

# UV Absorbance characteristics in Northern Lakes

<https://github.com/rachelbash/absorbance-data-project>

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## **Abstract**

Experimental overview. This section should be no longer than 250 words. What contributes to absorbance values in the NTL\_LTER Carbon data set (will consider things such as DIC, DOC, depth, and water pressure). Also, is there a significant change in absorbance values in lakes over time?

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# 1 Research Question and Rationale

Absorbance is a unitless measurement that describes how much a substance can absorb light over a certain range of wavelength. The absorbance values of water samples from lakes can provide details regarding its physical characteristics and the health of the lake. The amount of light entering a lake is a component that drives photosynthesis and lake metabolism. Additionally, lake temperature and its absorbance characteristics are deeply intertwined. With the right equipment, absorbance is fairly easy to measure. Therefore, measuring absorbance in lakes can give researchers insight into other processes happening that depend in part on sunlight, such as algal growth or temperature-dependent processes.

This research project intends to answer two main questions:

- What contributes to absorbance values in five lakes located in Michigan's Upper Peninsula?
- Do absorbance values in these five study lakes change over time?

The data that answer these questions come from the North Temperate Lakes Project, which seeks to measure data on carbon and other related variables in lakes. My analysis of the data provides a model that shows the variables that best predict absorbance values and also takes a closer look at how absorbance values have changed over time in different lakes. Time variations in absorbance have implications that other physical characteristics are changing, which may damage biota in the lakes or bring about significant changes in the greater ecosystem that surrounds the lake.

## 2 Dataset Information

The dataset was collected from 1984 to 2016 by researchers working for the Cascade Project and Northern Temperate Lakes at a total of 14 sites. Samples of water were collected, and then were measured. Measurements included dissolved organic and inorganic carbon, particulate organic matter, partial pressure of carbon dioxide, and absorbance. Absorbance was measured using a spectrophotometer at a wavelength of 440nm.

For some variables, a water depth sample was taken that was measured in meters, while in others, samples were taken to reflect a depth that was proportional across all lakes. Therefore, Hypolimnion, Epilimnion, Metalimnion, and pooled mixed layer (PML) are also included as depth values. All water samples were taken with a syringe and then filtered through a mesh filter in order to remove any large debris or zooplankton.

Data Summary	Relevant Information
Date range	1984-06-03 to 2016-08-17
Structure	15 variables with 13,557 observations
Column variables	Lake ID, Lake Name, Year, Day No., Date, Depth, Depth ID, TPC, TPC, DIC, PCO2 air, PCO2 water, DOC, Absorbance
Lakes sampled	Crampton Lake, East Long Lake, Hummingbird Lake, Long Lake, Morris Lake, North Gate Bog, Paul Lake, Peter Lake, Reddington Lake, Roach Lake, Tender Bog, Tuesday Lake, Ward Lake, West Long Lake

## 3 Exploratory Data Analysis and Wrangling

### 3.1 Importing raw data and identifying its attributes

```
colnames(carbon.data)
```

```
## [1] "lakeid"      "lakename"    "year4"       "daynum"      "sampledate"
## [6] "depth"       "depth_id"    "tpc"         "tpn"         "DIC_mg"
## [11] "DIC_uM"      "air_pco2"    "water_pco2"  "doc"         "absorbance"
```

```
str(carbon.data)
```

```
## 'data.frame': 13557 obs. of 15 variables:
## $ lakeid : Factor w/ 14 levels "E","H","L","Long",...: 3 3 3 3 3 8 8 8 8 8 ...
## $ lakename : Factor w/ 14 levels "Crampton Lake",...: 7 7 7 7 7 8 8 8 8 8 ...
## $ year4 : int 1984 1984 1984 1984 1984 1984 1984 1984 1984 1984 ...
## $ daynum : int 155 155 155 155 155 156 156 156 156 156 ...
## $ sampledate: Date, format: "1984-06-03" "1984-06-03" ...
## $ depth : Factor w/ 231 levels "0","0.1","0.15",...: 1 62 102 140 180 1 62 102 140 2 ...
## $ depth_id : int 1 2 3 4 5 1 2 3 4 5 ...
## $ tpc : num NA NA NA NA NA NA NA NA NA NA NA ...
## $ tpn : num NA NA NA NA NA NA NA NA NA NA NA ...
## $ DIC_mg : num 1.45 1.82 1.51 1.47 2.69 2.85 2.84 3.27 2.98 7.26 ...
## $ DIC_uM : num 121 152 126 122 224 ...
## $ air_pco2 : num NA NA NA NA NA NA NA NA NA NA NA ...
## $ water_pco2: num NA NA NA NA NA NA NA NA NA NA NA ...
## $ doc : num NA NA NA NA NA NA NA NA NA NA NA ...
## $ absorbance: num NA NA NA NA NA NA NA NA NA NA NA ...
```

```
summary(carbon.data)
```

```
##      lakeid      lakename      year4      daynum
## R      :3887    Peter Lake    :3887    Min.     :1984    Min.     : 82.0
## L      :3852    Paul Lake     :3852    1st Qu.:1993    1st Qu.:166.0
## T      :1818    Tuesday Lake :1818    Median :1999    Median :192.0
## W      :1571    West Long Lake:1571    Mean    :2000    Mean    :192.4
## E      :1435    East Long Lake:1435    3rd Qu.:2007    3rd Qu.:218.0
## M      : 456    Crampton Lake : 456    Max.     :2016    Max.     :310.0
## (Other): 538    (Other)       : 538
##      sampledate      depth      depth_id      tpc
## Min.     :1984-06-03    0      :1719    Min.     : -2.000    Min.     : 0.100
## 1st Qu.:1993-06-16    Metalimnion:1297    1st Qu.: 1.000    1st Qu.: 0.580
## Median :1999-07-06    Hypolimnion:1020    Median : 3.000    Median : 0.890
## Mean    :2000-07-14    PML           : 876    Mean    : 2.775    Mean    : 1.110
## 3rd Qu.:2007-08-28    Epilimnion   : 570    3rd Qu.: 5.000    3rd Qu.: 1.305
## Max.     :2016-08-17    (Other)      :7918    Max.     : 7.000    Max.     :11.860
##                      NA's      : 157    NA's     :170      NA's     :11410
##      tpn      DIC_mg      DIC_uM      air_pco2
```

```
## Min. :0.000 Min. : 0.023 Min. : 1.917 Min. :197.7
## 1st Qu.:0.070 1st Qu.: 0.812 1st Qu.: 67.625 1st Qu.:343.4
## Median :0.103 Median : 1.322 Median : 110.167 Median :362.9
## Mean :0.149 Mean : 2.310 Mean : 192.487 Mean :360.4
## 3rd Qu.:0.180 3rd Qu.: 1.968 3rd Qu.: 164.000 3rd Qu.:379.0
## Max. :2.170 Max. :48.599 Max. :4049.883 Max. :608.1
## NA's :11409 NA's :3642 NA's :3642 NA's :12411
## water_pco2 doc absorbance
## Min. : 0.0 Min. : 2.710 Min. :0.011
## 1st Qu.: 478.0 1st Qu.: 4.570 1st Qu.:0.060
## Median : 838.5 Median : 5.603 Median :0.146
## Mean :1012.3 Mean : 6.932 Mean :0.194
## 3rd Qu.:1175.6 3rd Qu.: 8.370 3rd Qu.:0.265
## Max. :9348.2 Max. :44.080 Max. :1.213
## NA's :12411 NA's :9993 NA's :10658
```

```
dim(carbon.data)
```

```
## [1] 13557 15
```

```
summary(carbon.data$absorbance)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
## 0.011 0.060 0.146 0.194 0.265 1.213 10658
```

```
class(carbon.data$depth)
```

```
## [1] "factor"
```

```
head(carbon.data$depth, 10)
```

```
## [1] 0 1 2 3.5 5.5 0 1 2 3.5 7
## 231 Levels: 0 0.1 0.15 0.17 0.18 0.19 0.2 0.21 0.22 0.23 0.25 0.28 ... surface
```

