- Are translation equivalents special? Evidence from simulations and empirical data from
- bilingual infants
- Rachel Ka-Ying Tsui¹, Ana Maria Gonzalez-Barrero¹, Esther Schott¹, & Krista
- 4 Byers-Heinlein¹

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¹ Concordia University

Abstract 6

The acquisition of translation equivalents is often considered a special component of bilingual children's vocabulary development, as bilinguals have to learn words that share the same meaning across their two languages. This study examined three contrasting accounts for bilingual children's acquisition of translation equivalents relative to singlets 10 (i.e., words that are first labels for a referent): the Avoidance Account whereby translation 11 equivalents are harder to learn, the Preference Account whereby translation equivalents are 12 easier to learn, and the Neutral Account whereby translation equivalents and singlets are 13 learned similarly. To adjudicate between these accounts, Study 1 explored patterns of translation equivalent learning under a novel computational model — the Bilingual 15 Vocabulary Model — which quantifies translation equivalent knowledge as a function of the probability of learning words in each language, and includes a bias parameter that varies the difficulty of learning translation equivalents according to each account. Study 2 tested 18 model-derived predictions against vocabulary data from 200 French-English bilingual 19 children aged 18–33 months. Results showed a close match between the model predictions 20 and bilingual children's patterns of translation equivalent learning. At smaller vocabulary 21 sizes, data matched the Preference Account, while at larger vocabulary sizes they matched 22 the Neutral Account. Our findings show that patterns of translation equivalent learning 23 emerge predictably from the word learning process, and potentially reveal a qualitative 24 shift in translation equivalent learning as bilingual children develop and learn more words. 25 Keywords: bilingualism, infants, translation equivalents, vocabulary development, 26

word learning, computational modeling

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1 Introduction

Bilingual children must learn words that take a different form in each of their 31 languages, but share the same or highly similar meanings. For instance, to refer to the 32 same crisp red-skinned fruit, an English-French bilingual child must use the word "apple" 33 when speaking English, and the word "pomme" when speaking French. These 34 cross-language synonyms are known as translation equivalents (also called doublets; Umbel 35 et al., 1992), and are observed amongst bilingual children's first words (e.g., David & Wei, 2008; De Houwer et al., 2006; Pearson et al., 1995). Translation equivalents are thought to hold a special status in a bilingual's developing lexicon due to the strong overlap in their semantics. For example, studies with bilingual toddlers show that the associative semantic properties of a word in one language facilitate the activation of its translation equivalent (e.g., Bilson et al., 2015; Floccia et al., 2020; Jardak & Byers-Heinlein, 2019). That is, upon hearing the English word "apple," the corresponding French word "pomme" is more 42 easily activated in bilinguals' minds. In vocabulary acquisition, bilingual children must 43 learn a first label for a referent (a "singlet"; Umbel et al., 1992) before they can learn its translation equivalent (i.e., a second label for a referent, in a different language, learned 45 following a singlet)¹. Is translation equivalent learning different from singlet learning? The current paper contrasts three competing accounts: 1) translation equivalents are harder to ¹ We note that in some cases a singlet may not have a close translation equivalent, for example the recently popular Danish word "hygge", which refers to a type of cozy contentment and enjoyment of simplicity. Moreover, even when a word that could be considered a translation equivalent exists, adults' concepts may not be congruent across languages (e.g., Malt & Majid, 2013). However, in early development, vocabulary words tend to be concrete, and evidence suggests that concepts are largely shared across languages (Storms

et al., 2015; White et al., 2020). Thus, we make the assumption that most early words have a translation

equivalent and that these are fairly congruent for the age range of focus in the current paper.

- learn than singlets (Avoidance Account), 2) translation equivalents are easier to learn than
- singlets (Preference Account), and 3) translation equivalents and singlets are learned
- 50 similarly (Neutral Account). To adjudicate between these accounts, we introduce the
- 51 Bilingual Vocabulary Model, which provides a computational account of vocabulary
- bilinguals' vocabulary in each language and their
- developmental level. In Study 1, we use the Bilingual Vocabulary Model to derive a set of
- predictions, which we then test against vocabulary data from 200 18- to 33-month-old
- ⁵⁵ bilingual children in Study 2.

$_{56}$ 1.1 Accounts of translation equivalent learning

- 57 1.1.1 Avoidance Account: Translation equivalents are harder to learn than
- singlets. Early theories of bilingual development claimed that translation equivalents are
- conspicuously missing from bilingual children's early vocabularies (e.g., Imedadze, 1967;
- 60 Swain & Wesche, 1975; Volterra & Taeschner, 1978). The phenomenon of missing
- 61 translation equivalents led theorists to propose that young bilingual children do not
- differentiate their languages, and thus tend to learn only a single word for each referent.
- This avoidance of translation equivalents particularly for nouns was thought to be
- due to word learning biases such as mutual exclusivity, whereby children assume that a
- referent is only associated with one word at the basic level (Markman, 1992, 1994;
- 66 Markman & Wachtel, 1988). For example, when monolingual children see a familiar object
- (e.g., a cup) next to a novel object (e.g., a garlic press) and hear a novel word like "wug,"
- they assume that "wug" refers to the garlic press the object unknown to them rather
- than to the cup, the object for which they already know the word.
- Although mutual exclusivity is helpful for monolingual vocabulary acquisition, its use
- ₇₁ is more complex for bilingual vocabulary acquisition (Byers-Heinlein & Werker, 2009;
- Davidson & Tell, 2005; Houston-Price et al., 2010). When encountering a potential singlet,
- mutual exclusivity would be equally useful for bilinguals as it is for monolinguals,

supporting them in associating an unlabeled referent with a novel word. However, a strong form of mutual exclusivity might prevent bilinguals from associating a translation equivalent with its referent, given that in this case the referent is already associated with another word (albeit in the other language). Thus, mutual exclusivity could prevent bilinguals from acquiring translation equivalents, leading to an abundance of singlets in their vocabularies.

Contrary to earlier studies, more recent work has indicated that bilinguals do
understand and produce translation equivalents from early in development (David & Wei,
2008; De Houwer et al., 2006; Holowka et al., 2002; Legacy et al., 2017; Pearson et al.,
1995). Indeed, experimental work has suggested bilingual experience in infancy might not
support the development of one-to-one mapping biases such as mutual exclusivity, at least
in early infancy. For example, when hearing a novel word like "nil," monolingual children
aged 17–22 months looked towards a novel object rather than a familiar object, but bi- and
multilingual children looked similarly to both objects (Byers-Heinlein & Werker, 2009;
2013; Houston-Price et al., 2010). A recent meta-analysis also indicated that bilingual
children show mutual exclusivity to a weaker degree than monolinguals (Lewis et al., 2020).

Overall, converging evidence refutes the position that a strong form of mutual exclusivity prevents bilinguals from acquiring translation equivalents. Nonetheless, it leaves open the possibility that translation equivalents may be less likely acquired in favour of learning singlets even if translation equivalents are not completely avoided. If bilingual children avoid lexical overlap across languages even to a small degree, then under the Avoidance Account translation equivalents would be harder to learn than singlets.

1.1.2 Preference Account: Translation equivalents are easier to learn than
singlets. Contrary to the Avoidance Account, the Preference Account posits that
translation equivalents are easier to learn than singlets. At a minimum, word learning
requires encoding and representing the relevant sounds of a word, creating a mental
representation of its referent, and linking the two. When a French-English bilingual child

encounters the word "pomme" after having learned "apple," one part of that process has 101 already occurred in that the referent is already represented; because part of the word 102 learning task is already accomplished, translation equivalents might therefore be easier to 103 learn than singlets (e.g., Montanari, 2010; Poulin-Dubois et al., 2013; 2018). Moreover, 104 research suggests that bilingual lexicons are not tightly encapsulated by language, but 105 instead include cross-language mental links between words that are semantically related 106 (e.g., Floccia et al., 2020; Jardak & Byers-Heinlein, 2019; Singh, 2014). In this context, the 107 strong semantic overlap makes translation equivalents special, and could facilitate their 108 acquisition (e.g., Bilson et al., 2015; Floccia et al., 2020). The Preference Account predicts 109 that translation equivalents are more easily learned than singlets. 110

There are several lines of empirical evidence to support the Preference Account. For
example, some early case studies reported that bilinguals tended to learn more translation
equivalents than singlets when experiencing a shift in their language exposure that inverted
their dominant and non-dominant languages (Lanvers, 1999; Pearson & Fernández, 1994).
The main explanation that has been given for this finding is that additional exposure to
their non-dominant language — which became their new dominant language — enabled
fast mapping of words to already-lexicalized concepts.

Other evidence suggesting translation equivalents might be easier to learn than 118 singlets comes from a study that included vocabulary-checklist data from 254 monolingual 119 and 181 bilingual children aged 6 months to 7.5 years (Bilson et al., 2015). The researchers 120 used a network analysis approach to investigate how translation equivalents are learned, 121 focusing on the semantic relationships between the words (e.g., words like "cat" and "dog" 122 are strongly semantically related). Using a statistical model that allowed free semantic 123 relations among vocabulary data from monolingual and bilingual children, the results 124 suggested that words were learned faster when they were semantically connected to more 125 known words in children's lexicons. This effect applied not only to words within the same 126 language, but also to words across languages including translation equivalents (e.g., English

"dog" and French "chien") and words that had other cross-language relations (e.g., "cat" and "chien"). The authors then simulated bilingual vocabularies by modeling bilingual 120 lexicons as combinations of two independent vocabulary-size-matched monolinguals. 130 Comparison with actual bilingual children's vocabulary data revealed that bilingual 131 children acquired more translation equivalents than predicted by the simulation. The 132 authors therefore concluded that bilingual children learn translation equivalents more 133 easily than singlets. Note that, in their study, expected translation equivalent knowledge 134 was simulated based on the number of lexical items that overlapped between two randomly 135 chosen English monolinguals (e.g., whether both monolinguals knew the word "cat"). 136 However, it is unclear whether this is an appropriate point of comparison for bilingual 137 children as this approach may overlook variables that impact bilinguals' vocabulary 138 learning, including vocabulary size in each language and the developmental level of a child — a point that we will return to later in the introduction.

Overall, there is some evidence that bilingual children more readily learn translation equivalents than singlets. If the strong semantic overlap between translation equivalents facilitates their learning, then under the Preference Account translation equivalents will be more easily learned than singlets.

1.1.3 Neutral Account: Translation equivalents and singlets are learned 145 The previous accounts rely on the idea that bilingual vocabulary development 146 unfolds differently than monolingual development, as monolinguals encounter only singlets 147 but bilinguals encounter both singlets and translation equivalents. There is an underlying 148 assumption that translation equivalent learning is somehow special relative to singlet learning — the Avoidance Account proposes that translation equivalents are harder to learn than singlets, whereas the Preference Account proposes that translation equivalents 151 are easier to learn than singlets. However, it is also possible that translation equivalents 152 are neither harder nor easier for bilingual children to learn than singlets. We call this the 153 Neutral Account.

The Neutral Account implies that bilingual children's two languages develop 155 relatively independently. Indeed, language and processing measures for bilingual children 156 tend to be tightly correlated within a particular language, and weakly if at all correlated 157 across languages. For example, 30-month-old bilingual children's processing efficiency in a 158 particular language closely correlated with vocabulary size in that language, but was 159 unrelated to vocabulary size in their other language (Marchman et al., 2010). Due to 160 differences in the amount of language exposure, bilingual children seldom show equal 161 vocabulary growth in both of their languages (e.g., Pearson & Fernandez, 1994; Pearson et 162 al., 1997), and the amount of exposure to a particular language has been reported to 163 modulate the within-language association between language processing ability and 164 vocabulary size (Hurtado et al., 2014). Bilingual children with greater exposure to a 165 particular language tend to process that language faster, and in turn learn more words in that language.

