

$$\begin{array}{r} \cancel{79,43,12} \\ + 15,88,624.085 \\ - \cancel{7,50,000} \end{array}$$

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## Assignment - Economics

### Chapter-3

Equivalent Worth Method.

Q.NO. 1  $\Rightarrow$

Investment life = 3 year

MARR = 10%.

present worth and future worth of each project.

Project's Cash flow (Rs).

N	A	B	C	D
0	-1000	-1000	-1000	-1000
1	0	600	1200	900
2	0	800	800	900
3	8000	1500	1500	1800

Soln:

for Project (A).

$$\begin{aligned}
 \text{Present Worth (Pw)} &= -1000 + 0 + 0 + 8000 \times \\
 &= P_0 + P_1 + P_2 + P_3 \\
 &= P_0 + P_1 + P_2 + A(P/A, 10\%, 3) \\
 &= -1000 + 8000 \times \frac{[(1+0.1)^3 - 1]}{0.1 \times (1+0.1)^3} \\
 &= -1000 + 
 \end{aligned}$$

$$\begin{aligned}
 \text{Present worth } (P_w) &= P_0 + P_1 + P_2 + P_3 \\
 &= P_0 + F(P/F, 10\%, 1) + F(P/F, 10\%, 2) \\
 &\quad + F_3(P/F, 10\%, 3) \\
 &= -1000 + 8000 \times [1+0.1]^{-3} \\
 &= -1000 + 2253.94 \\
 &= \text{Rs } 1253.94
 \end{aligned}$$

$$\begin{aligned}
 \text{Future worth } (F_w) &= f_0 + f_1 + f_2 + f_3 \\
 &= -1000 \times [F/P, 10\%, 3] \\
 &\quad + 3000 \\
 &= -1000 \times [1.1^3 - 1] + 3000 \\
 &= -1000 \times [1.1^3] + 3000 \\
 &= -1331 + 3000 \\
 &= \text{Rs } 1669
 \end{aligned}$$

for Project B.

$$\text{Present worth } (P_w) = P_0 + P_1 + P_2 + P_3$$

functionally

$$P = F(P/F, 10, N)$$

$$\begin{aligned}
 P_w &= -1000 + \frac{600}{(1.1)^1} + \frac{800}{(1.1)^2} + \frac{1500}{(1.1)^3} \\
 &= 1333.58
 \end{aligned}$$

future worth ( $F_w$ ) =  $f_0 + f_1 + f_2 + f_3$   
 functionally,  
 $f = P(F/P, 10\%, N)$

thus  
 $F_w = -1000 \times [1.1]^3 + 600 \times [1.1]^2 + 800 \times [1.1]^1 + 1500$   
 $= \text{Rs } 1775.$

for Project C.

present worth ( $P_w$ ) =  $p_0 + p_1 + p_2 + p_3$   
 functionally,  
 $P = F(P/F, 10\%, N)$ .

thus

$$P_w = -1000 + \frac{1200}{1.1^1} + \frac{800}{1.1^2} + \frac{1500}{1.1^3}$$

$$= \text{Rs } 1879.038$$

And,

future worth ( $F_w$ ) =  $F_0 + F_1 + F_2 + F_3$   
 functionally,  
 $F = P(F/P, 10\%, N)$ .

$$F_w = 1500 + 800[1.1]^1 + 1200[1.1]^2 + 100 \times [1.1]^3$$

$$= \text{Rs } 2501.$$

for Project D,

Present worth ( $P_w$ ) =  $P_0 + P_1 + P_2 + P_3$ .

functionally

$$P = F(P/F, 10\%, N)$$

Thus,

$$P_w = -1000 + \frac{900}{1.1} + \frac{900}{1.1^2} + \frac{1800}{1.1^3}$$

$$= 1914.35.$$

Again,

future worth ( $F_w$ ) =  $F_0 + f_1 + f_2 + f_3$ .

functionally.

$$F = P(P/F, 10\%, N)$$

Thus,

$$F_w = -1000 \times [1.1]^3 + 900 \times [1.1]^2 + 900 \times [1.1] + 1800 \\ = 2548.$$

Note!

In Every questions future worth can be directly calculated if we have present worth.  
i.e.

$$F_w(A) = P_w(A) \times [1+0.1]^3 = 1253.94 \times 1.1^3 = 1668.994$$

$$F_w(B) = P_w(B) \times [1+0.1]^3 = 1383.58 \times 1.1^3 = 1775$$

$$F_w(C) = P_w(C) \times [1+0.1]^3 = 1879.038 \times 1.1^3 = 2501$$

$$F_w(D) = P_w(D) \times [1+0.1]^3 = 1914.35 \times 1.1^3 = 2548.$$

Q. NO. 2  $\Rightarrow$

Interest Rate (I) = 10%.

Time Period (N) = 4 Years

Money withdraw.

Year 1: RS 25,000

Year 2: RS 3,000

Year 3: 0.

Year 4: RS 5000.

Cash flow diagram,

25,000      3,000      0      5,000 .

0 ↑      1 ↑      2 ↑

$\downarrow P_w = ?$

functionally:  $P = F(P/F, 10\%, N)$ .

We know.

Present worth ( $P_w$ ) =  $P_1 + P_2 + P_3 + P_4$ .

$$= \frac{25000}{[1+0.1]^1} + \frac{3000}{[1+0.1]^2} + 0 + \frac{5000}{[1+0.1]^4}$$

$$= \text{RS } 28621.678$$

$\therefore$  RS 28621.678 should be deposited Now.

Q. NO. B =>

Given

Initial investment ( $I$ ) = Rs 80,00,000.

Savings = Rs 12,00,000

operation and maintenance cost = Rs 2,00,50,000.

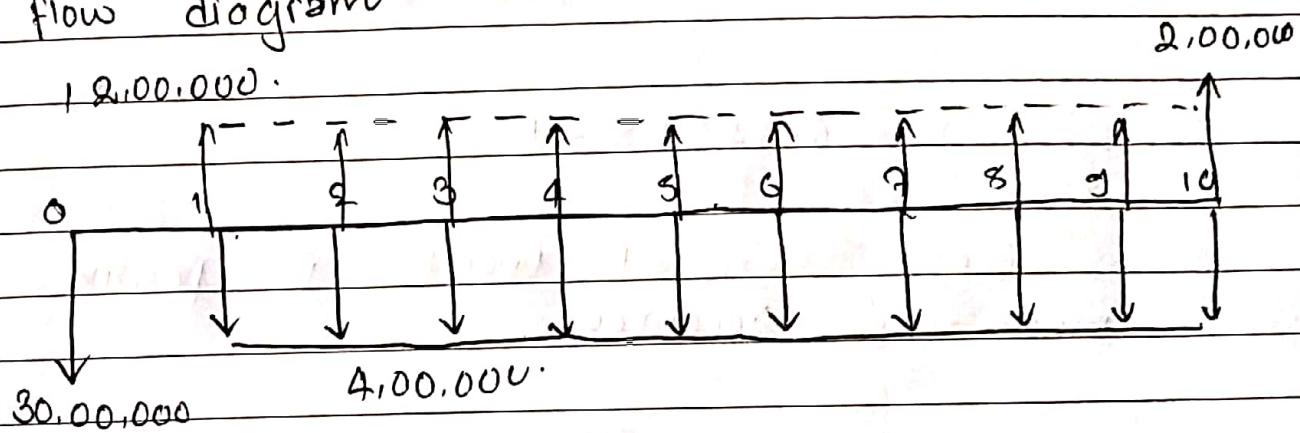
useful life ( $N$ ) = 10 years.

