

Exercise : Apply Breach & Bound

$$\max Z = 6x_1 + 8x_2$$

$$\begin{cases} 6x_1 + 3x_2 \leq 18 \\ 2x_1 + 3x_2 \leq 9 \\ x_1, x_2 \text{ are integers} \end{cases}$$

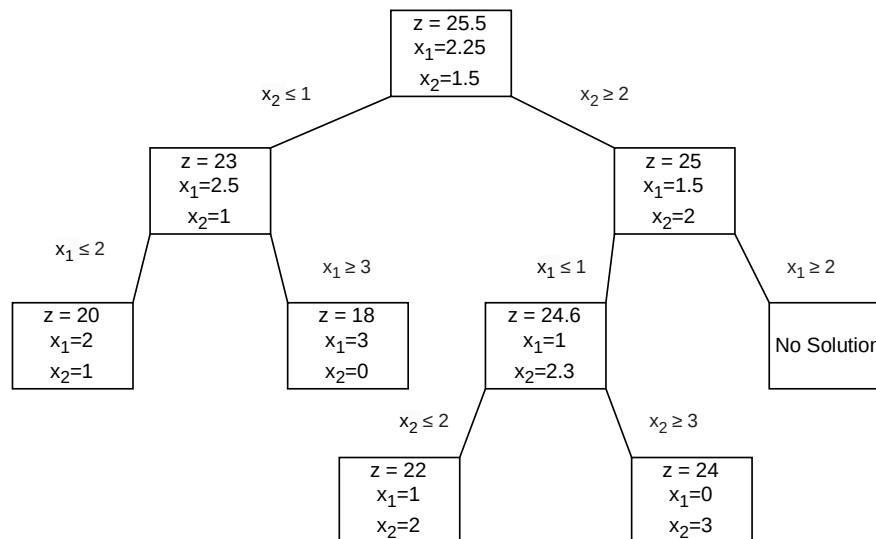
$$\min Z = x_1 - 2x_2$$

$$\begin{cases} -4x_1 + 6x_2 \leq 9 \\ x_1 + x_2 \leq 4 \\ x_1, x_2 \text{ are integers} \end{cases}$$

