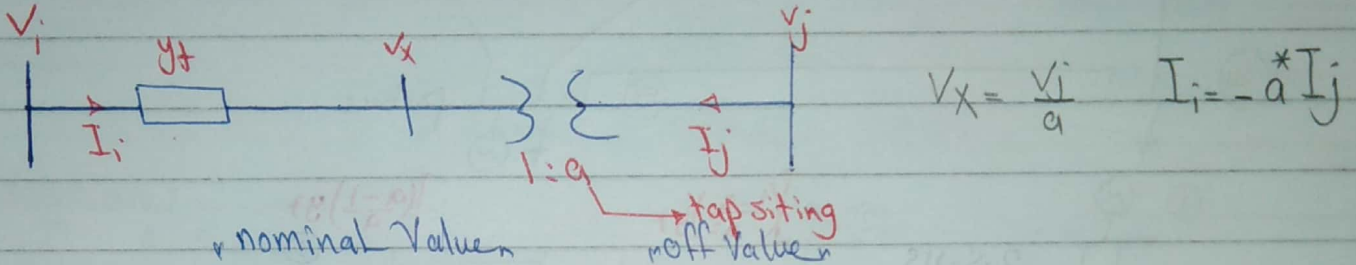


## Tap changing Transformer

يستخدم كوسيلة للتحكم في الفولت اللطالوع من Transf<sub>n</sub> وبالتالي أقرأ كآام في "Q"

في تاييم اسعفا "Phase shifter" موجودة في الفولت تستخدم كوسيلة للتحكم في angle Pow<sub>n</sub>

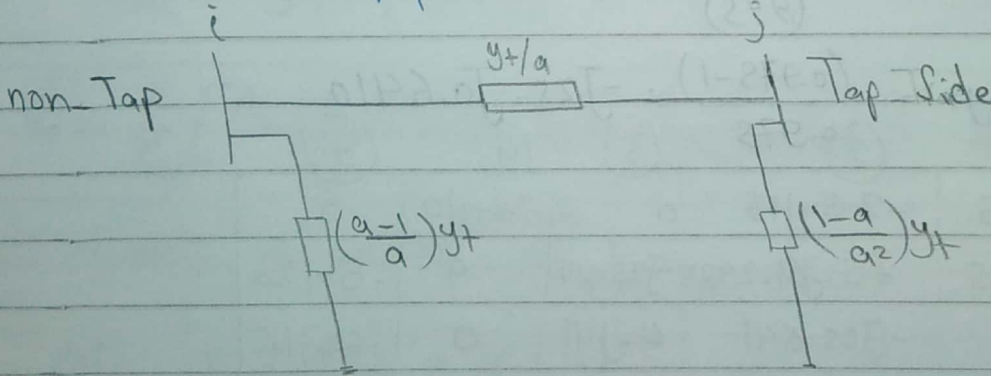


$$I_i = y_t (V_i - V_x) \rightarrow I_i = y_t V_i - y_t V_x$$

$$I_i = y_t V_i - \frac{y_t}{a} V_j \rightarrow \text{[1]} \quad I_j = -\frac{1}{a^*} I_i$$

$$I_j = -\frac{y_t}{a^*} V_i + \frac{y_t}{|a|^2} V_j \rightarrow \text{[2]}$$

$$\begin{bmatrix} I_i \\ I_j \end{bmatrix} = \begin{bmatrix} y_t & -y_t/a \\ y_t/a^* & \frac{y_t}{|a|^2} \end{bmatrix} \begin{bmatrix} V_i \\ V_j \end{bmatrix}$$