Annual Taxes, increment = Rs 1,50,000.

Salvage value ( $S$ ) = 2,00,000.

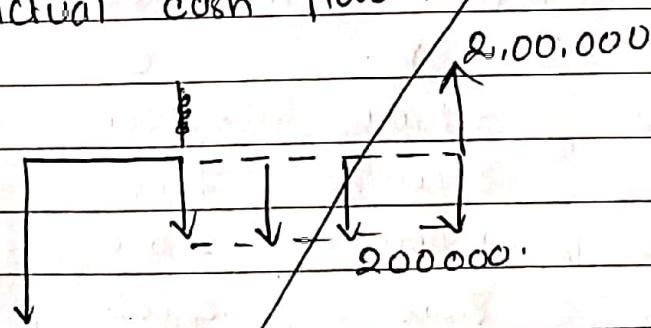
MARR = 18%.

Cash flow diagram



Now,

Actual cash flow is

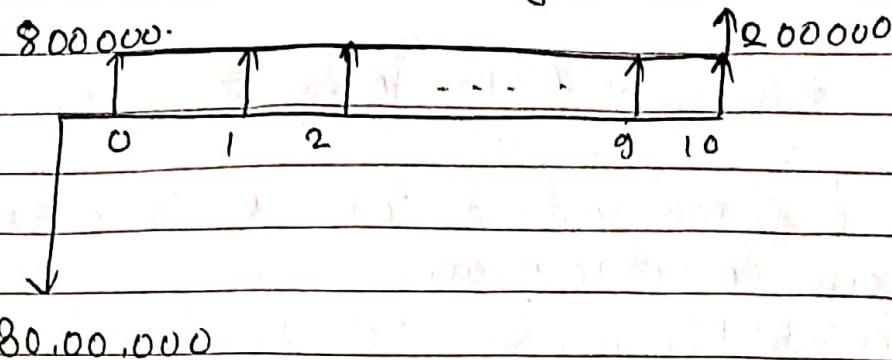


$$\text{Present worth (PW)} = -30,00,000 - \frac{200000 \times [1 - 1.18^{10}]}{0.18 \times 1.18^{10}}$$

$$+ \frac{200000}{1.18^{10}}$$

=

## Actual Cash flow diagram



Now, Present worth of 18% is,

$$\begin{aligned}
 &= -8000000 + 800000 \frac{(1.18^{10} - 1)}{1.18^{10} \times 0.18} + 200000 \times (1.18)^{10} \\
 &= \text{Rs } 633481.929
 \end{aligned}$$

Since Present worth is positive, the investment is accepted.

Q. NO. 4  $\Rightarrow$

## Project cash flow.

N	A	B	C	D
0	-2,500	-1,000	-2,500	-3,000
1	5,400	3,000	7,000	1,500
2	14,400	1,000	2,000	5,500
3	7,200	3,000	4,000	6,500

$$\text{MARR} = 10\%$$

Solution:-

for Project A.

$$\text{future worth } (F_w(10\%)) = f_0 + f_1 + f_2 + f_3$$

functionally,

$$F_w = P(F/P, 10\%, N)$$

thus:

$$\begin{aligned} F_w(10\%) &= 7200 + 14,400 \times [1.1]^1 + 5400 \times [1.1]^2 \\ &\quad - 2500 \times [1.1]^3 \\ &= 26246.5 \end{aligned}$$

for Project B.

$$\text{future worth } (F_w(10\%)) = f_0 + f_1 + f_2 + f_3$$

functionally,

$$F_w = P(F/P, 10\%, N)$$

thus,

$$\begin{aligned} F_w(10\%) &= f_0 + f_1 + f_2 + f_3 \\ &= 8000 + 1000 \times [1.1] + 8000 \times [1.1]^2 \\ &\quad - 1000 \times [1.1]^3 \\ &= \text{Rs } 6399 \end{aligned}$$

for Project C.

future worth ( $f_w(10\%) = f_0 + f_1 + f_2 + f_3$ )  
functionally,  
 $f_w = P(F/P, 10\%, N)$ .

Thus,

$$f_w(10\%) = 4000 + 2000 \times [1.1] + 4000 \times [1.1]^2 - 2500 \times [1.1]^3 \\ = \text{RS } 11842.5$$

for Project D.

future worth ( $f_w(10\%) = f_0 + f_1 + f_2 + f_3$ )  
functionally,  
 $f_w = P(F/P, 10\%, N)$

Thus,

$$f_w(10\%) = 6500 + 5500 \times [1.1] + 1500 \times [1.1]^2 - 3300 \times [1.1]^3 \\ = \text{RS } 10870.$$

Since, future worth of the Project A is highest it should be selected.

Q.NO.5 :-

Initial investment ( $F$ ) = 55,000

Net cash flow ( $y_1$ ) = 5000

Gradient Amount ( $A$ ) = 2500 per year.

Useful life ( $N$ ) = 10 years.

Salvage value ( $S$ ) = 6,000

Interest Rate ( $i$ ) = 12%.

