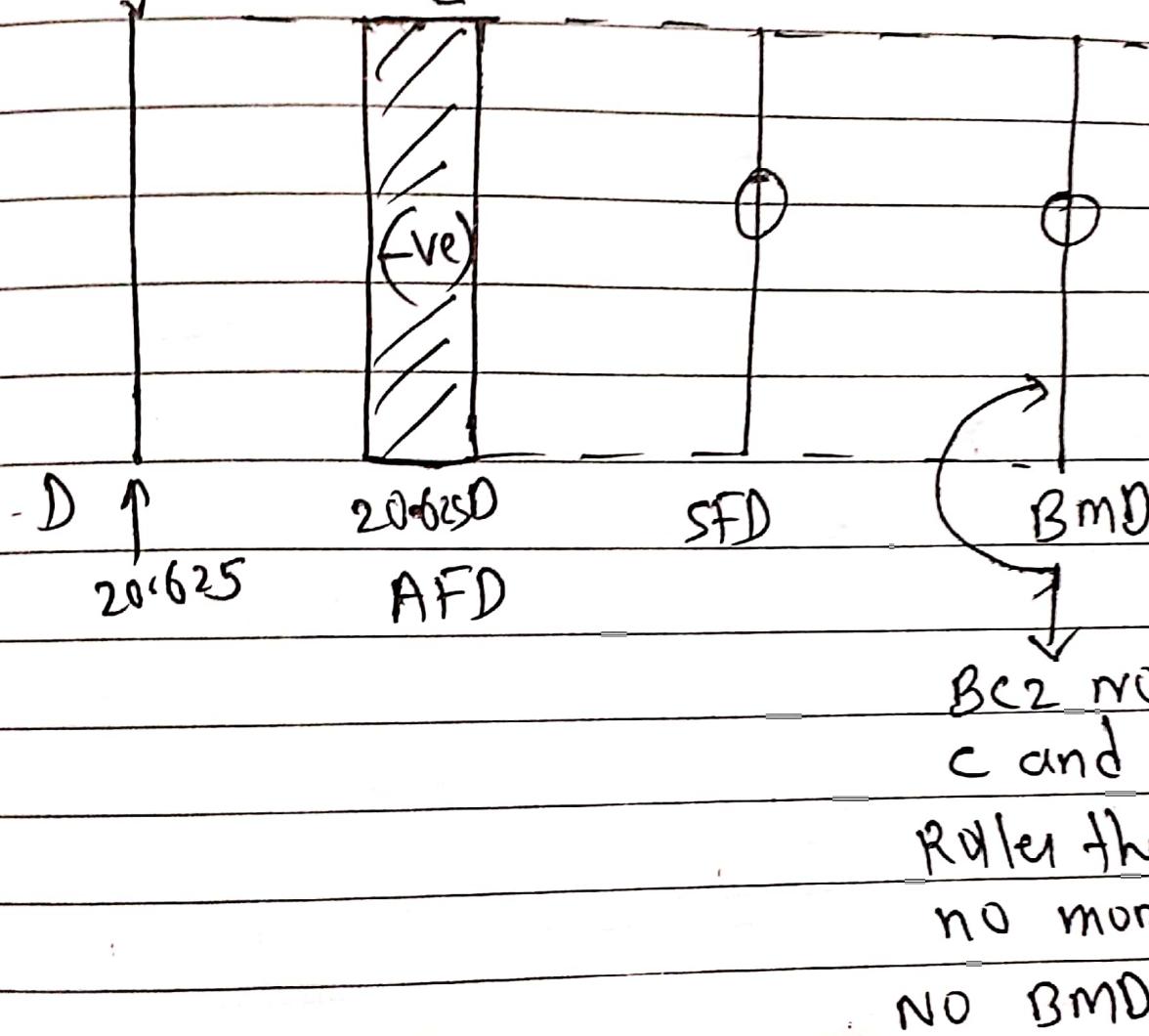
41.75

(+)

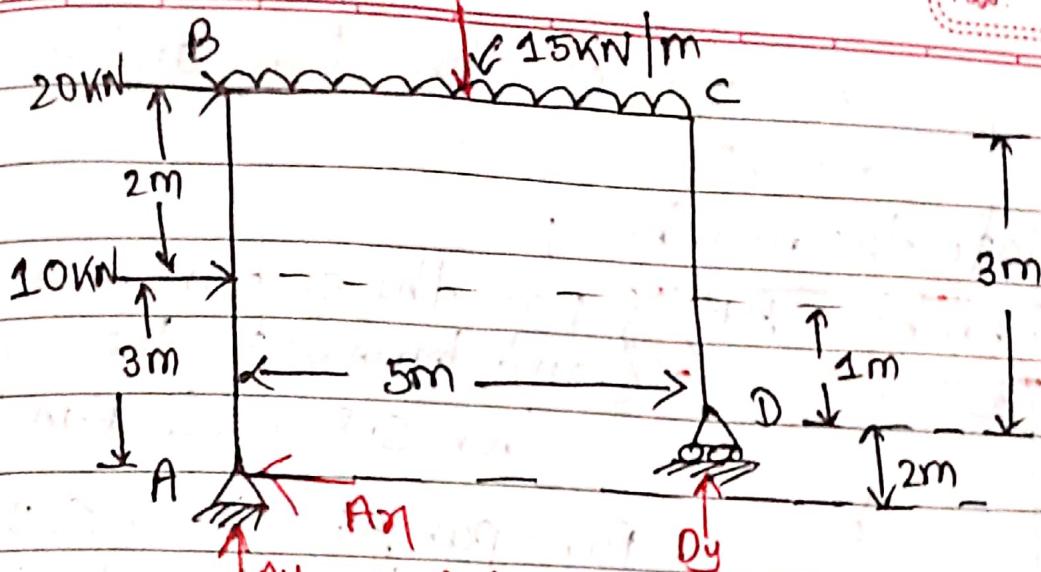


Member CD20.625
C|

(NO forces perpendicular to member thus NO shear force so, let's draw AFD, SFD and BMD)



(8)



Step 10 → Calculating the Reactions

$$\sum F_x = 0 \rightarrow A_x = 0$$

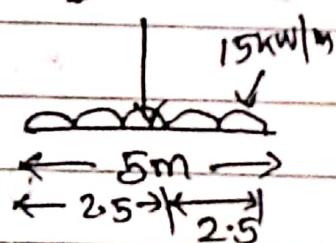
$$-A_y + 10 + 20 = 0$$

$$\Rightarrow A_y = 30 \text{ kN} \quad (\leftarrow)$$

$$\sum F_y = 0 \quad (\uparrow +ve)$$

$$A_y + \alpha_y - 75 = 0 \quad \dots \quad ①$$

$$15 \times 5 = 75 \text{ kN}$$



$$\sum M_A = 0 \quad (+ve) \quad \{ \text{clockwise } +ve \}$$

$$\Rightarrow 10 \times 3 + 20 \times 5 + 75 \times 2.5 - \alpha_y \times 5 = 0$$

$$\Rightarrow 30 + 100 + 187.5 - 5\alpha_y = 0$$

$$\Rightarrow \alpha_y = 63.5 \text{ kN} \quad (↑)$$

From eqn ①

$$\Rightarrow A_y + 63.5 - 75 = 0$$

$$\Rightarrow A_y - 11.5 = 0$$

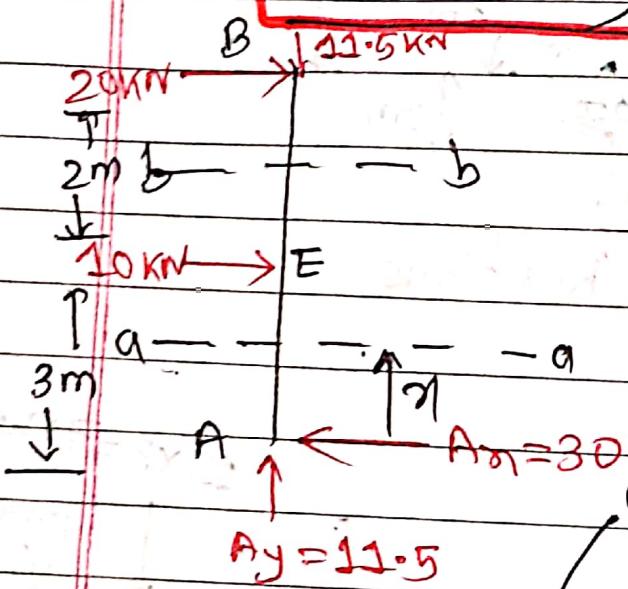
$$\Rightarrow A_y = 11.5 \text{ kN} \quad (\uparrow)$$

Step 2: Analysis of shear force and bending moment

Isolate the member;

Member AB;

{ pass the section a-a and b-b
and formulate the equation
for S.F and B.M }



For span AE ($0 \leq x \leq 3m$)

(Move from left to right)

$$V_x = 30 \rightarrow V_A = 30 \text{ kN}$$

$$@x=3m \quad V_{E,L} = 30 \text{ kN}$$

(clockwise +ve) \leftarrow Always take this

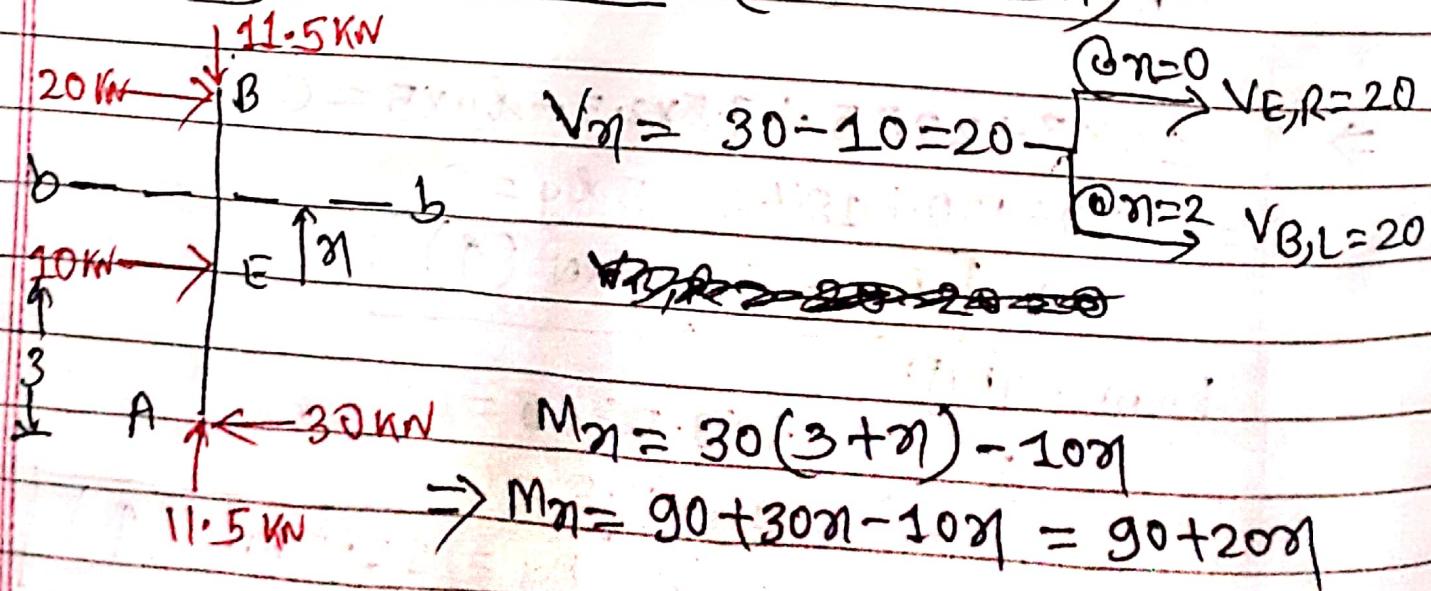
~~counter clockwise~~ while moving from
left to right

