

Weather Radar Signal processing – Signals to products

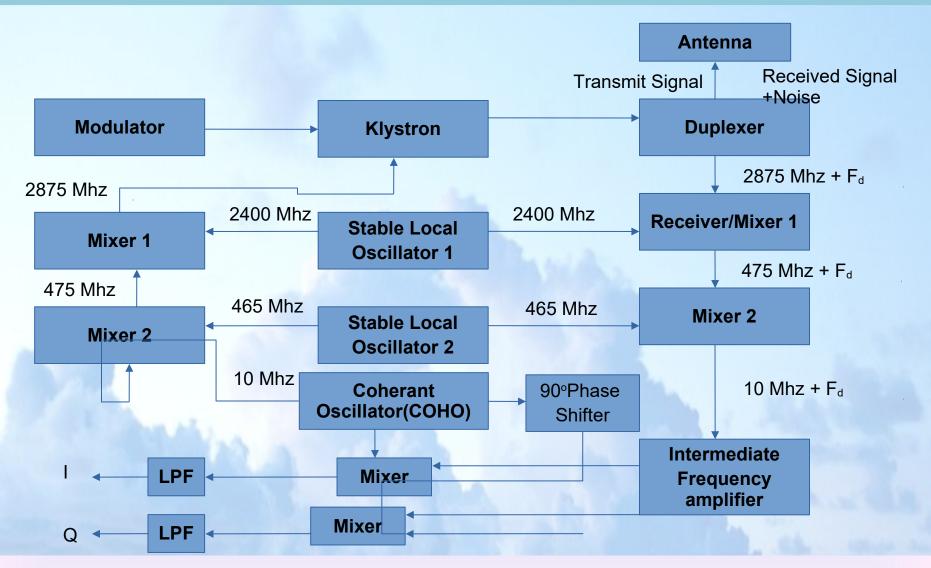
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भारत मौसम विज्ञान विभाग INDIAMETEOROLOGICAL DEPARTMENT



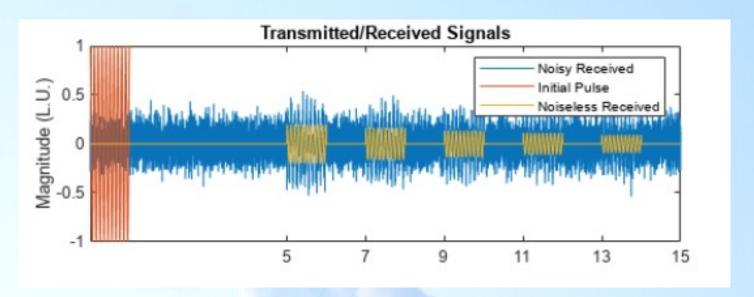


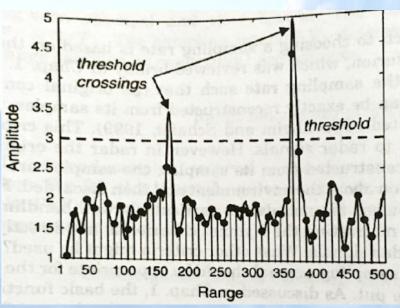
Block Diagram

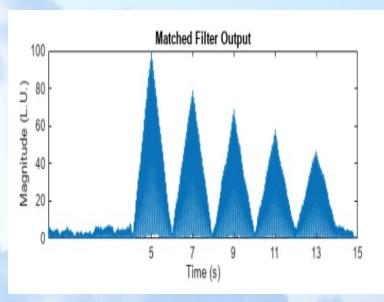
















Ray Data synchronization

Angle Coverage synchronization

$$V = \frac{Resolution * f(PRF)}{sampling}$$

$$sampling = \frac{Resolution * f(PRF)}{V}$$

Resolution= 0.7°

Min speed= 6 deg/sec

Sample=?

