

🧠 **Introduction**

🧠 **Working Principle and Torque Equation**

🧠 **Back EMF**

🧠 **Method of Excitation**

🧠 **Types of DC Motor**

🧠 **Performance Characteristics of DC Motors**

🧠 **Starting of DC Motors: 3 Point and 4 Point Starters** 🧠 **Speed Control of DC Motors: Field Control, Armature Control**

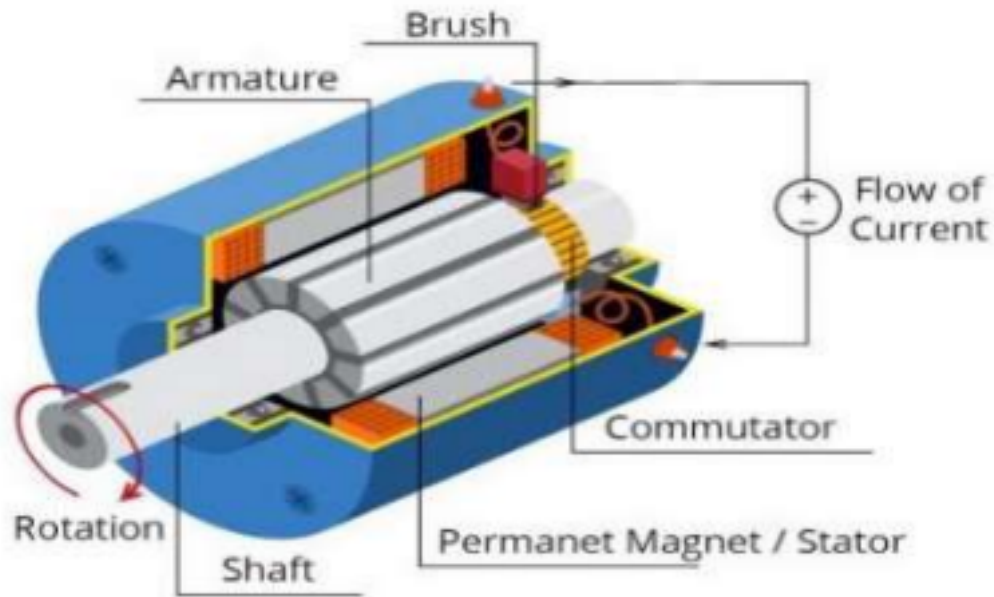
🧠 **Losses and Efficiency**

🧠 D. C. motors are seldom used in ordinary applications because

all electric supply companies furnish alternating current.

- 💡 However, for special applications such as in steel mills, mines and electric trains, it is advantageous to convert alternating current into direct current in order to use d.c. motors.
- 💡 The reason is that speed/torque characteristics of d.c. motors are much more superior to that of a.c. motors.
- 💡 Therefore, it is not surprising to note that for industrial drives, d.c. motors are as popular as 3-phase induction motors.
- 💡 An electric motor is a machine which converts electrical energy into mechanical energy whereas a generator is that machine which converts mechanical energy into electrical one.
- 💡 As regards fundamental principles, the d.c. motors are identical with the d.c. generators which have the same type of excitation i.e. a machine that operates as a motor will also operate satisfactorily as a generator.

- 💡 The only difference lies, however, in the mode of construction, which is due to the fact that the frame of the generator can as a rule be opened but those of motors should be either partly or totally enclosed.



### 💡 Generator action:

- 💡 An emf (voltage) is induced in a conductor if it moves through a magnetic field.

### 💡 Motor action:

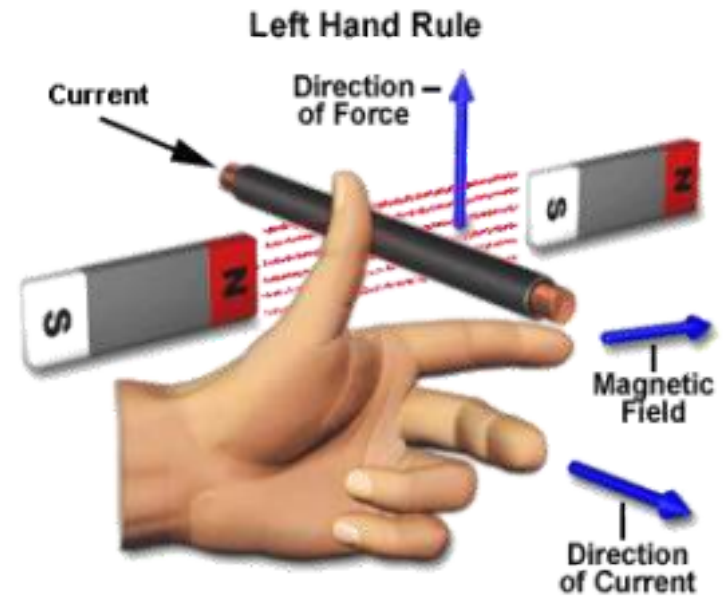
💡 A force is induced in a conductor that has a current going through it and placed in a magnetic field.

💡 Any DC machine can act either as a generator or as a

motor.

💡 A machine that converts d.c. power into mechanical power is known as a d.c. motor. 💡 Its operation is based on the principle that when a current carrying conductor is placed in a magnetic field, the conductor experiences a mechanical force.

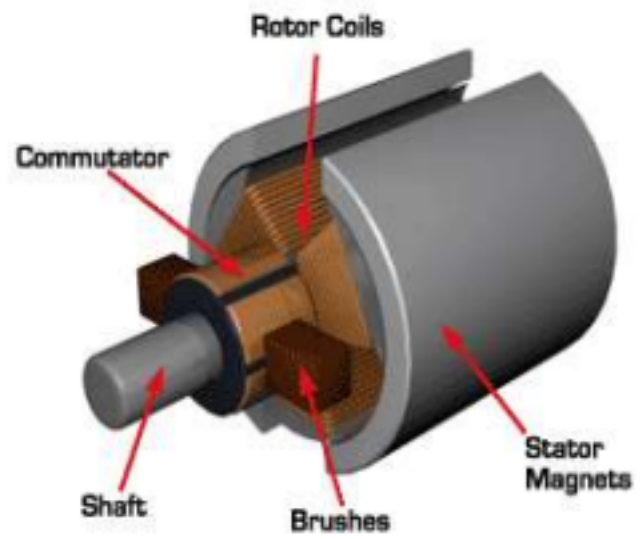
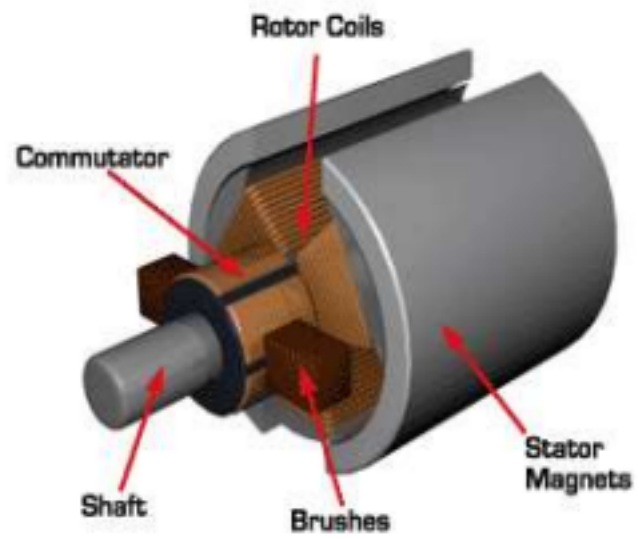
💡 The direction of this force is given by

