$\begin{array}{c} {\rm COMP\text{-}4540/8540} \\ {\rm Design\ and\ Analysis\ of\ Algorithms} \end{array}$

Winter 2025

Assignment 1

Due Date: February 4 (before 11:59p.m.)

- 1. Prove that $n! \in o(n^n)$ using the definition of o-notation.
- **2.** Prove or disprove: $\Theta(n) \Theta(n-1) = \Theta(1)$.
- **3.** Prove that $\sum_{k=1}^{n} \frac{1}{2k-1} = O(\lg \sqrt{n})$. [Hint: $\sum_{k=1}^{n} \frac{1}{k} = \ln n + \gamma + \frac{1}{2n} + o(\frac{1}{n})$.]
- 4. To be posted
- 5. To be posted
- **6.** To be posted