PRF= 1500 Hz

Sampling=
$$\frac{0.7}{6} * 1500 = 175$$





Ray Data synchronization

Pulse Number synchronization

Beam spacing (Resolution) =
$$\frac{Nsamp}{PRF} * Ant.speed$$

No of Samples = 80 PRF = 1000Hz and Antenna speed is 20 deg/sec

Then the resolution is 1.6 Deg





Samples to Integrate

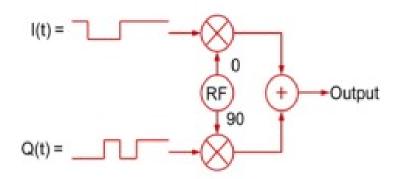
Antenna Beam width = 1 Degree

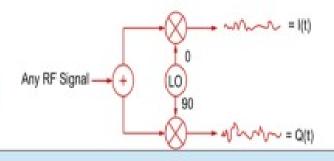
PRF	Antenna speed	Dwell time(sec)	Samples
180	6 Deg/Sec	1/6	30
180	3 Deg/sec	1/3	60
180	18 Deg/Sec	1/18	10
300	6 Deg/Sec	1/6	50
300	3 Deg/sec	1/3	100
300	18 Deg/Sec	1/18	17
600	6 Deg/Sec	1/6	100
600	3 Deg/sec	1/3	200
600	18 Deg/Sec	1/18	33





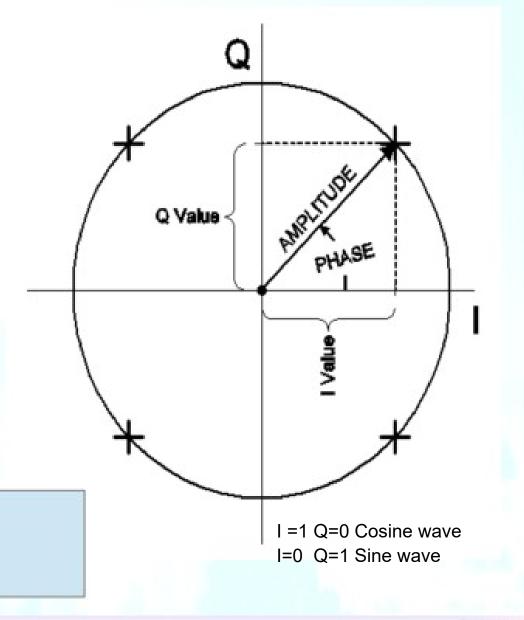
- I=+1 & Q=+1 results in 45 degree phase
- I=-1 & Q=+1 results in 135 degree phase
- I=-1 & Q=-1 results in 225 degree phase
- I=+1 & Q=-1 results in 315 degree phase