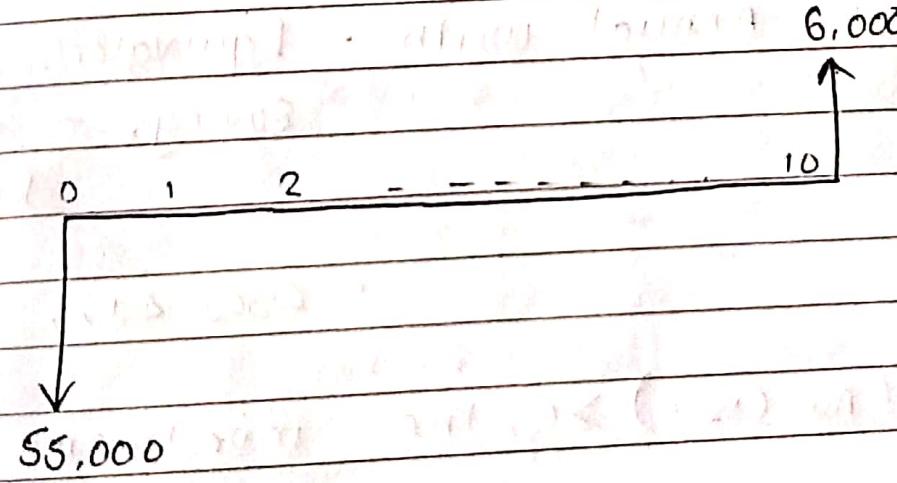
a) Determine the annual capital cost (ownership cost) for the equipment (9392.224).

b) Determine equivalent Annual Savings (Revenue)

c) Determine if this is wise investment.

Soln:

Cash flow diagram



i) Annual capital recovery cost =  $(55,000 - 6000)(A/P, 12\%, 10)$   
 $+ 6000 \times 0.12$ .

$$= 49000 \times \left[ \frac{0.12 \times (1.12)^{10}}{(1.12)^{10} - 1} \right] + 720$$

$$= 9392.224$$

## Equivalent Annual Savings

$$= 5,000 + 2500 (A/G, 12\%, 10)$$

$$= 5,000 + 2500 \left[ \frac{(1.12)^{10} - 1}{0.12} \right]$$

$$= 13961.63 \text{ #}$$

~~At Present worth (NPW) = ?~~

Equivalent To determine if the investment is safe or not.

Equivalent Annual Worth = Equivalent Annual Savings - Capital Recovery

$$= 4569.41,$$

$\therefore$  As  $(Aw(12\%) > 0)$ , the investment is safe.

else,  
e) Net present worth (NPW) = ?

$$\text{PW of future cash flow} = 5000 \left( P/A, 12\%, 10 \right) \\ + 2500 \left( P/G, 12\%, 10 \right) + 6000 \\ \left( P/F, 12\%, 10 \right)$$

$$= 5000 \times \frac{(1.12)^{10} - 1}{0.12}$$

+

$$\frac{2500}{0.12^2} \left( \frac{1.12^{10} - 1}{0.12} \right) + 6000 \times (1.12)^{-10}$$

$$= 80818.1767$$

$$\text{NPW} = \text{PW of future cash flow} - \text{Initial investment} \\ = 80818.1767 - 50500 \\ = 25818.1767$$

As, (NPW > 0). The investment is wise

Again,  
second condition.  
 $MARR = 10\%$

Q. NO. 6  $\Rightarrow$

Down payment = Rs 4000  
Interest =  $7\%$ .

$$\text{Remaining balance} = \text{Rs } 40000 - \text{Rs } 4000 \\ = \text{Rs } 36000$$

Now,

Calculating installments.

$$A = P(A/P, 7\%, 5) \\ = \frac{-36000 (0.7 \times 1.7^5)}{1.7^5 - 1} \\ = \text{Rs } -8780.065$$

Converting the down payment to annual form.

$$A = P(A/P, 10\%, 5) \\ = \frac{-4000 (0.1 \times 1.15^5)}{1.15^5 - 1} \\ = \text{Rs } 1055.18$$

$$\text{Total worth } Aw = \text{Rs } (-8780.065 - 1055.18) \\ = \text{Rs } -9835.24$$

$$\begin{aligned}
 &= -\frac{500000}{0.1} \times [(1.1)^{10} - 1] - \frac{50000}{0.1} \times [(1.1)^{10} - 1] \\
 &\quad + \frac{50000}{0.1} \times [(1.1)^{10} - 1] + \frac{10 \times 50000}{0.1} \\
 &= -360000 \times [(1.1)^{10} - 1] + 500000
 \end{aligned}$$

for buying entire machine at once,

$$\text{Investment} = \text{Rs } 86000$$

so, converting to annual form.

$$\begin{aligned}
 AW &= -36000 \left( P/A, 10\%, 5 \right) \\
 &= -36000 \frac{(1.15 \times 0.1)}{(1.15 - 1)} \\
 &= \text{Rs } -9496.70
 \end{aligned}$$

since,  $AW$  of buying the machine in cash >  
 $AW$  of buying in down payment

The machine must be bought in cash.

S. NO. 7 =>

Cost of workstations = Rs 25000 each

Total cost of three engineering workstations

$$= 25000 \times 3 \\ = 75000$$

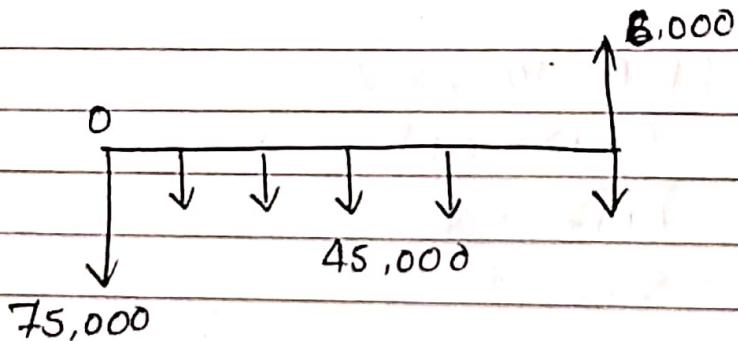
useful life period (N) = 5 years.

Salvage value (S) = Rs 2000.

Operating and Maintenance Cost = Rs 15,000 per year

$$= \text{Rs } 15,000$$

MARR = 15%.



Annual Expenses (E) = Rs 45,000

Capital Recovery cost (CR)

$$= I(A/P, i\%, N) - S(A/F, i\%, N)$$

$$= 75,000 \times \left[ \frac{0.15 \times (1.15)^5}{(1.15)^5 - 1} \right] - 6000 \times (0.1483)$$

$$= 22373.666 - 889.8933$$

$$= 21483.7720$$

NOW.

$$\text{Actual Cost} = E + CR.$$

$$= \text{RS } (45,000 + 81483.773)$$

$$= \text{RS } 66483.773.$$

Hence, the equivalent annual costs for operating and engineering center = RS 66483.773

