## A unified approach to inference with linked data

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#### Abstract

This paper studies what happens when the goal is to estimate a parametric model using observations (x, y), but x and y are observed in distinct datasets with imperfect identifiers. This setup requires that the researcher must attempt to identify which observations in the x- and y-datafiles refer to the same individual, prior to performing inference about the joint or conditional distributions of x and y. At a minimum, random errors in this matching step introduce measurement error that must be accounted for in subsequent analyses; however, concerns about sample selection arise when these errors are correlated with unobservables that affect x or y.

## 1 Introduction

Consider estimating  $\beta$  in a linear regression model,

$$y_i = x_i'\beta + \varepsilon_i, \ E[\varepsilon|x_i] = 0, \ E[\epsilon_i^2] = \sigma^2$$
 (1)

but, instead of observing (x, y) pairs directly, x and y are recorded in separate datasets. Additionally, both datasets contain a set of common variables w, that can be used to learn about the joint distribution of (x, y).

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Perhaps the most straightforward way to estimate  $\beta$  in this setting involves first identifying which (x, y) pairs refer to the same underlying units – the matching step – and then applying standard methods to estimate (1) using the matched pairs. Formally, for data  $\{x_i, w_i\}_{i=1}^{N_x}$  and  $\{y_j, w_j\}_{j=1}^{N_y}$ , the matching step consists of estimating a function,

$$\varphi: \{1, \dots, N_x\} \to \{1, \dots, N_y\} \cup \emptyset \tag{2}$$

where  $\varphi(i) = j$  if individual i in the x-datafile and individual j in the y-datafile refer to the same entity, and  $\varphi(i) = \emptyset$  if i does not have a match in y-datafile. Note that if w identifies individuals uniquely and without error, then  $\varphi(i) = j$  if and only if  $w_i = w_j$ , and  $\varphi(i) = \emptyset$  otherwise. However, if w is not unique or recorded with error, then  $\varphi$  needs to be estimated, and inference about  $\beta$  may need to be adjusted accordingly.

To fix ideas, suppose that  $\beta$  is the long-run impact of cash transfers on the longevity of children raised in poor families. The x variables include the characteristics of family and children who are listed in welfare program applications. The outcome variable y is age at death, which is recorded for all individuals in a universal database of death records. Both data sources contain the variables w, which include the first and last name, and place and date of birth, but the realizations of w that appear in the x- and y-datafiles may contain auxiliary variables such as place of death or ethnicity that are potentially correlated with other elements in w.

In this scenario, estimating  $\varphi$  becomes more challenging if multiple observations have identical w. In this case,  $\varphi$  may be extended to allow for multiple possible matches or probabilistic matching. In statistics, the task of recovering  $\varphi$  is called record linkage. A record linkage procedure consists of a set of decisions about (i) selecting and standardizing observations  $w_i$  and  $w_j$ , (ii) choosing which (x, y) pairs to consider as potential matches<sup>1</sup>, (iii) defining which patterns of  $(w_i, w_j)$  constitute (partial) agreements, and (iv) designating

<sup>&</sup>lt;sup>1</sup>This is primarily to reduce computation when  $N_x \times N_y$  is large

(x,y) pairs as matches.

In this setting, an example of a (deterministic) record linkage procedure consists of:

- (i) using a phonetic algorithm to standardize all string variables;
- (ii) considering as potential matches only (i, j) pairs whose phonetically standardized names begin with the same letter, and whose birth years are within  $\pm 2$  years;
- (iii) measuring agreements among names using Jaro-Winkler string distances, and weighing disagreements in birth year more than differences in birth month (and more than differences in birth day),
- (iv) designating as matches all (i, j) pairs with scores calculated using the metrics in (iii) exceeding a pre-specified cutoff; and, if a record i has multiple possible matches j that exceed the cut-off, then choosing the match with the highest score (or picking a random match if there is a tie).

Another record linkage procedure could be defined using the same rules for steps (i)-(iii), but replace (iv) with a probabilistic matching rule that does not enforce one-to-one matching:

(iv\*) use the Expectation-Maximization algorithm to compute "match weights" for each record pair; then designate as matches all pairs that exceed thresholds that are set to reflect specific tolerances for Type I and Type II error.

