



## Question - 1

### The Social Network

A social network has  $n$  active users, numbered from  $0$  to  $n - 1$ , who selectively friend other users to create groups of friends within the network. We define the following:

- Two users,  $x$  and  $y$ , are *direct* friends if they friend each other on the network.
- Two users,  $x$  and  $z$ , are *indirect* friends if there exists some direct friend,  $y$ , common to both users  $x$  and  $z$ .
- Two users,  $x$  and  $y$ , belong to the same *group* if they are friends (either directly or indirectly) with each other. In other words, if user  $x$  is part of a group, then all of user  $x$ 's friends and friends of friends belong to the same group.
- We describe the number of people in each group as an array of  $n$  integers, *counts*, where each *counts* <sub>$i$</sub>  ( $0 \leq i < n$ ) denotes the total number of users in the group that user  $i$  belongs to. For example, if *counts* = [3, 3, 3, 3, 3, 1, 3], then there are three groups; users 0, 1, 2, 3, 4, and 6 are in one of two 3-person groups, and user 5 is in a 1-person group.

ID	0	1	2	3	4	5	6
Group Size	3	3	3	3	3	1	3

- A group is *valid* if all the users in the group have minimal ID numbers. In other words, a group of size  $k$  must contain the  $k$  smallest ID numbers belonging to a group of that size with respect to the smallest user ID in the group. For example, if *counts* = [3, 3, 3, 3, 3, 1, 3], then the grouping [0, 1, 2], [3, 4, 6], and [5] is valid; however, the grouping [0, 1, 4], [2, 3, 6], and [5] is *not valid* because the group [0, 1, 4] does not contain the three smallest user IDs for the set of user IDs belonging to 3-person groups (i.e., {0, 1, 2, 3, 4, 6}).

#### ► Example

- We print the information for each valid group on a new line in the format `usersmallest ID ... userlargest ID`, where the users within each group are ordered by ascending ID and the groups themselves are ordered by ascending *user<sub>smallest ID</sub>*. For example, we print the valid grouping [0, 1, 2], [3, 4, 6], and [5] for *counts* = [3, 3, 3, 3, 3, 1, 3] as:

```
0 1 2
3 4 6
5
```

Complete the *socialGraphs* function. It has one parameter: an array of  $n$  integers, *counts*, where each *counts* <sub>$i$</sub>  denotes the total number of users in the group that user  $i$  belongs to. The function must print the information for each *valid group* in the format specified above.

Input Format

The first line contains an integer,  $n$ , describing the number of elements in *counts* (i.e., the total number of users active on the social network).  
Each line  $i$  of  $n$  subsequent lines (where  $0 \leq i < n$ ) contains an integer describing  $counts_i$ .

Constraints

- $1 \leq n \leq 2 \times 10^5$
- $1 \leq counts_i \leq n$ , where  $0 \leq i < n$ .
- It is guaranteed that a valid grouping always exists for the given *counts* array.

Output Format

The function must *print* the information for each *valid group* on a new line. The users within a group must be ordered by ascending user ID, and each group must be ordered by ascending smallest user ID.

▼ Sample Case 0

Sample Input

```
4
2
2
2
2
```

Sample Output

```
0 1
2 3
```

Explanation

We express  $counts = [2, 2, 2, 2]$  as the following table of group sizes:

ID	0	1	2	3
GroupSize	2	2	2	2

The *valid* grouping here is the groups  $[0, 1]$  and  $[2, 3]$ :

Valid Grouping

Group

0

1

Group

2

3

Invalid Grouping

Group

0

2

Group

1

3

Invalid Grouping

Group

0

3

Group

1

2

Possible groupings for  $counts = [2, 2, 2, 2]$ .

We then print each group on a new line, where the groups and their user IDs are listed in ascending order.