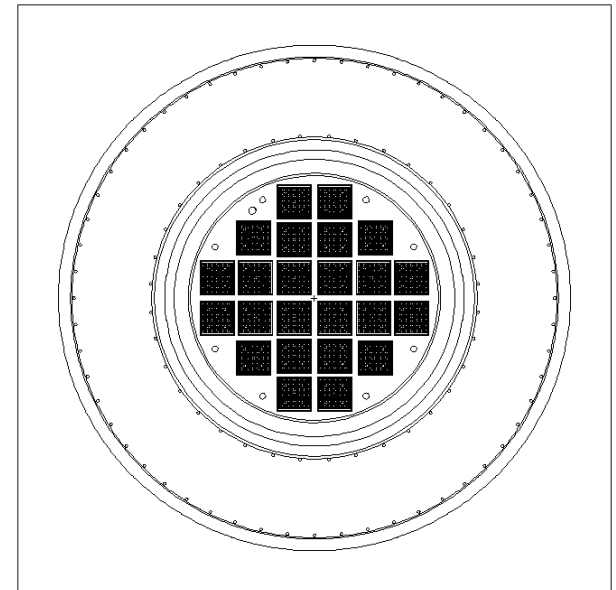
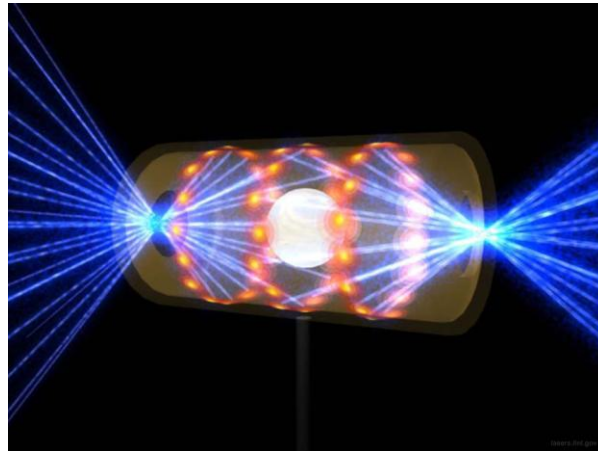
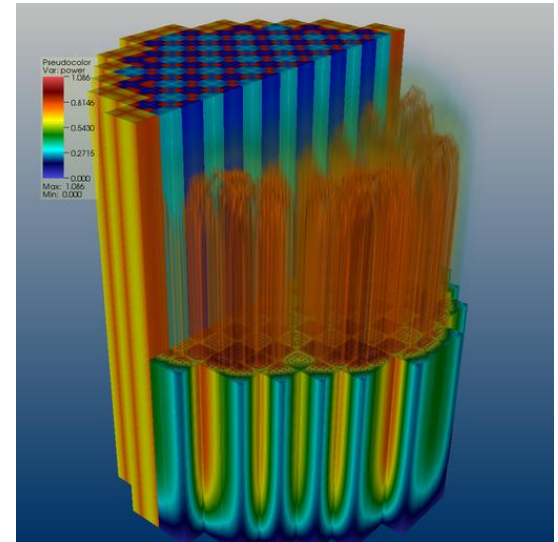


Research Overview for Neutronics Group

Prof. Rachel Slaybaugh

What exactly do you do?

$$\begin{aligned} [\hat{\Omega} \cdot \nabla + \Sigma(\vec{r}, E)] \psi(\vec{r}, \hat{\Omega}, E) = \\ \int dE' \int d\hat{\Omega}' \Sigma_s(\vec{r}, E' \rightarrow E, \hat{\Omega}' \cdot \hat{\Omega}) \psi(\vec{r}, \hat{\Omega}', E') \\ + \frac{\chi(E)}{k} \int dE' \nu \Sigma_f(\vec{r}, E') \int d\hat{\Omega}' \psi(\vec{r}, \hat{\Omega}', E') \end{aligned}$$



How do you do it?

