

Question - 1 The Social Network

A social network has n active users, numbered from 0 to n-1, who selectively friend other users to create groups of friends within the network. We define the following:

- Two users, x and y, are direct friends if they friend each other on the network.
- Two users, x and z, are *indirect* friends if there exists some direct friend, y, common to both users x and z.
- Two users, x and y, belong to the same group if they are friends
 (either directly or indirectly) with each other. In other words, if user
 x is part of a group, then all of user x's friends and friends of friends
 belong to the same group.
- We describe the number of people in each group as an array of n integers, counts, where each counts; (0 ≤ i < n) denotes the total number of users in the group that user i belongs to. For example, if counts = [3, 3, 3, 3, 3, 1, 3], then there are three groups; users 0, 1, 2, 3, 4, and 6 are in one of two 3-person groups, and user 5 is in a 1-person group.

ID	0	1	2	3	4	5	6
Group S	ize	3	3	3	3	1	3

• A group is valid if all the users in the group have minimal ID numbers. In other words, a group of size k must contain the k smallest ID numbers belonging to a group of that size with respect to the smallest user ID in the group. For example, if counts = [3, 3, 3, 3, 3, 1, 3], then the grouping [0, 1, 2], [3, 4, 6], and [5] is valid; however, the grouping [0, 1, 4], [2, 3, 6], and [5] is not valid because the group [0, 1, 4] does not contain the three smallest user IDs for the set of user IDs belonging to 3-person groups (i.e., {0, 1, 2, 3, 4, 6}).

▶ Example

• We print the information for each valid group on a new line in the format user_{smallest ID} ... user_{largest ID}, where the users within each group are ordered by ascending ID and the groups themselves are ordered by ascending user_{smallest ID}. For example, we print the valid grouping [0, 1, 2], [3, 4, 6], and [5] for counts = [3, 3, 3, 3, 3, 1, 3] as:

Complete the *socialGraphs* function. It has one parameter: an array of *n* integers, *counts*, where each *counts*; denotes the total number of users in the group that user *i* belongs to. The function must print the information for each *valid group* in the format specified above.



Input Format

The first line contains an integer, *n*, describing the number of elements in *counts* (i.e., the total number of users active on the social network).

Each line i of n subsequent lines (where $0 \le i < n$) contains an integer describing $counts_i$.

Constraints

- $1 \le n \le 2 \times 10^5$
- $1 \le counts_i \le n$, where $0 \le i < n$.
- It is guaranteed that a valid grouping always exists for the given *counts* array.

Output Format

The function must *print* the information for each *valid group* on a new line. The users within a group must be ordered by ascending user ID, and each group must be ordered by ascending smallest user ID.

▼ Sample Case 0

Sample Input

```
4
2
2
2
2
2
```

Sample Output

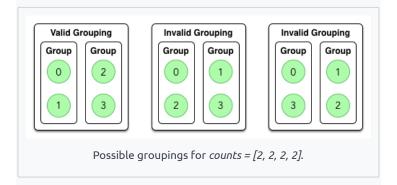
```
0 1
2 3
```

Explanation

We express counts = [2, 2, 2, 2] as the following table of group sizes:

ID	0	1	2	3
Gro	up2Si:	ze 2	2	2

The valid grouping here is the groups [0, 1] and [2, 3]:



We then print each group on a new line, where the groups and their user IDs are listed in ascending order.