Q. NO. 8  $\Rightarrow$

Given,

$$\text{Annual income (A)} = \text{RS } 5,00,000$$

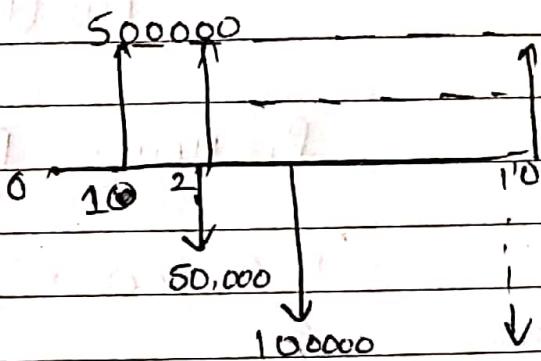
$$\text{Decreasing value & Rate} = \text{RS } 50,000$$

$$\text{Useful life (N)} = 10 \text{ years}$$

$$\text{Future worth (FW)} = ?$$

$$\text{MARR} = 10\%$$

Cash flow diagram



Using future worth formulation,

$$fw(0\%) = F_A - FG$$

$$fw(10\%) = +5,00,000 (f/A; 10\%, 10)$$

$$\rightarrow G(F/G, 10\%, 10)$$

$$fw(10\%) = +5,00,000 \left[ \frac{(1+0.1)^{10}-1}{0.1} \right] + -\frac{50,000}{0.1} \left[ \frac{1-1^{10}}{0.1} \right]$$

$$+ \frac{10 \times 50,000}{0.1}$$

$$= 50,00,000.$$

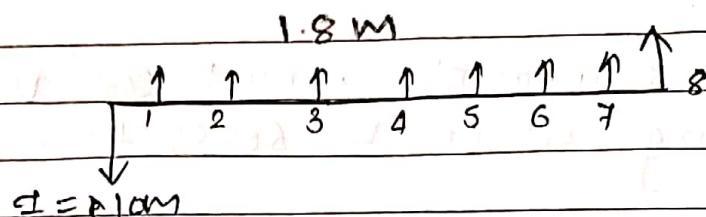
The equivalent fw using gradient series formula is RS 50,00,000.

## RATE OF RETURN METHOD

Q. NO. 9 =>

Solution:

$$S = 1M$$



$$MARR = 10\%$$

by calc (shift + calc)

$$0.1018$$

Using PW Method,

$$PW(i^*) = 0$$

$$P_{inflow} - P_{outflow} = 0$$

$$1800000 \times \frac{(1+i^*)^8 - 1}{i^* \times (1+i^*)^8} + 1,000,000 (1+i^*)^{-8}$$

$$- 10,000,000 = 0.1 \quad \dots \quad (1)$$

By hit and trial.

$$\text{At } i^* = 10\% = PW = 69374.536$$

$$\text{At } i^* = 15\%, \quad PW = -1595919.512$$

$\therefore$  The  $i^*$  lies between  $10\%$  and  $15\%$ .

Using linear interpolation.

$$\frac{i^* - 10\%}{15\% - 10\%} = \frac{69374.536 - 0}{69374.536 - (-1595919.512)}$$

$$i^* = 10.208\%$$

Using  $i^* = 10.208\%$  in eqn ①,  $P_w = -9907.272$

At  $i^* = 10\%$ ,  $P_w = 69374.536$

$i^* = 10.20890\%$ ,  $P_w = -9907.272$

Using linear interpolation.

$$\frac{i^* - 10\%}{10.208\% - 10\%} = \frac{0 - 69374.536}{-9907.272 - 69374.536}$$

$$\Rightarrow i^* = 10.182\%$$

Using  $i^* = 10.182\%$ ,  $P_w = 50.299$

At  $i^* = 10\%$ ,  $P_w = 69374.536$ .

$i^* = 10.182\%$ ,  $P_w = -50.299$ .

Using liner interpolation.

$$\frac{i^* - 10\%}{10.182\% - 10\%} = \frac{0 - 69374.536}{-50.299 - 69374.536}$$

$$\Rightarrow i^* = 10.181\%$$

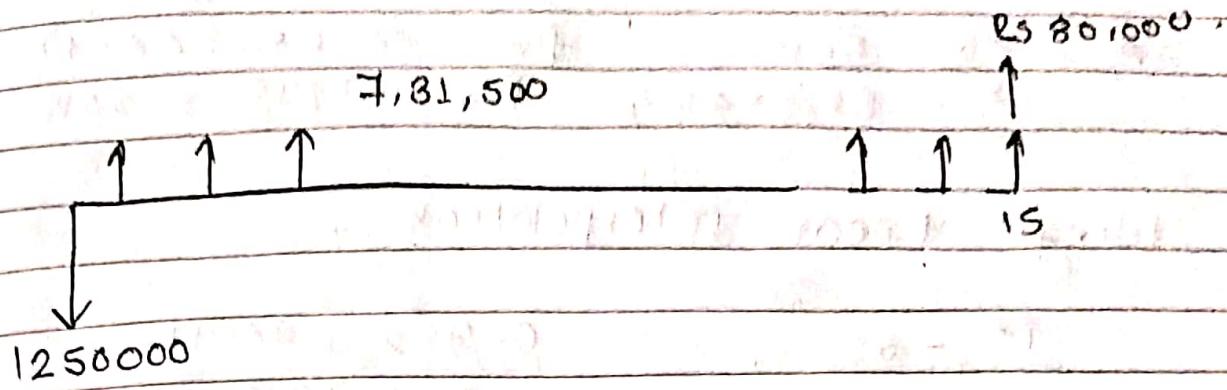
Using  $i^* = 10.181\%$ ,  $P_w = 329.117$ .

$i^* = 10.181 > MARR (10\%)$ , so the corporation should accept the project.

Now, Unrecovered balance:

	1.10181	11018100	↓ 1.8m	10156594.76
	↓ 1.8m	9218100	↓ 1.8m	9207319.624
	↓ 1.8m	↓ 1.10181	↓ 1.8m	8161458.835
	↓ 1.8m	7407319.624	↓ 1.8m	7009118.959
	↓ 1.8m	6361458.835	↓ 1.8m	5739459.35
	↓ 1.8m	5209118.959	↓ 1.8m	4340335.718
	↓ 1.8m	3939459.36	↓ 1.8m	2540535.714
0	1	2	3	4
5	6	7	8	9

S. N.O. 10.  $\Rightarrow$



Given

$$MARR = 15\%$$

using PW formulation,

$$PW(i^*) = 0$$

i.  $PW_{inflow} - PW_{outflow} = 0$

$$\left\{ \frac{781500}{1^* \times (1+i^*)^{15}} \times \frac{(1+i^*)^{-1}}{(1+i^*)^{15}} + 80,000 (1+i^*)^{-15} \right\} - 12000 = 0$$

By hit and trial method,

$$At i^* = 55\% \quad PW = 78254.44097$$

$$i^* = 60\% \quad PW = -81822.40297$$

using linear interpolation.

$$i^* - 55\% = \frac{0 - 78254.44097}{-81822.40297 - 78254.44097}$$

$$\Rightarrow i^* = 0.585545692$$

Using  $i^* = 58.5545$  in eqn (1)  $P_w = -1900.8989$

At,  $i^* = 55\%$ ,  $P_w = 78254.44097$   
 $i^* = 58.5545\%$ ,  $P_w = -1898.567418$ .