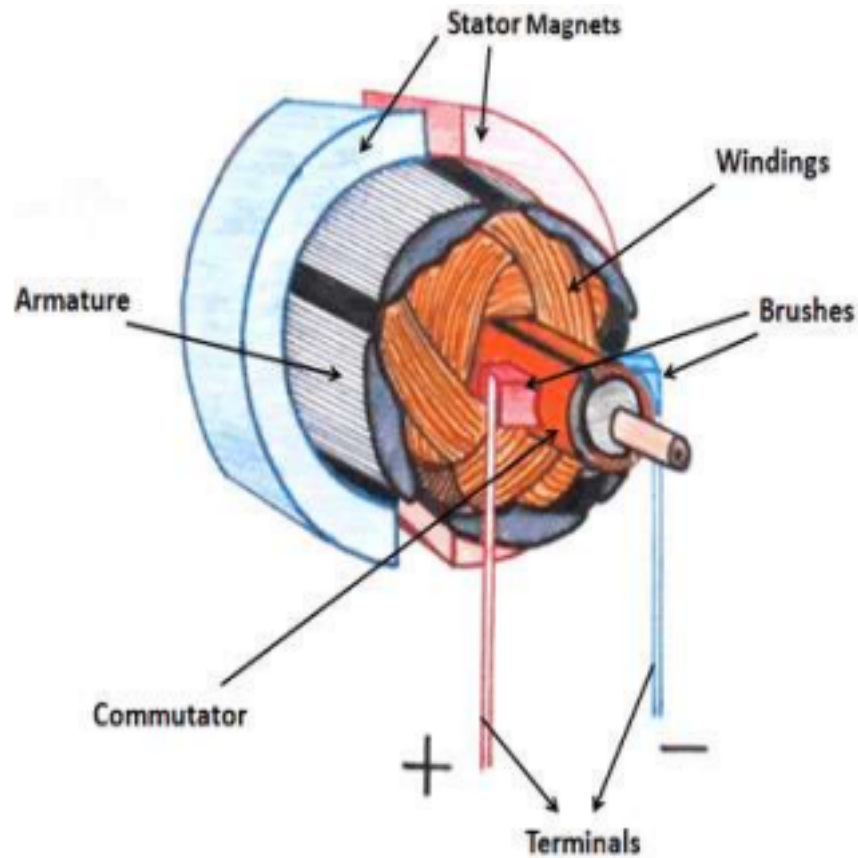


Fleming's left hand rule and magnitude is given by:  $F = BIl$  (newtons) .....

Eq.1

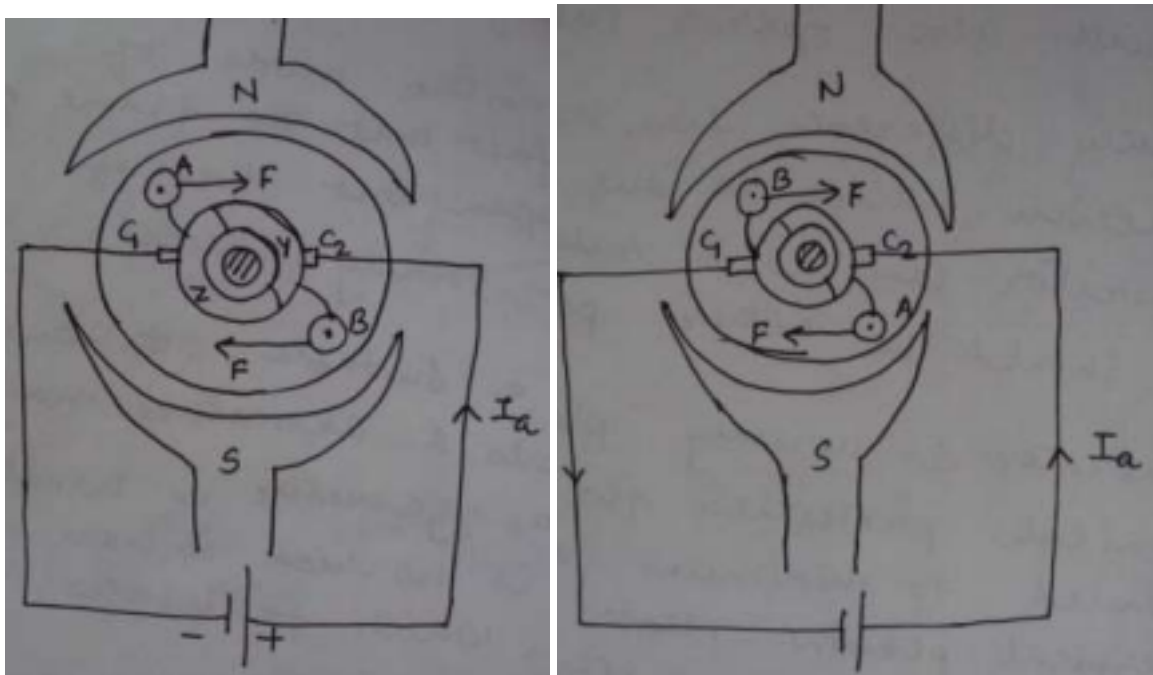
💡 Basically, there is no constructional difference between a d.c. motor and a d.c. generator. The same d.c. machine can be run as a generator or motor.





💡 The principle upon which a d.c. motor works is very simple. 💡 Figure 2 shows a simpler form of a d.c. motor. In case of d.c. motor, the electrical energy is given across the armature and field windings and the armature produces the mechanical rotation.





**Figure**

## 1: A DC Motor

### Figure 2: After 180° Rotation

- 💡 If a current carrying conductor is placed in a magnetic field, a mechanical force is experienced on the conductor, and hence the conductor moves in the direction of force.
- 💡 The magnitude of the mechanical force experienced on the conductor is given by equation 1.
- 💡 When the field winding is supplied by d.c. voltage, the field

current  $I_f$  will flow through the field winding.

💡 This current will magnetize the field pole, resulting a magnetic field in the space between the two poles.

💡 When the armature conductors are also supplied by d.c. current through the carbon brushes, these armature conductors interacts with the magnetic field produced by the field poles and force will develop on the armature conductors. This force will produce continuous rotation of armature.

💡 After  $180^\circ$  rotation of the armature, the situation will be as shown in Figure 2. Here, the direction of current through the armature conductors has been changed due to the action of carbon brushes and commutator segments and the direction of force will be again same as before.