These exploratory commands above function as helpful tools that help me see what kind of shape my data are in. It shows me how many NA's I have, what variables I am working with, the classes of my variables, and basic summary statistics. An important thing I discovered while doing the initial exploratory data analysis is that the depth variable has both numeric and factor-level observations, which is why its class is listed as **factor**. In other words, depth was measured in both numeric terms (1 meter, 13 meters, etc), but also in thermally stratified terms, such as Hypolimnion, Metalimnion, and Epilimnion. This was an important discovery that led to further data wrangling and filtering of this specific variable.

## 3.2 Visualizing the data

As seen by Figure 1, Absorbance values are not normally distributed. This is expected, as we are dealing with ecological data.

Relatedly, Figure 2 shows that different levels of depth (factor) had difference absorbance frequency values. It was helpful to create this graph to show that absorbance was measured at multiple



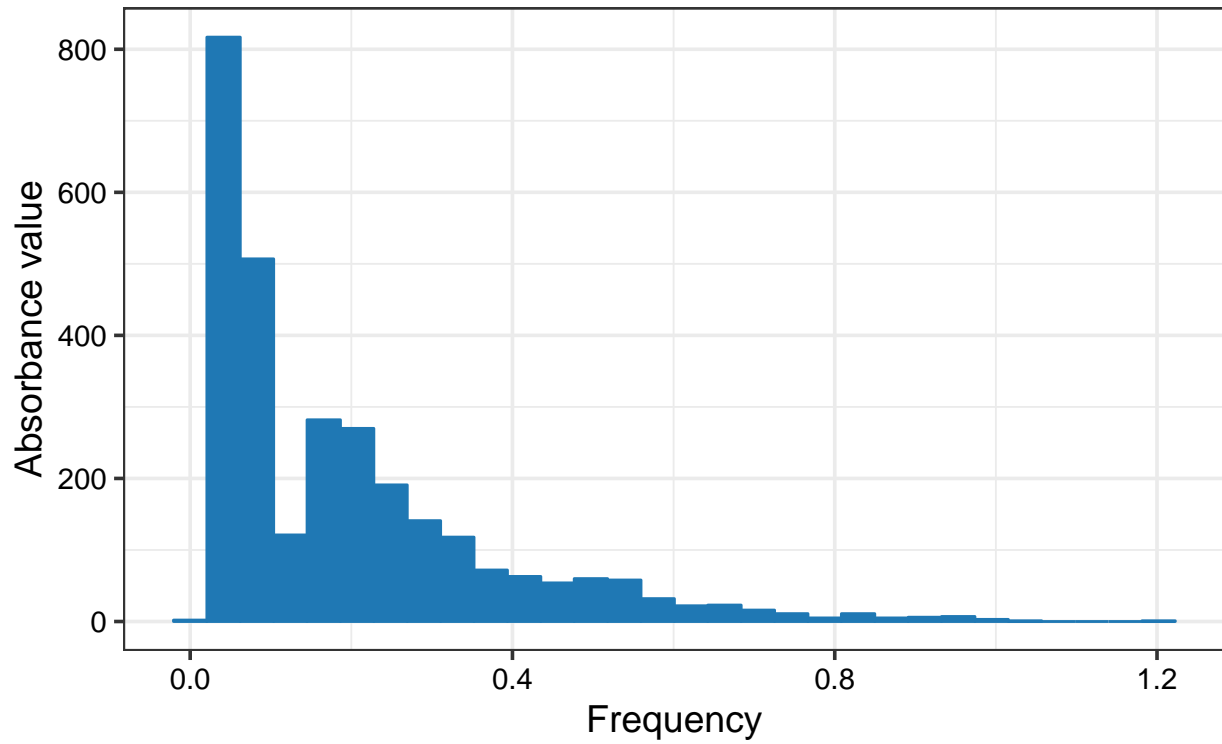


Figure 1: Absorbance frequency

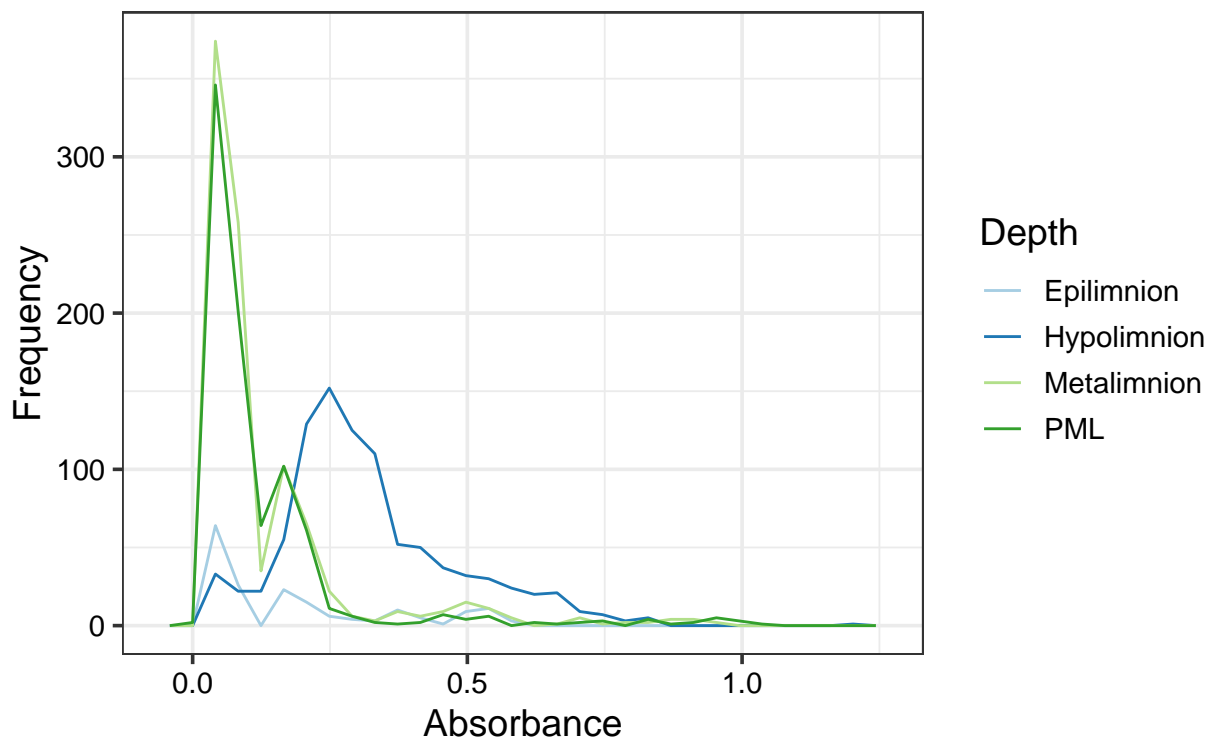


Figure 2: Absorbance frequency by depth category

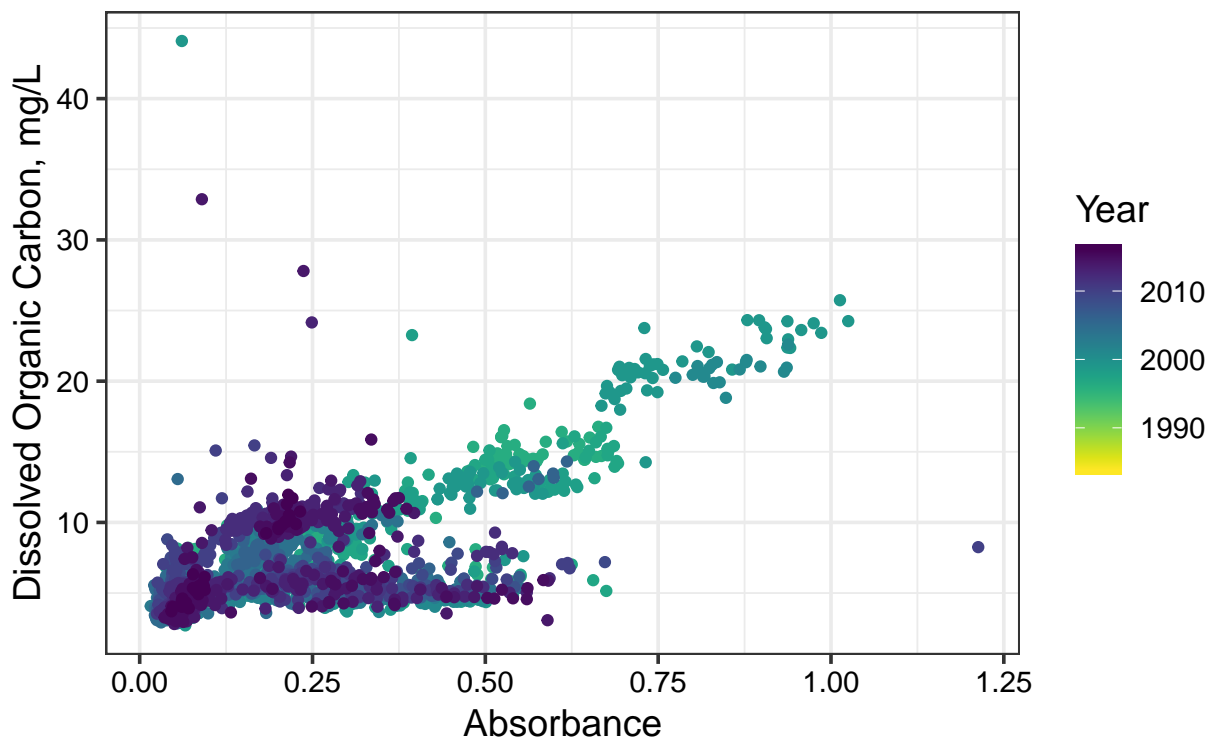


Figure 3: Dissolved organic carbon and absorbance relationship by year

different water depth levels.