Using linear interpolation,

$$\frac{i^* - 55\%}{58.5545 - 55\%} = \frac{0 - 78254.44097}{-1898.567418 - 78254.44097}$$

$$\Rightarrow i^* = 58.47\%$$

Using  $i^* = 58.47\%$  in eqn (1),  $P_w = -104.288$ .

At

$$i^* = 55\%, P_w = 78254.44097$$

$$i^* = 58.47\%, P_w = -104.288$$

Using linear interpolation,

$$\frac{i^* - 55\%}{58.47\% - 55\%} = \frac{0 - 78254.44097}{-104.288 - 78254.44097}$$

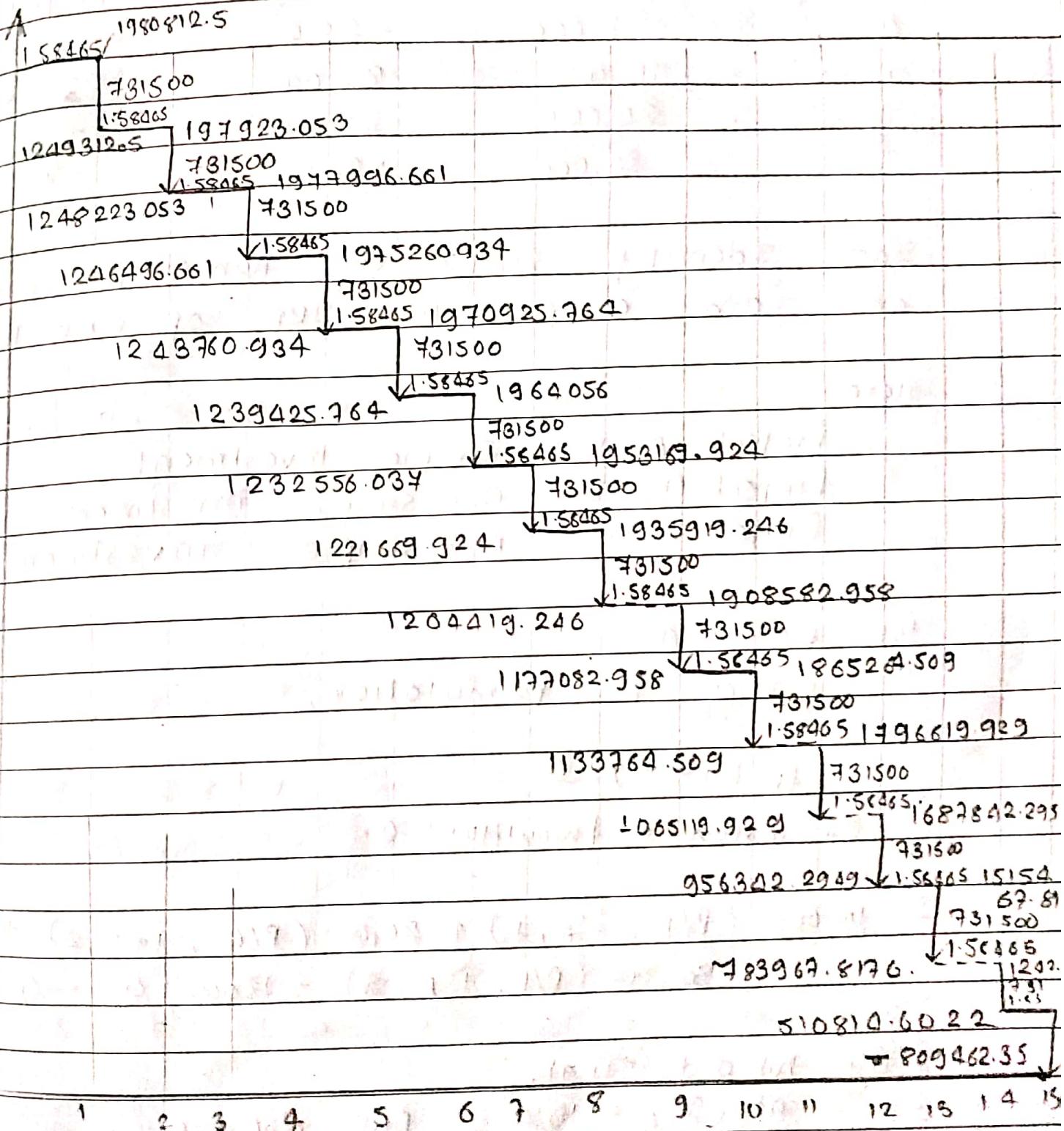
$$\Rightarrow i^* = 58.465\%$$

Using  $i^* = 58.465\%$  in eqn (1),  $P_w = 204$ .



Here IRR ( $58.465\%$ ) > MARR ( $18\%$ ).

Thus, the investment is Acceptable.



Q. NO. 11 :-

Year.	Project A	Net cash flow (Rs)	Project C
0	- 18,000	Project B	- 56,500
1	16,000	32,000	25,000
2	20,000	22,000	- 64,500
3	36,000	- 22,000	- 78,845

Find identify simple and non-simple investment and compute the IRR of each project.

here,

Project A is simple investment

Project B is non-simple investment

Project C is non-simple investment

for Project A .

using PW formulation ,

$$PW(i^* \%) = 0$$

$$PW_{inflow} - PW_{outflow} = 0$$

$$10,000 (P/F, i^A, 1) + 20,000 (P/A, i^A, 2) + \\ 36,000 (P/F, i^A, 3) - 18,000 = 0 \quad \text{---(1)}$$

By hit and trial ,

$$\text{At } i^A = 18\%, \quad PW = 250.868$$

$$i^{A*} = 18\%, \quad PW = -157.484$$



Using linear interpolation,

$$\frac{i_A^* - 73\%}{75\% - 73\%} = \frac{0 - 256.888}{-157.434 - 256.888}$$

$$\Rightarrow i_A^* = 74.24\%$$

wing  $i_A^* = 74.24\%$  in ①,  $P_w = -1.847$

At  $i_A^* = 73\%$ ,  $P_w = 256.888$

$$i_A^* = 74.24\%, P_w = -1.847$$

Using linear interpolation,

$$\frac{i_A^* - 73\%}{74.24\% - 73\%} = \frac{0 - 256.888}{-1.847 - 256.888}$$

$$\Rightarrow i_A^* = 74.231\%$$

using  $i_A^* = 74.231\%$  in ①,  $P_w = 0.00849\%$

for Project B.

