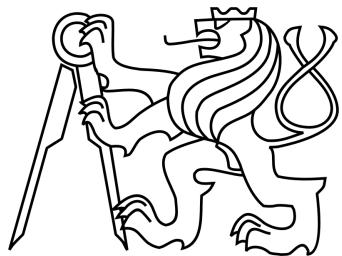


CZECH TECHNICAL UNIVERSITY IN PRAGUE  
FACULTY OF ELECTRICAL ENGINEERING  
DEPARTMENT OF CYBERNETICS



## BACHELOR THESIS

RRT-path method used for cooperative surveillance by  
group of helicopters

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In Prague, 2016

**Název práce:** Aplikace algoritmu RRT-path v úloze autonomního dohledu skupinou helikoptér

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**Abstrakt** Tato práce se zabývá plánováním trasy roje složeného z bezpilotních helikoptér v úloze autonomního dohledu. Popisují zde principy a implementaci algoritmu pro plánování trasy roje bezpilotního helikoptér za použití RRT-Path algoritmu. Algoritmus popsán v této práci kombinuje RRT-Path algoritmus s optimalizací pomocí Dubinových křivek. Tato práce zahrnuje implementaci algoritmu v jazycích C++ a Python. Funkce vyvinutého systému byla ověřena experimenty, které jsou prezentovány v této práci.

**Klíčová slova:** RRT, RRT-Path, Dubins curves, UAV, swarm

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**Abstract** In this thesis we study deployment of a swarm consisting of Unmanned Aerial Vehicles (UAVs) in the task of autonomous surveillance using motion planning. This thesis describes principles and implementation of the algorithm for motion planing of swarm of UAVs using the RRT-Path algorithm. Algorithm described in this thesis combines the RRT-Path algorithm with optimization by Dubins Curves. The thesis includes the implementation in C++ and Python, functionality was verified by experiments presented in this thesis.

**Keywords:** RRT, RRT-Path, Dubins curves, UAV, swarm

**Prohlášení autora práce**

Prohlašuji, že jsem předloženou práci vypracoval samostatně a že jsem uvedl veškeré použité informační zdroje v souladu s Metodickým pokynem o dodržování etických principů při přípravě vysokoškolských závěrečných prací.

V Praze dne \_\_\_\_\_

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Podpis autora práce

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CHAPTER  
**ONE**

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## INTRODUCTION

Unmanned Aerial Vehicle (UAV) is an aircraft intended to operate with no pilot on-board. The UAV is also known as drone and it has been gaining popularity in recent years in both academic circles and wide public. The term Micro Aerial Vehicle (MAV) is also used for very small UAV, typically intended for multi-robot scenarios. Drones are used in many applications, both military and civil, but unfortunately, the term “drone” has negative connotation and is mainly linked to military actions. The main complication of massive industrial use of drones is national regulation and legislation.

The drone may be controlled with various kinds of autonomy: either by a given degree of remote control from an operator, located on the ground or in another vehicle, or fully autonomously, by onboard computers [9].

For small drones, the quadrotor (also called quadcopter) design has become very popular and widely used. Quadrotor is a helicopter that is lifted and propelled by four horizontal rotors. Quadrotors are used in the Multi-Robot Systems group at CTU, which uses them in various multi-robot scenarios, such as formation flying [13, 14, 16, 17, 20], swarm robotics [12, 19], environment monitoring [18] and autonomous surveillance [15, 22], which is being solved also in this thesis. Example of a swarm of quadrotors can be seen in figure 1.1.

International Civil Aviation Organization (ICAO) [9] classifies UAVs into two groups: Remotely piloted aircraft - an aircraft where the pilot is not on board of the aircraft and control the aircraft from another location, and Autonomous aircraft - an unmanned aircraft that does not allow pilot intervention in the management of the flight.

Remotely piloted aircraft are teleoperated usually by a person with a remote radio controller. Some examples of uses of teleoperated aircraft are inspections of power lines [4], monitoring of agricultural areas [5], with proof of concept demonstrated in Château de Châtagneréaz vineyard [1], filming movies and acrobatic aerial footages [5], counting wildlife and searching people lost in wilderness [10] and crowd monitoring of large events including festivals and protests. UAV monitoring of crowds allow operators to see different parts of the surveyed scene, follow crowd/people and thus provide information that is not accessible with fixed infrastructure of immovable cameras. UAVs are handy in many use cases, where helicopters with human pilots are too costly or unwieldy.

Autonomous aircraft fly independently without an operator directly controlling the flight. The operator specifies a task for the aircraft to execute instead. The task difficulty depends on the level of autonomy of the aircraft. It can be anything from flying straight to a single point or



Figure 1.1: Quadrotors assembled in the Multi-Robot Systems group at CTU

following a path consisting of multiple points, to perform a complex task of following a moving object and avoiding collisions.

Both start-up companies and large corporates compete in developing various kinds of autonomous aircraft for many different purposes. Currently there are 368 projects on kickstarter tinkering with drones. The Amazon plans to use autonomous drones for packages delivery in their program Prime Air [25]. Next to delivering goods, the other commonly discussed topic is localization of people or other objects in rescue missions taking place in dangerous or hard to access areas and autonomous surveillance of Areas of Interest (abbreviated as AoI).

Miniaturization, more manufacturers and lowering costs of UAVs and nature inspired algorithms led to the idea of creating UAV swarms. Vito Trianni [23] defines four criteria for robotic system to be considered a swarm robotic system.

1. The system should be relevant for the coordination and control of a large number of robots.  
This includes all approaches that aim for scalability.
2. The system should involve relatively few groups of homogeneous robots, each group comprising a large number of individuals, high redundancy is required within each group.
3. The system should consider tasks that can not be effectively solved by the single robot, due to individual limitations.
4. The system should involve robots that have local and limited sensing and communication abilities.

The approach presented in this thesis is not scalable, but it satisfies the other criteria. Swarm cannot be remotely controlled by one person and controlling each UAV in swarm by one operator would be really hard to coordinate and practically impossible to avoid collisions between UAVs,

so the only plausible way to manually control the swarm is to remotely control whole swarm as one drone. This thesis deals exclusively with fully autonomous aircraft where no UAV needs to be remotely controlled by an operator.

In the problem of controlling of swarm, collisions between UAVs must be avoided. That means that a method to keep them in a safe distance between each other has to be found. Second, a precise enough relative localization system is needed to keep track of the swarm formation shape and relative distances. And finally, a motion planning algorithm has to be developed in order to move the swarm from its initial position to a target position (Area of Interest in case of the surveillance scenario) in a certain environment which can contain a set of obstacles [6]. Keeping track of the position of UAV individuals in the swarm is essential to prevent collisions between them and keeping the swarm organized. The most obvious approach would be to equip each UAV with a Global Positioning System (GPS) chip to obtain absolute positions and use them to calculate relative distances between each other. However, UAVs are often deployed in areas where GPS performs poorly or is impossible to use (e.g. inside buildings), moreover, even in open spaces with a good GPS signal the accuracy offered by GPS (around 3 m) is not sufficient for control of compact swarms with possibly smaller relative distances.[11]

## 1.1 Objective

The objective of this thesis is to explore the possibility of using swarms of UAVs in the task of autonomous surveillance. The task is defined as finding a collision free trajectories from initial depot to an AoI or more AoIs and covering the largest possible part of AoI or AoIs. For details on the problem definition see [22].

This task can be done using several approaches. One approach is finding an optimal position in AoI for each individual UAV and then searching feasible and collision-free trajectory for each UAV. This approach has the problem that the feasible solution may not exist due to obstacles and relative localization constrains, as shown in [22]. A demonstration of such problem can be seen in the figure 1.2. Another approach is to find trajectory to any points above AoIs and then to optimize AoI coverage.

This thesis presents implementation of finding feasible trajectories using the RRT-Path algorithm [26–28] and optimization by Dubins curves [2]. The RRT-Path algorithm is based on the Rapidly-exploring Random Tree algorithm (RRT), described in [7]. To guarantee proper function of the RRT-Path algorithm for multi-UAV deployment, many support algorithms and systems must be implemented. The motion model of UAVs is implemented and collision avoidance algorithm is used for obstacles avoidance. In the next step, trajectories found by the RRT-Path algorithm are optimized using the Dubins curves, which provide optimal trajectory for motion model used in this thesis.

Part of this thesis is also verification of the planning algorithm by following trajectories by UAVs swarm in simulation software V-REP. The last part of this thesis is to design an interface with system [21], where trajectories can be loaded to real UAVs for experiments.

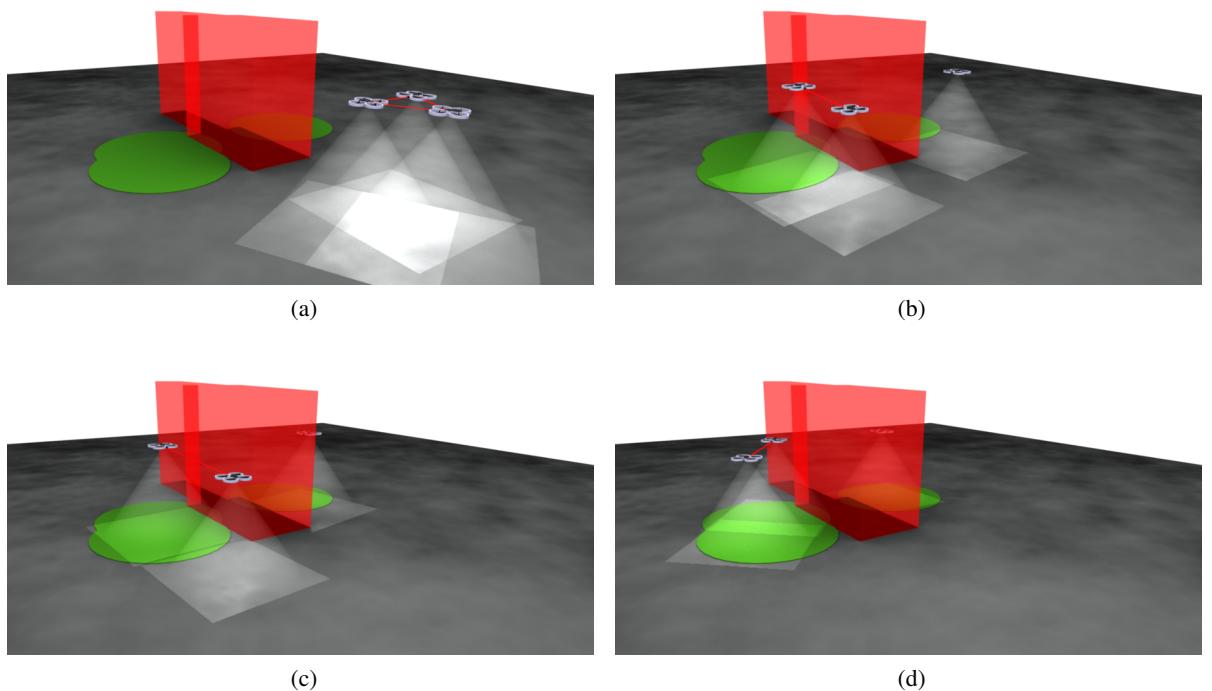


Figure 1.2: Violation of the relative localization constraints when trajectories are planned after searching the optimal positions. Relative localization constraints are violated in b), c), d). Obstacles are visualized by red colour, AoIs by green colour. Source [22]

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CHAPTER  
**TWO**

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## ALGORITHM

The basic structure of the whole algorithm is shown in the figure 2.1.

The first module represents finding the guiding paths for the trajectory planning. It takes map as an input and returns the optimal path from initial positions to AoIs. The path planning uses an A\* algorithm. All details regarding the path planning are explained in section 3.3. The trajectory planning consists of three sub-modules. The first sub-module is the RRT-Path trajectory planning which takes the map and the guiding path as the inputs and returns space-filling tree with some leaves in the AoIs. The next sub-module is RRT which continues to search the space above AoIs. All feasible trajectories are used as an input of the sub-module for finding the best coverage. This sub-module computes coverage of AoIs in each configuration and returns the trajectory to configuration with the best AoIs coverage. The quality of the coverage is determined by the cost function, which is described in chapter 5. The trajectories re-sampling module re-samples trajectories to higher sampling rate, which results in smoother trajectories. This module is here mainly due to constraints of real UAVs, which are mentioned in chapter 9. The last module is optimization of trajectories by Dubins curves. The optimization is explained in chapter 8.

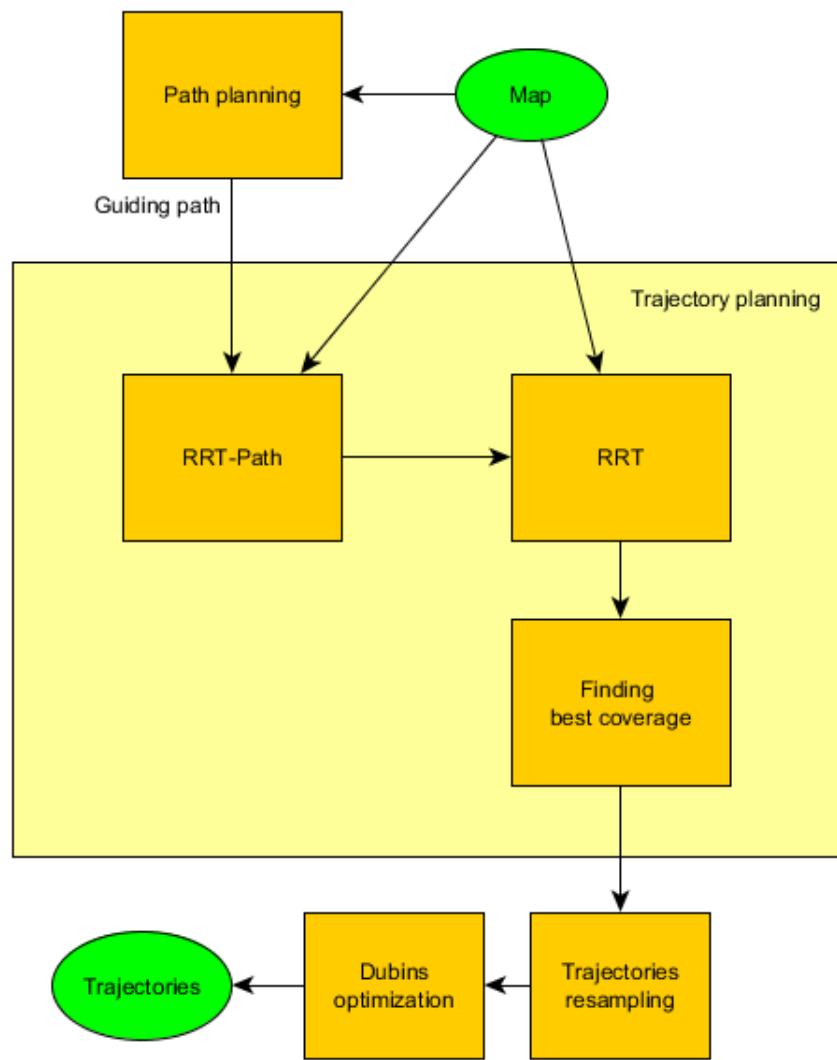


Figure 2.1: The basis of whole algorithm

## RRT-PATH

In this chapter a brief introduction of the RRT-Path algorithm is covered. Firstly, we need to define the RRT algorithm which the RRT-Path is based on.