Bending moment equation @ $x=0$

$$\Rightarrow M_x = 30x \rightarrow M_A = 0$$

$$@x=3m \rightarrow M_{E,L} = 90 \text{ kNm}$$

Similarly for span b-b ($0 \leq x \leq 2m$)



$$M_x = 30(3+x) - 10x$$

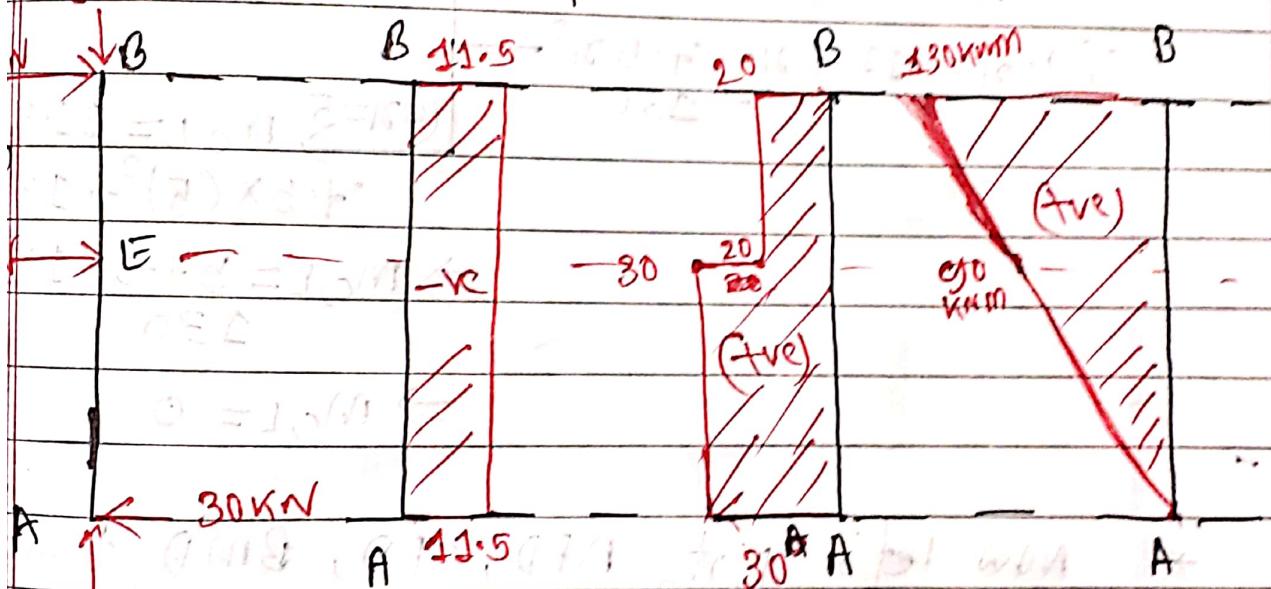
$$\Rightarrow M_x = 90 + 30x - 10x = 90 + 20x$$

$$M_n = 90 + 20\eta$$

① $\eta=0 \rightarrow M_{E,R} = 90 \text{ kNm}$

② $\eta=2 \rightarrow M_B, L = 90 + 40$
 $= 130 \text{ kNm}$

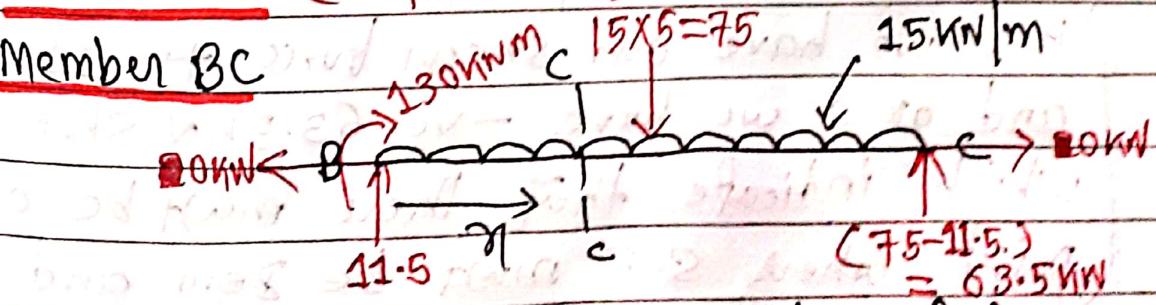
Let's plot AFD, SFD and BMD, for member AB,
 For AFD \rightarrow tensile $\rightarrow +ve$,
 compression $\rightarrow -ve$.



AFD (without 30 kN and 11.5 kN)

\Rightarrow 11.5 kN (compression -ve) added two

Member BC



Pass the section (c-c) and formulate the equation for shear force and bending moment.

Note in member AB by
 against which will be axial
 in member BC is already
 balanced.

$$V_n = 11.5 - 15\alpha$$

$\text{At } \alpha=0 \rightarrow V_{B,R} = 11.5 \text{ kN}$

$\text{At } \alpha=5 \rightarrow V_{C,L} = 11.5 - 15 \times 5$

$$\Rightarrow V_{C,L} = -63.5 \text{ kN}$$

✓ moment at B that we
 $M_n = 11.5\alpha - 15\alpha^2 + \frac{130}{2}$ bound
 $\text{At } \alpha=0 \rightarrow M_{B,R} = 130 \text{ kNm}$

$$\Rightarrow M_n = 11.5\alpha - 7.5\alpha^2 + 130$$

$\text{At } \alpha=5 \rightarrow M_{C,L} = 11.5 \times 5 - 7.5 \times (5)^2 + 130$

$$\Rightarrow M_{C,L} = 57.5 - 187.5 + 130$$

$$\Rightarrow M_{C,L} = 0$$

Now let's plot AFD, SFD, BMD taking our sign convention into consideration.

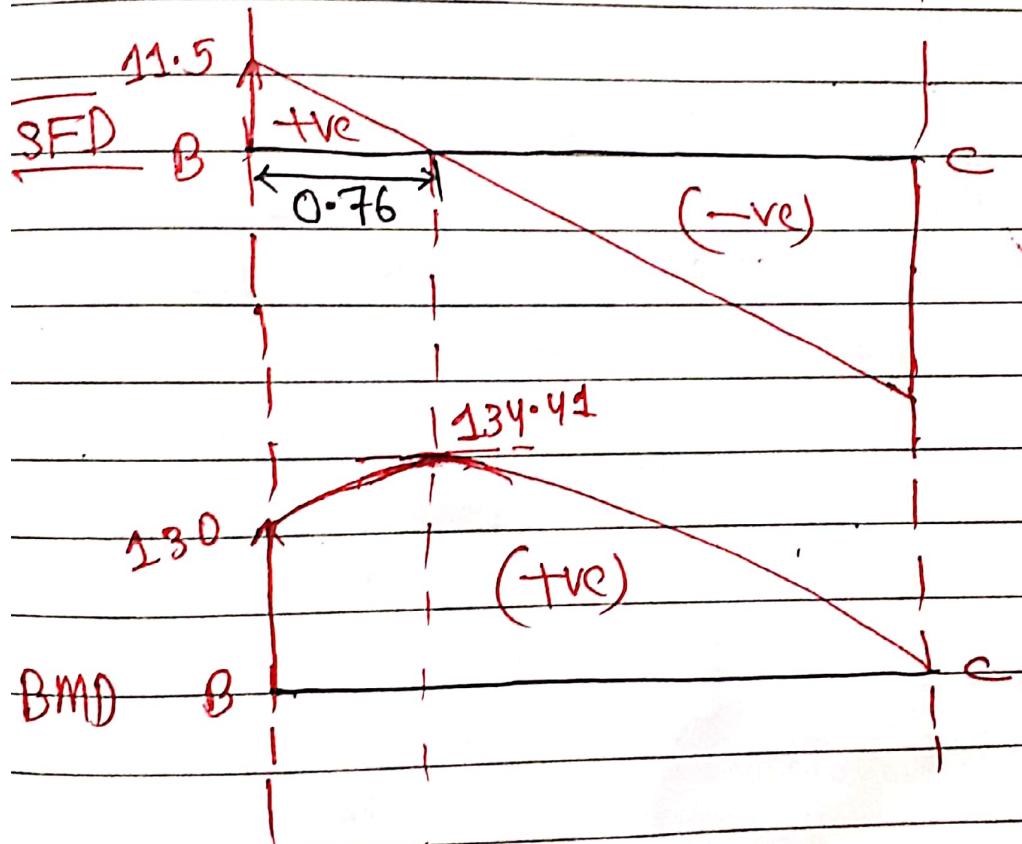
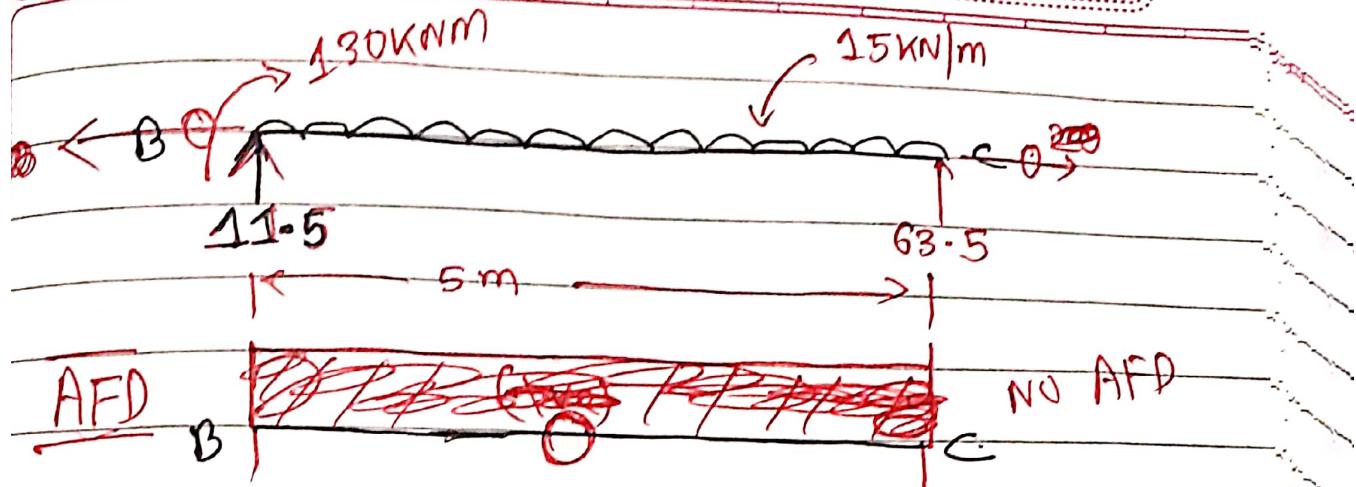
But before that see in the S.F. value

Here we have our shear force +ve 11.5 at B and at C we have -ve 63.5 kN shear force which indicates that there must be certain point where S.F. must be zero and at that point bending moment should be minimum
 \therefore point of zero shear $V_n = 11.5 - 15\alpha = 0$