Except in rare cases, the matching function outputted by replacing (iv) with (iv\*) will be different. Whereas the first procedure associates each  $x_i$  with at most one matched  $y_j$ , the second procedure may associate the same  $x_i$  with multiple  $y_j$  (in technical terms, this implies  $\varphi$  is a correspondence). The former case might use estimate  $\beta$  using OLS; while the latter requires methods that associates multiple values of  $y_j$  with each  $x_i$  (Anderson et al., 2019). This example shows that not only do the estimates of  $\beta$  likely depend on the

estimates of  $\varphi$ , but also the *methods* for estimating  $\beta$  may also differ.

Each step of the record linkage process introduces the possibility that a true match is overlooked (Type II error), or that a false match is designated as correct (Type I error), and there is generally a tradeoff between reducing either one of the two (Abramitzky et al., 2019; Doidge and Harron, 2018).

As observed by Bailey et al. (2017), record linkage procedures differ by the set of assumptions that motivate their use. However, all of the procedures discussed in this paper will be studied under the following, common set of assumptions (with some departures later on):

- 1. (De-duplication) Within a given dataset, each observation refers to a distinct entity.

  That is, if two observations share the same identifier, they represent two different individuals.
- 2. (No unobserved sample selection) The observed  $x_i$  and  $y_j$  are random samples conditional on  $w_i$  and  $w_j$ , respectively. This means that all individuals with the same identifying information have equal probability of appearing in the sample.
- 3. There exists a unique  $\beta_0$  that satisfies the relationship in (1), that can be consistently estimated using standard econometric techniques if  $\varphi_0$  is known.

Merging datasets with imperfect identifiers occurs frequently in projects that use historical U.S. data sources prior to the introduction of Social Security Numbers. For example, Aizer et al. (2016) link children listed on Mothers' Pension program welfare applications from 1911-1935 with Social Security Death Master File records from 1965-2012 using individuals' names and dates of birth. Although the authors match 48 percent of children to a unique death record, and 4 percent to multiple possible records, 48 percent of observations remain unmatched<sup>2</sup>. To avoid dropping the 52 percent of observations with zero or multiple

<sup>&</sup>lt;sup>2</sup>The authors estimate that at least 32 percent of individuals in the Mothers' Pension program data died before 1965, and therefore should have no match in the 1965-2012 data.

matches, Aizer et al. (2016) estimate hazard models using methods from Anderson et al. (2019) that allow observations to be associated with multiple, equally likely, outcomes.

The methods used by Aizer et al. (2016) illustrate how inference using linked data requires joint assumptions for the matching and estimation steps. Under different assumptions, the authors could have generated a "composite match" equal to the average of the linked observations (Bleakley and Ferrie, 2016), or constructed bounds on the parameter of interest using different configurations of matched data (Nix and Qian, 2015). This example also shows how the outputs of the matching process determine which estimation tools are available. Had the authors used probabilistic record linkage methods to link the data, they could have used the robust OLS estimators from Lahiri and Larsen (2005), or prior-informed imputation for missing records proposed by Goldstein et al. (2012).

Although there are a number of recent papers that separately compare the performance of different matching algorithms (Bailey et al., 2017; Abramitzky et al., 2018) and estimation methods for linked data (Harron et al., 2014), little is known about the *joint* impact of matching and estimation on the quality of inference with linked data. This paper fills this gap by comparing how different *combinations* of matching and estimation techniques affect parameter estimates and their confidence intervals in standard econometric models, with the hope of helping researchers choose which methods best suits their projects' needs.

In order to illustrate the techniques studied in this paper, I will now introduce a running example based on synthetic datasets that imitate historical U.S. Census data, yet offer the benefit that each observation's true match is known.

**Example 1.** The "ground truth" dataset consists of 1000 observations of  $(x_{1i}, x_{2i}, y_i, w_i)$ , where  $x_{1i}$  and  $x_{2i}$  are mutually independent,  $x_{1i} \stackrel{i.i.d}{\sim} \text{Bernoulli}(0.5)$ , and  $x_{2i} \stackrel{i.i.d}{\sim} \mathcal{N}(0, 2)$ . The

value  $y_i$  generated by the relationship,

$$y_i = \beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i} + \varepsilon_i, \quad \varepsilon_i \mid x_{1i}, x_{2i} \stackrel{i.i.d}{\sim} \mathcal{N}(0, \sigma^2)$$
 (3)

with  $(\beta_0, \beta_1, \beta_2, \sigma^2) = (2, 0.5, 1, 2)$ . Given these parameter values, estimating a correctly specified linear regression model yields an  $R^2$  value of approximately 0.50 (see Figure 1(a)). Each observation is associated with a vector of identifying variables,  $w_i$ , that consists of a first and last name drawn randomly from a list of first and last names<sup>3</sup>, and a random birthday between January 1, 1900, and December 31, 1925, so that the full synthetic dataset resembles the top panel in Figure 2. Note that the number of possible names is smaller than the number of observations to ensure that there are multiple observations with the same name.