In a study whose results support the Neutral Account, Pearson and colleagues (1995) 168 randomly paired the single-language English lexicons from a subset of bilingual children to 169 the single-language Spanish lexicons from another subset of bilingual children to derive a 170 percentage of by-chance lexical overlaps shared between monolingual lexicons of two 171 randomly paired children. The researchers found that the percentage of translation 172 equivalents observed in English-Spanish bilingual children was similar to the by-chance percentage of translation equivalents between randomly-paired children. This evidence implied that singlets and translation equivalents are equally learnable, although the paper 175 was limited by its somewhat small sample (n = 27) in the context of a wide age range (8) 176 months to 2.5 years). In sum, the Neutral Account predicts that, for bilingual infants, 177 learning translation equivalents is similar to learning singlets.

1.2 Contributors to translation equivalent knowledge

The previous section discussed three theoretical accounts concerning the relative
learnability of translation equivalents. However, to date, aspects of translation equivalent
learning have mostly been examined in isolation, rather than integrated within the larger
context of bilingual lexical development. In this section, we consider two proximal variables
that we expect to predict the number of translation equivalents bilingual children know:
vocabulary size in each language, and word learnability as a function of children's
developmental level.

1.1.1 Vocabulary size in bilinguals' two languages. Balance between the two 187 vocabulary sizes is a function of the number of words bilingual children produce in each 188 language, which tends to be tightly linked to their exposure to each language. In general, 189 more language exposure leads to a larger vocabulary size (e.g., Barnes & Garcia, 2013; 190 Boyce et al., 2013; Hurtado et al., 2014; Marchman et al., 2010; Pearson et al., 1997; Place 191 & Hoff, 2011). Bilingual children usually know more words in the language to which they 192 have greater exposure (i.e; dominant language) relative to the language to which they have 193 less exposure (i.e., non-dominant language; Pearson et al., 1997; Place & Hoff, 2011). This 194 is because the more often a bilingual hears a language, the more opportunities there will be 195 for learning new words in that language. 196

Because translation equivalents are words from different languages that refer to the
same concept, the number of words a bilingual knows in each of their languages will
necessarily constrain the number of translation equivalent pairs they could possibly know.
For example, a child with a less balanced vocabulary across their two languages might only
say 5 words in one language but many more words in the other language; this means that
the child could only produce a maximum of 5 translation equivalents, regardless of how
many words they know in their other language. Conversely, it seems reasonable to expect
that if a child knows a similar number of words in each language and thus has a more

balanced vocabulary across the two languages, there would be more potential for some of
those words to be translation equivalents.

1.1.2 Word learnability as a function of developmental level. An often 207 overlooked factor that could contribute to bilingual children's learning of translation 208 equivalents is related to the changes in the learnability of different words over time based 209 on children's developmental level. Evidence from monolingual children shows that some 210 types of words are characteristically learned before others. For example, across many 211 languages including English, children show a noun bias in their early lexicons (Braginsky et 212 al., 2019; Goodman et al., 2008), although for other languages such as Mandarin it appears 213 that verbs and nouns are more equally acquired (Tardif, 1996). Certain classes of words are 214 rarely known at the onset of lexical development, such as prepositions and words for time 215 (Fenson et al., 2007). This is thought to be due to the cognitive and linguistic machinery 216 that must be in place in order for children to represent these concepts, a necessary 217 prerequisite for learning certain word types (Bergelson, 2020; Braginsky et al., 2019). If 218 this is the case, then children might be more likely to learn translation equivalents than 219 singlets, simply because translation equivalents are more likely to be learnable at their 220 stage of development. That is, many potential singlets could be "too hard" to learn at a 221 particular age, while by definition potential translational equivalents refer to concepts that 222 children are already able to lexicalize. For example, an 14-month-old who has learned the French words "ballon" and "chien" would be capable of learning their translation equivalents "ball" and "dog," as well as easier potential singlets like "cup," but not later-acquired potential singlets like "vitamins," "tomorrow," "who," or "not." Thus, a 226 seeming overabundance of translation equivalents might be a product of developmental 227 constraints on word learning, rather than due to semantic facilitation. 228

9 1.3 The Bilingual Vocabulary Model

Taking into account the contributions of language exposure and developmental level 230 to bilingual children's vocabulary acquisition, we put forward the Bilingual Vocabulary 231 Model. This model proposes that the number of translation equivalents that bilingual 232 children produce is a function of vocabulary learning in each language, in the context of 233 the number of potentially learnable words given the children's developmental level. We 234 formalize learning a translation equivalent pair as the joint probability of learning each of 235 the words in the pair. This provides a straightforward empirical test of different theoretical 236 accounts of translation equivalent learning, by asking whether or not the probability of 237 knowing a word is independent of knowing its translation equivalent. The logic is similar to 238 that of the familiar chi-squared test for independence, where the independence of two 239 events from the same population is tested as the probability of their intersection computed 240 by multiplying the probability of each individual event: $P(A \text{ and } B) = P(A) \times P(B)$ if A 241 and B are independent². In the next paragraphs, we define each of the model parameters in

² To test the independence of two events from the same population, as an example, we might ask whether psychology majors are more likely to be left-handed. Imagine a college of 1000 students. If 100/1000 (or 1/10) students are left-handed, and 200/1000 (or 1/5) students are psychology majors, then if these variables are independent we expect a proportion of $1/10 \times 1/5 = 1/50$ students to be left-handed psychology majors. To determine the number we expect to observe in the college, we multiply $1/50 \times 1000 = 20$ students. When we compare this expected number to the actual number of left-handed students, there are three possible outcomes. First, we may observe many more than 20 left-handed psychology students at the college (say 100 students), which suggests that being left-handed increases the probability of majoring in psychology. Or, second, we may observe many fewer than 20 left-handed psychology students at the college (say 5 students), which suggests that being left-handed decreases the probability of majoring in psychology (in this example by a factor of 1/4). Finally, if left-handedness and majoring in psychology are independent, we can predict the number of left-handed psychology students by multiplying the observed number of left-handed students (100) by the observed number of psychology students (200), and dividing by the total population of the college (1000), so for example $100 \times 200/1000 = 20$. Thus, comparing expected and observed numbers can inform us about the independence of the underlying phenomena.

detail, and these are also summarized in Table 1.

The model takes four main parameters as predictors: the number of words produced 244 in the dominant language (DOM), the number of words produced in the non-dominant 245 language (NONDOM), vocabulary size of potentially learnable words in each language 246 (LEARNABLE), and a bias parameter (BIAS) which indicates whether the model is biased towards (BIAS > 1) or against (BIAS < 1) learning translation equivalents. The language in which a child knows more words is the dominant language, whereas the one in which a child knows fewer words is the non-dominant language. Next, we turn to the LEARNABLE parameter (i.e., the number of potentially learnable words). If DOM and NONDOM are 251 measured with an instrument such as the MacArthur-Bates Communicative Development 252 Inventories (CDI; Fenson et al., 2007), one option would be to set LEARNABLE to be the 253 total number of items on the CDI, which is typically 600-700 depending on the language of 254 the adaptation. Yet, not all children will be capable of learning all of the CDI words. 255 Typically, words that are more concrete occur more frequently in the input, and words that 256 are associated with babies tend to be acquired earlier than other words (Braginsky et al., 257 2019). That is, very young children would not be expected to produce many of the 258 advanced words on the CDI, such as "lawn mower," "sidewalk," or "vitamins." Thus, a 250 reasonable solution might be to determine how many CDI words are potentially learnable 260 given the child's developmental level, which could be approximated by their age. Since 261 there are no CDI norms for French-English bilingual children, we will take the average 262 English and French CDI norms to approximate how many words children might lexicalize 263 in either language. For example, imagine that Jamie who is 18 months old produces 50 English words and 20 French words, thus a total of 70 words. Monolingual children his age with the very largest productive vocabularies (those at the 90th percentile averaging between English and French norms) produce a total of 240 words (retrieved from the 267 Wordbank database version 0.3.1; Frank et al., 2016). Although there is likely considerable 268 individual variability as to the cognitive capacity even amongst children of the same age, we

argue that averaging between the English and French CDIs at the 90th percentile provides 270 a reasonable — if imperfect — estimate of the number of learnable words (LEARNABLE) 271 that a bilingual child of Jamie's age could potentially acquire in each language. Thus, we 272 might expect that Jamie could potentially have learned up to 240 words in English and 240 273 words in French, although he has thus far only learned 50 in English and 20 in French. 274 Note that we model learnability in terms of the number of words expected to be learnable 275 at a particular age, rather than modeling the learnability of individual words at a 276 particular age — a simplifying choice that we will return to in the discussion section. 277

Using the mathematical concept of independence, we can then quantify the number 278 of translation equivalents (TE) expected given children's vocabulary sizes in the dominant 279 (DOM) and non-dominant (NONDOM) languages, as well as the number of potentially 280 learnable words (LEARNABLE). If dominant-language and non-dominant-language words 281 are learned independently from each other, we multiply DOM × NONDOM (the number of 282 words known in the dominant and non-dominant language respectively), and divide by the 283 total number of learnable words in one language (LEARNABLE) — which is the possible 284 number of words that could overlap across both languages — to predict the number of 285 translation equivalents. We further introduce the bias parameter (BIAS), which allows us 286 to examine whether translation equivalent learning is best described by the Avoidance, 287 Preference, or Neutral Account. Adding this parameter, translation equivalents can be 288 derived from $TE = BIAS \times (DOM \times NONDOM)/LEARNABLE$. For the Avoidance 280 Account, BIAS will be less than 1, meaning that translation equivalents are less easily 290 learned than singlets; for the Preference Account, BIAS will be greater than 1, meaning that translation equivalents are more easily learned than singlets; for the Neutral Account, BIAS is exactly 1 (i.e., the model is unbiased with respect to whether translation equivalents are more difficult or easier to acquire than singlets). Going back to the example of 18-month-old Jamie, we would set the denominator at 240 which is the number of 295 potentially learnable words at 18 months. If translation equivalents are half as easy to 296

- learn as singlets (following the Avoidance Account), we would expect Jamie to produce $.5 \times (50 \times 20/240) = 2.1$ translation equivalents. Conversely, if translation equivalents are twice as easy to learn as singlets (following the Preference Account), we would expect Jamie to produce $2 \times (50 \times 20/240) = 8.3$ translation equivalents. Under the Neutral
- Account, we would expect Jamie to produce $1 \times (50 \times 20/240) = 4.2$ translation equivalents.

Table 1. Summary of the parameters in the Bilingual Vocabulary Model.

Variable	Definition	Constraints	Relationship.to.other.parameters
Main Parameters			
LEARNABLE	Number of words expected to be learnable in each	Varies by age. No greater than the number of	Maximum number that could be learned in DOM
	language, given the child's developmental level	words on CDI.	or NONDOM
DOM	Words produced in the dominant language	$\mathrm{DOM} \geq \mathrm{NONDOM}$ (children always produce	$DOM = (1 - BALANCE) \times WORD; DOM =$
		more words in dominant than non-dominant	WORD – NONDOM
		language); DOM \leq LEARNABLE	
NONDOM	Words produced in the non-dominant language	NONDOM \leq DOM (children always produce	$NONDOM = BALANCE \times WORD; NONDOM =$
		fewer words in non-dominant than dominant	WORD – DOM
		language); NONDOM \leq LEARNABLE	
BIAS	Bias parameter	BIAS < 1 implies the Avoidance Account; $BIAS$	
		> 1 implies the Preference Account; BIAS = 1	
		implies the Neutral Account	
Derived Parameters			
BALANCE	Balance (relative proportion of words produced in	$0 \leq \mathrm{BALANCE} \leq .50$ (greater values indicate	BALANCE = NONDOM/WORD; BALANCE =
	the non-dominant language to the total words	children producing a more similar number of	NONDOM/(DOM+NONDOM)
	produced in both languages)	words in their two languages)	
WORD	Word vocabulary (or total vocabulary size)	W $\leq 2 \times \text{LEARNABLE}$ (maximum word	WORD = DOM+NONDOM; WORD = DOM/(1
		vocabulary is knowing each word in both	- BALANCE); WORD =
		languages)	NONDOM/(BALANCE)
TE	Translation equivalents produced		$TE = BIAS \times DOM \times NONDOM/LEARNABLE$
CONCEPT	Concept vocabulary (or total conceptual		CONCEPT = WORD - TE; CONCEPT = TE +
	vocabulary size)		DOM-SINGLET + NONDOM-SINGLET
DOM-SINGLET	Singlets in dominant language		DOM-SINGLET = $DOM - TE$
NONDOM-SINGLET	Singlets in non-dominant language		NONDOM-SINGLET = NONCOM - TE
Note: All vocabulary	All vocabulary measures are constrained to be integers.		