### 3.1 Rapidly Exploring Random Tree

Rapidly Exploring Random Tree (RRT), introduced by LaValle [7] in 1998, is non-deterministic algorithm for motion planning, used to search non-convex spaces by randomly-built space-filling tree. The RRT method builds a tree  $T$  rooted at  $q_{start}$ . In each iteration, a random sample  $q_{rand}$  is chosen from the configuration space  $C$  and the nearest node  $q_{near}$  in the tree to  $q_{rand}$  is found. The node  $q_{near}$  is expanded using a local planner to obtain a set of new configurations reachable from  $q_{near}$ . The nearest configuration towards  $q_{rand}$  is selected from this set and added to the tree. The edge from  $q_{near}$  to the newly added configuration contains control inputs used by the local planner to reach the new configuration. The algorithm terminates if the distance between a node in the tree and  $q_{goal}$  is less than  $d_{goal}$  or after  $I_{max}$  of planning iterations. [28] The RRT method is sketched in pseudocode 3.1. In the RRT algorithm, configurations on the third line have uniform distribution. The implementation of the expansion step is sketched in pseudocode 3.2. The expansion step includes motion planning with the use of a motion model. Forward motion model  $\dot{q} = f(q, u)$  is considered there and the expansion of node  $q$  is realized by applying several control inputs  $u \in U$  to the model in order to obtain new configurations reachable from the node. The control inputs are applied over time  $\Delta t$ . New configurations are obtained by integration of the motion model, which can be solved analytically in the case of simple systems like Car-like robots [20], or using numerical integration like Euler integration of Runge-Kutta methods for complex systems. As UAVs can be driven by continuous values, the set  $U$  has to be discretized in order to allow RRT to expand the node  $q_{near}$  to a reasonable number of candidate configurations. [28]

### 3.2 RRT-Path

RRT-Path, introduced by Vonásek [26, 28] in 2015, is an improved version of RRT featuring preprocessing of configuration space. RRT-Path enables UAVs to manoeuvre around obstacles and find way in narrow passages. RRT-Path also finds goal much faster [11]. RRT-Path uses the

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**Algorithm 3.1** the RRT algorithm source [28]

**Input:** Configurations  $q_{alert}$  and  $q_{goal}$ , maximum number of iterations  $I_{max}$ , maximum distance to goal  $d_{goal}$ , configuration space  $C$

**Output:** Trajectory  $P$  or failure

```

1:  $T.add(q_{start})$  // create new tree and add initial configuration  $q$  in it
2: for iteration :=1: $I_{max}$  do
3:    $q_{rand} := \text{getRandomConfiguration}(C)$ 
4:    $q_{near} := \text{nearest node in tree } T \text{ to } q$ 
5:    $\text{expandTree}(q_{rand}, q_{near})$ 
6:    $d = \text{distance from tree } T \text{ to } q_{goal}$ 
7:   if  $d < d_{goal}$  then
8:      $P = \text{extract trajectory from } q_{start} \text{ to } q_{rand}$ 
9:     return  $P$ 
10:  end
11: end
12: return failure // no solution was found within  $I_{max}$  iterations

```

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**Algorithm 3.2**  $\text{expandTree}(q_{rand}, q_{near})$ : Expansion procedure of the RRT algorithm source [28]

**Input:** Random configuration  $q_{rand} \in C$ , configuration tree  $T$ , its nearest node in the tree  $q_{near} \in T$

**Output:** Extended tree  $T$

```

1:  $R = \emptyset$  // set of configurations reachable from  $q_{near}$  together with control inputs
2: foreach  $u \in U$  do
3:    $q = q_{near} + \int_0^{\Delta t} f(q_{near}, u) dt$ 
4:   if  $q$  is feasible then
5:      $R = R \cup \{(q, u)\}$ 
6:   end
7: end
8: if  $R \neq \emptyset$  then
9:    $(q_{new}, u) = \text{select a conuguration from } R \text{ closest to } q_{near};$ 
10:   $T.addNode(q_{new})$ 
11:   $T.addEdge(q_{near}, q_{new}, \Delta t, u)$ 
12: end

```

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guiding path during building the space-filling tree. Before running the RRT algorithm, the guiding path from  $q_{start}$  to  $q_{goal}$  is found and sampled. One of inputs to the RRT-Path algorithm is the probability  $p$  (*guided*). In the main loop of the algorithm, obtaining of the random configuration is modified. Instead of random configuration with uniform distribution, configuration around the  $q_i$  is selected with probability  $p$  (*guided*).

Let  $G$  be the guiding path and  $(q_{start}, q_1, q_2, \dots, q_{goal}) \in G$  the points of the guiding path, where  $q_i \in C_{free}$  and  $i \in (start, 1, 2, \dots, goal)$ . In the beginning,  $q_i := q_1$ , so random point is selected from the area around the point  $q_1$  with probability  $p$  (*guided*). When the leaves of the searching tree reach distance lower than  $r_{dist}$  to the  $q_i$ , then the next point of the guiding path will be used instead of  $q_i$ , so  $q_i := q_{i+1}$ . This continues until  $q_{goal}$  is reached, which means the RRT-Path algorithm ends.

### 3.3 Guiding path

The guiding path is obtained by transferring the map to a graph representation and then the path is found using the graph-search algorithms. The map can be transferred to graph representation by using the Voronoi diagram, a visibility graph or by discretization to a grid representation.

Then the path can be found by using Dijkstra algorithm or A\* algorithm. In this thesis, the A\* algorithm has been used because of its ability to find optimal path and easy calculation of heuristic function is Euclidean space.

The classic cost function of node  $q_i$  in A\* algorithm is  $f(q_i) = g(q_i) + h(q_i)$ . The  $g(q_i)$  is sum of costs of all edges in shortest path between nodes and  $q_{init}$  and  $q_i$ . The  $h(q_i)$  is heuristic estimate of distance between  $q_i$  and  $q_{goal}$ . In Euclidean space, it is calculated as  $h(q_i) = \|q_i - q_{goal}\|$ . This algorithm uses a modified cost function and in addition to a cost function of the A\* algorithm. The modified cost function is  $f(q_i) = g(q_i) + h(q_i) + j(q_i)$ , where  $j(q_i)$  is number representing the proximity to the nearest obstacle. For example, it can be  $j(q_i) = \frac{const}{\|q_i - nearest\ obstacle\|}$ , where  $const$  is weight of the  $j(q_i)$  and expresses how much obstacles should be avoided with respect to length of the whole path.

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CHAPTER  
**FOUR**

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## GROUPING OF GOALS FOR THE GUIDING PATH

During this processing of the map (method `MapProcessor::getEndNodes` in codebase) all AoIs are grouped to one big AoI, which is the smallest rectangle covering all AoIs.

If this modification is enabled, only one goal is used for all AoIs instead of one goal for every AoI (a node in the middle of AoI rectangle is considered to be the goal node). The whole swarm has only one guiding path, so the grouping prevents the swarm from splitting. The relative localization is the main reason to have only one big swarm instead of more smaller swarms (or individual UAVs in case of the same count of AoI and UAVs). Advantages of relative localization are more significant when we have only one big swarm.

Grouping of goals is done by finding the smallest rectangle containing all AoIs. Middle of this big rectangle is considered to be middle of the group of goals. When obstacle is in the middle, nearest node which is not obstacle is used as middle of goals group. The middle is used as target for guiding path.

This approach has the following advantage: when individual AoIs are near to a global goal of the whole group, as seen in 4.2, then the whole swarm follows one guiding path without any splitting, which makes the RRT-Path run faster and also the advantage of relative localization is included.

Maps with goals and obstacles are shown in figures 4.1 and 4.2. The goals are coloured green colour and obstacles grey.

The disadvantage of this method emerges when individual AoIs have a bigger distance from each other than can be covered by UAVs. Then this approach totally fails, because the goal of the RRT-Path, which is much faster than RRT, is very distant from AoIs, as can be seen in 4.1 and the main part of the path is found by RRT algorithm, which is slower.

Because of advantages of having only one swarm, all experiments in this thesis use grouping and all UAVs form one big swarm.

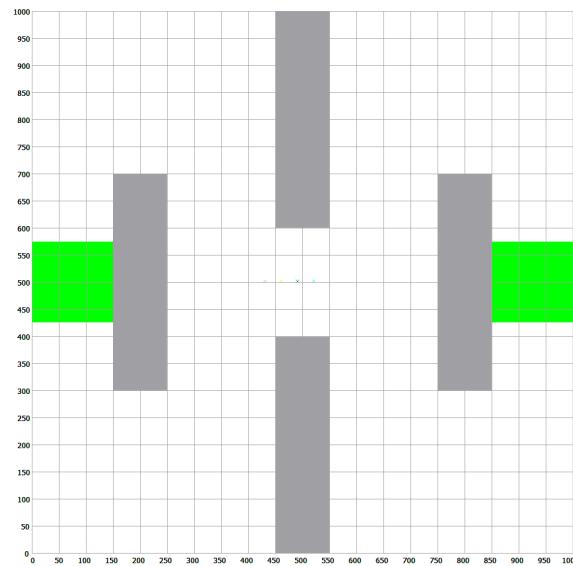


Figure 4.1: A map with the goals unsuitable for grouping

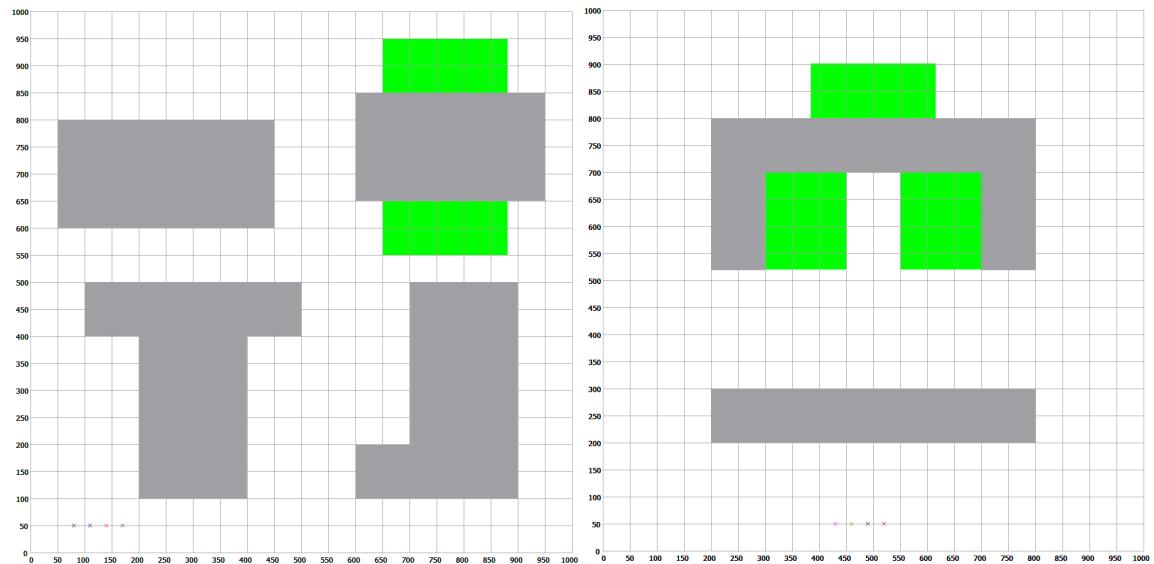


Figure 4.2: Maps with the goals suitable for grouping

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CHAPTER  
**FIVE**

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## AREAS OF INTEREST COVERAGE

Covering Areas of Interest (AoIs) with UAVs is key part of task of autonomous or cooperative surveillance. In task of surveillance, UAVs view space below them by on-board camera, as shown in figure 5.1. AoIs and areas seen by UAVs are represented by rectangles in this thesis for simplicity and fast computation.