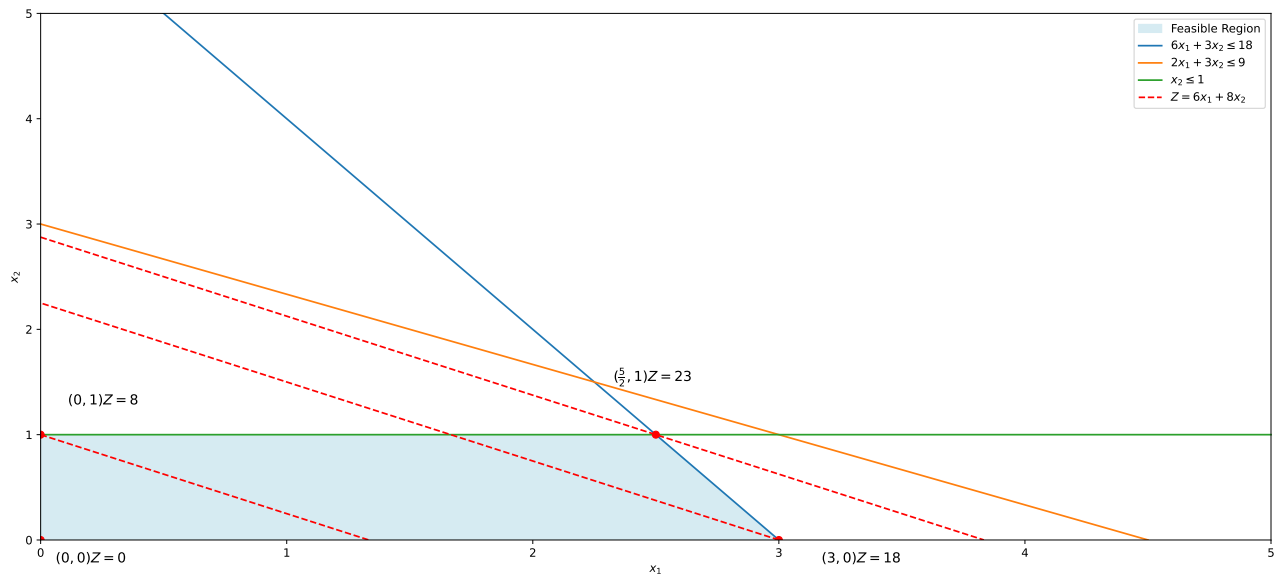
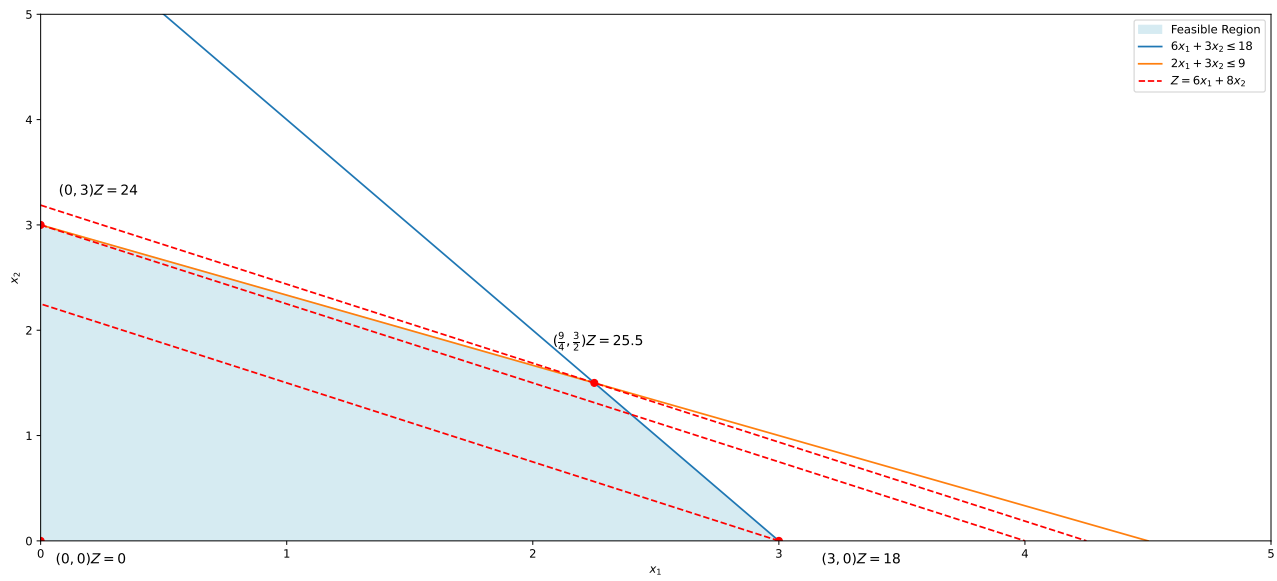
Solution