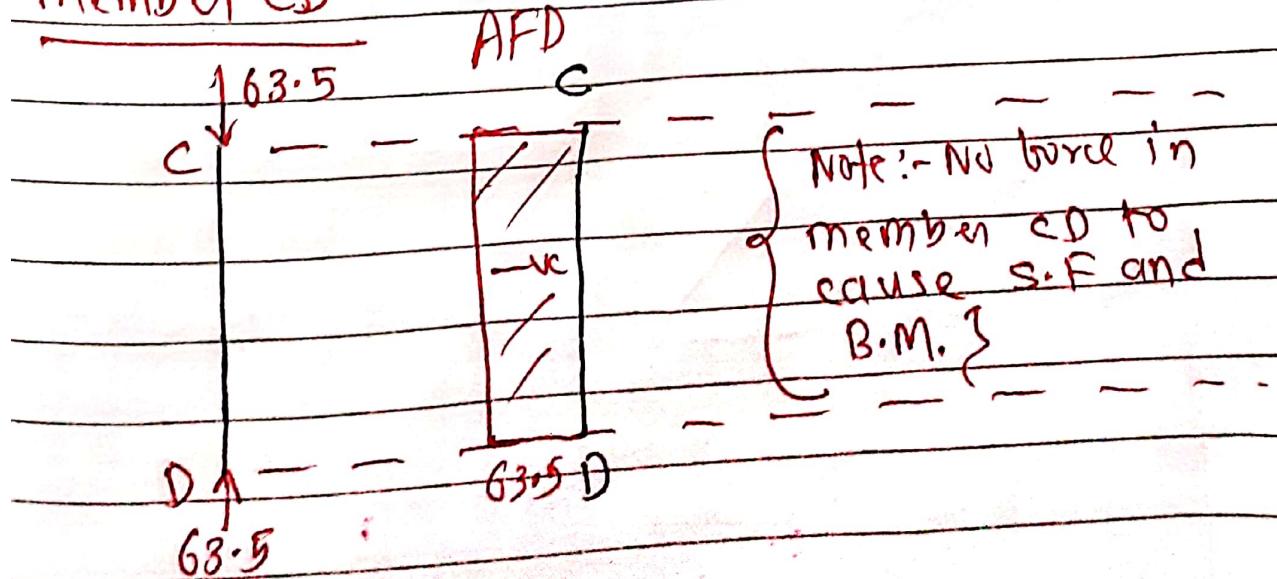
$$\Rightarrow \alpha = 11.5 / 15 \Rightarrow \alpha = 0.76 \text{ m from B}$$

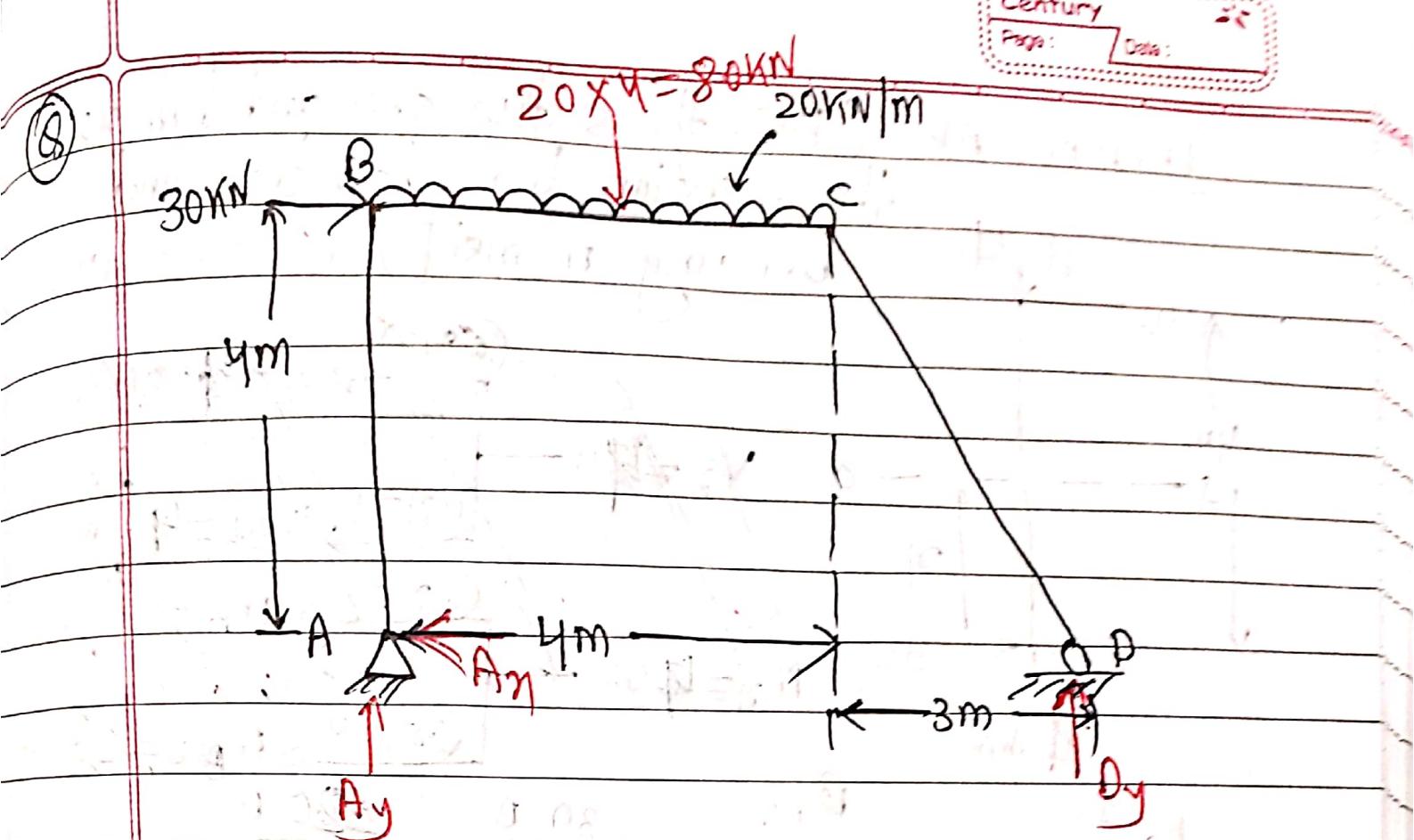
$$\therefore (M)_{\text{min}} = 11.5(0.76) - 7.5(0.76)^2 + 130$$

$$\Rightarrow (M)_{\text{min}} = 134.41 \text{ kNm}$$



Member CD





Step 1 → calculating the Reactions

$$\sum F_x = 0 \quad (\rightarrow +ve)$$

$$-A_x + 30 = 0$$

$$\Rightarrow A_x = 30\text{ kN}$$

$$\sum F_y = 0 \quad (1+ve)$$

$$A_y + D_y - 80 = 0 \quad \text{--- (1)}$$

$$\sum M_A = 0 \quad (\text{1+ve})$$

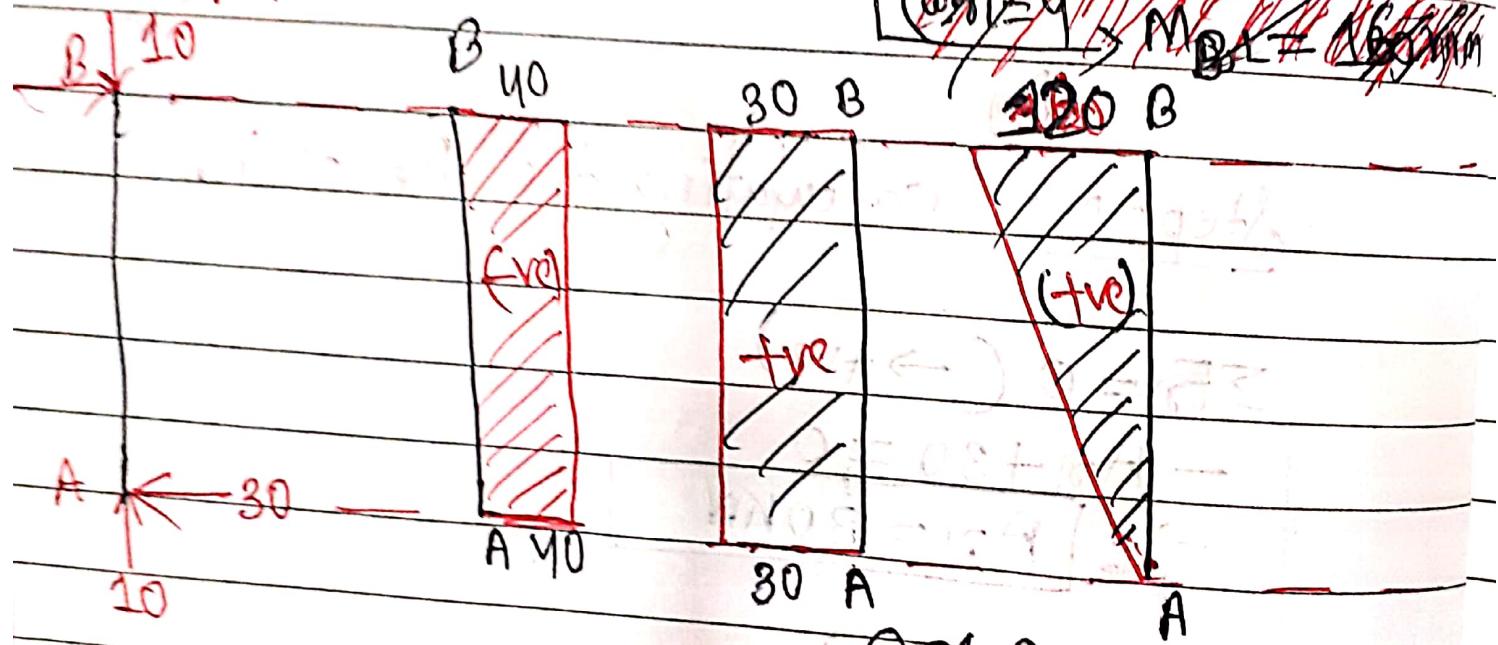
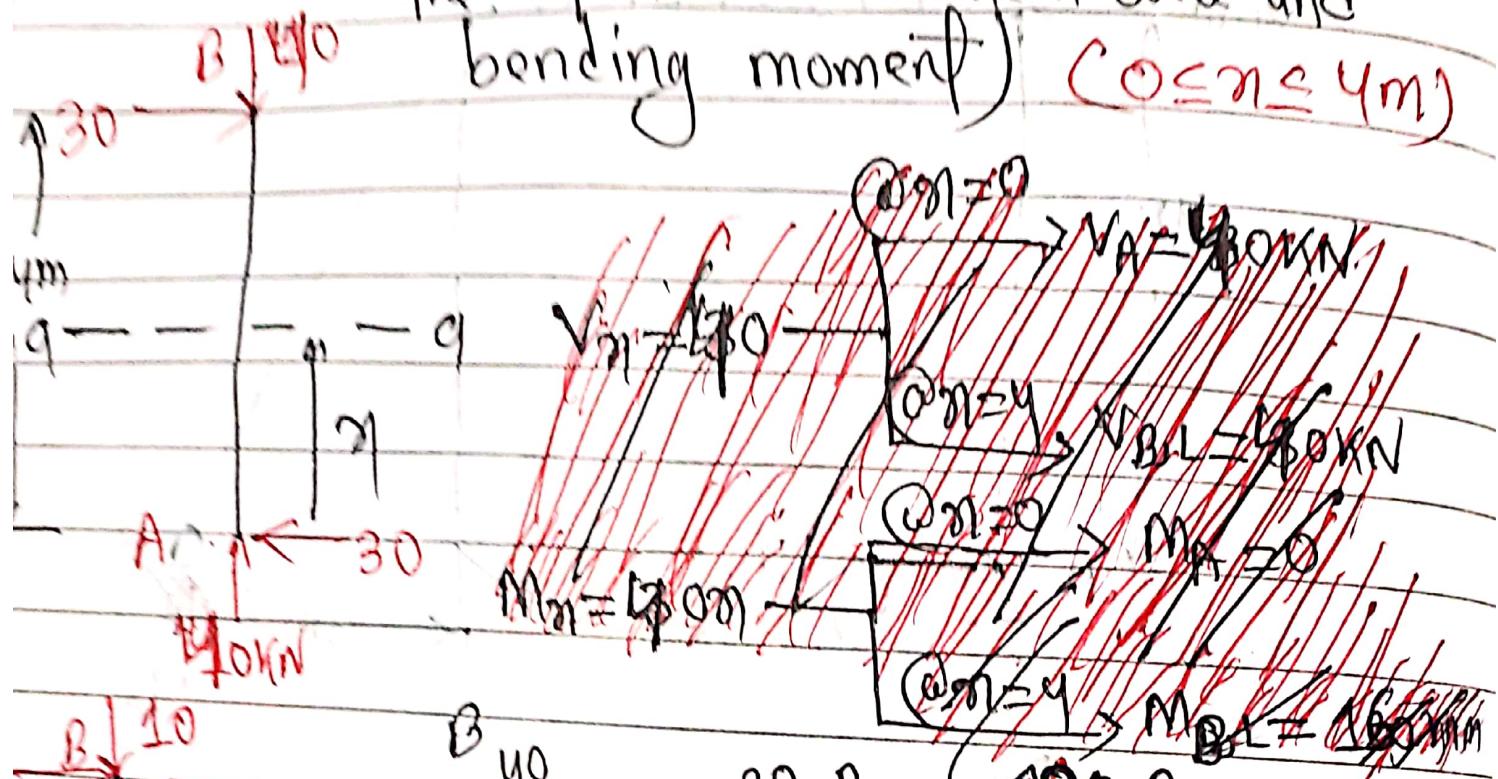
$$30 \times 4 + 80 \times 2 - d_y \times 7 = 0$$