Coverage of AoIs is optimization problem. This optimization problem can be solved by finding minimum of cost function. The value of cost function should objectively reflect the quality of coverage, the lower value should represent better coverage. In this thesis, cost function  $f(q_i)$  represents quality of coverage in configuration  $q_i$ , where configuration  $q_i$  is set of UAV positions. The cost function  $f$  in this thesis measures size of AoIs not covered by UAVs, which is equivalent to information not seen by UAVs. That means if  $f(q_1) < f(q_2)$  configuration  $q_1$  covers bigger part of AoIs than configuration  $q_2$ . The world  $W = R^2$  is discretized to square grid represented by matrix  $A \in R^2$ . One of parameters for coverage optimization is size of one square in grid  $a$  [map] units. Element  $A_{j,k}$  represents square with size  $a$  and left lower corner with coordinates  $[j \cdot a, k \cdot a]$ . Before computing areas seen by UAVs,  $A_{j,k} = A_{max}$  if it contains AoI, and  $A_{j,k} = 0$  otherwise.  $A_{max} = 100$  has been used in experiments, but the value is arbitrary. Then the

$$A_{j,k} := A_{j,k} \cdot l^m$$

formula is applied to every element of the world representing matrix  $A$ . Variable  $l$  must be in

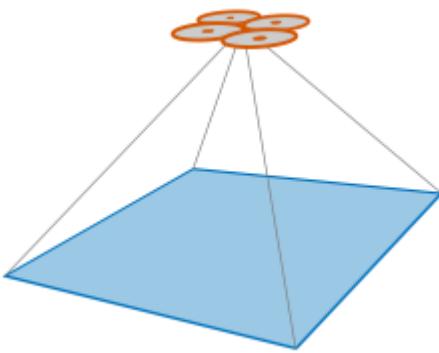


Figure 5.1: The area viewed by UAV on-board camera, source [11]

|   |   |   |   |   |   |   |   |     |     |     |     |     |     |     |     |     |     |   |   |   |
|---|---|---|---|---|---|---|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50  | 50  | 50  | 50  | 50  | 50  | 100 | 100 | 100 | 0   | 0 | 0 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50  | 50  | 50  | 50  | 50  | 50  | 100 | 100 | 100 | 0   | 0 | 0 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50  | 50  | 50  | 50  | 50  | 50  | 100 | 100 | 100 | 0   | 0 | 0 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50  | 50  | 50  | 50  | 50  | 50  | 100 | 100 | 100 | 0   | 0 | 0 |   |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0   | 0 | 0 | 0 |

Figure 5.2: AoI matrix with one UAV, source [11]

range  $1 > l > 0$  and represents amount of information not seen by UAV even if this UAV covers the element  $A_{j,k}$ . This is because quality of image obtained from on-board camera depends on many factors, such as time of day, weather conditions, flight altitude, camera chip resolution, lens parameters, stabilization, frame rate and so on. In this implementation,  $l = 0.5$ , but if the flight altitude will be considered in the optimization algorithm, higher flight altitude would lead worse image recording, so  $l(\text{flightAltitude}_1) > l(\text{flightAltitude}_2)$  for  $\text{flightAltitude}_1 > \text{flightAltitude}_2$ . Variable  $m \in N_0$  represents number of UAVs seeing the area of element  $A_{j,k}$ . Example can be seen in figure 5.2. AoI is marked with green colour and UAV is marked with blue colour. As we can see, parts of AoI not seen by an UAV have value  $A_{j,k} = A_{\max} = 100$  and parts of AoI seen by UAV have value  $A_{j,k} = A_{\max} \cdot l^m = 100 \cdot 0.5^1 = 50$ .

When UAV arrives above any AoI, the RRT-Path algorithm ends for this UAV and instead of it, RRT algorithm takes place. Random node for RRT algorithm is selected only from AoI beneath the UAV, not from whole world. When all UAVs arrive to their goal by the RRT-Path algorithm, RRT algorithm is run and it runs until being stopped. After stopping, all states found by RRT algorithm where UAVs are above AoIs, are gathered and their coverage cost function is calculated. State with lowest cost function is used as result of the path finding algorithm and used as input for Dubins curves optimization.

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CHAPTER  
**SIX**

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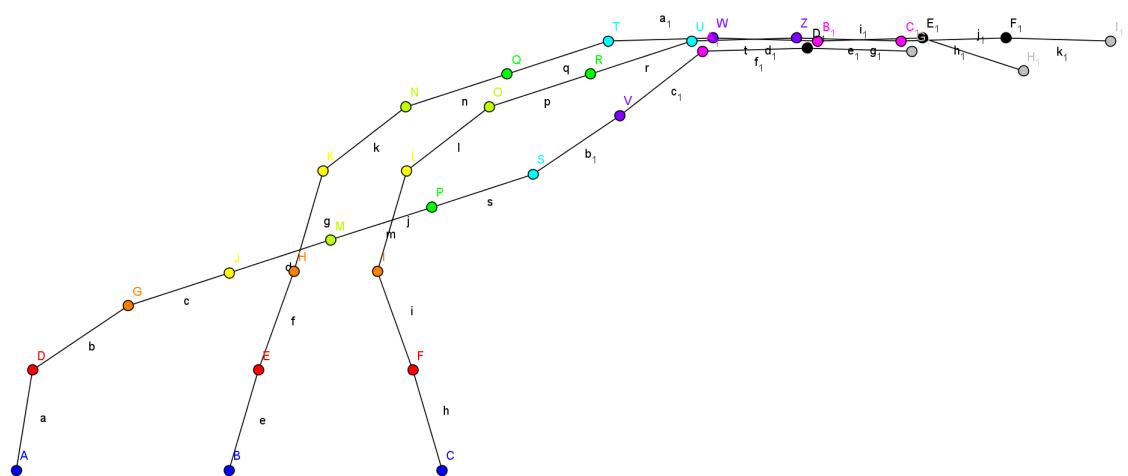
## PATHS STRAIGHTENING

In the RRT-Path algorithm, crossing paths between neighbouring states are checked, so no trajectories are crossing each other between the  $n$ -th state and the  $n + 1$ -th state, but this does not solve the problem completely. In figure 6.1 trajectories found by the RRT-Path algorithm are shown. Every colour marks one state in a RRT-Path. As we can see, check in algorithm prevents from crossing path between neighbouring states, but crossing of paths in different times can not be easily prevented. We can see in image, that paths cross between points J (yellow), M (light green) and H (orange), K (yellow), so there is no easy approach to prevent path collisions between  $n - 2$ -th state and  $n$ -th state. Optimization by Dubins curves shortens trajectory of UAVs, so UAVs could be in these trajectories in different time. Considering that, there could be collisions after optimization. Another complication occurs, when time difference between two states is too low, then UAVs could collide, because in reality UAV can not follow path precisely, but only with some errors.

There were attempts to straighten crossing trajectories, but all of them failed. Straightening was done by switching parts of crossing paths from the earliest crossing state to the end. But then lengths of paths differed, which was unsuitable for path planning for a swarm. This can be done by adding “waiting” points, points in different state but with the same position in different time. Due to these facts, it was really complicated to straighten a longer path with many crossings (this path is really short, paths in other maps are much longer and more complicated). Motion model with inertia is unable to stop immediately in one place, so path waiting states is hard to follow precisely. This fact complicates following the straightened trajectories. Due to all complications mentioned above, this part was removed from algorithm. But it is possible to add it, when better approach will be found.

todo: větší písma u obrázku

Figure 6.1: Crossing paths



## UAV SWARM PROPERTIES

### 7.1 Motion model

The RRT-Path algorithm is universal and works with any motion model, which allows us to find paths feasible for swarm of UAVs. For this purpose, car-like model was chosen. Car like model is very fast to compute and can be computed analytically. Differential equations of motion model in 3D from [?] are

$$\begin{aligned}\dot{x}(t) &= v(t) \sin \varphi(t) \\ \dot{y}(t) &= v(t) \cos \varphi(t) \\ \dot{z}(t) &= w(t) \\ \dot{\varphi}(t) &= K(t) v(t)\end{aligned}\tag{7.1}$$

where  $x(t), y(t), z(t)$  are coordinates of UAV,  $\varphi(t)$  represents heading of UAV,  $v(t)$  is forward velocity,  $K(t)$  is curvature,  $w(t)$  is ascent velocity. Vector  $[K(t) \ w(t) \ v(t)]$  represent the input vector of motion model. Differential equations are readable and useful for representation in equations, but they are not so useful for computer algorithm due to time consumption. Difference equations are better for usage in algorithm instead of differential equations because they are much faster and scalable. When inputs are held constant in each time interval between two time steps, difference equations are

$$\begin{aligned}x(k+1) &= \begin{cases} x(k) + \frac{1}{K(k+1)} (\sin(\varphi(k) + K(k+1)v(k+1)\Delta t(k+1)) - \sin(\varphi(k))) \\ \text{if } K(k+1) \neq 0 \\ x(k) + v(k+1) \cos(\varphi(k)) \Delta t(k+1) \\ \text{if } K(k+1) = 0 \end{cases} \\ y(k+1) &= \begin{cases} y(k) - \frac{1}{K(k+1)} (\cos(\varphi(k) + K(k+1)v(k+1)\Delta t(k+1)) - \cos(\varphi(k))) \\ \text{if } K(k+1) \neq 0 \\ y(k) + v(k+1) \sin(\varphi(k)) \Delta t(k+1) \\ \text{if } K(k+1) = 0 \end{cases} \\ z(k+1) &= z(k) + w(k+1) \Delta t(k+1) \\ \varphi(k+1) &= \varphi(k) + K(k+1)v(k+1)\Delta t(k+1)\end{cases}\tag{7.2}$$

## 7.2 Relative localization

When swarm consists of only one UAV, no relative localization is needed. But when more UAVS are in swarm, every UAV has to be aware of its neighbours in order to remain together in one swarm. In this thesis, relative localization is implemented by setting the minimal distance  $d_{min}$  and maximal distance  $d_{max}$ . The minimal distance is set because UAV push air beneath them when they fly. UAVs in the Multi-Robot Systems group at CTU have weight around 3 kg, which means 3 kg of air needs to be pushed below UAV in order to keep it flying. Because of this, UAVs can not fly too close to each other because of air currents they produce. The minimal distance is minimal distance in which UAVs do not affect each other by air currents. In last measurements, the minimal distance was 2 meters. The maximal distance needs to be set because of sensors range. UAVs in the Multi-Robot Systems group at CTU use on-board camera based localization system, published in [3]. Sensors have maximal range and UAVs in bigger distance than this maximal range can not be seen. In experiments, the maximal distance was 5 meters.

In configuration of whole algorithm, number of neighbours  $n$  is set. Every UAV must have  $n$  or more neighbours in distance  $d$ , where  $d_{min} < d < d_{max}$  in every step of configuration. Default setting is  $n = 2$ . Computation of this relative localization is fast, but unusable for more than 5 UAVs. Swarm of 6 or more UAVs can split to 2 or more groups and still fit this relative localization constraint. The only solution to check whether all UAVs are in same swarm can be obtained by using following algorithm, which consists of two steps and uses graph representation. Every UAV is node and every pair of UAVs with distance  $d$ , where  $d_{min} < d < d_{max}$  are connected by an edge. If the graph has only one connected component, all UAVs are in one swarm. Otherwise, the graph has more connected components, which implies UAVs are split into more swarms.

In the first step, the adjacency matrix  $A$  is built. Each UAV represents one column and one row in this matrix. The adjacency matrix  $A$  is built by following pattern.

$$A_{i,j} = \begin{cases} 1 & \text{if } d_{min} < d_{i,j} < d_{max} \\ 0 & \text{otherwise} \end{cases}$$

where  $i, j$  are indices of matrix  $A$  and  $d_{i,j}$  is distance between  $i$ -th and  $j$ -th UAV. In the second step, the graph represented by  $A$  is traversed by depth-first algorithm, starting at  $A_{1,1}$ . When all nodes are visited during the traversing, the graph has only one connected component and all UAVs are in one swarm. In configuration can be set whether swarm splitting is enabled or not.

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CHAPTER  
**EIGHT**

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## DUBINS CURVES

Dubins curves, also called Dubins manoeuvres or Dubins path were published by Lester Eli Dubins in 1957 [2]. Dubins path is optimal path for car-like motion model. Path is optimal, when car moves at constant forward speed. The other important constraint is the maximum steering angle  $\phi_{max}$ , which results in a minimum turning radius  $\rho_{min}$ . As the car travels, consider the length of the curve in  $\mathcal{W} = \mathbb{R}^2$  traced out by a pencil attached to the centre of the car. The task is to minimize the length of this curve as the car travels between any  $q_I$  and  $q_G$ . Due to  $\rho_{min}$ , this can be considered as a bounded-curvature shortest-path problem. If  $\rho_{min} = 0$ , then there is no curvature bound, and the shortest path follows a straight line in  $\mathbb{R}^2$ . In terms of a cost function, the criterion to optimize is

$$L(\tilde{q}, \tilde{u}) = \int_0^{t_F} \sqrt{\dot{x}(t)^2 + \dot{y}(t)^2} dt \quad (8.1)$$

, where  $t_F$  is the time at which  $q_G$  is reached, and a configuration is denoted as  $q = (x, y, \theta)$ ,  $\tilde{x}_t$  denotes the function  $\tilde{x}_t : [0, t] \rightarrow X$ , which is called the state trajectory (or state history). This is a continuous-time version of the state history, which was defined previously for problems that have discrete stages. Similarly,  $\tilde{u}_t$  denotes the action trajectory (or action history),. If  $q_G$  is not reached, then it is assumed that  $L(\tilde{q}, \tilde{u}) = \infty$ . [8]

When considering constraints of inputs (actions) for motion model, the system can be simplified to

$$\begin{aligned} \dot{x} &= \cos \theta \\ \dot{y} &= \sin \theta \\ \dot{\theta} &= u \end{aligned} \quad (8.2)$$

in which  $u$  is chosen from the interval  $U = \{-\tan \phi_{max}, 0, \tan \phi_{max}\}$ . For simplicity, assume that  $\tan \phi = 1$ . The following results also hold for any  $\phi_{max} \in (0, \pi/2)$ .

It was shown in [2] that between any two configurations, the shortest path for the Dubins car can always be expressed as a combination of no more than three motion primitives. Each motion primitive applies a constant action over an interval of time. Furthermore, the only actions that are needed to traverse the shortest paths are  $u \in \{-1, 0, 1\}$ . The primitives and their associated symbols are shown in 8.1. The *S* primitive drives the car straight ahead. The *L* and *R* primitives turn as sharply as possible to the left and right, respectively. Using these symbols, each possible kind of shortest path can be designated as a sequence of three symbols that corresponds to the

Table 8.1: The three motion primitives from which all optimal curves for the Dubins car can be constructed.

| Symbol | Steering u |
|--------|------------|
| L      | -1         |
| S      | 0          |
| R      | 1          |

order in which the primitives are applied. Let such a sequence be called a word . There is no need to have two consecutive primitives of the same kind because they can be merged into one. Under this observation, ten possible words of length three are possible. Dubins showed that only these six words are possibly optimal:

$$\{LRL, RLR, LSL, LSR, RSL, RSR\}. \quad (8.3)$$

The shortest path between any two configurations can always be characterized by one of these words. These are called the Dubins curves.

## 8.1 Optimization using Dubins curves

Because of the fact that Dubins curves provide us optimal trajectory, they can be used to optimize trajectory found with the RRT-Path algorithm.

For only one UAV, the situation is quite simple and optimization works as follows.

Two random points of trajectory are chosen and Dubins curves are calculated between them. If calculated curves do not collide with the obstacles, they are used instead of original trajectory between chosen points. This points choosing and trajectory replacing is repeated until the whole trajectory can not be shortened more and thus is optimal.

In a real situation, we do not know whether found trajectory is optimal or not, so we need to determine conditions for stopping the optimization. The optimization is stopped if the trajectory is not shortened after many (e. g. 150) iterations or optimization is too slow and trajectory is shortened only by small distances (e. g. shortening by 5% per 1000 iterations).