Finally, based on the four main predictive parameters, we can calculate additional,
commonly-reported descriptors of bilingual vocabulary, which we detail below and describe
as derived parameters (see also Table 1).

Balance of vocabulary (BALANCE) is the proportion of total words that children produce in each language. For convenience, balance is defined in reference to the non-dominant language with the formula NONDOM/(DOM+NONDOM), such that scores can range from 0.0 (completely unbalanced) to 0.5 (completely balanced). For example, since 18-month-old Jamie produces 50 dominant vocabulary words and 20 non-dominant vocabulary words, he would have a balance score of 0.29. Note that this calculation does not take into account overlap in meaning across the two languages (i.e., how many of the words he produces are translation equivalents).

Word vocabulary (WORD; sometimes called total vocabulary) is the total number of 313 words that a child produces across the two languages, calculated as the sum of the 314 dominant vocabulary (DOM) and non-dominant vocabulary (NONDOM). Concept 315 vocabulary (CONCEPT; sometimes called total conceptual vocabulary) is the number of 316 concepts that are lexicalized by the child — that is, the total number of concepts that are 317 lexicalized in either language. This can be calculated by subtracting the number of 318 translation equivalents (TE) from the word vocabulary (WORD). Finally, we can also 319 calculate singlets that are produced in each language, that is words for which the child 320 does not yet produce a translation equivalent. Singlets in the dominant language 321 (DOM-SINGLET) can be calculated by subtracting translation equivalents (TE) from dominant-language vocabulary (DOM); singlets in the non-dominant language 323 (NONDOM-SINGLET) can be calculated by subtracting translation equivalents (TE) from non-dominant language vocabulary (NONDOM). It is also possible to decompose children's 325 word vocabulary (WORD) into the sum of TE, DOM-SINGLET, and 326 NONDOM-SINGLET.

Finally, we note two simplifying assumptions made by our model. First, we assume 328 that children have the same communicative need in each language: our model does not 329 account for cases where bilinguals might systematically refer to a concept in only one 330 language and not the other (e.g., Grosjean, 2016). Second, we assume that translation 331 equivalents refer to the same underlying concept. Thus, our model does not consider the 332 nuanced and language-specific conceptual representations that bilingual adults might 333 ultimately develop (Malt & Majid, 2013; Storms et al., 2015; White et al., 2020). However, 334 we believe that these assumptions present a reasonable first approximation, especially in 335 the case of young children, and return to these assumptions in the discussion section. 336

1.4 Current studies

The current studies aimed to better understand the nature of translation equivalent learning in bilingual children. Study 1 simulated the expected patterns of translation equivalent learning under the Bilingual Vocabulary Model proposed in the introduction, with reference to the proportion of words learned in the dominant and non-dominant language and the number of words that are learnable at various developmental levels. We also compared predicted learning outcomes for when translation equivalent learning is harder than, easier than, or similar to singlet learning.

In Study 2, we examined real-world translation equivalent development in light of the predictions from the Bilingual Vocabulary Model, using archival data from 200
French-English bilingual children aged 18 to 33 months, whose vocabularies and translation equivalent knowledge were measured by parent report using the MacArthur-Bates CDI: Words and Sentences form in English (Fenson et al., 2007) and Québec French (Trudeau et al., 1999). Together, the Bilingual Vocabulary Model and real-world data allowed us to examine contrasting hypotheses about translation equivalents: whether translation equivalent learning is harder than (Avoidance Account), easier than (Preference Account), or similar to (Neutral Account) learning singlets.

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2 Study 1: Simulations

Study 1 provides a computational implementation of the Bilingual Vocabulary Model outlined in the introduction, which we use to simulate different scenarios to examine the effect of vocabulary sizes and developmental variables on translation equivalent learning. Simulations were conducted by holding constant or varying the main parameters across a set of possible values, and computing expected translation equivalents and derived parameters from these values. The number of children in each simulation was fully determined by the number of levels varied for each parameter: each combination of parameters was included, except those that violated constraints in the model (e.g., NONDOM could not be larger than DOM).

For each simulation, we generated predictions for expected patterns in bilingual 364 children's vocabularies. Several previous studies in the literature have examined relations 365 between translation equivalent knowledge and our main parameters including age or 366 developmental level (which determines LEARNABLE; David & Wei, 2008; Legacy et al., 367 2016), DOM (Legacy et al., 2016; Poulin-Dubois et al., 2013), and NON-DOM (Legacy et 368 al., 2016). However, others have examined derived parameters such as BALANCE (David 369 & Wei, 2008; Legacy et al., 2016; Montanari, 2010; Pearson et al., 1995; 1997), WORD 370 (Legacy et al., 2016; Montanari, 2010), CONCEPT (Pearson et al., 1993), DOM-SINGLET 371 and NONDOM-SINGLET (De Houwer et al., 2006; Pearson et al., 1993; 1995). To 372 facilitate comparison with the extant literature where main parameters are not always 373 reported, we generated predictions expressed both in terms of main parameters and derived parameters. This provides alternate ways of testing the model, depending on which 375 parameters are available in the dataset. Note that predictions from the main parameters 376 and those from derived parameters do not provide independent tests of our model for the 377 same dataset, as they can be algebraically calculated from one another. As an analogy, a 378 child's age is not independent from their birth date and today's date, yet we might make 379

reference to their age in some situations and their birth date in others. Similarly,
elucidating relations among both main and derived parameters provides a more complete
description of expected patterns in bilingual vocabulary development.

In the first simulation, we examined relations between translation equivalents (TE). 383 dominant-language vocabulary (DOM), non-dominant language vocabulary (NONDOM), 384 word vocabulary (WORD), and vocabulary balance (BALANCE), while keeping the 385 number of learnable words (LEARNABLE) constant. In the second simulation, we varied the number of learnable words (LEARNABLE), and examined expected number of 387 translation equivalents (TE), singlets in each language (DOM-SINGLET and 388 NONDOM-SINGLET), and concept vocabulary (CONCEPT). In both of the first two simulations, the BIAS parameter was held constant at 1 (Neutral Account); in the third 390 simulation, we varied the BIAS parameter to examine expected patterns of translation 391 equivalent (TE) learning as a function of word vocabulary (WORD) under the Avoidance, 392 Preference, and Neutral Accounts. A summary of the parameter values used in each 393 simulation is provided in Table 2. 394

Table 2. Summary of the parameters used in each simulation.

Simulation	Learnable	Words in dominant	Words in	Word vocabulary	Balance of	Bias parameter	Number of
	words	Language (DOM)	non-dominant	(WORD)	vocabulary	(BIAS)	simulated
	(LEARN-		language		(BALANCE)		children
	ABLE)		(NONDOM)				
П	Constant at	Varied, ranging	Varied, ranging	Calculated as	Calculated as	Constant at 1	216
	009	from 100 to	from 0 to DOM at	WORD = DOM +	BALANCE =		
		LEARNABLE at	an interval of 10	NONDOM	/ MONDON		
		an interval of 100			(DOM+NONDOM)		
73	Varied at	Varied, ranging	Varied, ranging	Calculated as	Calculated as	Constant at 1	301
	100, 200,	from 100 to	from 0 to DOM at	WORD = DOM +	BALANCE =		
	300, 400,	${\tt LEARNABLE\ at}$	an interval of 20	NONDOM	NONDOM /		
	500, 600	an interval of 100			(DOM+NONDOM)		
89	Varied at	Varied, ranging	Varied, ranging	Calculated as	Calculated as	Varied at 0.5	166
	150, 300,	from 100 to	from 0 to DOM at	WORD = DOM +	BALANCE =	(Avoidance	
	450, and	LEARNABLE at	an interval of 25	NONDOM	/ MOUNDON	Account), 1	
	009	an interval of 100			(DOM+NONDOM)	(Neutral Account),	
						and 1.5 (Preference	
						Account)	

The number of children simulated is derived from the total number of allowed combinations of the parameters (i.e., excluding combinations that violate parameter constraints; for example NONDOM could not be larger than DOM). Note:

2.1 Simulation 1: Children of the same developmental level with different word vocabularies and balances of vocabulary

In Simulation 1, we examined patterns of translation equivalent learning where 397 simulated children are at the same developmental level and thus have the same number of 398 potentially LEARNABLE words, but their vocabulary size in each language (DOM and 399 NONDOM) varied. For readers less familiar with this type of approach, we provide 400 expanded examples of three simulated infants in the Appendix. For convenience, we set 401 LEARNABLE constant at 600, which roughly corresponds to what is expected for an 402 English-French 27-month-old bilingual child. For example, a 27-month-old English-learner 403 at the 90th percentile of vocabulary produces around 633 words and a 27-month-old French-learner produces around 580 words as retrieved from the Wordbank database, giving us an average of 606 words across the two languages (Frank et al., 2016). BIAS was set constant at 1, meaning that in these simulations translation equivalents and singlets are 407 equally easy to learn. Data from a total of 216 simulated children were generated (see Table 408 2 for a summary of the parameter values used in this simulation). Based on these values, 409 we derived simulated children's word vocabulary (WORD, calculated as DOM+NONDOM) 410 and their vocabulary balance (BALANCE, calculated as NONDOM/(DOM+NONDOM)). 411 In Figure 1, we plotted TE knowledge as a function of WORD, DOM, and NONDOM 412 at different levels of BALANCE. Across all three Panels (1A, 1B, and 1C), simulated 413 children with the most balanced vocabulary consistently produced more translation 414 equivalents than other children. Moreover, Panels 1A and 1B show that, as WORD (word 415 vocabulary) and DOM (dominant language words) increased, TE (translation equivalents) 416 also increased regardless of BALANCE. Interestingly, Panel 1C shows that NONDOM and 417 TE were extremely tightly coupled. In sum, we observed three important patterns, which served as Prediction Set 1 from the Bilingual Vocabulary Model for Study 2:

• Prediction 1a: Children with more balanced vocabularies (BALANCE) will produce

420

- more translation equivalents (TE) (Figure 1, Panel 1A).
- Prediction 1b: Children who produce more total words (WORD) or more
 dominant-language words (DOM) will produce more translation equivalents (TE)

 (Figure 1, Panels 1A and 1B).
- Prediction 1c: Children who produce more non-dominant language words

 (NONDOM) will produce more translation equivalents (TE). Unlike for WORD and

 DOM, this will not interact with BALANCE; instead, non-dominant vocabulary size

 will be an almost perfect predictor of translation equivalent knowledge (Figure 1,

 Panel 1C).