$$\Rightarrow d_y = 40\text{ kN} \quad (1)$$

$$\text{From eqn (1)} ; \Rightarrow A_y + 40 - 80 = 0$$

$$\Rightarrow [A_y = 40\text{ kN}] \quad (1)$$

Member AB (Pass the section a-a and form up the equation for shear force and bending moment) ($0 \leq n \leq 4m$)



Member BC

$$V_n = 30 \rightarrow$$

$$\text{at } x=0 \rightarrow V_A = 30 \text{ N}$$

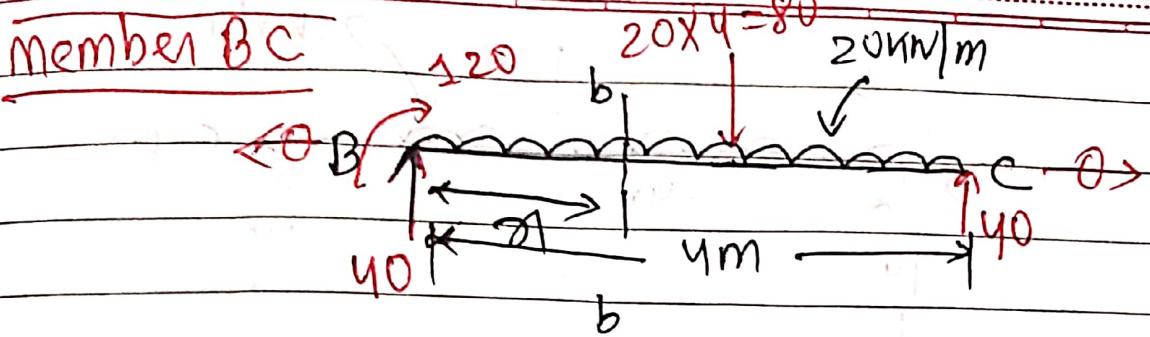
$$\text{at } x=4 \rightarrow M_A = 0$$

$$\text{at } x=4 \rightarrow M_{B,L} = 30 \text{ Nm}$$

$$M_n = 30 \rightarrow$$

$$\text{at } x=4 \rightarrow M_A = 0$$

$$\text{at } x=4 \rightarrow M_{B,L} = 120 \text{ Nm}$$



Pass the section (b-b) from B and from the equation for shear force and bending moment informs of σ_1 .

