

Poker Test

- Based on Chi-square Test

Steps:-

S1: Define Hypothesis for testing independence as

$H_0: R, C \sim$ independently

$H_1: R, C \not\sim$ independently.

S2: Generate frequency distribution table for all possible combinations
Es apply Chi-square test

S3: Compute $\chi^2_{calc} = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i}$

S4: Determine $\chi^2_{table} = \chi^2_{\alpha, df}$

$$df = n - 1$$

Where n is total number of combinations

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SS compare X_{calc} & X_{tab}

if $X_{calc} < X_{tab}$

Accept H_0 .

* Variation of Poker Test.

1) For 3 digits

117 For 4 digits

1117 For 5 digits

Numerical 1 (For 3 digits)

Possible combinations

567 - All diff

555 - All Same

565 - One pair

diff)

Probability for all diff = $P(1^{st} \& 2^{nd} \& 3^{rd} \& 4^{th} \& 5^{th})$

~~$\times P(1^{st})$~~

223
232
322

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a) Probability all digits are diff

$$= P(2^{\text{nd}} \text{ digit diff from } 1^{\text{st}}) \times P(3^{\text{rd}} \text{ digit diff from } 1^{\text{st}} \text{ and } 2^{\text{nd}})$$

$$= 0.9 \times 0.8 = 0.72$$

b) Probability all digits are same

$$= P(2^{\text{nd}} \text{ same as } 1^{\text{st}}) \times P(3^{\text{rd}} \text{ same as } 1^{\text{st}})$$

$$= 0.1 \times 0.1 = 0.01$$

c) Probability of one pair

$$= P(2^{\text{nd}} \text{ diff than } 1^{\text{st}}) \times$$

$$P(2^{\text{nd}} \text{ and } 3^{\text{rd}} \text{ same}) \times 3C_2$$

$$= 0.9 \times 0.1 \times 3$$

$$= 0.27$$

OR

$$= 1 - 0.72 - 0.01$$

$$= 0.27$$

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Ques:- A sequence of 3 digits nos are generated and analysis indicates that

560 have 3 diff digits

6080 contain 3 like digits

380 contain one pair of like digits

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Based on Poker Test, test for independence use $\alpha = 0.05$

S₁ Define Hypothesis

S₂ Generate frequency table & apply Chi-square test

Comb ⁿ	O_i	E_i	$\frac{(O_i - E_i)^2}{E_i}$
3 diff digits	560	0.72×1000 $= 720$	$= 35.55$
3 like digits	60	$= 0.01 \times 1000$ $= 10$	$= 280$
Exactly 1 pair	380	$= 0.29 \times 1000$ $= 290$	$= 44.81$

Here $N = 1000$

$$\chi^2_{\text{calc}} = \chi^2_0 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i}$$

Where n is total number of combⁿ possible

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$$= 330.36$$

$$S_4:- \chi^2_{n-1} = \chi^2_{0.05/2} = 5.99$$

So Compare

$$\chi^2_{\text{calc}} > \chi^2_{\text{tab}}$$

So reject H_0 .

For 4 digits possible combinations are:-

1234 - All diff

1111 - All same

1123 - One pair

1122 - Two pair

1112 - Three of a kind

$$\begin{aligned} P(\text{All diff}) &= P(\text{2nd diff from first}) \\ &\times P(\text{3rd diff from 1st and 2nd}) \\ &\times P(\text{4th diff from 1st, 2nd \& 3rd}) \end{aligned}$$

$$= 0.9 \times 0.8 \times 0.7 = 0.504$$

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$$\begin{aligned}
 2) P(\text{All same}) &= P(\text{2nd same as 1st}) \times \\
 &P(\text{3rd same as 1st}) \times P(\text{4th same as 1st}) \\
 &= 0.1 \times 0.1 \times 0.1 \\
 &= 0.001
 \end{aligned}$$

$$\begin{aligned}
 3) P(\text{one pair}) &= {}^4C_2 \times P(\text{2nd same as 1st}) \times P(\text{3rd diff from 2nd}) \\
 &\times P(\text{4th diff from 2nd \& 3rd}) \\
 &= {}^4C_2 \times 0.1 \times 0.9 \times 0.8 \\
 &= 0.432
 \end{aligned}$$

$$\begin{aligned}
 4) P(\text{Three of a kind}) &= {}^4C_3 \times P(\text{2nd and 1st same}) \times P(\text{3rd \& second same}) \\
 &\times P(\text{4th diff than first}) \\
 &= {}^4C_3 \times 0.1 \times 0.1 \times 0.9 \\
 &= 0.036
 \end{aligned}$$

$$\begin{aligned}
 5) P(\text{two pair}) &= 1 - 0.001 - 0.036 - 0.432 - 0.504 \\
 &= 0.027
 \end{aligned}$$

OR

$$\begin{aligned}
 &= \frac{{}^4C_2}{2!} \times (\text{1st and 2nd same}) \times (\text{3rd diff from 1st}) \times (\text{4th \& 3rd same})
 \end{aligned}$$

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$$= \frac{4C2}{2!} \times 0.1 \times 0.9 \times 0.1$$
$$= 0.027$$

For 5 digits

Possible combinations

1 2 3 4 5 - All diff

1 1 1 1 1 - All same

1 1 2 3 4 :- Exactly one pair

1 1 1 2 3 :- 3 of a kind

1 1 1 1 2 :- 4 of a kind

1 1 2 2 3 :- Exactly two pair

1 1 1 2 2 :- Full house

$$P(\text{all diff}) = 0.9 \times 0.8 \times 0.7 \times 0.6$$
$$=$$

$$P(\text{all same}) = 0.1 \times 0.1 \times 0.1 \times 0.1$$
$$= 0.01\%$$
$$= 0.0001$$

$$nCr = \frac{n!}{(n-r)!r!}$$

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$$P(3 \text{ of a kind}) = \cancel{P(0.1 \times 0.1 \times 0.1 \times 0.9 \times 0.8 \times 5C_3)} = 0.072$$

$$P(\text{Exactly one pair}) = 0.1 \times 0.9 \times 0.8 \times 0.7 \times 5C_2 = 0.5040$$

$$P(\text{Two pairs}) = \frac{5C_2}{2!} \times 0.1 \times 0.9 \times 0.1 \times 0.8 = 0.1080$$

$$P(4 \text{ of a kind}) = 5C_4 \times 0.1 \times 0.1 \times 0.9 \times 0.1 = 0.0045$$

$$P(\text{Full house}) = 1 - \text{Above all} = 0.009$$