But in a swarm, the situation is complicated because of relative localization and minimal and maximal distances between individual UAVs.

So the algorithm must be modified. Dubins curves must be sampled with same frequency as the rest of trajectory (this is frequency of the RRT-Path algorithm or higher frequency when a trajectory is being re-sampled) and each point has to be validated for feasibility in terms of minimal and maximal distance from another UAVs. So the curves can be used only when all trajectories between minimal and maximal distance of relative localization.

Due to using random points during optimization, the optimization is stochastic and non-deterministic.

### 8.1.1 One UAV demonstration

In 8.1 we have trajectory of one UAV found by the RRT-Path algorithm in map with one obstacle marked by a dark grey rectangle. Obstacle amplification is marked by a light grey rectangle. In 8.2 we can see optimal trajectory found using Dubins curves. The resulting trajectory consists

Figure 8.1: One UAV before Dubins curves optimization

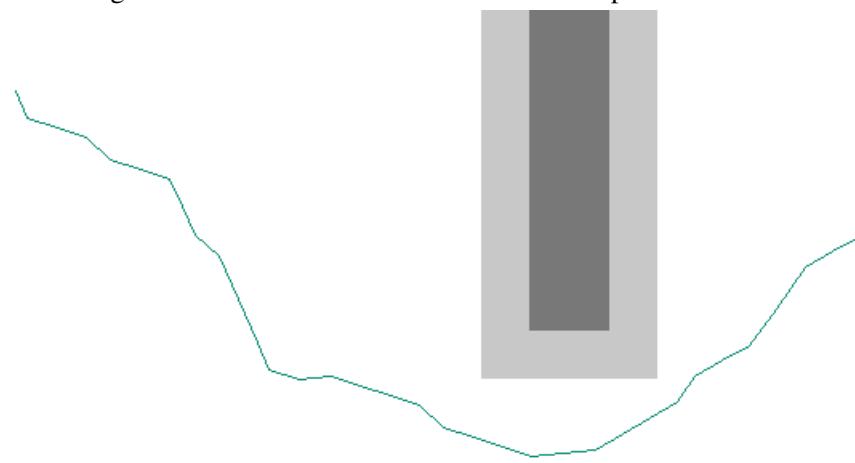
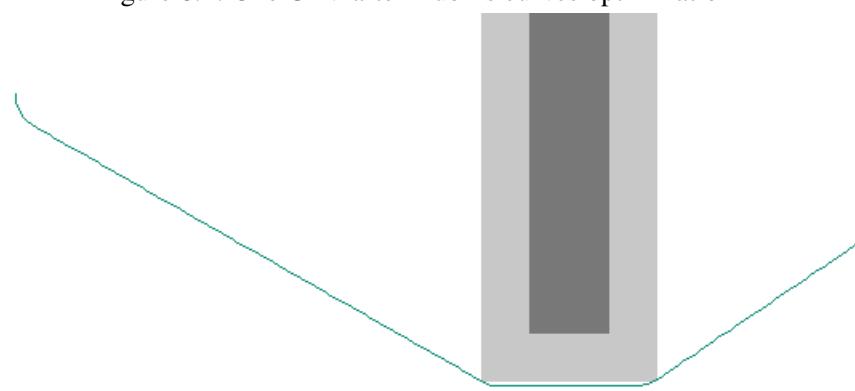


Figure 8.2: One UAV after Dubins curves optimization



of many Dubins curves and it was obtained by algorithm mentioned above. Random points have been replaced by Dubins curves and after many iterations, an optimal trajectory was found.

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CHAPTER  
**NINE**

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## TRAJECTORY RE-SAMPLING

Motion model in the RRT-Path algorithm uses constant input in range from 0.5 to 1 second. Smaller interval for constant input causes RRT-Path algorithm to run for too long. When using too short constant input interval, the tree has too many nodes, grows slowly and runs out of memory much faster than longer interval. An interval longer than 1 second makes UAVs unable to manoeuvre between smaller obstacles. Thus range from 0.5 to 1 second was experimentally chosen as best interval. Using  $x$  seconds long constant input interval also means  $\frac{1}{x} \text{Hz}$  frequency of points in resulting trajectory in the output of the algorithm. So the range from 0.5 to 1 second implies resulting frequency is in range 1Hz to 2Hz.

Real UAVs in Multi-Robot Systems group at CTU use frequency 70Hz for providing target points to UAVs and trajectories with lower frequency are linear interpolated to have frequency 70Hz. That means frequency 2Hz is too low for real usage because a trajectory generated with this frequency would not be smooth enough.

Change of frequency before the RRT-Path algorithm makes the algorithm unable to run efficiently in bigger maps, so this approach does not solve the problem.

Another solution is to re-sample the trajectory after Dubins curves. But this method failed because after Dubins optimization, the curves had different length and different constant input durations.

The best solution for this issue is re-sampling of trajectory generated by RRT-Path algorithm before it is optimized by Dubins curves. This solution also has big advantage in Dubins curves optimization because it results in shorter final trajectory as will be shown in the experiments in the chapter 13.

## COVERING MORE AOIS WITH ONE SWARM

Some maps have distribution of obstacles and AoIs where algorithm stated above fails. These maps can be seen in figure 10.1. Standard algorithm which uses only one guiding path always leads swarm to only one Area of Interest and the second area remains completely uncovered.

In case of using relative localization where every UAV needs only 1 to 2 neighbours, UAVs can create chain and reach to more distant targets or targets divided by obstacles which UAVs can not reach when moving as one swarm using standard RRT-Path algorithm.

Following modifications must be done if we want to cover all AoIs in figure 10.1.

UAVs are split to two groups, and every group has its own guiding path to one AoI. Relative localization keeps all UAVs in one swarm by its constraints described in section 7.2. With this setting, the swarm behaves like chain, because it is “pulled” to opposite sides by different guiding paths, but it is also connected by relative localization, so it does not split into more smaller swarms. Successful coverage by using the chain behaviour can be seen in figure 10.2.

Unfortunately, this approach does not work in all maps and configurations as can be seen in figure 10.3. The map on the right shows typical example of getting stuck in local minimum, where all UAVs preferred covering only one AoI over covering both AoIs, but the map on the left shows different issue. When we have symmetric map and UAVs do not have starting position in middle of this map, one side of the chain needs to be “pulled” with more power than the other side to cover both AoIs and encircle the obstacle between UAVs starting position and AoIs. This leads to configuration where only one side of chain covers AoI and the other side of chain does not reach the second AoI. This bigger pulling power, which would probably solve this issue, can not be simulated in RRT-Path algorithm. These problems demonstrates the fact this approach is not robust and needs manual preprocessing of UAVs starting positions. The limitation of this approach is also the fact it works only for two AoIs.

### 10.1 Proposition of improvement of the algorithm

This approach could be modified to be more robust and usable in more maps with more than 2 AoIs. Generalization of this approach would require not creating a chain, which is good only for covering two AoIs, but tree structure, where each leaf covers one AoI. I will now propose principle of the generalized algorithm.

In the first step, we need to decide, which AoIs can be covered by swarm. Some maps can have distant AoIs where all AoIs could not be covered at the same time. This requires finding shortest

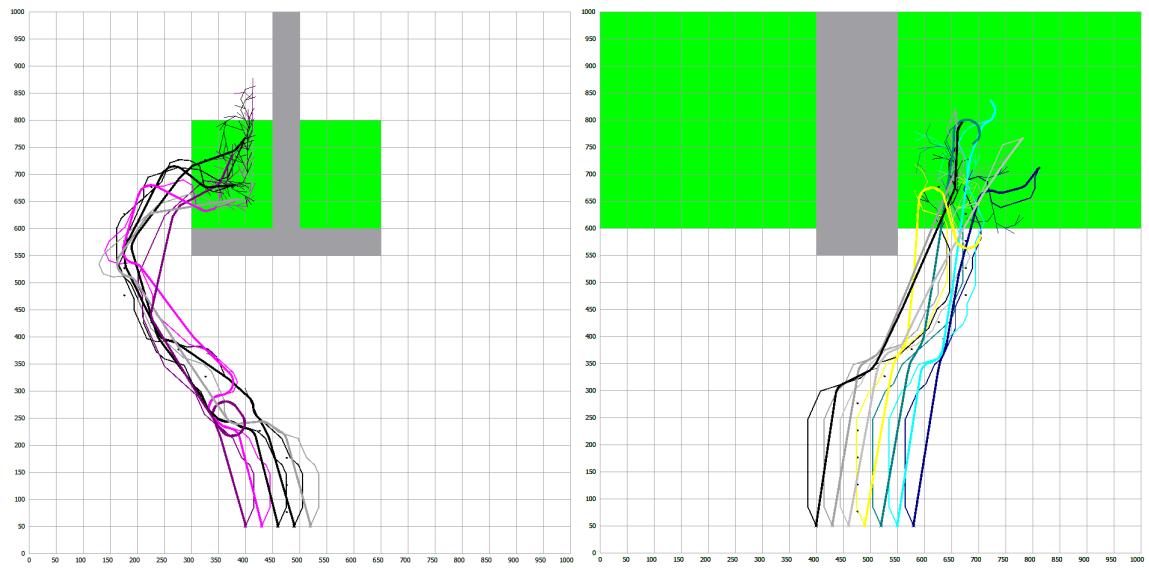


Figure 10.1: Maps with only one covered Area of Interest

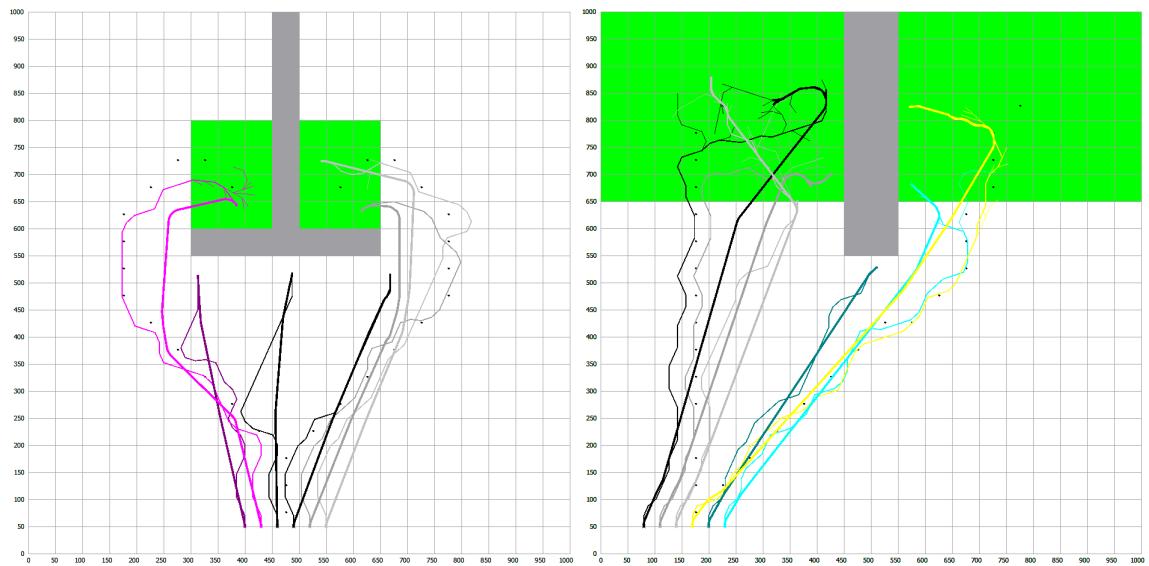


Figure 10.2: Maps with successful chaining behaviour

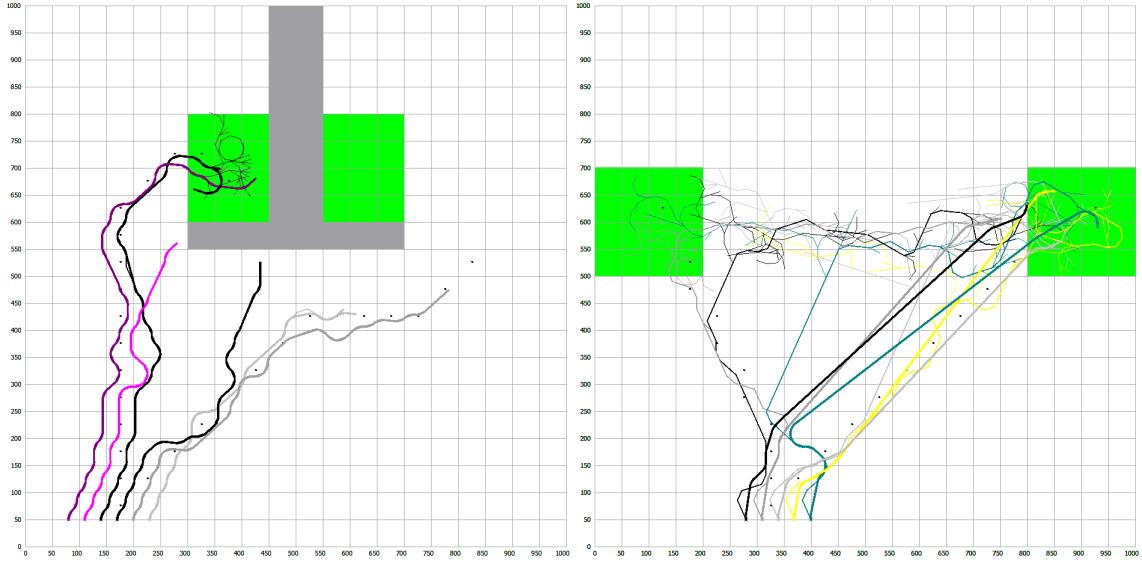


Figure 10.3: Maps with unsuccessful chaining behaviour

tree  $T$  which connects middles of all AoIs. When sum of all edges in this tree  $d_{total}$  is bigger than  $d_{max} = (\text{number of uavs} - 1) \cdot \text{maximal distance between neighbouring uavs}$ , which is maximal length of chain created by UAVs, some AoI and branch leading to its middle will be excluded. This results in shortening the value  $d_{total}$ . This process will be repeated while  $d_{total}$  will be bigger than maximal  $d_{max}$ . When  $d_{total} < d_{max}$ , we obtain set of AoIs which can be covered by swarm of UAVs. In the next step, UAVs will be split to multiple groups, one group for each AoI. Then the guiding paths will be planned for each groups to reach corresponding branches of  $T$ . Then the RRT-Path algorithm will take place. The final step will be optimization by Dubins curves, described in this thesis.