Next, I split the "ground truth" dataset into the x- and y-datafiles, which contain  $(x_1, x_2, w_x)$  and  $(y, w_y)$  values respectively. The y-datafile is identical to the ground truth data, except that it excludes the variables  $x_1$  and  $x_2$ . The x-datafile contains values for 400 observations, selected at random from the full dataset. To construct  $w_x$ , I modify the corresponding  $w_y$  by deleting characters (e.g., "Anderson" becomes "Andersn"), exchanging vowels (e.g., "Rachel" becomes "Rachal"), or swapping English phonetic equivalents (e.g. "Ellie" becomes "Elie"). I also add normally distributed errors to the birth day, month, and year. The probability of introducing an error to any one element of  $w_x$  is set to mimic real-world data <sup>4</sup>. The x- and y-datafiles are represented in the bottom panels of Figure 2.

Section 2 introduces the general problem that this paper seeks to address and outlines a common framework for comparing the techniques in Table ??. Sections 3 and 4 describe each of the methods in detail. Section 5 describes the implementation of the methods and the data. Section 6 contains the results. Section 7 will be a real empirical application, and

The first and last name lists contain 41 and 24 names, respectively, and can be found in the replication

<sup>&</sup>lt;sup>4</sup>add a footnote here

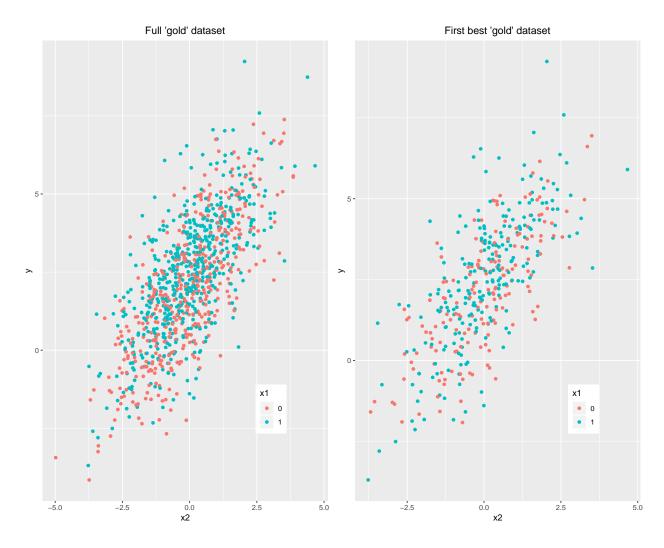


Figure 1: default

Figure 2: Creation of Synthetic Datasets

| ID   | y         | $x_1$       | $x_2$       | First Name | Last Name   | Birthday   |
|------|-----------|-------------|-------------|------------|-------------|------------|
| 1    | $y_1$     | $x_{1,1}$   | $x_{2,1}$   | Tyler      | Ashenfelter | 1915-05-13 |
| 2    | $y_2$     | $x_{1,2}$   | $x_{2,2}$   | Brandon    | Christensen | 1904-06-27 |
|      |           |             |             | :          |             |            |
| 195  | $y_{195}$ | $x_{1,195}$ | $x_{2,195}$ | Samantha   | Andersen    | 1914-08-18 |
| 196  | $y_{196}$ | $x_{1,196}$ | $x_{2,196}$ | Victoria   | Andersen    | 1918-11-25 |
|      |           |             |             | :          |             |            |
| 1000 | $y_{500}$ | $x_{1,500}$ | $x_{2,500}$ | Vicky      | Anderson    | 1915-04-14 |
|      |           |             |             | 1          |             |            |

| x-Datafile |  |                                |                          |  |
|------------|--|--------------------------------|--------------------------|--|
| ID         | x  | Name                           | Birthday                 |  |
| 2          | $(x_{1,2}, x_{2,2})$                                 | Branden Christenson            | 1905-06-27               |  |
| 195<br>198 | $(x_{1,195}, x_{2,195})$<br>$(x_{1,198}, x_{2,198})$ | Samantha Anderson<br>Jon Smyth | 1914-08-21<br>1918-12-20 |  |
| 1000       | $(x_{1,1000}, x_{2,1000})$                           | Vic Andersn                    | 1915-04-14               |  |

| y-Datame |             |  |                          |  |
|----------|-------------|--|--------------------------|--|
| ID       | y           | Name                                     | Birthday                 |  |
| 1<br>2   | $y_1$ $y_2$ | Tyler Ashenfelter<br>Brandon Christensen | 1915-05-13<br>1904-06-27 |  |
| 195      | $y_{1,195}$ | Samantha Anderson                        | 1914-08-18               |  |
| 1000     | $y_{1000}$  | Vicky Anderson                           | 1915-04-14               |  |