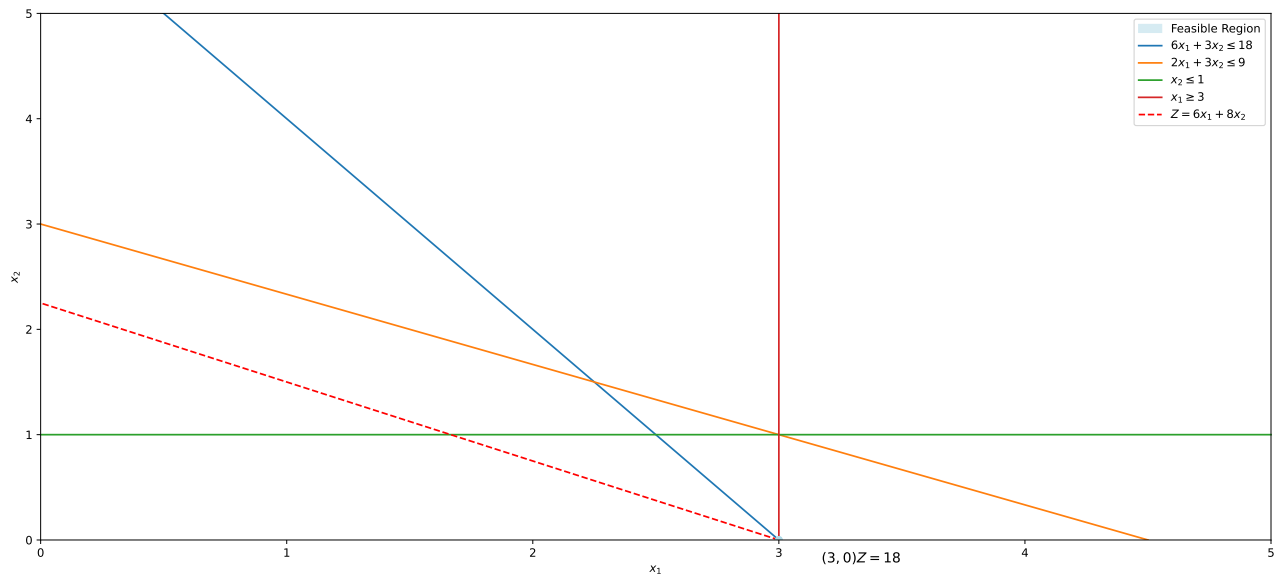
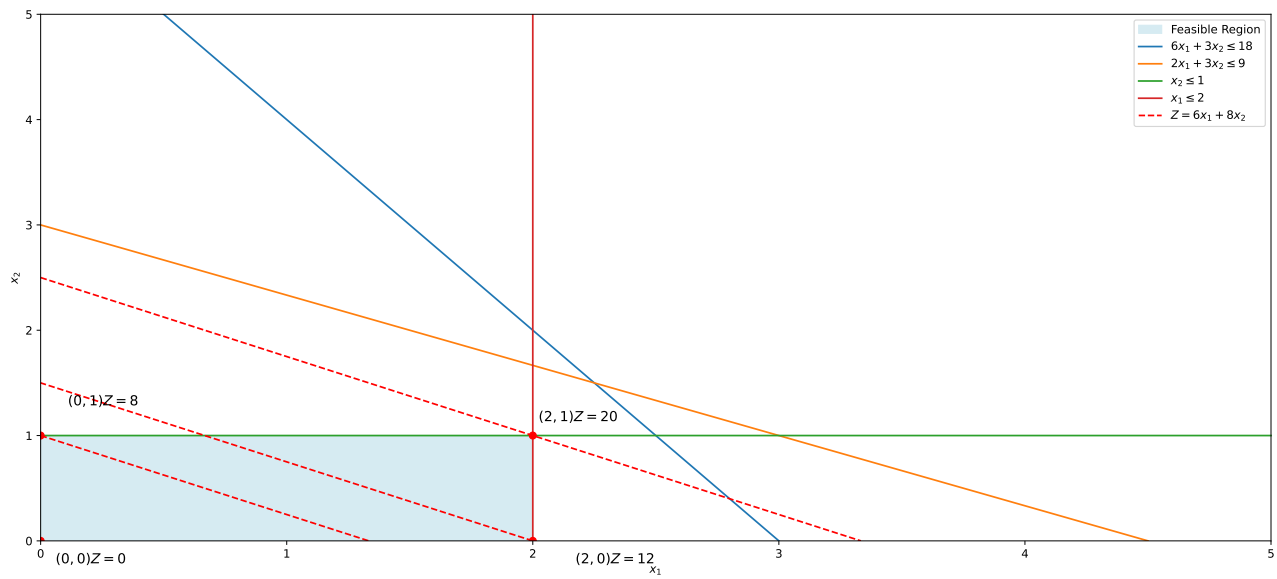
$$\max Z = 6x_1 + 8x_2$$