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CHAPTER  
**ELEVEN**

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## V-REP SIMULATIONS

V-REP is an acronym for Virtual robot experimentation platform, a simulator developed by Coppelia Robotics, providing an advanced environment for testing and simulations of robots of all types. The V-REP environment is free and open-source for educational purposes and also has commercial licence. The environment takes in account certain physical laws like gravity, inertia or friction, which enables to truthfully verify applicability for deployment of UAVs in the real world. V-REP has many build-in models, but user can also create his own robot. V-REP enables to control robots over API and has API clients for C, C++, Python, Java, Lua, Matlab, Octave and Urbi.

### 11.1 UAV control and trajectory simulation

Python is convenient for fast prototyping and has native functions for easy JSON parsing, which made it good choice for simulations of generated trajectories in V-REP.

UAVs in V-REP can be controlled over remote API only by changing location of their target. Then UAV tries to reach the location of its target. Unfortunately, UAVs only follow location, with speed proportional to distance. UAVs do not try to reach target and simultaneously to have zero speed when reaching their target, which causes overshoot. This fact leads to another disadvantage of UAV controller. When keeping target in same distance and direction from UAV, the UAV increases its speed, which causes overshoot when target changes its direction to UAV. These overshoots were many times bigger than size of UAVs, so they could not be ignored and had to be fixed.

During first, naive implementation, position of next state was set as target position for UAV, but due to overshoot and large distances between states UAVs failed to follow the trajectory.

Another implementation uses linear interpolated trajectory between UAV and its next state position. The calculated target is placed in the line between UAV and next state position, in the constant distance to UAV.

So the calculation was defined as follows

$$\mathbf{X}(k+1)_{target} = \mathbf{X}(k)_{UAV} + \frac{(\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV})}{\|\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV}\|} \cdot const$$

where  $\mathbf{X}(k)_{UAV}$  is UAV position in  $k$ -th iteration of simulation,  $\mathbf{X}(k)_{ns}$  is position of next state in planned trajectory in  $k$ -th iteration,  $\mathbf{X}(k+1)_{target}$  is position of UAV target in  $k+1$ -th

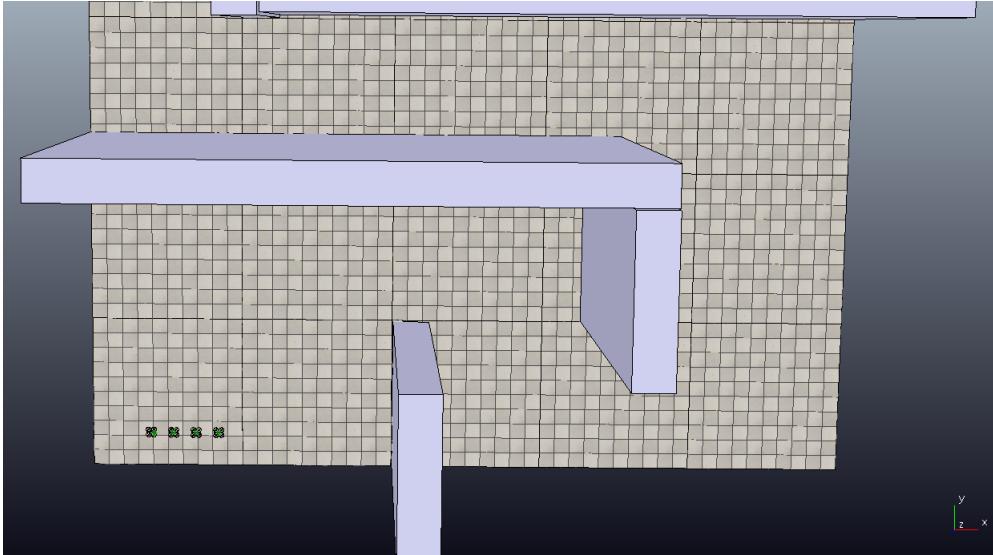


Figure 11.1: Map with UAV overshoot

iteration and  $const$  is constant experimentally tuned, so the UAV does not move too fast nor too slow. Too fast movements cause overshoot and too slow movements cause the simulation to run for needlessly long time.

But as mentioned earlier, even this approach did not go well. In long passages, where trajectory did not turn, UAVs increased their velocity and inertia, which made them harder to turn. The problem of overshooting is shown in figures 11.1 and 11.2. Overshoot is at the end of long passage in the map 11.1. Red and violet balls represent positions of next states and green balls represent UAV targets. In the first image, we can see UAVs leaving the narrow passage. As you can see in second and third image, positions of next state are still, but because of constant distance of target and UAV, the target is dragged by UAVs inertia.

This has been fixed by not updating the position of the target when distance between UAV and next state is bigger than in previous iteration and the position of next state is still the same, so the equation describing target position is

$$\mathbf{X}(k+1)_{target} = \begin{cases} \mathbf{X}(k)_{UAV} + \frac{(\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV})}{\|\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV}\|} \cdot const \\ \text{if } \|\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV}\| < \|\mathbf{X}(k-1)_{ns} - \mathbf{X}(k-1)_{UAV}\| \\ \wedge \mathbf{X}(k)_{ns} = \mathbf{X}(k-1)_{ns} \\ \mathbf{X}(k)_{target} \\ \text{else} \end{cases}$$

. This prevents the target from dragging by UAV with big inertia.

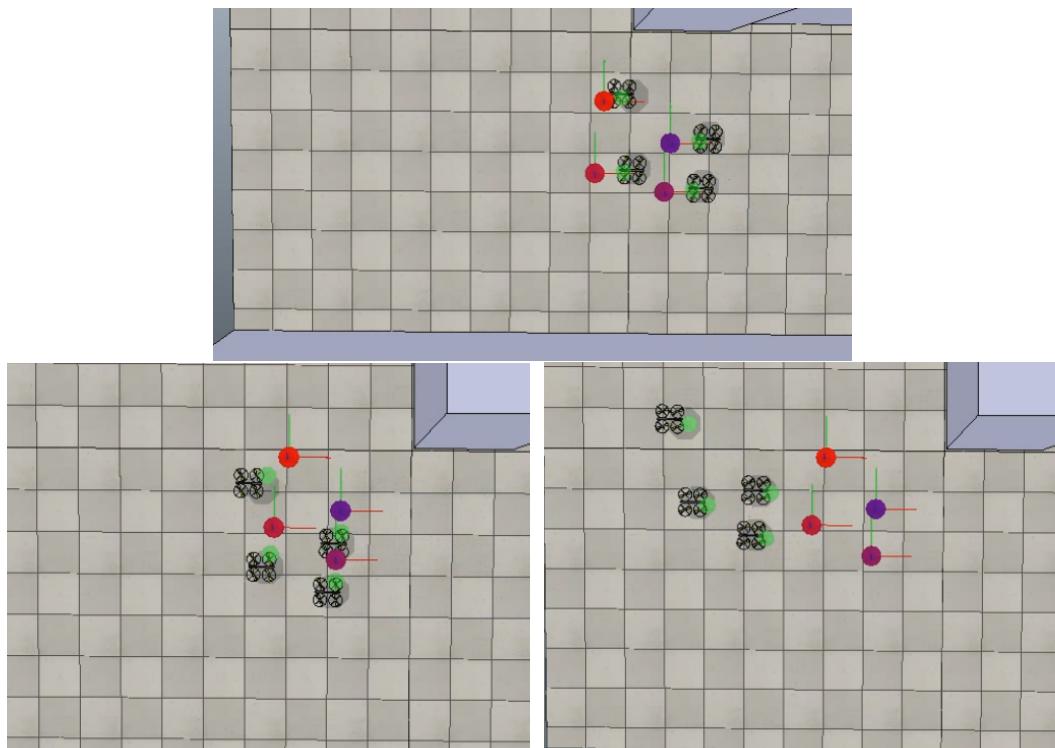


Figure 11.2: UAV overshoot

Here can be seen 3 iterations. Next state is changed during

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CHAPTER  
**TWELVE**

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## IMPLEMENTATION

This part will cover implementation of the algorithm, which was used for simulations. Whole codebase in C++ can be found at this github repository. Apart from the C++ program, I also created some CLI scripts in PHP, for drawing map and trajectories from the JSON representation, batch running of Dubins curves optimization and concatenation of the experiment results before plotting them in Matlab. These can be seen at this github repository. V-REP simulations were made by communicating with V-REP through remote API, the client is written in Python and can be seen here. Trajectories are persisted in JSON format. JSON is more compact than XML and can be easily parsed by all widely used programming languages. Trajectories are also persisted to CSV format, so they can be loaded to MATLAB and then into real UAVs.

### 12.1 External libraries

Some external libraries are used in the implementation. Every used library is mentioned here. Boost libraries are used for smart pointers, libraries for Dubins curves are from Master Thesis by Petr Váňa [24]. Generating of JSON from C++ object is done via Json Spirit library. Another external library is V-Collide from The University of North Carolina at Chapel Hill.

Because V-Collide sources were written in 1997 and because I used C++11 compiler to compile my source codes, I had to rewrite part of this library for compatibility and to make public API easier to use. Modifications can be seen in this github repository.

Last used external library is QT, which was used to create platform independent GUI.

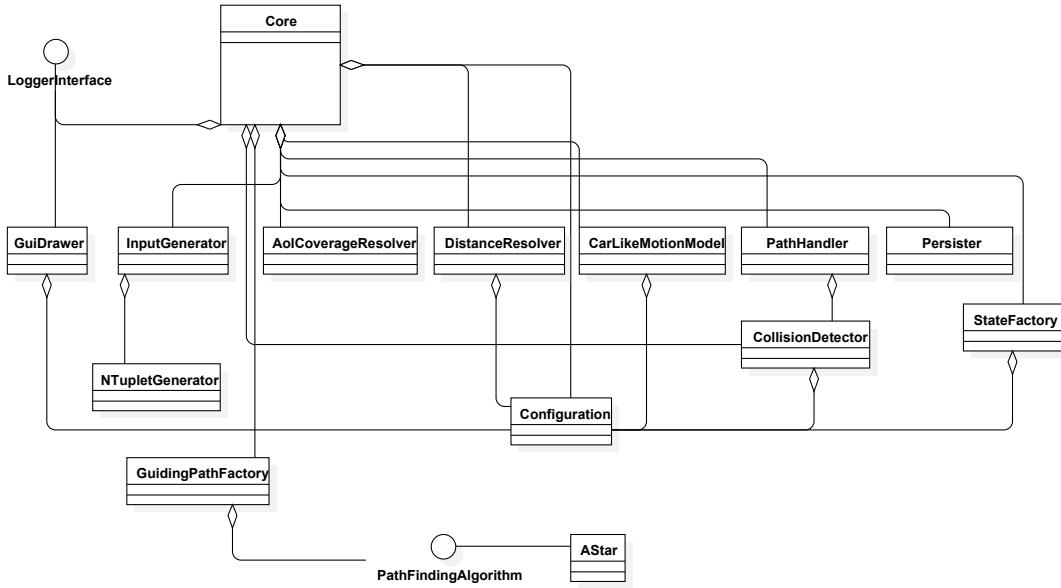
### 12.2 Code structure and services

Here is shown brief UML scheme demonstrating dependency diagram of codebase. To keep diagram simple, only services are displayed, other classes, which are not services, were left out for readability. Diagram was generated using software StarUML

Core class holds core of whole Application and has all other classes as dependencies, as is shown in the image 12.1.

As mentioned in the chapter 2, Configuration is DTO for all configuration variables, but to keep reasonable amount of classes, Configuration is also service, which delegates all configuration changes from GUI to Core class. Configuration and GuiDrawer implementation LoggerInterface are the only connections between Core and GUI.

Figure 12.1: Dependency diagram



State factory creates State classes according to Factory pattern. State class represents state in RRT-Path algorithm. State has coordinates and rotations for all UAVs. Persister persists found trajectories to JSON using Json Spirit library. PathHandler serves as utils class for manipulations with trajectories (vector of State classes). CarLikeMotionModel holds motion model algorithm. InputGenerator is used to generate inputs to motion model. NTupletGenerator only generates variation with repeating for given input. DistanceResolver counts distances between two states and length of trajectory. AoICoverageResolver determines cost function for states, where all UAVs are in AoIs. GuidingPathFactory is wrapper for PathFindingAlgorithm interface and is used by Core to find guiding path. Implementation of PathFindingAlgorithm is AStart class.

## 12.3 Utility scripts

All graphs in experiments with re-sampling and Dubins optimization were generated with usage of PHP scripts. Script runDubinsOptimization.php runs sequentially resampling with given frequencies multiple times. This script can be run many times at once with different configuration, which brings advantage of parallel run without need to deals with threads. Script processDubinsOptimizationData.php merges all CSV result files to one big matrix, with number of rows equal to maximal number of iterations and number of columns equal number of runs of the optimization. For example, as seen in experiment 13.2.1 for frequency 1 Hz it is matrix with size 2095x100. This can be loaded directly to matlab so the graph can be generated. Script drawPaths.php generates map to png image. E. g. map generated by this script can be seen in 13.4.

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CHAPTER  
**THIRTEEN**

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## EXPERIMENTS

### 13.1 RRT-Path

In this experiment, a trajectory in a map shown in the figure 13.1, is searched by using the RRT-Path algorithm. As we can see, the map is quite complex and has many obstacles. UAVs start in the lower left corner. In this figure, we can also see the trajectory found by RRT-Path algorithm. The algorithm follows the guiding path quite precisely, and whole searching tree for each UAV looks like one long branch. Only the AoI is covered by branches of searching trees. The algorithm is run 1000 times. The algorithm found the trajectory to AoI in every run. The results can be seen in the figures 13.2 and 13.3, where can be seen mean value and standard deviation in each iteration of all 1000 runs. In the graph 13.3 we can see total distance between current position of UAVs and their final position above AoI. As we can see, in the beginning, the UAVs are very distant from AoI, but they get closer to goal and try to minimize the distance. The increase of distance to goal corresponds with obstacles avoidance. The graph 13.2, describes distance to nearest neighbour. This experiment has been run with 3 UAVs. In every iteration of the algorithm, each UAV has some nearest neighbour. Distances between the UAV and its nearest neighbour is shown in the graph. This information is important for the relative localization. The minimal and maximal distance are 24 and 180 map units, in this experiment. During the whole flight, UAVs fly really close to each other. But in the end, they fly away from each other, because they can cover bigger part of AoI when they have bigger distance between each other.