Figure 3 shows a positive relationship between dissolved organic carbon and absorbance, with a layer of color by year. This result is expected, and it gave me a good sense of what to expect during my analysis portion of the project. It is interesting to note that as time went on, measures for both absorbance and for DOC began to shrink to smaller values, as seen with the color gradient by year.

### 3.3 Data Wrangling

```
carbon.data.processed <- carbon.data %>%
  filter(depth %in% c("PML", "Hypolimnion", "Epilimnion", "Metalimnion")) %>%
  filter(lakename %in% c("Peter Lake", "Paul Lake", "East Long Lake", "Tuesday Lake", "Wes")) %>%
  select(lakename:depth_id, DIC_mg, doc, absorbance, tpc)
```

There were many things to consider when wrangling my data to a more manageable and workable dataset. I noticed that all absorbance values had associated depth measurements using only the thermally stratified depth categories. Therefore, I filtered out any depth that was measured in meters, in order to simplify the process. Next, I chose the five lakes in the dataset that had the most number of data points. Shortening the lake list from 14 to 5 gives the research project a more focused view and potentially stronger relationships among variables. Lastly, I selected only the columns that I wanted to study and that could be analyzed in relation to absorbance values. These variables included lake name, depth, dissolved inorganic carbon, dissolved organic carbon, total particulate carbon, and absorbance.