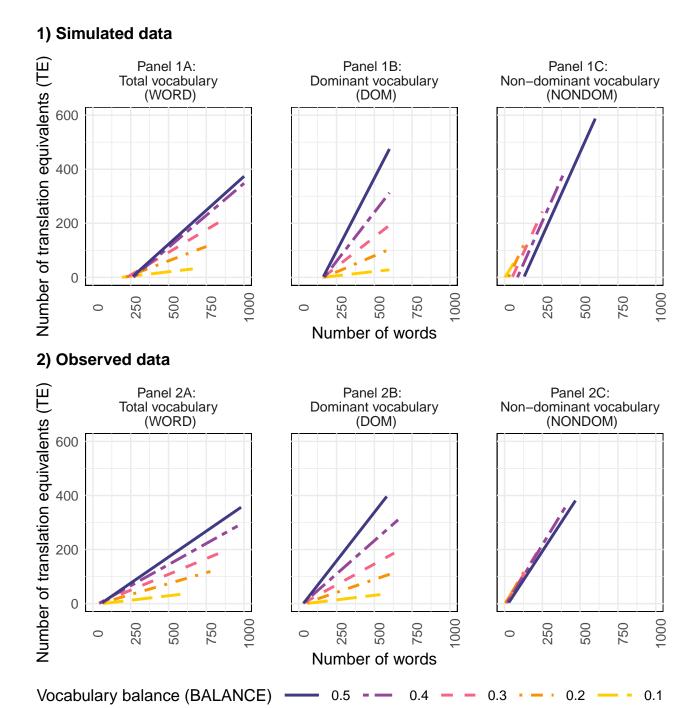


Figure 1. Number of translation equivalents (TE) across different levels of vocabulary balance (BALANCE) in relation to word vocabulary (WORD; Panel A), dominant vocabulary size (DOM; Panel B), and non-dominant vocabulary size (NONDOM; Panel C). Row 1 plots the simulated data in Study 1 while holding the number of learnable words (LEARNABLE) constant at 600 and BIAS constant at 1. Row 2 plots the observed vocabulary data in Study

2.2 Simulation 2: Acquisition of translation equivalents and singlets at different developmental levels

In our previous simulation, we assumed that each simulated child was at the same
developmental level and had the capacity to learn up to 600 words in each language (i.e.,
LEARNABLE was held constant at 600). As laid out in the introduction, under the
Bilingual Vocabulary Model, the learnability of different words changes with a child's
developmental level, where LEARNABLE increases as a child grows older. Therefore, in
Simulation 2, we looked at the expected patterns of translation equivalent learning across
varying levels of LEARNABLE (i.e., the number of learnable words in each language as
developmental level changes). Additionally, we further examined vocabulary composition
by computing the number of singlets in the dominant (DOM-SINGLET) and non-dominant
(NONDOM-SINGLET) language. BIAS was once again kept constant at 1.

Translation equivalent knowledge was simulated across children at six developmental 442 levels (number of LEARNABLE words = 100, 200, 300, 400, 500, 600), in conjunction with 443 a wide range of values for words in the dominant language (DOM) and the non-dominant 444 language (NONDOM). In total, data from 301 simulated children were generated (see 445 Table 2 for a summary of the parameters used in this simulation). Again, balance (BALANCE) was calculated based on the values of DOM and NONDOM. We also 447 calculated the number of singlet words in the dominant (DOM-SINGLET) and 448 non-dominant (NONDOM-SINGLET) languages by the formula DOM-SINGLET = DOM 449 - TE and NONDOM-SINGLET = NONDOM - TE. Figure 2 plots the number of CONCEPT, TE, DOM-SINGLET, and NONDOM-SINGLET at different BALANCE 451 levels across different levels of LEARNABLE. Overall, we generated 4 additional predictions (Prediction Set 2) made by the Bilingual Vocabulary Model. Compared to 453 children at an earlier developmental level (i.e., younger infants with fewer potentially 454 learnable words), children at a later developmental level (i.e., older infants with more

456 potentially learnable words) will:

- Prediction 2a: Have larger concept vocabularies (CONCEPT) (Figure 2, Panel 1A).
- Prediction 2b: Produce more translation equivalents (TE), regardless of vocabulary balance (BALANCE) (Figure 2, Panel 1B).
- Prediction 2c: Produce more dominant-language singlet words (DOM-SINGLET).

 Moreover, those with the least balanced vocabulary (BALANCE) will produce the

 most DOM-SINGLET (Figure 2, Panel 1C).
- Prediction 2d: Produce more non-dominant-language singlets

 (NONDOM-SINGLET). Moreover, those with the most balanced vocabulary

 (BALANCE) will produce the most NONDOM-SINGLET (Figure 2, Panel 1D).

1) Simulated data

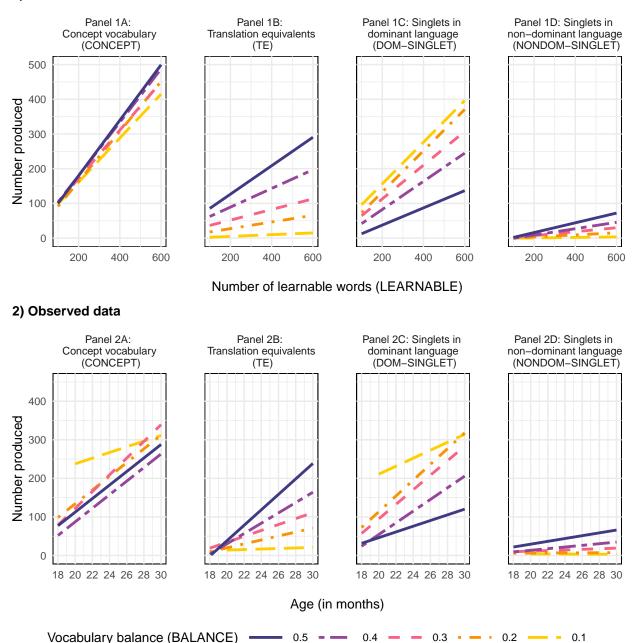


Figure 2. Number of concept vocabulary (CONCEPT; Panel A), translation equivalents (TE; Panel B), singlets in dominant (DOM-SINGLET; Panel C) and singlets in the non-dominant language (NONDOM-SINGLET; Panel D) across different levels of vocabulary balance (BALANCE) in relation to different developmental levels/ages, which set the number of LEARNABLE words. Row 1 represents the simulated data in Study 1. Row 2 represents the observed vocabulary data in Study 2.

2.3 Simulation 3: Bias towards or against translation equivalent learning

In Simulations 1 and 2, we modeled cases with the bias parameter held constant at 1 467 and translation equivalent (TE) was calculated as DOM×NONDOM/LEARNABLE. Thus, 468 these simulations were in accordance with the Neutral Account where dominant-language 469 and non-dominant language vocabularies were learned independently. In our final 470 simulation, we examined cases where dominant-language and non-dominant language 471 vocabularies were not independent, corresponding to the Avoidance Account and the 472 Preference Account. Mathematically, this requires varying the BIAS parameter. For the 473 Preference Account, BIAS will be greater than 1, meaning that translation equivalents are more easily learned than singlets. By contrast, for the Avoidance Account, BIAS will be less than 1, meaning that translation equivalents are less easily learned than singlets.

Translation equivalent (TE) knowledge was first simulated across different 477 developmental levels (number of LEARNABLE words = 150, 300, 450, 600), in conjunction 478 with a wide range of values for DOM and NONDOM. Again, BALANCE and word 479 vocabulary (WORD) were derived based on the values of DOM and NONDOM. The final 480 simulated data set contained 166 data points (see Table 2 for a summary of the parameters 481 used). Three scenarios of translation equivalent learning (TE) were then generated using 482 the formula $TE = BIAS \times DOM \times NONDOM/LEARNABLE$. To illustrate the Avoidance 483 Account, BIAS was set at .5 (i.e., TEs are 50% less likely to be learned than singlets). To 484 illustrate the Neutral Account, BIAS was set at 1 (i.e., TEs and singlets are equally 485 learnable). Finally, to illustrate the Preference Account, BIAS was set at 1.5 (i.e., TE are 50% more likely to be learned than singlets). In Figure 3, we illustrate the three different 487 scenarios of simulated translation equivalent (TE) knowledge. Again, we observed a pattern consistent with prediction 1a where, in all cases, simulated children with more balanced vocabularies (BALANCE) produced more translation equivalents (TE). Thus, 490 overall relationships between BALANCE and TE remained similar across the Avoidance, 491

Preference, and Neutral Accounts. What changed was the slope of translation equivalent learning: the slopes were the shallowest under the Avoidance Account where BIAS = 0.5, whereas the slopes were steepest under the Preference Account where BIAS = 1.5. With this, we further outline Prediction Set 3:

• Prediction 3: Whether learning translation equivalents is harder than, easier than, or similar to learning singlets, the slope of translation equivalent learning will change as a function of word vocabulary (WORD), with a shallower slope if TEs are less easily learned (i.e., Avoidance Account), and a steeper slope if TEs are more easily learned (i.e., Preference Account) compared to where translation equivalents and singlets are similar to learn (i.e., Neutral Account).

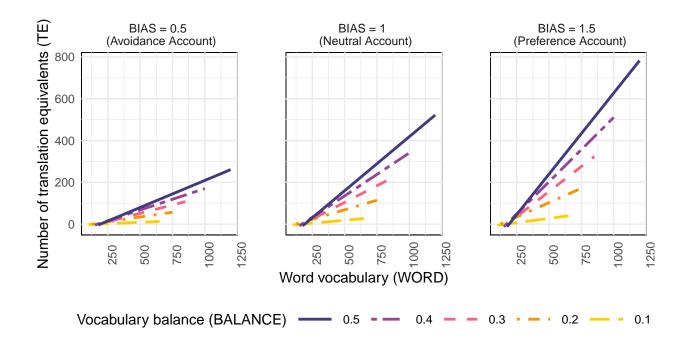


Figure 3. Different scenarios of expected translation equivalent learning (TE) as a function of WORD vocabulary, under scenarios where learning TEs is harder than (BIAS < 1), easier than (BIAS > 1), or similar to (BIAS = 1) learning singlets.

2.4 Summary of model predictions

Study 1 generated predictions under the Bilingual Vocabulary Model with regards to
the effect of vocabulary sizes and developmental variables on translation equivalent
learning. The generated predictions were expressed in terms of the model's four main
predictive parameters as well as a function of derived parameters to illustrate expected
patterns in bilingual children's vocabularies. Assuming that translation equivalents were
learned similarly to singlets (i.e., the Neutral Account), three sets of predictions were made.

Prediction Set 1 illustrated that the more words children produce in total word 509 vocabulary, in their dominant language, or in their non-dominant language, the more 510 translation equivalents they are predicted to produce. Moreover, children with more 511 balanced vocabularies (i.e., producing a similar number of words in each of their languages) 512 are also expected to produce more translation equivalents. Prediction Set 2 described 513 translation equivalent knowledge in relation to the number of learnable words constrained 514 by a child's developmental level. Older children are predicted to have a larger concept 515 vocabulary (i.e., to have lexicalized more concepts), including translation equivalents and 516 singlets in both dominant and non-dominant languages, than younger children. Moreover, 517 the most balanced children are expected to produce more singlets in their non-dominant 518 language than the least balanced children, whereas the least balanced children are expected to produce more singlets in their dominant language than the most balanced children. Finally, Prediction Set 3 quantitatively demonstrated the patterns of translation equivalent learning under the three different accounts: the Avoidance Account, the Preference 522 Account, and the Neutral Account. In Study 2, we used vocabulary data from real 523 bilingual infants to investigate our predictions, thus validating our model.

3 Study 2: Empirical data

In Study 1, we used simulations based on the Bilingual Vocabulary Model to generate several predictions about the relationship between translation equivalent knowledge and other vocabulary variables. In Study 2, we tested these predictions using archival vocabulary data from 200 French–English bilingual children aged 18 to 33 months.

530 **3.1 Method**

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Ethics approval was obtained by the Human Research Ethics Board of Concordia University (Certificate Number 10000439) and informed consent was obtained from the children's parents.