### 13.2 Influence of re-sampling on Dubins curves optimization

To demonstrate the optimization, few maps were selected to be used in re-sampling and optimization experiments. The RRT-Path algorithm found trajectories for UAVs. These trajectories were re-sampled and optimized 100 times to obtain relevant results because of using random numbers during the optimization and avoiding getting stuck in local optima.

Due to time and memory consumption, each optimization is stopped after 200 iterations where optimization did not shorten the trajectory or when speed of trajectory shortening was slower than 5% of original trajectory length per 1000 iterations.

The algorithm also stops when consumed memory exceeds 1900 MB. This is right before shutting of program by operating system, because 32bit processes are not allowed to use more than 2 GB of RAM. This feature was implemented using an ugly platform-dependent hack.

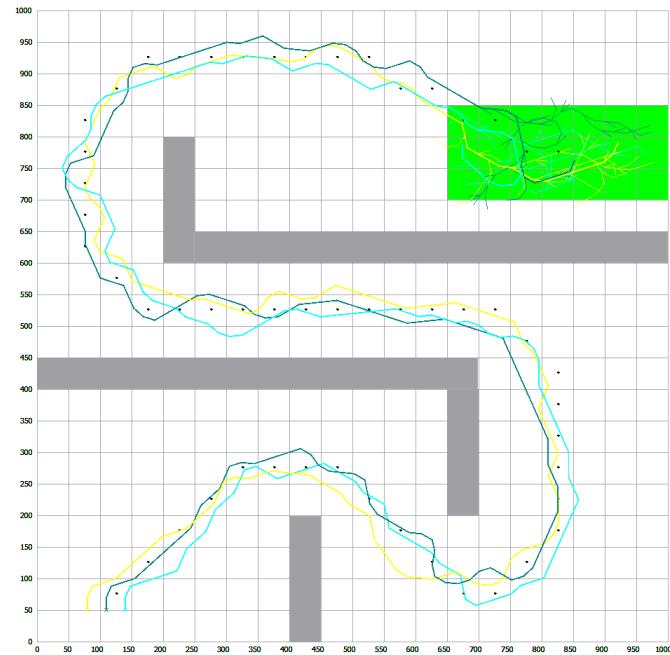


Figure 13.1: Map used for experiment

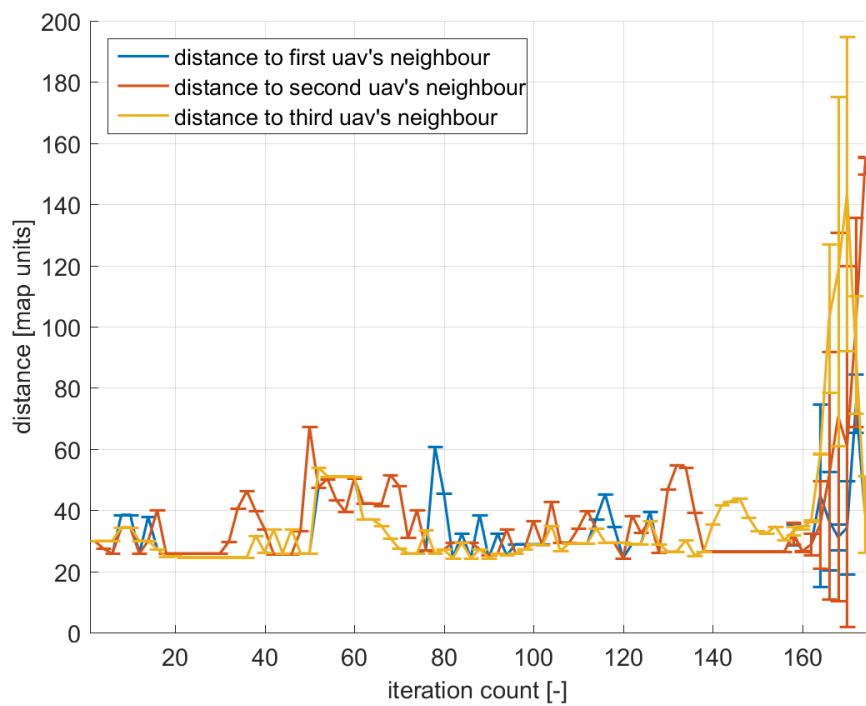


Figure 13.2: Distances between nearest UAVs in swarm and distance to AoI

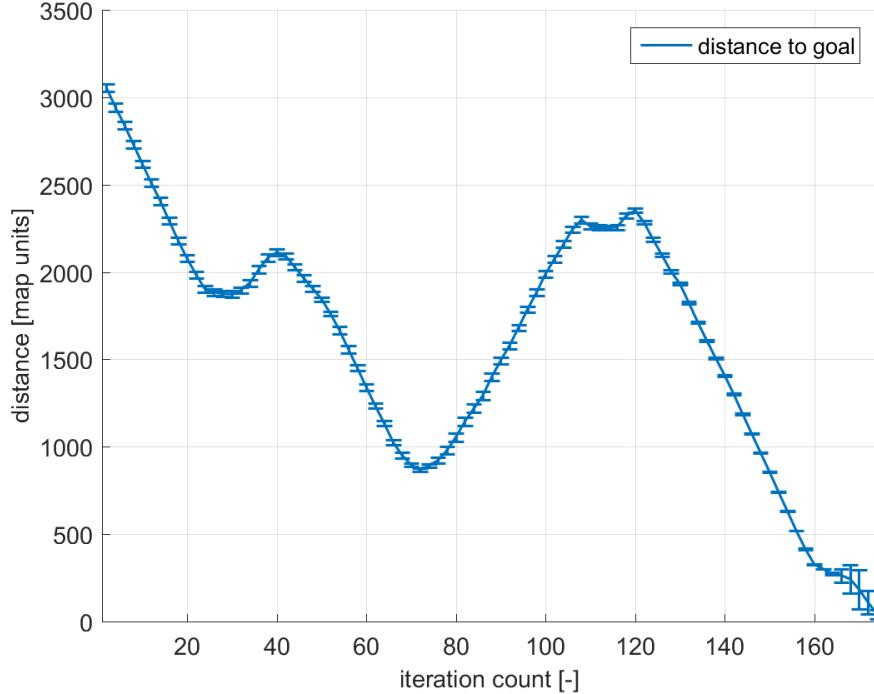


Figure 13.3: Distance between UAVs ans AoI

In next sections, maps with obstacles, AoIs and trajectories will be shown. Obstacles are grey rectangles, AoI is green rectangle and each UAV has trajectory marked with different colour. For measuring of influence of re-sampling of trajectory to Dubins curves optimization, following frequencies were selected: 1 Hz (initial frequency used in RRT-Path algorithm), 2 Hz, 4 Hz, 6 Hz, 8 Hz, 10 Hz, 12 Hz, 14 Hz, 16 Hz, 18 Hz, 20 Hz.

### 13.2.1 First experiment

The map with trajectories found by the RRT-Path algorithm can be seen in 13.4.

The best result of Dubins curves optimization (re-sampling of 20Hz) is shown in 13.5. As we can see, trajectories are much shorter than trajectories before optimization in 13.4. At the beginning of trajectories, in the left upper corner of the picture, we can see much smoother curves than before optimization. This is due to re-sampling to frequency 20Hz, which smooths trajectories.

In real flight, it is undesirable to have trajectories close to obstacles, so obstacles are amplified before optimization. This can be seen in 13.5 where UAVs keep certain distance from the obstacles.

The following table shows average total, minimal and maximal distance of all trajectories from 100 optimizations after the re-sampling and optimization.

The results are also shown in graph 13.6. In the graph we can see that the initial frequency 1 Hz has worst results and the frequency 20 Hz has the best results. We can also see that in frequency 14 Hz and higher, all 100 iterations had same results, the minimum, maximum and mean value are the same. But the second best frequency in terms of minimal, maximal and mean

Figure 13.4: Trajectory before Dubins curves optimization

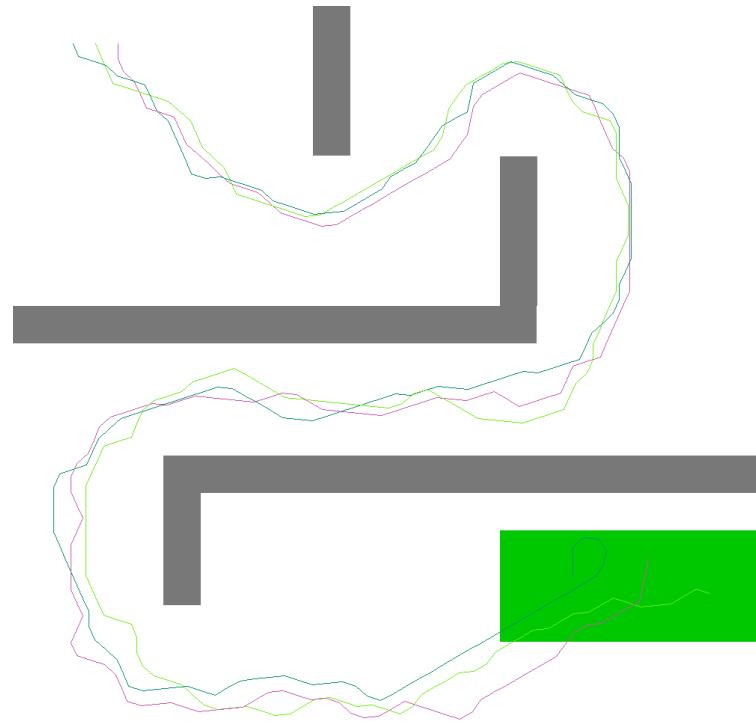


Figure 13.5: Trajectory after Dubins curves optimization

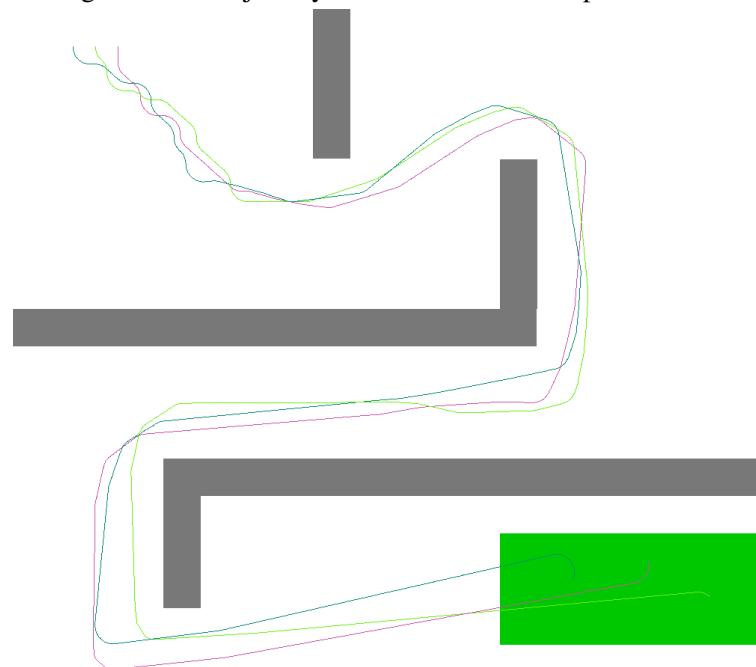


Table 13.1: Re-sampling and optimization results

| Frequency [Hz] | Minimal distance [m] | Maximal distance [m] | Average distance [m] |
|----------------|----------------------|----------------------|----------------------|
| 1              | 8582.18              | 8849.7               | 8721.2904            |
| 2              | 8311.65              | 8548.81              | 8430.23              |
| 4              | 8366.88              | 8393.09              | 8379.985             |
| 6              | 8248.9               | 8275.7               | 8262.3               |
| 8              | 8249.88              | 8378.51              | 8314.195             |
| 10             | 8286.22              | 8472.2               | 8379.21              |
| 12             | 8302.51              | 8309.2               | 8307.6613            |
| 14             | 8303.18              | 8303.18              | 8303.18              |
| 16             | 8363.92              | 8363.92              | 8363.92              |
| 18             | 8510.32              | 8510.32              | 8510.32              |
| 20             | 8194.22              | 8194.22              | 8194.22              |

value is 6 Hz and even the worst optimization in 6 Hz has smaller total distance than 8 to 18 Hz.

Depending on re-sampling frequency, the courses of optimization are also different.

In 13.7, 13.8 and 13.9 we can see mean values and standard deviations for different frequencies, divided into three graphs for better readability. The vertical lines are error bars, they show standard deviation during the optimization. Because the error bars would be too dense if they were shown for each iteration, only every 100th iteration is shown in the graphs. For comparison, frequency 1 Hz is also shown in each graph, the initial frequency before re-sampling. As we can see, frequencies 14, 16, 18 and 20 Hz have almost zero standard deviation and converge to lower value than the initial frequency. High standard deviation can be seen in frequency 10 Hz. That means the optimization got stuck in local optimum and was not able to shorten any trajectory for many iterations.

### 13.2.2 Second experiment

The best result of Dubins curves optimization (re-sampling of 4Hz) is shown in 13.11. As we can see, trajectories are much shorter than trajectories before optimization in 13.10, as in experiment 1, but curves in the upper part of figure still were not optimized. This was caused by optimization algorithm getting stuck in local optimum. The algorithm tried to optimize other parts and ended due to stopping conditions mentioned above. Light grey colour represents obstacle amplification.

The results are shown in graph 13.12. On the graph can be seen interesting results. Contrary to the graph from experiment 1 13.6, all frequencies have same minimal distance, maximal distance and mean distance. This shows us interesting fact. For same frequency, all 100 runs got stuck in same local optimum, but every frequency has different local optimum where the algorithm can stuck. Trajectory in this experiment is much smaller, which leads to zero standard deviation and difference between minimal and maximal distance between optimization results in one frequency. The difference between maximal and minimal results is bigger when optimizing longer and more complicated trajectory. As we can also see from graphs, we can not predict optimal re-sampling frequency from trajectory.

Depending on re-sampling frequency, the courses of optimization are also different.