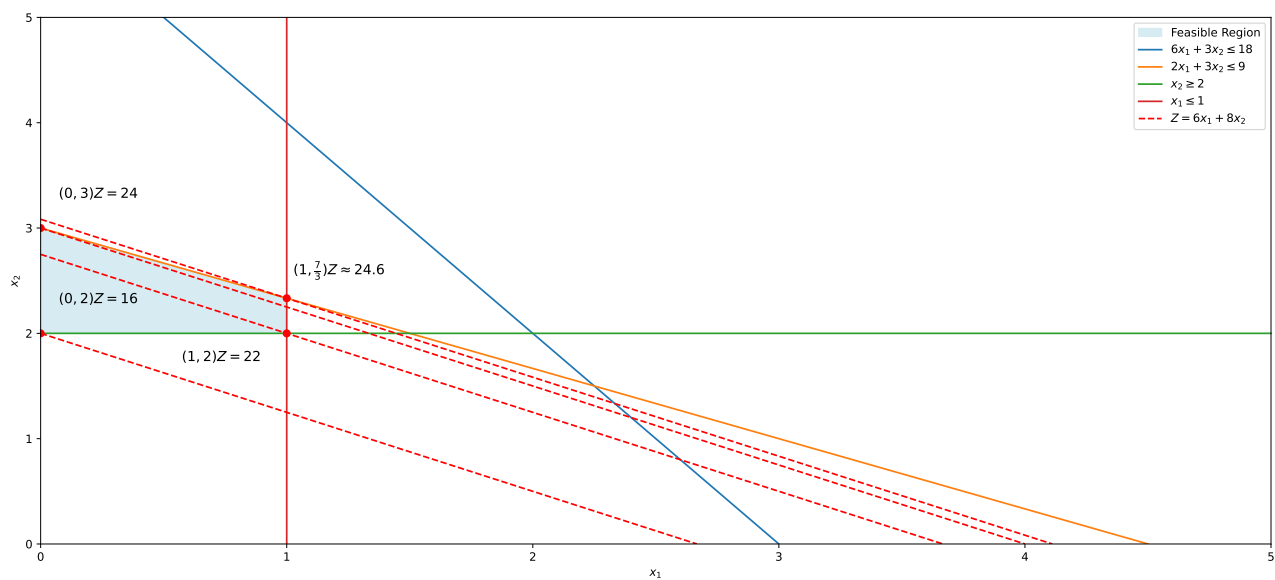
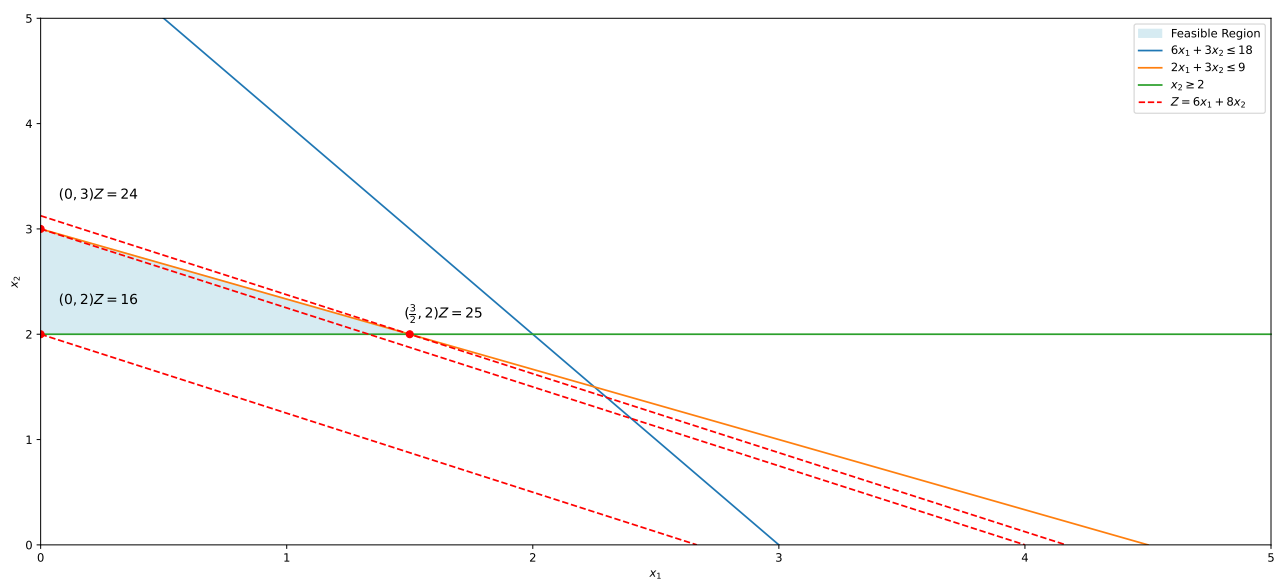
$$\begin{cases} 6x_1 + 3x_2 \leq 18 \\ 2x_1 + 3x_2 \leq 9 \\ x_1, x_2 \text{ are integers} \end{cases}$$