Archival data from 200 bilingual children acquiring English 3.1.1 Participants. 534 and French (age range: 18.40 – 33.50 months; 94 girls and 106 boys) who participated in 535 prior studies at the Concordia Infant Research Lab were included in the present study, 536 drawn from the same set of participants as Gonzalez-Barrero et al. (2020). Data collection 537 was conducted in Montréal, Québec, Canada. Montréal is a multicultural city where both 538 English and French are widely used in society. Some children took part in more than one 530 in-lab study (n = 28); thus, they contributed data at more than one time point. This resulted in a larger number of datapoints relative to the number of unique participants. 541 The total number of data points included in the analyses was 229 (i.e., 229 English and 229 French CDI questionnaires). Participants were recruited through government birth lists, online ads, daycares, and infant-parent group activities (e.g., children's library activities). Inclusion criteria were the following: full term-pregnancy (i.e., > 36 weeks of gestation), normal birth weight (> 2500 grams), and absence of major medical conditions (e.g., meningitis). Only children who had complete data in both CDI forms (i.e., English and French) were retained for analysis. Bilingual children were defined as those exposed at least 548 25% of the time over the course of their lives globally to both English and French and with

less than 10% of exposure to a third language. For children who participated more than 550 once, their language exposure followed such criteria for all visits. Following the approach in 551 Study 1, children's dominant language was deemed to be the language in which the child 552 produced a greater number of words; vocabulary balance was then determined based on the 553 proportion of words produced in the non-dominant language relative to the total words 554 produced across both languages using the same formula as in Study 1: 555 NONDOM/(DOM+NONDOM). Within the 229 data points, 59.80% of children were 556 English-dominant and 40.20% were French-dominant. Children's demographic 557 characteristics including age, maternal education, and language exposure, are presented in 558 Table 3.

560

Table 3. Demographic characteristics of participants (data points = 229).

	Mean	SD	Range
Age in months	24.4	4.7	18.4 - 33.5
Maternal education in years	16.6	2.1	10 - 21
% Global exposure to English	51.7	14.8	25 - 75
% Global exposure to French	47.8	15.0	25 - 75
% Global exposure to Other	0.6	1.8	0 - 10

$_{\scriptscriptstyle 11}$ 3.1.2 Measures

3.1.2.1 MacArthur-Bates Communicative Development Inventories: Words and Sentences (CDI). Bilingual children's expressive vocabulary was measured by the Words and Sentences form of the MacArthur-Bates CDI. Caregivers completed the original

CDI English version (Fenson et al., 2007) and its Québec French adaptation (Trudeau et 565 al., 1999). We asked the caregiver more familiar with each language to complete the 566 respective CDI form. The forms were mainly filled out by mothers (64%), fathers (7%), 567 both parents (4%), other caregivers (< 1%; e.g., grandmother), or else the respondent was 568 not indicated (24%). In some cases different caregivers filled out each form, while in other 560 cases the same caregiver filled out both forms. Our analyses focused on the vocabulary 570 checklist of this questionnaire, which includes different nouns, verbs, adjectives, and other 571 words used by young children. There are 680 words on the English CDI version and 664 on 572 the Québec French version. 573

Translation equivalents (TE) were determined in the same manner as 574 Gonzalez-Barrero et al. (2020) by three proficient bilingual French-English adults who 575 carefully examined each language version of the CDI. Word pairs that made reference to 576 the same concept (e.g., English "apple" and French "pomme") were considered to be 577 translation equivalents. In cases of disagreement, a discussion of the likely uses of the word 578 in question by children (rather than potential adult uses of the word) was conducted and 579 then a decision was made. Words with the same meaning that had similar phonetic 580 realizations (e.g., English "alligator" and French "alligator") were considered translation equivalents. Most of the items on both vocabulary checklists had an equivalent word in the other language, which resulted in a total of 611 translation equivalents. A full list of 583 translation equivalents is available at https://osf.io/2t5kw/. 584

After determining the dominant language of a child based on relative vocabulary size,
we then computed the number of singlets that children knew in their dominant
(DOM-SINGLET) and non-dominant (NONDOM-SINGLET) languages by deducting the
number of translation equivalents produced from the total number of words produced in
each language (i.e., DOM – TE and NONDOM – TE as in Study 1). Concept vocabulary
(CONCEPT) was computed based on the number of concepts for which a child produced a
word, calculated by subtracting the number of translation equivalents from word

vocabulary (i.e., WORD – TE as in Study 1).

3.1.2.2 Language Exposure Questionnaire using the MAPLE approach.

Children's language exposure was measured using the Language Exposure Questionnaire 594 (LEQ; Bosch & Sebastián-Gallés, 2001) and the Multilingual Approach to Parent Language 595 Estimates (MAPLE; Byers-Heinlein et al., 2020). The LEQ is a structured interview that 596 lasts approximately 15 minutes. It includes targeted questions that quantify the child's 597 language exposure from birth until their current age. The LEQ and MAPLE provide a 598 global language exposure estimate based on the number of hours the child is exposed to 590 each language within all contexts (e.g., home, daycare, etc.). Children's average global 600 exposure to each language is described in Table 3. 601

602 3.1.3 Procedure

593

Caregivers were asked to fill out the CDI questionnaires as part of their child's
participation in experimental studies on language and cognitive development. Caregivers
were instructed to check off the words produced by their child using either a CDI paper
questionnaire or the same questionnaire administered on a tablet. Data from paper based
questionnaires were double entered and checked by trained research assistants.

$_{608}$ 3.2 Results

Data analyses were conducted using R (Version 4.0.2, 2020). Analysis scripts and the
data set used in the present study are available at https://osf.io/2t5kw/. We first present
descriptive measures of vocabulary, and then tests of the three sets of predictions generated
in Study 1.