$$V_{B,R} = 40 \text{ kN}$$

$$V_B = 40 - 20\sigma_1$$

$$V_{C,L} = -40 \text{ kN}$$

point of zero shear force

$$\Rightarrow V_B = 40 - 20\sigma_1 = 0$$

$$\Rightarrow \sigma_1 = 2 \text{ m}$$

$$M_B = 40\sigma_1 - 20\sigma_1 \times \frac{\sigma_1}{2} + 120$$

$$M_{B,R} = 0 + 120$$

$$\Rightarrow M_B = 40\sigma_1 - 10\sigma_1^2 + 120$$

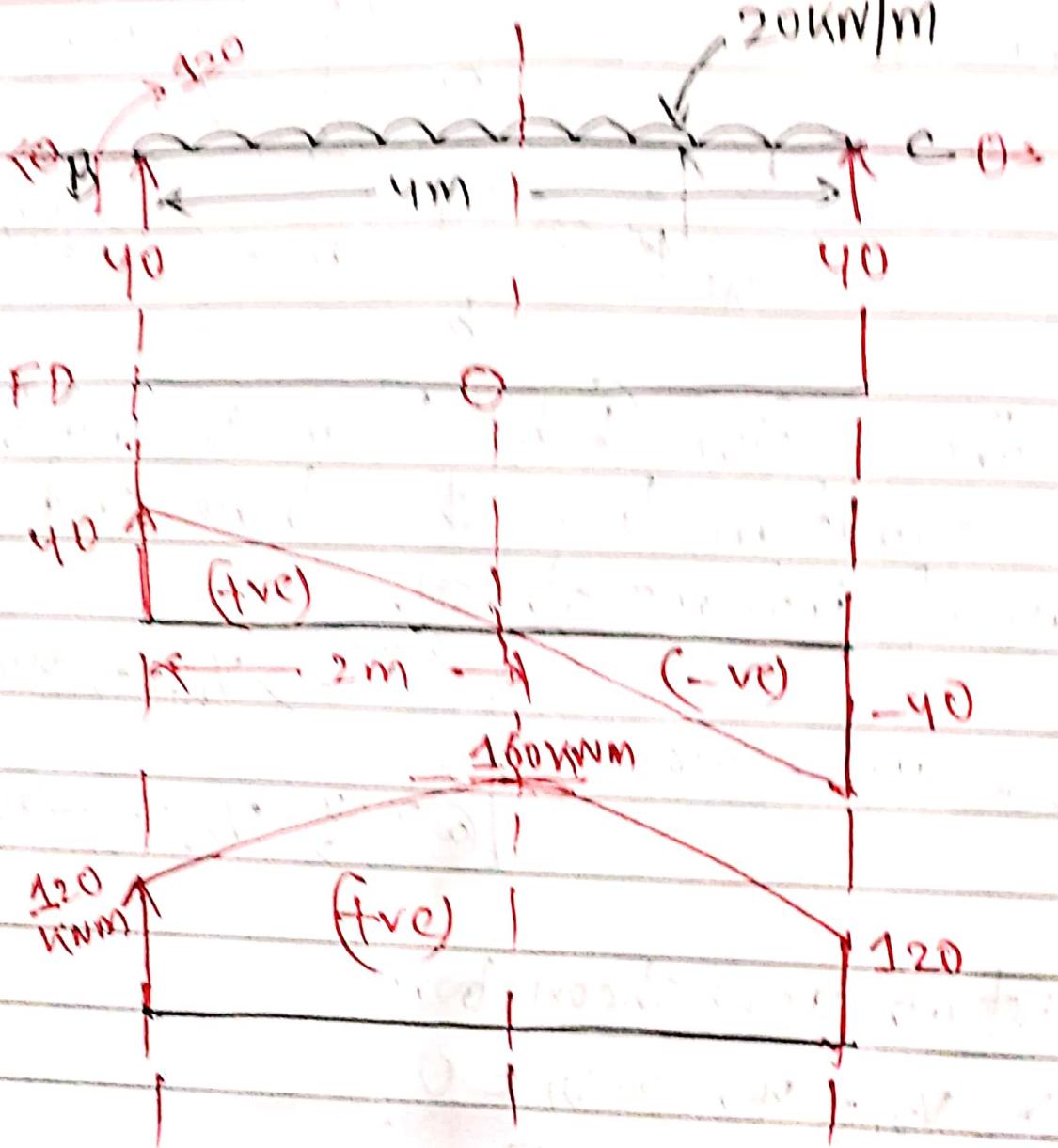
$$M_{B,R} = 120 \text{ kNm}$$

$$M_{C,L} = 40 \times 4 - 10(4)^2 + 120$$

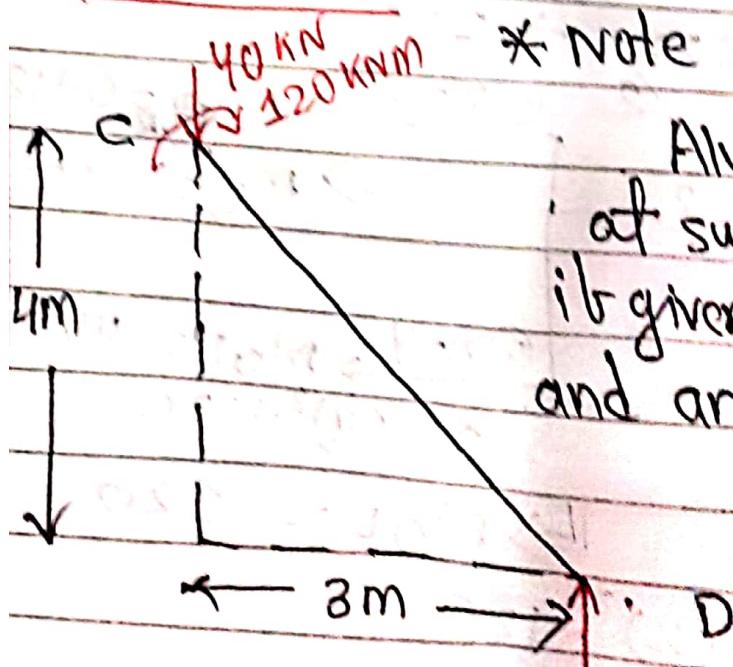
$$M_{C,L} = 120$$

$$(M)_{max} = 40 \times 2 - 10(2)^2 + 120$$

$$\Rightarrow (M)_{max} = 160 \text{ kNm.}$$

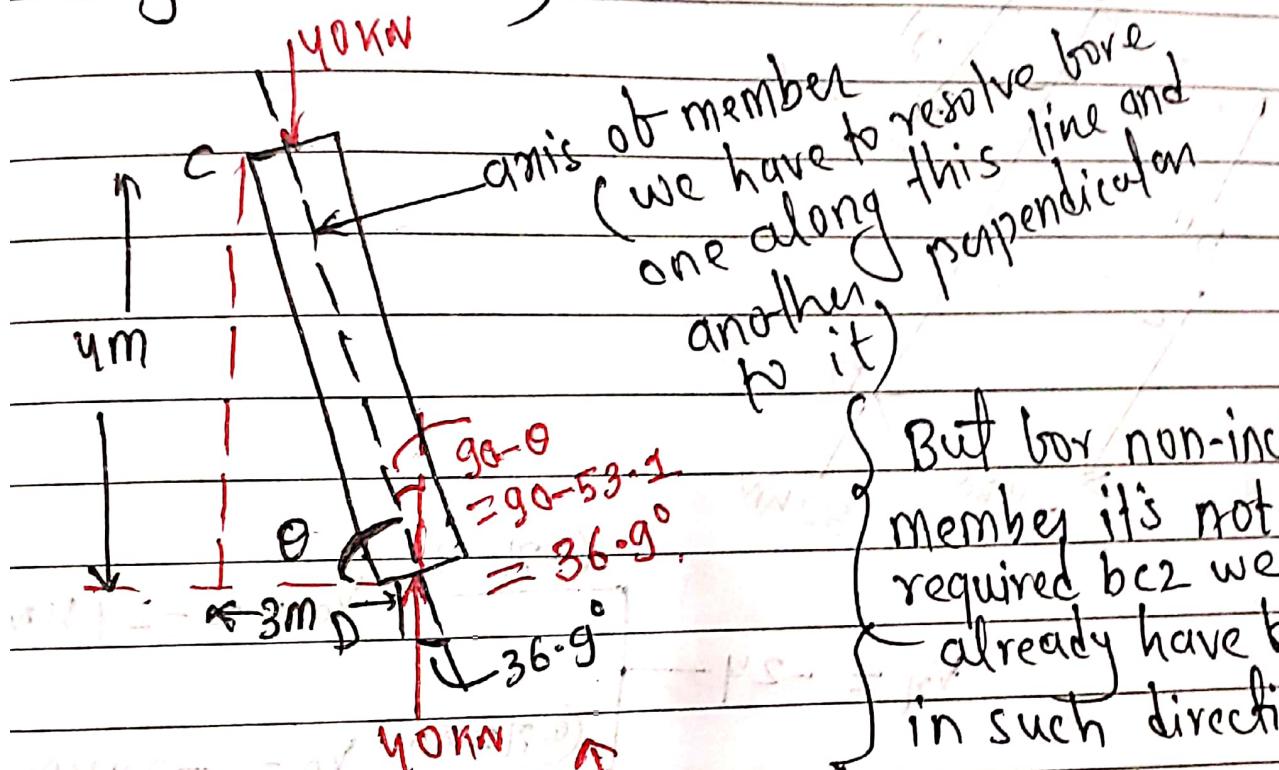


Member CD



* Note for Inclined member
 Always first resolved the forces at supports or joints ~~or~~ and member if given along the axis of member and another perpendicular to it.
 for given case we only have forces at joint (C) and support D
 length of member(CD) = $\sqrt{4^2 + 3^2} = 5\text{m}$ so we have to resolve both

To make it more clean consider CD member member as shown in the figure below;



$$\tan \theta = P/b = \frac{4}{3}$$

$$\Rightarrow \theta = \tan^{-1} \left(\frac{4}{3} \right)$$

$$\Rightarrow \theta = 53.1^\circ$$

$$40 \cos 36.9^\circ = 32$$

$$40 \sin 36.9^\circ = 24$$

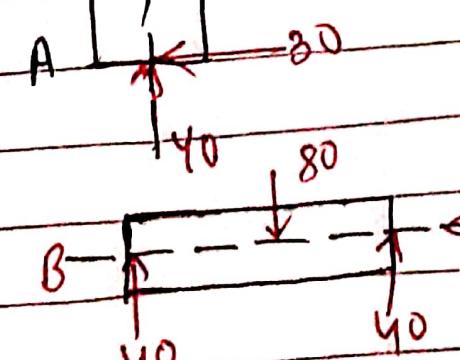
$$40 \cos 53.1^\circ = 24$$

$$40 \sin 53.1^\circ = 32$$

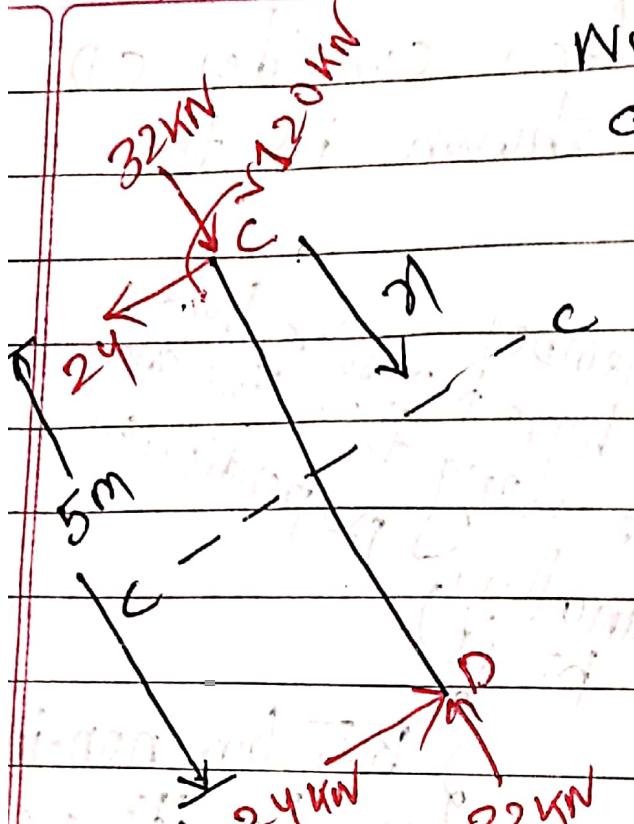
This is just to explain

You show like this

For ex:- in give question



Now pass the section C-C
and formulate the equation for
C-D.



$$V_{Dl} = -24$$

$$@ \eta=0$$

$$V_{CR} = -24 \text{ kN}$$

$$@ \eta=5 \text{ m} \rightarrow V_D = -24 \text{ kN}$$

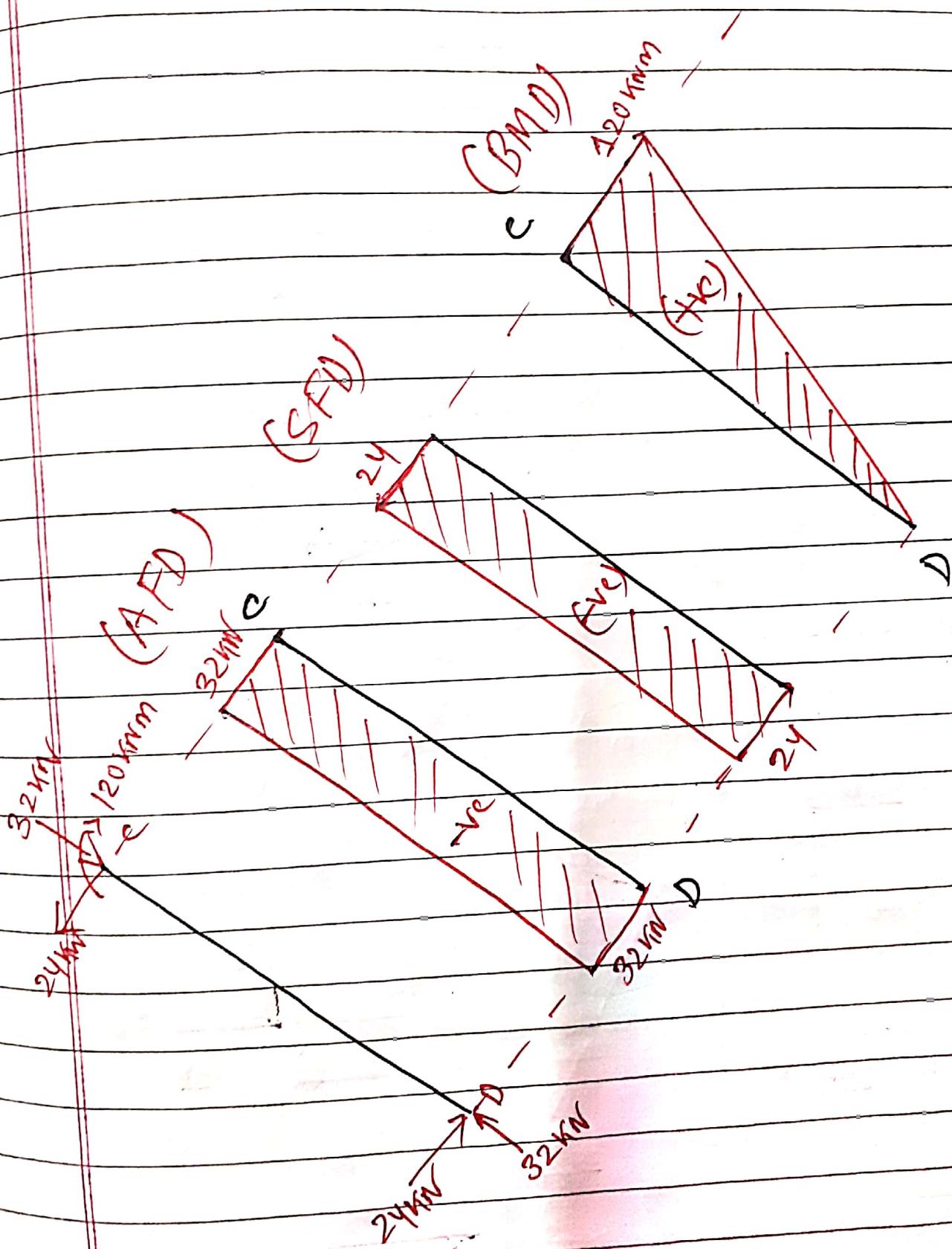
$$@ \eta=0$$

$$M_{CR} = 120$$

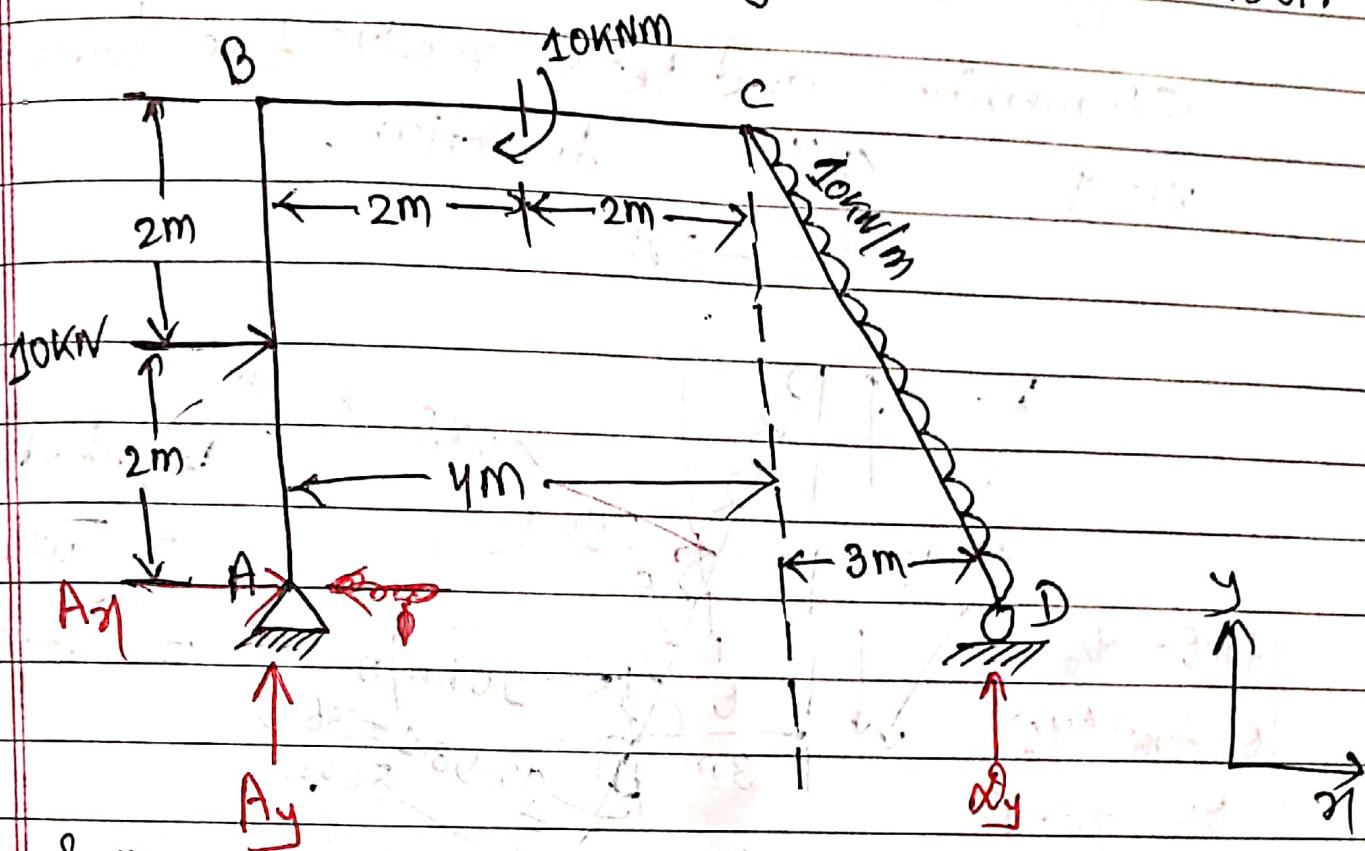
$$@ \eta=5 \rightarrow M_D = -120 + 120$$

$$= 0$$

$$M_H = -24 \times 5 + 120$$



IB UDL is acting on inclined member.