Section 8 will conclude.

## 2 Record Linkage Methods

In total, I implement two record linkage techniques, each of which I implement while allowing multiple or enforcing single matches. Here I provide an overview of those techniques.

### 2.1 Deterministic

The deterministic matching algorithm described herein is based upon Abramitzky et al. (2012). It consists of the following steps

1. Clean names in x and y datafiles to remove any non-alphabetic characters and account

for common mis-spellings and nicknames (e.g., so that Ben and Benjamin would be considered the same name).

- 2. Restrict the sample to people who are unique by first and last name, and year and place of birth
- 3. For each record in the x-datafile, look for records in the y-datafile that match on first name, last name, place of birth, and exact birth year. At this point there are three possibilities
  - (a) If there is a *unique* match, this pair of observations is considered a match.
  - (b) If there are multiple potential matches in the y-datafile with the same year of birth, the observation is discarded.
  - (c) If there are no matches by exact year of birth, the algorithm searches for matches within ± 1 year of reported birth year, and if this is unsuccessful, it looks for matches within ± 2 years. In each of these steps, only unique matches are accepted. If none of these attempts produces a unique match, the observation is discarded.
- 4. Step 3 is repeated for each record in the y-datafile, after which the intersection of the two matched samples is taken.

I alter the algorithm slightly so that Step 2 becomes restrict the sample to people who are unique by first and last name, year, place of birth, and  $(x_1, x_2)$  values<sup>5</sup>. When allowing for multiple matches, I count as matches all record pairs with the same name, and the difference in recorded birth years is within two (or five) years. That is, I designate all potential matches that arise in Step 3 as matches.

A quirk of this algorithm is that one person could have a unique exact year match, but then multiple matches with birth years off by 1; this person is included when a unique

<sup>&</sup>lt;sup>5</sup>This becomes y values when I repeat the algorithm linking y to the x-datafile

match is desired. But if the unique match with zero year difference were not present, then the observation would be dropped.

Example 1 (cont'd).

### 2.2 Probabilistic Record Linkage

In describing the record linkage techniques implemented in this paper, I use notation from Fellegi and Sunter (1969). As before, consider two datafiles X and Y that record information from two overlapping sets of individuals or entities. The files originate from two record-generating processes that may induce errors and missing values, so that identifying which individuals are represented in both X and Y is nontrivial. I assume that individuals appear at most once in each datafile, so that the goal of record linkage is to identify which records in files X and Y refer to the same entities.

Suppose that files X and Y contain  $N_x$  and  $N_y$  records, respectively, and without loss of generality that  $N_y \geq N_x$ . Denote also the number of entities represented in both files as  $N_{xy}$ , so that  $N_x \geq N_{xy} \geq 0$ .

We say that the set of ordered record pairs  $X \times Y$  is the union of two disjoint sets,  $matches\ (M)$  and  $non-matches\ (U)$ :

$$M=\{(i,j):i\in X,j\in Y,i=j\}$$

$$U=\{(i,j):i\in X,j\in Y,i\neq j\}$$

Hence, the formal goal of record linkage is to identify whether an arbitrary record pair  $(i, j) \in X \times Y$  belongs to M or U.

To perform this task, each record pair is evaluated according to K different comparison criteria, which are the result of comparing data fields for records i and j. For example, if a

record pair (i, j) represents two individuals, the pair may be evaluated according to whether they share a first name or have the same birthday. These comparisons are represented by a comparison vector,

$$\boldsymbol{\gamma_{ij}} = (\gamma_{ij}^1, \dots, \gamma_{ij}^k, \dots, \gamma_{ij}^K)$$

where each comparison field  $\gamma_{ij}^k$  may be binary-valued, as in "i and j have the same birthday," or use levels to account for partial agreement between strings (see ?, for details).