3.2.1 Descriptive measures of vocabulary

```
On average, bilinguals in the sample had a mean word vocabulary size (WORD) of
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   295 \text{ (SD} = 254.60), with a wide range of 6 - 1071 words. As expected by the way language
615
   dominance was defined, children produced more words in their dominant language (DOM;
616
   M = 206.10, SD = 175.60, range = 4 - 657) than in their non-dominant language
617
   (NONDOM; M = 88.90, SD = 98.50, range = 2 - 469), t(228) = 13.89, p < .001, d = 0.92.
         Children produced an average of 67.70 translation equivalents (TE; SD = 85.10,
619
   range = 1 - 409). The remainder of words were singlets, and children produced many more
620
   singlets in their dominant language (DOM-SINGLET; M = 138.40, SD = 124.40, range =
621
   2 - 523) than in their non-dominant language (NONDOM-SINGLET; M = 21.20, SD =
622
   20.10, range = 0 - 94), t(228) = 13.89, p < .001, d = 0.92. On average, children's concept
   vocabulary size was 227.30 words (CONCEPT; SD = 181.30, range = 4 - 695).
         Vocabulary balance (BALANCE) was then determined based on the proportion of
625
   total words produced in the non-dominant language following the formula BALANCE =
626
   NONDOM/WORD as in Study 1. On average, bilingual children in our sample had a
627
   balance score BALANCE of 0.31 (SD = 0.13), ranging from 0.02 to 0.50. Similar
   vocabulary balance was found between the children who were English-dominant and those
   who were French-dominant, t(200.43) = 0.57, p = .566, d = 0.08. The 59.80% of children
630
   who were English-dominant had an average BALANCE of 0.31 (SD = 0.13, range = 0.02-
631
   0.50) whereas the remaining 40.20% who were French-dominant had an average BALANCE
632
   of 0.30 (SD = 0.12, range = 0.05 - 0.50).
633
         Note that in this paper, we defined BALANCE in terms of relative vocabulary in
634
   each language, which numerous studies have found is related to children's relative input in
635
   each language (e.g., David & Wei, 2008; Hurtado et al., 2014; Pearson et al., 1997). We
636
   therefore investigated the relationship between vocabulary balance and the percent of
637
   exposure bilingual children received in their non-dominant language. For most children, the
638
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language in which they produced the most words was also the language that they heard 639 most often (181 children, 79%), although this was not the case for a minority of children 640 (48 children, 21%). The correlation between BALANCE and the percentage of exposure to 641 the non-dominant language was moderate, r(227) = 0.45, p < .001 (see also Figure 4). The 642 imperfect correlation between these two measures could result from measurement error (see 643 Byers-Heinlein et al., 2021, for a discussion of attenuation of correlation due to 644 measurement error in developmental research) or could also be because vocabulary size in 645 each language is determined by factors beyond parent-reported proportion of input in each language, for example the quality of that input (for a discussion of input quality for 647 bilinguals, see Unsworth, 2016). 648

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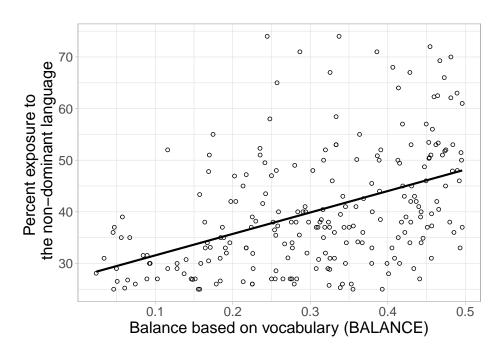


Figure 4. Correlation between balance defined by vocabulary (BALANCE) and balance defined by exposure.

3.2.2 Testing Prediction Set 1: Univariate relationships between translation equivalents and different vocabulary measures

Prediction Set 1 pertained to the pairwise relationships between translation
equivalents (TE), word vocabulary (WORD), dominant (DOM) and non-dominant
vocabulary (NONDOM), and vocabulary balance (BALANCE), which we examined
through Pearson's correlations. Overall, the univariate statistics showed strong
correspondence with the relationships expressed in Prediction Set 1 under the Bilingual
Vocabulary Model (see Table 4 for a full table of pairwise correlations³).

Prediction 1a was that children with more balanced vocabularies would produce more 658 translation equivalents. As shown in Figure 1 Row 2 (Observed data), our vocabulary data 659 confirmed the prediction, r(227) = 0.25, p < .001, where children with the most balanced 660 vocabulary produced the most translation equivalents. Prediction 1b was that children 661 with larger word vocabularies and larger dominant-language vocabularies would produce 662 more translation equivalents, and the results from our dataset confirmed this prediction, 663 for word vocabulary (WORD): r(227) = 0.90, p < .001, and dominant-language vocabulary 664 (DOM): r(227) = 0.76, p < .001. Figure 1 Panels 2A and 2B further illustrate these 665 relationships observed in our dataset. 666

Prediction 1c was that children who produce more words in the non-dominant language (NONDOM) would produce more translation equivalents (TE) — specifically, that this relationship would be nearly perfect. As shown in Figure 1 Panel 2C, we observed

³ Note that there was a negative correlation between BALANCE and age in our sample, such that older children had vocabularies that were less equal across their languages. This is not predicted by our model, and we can only speculate as to why this pattern was observed. For example, older children may spend more time in childcare where mostly one language is used, therefore leading to a less balanced vocabulary learning. Another possibility is that older children increasingly elicit speech in their dominant language, which in turn amplifies vocabulary imbalance. Testing these possibilities is beyond the scope of the current paper.

that these two variables were indeed nearly perfectly correlated, r(227) = 0.99, p < .001.

Table 4. Pairwise correlations among variables (corrected for multiple comparisons using Benjamini and Yekutieli

	LEARNABLE	BALANCE WORD	WORD	DOM	NONDOM	TE	DOM-SINGLET	DOM-SINGLET NONDOM-SINGLET CONCEPT	CONCEPT
))))))	÷))
Age (in month)	0.96***	-0.24***	0.65	0.69***	0.45***	0.48***	0.65	0.19**	0.69***
LEARNABLE		-0.23***	0.62***	***99.0	0.43***	0.45	0.63***	0.21**	0.67***
BALANCE			-0.07	-0.29***	0.35***	0.25	******	0.63***	-0.21**
WORD				***96.0	0.87***	***06.0	0.74***	0.44***	0.98***
DOM					0.70***	0.76***	0.89***	0.23***	0.99***
NONDOM						***66.0	0.31***	0.72***	0.76***
TE							0.38**	***09.0	0.80***
DOM-SINGLET								-0.09	0.86***
NONDOM-SINGLET									0.33***
CONCEPT									

Note. *** p < .001, ** p < .01, * p < .05.

3.2.3 Testing Prediction Set 2: The vocabulary composition of bilingual children at different developmental levels

Prediction Set 2 pertained to expected patterns of acquisition of translation
equivalents and singlets for children of different developmental levels. In our data set,
developmental level was approximated by children's age. Figure 2 Panel B shows the
number of concept vocabulary (CONCEPT), translation equivalents (TE), singlets in the
dominant language (DOM-SINGLET), and singlets in the non-dominant language
(NONDOM-SINGLET) of the bilingual children as a function of age (our proxy for
developmental level), used to estimate the number of LEARNABLE words.

Prediction 2a was that older children (i.e., those at a later developmental level) would have larger concept vocabularies than younger children (i.e., those at an earlier developmental level). As shown in Figure 2 Panel 2A, we observed a positive correlation between age (used as a proxy for developmental level, which determines LEARNABLE) and concept vocabulary (CONCEPT) in our dataset, r(227) = 0.69, p < .001, and therefore confirmed the prediction.

Prediction 2b was that older children would produce more translation equivalents than younger children. As illustrated in Figure 2 Panel 2B, we observed a positive correlation between age (our proxy for LEARNABLE) and number of translation equivalents in our dataset, r(227) = 0.48, p < .001, and therefore confirmed the prediction.

Prediction 2c was that both older children and those with the least balanced vocabularies (BALANCE) would produce more dominant-language singlets (DOM-SINGLET). This pattern was confirmed by the results from our dataset, with a positive correlation between dominant-language singlets (DOM-SINGLET) and age (which determined LEARNABLE), r(227) = 0.65, p < .001, and a negative correlation between BALANCE and dominant-language singlets (DOM-SINGLET), r(227) = -0.58, p < .001. This is illustrated in Figure 2 Panel 2C.

Prediction 2d was that older children and those with the most balanced vocabularies (BALANCE) would produce more singlets in their non-dominant language. This pattern was also observed in our dataset, with a positive correlation between the number of non-dominant singlets (NONDOM-SINGLET) and age (which determined LEARNABLE), r(227) = 0.19, p = .005, and a positive correlation between BALANCE and the number of non-dominant singlets (NONDOM-SINGLET), r(227) = 0.63, p < .001. This is illustrated in Figure 2 Panel 2D.

3.2.4 Testing Prediction Set 3: Rate of translation equivalent learning

Prediction Set 3 pertained to the overall nature of translation equivalent learning,
describing expected patterns of translation equivalent learning under the Neutral Account,
the Avoidance Account, and the Preference Account. To directly test the correspondence of
our data with these different accounts, we built a linear regression model predicting the
observed number of translation equivalents from the Bilingual Vocabulary Model using the
formula TE = DOM×NONDOM/LEARNABLE, and we allowed the model to estimate the
BIAS parameter.

First, we will walk through the parameters in this model. Dominant vocabulary size 712 (DOM) and non-dominant vocabulary size (NONDOM) were taken to be the number of 713 words produced by individual children observed in the vocabulary data. Again, the number 714 of learnable words (LEARNABLE) was determined by averaging English and French 715 productive CDI vocabulary norms at the 90th percentile at different ages (percentile 716 information obtained from Wordbank version 0.3.1; Frank et al., 2016). Table 5 lists the denominators derived from averaging these percentiles, or LEARNABLE, at different ages. 718 For example, for an 18-month-old infant, the denominator was 240 words, which was calculated by averaging the 259 English words and 220 French words that 18-month-old 720 children would typically produce at the 90th percentile. For children who were between 31 721 and 33 months old in our dataset, the 90th percentile for 30-month-old children was used, 722

since vocabulary norms were only available up to 30 months. Finally, the intercept of the linear regression model was set at 0, since no translation equivalents are expected to be produced if a child does not have any dominant or non-dominant vocabulary (i.e., when the predictor variables are 0).

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Table 5. The number of total English and French productive CDI vocabulary words at the 90th percentile at different ages according to WordBank, and the average between the two which serves as the denominator in our computation model. Values are rounded to the nearest integer.

Age (months)	Number of English words produced at 90th percentile	Number of French words produced at 90th percentile	Average (LEARNABLE)
18	259	220	240
19	321	274	298
20	378	325	352
21	430	372	401
22	476	416	446
23	517	456	486
24	553	492	522
25	583	525	554
26	610	554	582
27	633	580	606
28	653	602	627
29	668	620	644
30 - 33	681	635	658

Note: 90th percentile information was only available up to age 30 months from WordBank, so we used that value for all children in our dataset aged 30 months and older.

To reproduce the Bilingual Vocabulary Model's formula TE =

DOM×NONDOM/LEARNABLE, an interaction between dominant and non-dominant

vocabulary was entered in the model, but main effects were not included (denoted in R by using a colon rather than an asterisk between the interacting predictors). Therefore, our final linear regression model equation was⁴:

Observed $TE \sim 0 + Dominant\ vocabulary: Non-dominant\ vocabulary/90th\ percentile\ of$ CDI items.

With the observed number of translation equivalents as the dependent variable, the 735 regression coefficient estimated by the model indicates how the BIAS parameter relates to 736 the empirical vocabulary data, which in turn indicates whether bilingual children were 737 biased towards or against learning translation equivalents. If the coefficient is close to 1, 738 then there is no bias and translation equivalents and singlets are learned similarly (i.e., the 739 Neutral Account). Otherwise, a coefficient less than 1 indicates a bias against learning 740 translation equivalents where translation equivalents are less easily learned (i.e., the 741 Avoidance Account), and a coefficient greater than 1 indicates a bias towards learning 742 translation equivalents where translation equivalents are more easily learned (i.e., the 743 Preference Account). 744

Our model showed an excellent model fit of $R^2 = 0.96$, indicating that our model explained 96% of the variance in bilinguals' translation equivalent knowledge. The BIAS coefficient was estimated at 1.04. This value is close to 1, suggesting that our data are consistent with the Neutral account, whereby translation equivalents are learned equivalently to other words⁵.

⁴ Note that for the purposes of running the model in R, the formula was rearranged and entered as Observed TE * 90th percentile of CDI items ~ 0 + Dominant vocabulary:Non-dominant vocabulary.

⁵ We also explored how these results would vary if we set the number of LEARNABLE words at the 75th percentile, rather than at the 90th percentile. Overall, model fit was slightly reduced compared to our main model, although still good, $R^2 = 0.95$. The estimated BIAS parameter was lower, at 0.95, which is nonetheless still quite close to 1, and thus consistent with the Neutral Account. This change in the BIAS parameter is mathematically expected due to the reciprocal nature of LEARNABLE and BIAS, an issue

To illustrate the close fit between the Neutral Account and our data, we used the 750 Bilingual Vocabulary Model formula $TE = 1 \times (DOM \times NONDOM/LEARNABLE)$ to 751 estimate each child's expected translation equivalent knowledge (setting BIAS = 1; also 752 setting the intercept at 0 to replicate our linear regression model), which is plotted against 753 our observed data in Figure 5. Expected and observed translation equivalents were closely 754 aligned with the Neutral Account of the Bilingual Vocabulary Model (i.e., BIAS = 1), 755 suggesting that the Neutral Account provides a parsimonious explanation for bilinguals' 756 translation equivalent knowledge. This provides evidence for the notion that translation 757 equivalents are neither harder nor easier to learn than singlets in bilingual vocabulary 758 learning. Note that visual inspection suggested that there could be some possible outliers. 759 Cook's distance was estimated for our linear regression model described above and 760 identified two data points with a Cook's distance over 0.4. After removing those two data points, the linear regression model returned a coefficient of 1.07, with $R^2 = 0.96$. As the model fit was similar to the model without eliminating the two outlier data points, we proceeded with the full data set keeping the two potential outlier data points. 764

Despite the good overall fit to the data, a close examination of Figure 5 suggested 765 that the model might less closely fit the data of children with smaller vocabulary sizes. Figure 6 displays the model fit separately for children with a word vocabulary (WORD) 767 less than 300 words and those with a word vocabulary (WORD) of 300 or greater. Based on visual inspection, the slope of translation equivalent learning appeared steeper for children with less than 300 word vocabulary, suggesting that translation equivalents are more easily learned (i.e., BIAS > 1); whereas the slope of translation equivalent learning 771 appeared to align with the Neutral Account (i.e., BIAS = 1) for children with more than 772 300 word vocabulary. To further explore this pattern, we ran the same linear regression 773 twice, separately for children with less than 300 word vocabulary and for those with more 774 than 300 word vocabulary. The model for those with a larger word vocabulary (WORD) 775