In 13.13, 13.14 and 13.15 we can see mean values and standard deviations for different frequencies, divided into three graphs for better readability. The vertical lines are error bars, they

Figure 13.6: Re-sampling and optimization results graph

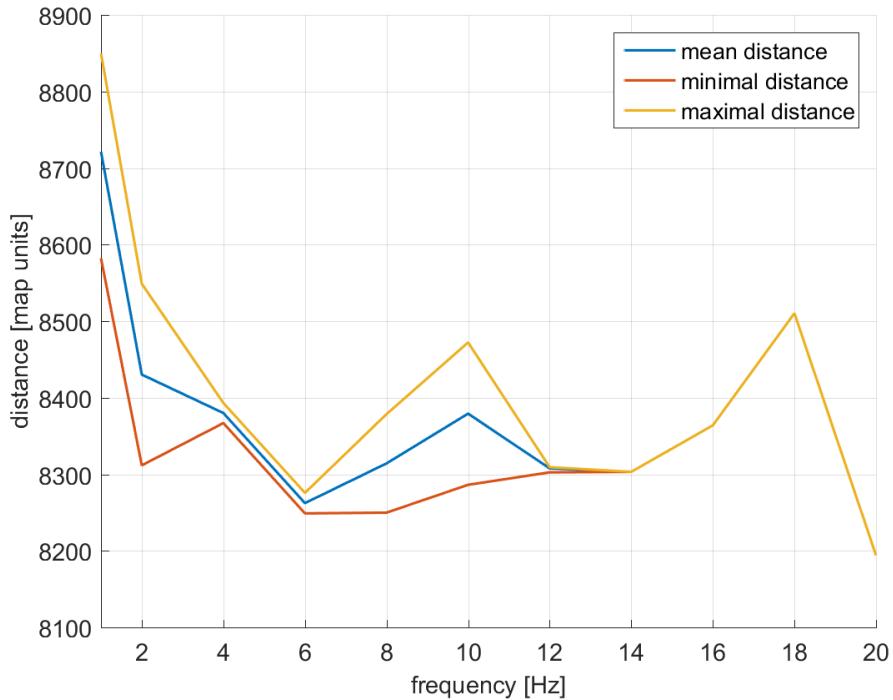


Figure 13.7: Time course of optimization for 2 Hz, 4 Hz, 6 Hz

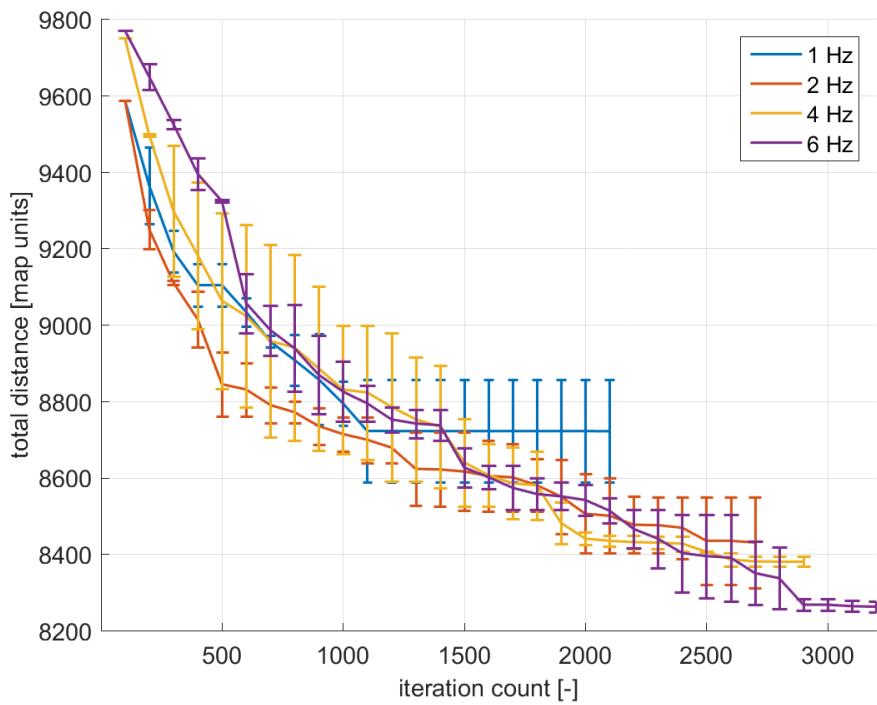


Figure 13.8: Time course of optimization for 8 Hz, 10 Hz, 12 Hz

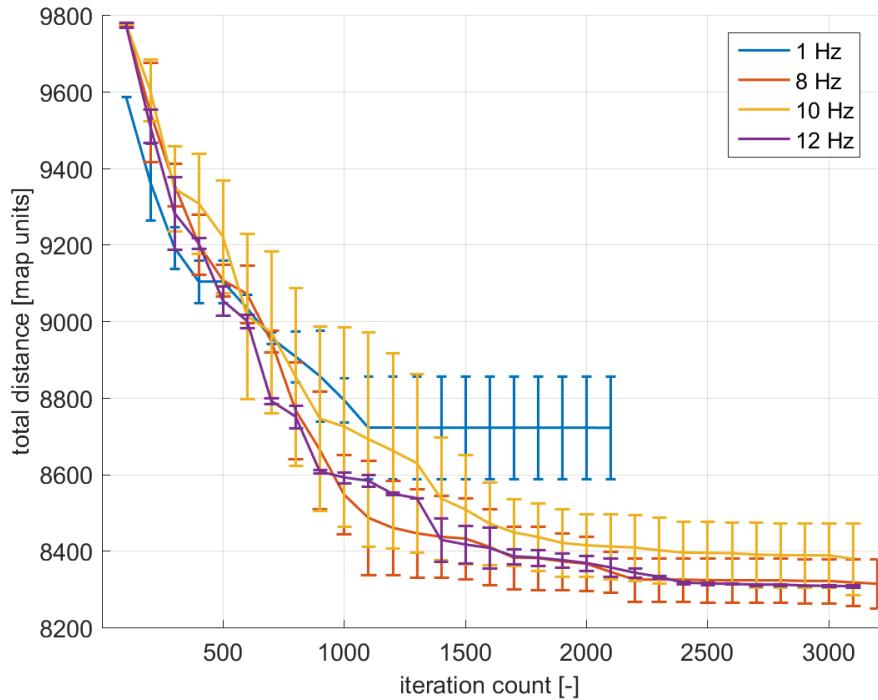


Figure 13.9: Time course of optimization for 14 Hz, 16 Hz, 18 Hz, 20 Hz

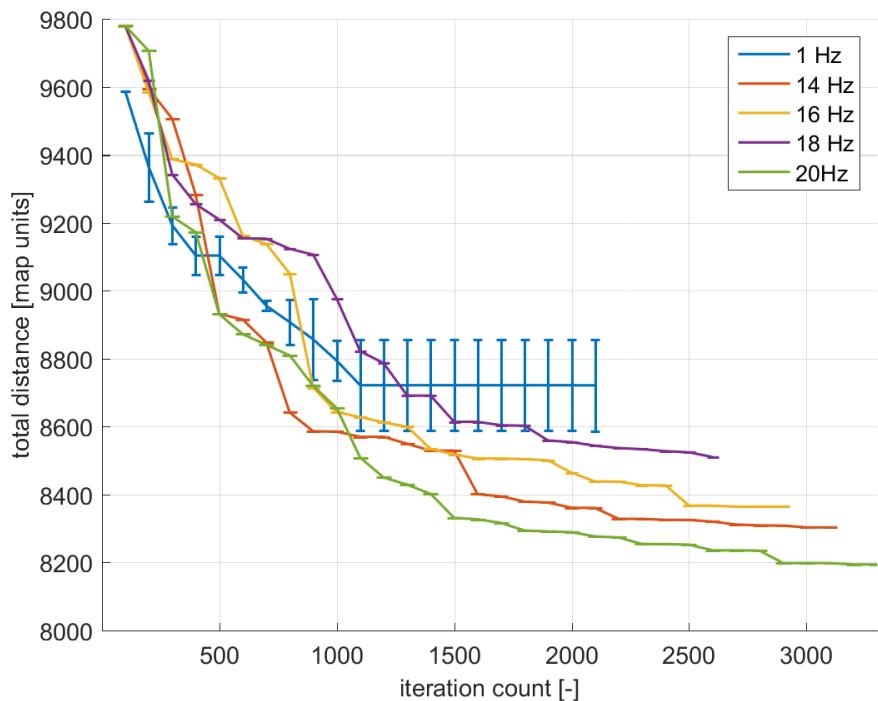


Figure 13.10: Trajectory before Dubins curves optimization

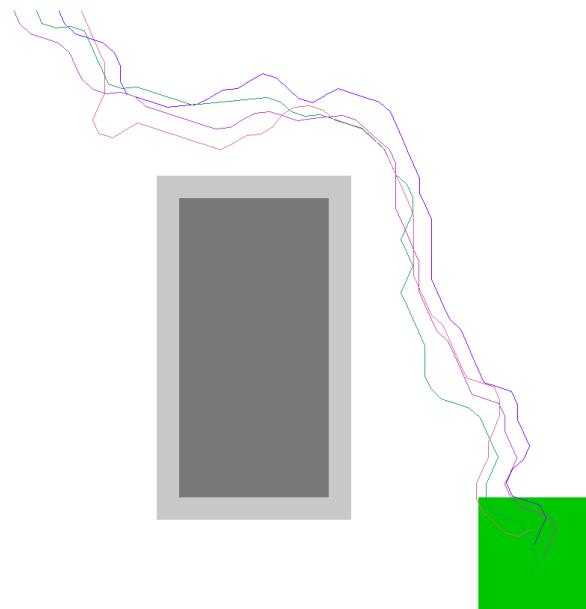


Figure 13.11: Trajectory after Dubins curves optimization

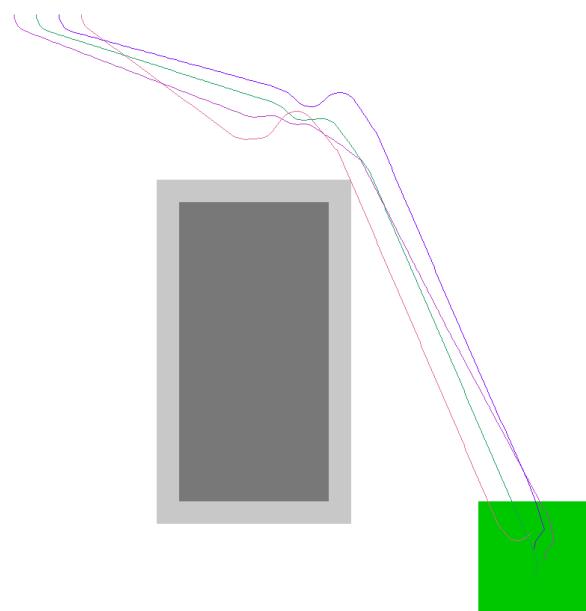
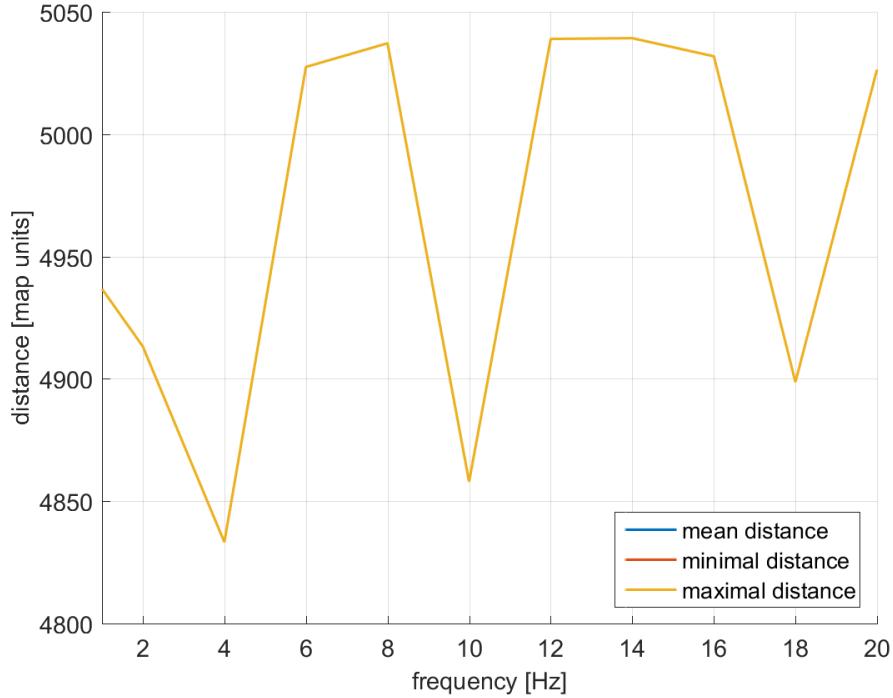


Figure 13.12: Re-sampling and optimization results graph



show standard deviation during the optimization. Because the error bars would be too dense if they were shown for each iteration, only every 10th iteration is shown on graphs. For comparison, on each graph is shown also frequency 1 Hz, the initial frequency before re-sampling. As we can see, in comparison to experiment 1, standard deviations are zero, so the optimization algorithm exhibits deterministic behaviour even if this optimization method is stochastic.