Using  $P_w$  formulation,

$$P_w (i_B^* \%) = 0$$

$$P_{w\text{inflow}} - P_{w\text{outflow}} = 0 \\ 82,000 (P/F, i_B^*, 1) + 82,000 (F/F, i_B^*, 2) - \\ 22,000 (P/F, i_B^*, 3) - 20,000 = 0 \quad \text{--- (2)}$$

By hit and Trial.

$$\text{At } i_B^* = 110\% , P_w = 118.777$$

$$i_B^* = 118\% , P_w = -199.886$$

Using linear interpolation,

$$\frac{i_B^* - 110\%}{118\% - 110\%} = \frac{0 - 118.777}{-199.886 - 188.777}$$

$$\Rightarrow i_B^* = 111.118\%$$

Using  $i_B^* = 111.118\%$  in eq<sup>n</sup> ②,  $Bw = -1.025$ .

$$\text{At, } i_B^* = 110\% , P_w = 118.777$$

$$i_B^* = 111.118\% , P_w = -1.025$$

Using linear interpolation,

$$\frac{i_B^* - 110\%}{111.118\% - 110\%} = \frac{0 + 18.77}{-1.025 - 118.77}$$

$$\Rightarrow i_B^* = 111.108\%$$

Using  $i_B^* = 111.108\%$  in eq<sup>n</sup> ②,  $P_w = 0.09$ .

Thus - irr of Project B is  $111.108\%$ .

for Project C,  
using PW formulation,

$$PW(i^*) = 0$$

$$P_{\text{inflow}} - P_{\text{outflow}} = 0$$

$$8500(P/F, i^*, 1) - 6459(P/F, i^*, 2) - 8345(P/F, i^*, 3) \\ - 56500 = 0 \quad \text{--- (3)}$$

using calculator,  
→ Not available.

i.e. calculation of IRR is NOT feasible for such type of cashflow.

12]. calculate the ERR for following Project if MRR = 15%.

a) EOY

Net Cash Flow.

0

- 25,000

1

8,000

2

3

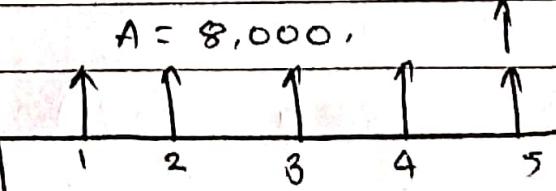
4

5.

13,000

5,000

$$A = 8,000$$



$$I = 25,000$$

Soln:

Step 1: Discount all cash outflow at point zero at 15% per compounding period.

So,

$$\text{Net cash flow outflow} = \text{Rs } 25,000 = P \sim \textcircled{1}$$

Step 2: Compounding all cash inflow to year 5 at

$$15\% \cdot 8,000 (\text{F/A}, 15\%, 5) + 5000 = \\ = 8000 \times [(1.15)^5 - 1] + 5,000 \\ = \text{Rs } 58989.05 \quad \textcircled{ii}$$

Step 3: Establishing the equivalence between two eq's

$$25000(F/P, i, 5) = 58989.05$$

$$\text{or, } 25,000 (1+i)^5 = 58989.05$$

$$\Rightarrow i' = 18.71\%$$

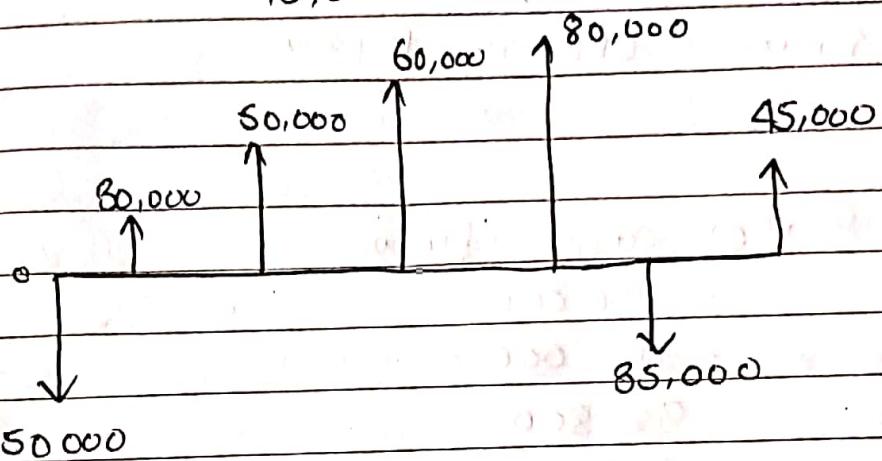
Since ERR (18.71%) > MARR (15%)

So, the project is accepted.

∴ The Required ERR is 18.71%.

b) Eoy NET cash flow

0	- 1,50,000
1	80,000
2	50,000
3	60,000
4	- 35,000 80,000
5	- 85,000
6	45,000



Step 1: Discount all the cash outflow to year 0 at 15%.

$$150,000 + 85,000 (P/F, 15\%, 5).$$

$$= \text{Rs } 1,67,401.1857$$

Step 2: Corresponding all the cash inflow to year 6 at 15%.

$$80,000 (F/P, 15\%, 5) + 50,000 (F/P, 15\%, 4) + 60,000 (F/P, 15\%, 3) + 80,000 (F/P, 15\%, 2) + 45,000$$

$$= \text{Rs } 389843.5281$$

Step 0: Establishing the equivalence between two eqns.

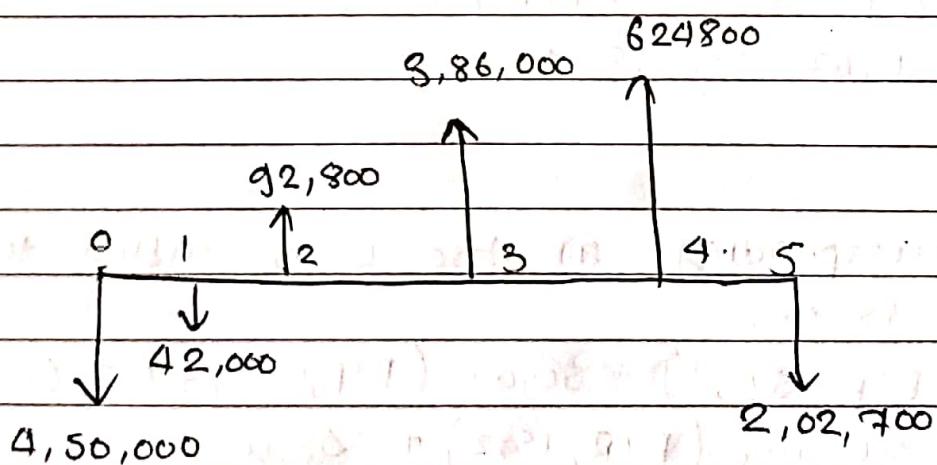
$$1167,401 \cdot 1857 (F/P, i\%, 6) = 3,89,843.528$$

$$1,67,401 \cdot 1857 (1+i)^6 = 319843.528$$

$$i = 15.13\%$$

Thus required ERR is 15.13%.