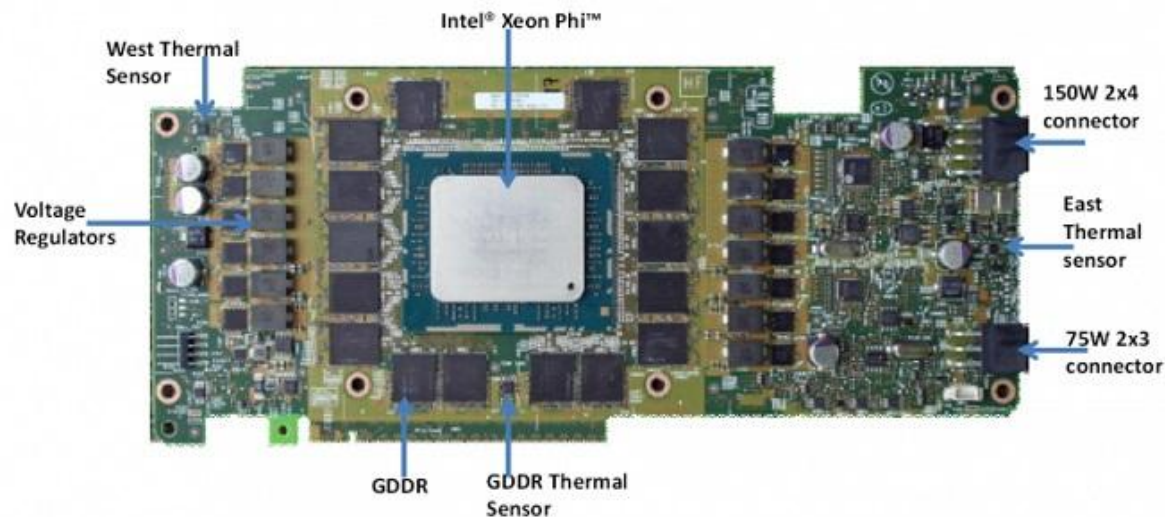
- **Deterministic** methods require discretization of phase space
 - discretize more finely to improve solution quality
 - use advanced solvers to converge solution more quickly
- **Monte Carlo** (MC) treats phase space continuously
 - accuracy depends on number of particles simulated
 - often requires variance reduction (VR)
- **Hybrid** methods: create MC VR parameters using deterministic solutions

Algorithms + Architecture



Current Projects: WARP

- “Weaving All the Random Particles” (Bergmann)
- GPU-Based Monte Carlo
- Kelly has implemented and is completing testing of Woodcock Delta-tracking
- Next up: adaptation for MICs (Multi Integrated Cores, e.g. Intel XeonPhi)