💡 When the armature conductors are supplied by d.c. current in the

direction shown in Figure 1, the current is flowing inside through the conductor 'A'. Hence, the direction of force developed will be as shown in the figure as determined by the Fleming's left hand rule and the armature rotates in the clockwise direction.

- 💡 When the armature of a d.c. motor rotates under the influence of the driving torque, the armature conductors move through the magnetic field and hence e.m.f. is induced in them as in a generator.
- 💡 The induced e.m.f. acts in opposite direction to the applied voltage  $V$  (Lenz's law) and is known as back or counter e.m.f. ( $E_b$ ).
- 💡 The back e.m.f.  $E_b (= Z\Phi NP/60A)$  is always less than the applied voltage  $V$ , although this difference is small when the motor is running under normal conditions.
- 💡 Consider a shunt wound motor shown in Figure 3. 💡 When d.c. voltage  $V$  is applied across the motor terminals, the field magnets

are excited and armature conductors are supplied with current. Therefore, driving torque acts on the armature which begins to rotate.

As the armature rotates, back e.m.f.  $E_b$  is induced which opposes the applied voltage  $V$ .

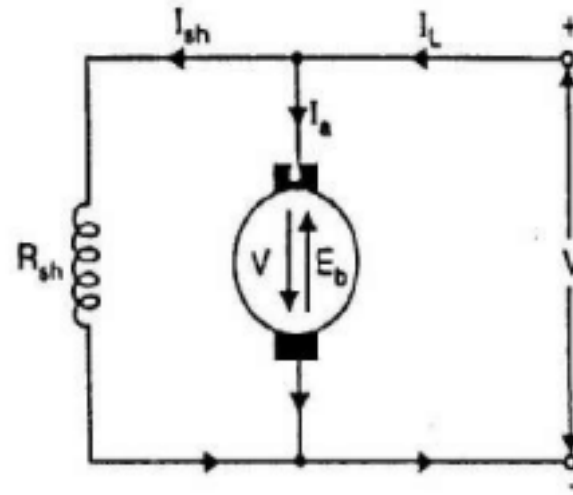
The applied voltage  $V$  has to force current through the armature against the back e.m.f.  $E_b$ .

The electric work done in overcoming and causing the current to flow against  $E_b$  is converted into mechanical energy developed in the armature.

Net voltage across armature circuit  $= V - E_b$

If  $R_a$  is the armature circuit resistance, then,

It follows, therefore, that energy conversion in a d.c. motor is only possible due to the production of back e.m.f.  $E_b$ .



**Shunt Wound D.C. Motor**

**Figure 3: A**

$$I_a = \frac{V - E_b}{R_a}$$

💡 Since  $V$  and  $R_a$  are usually fixed, the value of  $E_b$  will determine the current drawn by the motor. If the speed of the motor is high, then back e.m.f. is large and hence the motor will draw less armature current and vice versa.

$$E_b = \frac{Z\Phi N}{60} \times \frac{P}{A}$$

1) The back e.m.f. protects the armature from short circuit during normal condition. As armature current,

•  $I_a = \frac{V - E_b}{R_a}$

- If there was no back emf i.e.  $E_b=0$

$$I_a = V/R_a$$

- $R_a$  is very low in DC motor so from above equation we can see that current  $I_a$  will be very large just like a short circuit.

## 2) Back emf acts as a current controlling agent:

- It helps to control the magnitude of armature current according to the load. When the mechanical load on the shaft increases, the speed of the armature will be decreased. Then, the magnitude of back emf  $E_b$  will decrease. Hence, more current will pass through the armature windings. Hence, the motor will be able to develop more torque to overcome the increased mechanical load
- The induced emf in the armature of a motor,  $E_b$  depends upon other factors such as armature speed and armature current depends upon the back emf  $E_b$  for a constant applied voltage and armature resistance. If the armature speed is high, back

emf  $E_b$  will be large and therefore, armature current will be small. If the speed of the armature is low, then, back emf  $E_b$  will be less and armature current  $I_a$  more resulting in the development of large torque.

- Hence, the presence of the back emf makes the d.c. motor a self-regulating machine i.e. it makes the d.c. motor to draw as much armature current as is just sufficient to develop the required load torque.

### 3) Back emf also acts as an energy converting agent:

In any energy conversion system, there must be an opposing agent without which energy conversion is not possible. In case of dc motor back emf,  $E_b$  acts as an opposing agent due to which the d.c. motor is able to convert electrical energy into mechanical rotation.

💡 Let in a d.c. motor (See Figure 4),

$V$  = applied voltage

$E_b$  = back e.m.f.

$R_a$  = armature resistance

$I_a$  = armature current

💡 Since back e.m.f.  $E_b$  acts in opposition to the applied voltage  $V$ , the net voltage across the armature circuit is  $V - E_b$ .

💡 The armature current  $I_a$  is given by;

$$I_a = \frac{V - E_b}{R_a}$$

Or,  $V = E_b + I_a \times R_a$

💡 This is known as the voltage equation of a D.C. Motor.

💡 If the voltage equation is multiplied by  $I_a$ , we get,



$$VI_a = E_b \times I_a + I_a^2 \times R_a$$

💡 This is known as power equation of the d.c. motor.

Where,

$VI_a$  = electric power supplied to armature

(armature input)  $E_b I_a$  = power developed by armature (armature output)

$I_a^2 R_a$  = electric power wasted in armature (armature Cu loss)

Thus, out of the armature input, a small portion (about 5%) is wasted as  $I_a^2 R_a$  and the remaining portion  $E_b I_a$  is converted into mechanical power within the armature.

💡 The mechanical power developed by the motor is  $P_m = E_b I_a$ . 💡 Now,

💡 Since,  $V$  and  $R_a$  are fixed, the motor depends upon maximum power, should be zero.

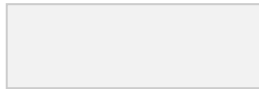


power developed by armature current. For

💡 Therefore,



💡 Now,



💡 Hence, mechanical power developed by the motor is maximum when back e.m.f. is equal to half the applied voltage.

💡 In practice, we never aim at achieving maximum power due to the following reasons:

💡 The armature current under this condition is very large (much excess of rated current of the machine).

💡 Half of the input power is wasted in the armature circuit. In fact, if we take into account other losses (iron and mechanical), the efficiency will be well below 50%.

💡 Like generators, there are armature viz.:

three types of d.c. motors

characterized by the connections of field winding in relation to the

💡 **Shunt-wound motor** in which the field winding is connected in

parallel with the armature (See Figure 4). The current through the shunt field winding is not the same as the armature current.

Shunt field windings are designed to produce the necessary m.m.f. by means of a relatively large number of turns of wire having high resistance.

Therefore, shunt field current is relatively small compared with the armature current.

**Figure 4: D.C. Shunt Motor**

💡 **Series-wound motor** in which the field winding is connected in series with the armature (see Figure 5). Therefore, series field winding carries the armature current. Since the current passing through a series field winding is the same as the armature current, series field windings must be designed with much fewer turns than shunt field windings for the same m.m.f. Therefore, a series field winding

has a relatively small number of turns of thick wire and, therefore, will possess a low resistance.