c)	EOY	Net cash flow
0		- 450 000
1		- 42,000
2		92,800
3		3,86,000
4		6,24,600
5		- 2,02,700



SOL:

Step 1: Discount all the cash outflow to year zero  
at 15%.

$$4,50,000 + 42,000 (P/F, 15\%, 1) + 2,02,200 (P/F, 15\%, 5) \\ = \text{RS } 587,2934.634$$

Step 2: Compounding all the cash outflow inflow  
to year 6 at 15%.

$$92,800 (F/P, 10\%, 3) + 3,86,000 (F/P, 10\%, 2) + 624 (F/P, 15\%, 1) \\ = 1358412.2$$

Step 3: Establishing the equivalence between two eqn.

$$587299.4634 (F/P, i\%, 5) = 1358412.2$$

$$\text{or, } 587299.4634 (1+i)^5 = 1358412.2$$

$$i\% = 18.259\%$$

Thus, Required ERR is 18.259%.

## \* Benefit Cost Analysis.

13. Find by using both types of B/C ratio using AW and PW method.
- i) Investment = Rs 25000
  - ii) Annual Benefit = Rs 75,000
  - iii) Annual Cost = Rs 15,000
  - iv) Salvage Value = Rs 25,000
  - v) MARR = 12%
  - vi) Number of Years = 10.

Using PW formulation,

$$\text{Capital Recovery (CR)} = 25000 \left( A/P, 12\%, 10 \right) - 25000 \left( A/F, 12\%, 10 \right)$$

$$= \frac{250,000 \times 0.12 \times (1.12)^{10}}{(1.12^{10} - 1)} - \frac{25000 \times 0.12}{(0.12(1.12^{10} - 1))}$$

$$= 42821.4369$$

So,

$$\text{Conventional B/C Ratio} = \frac{AW(B)}{CR + AW(O+M)}$$

$$= \frac{25,000}{42821.4369 + 15,000}$$

$$= 1.29.$$

Modified BIC Ratio =  $\frac{Aw(B) - Aw(O\&M)}{CR}$

$$= \frac{25000 - 15000}{42821.4369}$$

$$= 1.4$$

• Using fw formulation.

$$fw(B) = 75,000 (F/A, 12\%, 10) = 75,000 \times \frac{(1+12)^{10} - 1}{0.12}$$

$$= Rs 1316155.13$$

$$fw(O\&M) = 15000 \times (F/A, 12\%, 10)$$

$$= 15000 \times \frac{(1+12)^{10} - 1}{0.12}$$

$$= 263231.026$$

Now,

conventional BIC Ratio =  $\frac{fw(B)}{fw(F) - S + fw(O\&M)}$

$$= \frac{1316155.13}{776462.0521 - 25000 + 263231.82}$$

$$= 1.29$$

$$\text{Modified BIC Ratio} = \frac{fw(B) - fw(O&M)}{fw(F) - S}$$

$$= \frac{1816155.13 - 263231.026}{836462.0521 - 25000}$$

$$= 1.4 F$$

14. Sol'n:

Initial cost = 250,000

Annual revenue = 75,000 at the end of first year  
and increasing by RS 5,000 each year.

Annual O&M = 15,000

Salvage value = 25,000

MARR = 10%

Let N = 10 years

$$fw(F) = 250,000 \times (F/P, 10\%, 10)$$

$$= 250,000 \times (1.1)^{10}$$

$$= 648435.615$$

$$fw(B) = (75000) \times \frac{(1.1)^{10}-1}{0.1} + 5000 \times \left[ \frac{(1.1)^{10}-1}{0.1^2} - \frac{10 \times 5000}{0.1} \right]$$

$$= 149278.075$$

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$$FW(0\&M) = 15000 (F/A, 10\%, 10)$$
$$= 15000 \times \frac{(1.1)^{10} - 1}{0.1}$$
$$= 289061.369$$

Now,

Conventional B/C ratio =  $\frac{fw(B)}{fw(C) - S + FW(0\&M)}$

$$= \frac{1492178.075}{648435.815 - 25000 + 289061.30}$$

$$= 1.73,,$$

Modified B/C Ratio =  $\frac{fw(B) - FW(0\&M)}{fw(C) - S}$

$$= \frac{1492178.075 - 289061.369}{648435.815 - 25000}$$

$$= 2.01 \#$$

Q. NO. 15 :-

Soln:-

Initial Cost = RS 18,00,00,000

Annual Power Sales = RS 1,20,00,000

Annual Flood Control Saving = RS 50,00,000

Annual irrigation benefit = RS 80,00,000

Annual recreation benefit = RS 40,00,000

Annual Operating & maintenance costs = RS 50,00,000

Life of the project = 40 years.

MARR = 15%.

Soln:-

Using AW formulation,

$$CR = 18,00,00,000 \left( A/P, 15\%, 40 \right) - 0$$

$$= 18,00,00,000 \times 0.15 \times 1.15^{40} / (1.15^{40} - 1)$$

$$= RS 27101175.3$$

$$AW(B) = 1,20,00,000 + 50,00,000 + 80,00,000 + 40,00,000$$

$$= 290,00,000$$

$$AW(0&M) = RS 50,00,000 .$$

Now.

$$\text{Conventional B/C Ratio} = \frac{AW(B)}{CR + AW(0&M)}$$

$$= \underline{2,90,000}$$

$$\underline{271,01175.3 + 50,00,000}$$

$$= 0.903 < 1 \text{ (Rejected)}$$

$$\text{Modified BIC Ratio} = \frac{\text{Aw(B)} - \text{Aw(DM)}}{\text{CR}}$$

$$= \underline{290000 - 500000}$$

$$\underline{271,01175.3}$$

$$= 0.885 < 1 \text{ (reject) } //$$

## \* Payback Period Method

Q. NO. 16  $\Rightarrow$

Soln:

~~MARR = 20%~~

Merits:

- Simple to use and easy to understand
- It is interpreted in tangible terms (in years)
- o It doesn't require any assumption in term of timing, life time & interest rates.
- Quick solutions.
- Useful in case of uncertainty

Demerits:

- Not all cash flow are covered
- No concrete decision criteria that indicate whether the investment increases the value
- Not realistic and ignores profitability

### Simple payback Period

- i) It doesn't consider time value of money ( $i=0$ )
- ii) It doesn't use discounted cash flow, thus is less accurate

### Discounted Payback Period

- i) It considers time value of money.
- ii) It uses discounted cash flow, thus is more accurate.