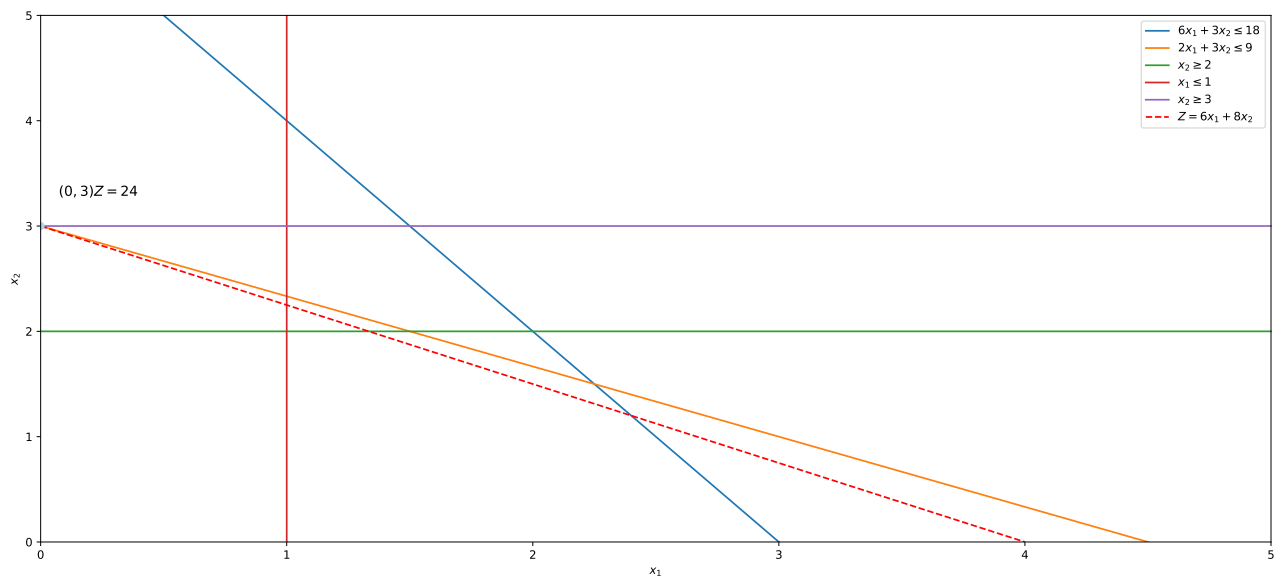
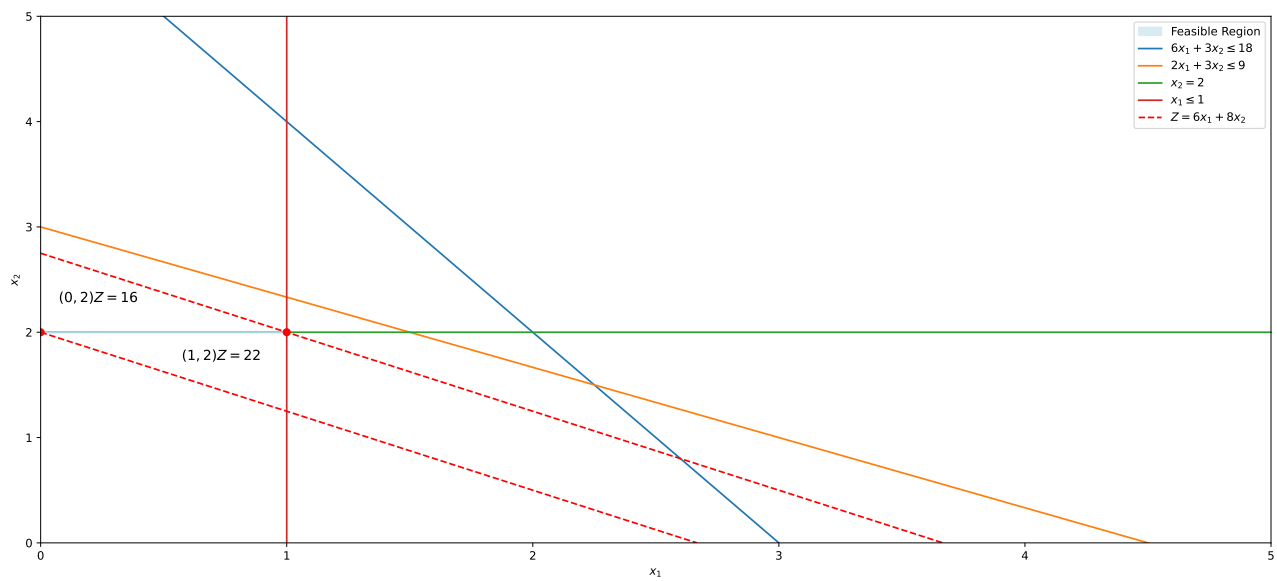