**Figure 5: D.C. Series Motor**

💡 **Compound-wound motor** which has two field windings; one connected in parallel with the armature and the other in series with it. There are two types of compound motor connections (like generators).

💡 When the shunt field winding is directly connected across the armature terminals (see Figure 6), it is called short-shunt connection.

💡 When the shunt winding is so connected that it shunts the series combination of armature and series field (see Figure 7), it is called long-shunt connection.

💡 The compound machines (generators or motors) are always designed so that the flux produced by shunt field winding is

considerably larger than the flux produced by the series field winding. Therefore, shunt field in compound machines is the basic dominant factor in the production of the

**Figure 6: Short-shunt Connection Figure 7: Long-shunt**

**Connection**

machine.

magnetic field  
in the

💡 The measure of causing the rotation of a wheel or the turning or twisting moment of a force about the axis is called the torque.

💡 Torque is measured by the product of force and the radius at which this force acts.

💡 Consider a wheel of radius  $r$  metres acted by circumferential force  $F$  newtons (see Figure 8). Let the force  $F$  cause the wheel to rotate at  $n$  rps.




💡 Since  $F \times r = \text{Torque}$ ,  $T$  and  $2\pi n = \omega$ , angular velocity in radians per second,

**Figure 8**

💡 Torque is the turning moment of a force about an axis and is



measured by the product of force (F) and radius (r) at right angle to which the force acts i.e. 

💡 In a d.c. motor, each conductor is acted upon by a circumferential force F at a distance r, the radius of the armature (see Figure 8). Therefore, each conductor exerts a torque, tending to rotate the armature. The sum of the torques due to all armature conductors is known as gross or armature torque ( $T_a$ ).

💡 Let in a d.c. motor,

$r$  = average radius of armature in m;

$l$  = effective length of each conductor in m;

$Z$  = total number of armature conductors

$A$  = number of parallel paths

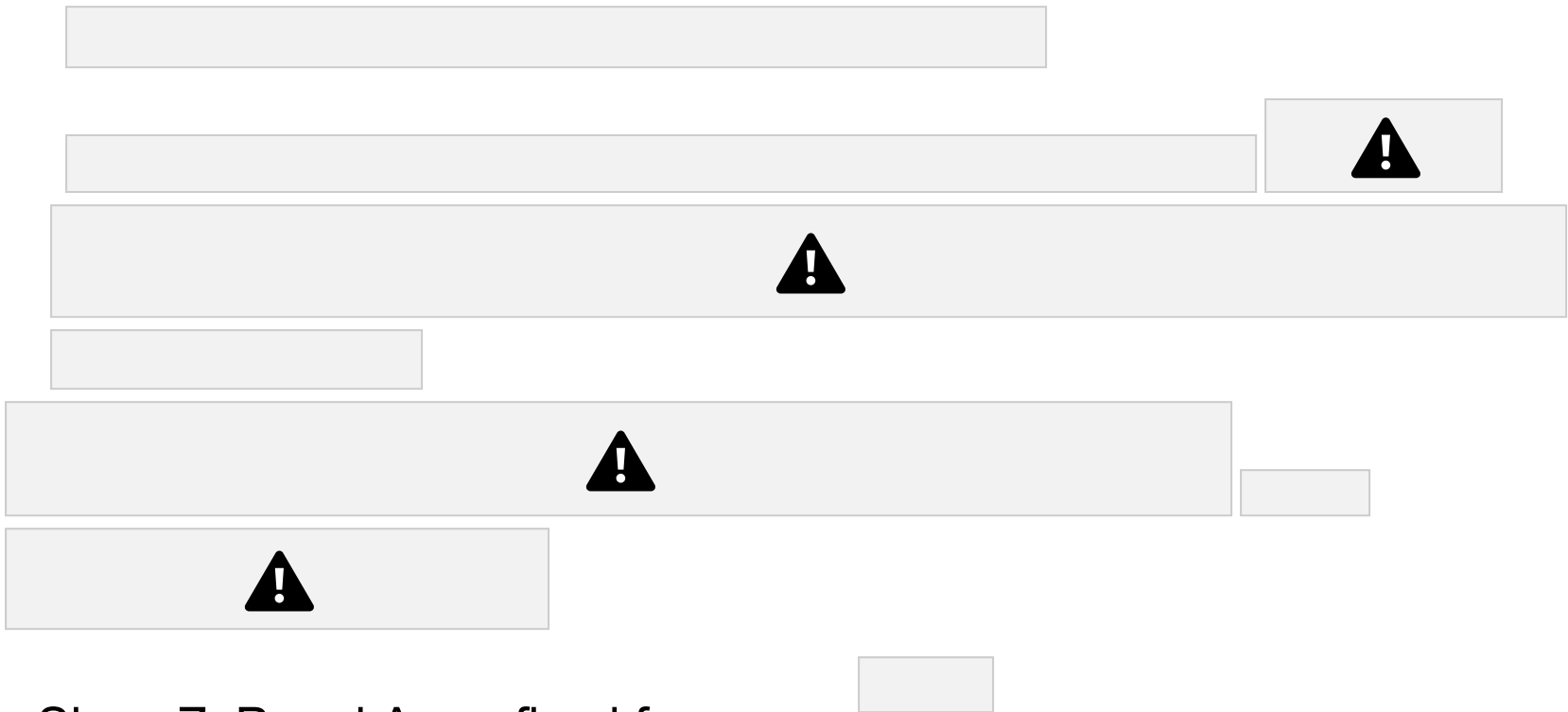
$i$  = current in each conductor =  $I_a/A$

$B$  = average flux density in  $\text{Wb/m}^2$

$\phi$  = flux per pole in  $\text{Wb}$

$P$  = number of poles

Force on each conductor,  $F = B i l$  newtons



Since  $Z$ ,  $P$  and  $A$  are fixed for a given machine,

Hence torque in a d.c. motor is directly proportional to flux per pole and armature current.

For a shunt motor, flux  $\Phi$  is practically constant.

💡 For a series motor, flux  $\Phi$  is directly proportional to armature current  $I_a$  provided magnetic saturation does not take place.



From the expression of  $T_a$ ,



It should be noted that developed torque or gross torque means armature torque,  $T_a$ .

💡 The torque which is available at the motor shaft for doing useful work is known as shaft

torque. It is represented by  $T_{sh}$ .

💡 Figure 9 illustrates the

concept of shaft torque.

- 💡 The total or gross torque  $T_a$  developed in the armature of a motor is not available at the shaft because a part of it is lost in overcoming the iron and frictional losses in the motor.
- 💡 Therefore, shaft torque  $T_{sh}$  is somewhat less than the armature torque  $T_a$ . The difference  $T_a - T_{sh}$  is called lost torque.

