

**S1 Text. Derivation of the relationship between the dispersion parameter and the mean crowding parameter.**

1. Let  $m^*$  be mean crowding and  $m$  be the mean.

$$m^* = m + \left(\frac{\sigma^2}{m} - 1\right) \text{ (by definition of mean crowding)}$$

$$\implies m^* - m = \frac{\sigma^2}{m} - 1$$

2. Let  $\theta$  be the dispersion parameter and  $\sigma^2$  be the variance of the negative binomial distribution.

$$\sigma^2 = m + \frac{m^2}{\theta} \text{ (by definition of negative binomial variance)}$$

$$\implies \frac{\sigma^2}{m} = 1 + \frac{m}{\theta}$$

$$\implies \frac{m}{\theta} = \frac{\sigma^2}{m} - 1$$

3.  $\frac{m^*}{m} - 1 = \frac{1}{\theta}$  (by equating the left-hand sides of the results in 1 and 2 and dividing by  $m$ )

$$\implies m^* = m + \frac{m}{\theta}$$