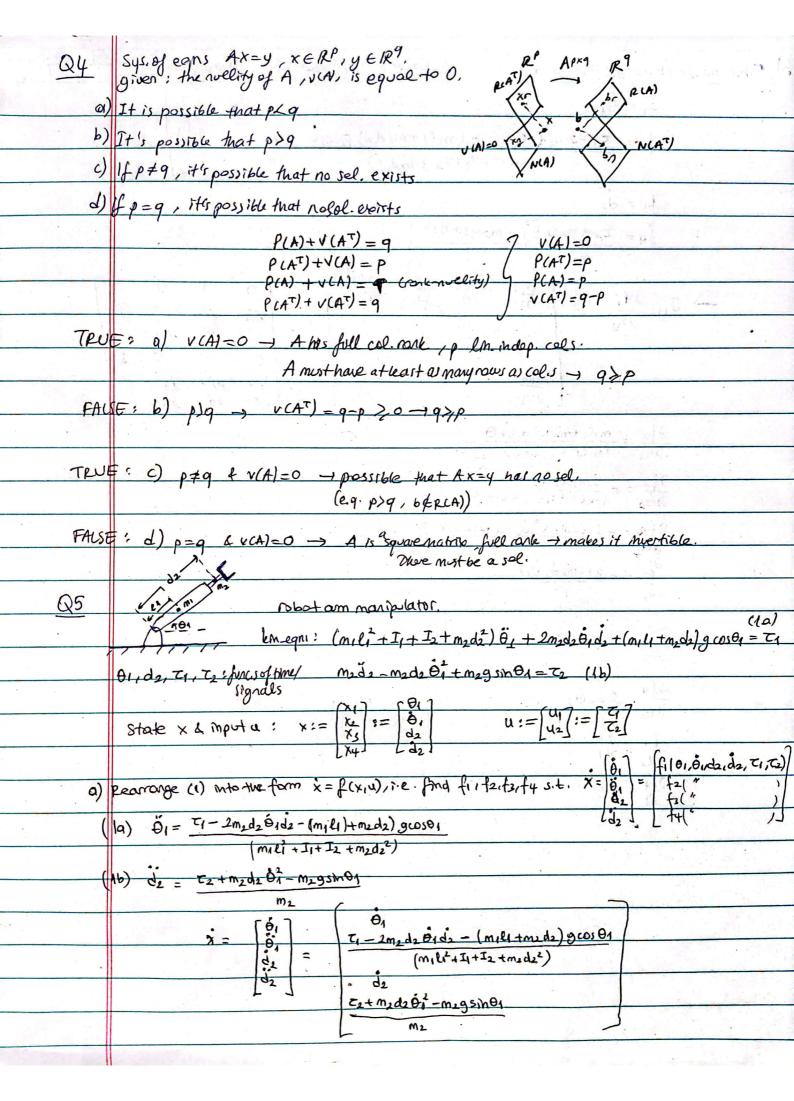


```
U' -> 4.x=0 for +uEU
                U(x=0 - /1/x=0-1 x+y=0 -1 x=-y
               42 \times 20 = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \times 20 \longrightarrow 942 = 0
b) basis vector: v= [-1] - normalize it. \( \frac{1}{1\sqrt{3}} \)
Q3
        Sol, to the optimization problem
                MINIMINE IXTX Subject to AX=Y
       is x=Aty, where At:=AT(AAT)-1 is the unweighted pseudo-inverse. We now define
 the weighted pseudo-inverse A_8^+ := BA^T (ABA^T)^{-1}. What appropriation problem does x = A_8^+ y
  solve? (nother words, find f(x) s.t. x = Afy is the solution to problem minimize f(x)
                                                                                   subject to Ax=y.
  Hint : Make a guess at what f(x) might be therese
 Hamiltonian to check whether thesel is indeed x = Asty.
     guess : f(x)=1 xTBx
             H(x,\lambda) = f(x) + \lambda^{T}(Ax-y) = fx^{T}Bx + \lambda^{T}(Ax-y)
                \nabla H = BX + A^T\lambda = 0
                     X = -B^{-1}A^{T}\lambda
               -AB^{-1}A^{T}\lambda = y
                 \lambda = -(AB^{-1}A^{T})^{-1}y
            -> x = B-1A' (AB-A'). y -> f(x)=2x'Bx
                 X = A& y - , indeed a sal to the optimization problem.

minimize f(x)=1xTBX subject to Ax=y
```



/1			1 - Y. n . = 2 × 3 · ·	7 /	ador of Orwint
b) Find the Jacobian of f(x,14)	wrt x. Mint; Olu	volve of the it		r -	T X
$f_1 = \Theta_1$			\ \ \ \ \ =		VI
for= 1-21	12d2 O1d2 - (m1		101 - N	1 1 2	(6
	(M1212+ I1-1I2	+m2d22)	D	$\begin{bmatrix} d_2 \end{bmatrix}$	6.
$f_3 = d_2$		1545 5	200 Herior	H. CAN	Sh
fy = = == =============================	d2 01 - m29sm0	The state	· *(A, *)		
M ₂		(A. V	(· A · · · · · ·		
-) Jij= 2+i =	261 261	ada ada	= \frac{\text{0}}{\text{fr}} \frac{2}{20}	1 0 0 1 2/2 2/2 162 2/2 2/2	
~ \\		Am.	200 8		Teil
		264		0 0 1	
	261	264	201 20	4 H4 0	ń.
the (military	2d2) a sin 01				
afz = (military)	II+I2+m2d22)				
$\frac{\partial f_2}{\partial \dot{\theta}_1} = -\frac{2m_2d}{(m_1L_1^2 +$	14 + 12 + n2 d22)	<u> </u>			
2f1 = - 1 (2m	2 (de) +N(2m2de	2)			N. IFT
367	D ²			1	
$\frac{\partial f_2}{\partial J_2} = 0 (2m_2)$	2 01)		1.		
dá ₂ D		in the second			
2fy = - georg	21			1 5	
901				k A	
26y = 22204					
2 6 ₁	**	3	2 2 2 2 3	do	
$\frac{2f4}{24z} = \theta_1^2$	1, 1				
37r = 0		1	v 6 50 %	D ₁ 19 19 13	(6
		i e y i nin		in the second	
		1.6	(12 x 3 x 1		a true
			A THE PARTY HE PROPERTY	The state of the s	

```
c) Jacobson untl u.
                                                                         V = \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} T_1 \\ T_2 \end{bmatrix}
                   (mili+I1+I2+ med2) g cosos
             fy= tetmadeoi - magsmon
                                                        1/2
                                            Ly T1=0 (if (xop/upp) is (
          et's check >
                                                   (M162+I1+I2+m29)
                                    0+m2302-m2gsmco)
                * So , since for a (xop, 40p) $=0 -> (kop, 40p) is not egm.pt.
```