**Figure 9: Shaft Torque**

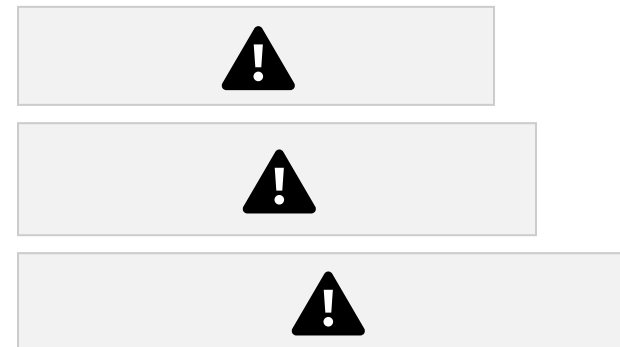


For example, if the iron and frictional losses in a motor are 1600 W and the motor runs at 800

 r.p.m.,

then,

As stated above, it is the shaft torque  $T_{sh}$  that produces the useful output. If the speed of the motor is  $N$  r.p.m., then,



(since  $60/2\pi=9.55$ )

- 💡 There are three principal types of d.c. motors viz., shunt motors, series motors and compound motors.

💡 Both shunt and series types have only one field winding wound on the core of each pole of the motor.

💡 The compound type has two separate field windings wound on the core of each pole. 💡 The performance of a d.c. motor can be judged from its

characteristic curves known as motor characteristics, following are the three important characteristics of a d.c. motor: 💡 **Torque and Armature current characteristic ( $T_a/I_a$ )**

💡 It is the curve between armature torque  $T_a$  and armature current  $I_a$  of a d.c. motor. It is also known as electrical characteristic of the motor.

💡 **Speed and armature current characteristic ( $N/I_a$ )**

💡 It is the curve between speed  $N$  and armature current  $I_a$  of a d.c. motor. It is very important characteristic as it is often the deciding factor in the selection of the motor for a particular application. It is also known as speed characteristics of the motor. 💡 **Speed and torque characteristic**

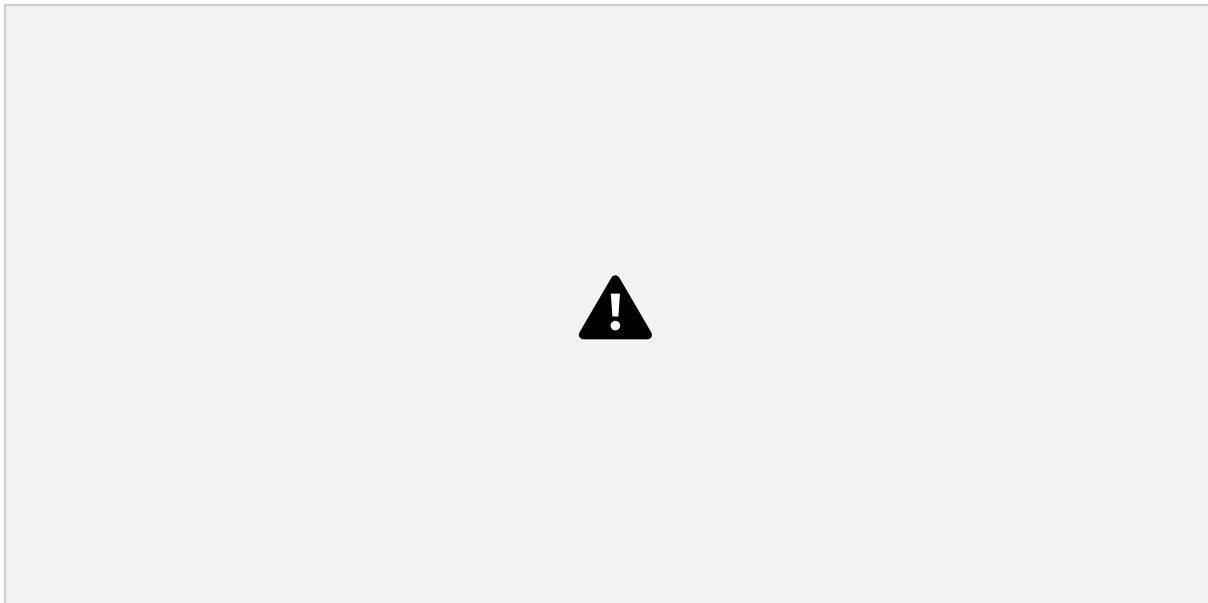
**( $N/T_a$ )**

💡 It is the curve between speed  $N$  and armature torque  $T_a$  of a d.c. motor. It is also known as mechanical characteristic of the motor.

This characteristic gives us information that, how torque of machine will vary with armature current, which depends upon load on the motor.

$$T \propto I_a$$

Thus,



The back emf of dc motor is  $E_b = \frac{P}{I_a}$

$$E_b = V - I_a R_a$$



Therefore shunt motor is considered as constant speed motor.

- From the above two characteristics of dc shunt motor, the torque developed and speed at various armature currents of dc shunt motor may



be noted.

- If these values are plotted, the graph representing the variation of speed with torque developed is obtained.
- This curve resembles the speed Vs current characteristics as the torque is directly proportional to the armature current.

These motors are constant speed motors, hence used in applications requiring constant speed.

Like:

- 1) Lathe machine
- 2) Drilling machine
- 3) Grinders
- 4) Blowers



## 5) Compressors

- In this type of DC motor the armature and field windings are connected in series.

- the resistance of the seriesfield winding

$R_s$  is much smaller than the armature

resistance  $R_a$

- The flux produced is proportional to

the field current but in this

$$I_a = I_f \text{ thus } \phi \propto I_a$$

- Thus flux can never become constant in dc series motor as load changes  $I_f$  and  $I_a$  also gets changed
- Thus dc series motor is not a constant flux motor.



As we have seen for dc motor

$$T \propto \phi I_a$$

But for dc series motor as

$$I_a = I_f = I \quad \phi \propto I$$

So torque in dc series motor is

$$T \propto \phi I_a^2 = \frac{K \phi I_a^2}{60}$$

$$T \propto I_a^3$$

$K$ ,  $\phi$ ,  $I_a$ ,  $I_f$ ,  $I$ ,  $60$  are constants

$$\text{Thus, } T \propto I_a^3 \propto \frac{I_a^3 - I_f^3}{I_a - I_f} = \frac{I_a^3 - I_f^3}{(I_a + I_f)(I_a - I_f)} = \frac{I_a^3 - I_f^3}{(I_a + I_f)(I_a - I_f)}$$

$$\phi \propto I \quad \text{as } I_a = I_f = I$$

Ø

for dc series motor

- To study the performance of the DC series Motor various types of characteristics are to be studied.
  1. Torque Vs Armature current characteristics.
  2. Speed Vs Armature current characteristics.
  3. Speed Vs Torque characteristics

