

STA365 Homework 4

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Please submit your answers as a **single pdf document** via Quercus. The documents should be prepared in an RMarkdown document. It will be **Due Tuesday 31 March at 12pm**. Late submissions will be heavily penalized.

This homework counts towards 5% of the final grade for the course.

Multilevel Regression and Poststratification

A very scientific (and definitely very real) survey was conducted to find out whether a person preferred cats or dogs. The data is here:

```
survey <- readr::read_csv(file = "survey.csv" )
```

```
## Parsed with column specification:
## cols(
##   cat_pref = col_double(),
##   male = col_double(),
##   age = col_double(),
##   eth = col_double(),
##   income = col_double(),
##   state = col_double(),
##   id = col_double()
## )
```

```
head(survey)
```

```
## # A tibble: 6 x 7
##   cat_pref male   age   eth income state   id
##   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1         1     0     7     3     1    13     1
## 2         1     0     7     2     1    37     2
## 3         1     1     5     3     2    45     3
## 4         1     1     7     1     1     1     4
## 5         0     1     5     1     3    12     5
## 6         1     0     6     3     3    14     6
```

The first column `cat_pref` records a 1 if the respondent preferred cats over dogs. The remaining columns encode if a person is male or not, their age group (1-7), race/ethnicity (1-3), income group (1-3), and state (1-50). The `id` column is not useful for us.

The full population information is contained in the following poststratification matrix.

```
poststrat <- readr::read_csv(file = "poststrat.csv" )
```

```
## Parsed with column specification:
## cols(
##   male = col_double(),
##   eth = col_double(),
##   age = col_double(),
##   income = col_double(),
```

```
## state = col_double(),
## N = col_double()
## )
```

```
head(poststrat)
```

```
## # A tibble: 6 x 6
##   male   eth   age income state      N
##   <dbl> <dbl> <dbl>   <dbl> <dbl>   <dbl>
## 1     0     1     1       1     1  94877
## 2     0     1     1       1     2 156645
## 3     0     1     1       1     3 137803
## 4     0     1     1       1     4 141987
## 5     0     1     1       1     5 121577
## 6     0     1     1       1     6  93574
```

Questions

1. Write a stan program that fits a multilevel logistic regression to the survey data. It should treat **male** as a fixed covariate (no random effect) and **age**, **ethnicity**, **income**, and **state** as varying intercepts. In mathematical notation, this is the model

$$y_i | p_i \sim \text{Binomial}(1, p_i)$$

$$\log \left(\frac{p_i}{1 - p_i} \right) = \mu + \beta \text{male} + \alpha_{\text{age}(i)}^{(\text{age})} + \alpha_{\text{eth}(i)}^{(\text{eth})} + \alpha_{\text{inc}(i)}^{(\text{inc})} + \alpha_{\text{state}(i)}^{(\text{state})}$$

where the notation $\text{age}(i)$ is the age group that observation i is in.

2. Use the poststratification matrix and the samples from the posterior (which you can extract using the **extract** function) to get the posterior of the total proportion of cat lovers. Plot the posterior.