#### Example 1 (cont'd).

The probability of observing a particular configuration of  $\gamma_{ij}$  can be modeled as arising from the mixture distribution:

$$P(\gamma_{ij}) = P(\gamma_{ij}|M)p_M + P(\gamma_{ij}|U)p_U$$
(4)

where  $P(\gamma_{ij}|M)$  and  $P(\gamma_{ij}|U)$  are the probabilities of observing the pattern  $\gamma_{ij}$  conditional on the record pair (i,j) belonging to M or U, respectively. The proportions  $p_M$  and  $p_U = 1 - p_M$ are the marginal probabilities of observing a matched or unmatched pair. Applying Bayes' Rule, we obtain the probability of  $(i,j) \in M$  conditional on observing  $\gamma_{ij}$ ,

$$P(M|\gamma_{ij}) = \frac{p_M P(\gamma_{ij}|M)}{P(\gamma_{ij})}$$
(5)

so that if we can estimate the variables in (4), we can estimate the probability that any two records refer to the same entity in (5). These probabilities can then be used to designate pairs as matches, and to estimate the false positive rates associated with any potential match configuration.

Let  $\Gamma \equiv \{ \gamma_{ij} : (i,j) \in X \times Y \}$  denote the set of comparison vectors for all records pairs  $(i,j) \in X \times Y$ . Note that  $\Gamma$  contains potentially  $N_x \times N_y$  elements, so that calculating  $\Gamma$  may be computationally expensive when X or Y is large. In practice, researchers partition  $X \times Y$ 

into "blocks," such that only records belonging to the same block are attempted to be linked, and records belonging to different blocks are assumed to be non-matches. Importantly, the blocking variables should be recorded without error, and sometimes there are none available.

**Example 1 (cont'd).** This paper assumes that no blocking is used; or, alternatively, that records are already divided into blocks that can be analyzed independently using the methods outlined below.

Another important simplifying assumption is that of conditional independence. While in principle we can model,

$$(\gamma_{ij}^1, \dots, \gamma_{ij}^K) \mid M \sim \text{Dirichlet}(\boldsymbol{\delta}_{\mathbf{M}})$$

$$(\gamma_{ij}^1, \dots, \gamma_{ij}^K) \mid U \sim \text{Dirichlet}(\boldsymbol{\delta}_{\mathbf{U}})$$

there are  $2^K - 1$  possible configurations of each  $\gamma_{ij}$ , so that  $\delta_{\mathbf{M}}$  and  $\delta_{\mathbf{U}}$  may be high-dimensional. Instead, if the comparison fields are structured so that the  $\gamma_{ij}^k$  are independent across k conditional on match status, then,

$$P(\gamma_{ij}|C) = \prod_{k=1}^{K} P(\gamma_{ij}^{k}|C)^{\gamma_{ij}^{k}} (1 - Pr(\gamma_{ij}^{k}|C))^{1-\gamma_{ij}^{k}} \qquad C \in \{M, U\}$$
 (6)

and the number of parameters used to describe each mixture class is reduced to K. This assumption can be relaxed using log-linear models, but for now I assume conditional independence to ease computation.

**Example 1 (cont'd)**. Errors are constructed to satisfy this assumption

## 3 Estimation Methods

This section provides an overview of the estimation methods I compare for analyzing the matched datasets.

#### 3.1 OLS Bias Correction

Scheuren and Winkler (1993) and Lahiri and Larsen (2005) propose techniques for correcting the bias from mismatched pairs in linear regression. They assume that the matching procedure produces n pairs  $(x_i, z_i)$ , where  $z_i$  may or may not correspond to  $y_i$ , yet the true  $y_i$  is included among the matches. Hence,

$$z_i = \begin{cases} y_i & \text{with probability } q_{ii} \\ y_j & \text{with probability } q_{ij} \text{ for } j \neq i, \ j = 1, \dots, n \end{cases}$$

and  $\sum_{j=1}^{n} q_{ij} = 1$ , i = 1, ..., n. Estimating (1) using  $z_i$  as the dependent variable yields the naive least squares estimator,

$$\hat{\beta}_N = (X'X)^{-1}X'z \tag{7}$$

which is biased. Denoting  $q_i = (q_{i1}, \dots, q_{in})'$  and  $Q = (q_1, \dots, q_n)'$ , we can write the bias of  $\hat{\beta}_N$  as

$$\operatorname{bias}(\hat{\beta}_N) = [(X'X)^{-1}X'QX - I]\beta$$

since  $E[z_i] = E[q'_i y] = q'_i X \beta = \sum_{j=1}^n q_{ij} x'_j \beta$ .