- Torque developed in any dc motor is

$$T \propto \Phi I_a$$

- In case of a D.C. series motor, as field current is equal to armature current, and for small value of  $I_a$

$$\Phi \propto I_a$$

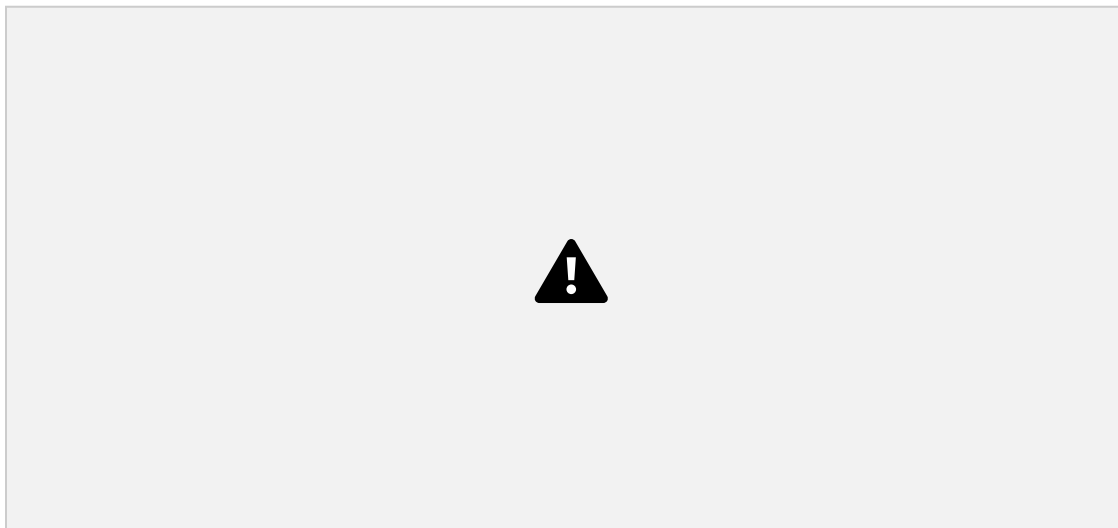
- Therefore the torque in the dc series motor for small

value of  $\phi \propto I_a^2$

- When  $I_a$  is large the  $\phi$  remains the constant due to saturation, thus torque is directly proportional to armature current for large value of  $I_a$

$$T \propto \phi I_a$$

- Thus Torque Vs Armature current characteristics begin to raise parabolically at low value of armature current and when saturation is reached it become a straight line as shown below.



- Consider the following equation

$$N = \frac{V}{\phi} \left( \frac{60}{2\pi} - \frac{K_a K_f}{\phi} \right)$$

- When supply voltage  $V$  is kept constant, speed of the motor will be inversely proportional to flux. In dc series motor field exciting current is equal to armature current which is nothing but a load current. Therefore at light load when saturation is not attained, flux will be proportional to the armature current and hence speed will be inversely proportional to armature current. Hence speed and armature current characteristics is hyperbolic curve upto saturation.
- As the load increases the armature current increases and field gets saturated, once the field gets saturated flux will become constant irrespective of increases in the armature current. Therefore at heavy load the speed of the dc series motor remains constant.
- This type of dc series motor has high starting torque.



- The Speed Vs Torque characteristics of dc series motor will be similar to the Speed Vs Armature current characteristics it will be rectangular hyperbola, as shown in the fig.



These motors are useful in applications where starting torque required is high and quick acceleration. Like:

- 1) Traction
  - 2) Hoists and Lifts
  - 3) Crane
  - 4) Rolling mills
  - 5) Conveyors
- The DC compound motor is a combination of the series motor and

the shunt motor. It has a series field winding that is connected in series with the armature and a shunt field that is in parallel with the armature. The combination of series and shunt winding allows the motor to have the torque characteristics of the series motor and the regulated speed characteristics of the shunt motor. Several versions of the compound motor are:

- [Short shunt Compound Motors](#)
- [Long shunt Compound Motors](#)

When shunt field winding is connected in parallel with armature like dc shunt motor and

this assembly is connected in series with the

series field winding then this type of motor is

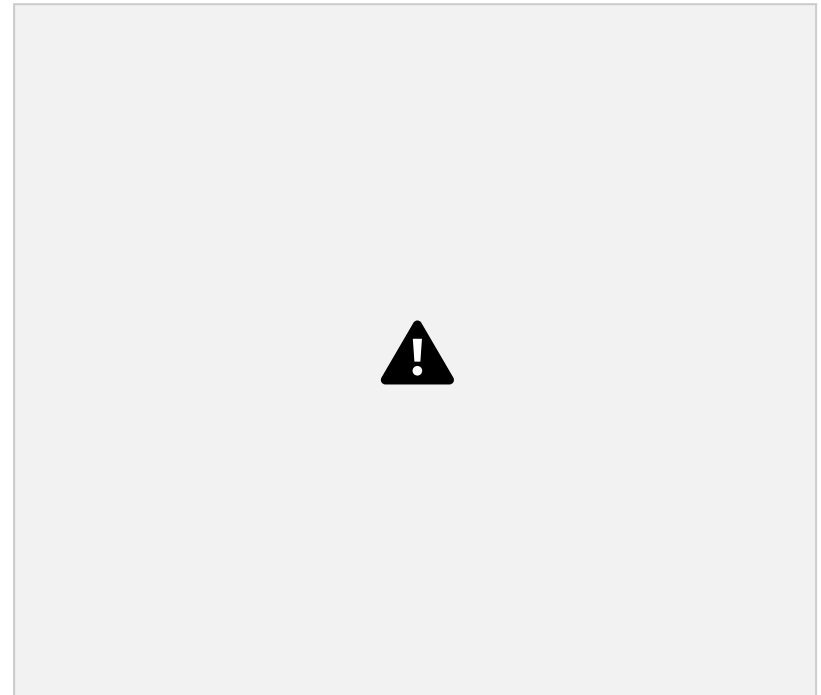




called as short shunt compound motor.

- Depending on the polarity of the connection short shunt motor is classified as: 1. Cumulative compound motor.  
2. Differential compound motor.

- Figure shows a diagram of the cumulative compound motor. It is so called because the shunt field is connected so that its coils are aiding the magnetic fields of the series field and armature.
- In this figure that the top of the shunt field is positive polarity and that it is



connected to the positive terminal of the armature.

- The cumulative compound motor is one of the most common DC motors because it provides high starting torque and good speed regulation at high speeds. Since the shunt field is wired with similar polarity in parallel with the magnetic field aiding the series field and armature field, it is called cumulative. When the motor is connected this way, it can start even with a large load and then operate smoothly when the load varies slightly.
- You should recall that the shunt motor can provide smooth operation at full speed, but it cannot start with a large load attached, and the series motor can start with a heavy load, but its speed cannot be controlled. The cumulative compound motor takes the best characteristics of both the series motor and shunt motor, which makes it acceptable for most applications.

- Differential compound motors use the same motor and windings as the cumulative compound motor, but they are connected in a slightly different manner to provide slightly different operating speed and torque characteristics. Figure shows the diagram for a differential compound motor with the shunt field connected so its polarity is reversed to the polarity of the armature. Since the shunt field is still connected in parallel with only the armature, it is considered a short shunt.
- In the above diagram you should notice that  $F_1$  and  $F_2$  are connected in reverse polarity to the armature. In the differential



compound motor the shunt field is connected so that its magnetic field opposes the magnetic fields in the armature and series field. When the shunt field's polarity is reversed like this, its field will oppose the other fields and the characteristics of the shunt motor are not as pronounced in this motor. This means that the motor will tend to overspeed when the load is reduced just like a series motor. Its speed will also drop more than the cumulative compound motor when the load increases at full rpm. These two characteristics make the differential motor less desirable than the cumulative motor for most applications.