Current Projects: Angle-Informed Hybrid Methods

Use adjoint relationship to create VR parameters for MC

$$\int \int q^+(r, E) \phi(r, E) dr dE = \int \int q(r, E) \phi^+(r, E) dr dE$$

$$q^+(r, E) = f(r, E)$$

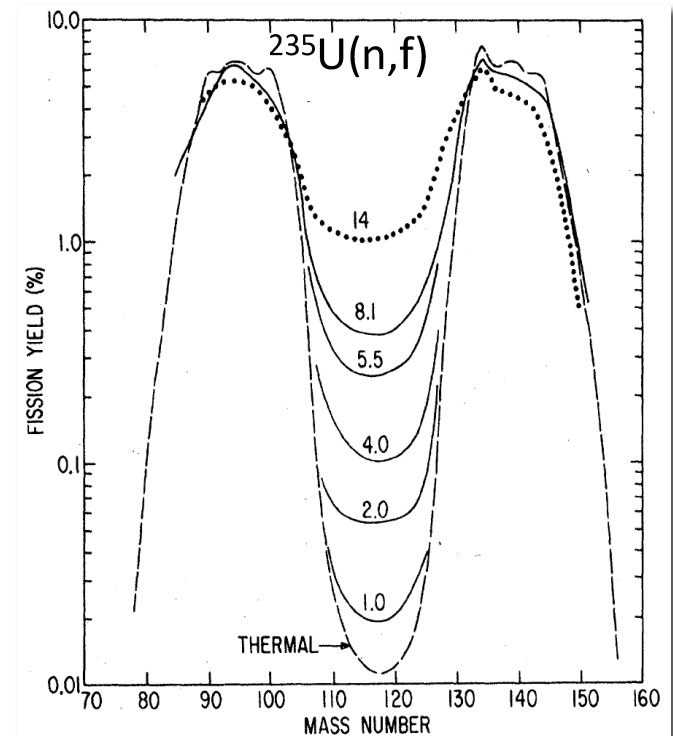
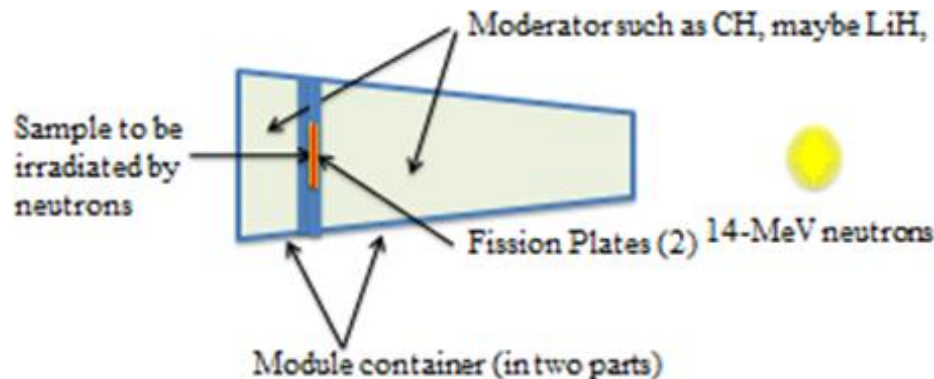
$$R = \int \int_{E V_f} f(r, E) \phi(r, E) dr dE \quad \longrightarrow \quad R = \int \int_{E V_S} q(r, E) \phi^+(r, E) dr dE$$

Create an importance map augmented by angular information

$$\phi^\dagger(\mathbf{r}, E) = \frac{\int \psi(\hat{\Omega}, \mathbf{r}, E) \psi^\dagger(\hat{\Omega}, \mathbf{r}, E) d\hat{\Omega}}{\int \psi(\hat{\Omega}, \mathbf{r}, E) d\hat{\Omega}}$$

Current Projects: Energy Tuning Assembly

- Develop a tailored spectrum irradiator for forensics applications at NIF
- Constraints
 - Thermonuclear weapon-like spectra
 - Geometry: $\sim 7.5\%$ solid angle
 - $\sim 10^{12}$ fissions
 - Minimize fertile/fissile material



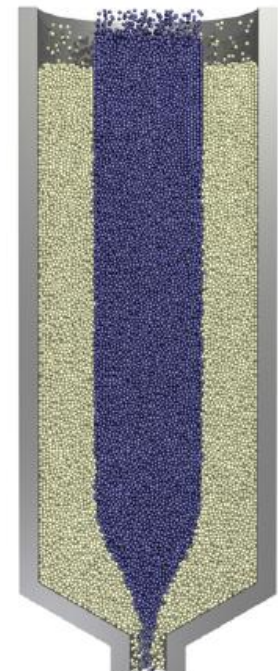
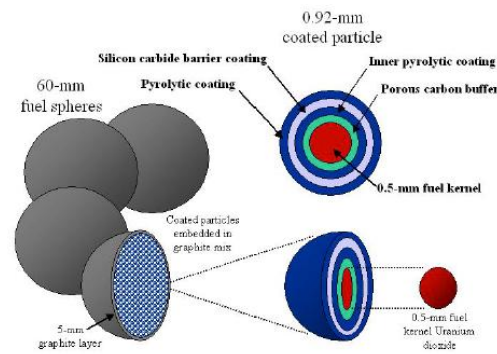
[8] Gene Henry and Bill Dunlop

[9] J.E. Gindler et al.