we will return to in the discussion.

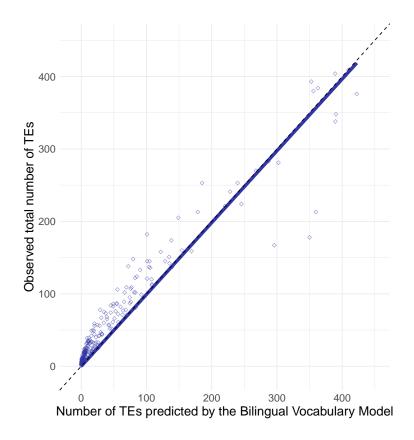


Figure 5. The number of observed and predicted translation equivalents plotted against each other. The dots represent the value of a child tested on the CDI, with their observed number of TEs and the expected number of TEs based on our model. The diagonal dashed line represents the case where the bias parameter equals 1 (BIAS = 1) such that the predicted and observed number of TEs are equal, and the solid blue line represents the model predictions.

returned a coefficient of BIAS = 1.04, whereas the model for those with a smaller word vocabulary (WORD) returned a coefficient of BIAS = 2.21. Both models fit well, although a somewhat better fit was obtained for children with larger vocabulary sizes ($R^2 = 0.96$) than children with smaller vocabulary sizes ($R^2 = 0.88$). Overall, this analysis suggests that translation equivalent learning for children with larger vocabularies corresponds best to the Neutral Account, but translation equivalent learning for children with smaller vocabularies corresponds best to the Preference Account.

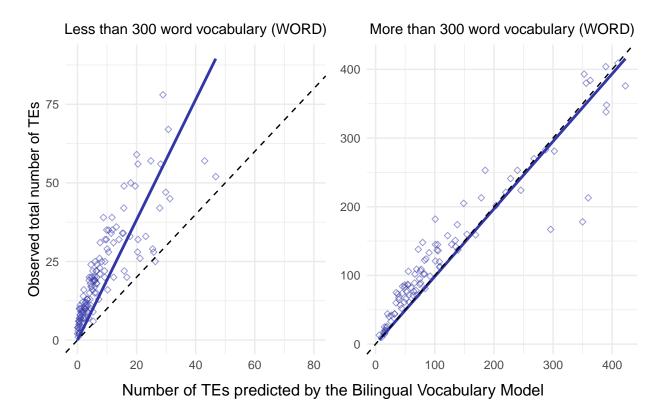


Figure 6. The number of observed translation equivalents as a function of the number of expected translation equivalents under the Bilingual Vocabulary Model (represented by the blue solid line), plotted separately for children with fewer than 300 word vocabulary (left panel) and for those with more than 300 word vocabulary (right panel). The dashed diagonal line represents the case where the parameter equals 1 (BIAS = 1) such that the predicted and observed number of TEs are equal.

4 Discussion

The aim of the current study was to better understand translation equivalent learning in bilingual children. To do so, we developed a simple model, the Bilingual Vocabulary Model, which quantifies the number of translation equivalents that children produce as a product of words they know in their dominant and non-dominant language, divided by the number of words that are learnable at their developmental level. The inclusion of a learnability parameter was a unique aspect of our approach, and was crucial to quantifying

how many translation equivalents versus singlets (i.e., the first label for a particular referent) were possible for an individual child to learn. The nature of translation equivalent learning was modeled via a parameter that indicated whether translation equivalent learning is harder than (Avoidance Account), easier than (Preference Account), or similar to (Neutral Account) learning singlet words.

In Study 1, we generated specific predictions from the model via a series of
simulations, and in Study 2 we tested these predictions against CDI production data from
200 bilingual children aged 18–33 months. There were two main findings: 1) The
predictions from the Bilingual Vocabulary Model were born out in our data, thus showing
that our simple quantitative model can explain numerous patterns in young bilinguals'
word learning; and 2) younger children's learning of translation equivalents was more
consistent with the Preference Account, while older children's learning was more consistent
with the Neutral account. In what follows, we elaborate on each of these findings.

804 4.1 Understanding patterns in bilingual children's vocabulary development

Translation equivalent learning has been of interest in studies of bilingual children's 805 development from the very earliest descriptive work (Ronjat, 1913), to more recent 806 quantitative research (David & Wei, 2008; Legacy et al., 2016; Montanari, 2010; Pearson et 807 al., 1995; 1997). Many previous studies have examined univariate relations between 808 translation equivalent knowledge and predictors such as age or vocabulary balance (David 809 & Wei, 2008; Legacy et al., 2016; Montanari, 2010; Pearson et al., 1995; 1997), but such 810 observations lacked a unifying framework. The current paper developed and validated such a framework — the Bilingual Vocabulary Model — which specifies the relationship 812 amongst multiple parameters simultaneously. Translation equivalent production is 813 predicted from four parameters: vocabulary size in the dominant language, vocabulary size 814 in the non-dominant language, the number of potentially learnable words in each language 815 given a child's developmental level, and a bias parameter indicating whether translation 816

equivalent learning is harder than, easier than, or similar to singlet learning. Translation
equivalent production can also be re-expressed via other derived variables such as
vocabulary balance, word vocabulary, concept vocabulary, and singlet vocabulary (i.e.,
words for which the child does not yet produce a translation equivalent), which can be
calculated algebraically from the original parameters (e.g., word vocabulary = dominant
vocabulary + non-dominant vocabulary).

We validated the Bilingual Vocabulary Model by generating a set of predictions in 823 Study 1 which were then tested on our empirical dataset in Study 2. First, we predicted 824 that children would produce more translation equivalents if they have more balanced 825 vocabularies (i.e., producing a similar number of words in each language), produce more words (whether in total, in their dominant language, or in their non-dominant language), 827 and if they are at a more advanced developmental level (i.e., older). Specifically, our model 828 predicted that vocabulary size in the non-dominant language would have a near-perfect 829 relationship with translation equivalent production. Second, we predicted that children 830 would produce more singlets in their dominant language if they had less balanced 831 vocabularies, and more singlets in their non-dominant language if they had more balanced 832 vocabularies. Each of these predictions was confirmed in our empirical data, and the 833 patterns found were consistent with numerous previous reports in the literature (Boyce et 834 al., 2013; David & Wei, 2008; Hoff et al., 2012; Legacy et al., 2016; Marchman et al., 2010; 835 Montanari, 2010; Pearson et al., 1993; 1995; 1997; Place & Hoff, 2011; Poulin-Dubois et al., 836 2013). We summarize our model's predictions and related empirical literature in Table 6. 837 This work therefore advances the field by providing a unifying model that explains patterns 838 in bilingual children's vocabulary development. 839

NONDOM-SINGLET.

Table 6. Summary of model predictions, related findings from previous literature, and whether our empirical data were

consistent with the prediction.

Model predictions	Evidence in previous literature	Did we observe the same pattern in our
		empirical data?
1A: Children with more balanced vocabularies	Children with more balanced vocabularies (i.e., those who produced a	Yes
(BALANCE) will produce more translation equivalents	similar number of words in each of their languages) produced more	
(TE).	translation equivalents (David & Wei, 2008; Legacy et al., 2016;	
	Montanari, 2010; Pearson et al., 1995; 1997).	
1B: Children who produce more total words (WORD) or	The number of translation equivalents a bilingual child knows increases	Yes
more dominant-language words (DOM) will produce	along with their total vocabulary size (Legacy et al., 2016; Montanari,	
more translation equivalents (TE).	2010). There is a positive correlation between bilingual children's	
	dominant language vocabulary size and the proportion of translation	
	equivalents (Legacy et al., 2016; Poulin-Dubois et al., 2013)	
1C: Children who produce more non-dominant language	Vocabulary size in the non-dominant language was positively correlated	Yes
words (NONDOM) will produce more translation	with the proportion of translation equivalents known by the child	
equivalents (TE); but unlike for WORD and DOM this	(Legacy et al., 2016).	
does not interact with BALANCE; instead,		
non-dominant vocabulary size will be an almost perfect		
predictor of translation equivalent knowledge		
2A: Older children will have larger concept vocabularies	Older children had larger concept vocabularies (Pearson et al., 1993).	Yes
(CONCEPT) than younger children.		
2B: Older children will produce more translation	Older bilingual children knew more translation equivalents than	Yes
equivalents (TE), regardless of vocabulary balance	younger children (David & Wei, 2008; Legacy et al., 2016)	
(BALANCE).		
2C: Older children will produce more dominant-language	Bilingual children learned words in proportion to their relative	Yes
singlet words (DOM-SINGLET). Moreover, those with	exposure to each language (e.g., Boyce et al., 2013; Hoff et al., 2012;	
the least balanced vocabulary (BALANCE) will produce	Marchman et al., 2010; Pearson et al., 1997; Place & Hoff, 2011)	
the most DOM-SINGLET.		
2D: Older children will produce more		
non-dominant-language singlets (NONDOM-SINGLET).		
Moreover, those with the most balanced vocabulary		
(BALANCE) will produce the most		

4.2 The status of translation equivalents in bilingual vocabulary development

Applying the Bilingual Vocabulary Model to a large set of empirical vocabulary data 841 from bilingual children allowed us to quantitatively test three conceptual accounts of 842 translation equivalent learning: the Avoidance Account, the Preference Account, and the 843 Neutral Account. Contrary to early theories of bilingual development, in our data children 844 did not seem to avoid producing a word if they knew its translation equivalent in the other 845 language (Avoidance Account; Imedadze, 1967; Swain & Wesche, 1975; Volterra & 846 Taeschner, 1978); the number of translation equivalents children produced was a very close 847 fit to the Neutral Account (i.e., translation equivalents and singlets are learned similarly), 848 with this model explaining 96% of variance in the data. This overall finding is in line with 849 previous reports that bilinguals' vocabularies in each language develop relatively 850 independently (Hurtado et al., 2014; Marchman et al., 2010). 851

However, there was some indication that the Neutral Account provided a poorer fit
for children with smaller vocabulary sizes. Modeling their data separately, we found
evidence for the Preference Account: younger children at around 22 months old appeared
to learn translation equivalents more easily than singlets, whereas older children at around
months old learned translation equivalents similarly to singlets. This could indicate a
qualitative shift in word learning that occurs as bilingual children develop and learn more
words, from the Preference Account to the Neutral Account.

We hypothesize that this pattern could stem from changes in children's word learning
abilities across development. Previous studies have suggested that strong semantic overlap
helps bilingual children learn translation equivalents more easily than singlets (Bilson et
al., 2015). However, it is possible that the boost children receive from this semantic
facilitation changes as bilingual children develop. Younger bilinguals, who are relative word
learning novices, might strongly benefit from translation equivalents, especially if
establishing a conceptual representation is a particularly hard part of the word learning

process. For translation equivalent words, children have already formed a conceptual 866 representation and only need to learn a second label for a particular referent (Montanari, 867 2010; Poulin-Dubois et al., 2013; 2018). By contrast, older bilinguals are relative word 868 learning experts. It may be that establishing a conceptual representation is somewhat easy, 869 and thus any facilitation effects of translation equivalents might be relatively small. Such 870 developmental changes would be consistent with work showing that children's word 871 learning abilities develop substantially across the first years of life (Bergelson, 2020; 872 Hirsh-Pasek & Golinkoff, 2000; Nazzi & Bertoncini, 2003; Tsui et al., 2019). 873

An additional possibility is that the nature of bilingual input changes as children 874 become more advanced word learners. Some recent research has suggested that bilingual 875 parents sometimes code-switch to use a word that they know to be in their child's 876 vocabulary (Kremin et al., 2021; Nicoladis & Secco, 2000). For example, a caregiver may 877 choose to say to their English–French bilingual child "Can you give me the livre?" if they 878 know their child understands the French word "livre" but not the English equivalent 879 "book." This may provide fewer opportunities for children to learn translation equivalents, 880 since they would be less exposed to the unfamiliar translation equivalents. However, this 881 observation would predict that young bilinguals would know fewer translation equivalents as a proportion of their vocabularies than older bilinguals, which was opposite to what we observed. Thus, changes in bilingual input may not provide an adequate explanation for our results of a qualitative change in translation equivalent learning. 885

Another explanation for the developmental pattern we observed is that the way in which age and developmental level are related changes across infancy. Indeed, even controlling for age, vocabulary size is linked to multiple factors, including cognitive abilities (e.g., Reuter et al., 2018), speech perception skills (e.g., Cristia et al., 2014), and amount of language experience (e.g., Weisleder & Fernald, 2013). Our model used age as a proxy for developmental level, assuming that all children of a particular age could potentially learn the same number of words as children at the 90th vocabulary percentile. However, there

could be much more variability in the developmental level of younger infants than of older infants. In this case, the 90th percentile might be a reasonable estimate for the number of learnable words for most older infants, but an overestimate of the number of learnable words for all but the most cognitively advanced younger infants. Given the importance of the learnability parameter in our models, future research will be needed to more precisely quantify the number of words that are learnable by particular children at particular ages.

Longitudinal data might be useful for taking these individual differences into account.

Finally, we must consider whether the pattern we observed could be related to 900 changes in children's use of one-to-one mapping biases such as mutual exclusivity. As 901 revealed by previous studies, younger children and children with smaller vocabulary sizes 902 (and thus less vocabulary knowledge) seem to have only a weak bias for a one-to-one 903 mapping between words and referents (Halberda, 2003; Lewis et al., 2020; Merriman et al., 904 1989). In other words, children with less experience in word learning may be more inclined 905 to accept multiple words for the same referent (Halberda, 2003; Merriman et al., 1989). In 906 contrast, children with larger vocabularies appear to become more certain about one-to-one 907 mapping relationships between referents and words (Lewis et al., 2020), while 908 simultaneously using their bilingual experience to understand that referents can have 909 different words between languages (Au & Glusman, 1990; Davidson & Tell, 2005). At first 910 blush, strengthening of one-to-one mapping biases with age could explain why younger 911 children appear to learn relatively more translation equivalents than older children. Yet, 912 this explanation would not predict that younger bilinguals' data would follow the Preference Account as we observed, and might instead predict development from the Neutral to the Avoidance Account (i.e. from no bias to a bias against many-to-one mappings), before perhaps returning to the Neutral Account once children realize that each 916 referent should have a label in each language. Thus, changes in one-to-one mapping biases 917 do not provide a complete explanation for our results. 918