- when the shunt field is connected in parallel with both the series field and the armature then this type of motor is called as long shunt compound motor.
- Depending on the polarity of



connection of shunt field winding, series field winding and armature, long shunt motor is classified as: 1. Cumulative Compound Motor.

2. Differential Compound Motor.

- To study the performance of the DC compound Motor various types of characteristics are to be studied.

1. TorqueVsArmature currentcharacteristics.

2. SpeedVsArmature currentcharacteristics.

3. SpeedVsTorque characteristics

- In dc compound motors both shunt and series field acting simultaneously.
- In cumulative compound motor series field assist the shunt field.
- In such motors when armature current increases the field flux increases.
- So for given armature current the torque developed will be greater and speed lower when compared to a dc

shunt motor.

- In differential compound motor series field opposes the shunt field, therefore when armature current decreases the field flux decreases, so for given armature current the torque developed will be lower and speed greater when compare to the dc shunt motor.

characteristics of dc compound motors



characteristics are compared with that of shunt



motor.

- These motors have high starting torque.
- They can be operated even at no loads as they run at a moderately high speed at no load.
- Hence cumulative compound motors are used for the following applications.
  - ❖ Elevators ,Rolling mills,Punches,Shears planers
- The speed of these motors increases with increases in

the load which leads to an unstable operation.

- Therefore we can not use this motor for any practical applications.

💡 It has been shown in the previous section that the current drawn by the armature circuit of a DC motor is given by

💡 
$$I_a = (V - E_b) / R_a$$

💡 At the instant of starting, there will be no back emf.

💡 If we apply full rated voltage to the motor at starting, the armature will draw a very high current which may be 20 – 30 times greater than its rated full load current.

💡 This high starting current will blow out the fuse and, prior to that it will damage the commutator and carbon brushes.

💡 To avoid this happening DC motor starter is necessary.

💡 A DC motor starter is a variable resistance connected in series with the armature winding (during the starting period only), which limits the starting current to a safe value.

💡 The starting resistance gradually cutout as the motor speeds up and develops back emf which in turn reduces the armature current.



- 💡 When the armature rotates with full rated speed, the starting resistance will be completely cutout.
- 💡 Very small motors, however, can be started from the rest without starter because:
  - 💡 Such motors have a relatively higher armature resistance than the large motors; hence their starting current is not so high.
  - 💡 Being small, they have low moment of inertia, hence they speed up quickly.
- 💡 Figure shows the current diagram of a practical DC motor starter. 💡 It is called as three point starter.
- 💡 The three terminals of the starter are marked as L,A and Z.
  - 💡 The negative line of supply is directly connected to the negative terminal of the armature which is also connected to the negative terminal of the field winding. 💡 The positive terminal of the supply

line is connected to the terminal marked 'L' of the starter, which is further connected to the starting arm 'B' through over current release 'M'.



- 💡 To start the motor, the main switch is first closed and starting arm 'B' is slowly moved to the stud no-1.
- 💡 As soon as the arm makes contact with stud no – 1, the field

winding gets full supply voltage through the conductive arc and at the same time full starting resistance  $R_s$  is connected in series with the armature.

💡 The starting current drawn by the armature is given by:

$$I_a = V / (R_a + R_s)$$

💡 As the motor speeds up, arm is further moved and the starting resistance is gradually cut out.

💡 When the arm reach the position 'ON', the starting resistance  $R_s$  is completely cutout and at the same time the motor will have full rated speed, thus producing normal value of back emf to set armature current at normal value.

💡 The arm moves over the various studs against a strong spring force which tends to pull back the arm to the 'OFF' position. But is a soft iron piece 'S' attached to the arm in which the 'ON'

position is attracted and hold by an electromagnet 'E' (known as hold- on coil) energized by the shunt field current.

- 💡 When the motor is switched off by the main switch, the hold- on coil 'E' will get demagnetized and starting arm 'B' is thrown back to the 'OFF' position under the action of spring force. It also release the starting arm 'B' to the 'OFF' position at the instant of break in field winding and low voltage condition.
- 💡 If the motor is over loaded, the motor will draw high current and the electromagnet 'M' will be strong enough to lift up the liver 'D' and it will short circuits the electromagnet 'E'. Then the electromagnet 'E' will get de energised and it will release the starting arm to 'OFF' position.







Therefore the factors controlling the speed of DC motor are: Applied voltage ' $V$ ', Armature resistance ' $R_a$ ' and Flux per pole ( $\phi$ )





💡 The speed regulation of a motor is the change in speed from full-load to no load and is expressed as a percentage of the speed at full-load i.e.



Speed of shunt motor can be controlled in two ways:

**Flux Control Method &  
Armature Control Method Flux  
Control Method:**

💡 It is clear that the speed of motor is inversely proportional to the flux per pole ( $\phi$ ).

💡 In this method of speed control,

a variable resistance  $R_v$  is connected in series with the field winding to regulate the field current thereby regulates the flux per pole.

**Figure: Flux Control Method of Speed Control**

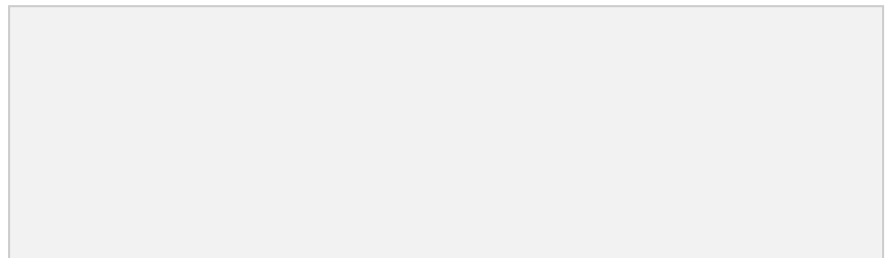


- 💡 The variable resistance  $R_v$  can only reduce the field current below its rated value.
- 💡 Therefore, this method is only suitable to control the speed

above the rated speed.

- 💡 When  $R_v$  is reduced to '0' position, full rated field current ( $I_f = V/R_f$ ) will flow and the motor rotates with normal rated speed.
- 💡 When full  $R_v$  is connected at position '1', the field current will reduce to  $I_f = V/(R_f + R_v)$  thereby reducing the flux per pole, then the motor rotates with a speed higher than normal rated speed.
- 💡 Between the positions '0' and '1' many intermediate speed can be obtained by sliding the variable point contact.

💡 This method is used when speed below the normal rated speed is



required.

- 💡 As the supply voltage is normally constant, the voltage across the armature is varied by inserting a variable resistance  $R_v$  in series with the armature circuit.
- 💡 As the field winding is directly proportional across the full supply voltage, the field current remains constant. **Figure: Armature Control Method**

💡 Therefore, the flux per pole remains constant.

💡 The armature torque depends on the flux per pole and armature current ( $T \propto \phi I_a$ ).