Tap Side

$(\frac{1-a}{a^2}) y_t$

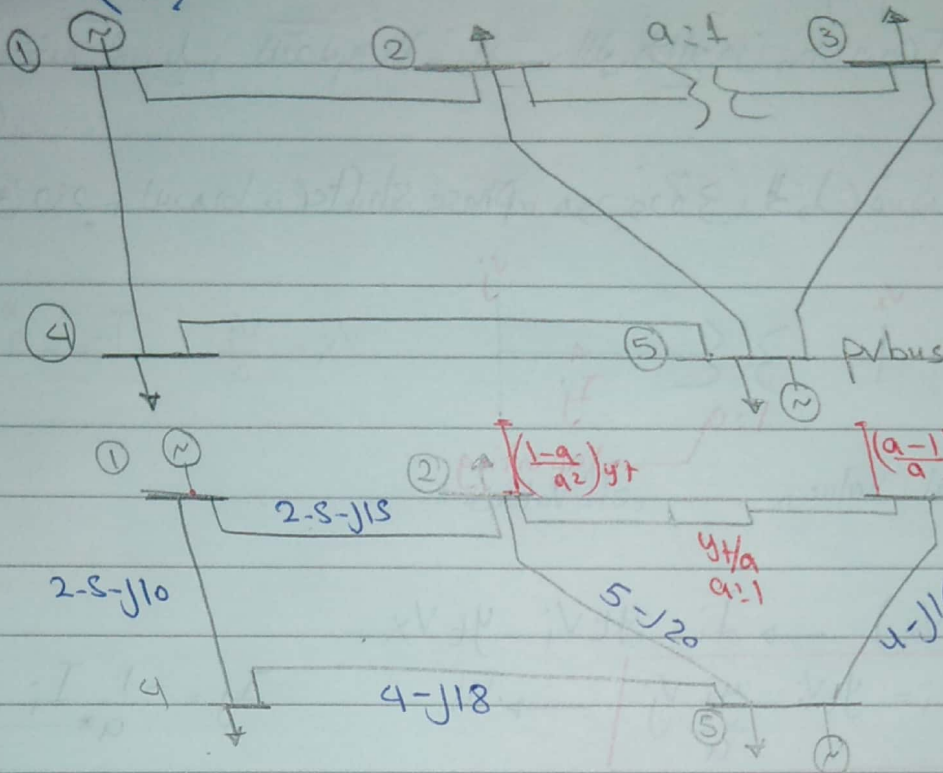
$(\frac{a-1}{a}) y_t$

non Tap

$(\frac{a-1}{a}) y_t$

$$a \geq 1$$

Ex 2.13 (110).



Tap sining = 0.975  
reactance = 0.04

$$y_t = \frac{1}{0.04j} = -j25$$

Tap sining = 0.975

$$(2 \rightarrow 3) \rightarrow y_t/a = \frac{-j25}{0.975} = -j25.641$$

$$(2 \rightarrow 0) \rightarrow \left(\frac{1-a}{a^2}\right)y_t = \frac{1-0.975}{(0.975)^2} \times -j25 = -j0.6575$$

$$(3 \rightarrow 0) \rightarrow \left(\frac{a-1}{a}\right)y_t = \frac{(0.975-1)}{0.975} \times -j25 = j0.6410$$

	①	②	③	④	⑤
$Y_{bus}$	5-j25	-2-S+j15	0	-2-S+j10	0
	-2-S+j15	7-S-j61.2985	-j25.641	0	-5+j20
	0	-j25.641	4-j4	0	-4+j16
	-2-S+j10	0	0	6-S-j28	-4+j18
	0	-S+j20	-4+j16	-4+j18	13-j54



bus ① slack  $V_1 = 1 \angle 0$

bus ② PQ bus  $P_{2sch} = P_g - P_d = \frac{-60}{100} = -0.6 \text{ pu}$   $Q_{2sch} = \frac{-35}{100} = -0.35 \text{ pu}$

bus ③ PQ bus  $P_{3sch} = \frac{-70}{100} = -0.7 \text{ pu}$   $Q_{3sch} = \frac{-42}{100} = -0.42 \text{ pu}$

bus ④ PQ bus  $P_{4sch} = \frac{-80}{100} = -0.8 \text{ pu}$   $Q_{4sch} = \frac{-50}{100} = -0.5 \text{ pu}$

bus ⑤ PV bus  $P_{5sch} = P_g - P_d = \frac{190 - 65}{100} = 1.25 \text{ pu}$   $V_5 = 1 \angle 0$

using Gauss Seidel

1<sup>st</sup> iteration

$$V_2^{(1)} = \frac{1}{Y_{22}} \left[ \frac{P_{2sch} - jQ_{2sch}}{V_2^{(0)}} - Y_{21}V_1^{(0)} - Y_{23}V_3^{(0)} - Y_{24}V_4^{(0)} - Y_{25}V_5^{(0)} \right]$$

$$= \frac{1}{7.5 - j61.2985} \left[ \frac{-0.6 + j3.5}{1} - (-2.5 + j15)(1) - (-j25.641)(1) - (-5 + j20)(1) \right]$$

$$= -0.6049 + j0.6441 \quad [0.1584 + j0.0931]$$

$$V_{2acc}^{(1)} = V_2^{(0)} + \alpha (V_2^{(1)} - V_2^{(0)}) = 1 + 1.6(-0.6049 + j0.6441 - 1) = -0.3466 + j0.1491$$

$$V_3^{(1)} = \frac{1}{Y_{33}} \left[ \frac{P_{3sch} - jQ_{3sch}}{V_3^{(0)}} - Y_{31}V_1^{(0)} - Y_{32}V_2^{(0)} - Y_{34}V_4^{(0)} - Y_{35}V_5^{(0)} \right] =$$

$$V_{3acc}^{(1)} = V_3^{(0)} + \alpha (V_3^{(1)} - V_3^{(0)})$$

$$V_4^{(1)} = \frac{1}{Y_{44}} \left[ \frac{P_{4sch} - jQ_{4sch}}{V_4^{(0)}} - Y_{41}V_1^{(0)} - Y_{42}V_2^{(0)} - Y_{43}V_3^{(0)} - Y_{45}V_5^{(0)} \right] =$$