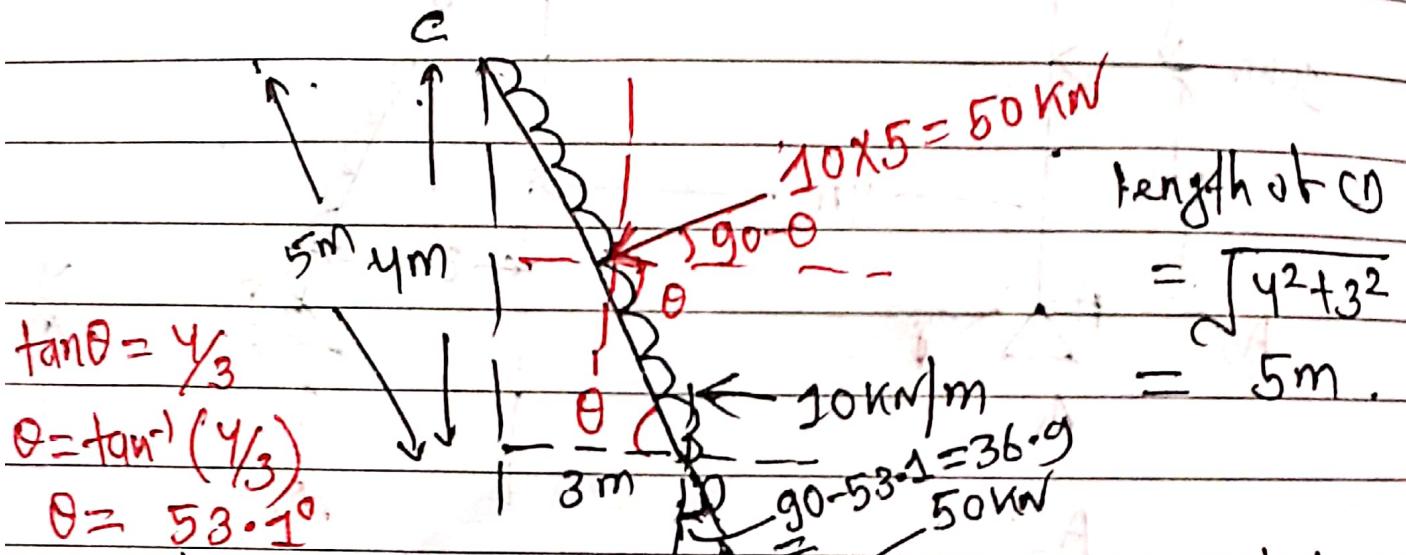
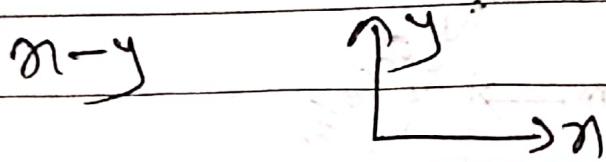


Soln

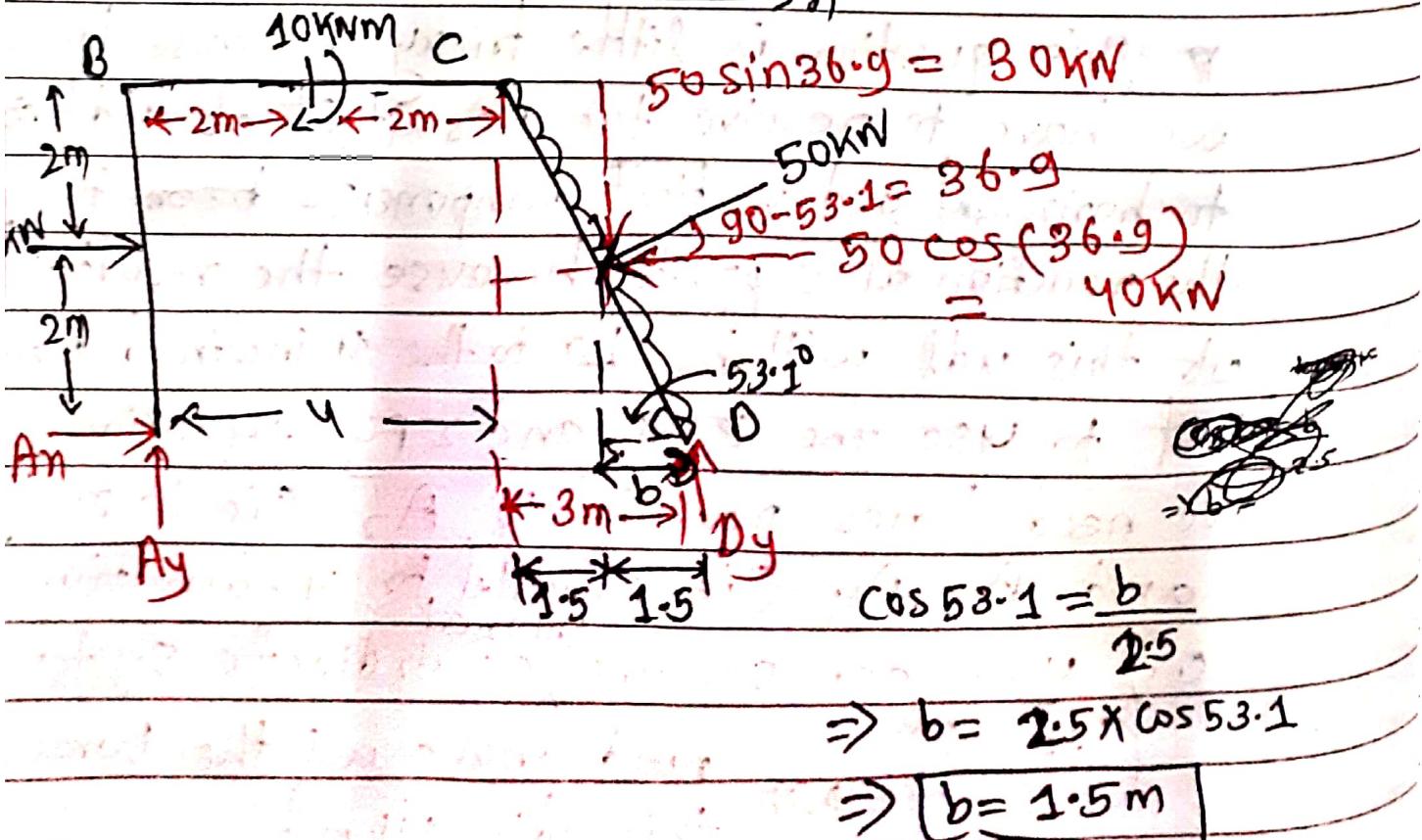
Step 1 :- Calculating the Reactions.

This question is little tricky because here we have to resolve the resultant of udl of the inclined member into horizontal and vertical components to bind the reaction at supports because the resultant of this udl will be parallel to the inclined member but to use the $\sum F_x$ and $\sum F_y$ equation we need forces parallel to A_x (ie in x-direction) and A_y, D_y (ie parallel to y-direction) or, you can see the coordinate system (ie $\begin{matrix} \uparrow y \\ \rightarrow x \end{matrix}$) and make all the forces in this direction)

To give you more insight let's just take CD member and let's resolve the forces in $x-y$ direction.



we have 50kN line \Rightarrow but we need force in $x-y$ direction
so we have to resolve to bind reactions



$$\Rightarrow \sum F_n = 0 (\rightarrow \text{tre})$$

$$A_n + 10 - 40 = 0$$

$$A_n - 30 = 0 \Rightarrow A_n = 30 \text{ kN}$$

$$\sum F_y = 0 (\uparrow \text{tre})$$

$$A_y + D_y - 30 = 0 \quad \textcircled{1}$$

$$\sum M_A = 0 (\text{anti-clockwise} \rightarrow \text{clockwise tre})$$

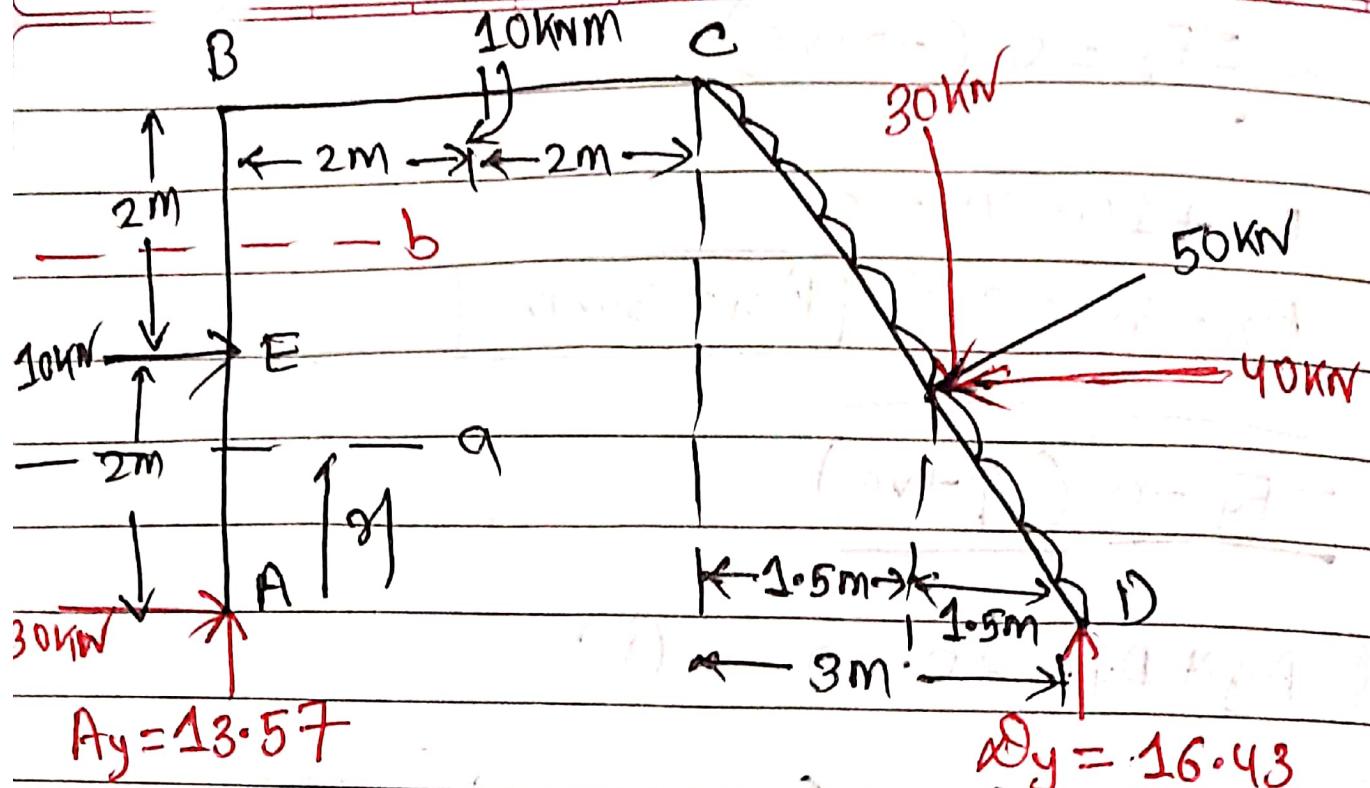
$$10 \times 2 + 10 + 30(4 + 1.5) - 40 \times 2 - d_y \times 7 = 0$$

$$\Rightarrow d_y = 16.43 \text{ kN}$$

From eqn ①

$$A_y + 16.43 - 30 = 0$$

$$\Rightarrow A_y = 13.57 \text{ kN}$$



Step 2: Analysis of shear force and bending moment.