💡 If the controller resistance  $R_v$  is increased keeping the load

torque constant, the armature current remains constant, but the potential difference across the armature will decrease.

🧠 Hence the speed of the armature will decrease.

🧠 Let  $N_1$  = speed of the motor when  $R_v = 0$

🧠  $N_2$  = speed of the motor when  $R_v$  is connected

🧠 Since the flux per pole is constant and load torque is also constant  $\Phi_{1} = \Phi_{2}$  (since  $\Phi \propto \phi$ )

Then back emf

$$E_{b1} = V - I_a R_a \text{ and } E_{b2}$$

$$= \Phi_1 - \Phi_2 + \Phi_2 \text{ Now, } \Phi_2$$

$$\Phi_1 = \frac{N_1 I_1}{R_1} \times \frac{1}{\phi_1}$$

$$\phi_2 \Phi_1 \Phi_2 = \phi_1$$

Therefore,

$$\Phi_2$$

$$\Phi_1 = \frac{N_1 I_1}{R_1} - \frac{N_2 I_2}{R_2} (\Phi_1 + \Phi_2)$$

$$\Phi_1 - \frac{N_2 I_2}{R_2} \Phi_1 = \frac{N_2 I_2}{R_2} \Phi_2$$

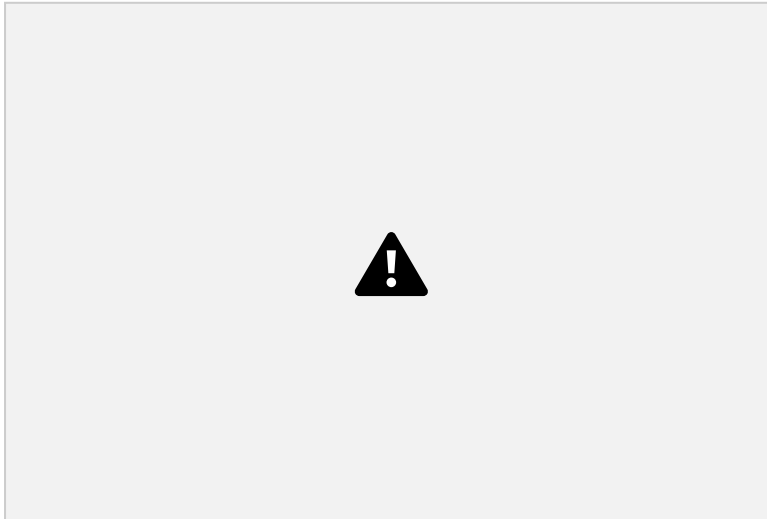
Flux control method: Variation of flux in DC series motors can be done by anyone of the following methods.

Field diverter method:

- In this method, a variable resistance is connected across the series field winding as shown in the figure. When this variable resistance is connected some of the field current will get diverted

and pass through  $R_v$ . Any desired amount of current can be passed through the field winding by adjusting the value of  $R_v$ . Hence, flux can be decreased and speed can be increased.

**Figure: Field Diverter Method**

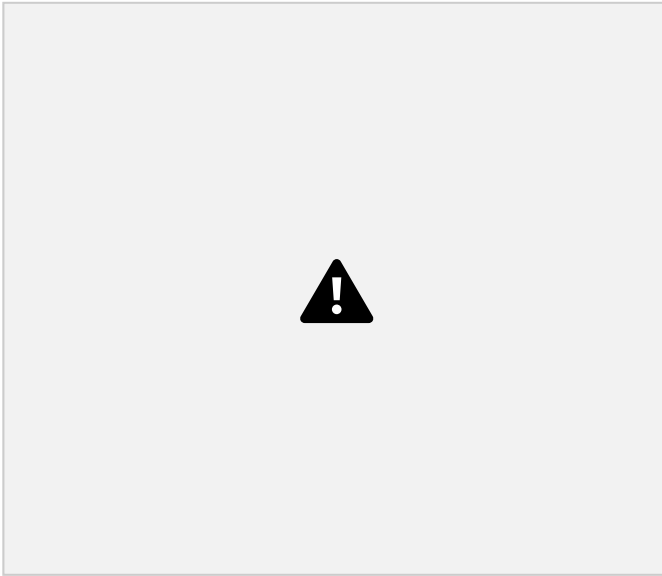




### Armature diverter method:

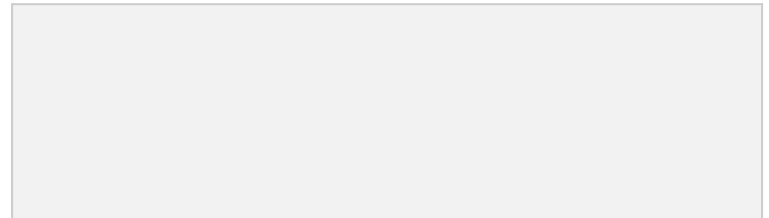
- In this method, a variable resistance is connected across armature winding as shown in the figure. When this variable resistance is connected some of the armature current will be diverted and pass through  $R_v$ . For a constant load torque, if the armature current  $I_a$  is reduced due to diverted  $R_v$ , then the flux per pole must increase to produce constant torque.
- Hence,  $T_a \propto \phi I_a$
- This results in an increase in main line current taken from the supply and a fall in speed (Hence,  $N \propto 1/\phi$ ). The variation in speed can be controlled by varying the value of diverter resistance  $R_v$ . This method is only suitable for controlling the speed below the normal rated speed.

**Figure: Armature Diverter Method**



Tapped field control method:

💡 In this method, the series field winding is



provided with number of tappings as shown in the figure.

- 💡 The number of series turns in the circuit can be changed by the changer.
- 💡 With full field winding, the motor runs at its minimum speed. The speed can be raised in steps by cutting out some of the series turns.

**Figure: Tapped field control method**

- The direction of the magnetic flux in the air gap depends on the direction of the field current.
- And the direction of the force exerted on the armature winding depends on the direction of flux and the direction of armature

current.

- Thus in order to reverse the direction of dc motor, we have to reverse the direction of force.
- This can be achieved either by changing the terminals of the armature or the terminals of the field winding.
  - 💡 The losses occurring in a d.c. motor are the same as in a d.c. generator .These are :
    - i. copper losses
    - ii. Iron losses or magnetic losses
    - iii. mechanical losses



- 💡 Like a d.c. generator, the efficiency of a d.c. motor is the ratio of output power to the input power i.e.



- 💡 As for a generator, the efficiency of a d.c. motor will be maximum when:

$$\text{Variable losses} = \text{Constant losses}$$

- 💡 Therefore, the efficiency curve of a d.c. motor is similar in shape to that of a d.c.generator.

💡 The power stages in a d.c. motor are represented diagrammatically in Figure below. 💡  $A - B = \text{Copper losses}$

💡  $B - C = \text{Iron and friction losses}$

💡 Overall efficiency,  $\eta_c = C/A$

💡 Electrical efficiency,  $\eta_e = B/A$

💡 Mechanical efficiency,  $\eta_m = C/B$



**Figure : Power Stages**