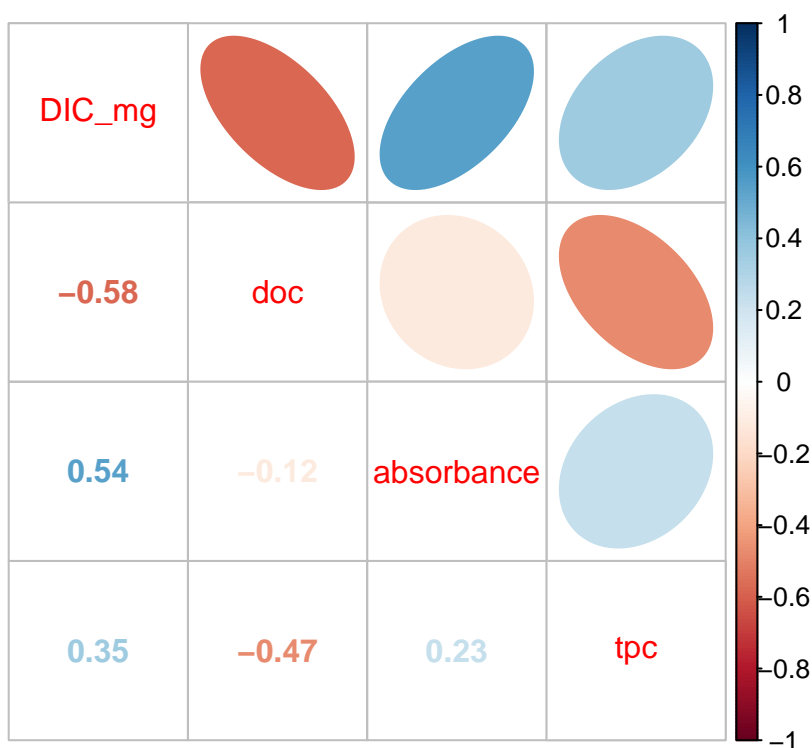


Figure 4: Correlation plot between continuous variables

### 3.4 Correlation between continuous variables

The last piece of data exploration I completed was visualizing the correlation between the continuous variables in the data. Figure 4 illustrates the relationships between each of the continuous variables in question. All relationship correlations range pretty low to moderate, with DOC and absorbance having the lowest correlation coefficient of -0.12, and DIC and DOC having the highest negative correlation coefficient of -0.58. It is important to consider this visualization critically, as the data have been thoroughly at this point, leaving much fewer data points than what we started with, which could manipulate the strength (or weakness) of these correlation coefficients.

## 4 Analysis

### 4.1 Differences in absorbance values across lakes

It was important for me to know whether absorbance values were significantly different across the five lakes of interest. This can be answered by a simple ANOVA test. However, the data must meet certain criteria. First, data had to be normally distributed, and second, equal variance across groups must exist. I tested these assumptions using the Shapiro test and the Bartlett test, respectively. Both tests resulted in significant p-values, indicating that the data fail the tests for normality and equal variances.

Therefore, another method had to be utilized. I opted for a non-parametric test called the Kruskal Wallis test, a great alternative to ANOVAs. Here, I received a significant p-value result, indicating that there is a significant difference in absorbance values across different lakes. A non-parametric post-hoc test (Dunn Test) reveals that all lakes' mean absorbance values are significantly different from all other lakes (p-values < 0.05). ?? illustrates how absorbance values vary vastly by lake. Even though all of these lakes are located close to each other in Michigan's Upper Peninsula along the Wisconsin border, it is clear that absorbance values can vary greatly among them.

```
# test for normality
shapiro.test(carbon.data.processed$absorbance
             [carbon.data.processed$lakename == "Tuesday Lake"])

##
##  Shapiro-Wilk normality test
##
## data:  carbon.data.processed$absorbance[carbon.data.processed$lakename == "Tuesday Lake"]
## W = 0.97269, p-value = 8.155e-06

shapiro.test(carbon.data.processed$absorbance
             [carbon.data.processed$lakename == "Paul Lake"])

##
##  Shapiro-Wilk normality test
##
## data:  carbon.data.processed$absorbance[carbon.data.processed$lakename == "Paul Lake"]
## W = 0.71627, p-value < 2.2e-16

shapiro.test(carbon.data.processed$absorbance
             [carbon.data.processed$lakename == "Peter Lake"])

##
##  Shapiro-Wilk normality test
##
## data:  carbon.data.processed$absorbance[carbon.data.processed$lakename == "Peter Lake"]
## W = 0.79554, p-value < 2.2e-16

shapiro.test(carbon.data.processed$absorbance
             [carbon.data.processed$lakename == "East Long Lake"])
```

```
##
## Shapiro-Wilk normality test
##
## data: carbon.data.processed$absorbance[carbon.data.processed$lakename == "East Long
## W = 0.92578, p-value = 1.573e-09

shapiro.test(carbon.data.processed$absorbance
             [carbon.data.processed$lakename == "West Long Lake"])
```

```
##
## Shapiro-Wilk normality test
##
## data: carbon.data.processed$absorbance[carbon.data.processed$lakename == "West Long
## W = 0.94549, p-value = 1.008e-08

#result: all have significant p-values, meaning they are not normally distributed data

#bartlett test to determine whether there is equal variance between groups
bartlett.test(carbon.data.processed$absorbance ~ carbon.data.processed$lakename)
```

```
##
## Bartlett test of homogeneity of variances
##
## data: carbon.data.processed$absorbance by carbon.data.processed$lakename
## Bartlett's K-squared = 846.15, df = 4, p-value < 2.2e-16

#result: significant p-value, not equal variances

#non-parametric test instead
kruskal.test(carbon.data.processed$absorbance ~ carbon.data.processed$lakename)
```

```
##
## Kruskal-Wallis rank sum test
##
## data: carbon.data.processed$absorbance by carbon.data.processed$lakename
## Kruskal-Wallis chi-squared = 739.62, df = 4, p-value < 2.2e-16

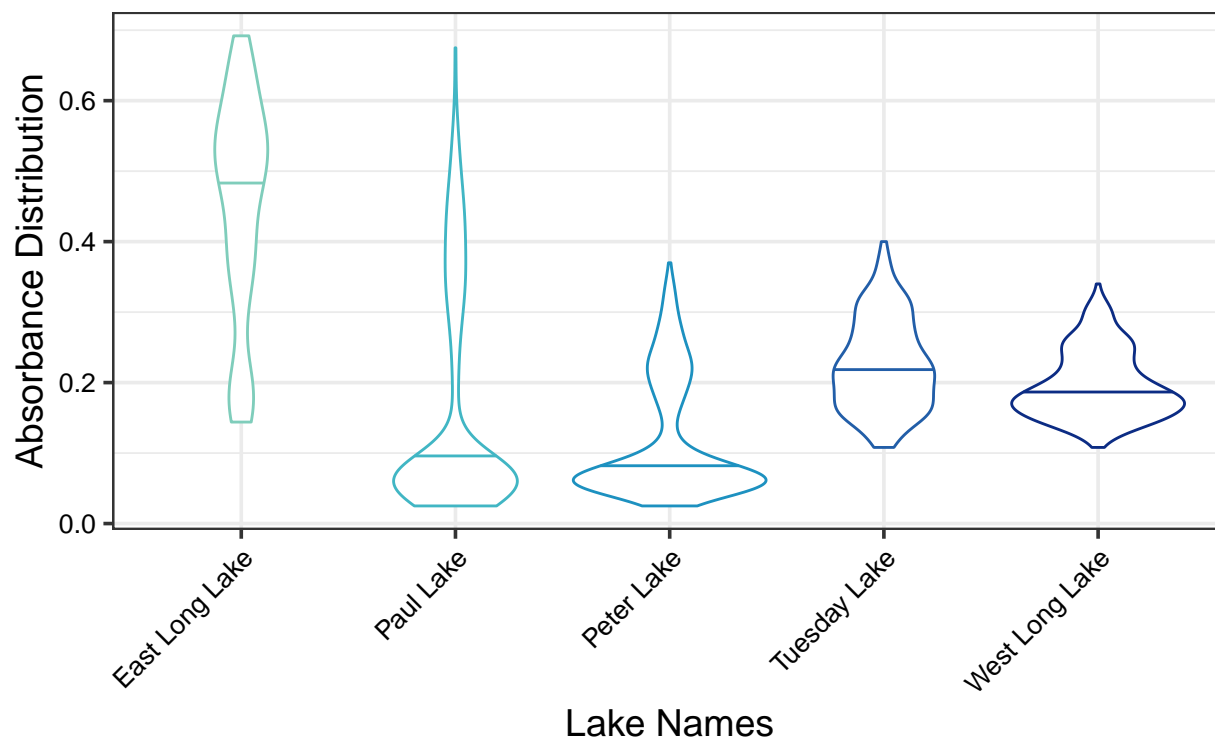
#lakename is a significant predictor of absorbance

#post-hoc non-parametric test
dunnTest(carbon.data.processed$absorbance ~ carbon.data.processed$lakename)
```