$$s = I + jQ$$

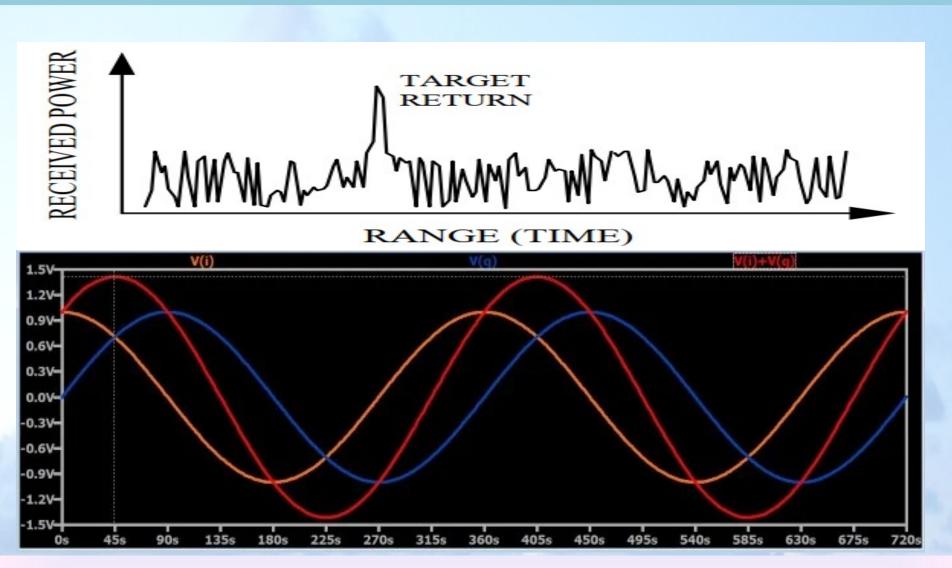
PHASOR







Mixing of signals







I components

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X V																		
_^	HI [167	722x746 double]						_			40		40			45	4.5	
Ш,		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	
		-0.22028	0.11868	-0.42908	0.0037794	0.00043416	-0.020264	-0.0053558	-0.00012493	0.00026989	-0.0023165	-0.00092387	0.0010405	0.01693	0.00015074	0.00023246	-0.00073481	0.000
2	2	0.21228	0.07486	-0.33228	0.0024843	0.00050974	-0.020241	-0.0050697	0.00013822	-0.00014693	-0.002182	-0.00077009	0.0011458	0.017052	0.00012583	-0.00030494	-0.00095487	-0.00
. 3	3	-0.16766	0.062347	-0.33777	0.0017219	0.00077295	-0.018143	-0.0046711	0.00020009	-0.00023991	-0.0020723	-0.00050616	0.001266	0.01683	-7.1585e-05	0.00014567	-0.0009315	-1.25
. 4	4	-0.21136	0.00042832	-0.34229	-0.00063896	0.00048614	-0.016541	-0.0040073	-3.0518e-05	0.0001117	-0.0020866	-0.00021976	0.0015826	0.01664	4.4405e-05	-7.2181e-05	-0.00089669	-2.33
. 5	5	-0.10709	0.016975	-0.24298	0.0024128	-0.00016826	-0.014839	-0.0039635	0.00028789	-0.00041378	-0.0018568	-0.00052786	0.0012312	0.01664	0.00012678	9.7752e-05	-0.0010085	9.656
. 6	5	0.20728	0.027283	-0.22913	0.0028744	-3.9876e-05	-0.014622	-0.0029802	0.00014269	0.00012875	-0.0018134	0.00012779	0.0016408	0.016479	-0.00018382	-0.00020999	-0.00079536	9.530
7	7	0.051498	0.17297	-0.23926	0.0012794	0.00014055	-0.01252	-0.0031252	5.0008e-05	-0.00024402	-0.0017133	-0.00037289	0.0016689	0.016685	-4.3988e-05	-2.8849e-05	-0.00092387	-0.00
8	3	-0.21643	0.0021038	-0.25793	0.0016093	-2.3961e-05	-0.011044	-0.0028915	0.00024241	-0.00017059	-0.0015473	0.00021231	0.0014601	0.016335	-9.0718e-05	3.8505e-05	-0.00093842	0.000
9	9	-0.1972	0.084198	-0.18738	0.0034847	0.00030589	-0.0098076	-0.0026989	6.6698e-05	7.6652e-05	-0.0012937	-0.00027764	0.0018606	0.016541	0.00013095	-6.7592e-05	-0.00075102	-0.00
×	10	0.1756	0.070801	-0.17303	0.0029497	0.0003022	-0.0088501	-0.0025063	0.00014526	-0.00025034	-0.0013232	4.4763e-05	0.0016112	0.016335	5.9605e-08	9.5546e-05	-0.00092936	-0.00
<u>^</u> 1	11	0.031891	0.057098	-0.18549	0.0033073	0.00058246	-0.007412	-0.0017281	0.00014222	-8.7261e-05	-0.0011506	-0.00017881	0.001534	0.016418	-6.7174e-05	-5.3167e-05	-0.00086641	4.440
1	12	-0.1759	0.039627	-0.13721	0.0026073	0.00064373	-0.006094	-0.0016937	4.7743e-05	-4.6372e-05	-0.0010352	-0.00018907	0.0017939	0.016373	6.7353e-05	0.00014752	-0.00064731	-9.7
1	13	0.17078	0.064514	-0.12106	0.002346	0.00049233	-0.0052719	-0.0023537	0.0001139	-2.867e-05	-0.00099897	-0.00015283	0.0017853	0.016296	-0.00012851	-5.56lle-05	-0.00085258	-1.0
1	14	-0.0061493	0.04747	-0.13318	0.0015783	0.00030959	-0.0054588	-0.0010948	0.00011384	-0.00025499	-0.00097322	-0.00030899	0.0014505	0.016304	-5.1856e-06	3.3557e-05	-0.00064611	-5.29
1	15	0.054123	0.046249	-0.11038	0.0023727	0.00012165	-0.00453	-0.0012927	9.7752e-05	-1.1384e-05	-0.00081801	-6.5804e-05	0.0018916	0.016022	0.00019145	2.0862e-06	-0.00060129	-3.5
1	16	0.06604	0.030251	-0.092102	0.0024118	-2.4498e-05	-0.0036964	-0.0011039	9.3281e-05	8.3447e-06	-0.00098801	-0.00047708	0.0017405	0.016502	-3.8028e-05	4.7207e-05	-0.00061226	2.16