9 4.3 Assumptions, limitations, and future directions

Our Bilingual Vocabulary Model presented an integrated computational account of 920 translation equivalent learning, focusing on the joint probability of learning the word for a 921 concept in each language. To do so, our model parameters included the number of words 922 produced in each language, as well as children's developmental level. This represents an 923 important methodological advance compared to previous approaches, which used data from 924 randomly-paired monolinguals or the vocabularies of two different bilinguals as a reference 925 point (e.g., Bilson et al., 2015; Pearson et al., 1995). However, our approach does not directly model individual difference factors such as children's ability to segment words from the continuous stream of speech (e.g., Brent & Siskind, 2001; Swingley & Humphrey, 2018), children's efficiency of processing words they hear (e.g., Hurtado et al., 2014; Weisleder & Fernald, 2013), and cognitive development and perceptual bias (e.g., Benedict, 1979; 930 Goodman et al., 2008), nor does it consider qualitative factors including family 931 socioeconomic status (e.g., Fernald et al., 2013; Hoff, 2003), parents' interaction with their 932 children (e.g., Blewitt et al., 2009; Yu & Smith, 2012), and the quality of parental language 933 input over time (e.g., Raneri et al., 2020; Rowe, 2012). It would be interesting for future 934 studies to take into consideration such factors in a bilingual word learning model, including 935 different amounts of input and the quality of that input. Such a model may better 936 characterize and predict individual differences in bilingual vocabulary development. 937

One assumption of our model was that bilingual children use labels from both languages for the same set of referents. However, according to the Complementarity Principle (Grosjean, 2016), bilinguals may have different experiences in each of their languages. For example, a French–English bilingual child who always spends bathtime with an English-speaking caregiver might encounter and use bath words primarily in English (e.g., "soap," "bath," "bubbles"), therefore having less opportunity to acquire their translation equivalents in French. At the same time, cross-linguistic data has provided

evidence of a high degree of commonality in the first words children produce (e.g., 945 Braginsky et al., 2019; Tardif et al., 2008). For example, words for important people 946 ("mommy," "daddy"), social routines ("hi," "bye," "yes," "no"), and common nouns 947 ("ball," "dog") are among the first words children acquire across languages and cultures. It 948 therefore seems reasonable to expect that young bilingual children would be exposed to 949 and produce words for a similar set of referents in each of their languages. Moreover, if 950 indeed bilingual children tend to use different words in different linguistic contexts, we 951 would have expected our data to be consistent with the Avoidance Account (e.g., fewer 952 than expected translation equivalents), which is not what we observed. Nonetheless, future 953 studies of bilingual corpora could directly address whether early translation equivalent 954 learning might be impacted by the Complementarity Principle. 955

Another consideration is that our model takes a somewhat simplified view of 956 translation equivalents, assuming that children encounter the same conceptual categories in 957 each of their languages and are exposed to the corresponding words. However, the reality 958 of bilingual experience might be more complex. First, some concepts expressed as a single 959 word in one language may be lexicalized by two words in another language (e.g., English 960 has a single word for "sister" but Mandarin has separate words for "jiějie" [older sister] 961 and "mèimei" [younger sister]). As another example, some words may not have a 962 translation equivalent in the other language (e.g., the Japanese word "sushi" is borrowed 963 into other languages). Still other languages categorize objects differently within conceptual 964 categories (e.g., a shallow dish might be called a "bowl" in English but an "assiette" [plate] in French). There is mixed evidence for whether bilingual adults maintain separate (Jared et al., 2012) versus integrated (Ameel et al., 2009) conceptual representations across their two languages, while evidence for young bilingual children suggests that conceptual representations are mostly shared between languages (Storms et al., 2015; White et al., 969 2020). Therefore, it seems reasonable to assume that early vocabulary may be represented 970 similarly across languages, especially for the age group we looked at in this study. 971

Nonetheless, future iterations of the Bilingual Vocabulary Model may consider capturing
the cases where concepts are less well aligned across languages.

Another limitation of our approach is that we modeled the number of words that 974 might be learnable at a particular age, rather than modeling the learnability of individual 975 words. For example, our model did not take into account that bilingual children appear to 976 learn similar-sounding translation equivalents (i.e., cognates like the English-French pair 977 "banana" – "banane") more easily than those that do not share similar phonological form 978 (e.g., the English-French pair "dog" - "chien") (Bosch & Ramon-Casas, 2014; Mitchell et 979 al., 2021). Likewise, some bilingual children learn language pairs that share more cognates 980 than others (e.g., Spanish and Italian share more phonologically similar translation 981 equivalents than English and French; Schepens et al., 2013). There are many other 982 individual differences between words that affect their learnability, such as frequency of 983 occurrence in speech input, concreteness, babiness, word length, semantic category, etc. 984 (Braginsky et al., 2019). It is likely that within the set of words that are learnable at a 985 given age, some will be more easily learned than others, which our model does not take 986 into account. However, the close correspondence between our model and data from 987 bilingual children suggest that even if our model is a simplification, deviations from our assumptions might have a relatively small impact. On the other hand, individual item differences could be particularly consequential at younger ages, and the apparent shift we observed in development from the Preference Account to the Neutral Account could be an 991 artifact of this issue. Future iterations of the Bilingual Vocabulary Model could explicitly 992 add such word-level factors into the model and test the importance of those factors in early bilingual vocabulary development. 994

We must also note the reciprocal relationship in the Bilingual Vocabulary Model
between the parameter that indicates whether or not children are biased to learn
translation equivalents and the parameter that accounts for how many words are
potentially learnable at a particular age. Under the Bilingual Vocabulary Model, these two

parameters jointly predict the number of translation equivalents that a child will produce 999 based on the number of words that they know in each of their languages. That is, if the 1000 assumed learnability parameter decreases by a factor of two (e.g., whereby only 120 words 1001 in each language are learnable for 18-month-olds, rather than 240), then estimates of the 1002 bias parameter will also decrease by a factor of two (i.e., rather than a parameter of 2.21 1003 which supports the Preference Account, we would estimate a parameter of 1.10 which is 1004 closer to the Neutral Account). Our main model estimated the number of learnable words 1005 to be that which children at the 90th percentile at a particular age produce, and this 1006 approach resulted in a bias parameter around 1.04, which supports the Neutral Account. 1007 The 90th percentile was chosen prior to analysis, following the reasoning that the largest 1008 vocabulary size observed at a particular age would be a reasonable estimate of how many 1009 words were potentially learnable at that age. However, we also explored the effects of 1010 setting the number of learnable words at the 75th percentile, and as mathematically 1011 expected, the estimated bias parameter decreased to 0.95, which is lower, although 1012 nevertheless still consistent with the Neutral Account. It will be important for future work 1013 to more fully explore the learnability parameter, for example, by estimating the number of 1014 words that are potentially learnable for individual children while taking into account 1015 factors beyond chronological age. 1016

Finally, the bilingual children in our sample were learning one particular language 1017 pair: French and English. In both French and English, children tend to initially learn more 1018 nouns than verbs or other word classes (i.e., noun bias; Gentner, 1982), whereas children 1019 learning other languages such as Mandarin show more equal learning of nouns and verbs 1020 (Tardif, 1996). Moreover, French and English are also typologically similar, for example 1021 they share the same basic subject-verb-object word order. Similarities across bilinguals' 1022 two languages might make it more likely that children will acquire translation equivalents. 1023 Future research could extend our approach to bilinguals learning different language pairs, 1024 and could also examine translation equivalent learning separately for different word classes. 1025

5 Conclusions

In sum, the acquisition of translation equivalents has been considered a special 1027 component in bilingual children's vocabulary development. Previous research has put 1028 forward three diverging accounts of translation equivalent learning: the Avoidance Account, 1029 the Preference Account, and the Neutral Account. We proposed the Bilingual Vocabulary 1030 Model, which provides a quantitative way to test these accounts, by modeling translation 1031 equivalent learning in relation to vocabulary size in each language and the number of 1032 potentially learnable words, which is constrained by children's developmental level. Results 1033 using archival data from a large number of young French-English bilingual children showed 1034 that our model parsimoniously explains previously disparate observations about bilingual 1035 children's translation equivalent learning. Overall, our model was a good fit to the Neutral 1036 Account suggesting that translation equivalent learning may be neither easier nor harder 1037 for bilingual children to learn than singlets, although younger children may show a 1038 preference for translation equivalent learning in line with the Preference Account. We 1039 hypothesize that such a developmental change reflects changes in bilingual children's word 1040 learning abilities, where bilingual children initially gain substantial benefit from the 1041 semantic overlap in translation equivalents, and subsequently benefit less from this type of 1042 facilitation as they grow older and become more proficient at word learning. Future studies 1043 with data from other populations of bilinguals will be important to more fully test the 1044 Bilingual Vocabulary Model. 1045

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Author Contributions

Rachel Ka-Ying Tsui: Conceptualization, Data Curation, Formal analysis, Investigation,
Methodology, Visualization, Writing - Original draft preparation, Writing - Review &
Editing, Project administration. Ana Maria Gonzalez-Barrero: Conceptualization,
Data Curation, Writing - Review & Editing. Esther Schott: Conceptualization, Data
Curation, Writing - Review & Editing. Krista Byers-Heinlein: Conceptualization,
Funding Acquisition, Methodology, Resources, Writing - Original draft preparation,
Writing - Review & Editing, Supervision, Project administration.

1067 Appendix

To more clearly illustrate the relationships between different variables in the 1068 Bilingual Vocabulary Model, we provide a more expanded and detailed illustration of our 1069 simulation approach. Here, we simulated three hypothetical children Annie, Bernie and 1070 Charlie who are at the same developmental level and thus have the same number of 1071 potentially learnable words (LEARNABLE), but with different word vocabularies (WORD) 1072 and BALANCE. As we did in the main text, we again set LEARNABLE = 600 and BIAS 1073 = 1 in this example. Other vocabulary metrics for each of the three hypothetical children 1074 are described in Table A1. 1075

Our first simulated infant, Annie (small vocabulary, unbalanced exposure), produces
270 words in the dominant language and 30 words in her non-dominant language. She has
a word vocabulary of 300, and a balance score of .10 (10% of her words are in the
non-dominant language). Based on the formula TE = DOM×NONDOM/LEARNABLE
(we drop BIAS from the formula since it is 1 here) and as seen in Table A1, Annie is
expected to produce 13.5 translation equivalents.

Our second infant, Bernie (small vocabulary, balanced exposure), produces 180 1082 dominant-language words and 120 non-dominant language words. Like Annie, he has a 1083 word vocabulary of 300, but he has a higher balance score of .40 (40% of his words are in 1084 the non-dominant language). Based on our formula, we expect Bernie to produce 36 1085 translation equivalents. Comparing Annie and Bernie, two children who produce the same 1086 total number of word vocabulary (i.e., WORD is held constant), the child with the more 1087 balanced bilingual vocabulary (Bernie) is expected to produce more translation equivalents. 1088 This corresponds to Prediction 1a in the main text. 1089

Like Bernie, our third infant Charlie also has a balanced vocabulary, but has a larger word vocabulary (WORD), producing 540 words in the dominant language (DOM) and 360 in the non-dominant language (NONDOM), for a total of 900 words (WORD), and thus

BALANCE = .40. Based on our formula for Simulation 1, we expect Charlie to produce
324 translation equivalents (TE). Infants Bernie and Charlie illustrate that for two children
equal in BALANCE, the child with larger word vocabulary (WORD) is expected to produce
more translation equivalents (TE). This corresponds to Prediction 1b in the main text.

(WORD) and vocabulary balances (BALANCE), where the number of learnable words (LEARNABLE) = 600 and BIAS = 1. Table A1. Expanded examples for Simulation 1 of three simulated children with different hypothetical word vocabularies

Vocabulary values are rounded to the nearest integer.

Variable	Definition	Calculation	Infant Anne	Infant Bernie	Infant Charlie
			(small	(small	(large
			vocabulary,	vocabulary,	vocabulary,
			unbalanced)	balanced)	balanced)
Main Parameters					
BIAS	Bias parameter		1	1	1
LEARNABLE	Learnable words in each language		009	009	009
DOM	Words produced in the dominant		270	180	540
	language				
NONDOM	Words produced in the non-dominant		30	120	360
	language				
Derived Parameters					
WORD	Word vocabulary (or total	DOM + NONDOM	300	300	006
	vocabulary size)				
BALANCE	Vocabulary balance	NONDOM / (DOM + NONDOM)	0	0	0
TE	Translation equivalents produced	${\rm DOM} \times {\rm NONDOM} \ / \ {\rm LEARNABLE}$	14	36	324
CONCEPT	Concept vocabulary (or total	WORD - TE	286	264	576
	conceptual vocabulary size)				
DOM-SINGLET	Singlets in dominant language	DOM – TE	256	144	216
NONDOM-SINGLET	Singlets in non-dominant language	NONDOM - TE	16	84	36

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