	Comparison	Z	P.unadj	P.adj
## 1	East Long Lake - Paul Lake	21.376177	2.226386e-101	2.003747e-100
## 2	East Long Lake - Peter Lake	23.056681	1.260584e-117	1.260584e-116
## 3	Paul Lake - Peter Lake	2.633408	8.453271e-03	1.690654e-02
## 4	East Long Lake - Tuesday Lake	8.552531	1.204182e-17	3.612546e-17
## 5	Paul Lake - Tuesday Lake	-12.824220	1.199877e-37	8.399141e-37
## 6	Peter Lake - Tuesday Lake	-14.730183	4.125885e-49	3.300708e-48
## 7	East Long Lake - West Long Lake	10.416882	2.076502e-25	1.038251e-24

```
## 8      Paul Lake - West Long Lake  -9.446619  3.499535e-21  1.399814e-20
## 9      Peter Lake - West Long Lake -11.265531  1.941779e-29  1.165067e-28
## 10     Tuesday Lake - West Long Lake  2.295393  2.171061e-02  2.171061e-02
```

*#shows all lakes differ from one another significantly*



## 4.2 Linear regression model

In order to determine what factors contribute to absorbance values, I conducted a step-wise linear regression model. I was not able to include DIC in the full model, because DIC was only measured at numeric depths and not thermally stratified depths. Therefore, no data between absorbance and DIC overlapped. The full model included the following parameters: depth, DOC, Lake Name, and Total Particulate Carbon.

By performing a step-wise linear regression model, I can use the lowest Akaike's Information Criterion (AIC) value to determine the ideal statistical model that balances both simplicity and statistical power. The regression analysis showed that all variables are significant and allow us to best predict absorbance values. The resulting linear expression is as follows:

$$\begin{aligned} \text{Absorbance} = & 0.18(\text{Epi} * \text{East}) + 0.17(\text{Hypo}) + 0.02(\text{DOC}) - \\ & 0.18(\text{Paul}) - 0.24(\text{Peter}) - 0.23(\text{Tuesday}) - 0.19(\text{West}) + 0.02(\text{TPC}) \end{aligned}$$

For example, for every one unit increase in DOC, absorbance value increases by 0.02 units. Alternatively, if absorbance is measured in Peter Lake, absorbance will decrease by 0.24 units. The step function shows that all variables, except for Metalimnion and PML depth categories were significant predictors of absorbance, and the full model had an adjusted R-squared value of 0.86, which is quite significant. However, it is important to note that because of missing values within each of the variables, there is an exceptionally high degrees of freedom value of 1119.

?? illustrates all predictors, with the exception of lake name, and their relationship to absorbance.

*#Step-wise linear regression*

```
steplm <- lm(data=carbon.data.processed, absorbance ~ depth + doc + lakename + tpc)
step(steplm)
```

```
## Start: AIC=-6251.63
## absorbance ~ depth + doc + lakename + tpc
##
##           Df Sum of Sq   RSS   AIC
## <none>                4.3669 -6251.6
## - tpc             1    0.1978 4.5647 -6203.6
## - doc             1    0.5211 4.8880 -6126.4
## - lakename        4    3.2696 7.6365 -5628.7
## - depth           3    5.1414 9.5084 -5379.1
##
## Call:
## lm(formula = absorbance ~ depth + doc + lakename + tpc, data = carbon.data.processed)
##
## Coefficients:
##           (Intercept)          depthHypolimnion          depthMetalimnion
##           0.175600              0.171535              0.008826
##           depthPML              doc          lakenamePaul Lake
##           0.005411              0.018642             -0.184280
```