Upcoming Projects: non-classical transport

- Classical Transport inherently assumes that the distances between collisions are exponentially distributed: $p(s) = \Sigma_t e^{-\Sigma_t s}$
- Non-Classical Transport drops this assumption, generalizing the linear Boltzmann equation

$$\frac{\partial \psi}{\partial s}(\mathbf{x}, \Omega, s) + \Omega \cdot \nabla \psi(\mathbf{x}, \Omega, s) + \Sigma_t(\Omega, s) \psi(\mathbf{x}, \Omega, s) \\ = c \delta(s) \int_{4\pi} \int_0^\infty P(\Omega' \cdot \Omega) \Sigma_t(\Omega', s') \psi(\mathbf{x}, \Omega', s') ds' d\Omega' + \delta(s) \frac{Q(\mathbf{x})}{4\pi}$$





Full PWR-900 Details

2 x 2 spatial cells/pin

17 x 17 pins/assembly

289 assemblies (132 reflector,
159 fuel of varying enrichment)

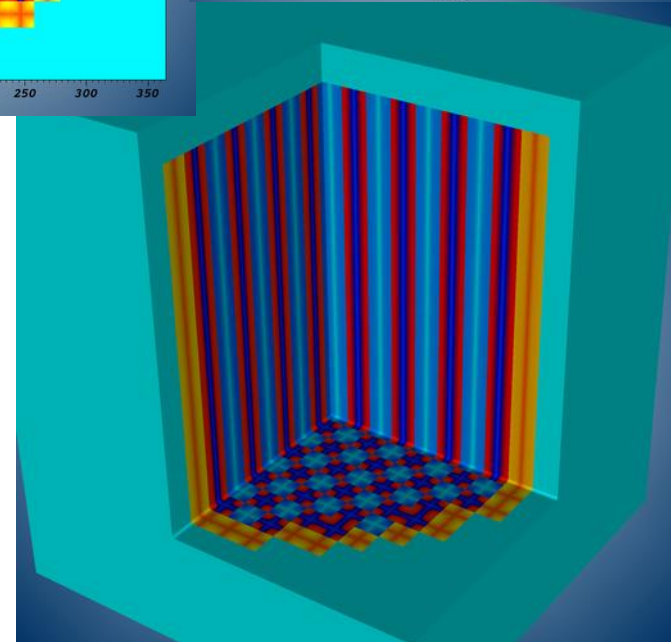
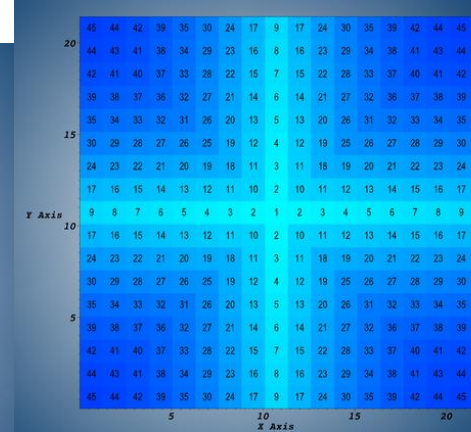
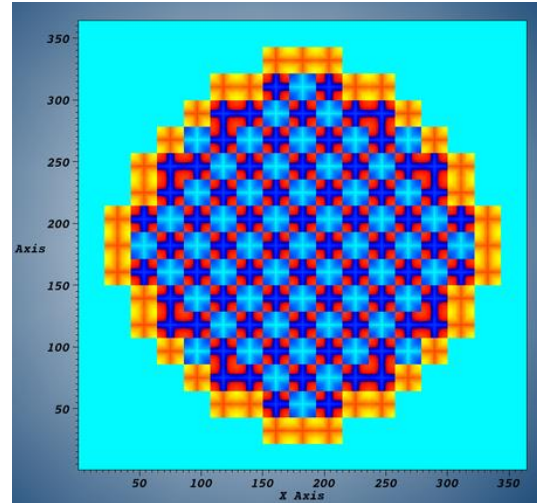
P_0 : 1 moment

S_{12} : 168 angle sets (MGE: S_2)

233,858,800 cells; 1 unknown/cell

44 groups: *1.73 trillion unknowns*

12,544 blocks; 137,984 cores (11 sets)





RQI Can Beat PI

- RQI needed **less time** and **fewer iterations**

Solver	Precond	Krylov	Eigen	Time (m)
PI	none	5.602	149	612.2
PI	w1r2v2	946	86	720 [*]
PI	w1r3v3	111	11	480 ^{*,+}
RQI	w1r2v2	70	5	54.8
RQI	w1r3v3	76	6	330.4 ⁺

^{*}Exceeded wall time limit

⁺S₁₂ in MGE; different tolerances and decomposition



RQI+MGE Strong Scaling

**Time vs. Cores for PWR-900 with
Preconditioned RQI**