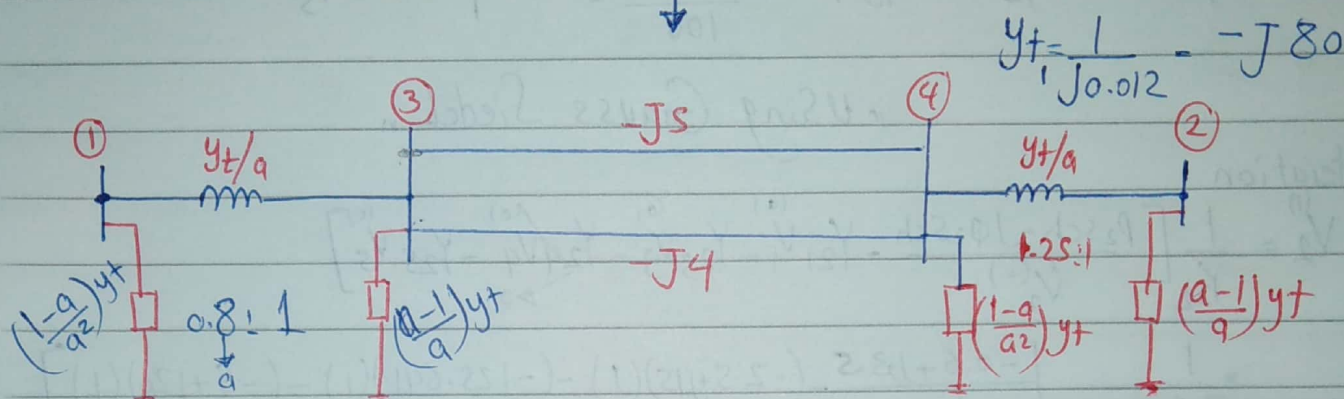
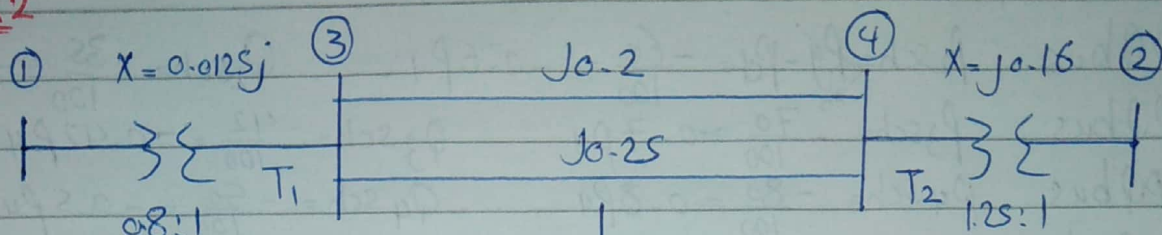
$$V_{4acc}^{(1)} = V_4^{(0)} + \alpha (V_4^{(1)} - V_4^{(0)}) =$$

$$Q_5^{(1)} = -\text{Im} \left[ V_5^{(0)*} \left[ Y_{51}V_1^{(0)} + Y_{52}V_2^{(0)} + Y_{53}V_3^{(0)} + Y_{54}V_4^{(0)} + Y_{55}V_5^{(0)} \right] \right]$$

$$V_5^{(1)} = \frac{1}{Y_{55}} \left[ \frac{P_{5sch} - jQ_{5sch}}{V_5^{(0)}} - Y_{51}V_1^{(0)} - Y_{52}V_2^{(0)} - Y_{53}V_3^{(0)} - Y_{54}V_4^{(0)} \right] =$$

$$V_{5Gr}^{(1)} = \frac{1 \angle 0}{\sqrt{\phantom{x}}} = \angle$$

Ex2



$$y_t = \frac{1}{j0.0125} = -j80$$

$$y_{t2} = \frac{1}{j0.16} = -j6.25$$

$$\begin{aligned} \text{at Trans 1} \quad (1-3) &\rightarrow y_t/a = -j80 = -j100 \\ (1-0) &\rightarrow \left(\frac{1-a}{a^2}\right)y_t = \frac{(1-0.8) \times -j80}{(0.8)^2} = -j25 \end{aligned}$$

$$(3-0) \rightarrow \left(\frac{a-1}{a}\right)y_t = \frac{(0.8-1) \times -j80}{0.8} = j20$$

$$\text{at } T_2 \quad (4-2) \rightarrow y_t/a = \frac{-j6.25}{1.25} = -j5$$

$$(4-0) = \left(\frac{1-a}{a^2}\right)y_t = \frac{1-1.25}{(1.25)^2} \times -j6.25 = j$$

$$(2-0) = \left(\frac{a-1}{a}\right)y_t = \frac{1.25-1}{1.25} \times -j6.25 = -j1.25$$

$$Y_{bus} = \begin{bmatrix} -j125 & 0 & -j100 & 0 \\ 0 & -j6.25 & -j & -j5 \\ -j100 & 0 & -j89 & -j9 \\ 0 & -j5 & -j9 & -j13 \end{bmatrix}$$