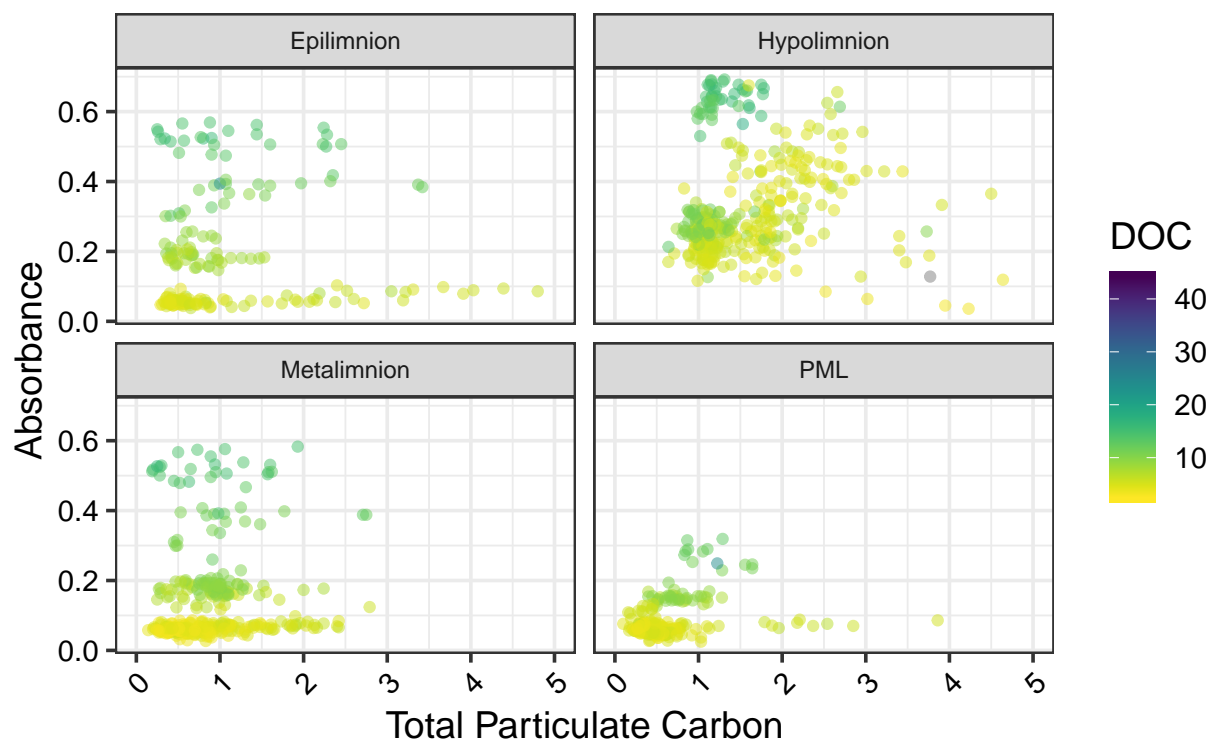
```
##      lakenamePeter Lake      lakenameTuesday Lake      lakenameWest Long Lake
##              -0.241944              -0.229613              -0.188448
##              tpc
##              0.018681

#taking out none would result in the lowest AIC value

#full-model is the best, as shown by the step
fullmodel <- lm(data=carbon.data.processed, absorbance ~ depth + doc + lakename + tpc)
summary(fullmodel)

##
## Call:
## lm(formula = absorbance ~ depth + doc + lakename + tpc, data = carbon.data.processed)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.27056 -0.03147 -0.00548  0.02536  0.38625
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      0.175600   0.023113   7.598 6.35e-14 ***
## depthHypolimnion    0.171535   0.006031  28.441 < 2e-16 ***
## depthMetalimnion    0.008826   0.005946   1.484  0.138
## depthPML           0.005411   0.006724   0.805  0.421
## doc                0.018642   0.001613  11.555 < 2e-16 ***
## lakenamePaul Lake   -0.184280   0.015929 -11.569 < 2e-16 ***
## lakenamePeter Lake  -0.241944   0.014605 -16.566 < 2e-16 ***
## lakenameTuesday Lake -0.229613   0.009794 -23.444 < 2e-16 ***
## lakenameWest Long Lake -0.188448   0.011833 -15.926 < 2e-16 ***
## tpc                0.018681   0.002624   7.119 1.94e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06247 on 1119 degrees of freedom
## (2294 observations deleted due to missingness)
## Multiple R-squared:  0.8584, Adjusted R-squared:  0.8572
## F-statistic: 753.6 on 9 and 1119 DF, p-value: < 2.2e-16
```





## 4.3 Time Series Analysis

A time series analysis will show whether absorbance values in lakes have changed over time. I used a Mann Kendall test to determine whether there is a monotonic overall trend in absorbance over time for the five lakes of interest. While there is perhaps seasonality differences in absorbance values, I am only interested in yearly trends, and so have decided not to look at seasonal differences of absorbance.

```
#trimming data to only look at points of interest
carbon.data.processed.trimmed <- carbon.data.processed %>%
  filter(depth == "Hypolimnion") %>%
  select(absorbance, sampleddate, lakename) %>%
  filter(sampledate > as.Date("1996-06-01") & sampleddate < as.Date("2016-08-17"))
```

### 4.3.1 East Long Lake

```
#East Lake
East.mktest <- filter(carbon.data.processed.trimmed, lakename == "East Long Lake")

#run MK test
mk.test(East.mktest$absorbance) #p=2e-9, so there is a significant negative trend from be

##
## Mann-Kendall trend test
##
## data: East.mktest$absorbance
## z = -5.9962, n = 73, p-value = 2.019e-09
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## -1260.0000000 44085.3333333   -0.4800003

# Test for change point
pettitt.test(East.mktest$absorbance) #change point detected at place 30 1998-05-28

##
## Pettitt's test for single change-point detection
##
## data: East.mktest$absorbance
## U* = 1165, p-value = 2.151e-09
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                                30

#run second MK test for each change point range
mk.test(East.mktest$absorbance[1:29]) #p=1e-5, significant positive trend in this range
```

```

##
## Mann-Kendall trend test
##
## data: East.mktest$absorbance[1:29]
## z = 4.4118, n = 29, p-value = 1.025e-05
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 236.0000000 2837.3333333 0.5841656

#test for change point
pettitt.test(East.mktest$absorbance[1:29]) #change point detected at place 17 1997-06-12

##
## Pettitt's test for single change-point detection
##
## data: East.mktest$absorbance[1:29]
## U* = 185, p-value = 0.0005838
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                                17

mk.test(East.mktest$absorbance[1:16]) #no trend

##
## Mann-Kendall trend test
##
## data: East.mktest$absorbance[1:16]
## z = 1.2156, n = 16, p-value = 0.2241
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 28.0000000 493.3333333 0.2333333

mk.test(East.mktest$absorbance[17:29]) #no trend

##
## Mann-Kendall trend test
##
## data: East.mktest$absorbance[17:29]
## z = 1.5972, n = 13, p-value = 0.1102
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 27.0000000 265.0000000 0.353009

mk.test(East.mktest$absorbance[30:73]) #significant negative trend over time

##

```

```

## Mann-Kendall trend test
##
## data: East.mktest$absorbance[30:73]
## z = -3.4795, n = 44, p-value = 0.0005024
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## -345.0000000 9774.3333333 -0.3648864

pettitt.test(East.mktest$absorbance[30:73]) #change point detected at place 17 (which mea

##
## Pettitt's test for single change-point detection
##
## data: East.mktest$absorbance[30:73]
## U* = 365, p-value = 0.0002071
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                                17

mk.test(East.mktest$absorbance[30:46]) #no trend

##
## Mann-Kendall trend test
##
## data: East.mktest$absorbance[30:46]
## z = 0.82455, n = 17, p-value = 0.4096
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
##  21.0000000 588.3333333  0.1549826

mk.test(East.mktest$absorbance[47:73]) #no trend

##
## Mann-Kendall trend test
##
## data: East.mktest$absorbance[47:73]
## z = 0, n = 27, p-value = 1
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## -1.000000e+00 2.301000e+03 -2.849003e-03