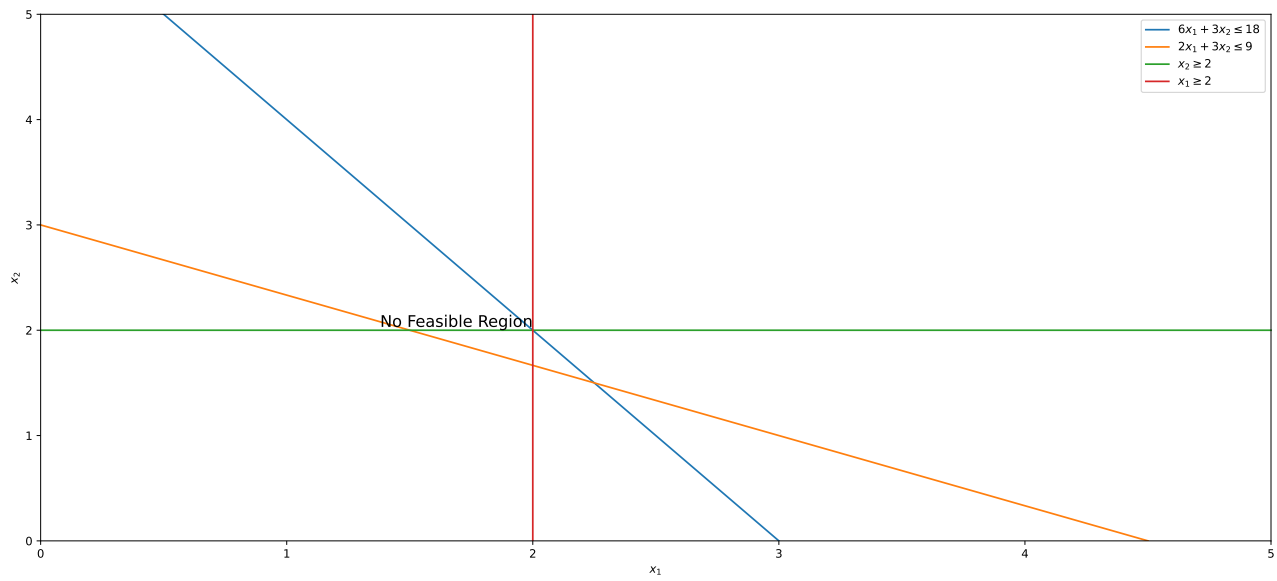
Optimal Solution is $(x_1, x_2) = (0, 2)$





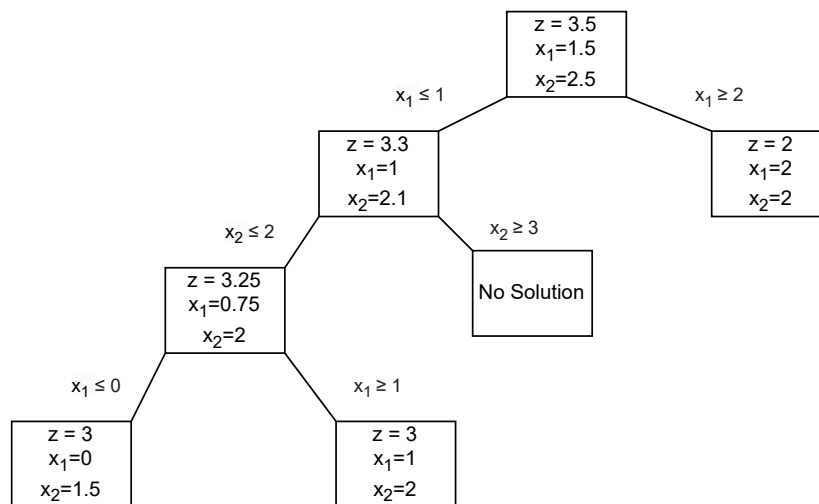






$$\min Z = x_1 - 2x_2 \implies \max -Z = -x_1 + 2x_2$$

$$\begin{cases} 6x_1 + 3x_2 \leq 18 \\ 2x_1 + 3x_2 \leq 9 \\ x_1, x_2 \text{ are integers} \end{cases}$$



Optimal Solution is $(x_1, x_2) = (1, 2)$

Note

We did not branch the node $(Z = 3, x_1 = 0, x_2 = 1.5)$ because another node at the same level $(Z = 3, x_1 = 1, x_2 = 2)$ was already completed. Continuing to branch the first node would only cause Z to keep decreasing. Hence, we pruned it.