$T = 5$  years (Assumption)

Period	Cash	FV@ 20%	Cumulative
0	-25,000	-25,000	-25,000
1	8,000	6,667	-18,333
2	8,000	5556	-12,133
3	8,000	4680	-8,147
4	8,000	3858	-4,289
5	18,000	5223	+934

here, the cumulative cash flow turns positive in year 5, therefore, payback period lie between year 4 and 5. By interpolating, we get the payback period =  $4 + \frac{4289}{5223} = 4.82$  years

Q.NO. 17/1

Project	Involvement (Rs)	Annual cash flow	Life in yrs
A	10,000	4,000	12
B	25,000	10,000	4
C	80,000	6,000	20
D	85,000	12,000	16

which project would be the best one?

for

P.T.O

For Project A.

Period	Cash	PW at 10%	Cumulative
0	- 10,000	- 10,000	- 10,000
1	4,000	3686.36	- 6386.64
2	"	3305.78	- 3057.56
3	"	3005.259	- 52.601
4	"	2732.054	2679.453
5	"	2483.685	5168.138

Here, cumulative cash flow is negative on year 3 and positive on year 4. Hence, the payback period lies between 3 and 4.

By interpolating,

$$8 + \frac{52.601}{2732.054} = 8.019$$

$$= 8.019 \text{ years}$$

For Project B.

n	flow	PW at 10%	Cumulative
0	- 25,000	- 25,000	- 25,000
1	10,000	9090.90	- 15,909.1
2	10,000	8264.46	- 7644.64
3	10,000	7513.148	- 121.492
4	10,000	6830.13	6698.638

Interpolating,  $8 + \frac{191.492}{6830.13} = 8.0192 \text{ years}$

for Project C.

n.	flow	PW at 10%	commulative
0	- 30,000	- 30,000	- 30,000
1	6,000	5454.54	- 24545.46
2	6,000	4958.67	- 19586.79
3	6,000	4507.88	- 15078.92
4	6,000	4098.08	- 10980.83
5	6,000	3725.527	- 2255.303
6	6,000	3386.84	- 3868.463
7	6,000	3078.948	- 789.525
8	6,000	2799.048	2009.529

Interpolating,  $7 + \frac{789.515}{2799.048} = 7.28$  years  $\approx$   
~~2799.048~~

for Project D,

n	flow	Pw at 10%	commulative
0	-35,000	-35,000	-35,000
1	12,000	10909.09	-24090.91
2	"	9917.35	-14173.56
3	"	9015.77	-5157.79
4	"	8196.16 <sup>2</sup>	8038.371

Interpolating

$$3 + \frac{5157.79}{8196.162} = 3.629 \text{ years},$$

Since payback period of Project A and Project B is less than other, I would recommend Project A and Project B as the best one.,

Q. NO. 18 :-

EOY	A	B	C	D
0	-1500	-4000	4500	3000
1	300	2000	2000	5000
2	"	1500	2000	8,000
3	"	1500	2000	2,000
4	"	500	2000	1,000
5	"	500	5000	1,000
6	"	1500		1,000
7	"			2,000
8	"			3,000

Q7

Soln?

for Q7 for Project A,

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$$\text{Payback Period} = \frac{1500}{300} = 5 \text{ years.}$$

for Project B.

Period

0

1

2

3

4

5

6

7

8

9

10

Net cash flow (Rs)

-4,000

2000

1500

1500

500

500

1500

1500

Cumulative cash flow

-4,000

-2,000

-5,000

1000

1500

2000

3500

Change is in between two and 3 years.

interpolating

~~2.5~~

$$2 + \frac{500}{1500}$$

1500

$$= 2.83 \text{ years.}$$

for Project C.

n

0

1

2

3

4

5

Net cash flow

-24500

2,000

"

"

5000

"

Cumulative

-4500

-2500

-500

1500

6500

11,500

There is sign change between 2<sup>nd</sup> and 3<sup>rd</sup> year.

So, interpolating,

$$2 + \frac{500}{2000} = 2.25 \text{ years.}$$

for Project D,

n	Net cash flow	Commulative
0	-3,000	-3,000
1	5,000	2000
2	3,000	5000
3	-2000	3,000
4	1000	4,000
5	1,000	5,000.

Here, cumulative cash flow turn positive in year 2,

interpolating,

$$0 + \frac{3000}{5000} = 0.6 \text{ years.}$$

c) Assuming  $i = 10\%$ . calculating discounted payback period.

for project A.

n	flow	Pw at 10%	commulative
0	1500	-1800	-1500
1	800	273	-1227
2	800	248	-979
3	"	226	-753
4	"	205	-548
5	"	187	-362
6	"	170	-192
7	"	150	-97
8	"	140	+108

Here commulative cash flow turns to positive in year 8.

So the payback period lies between 7 and 8.  
By interpolating

$$\text{payback period} = 7 + \frac{37}{140}$$

$$= 7.289$$

for Project B

Period	Flow	Pw at 10%	commulative
0	- 4000	- 4000	4000
1	2000	1819	- 2189
2	1500	1240	- 942
3	1500	1127	+ 186
4	500	842	+ 528
5	500	811	+ 839
6	1500	847	+ 1686.

Here commulative cash flow turns positive in year 3, so payback period lies between 2 and 3, By interpolating,

$$\text{Payback Period} = 2 + \frac{941}{186+941}$$

$$= 2.835 \text{ years}$$

Project C.

n	flow	Pw at 10%	commulative
0	- 4800	- 4500	- 4500
1	2000	1819	- 2681
2	2000	1653	- 1028
3	2000	1503	+ 425
4	5000	8415	+ 3090
5	5000	8105.	+ 6995.

here, commulative cash flow turns to tve in year 3, so the payback period lies between year 2 & 3.

ay interpolating

$$\text{Payback Period} = \frac{2 + 1028}{425 + 1028}$$

$$= 2.634 \text{ years}$$

Project D.

n	Flow	PW at 10% -	commulative
0	-3000	-3000	-3000
1	5000	4546	1548
2	3000	2479	4025

for input D, it is not meaningful to calculate payback period as commulative cash flow turns positive in year 1 #.

b)  $\Rightarrow$

It is Not meaningful to calculate payback period of project D as according to given cash flow, the payback period should lie between 0 & 1, but is it not possible for payback period to lie between 0 and 1, ~~but this is not~~ possin as initial investment can't be returned back without net Annual cash flow