```

### 4.3.2 West Long Lake

```
#split data by lake
West.mktest <- filter(carbon.data.processed.trimmed, lakename == "West Long Lake")

#run MK test
mk.test(West.mktest$absorbance) #p is significant, so there is a significant negative trend

##
## Mann-Kendall trend test
##
## data: West.mktest$absorbance
## z = -4.8587, n = 87, p-value = 1.181e-06
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## -1326.0000000 74368.0000000  -0.3559285

# Test for change point
pettitt.test(West.mktest$absorbance) #change point detected at place 44 1998-08-31

##
## Pettitt's test for single change-point detection
##
## data: West.mktest$absorbance
## U* = 1584, p-value = 3.057e-10
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                                44

#run second MK test for each change point range
mk.test(West.mktest$absorbance[1:43]) #no trend

##
## Mann-Kendall trend test
##
## data: West.mktest$absorbance[1:43]
## z = 0.59704, n = 43, p-value = 0.5505
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 5.800000e+01 9.114667e+03 6.469774e-02

mk.test(West.mktest$absorbance[44:87]) #no significant trend in this range

##
## Mann-Kendall trend test
##
```

```
## data: West.mktest$absorbance[44:87]
## z = 1.4676, n = 44, p-value = 0.1422
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 146.0000000 9762.0000000  0.1553223
```

### 4.3.3 Peter Lake

```
#Peter Lake
Peter.mktest <- filter(carbon.data.processed.trimmed, lakename == "Peter Lake") %>% na.omit()

#run MK test
mk.test(Peter.mktest$absorbance) #p val is significant so there is a significant positive trend

##
## Mann-Kendall trend test
##
## data: Peter.mktest$absorbance
## z = 4.8159, n = 287, p-value = 1.465e-06
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 7.826000e+03 2.640047e+06 1.911373e-01

# Test for change point
pettitt.test(Peter.mktest$absorbance) #change point detected at place 202 2011-06-06

##
## Pettitt's test for single change-point detection
##
## data: Peter.mktest$absorbance
## U* = 7794, p-value = 4.25e-07
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                               202

#run second MK test for each change point range
mk.test(Peter.mktest$absorbance[1:201]) #p>0.05, no significant trend in this date range

##
## Mann-Kendall trend test
##
## data: Peter.mktest$absorbance[1:201]
## z = -0.89267, n = 201, p-value = 0.372
## alternative hypothesis: true S is not equal to 0
```

```

## sample estimates:
##           S           varS           tau
## -8.520000e+02  9.088247e+05 -4.250453e-02
mk.test(Peter.mktest$absorbance[202:287]) #significant positive trend over time

##
## Mann-Kendall trend test
##
## data: Peter.mktest$absorbance[202:287]
## z = 4.0658, n = 86, p-value = 4.786e-05
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##           S           varS           tau
## 1.091000e+03 7.187167e+04 2.989044e-01
pettitt.test(Peter.mktest$absorbance[202:287]) #change point detected at place 50 (which

##
## Pettitt's test for single change-point detection
##
## data: Peter.mktest$absorbance[202:287]
## U* = 1301, p-value = 2.796e-07
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                               50
mk.test(Peter.mktest$absorbance[202:251]) #no trend

##
## Mann-Kendall trend test
##
## data: Peter.mktest$absorbance[202:251]
## z = -1.9409, n = 50, p-value = 0.05227
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##           S           varS           tau
## -233.0000000 14287.6666667  -0.1905154
mk.test(Peter.mktest$absorbance[252:287]) #no trend

##
## Mann-Kendall trend test
##
## data: Peter.mktest$absorbance[252:287]
## z = 0.29974, n = 36, p-value = 0.7644
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##           S           varS           tau

```

```
## 2.300000e+01 5.387000e+03 3.659517e-02
```

#### 4.3.4 Paul Lake

```
#Paul Lake
```

```
Paul.mktest <- filter(carbon.data.processed.trimmed, lakename == "Paul Lake") %>% na.omit()
```

```
#run MK test
```

```
mk.test(Paul.mktest$absorbance) #p>0.05 so no significant over time
```

```
##
```

```
## Mann-Kendall trend test
```

```
##
```

```
## data: Paul.mktest$absorbance
```

```
## z = -1.6421, n = 291, p-value = 0.1006
```

```
## alternative hypothesis: true S is not equal to 0
```

```
## sample estimates:
```

```
##           S           varS           tau
```

```
## -2.725000e+03 2.751921e+06 -6.466546e-02
```

```
# Test for change point
```

```
pettitt.test(Paul.mktest$absorbance) #change point detected at place 72 2001-08-20
```

```
##
```

```
## Pettitt's test for single change-point detection
```

```
##
```

```
## data: Paul.mktest$absorbance
```

```
## U* = 4575, p-value = 0.01245
```

```
## alternative hypothesis: two.sided
```

```
## sample estimates:
```

```
## probable change point at time K
```

```
##                               72
```

```
#run second MK test for each change point range
```

```
mk.test(Paul.mktest$absorbance[1:71]) #no trend
```

```
##
```

```
## Mann-Kendall trend test
```

```
##
```

```
## data: Paul.mktest$absorbance[1:71]
```

```
## z = -1.1566, n = 71, p-value = 0.2474
```

```
## alternative hypothesis: true S is not equal to 0
```

```
## sample estimates:
```

```
##           S           varS           tau
```

```
## -2.340000e+02 4.058333e+04 -9.425987e-02
```

```
mk.test(Paul.mktest$absorbance[72:291]) #no trend
```



```
##
## Mann-Kendall trend test
##
## data: Paul.mktest$absorbance[72:291]
## z = 1.7089, n = 220, p-value = 0.08747
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 1.866000e+03 1.191044e+06 7.756263e-02
```