Member AB → pass the section (a-a) and (b-b) to form the S.F and B.M equation in terms of η .

Span AE ($0 \leq \eta \leq 2m$)

$$@ \eta=0 \rightarrow V_A = -30kN$$

$$V_\eta = -30kN$$

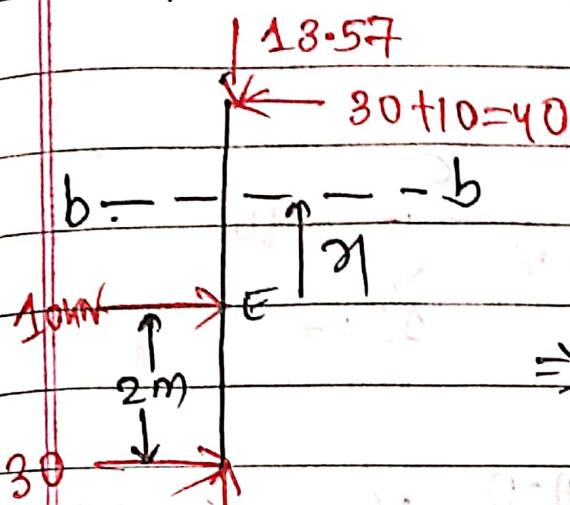
$$@ \eta=2 \rightarrow V_{E,L} = -30kN$$

$$M_\eta = -30\eta$$

$$@ \eta=0 \rightarrow M_A = 0$$

$$@ \eta=2 \rightarrow M_{E,L} = -60kN$$

Span (EB) ($0 \leq n \leq 2m$)



$$V_n = -30 - 10 = -40$$

$$\Rightarrow V_n = -40$$

① $n=0 \rightarrow V_{E,R} = -40$

② $n=2 \rightarrow V_{B,L} = -40$

$$A_y = 13.57$$

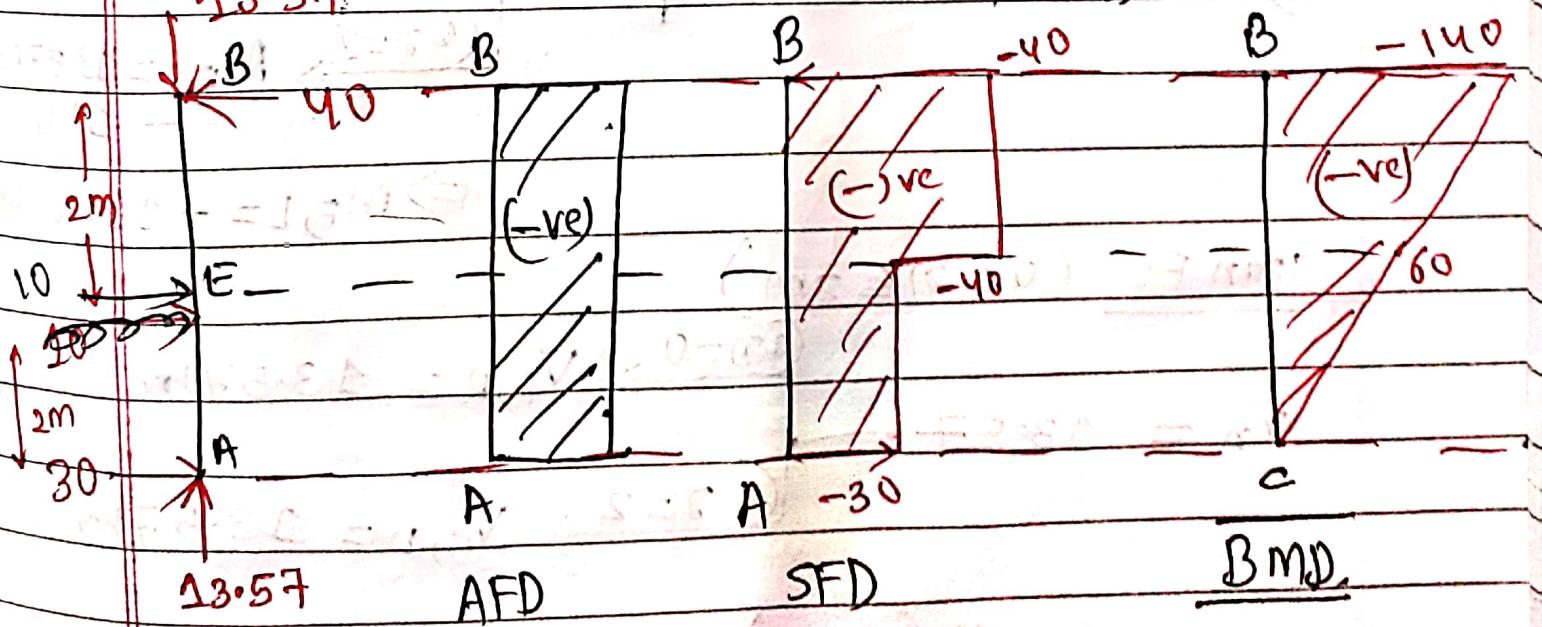
$$M_n = -30(2+n) - 10n = -60 - 30n - 10n$$

$$\Rightarrow M_n = -60 - 40n$$

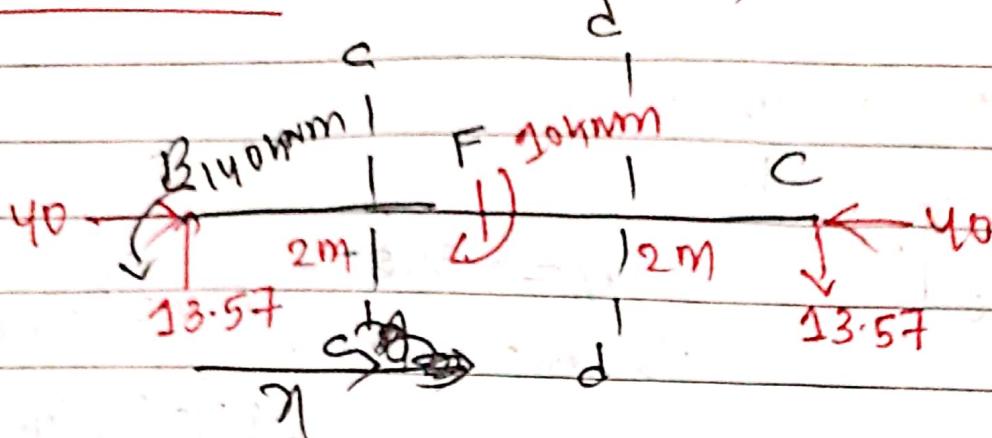
① $n=0 \rightarrow M_{E,R} = -60 \text{ kNm}$

② $n=2 \rightarrow M_{B,L} = -60 - 80$

$$\Rightarrow M_{B,L} = -140 \text{ kNm.}$$



Member BC ($0 \leq n \leq 2$) \rightarrow Span BF



SP

$$V_n = 13.57$$

$$\textcircled{n=0} \rightarrow V_{B,R} = 13.57 \text{ kN}$$

$$\textcircled{n=2} \rightarrow V_{F,L} = 13.57 \text{ kN}$$

$$M_n = 13.57n - 140$$

$$\Rightarrow M_n = 13.57n - 140$$

$$\textcircled{n=0} \rightarrow M_{B,R} = -140$$

$$\textcircled{n=2} \rightarrow M_{F,L} = 13.57 \times 2 - 140$$

$$\Rightarrow M_{F,L} = -112.86 \text{ kNm}$$

Span FC ($0 \leq n \leq 2m$)

$$V_n = 13.57 \rightarrow \textcircled{n=0} \rightarrow V_{F,R} = 13.57 \text{ kN}$$