To reduce the bias of  $\hat{\beta}_N$ , Scheuren and Winkler (1993) observed that

$$bias(\hat{\beta}_N|y) = E[(\hat{\beta}_N - \beta)|y] = (X'X)^{-1}X'B$$
(8)

where  $B = (B_1, \ldots, B_n)'$  and  $B_i = (q_{ii} - 1)y_i + \sum_{j \neq i} q_{ij}y_j = q_i'y - y_i$ , which is the difference

between a weighted average of responses from all observations and the actual response  $y_i$ . The authors suggest estimating 8 using the first and second highest elements of the vector  $q_i$ , so that  $\hat{B}_i^{TR} = (q_{ij_1} - 1)z_{j_1} + q_{ij_2}z_{j_2}$ , and

$$\hat{\beta}_{SW} = \hat{\beta}_N - (X'X)^{-1}X'\hat{B}^{TR} \tag{9}$$

The estimator can incorporate any number of elements of  $q_i$ , but, if the probability is high that the best candidate link is the true link, then the truncation might produce a very small bias.

Using  $E(z_i) = w_i'\beta$ , where  $w_i = q_i'X_i\beta$ , Lahiri and Larsen (2005) propose the unbiased estimator:

$$\hat{\beta}_U = (W'W)^{-1}W'z$$

where  $W = (w_1, ..., w_N)'$ . They also suggest using a truncated version of W, with  $w_i^{TR} = q_{ij_1}x_{j_1} + q_{ij_2}x_{j_2}$ , where values of  $q_{ij}$  are estimated by using a probabilistic record linkage procedure.

For both methods, standard errors are calculated according to a parametric bootstrap procedure/formulas in the appendix.

These procedures are valid if the estimated probabilities in  $\hat{Q}$  are independent of z. They argue that this is expected to be true in most applications, because the distribution of matching variables (e.g. first and last name, age), which determines the distribution of  $\hat{Q}$ , is usually independent of the response variable y (e.g. income), and hence of z. However, this assumption is unlikely to hold in important economics applications, such as the racial "passing" example from Nix and Qian (2015).

### 3.2 Multiple match WLS

Anderson et al. (2019) consider the case where the researcher has a dataset  $(x_i, \{y_{i\ell}\}_{\ell=1}^{L_i}, w_i)$ . That is, each  $x_i$  is linked to many possible  $L_i$ , each of which is considered to be equally likely. They suggest estimating  $\beta$  in the smoothed regression:

$$\sum_{\ell=1}^{L_i} y_{i\ell} - (L_i - 1)g(w_i, L_i) = x_i'\beta + \epsilon_i$$
(10)

where  $g(w_i, L_i) = E[y_{i\ell}|w_i, L_i]$ , which can be estimated nonparametrically. This results in a weighted least squares setup.

Let  $M_i = \{y_{i\ell}\}_{\ell=1}^{L_i}$ , the set of outcomes linked to observation  $x_i$ . If  $M_i$  contains the true match  $y_i$ , then the estimator is unbiased:

$$E[\hat{\beta}] = E[x_i x_i']^{-1} E\left[x_i \left(\sum_{\ell=1}^{L_i} y_{i\ell} - (L_i - 1)g(w_i, L_i)\right)\right]$$

$$= \beta + E[x_i x_i']^{-1} E\left[x_i \left(\sum_{M_i/y_i} y_{i\ell} - (L_i - 1)g(w_i, L_i)\right)\right]$$

$$= \beta + E[x_i x_i']^{-1} E\left[E[x_i|w_i, L_i]E\left[\sum_{M_i/y_i} y_{i\ell} - (L_i - 1)g(w_i, L_i)|w_i, L_i\right]\right]$$

$$= \beta$$

The second to last line follows from the assumption that  $x_i$  and  $y_{i\ell}$  are random samples conditional on  $w_i, L_i$ .

|   | method        | nMatches | pCorrect | nUniqueX |
|---|---------------|----------|----------|----------|
| 1 | abe_single    | 338      | 0.96     | 338      |
| 2 | $abe\_multi$  | 479      | 0.77     | 375      |
| 3 | $prl\_single$ | 335      | 0.87     | 335      |
| 4 | prl_multi     | 397      | 0.79     | 335      |

## 4 Simulation Results

# 5 Conclusion

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