#### 4.3.5 Tuesday Lake

```
#Tuesday
Tuesday.mktest <- filter(carbon.data.processed.trimmed, lakename == "Tuesday Lake") %>% na.rm()

#run MK test
mk.test(Tuesday.mktest$absorbance) #p is significant, so there is a significant positive trend

##
## Mann-Kendall trend test
##
## data: Tuesday.mktest$absorbance
## z = 3.4932, n = 102, p-value = 0.0004773
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 1.209000e+03 1.195877e+05 2.353522e-01

# Test for change point
pettitt.test(Tuesday.mktest$absorbance) #change point detected at place 68 2014-06-25

##
## Pettitt's test for single change-point detection
##
## data: Tuesday.mktest$absorbance
## U* = 1824, p-value = 1.626e-08
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                                68

#run second MK test for each change point range
mk.test(Tuesday.mktest$absorbance[1:67]) #p<0.05, significant negative trend in this range

##
## Mann-Kendall trend test
##
```

```

## data: Tuesday.mktest$absorbance[1:67]
## z = -3.3124, n = 67, p-value = 0.0009249
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## -613.0000000 34135.6666667   -0.2780056

#test for change point
pettitt.test(Tuesday.mktest$absorbance[1:67]) #change point detected at place 44 2012-08-

##
## Pettitt's test for single change-point detection
##
## data: Tuesday.mktest$absorbance[1:67]
## U* = 712, p-value = 9.409e-05
## alternative hypothesis: two.sided
## sample estimates:
## probable change point at time K
##                                44

mk.test(Tuesday.mktest$absorbance[1:43]) #no trend

##
## Mann-Kendall trend test
##
## data: Tuesday.mktest$absorbance[1:43]
## z = 0.8898, n = 43, p-value = 0.3736
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 8.600000e+01 9.125333e+03 9.550287e-02

mk.test(Tuesday.mktest$absorbance[44:67]) #no trend

##
## Mann-Kendall trend test
##
## data: Tuesday.mktest$absorbance[44:67]
## z = -0.62049, n = 24, p-value = 0.5349
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## -26.00000000 1623.3333333   -0.09454608

mk.test(Tuesday.mktest$absorbance[68:102]) #no trend

##
## Mann-Kendall trend test
##
## data: Tuesday.mktest$absorbance[68:102]

```

## Absorbance over Time

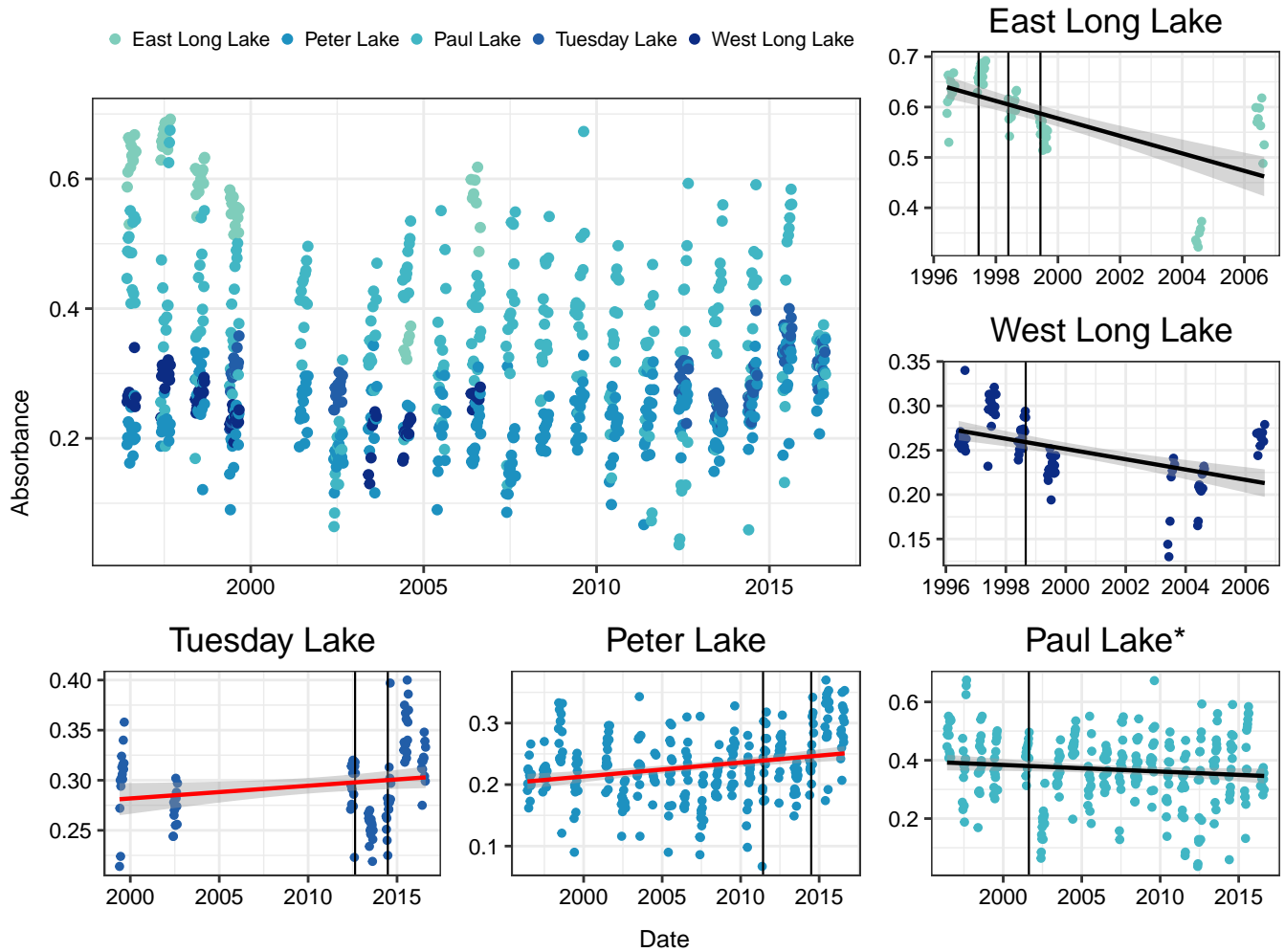


Figure 5: Absorbance in East Long Lake, West Long Lake, Peter Lake, Paul Lake, and Tuesday Lake over time

```
## z = 0.53976, n = 35, p-value = 0.5894
## alternative hypothesis: true S is not equal to 0
## sample estimates:
##          S          varS          tau
## 3.900000e+01 4.956333e+03 6.565666e-02

## TableGrob (5 x 4) "arrange": 9 grobs
##   z    cells    name      grob
## 1 1 (2-3,2-3) arrange    gtable[layout]
## 2 2 (2-2,4-4) arrange    gtable[layout]
## 3 3 (3-3,4-4) arrange    gtable[layout]
## 4 4 (4-4,2-2) arrange    gtable[layout]
## 5 5 (4-4,3-3) arrange    gtable[layout]
## 6 6 (4-4,4-4) arrange    gtable[layout]
## 7 7 (1-1,2-4) arrange text[GRID.text.799]
## 8 8 (5-5,2-4) arrange text[GRID.text.800]
```

```
## 9 9 (1-5,1-1) arrange text[GRID.text.801]
```

## 5 Summary and Conclusions