$$\textcircled{n=2} \rightarrow V_{C,L} = 13.57 \text{ kN}$$

$$M_n = 13.57(2+n) + 10 - 140$$

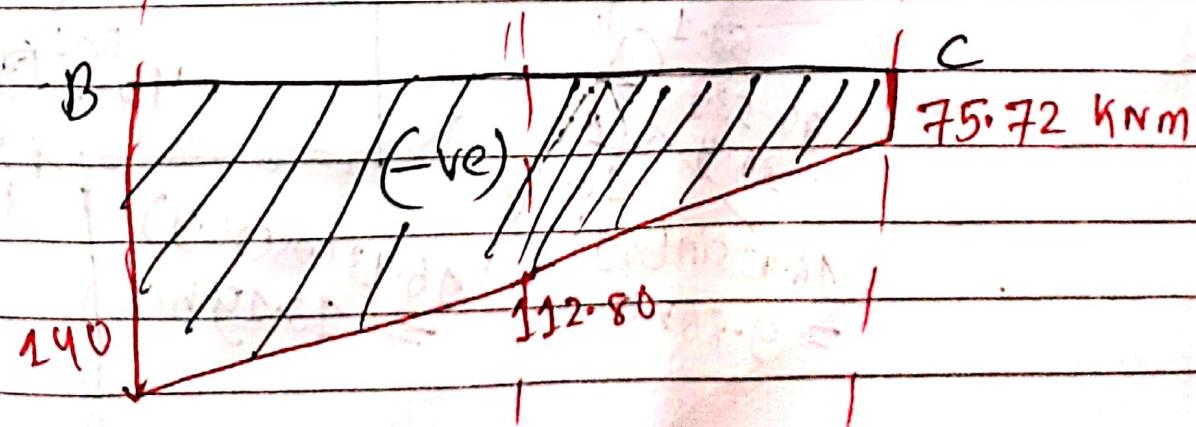
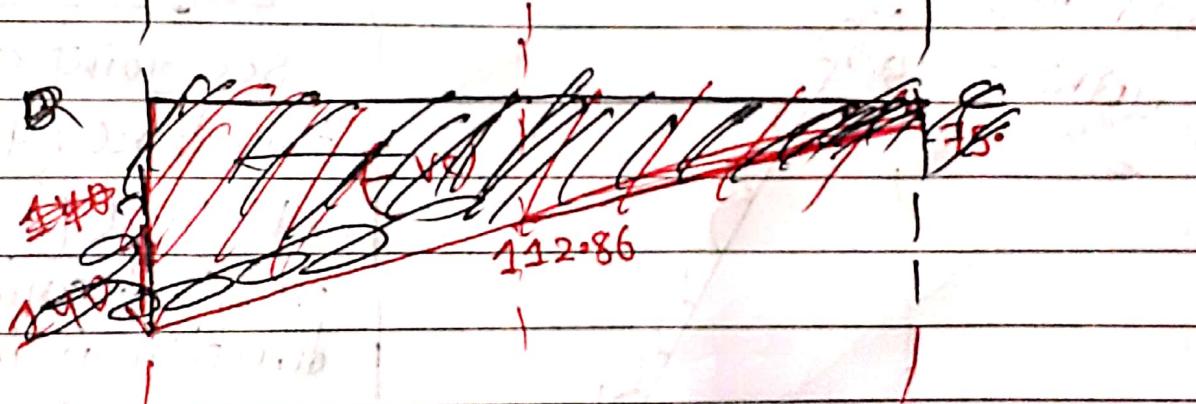
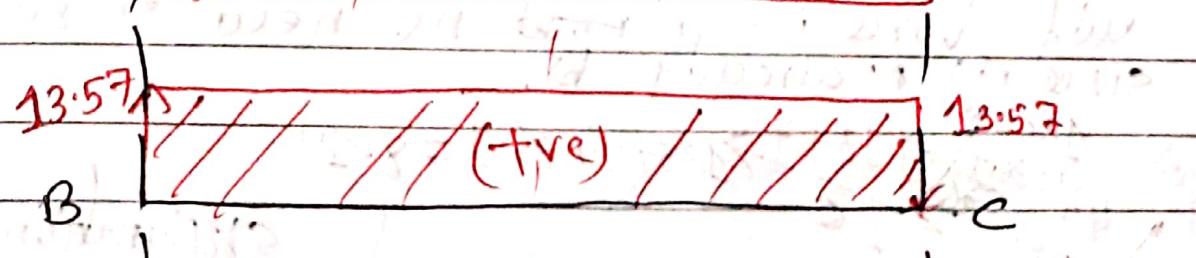
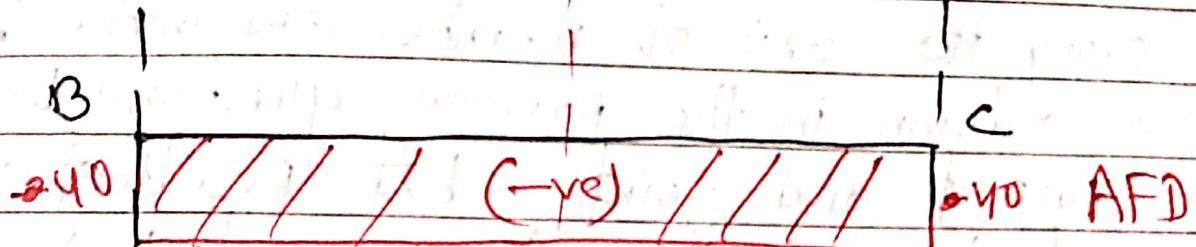
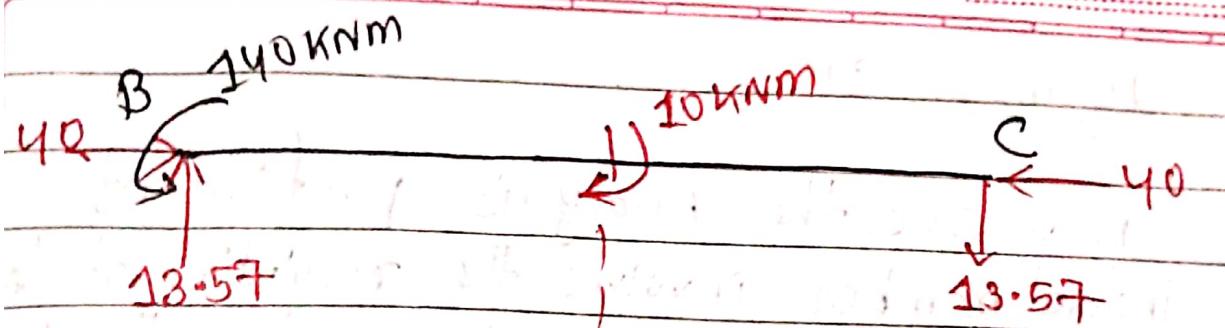
$$= 27.14 + 13.57n - 130$$

$$= 13.57n - 102.86$$

$$\textcircled{n=0} \rightarrow M_{F,R} = -102.86$$

$$\textcircled{n=2} \rightarrow M_{C,L} = 13.57 \times 2 - 102.86$$

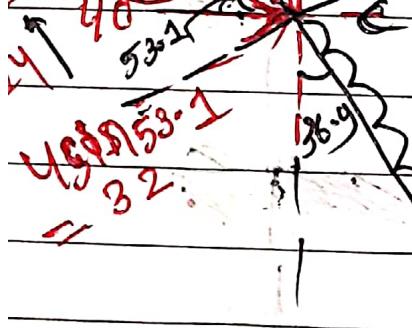
$$\Rightarrow M_{C,L} = -75.72 \text{ kNm}$$



Member CD

Now see the Analysis portion of inclined member involves the resolution of forces along the axis of member and another br to it as down in the previous questions, but the supports and joints but Resultant of udl force is in ~~root~~ no need to be resolved since it's already br.

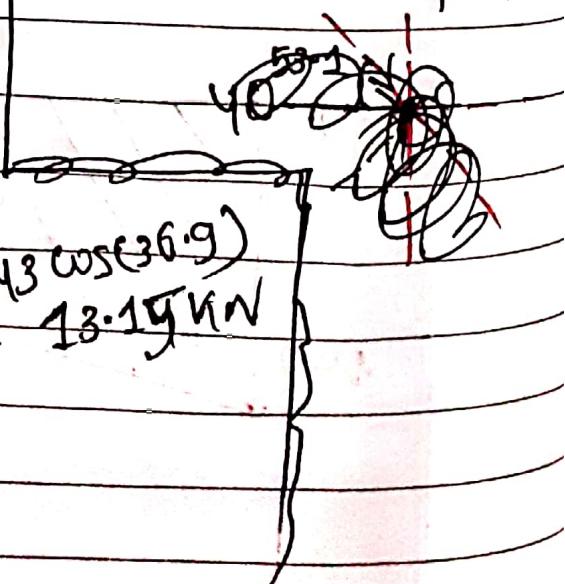
$$\rightarrow \frac{13.57}{\cos 36.9} \rightarrow 13.57 \rightarrow 13.57 \sin 36.9 = 8.14$$



Explanation

see joint C has two force ($40 \rightarrow$) and $13.57 (\uparrow)$ to be resolved and it's direction is important

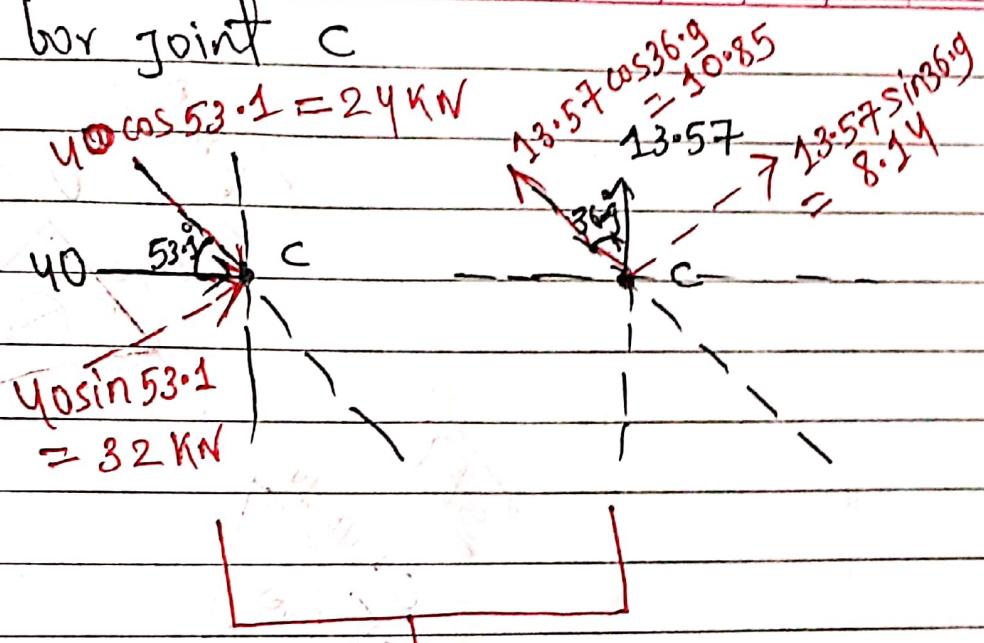
$$\begin{aligned}
 & 53.1 \\
 & 90 - 53.1 \\
 & = 36.9 \\
 & 16.43 \\
 & -16.43 \sin(36.9) \\
 & = 9.86 \text{ kN} \\
 & 16.43 \cos(36.9) \\
 & = 13.19 \text{ kN}
 \end{aligned}$$



Explanation for Force Resolve

Century
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Let see for joint C



We will take net of each of forces at joint C.

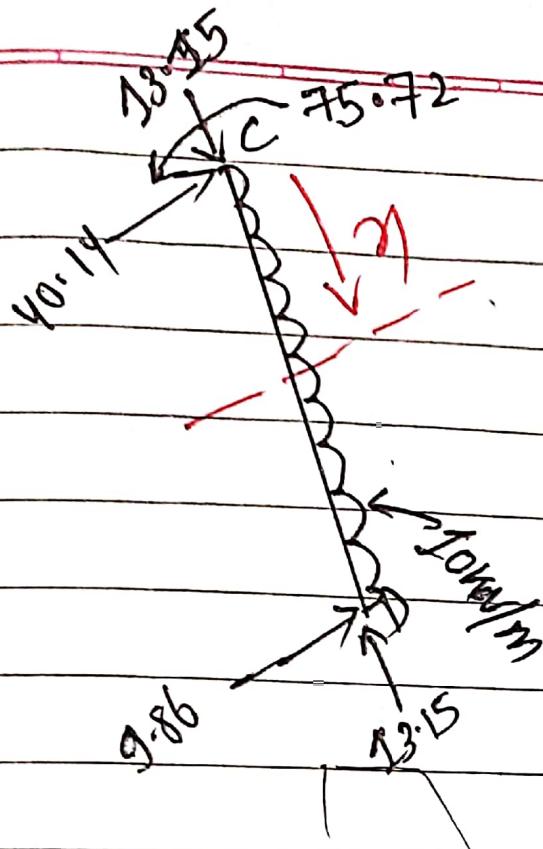
$$24 - 10.85 = 13.15$$

$$32 + 8.14 = 40.14$$

For joint support at D.

$$16.43 \sin 36.9^\circ = 9.86 \text{ kN}$$

$$16.43 \cos (36.9^\circ) = 13.15$$



Member CD ($0 \leq x_1 \leq 5m$)

$$V_{n1} = 40.14 - 10x_1 \quad @x_1=0 \rightarrow V_{C,R} = 40.14$$

$$@x_1=5 \rightarrow V_D = 40.14 - 50 \\ \Rightarrow V_D = -9.86$$

point of zero shear force

$$\Rightarrow V_n = 40.14 - 10x_1 = 0$$

$$\Rightarrow x_1 = 4.01m$$

$$M_{n1} = 40.14x_1 - 75.72 - 10x_1 \times \frac{x_1}{2} \quad @x_1=0 \rightarrow M_{C,R} = -75.72$$

$$@x_1=5m \rightarrow M_D = 40.14 \times 5 - 75.72 - 5(5)^2$$

$$\Rightarrow M_D = 200.7 - 75.72 - 125$$

$$\Rightarrow M_D = -0.02 \approx 0$$

$$@x_1=4.01$$

$$(M)_{max} = 40.14 \left(\frac{4.01}{4.01}\right) - 75.72 - 5(4.01)^2$$

$$\Rightarrow (M)_{max} = 161.12 - 75.72 - 80.56$$

$$\Rightarrow (M)_{max} = 4.84 \text{ KNM.}$$