Figure 13.13: Time course of optimization for 2 Hz, 4 Hz, 6 Hz

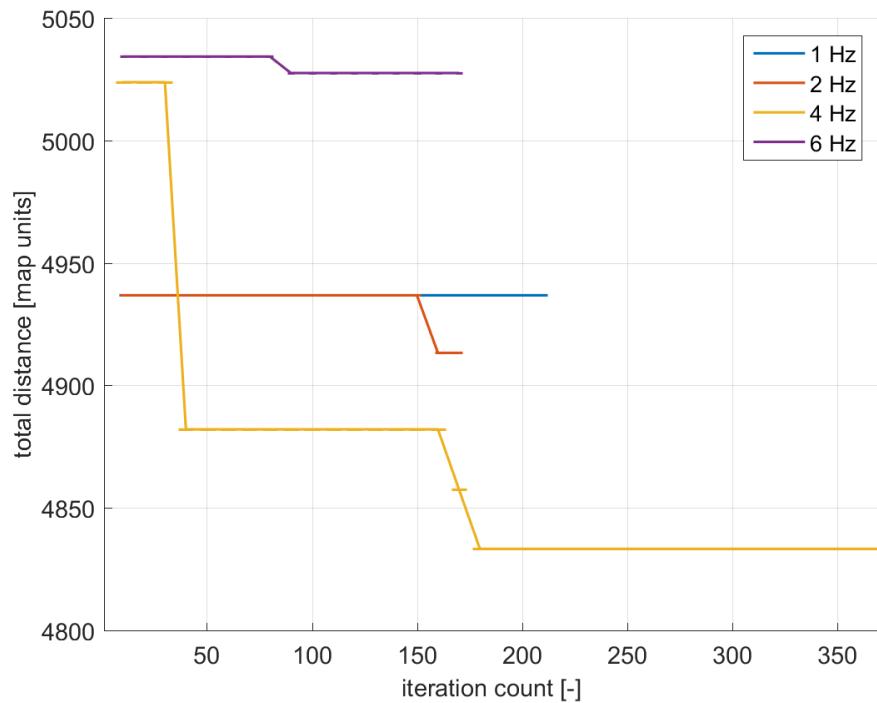


Figure 13.14: Time course of optimization for 8 Hz, 10 Hz, 12 Hz

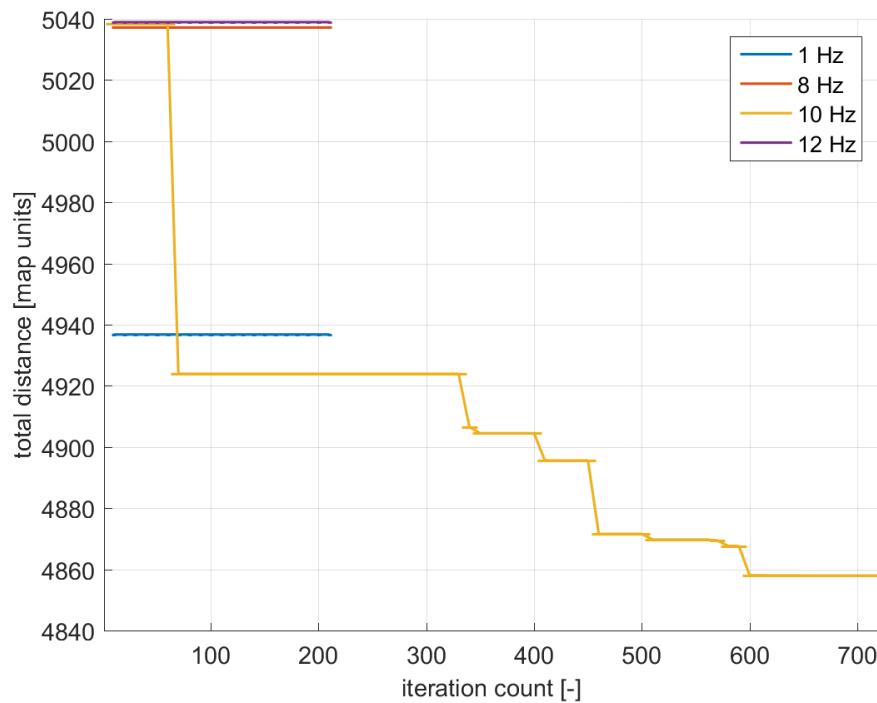
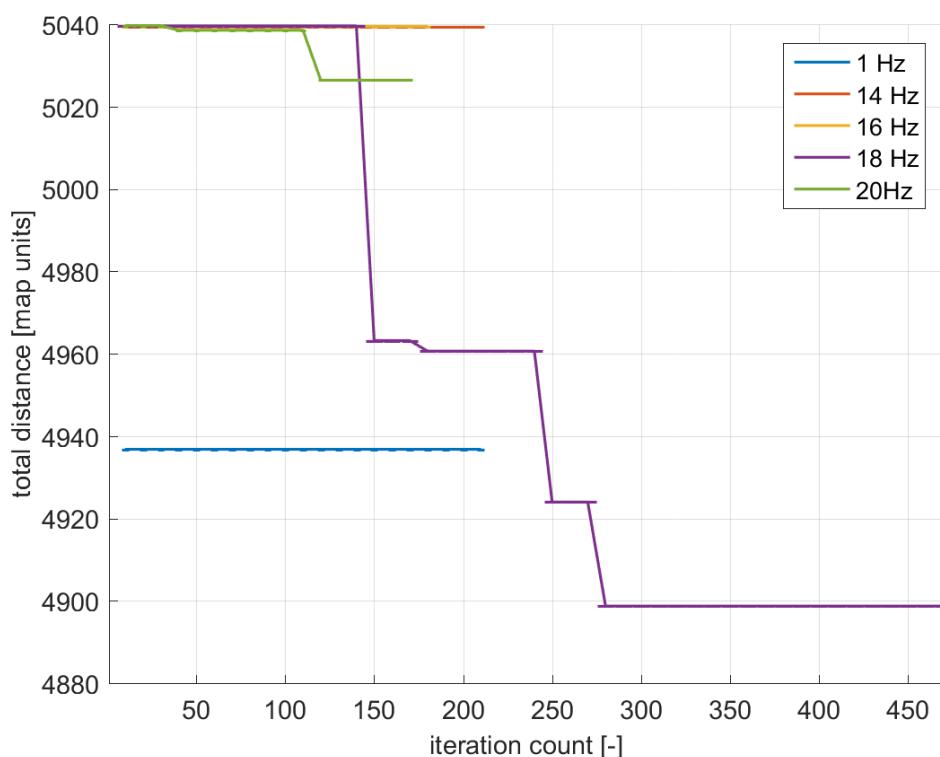


Figure 13.15: Time course of optimization for 14 Hz, 16 Hz, 18 Hz, 20 Hz



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CHAPTER  
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## CONCLUSION

This thesis contributes to the problems of autonomous surveillance with a novel approach by using a sampling-based algorithm for trajectory planning of a UAVs swarm and optimizing by Dubins curves. This thesis also examined the possibility of re-sampling of trajectories and influence of re-sampling on the optimization process.

The goal of this thesis was to design and implement an algorithm based on RRT-Path algorithm for motion planning of a swarm of cooperating unmanned aerial vehicles in the task of autonomous surveillance, optimize it by Dubins curves and simulate the flight of the swarm in V-REP platform. The algorithm provides trajectories from a depot station to optimal positions in Areas of Interest in two internationally standardized formats (CSV and JSON). An easy computable cost function had to be created and implemented. Feasibility of trajectory in each point has been ensured by an appropriate motion model and relative localization system.

The task was approached by separating the task to more smaller subtasks. The first subtask is finding a trajectory to a position, in which all UAVs are located above Areas of Interest. The trajectory finding is realized by using A\* algorithm to find the optimal guiding path and the RRT-Path algorithm uses this path to guide the space-filling tree. The second subtask is optimization of AoIs coverage using the RRT algorithm. The next subtask is re-sampling of trajectories and optimizing trajectories by Dubins manoeuvres, which provide us shorter trajectories than trajectories found only by using the RRT-Path algorithm. The effectiveness of Dubins curves optimization depends on re-sampling frequency, but unfortunately, the best frequency is heavily dependent on the map where trajectories are searched.

The presumed use of autonomous surveillance is monitoring of a parking lot near supermarket, shopping centre or a company campus. The advantage of an autonomous system over static cameras is the fact the UAV swarm can operatively change the distribution of individual UAVs according to the position of cars and minimize dead angles by moving UAVs. Static cameras usually fail to capture the identity of a criminal due to large distance or a bad angle, while UAVs can change their positions to capture the image of criminal in higher quality or from better angle and even provide simultaneous record from more cameras. Not only parking lots can be monitored, another possibility is monitoring of people during large events or large scale monitoring of agricultural areas. UAVs also scale much easier than static cameras, because UAVs can fly to their destination without human help, but static cameras must be installed by human and fast scalability is important factor in massive events and situations where size of Area of Interest change over time. Contrarily to GPS localized UAVs, swarm described in this thesis can

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even operate in hard to access areas, dense urban areas, inside buildings and other places with no GPS signal, thanks to the relative localization system.

## BIBLIOGRAPHY

- [1] Heard on the grapevine: drones to transform viticulture, July 2015. URL <https://droneapps.co/case-study-drones-to-transform-viticulture/>.
- [2] Lester Eli Dubins. On curves of minimal length with a constraint on average curvature, and with prescribed initial and terminal positions and tangents. *American Journal of Mathematics*, 79(3):497–516, July 1957. URL [http://www.jstor.org/stable/2372560?origin=crossref&seq=1#page\\_scan\\_contents](http://www.jstor.org/stable/2372560?origin=crossref&seq=1#page_scan_contents).
- [3] Jan Faigl, Tomáš Krajník, Jan Chudoba, and Martin Saska. Low-cost embedded system for relative localization in robotic swarms. *Robotics and Automation (ICRA), 2013 IEEE International Conference on*, pages 993 – 998, May 2013.
- [4] Roosevelt A. Fernandes. Monitoring system for power lines and right-of-way using remotely piloted drone., April 1989. URL <http://www.google.com/patents/US4818990>.
- [5] Brian Fung. Why drone makers have declared war on the word ‘drone’, August 2013. URL <https://www.washingtonpost.com/news/the-switch/wp/2013/08/16/why-drone-makers-have-declared-war-on-the-word-drone/>.
- [6] L. E. Kavraki, P. Svestka, J. C. Latombe, and M. H. Overmars. Probabilistic roadmaps for path planning in high-dimensional configuration spaces. *IEEE Transactions on Robotics and Automation*, 12:566–580, August 1996.
- [7] Steven M. LaValle. Rapidly-exploring random trees: A new tool for path planning. Technical report, Department of Computer Science, Iowa State University, 1998. URL <http://msl.cs.uiuc.edu/~lavalle/papers/Lav98c.pdf>.
- [8] Steven M. LaValle. *Planning Algorithms*. Cambridge University Press, 2006. URL <http://planning.cs.uiuc.edu/>.
- [9] International Civil Aviation Organization. *Unmanned Aircraft Systems (UAS)*. International Civil Aviation Organization, April 2011.
- [10] Andrea Peterson. The switch states are competing to be the silicon valley of drones, August 2013.

- [11] Mat  j Petrl  k. Planning of swarm deployment for autonomous surveillance. Bachelor's thesis, Czech technical university in Prague Faculty of Electrical Engineering Department of Cybernetics, 2015.
- [12] M. Saska. MAV-swarms: unmanned aerial vehicles stabilized along a given path using on-board relative localization. In *Proceedings of 2015 International Conference on Unmanned Aircraft Systems (ICUAS)*, 2015.
- [13] M. Saska, V. Vonasek, T. Krajnik, and L. Preucil. Coordination and Navigation of Heterogeneous UAVs-UGVs Teams Localized by a Hawk-Eye Approach. In *Proceedings of 2012 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, 2012.
- [14] M. Saska, T. Krajnik, V. Vonasek, P. Vanek, and L. Preucil. Navigation, Localization and Stabilization of Formations of Unmanned Aerial and Ground Vehicles. In *Proceedings of 2013 International Conference on Unmanned Aircraft Systems (ICUAS)*, 2013.
- [15] M. Saska, J. Chudoba, L. Preucil, J. Thomas, G. Loianno, A. Tresnak, V. Vonasek, and V. Kumar. Autonomous Deployment of Swarms of Micro-Aerial Vehicles in Cooperative Surveillance. In *Proceedings of 2014 International Conference on Unmanned Aircraft Systems (ICUAS)*, 2014.
- [16] M. Saska, Z. Kasl, and L. Preucil. Motion Planning and Control of Formations of Micro Aerial Vehicles. In *Proceedings of The 19th World Congress of the International Federation of Automatic Control (IFAC)*. IFAC, 2014.
- [17] M. Saska, T. Krajnik, V. Vonasek, Z. Kasl, V. Spurny, and L. Preucil. Fault-Tolerant Formation Driving Mechanism Designed for Heterogeneous MAVs-UGVs Groups. *Journal of Intelligent and Robotic Systems*, 73(1-4):603–622, 2014.
- [18] M. Saska, J. Langr, and L. Preucil. Plume Tracking by a Self-stabilized Group of Micro Aerial Vehicles. In *Modelling and Simulation for Autonomous Systems*, 2014.
- [19] M. Saska, J. Vakula, and L. Preucil. Swarms of Micro Aerial Vehicles Stabilized Under a Visual Relative Localization. In *Proceedings of 2014 IEEE International Conference on Robotics and Automation (ICRA)*. IEEE, 2014.
- [20] M. Saska, V. Vonasek, T. Krajnik, and L. Preucil. Coordination and Navigation of Heterogeneous MAV&#8211;UGV Formations Localized by a &#8216;hawk-eye&#8217;-like Approach Under a Model Predictive Control Scheme. *International Journal of Robotics Research*, 33(10):1393–1412, 2014.
- [21] M. Saska, T. Baca, J. Thomas, J. Chudoba, L. Preucil, T. Krajnik, J. Faigl, G. Loianno, and V. Kumar. System for deployment of groups of unmanned micro aerial vehicles in GPS-denied environments using onboard visual relative localization. *Autonomous Robots*. *First online.*, 2016.
- [22] M. Saska, V. Von  sek, J. Chudoba, J. Thomas, G. Loianno, and V. Kumar. Swarm distribution and deployment for cooperative surveillance by micro-aerial vehicles. *Journal of Intelligent & Robotic Systems*. *First online.*, 2016.

- [23] V. Trianni. *Evolutionary Swarm Robotics: Evolving Self-Organising Behaviours in Groups of Autonomous Robots*. Studies in Computational Intelligence. Springer Berlin Heidelberg, 2008. ISBN 9783540776123. URL <https://books.google.cz/books?id=sg9rCQAAQBAJ>.
- [24] Petr Váňa. Path planning for non-holonomic vehicle in surveillance missions. Master's thesis, Czech Technical University in Prague, 2015. URL <https://dspace.cvut.cz/bitstream/handle/10467/61814/F3-DP-2015-Vana-Petr-thesis.pdf>.
- [25] Chris Velazco. Amazon is experimenting with autonomous flying delivery drones, December 2013.
- [26] V. Vonasek, J. Faigl, T. Krajnik, and L. Preucil. RRT-Path: a guided Rapidly exploring Random Tree. In *Robot Motion and Control 2009*, pages 307–316, Heidelberg, 2009. Springer. ISBN 978-1-84882-984-8.
- [27] V. Vonasek, M. Saska, L. Winkler, and L. Preucil. High-level motion planning for cpg-driven modular robots. *Robotics and Autonomous Systems*, 68:116 – 128, 2015.
- [28] Vojtěch Vonásek. *A guided approach to sampling-based motion planning*. PhD thesis, Czech Technical University in Prague Faculty of electrical engineering Department of cybernetics, August 2015.