1	17	-0.060349	0.023994	-0.12665	0.0022602	0.00011075	-0.0027103	-0.0004586	8.8096e-05	8.3447e-06	-0.00097203	2.6226e-06	0.0014834	0.016235	5.132e-05	-2.11e-05	-0.00043035	4.655
1	18	0.21509	0.053894	-0.068268	0.0022058	0.00029206	-0.0022812	-0.00099182	8.1301e-05	7.7367e-05	-0.00096583	-0.00039756	0.0017953	0.016327	0.00010514	-6.4373e-05	-0.00060368	-0.00
- 1	19	0.21893	0.027626	-0.077637	0.0029221	4.4823e-05	-0.0022211	-0.00024301	4.2617e-05	-8.2076e-05	-0.0010014	-0.00018179	0.0016098	0.016182	-6.0201e-06	6.1393e-06	-0.00035906	2.68
	20	0.21948	0.041321	-0.063416	0.0026731	-0.00019121	-0.001636	3.2723e-05	1.4305e-06	8.7023e-06	-0.0010953	-0.00020021	0.0016823	0.016289	8.595e-05	-5.1856e-05	-0.0003773	-2.96
	71	0.18304	0.018509	-0.045639	0.002471	-0.00017983	-0.0012951	-0.00025392	-7.3671e-05	-1.8477e-05	-0.0012326	-0.0001995	0.0015244	0.016167	5.6803e-05	-8.2195e-05	-0.00045538	-0.00
	22	-0.20111	0.023209	-0.067017	0.0026493	0.00016826	-0.0012536	0.00057721	-5.5194e-05	-5.1677e-05	-0.0012894	-0.00017202	0.0015574	0.016197	-2.0444e-05	0.00014472	-0.00027966	0.000
>	23	0.1875	0.025047	-0.073578	0.0028181	1.3053e-05	-0.00042117	0.00040138	-0.00010455	-4.065e-05	-0.0014739	-0.00013697	0.0015144	0.016129	0.00010854	6.6221e-05	-0.00040269	4.959
X	24	0.17621	0.036194	-0.049545	0.0037861	-0.00028634	0.00018543	0.00017667	-0.00014549	-7.2956e-05	-0.0014334	-4.5657e-05	0.0014696	0.015816	1.1981e-05	-8.0884e-05	-0.00028956	0.000
·	25	0.046722	-0.0022964	-0.05101	0.0044708	1.0431e-05	-8.1658e-05	0.00082707	-0.00012738	3.463e-05	-0.0015244	-0.00020009	0.0014458	0.015869	-8.2552e-05	2.8253e-05	-0.00028932	-2.11
	26	0.078522	-0.003541	-0.066467	0.0044594	-8.7023e-05	-2.3723e-05	1.6212e-05	-0.00011796	-8.3745e-05	-0.001503	1.2636e-05	0.0014067	0.015511	7.3731e-05	3.4153e-05	-0.0001961	-3.65
	20 27	0.12958	-0.05365	-0.037506	0.0044354	6.3419e-05	-7.1526e-05	0.00050807	-0.00011750	-0.00010121	-0.0014648	-0.00014985	0.0012059	0.015358	-5.0664e-06	-2.5332e-05	-0.00024796	3.618
		0.12986	-0.015202	-0.064728	0.0040169	-0.0002054	-0.00049663	0.00080807	-2.4319e-05	9.2387e-06	-0.0014648	-0.00014388	0.0012089	0.015163	-2.2709e-05	-5.3227e-05	-0.00024796	3.528
	28	0.12155	-0.015202	-0.084728	0.0043564	-8.9109e-05	-3.3557e-05	-0.00036728	-2.4319e-05 -9.2626e-05	-0.00017852	-0.0015121	-0.00010329	0.0012779	0.015163	-2.2709e-05 -5.3346e-05	-3.2604e-05	-0.00026703	1.279
	29																	
	30	0.046539	-0.049408	-0.052017	0.0049267	-0.00011063	9.8288e-05	0.00017667	-4.2617e-05	-1.2338e-05	-0.00141	-0.00013369	0.00093818	0.014523	3.0696e-05	2.7597e-05	-0.00018489	-4.10
3		0.17719	-0.052307	-0.036926	0.0053558	-8.6606e-05	-0.0003016	-0.00018442	5.7817e-06	-3.01e-05	-0.0014014	-0.00017864	0.0010223	0.014145	-8.4162e-05	6.4373e-06	-0.00026798	3.695
	32	-0.1391	-0.12347	-0.049911	0.0056	-0.00011766	-0.00065613	-0.00078654	8.9645e-05	-0.00012904	-0.0013103	-0.00014728	0.0012331	0.013622	-7.4744e-05	1.4186e-05	-0.0001803	-2.52
	33	0.2168	-0.072266	-0.037521	0.0060005	-0.00019664	-0.00039685	-0.00050759	-9.4175e-06	-0.00016427	-0.0012627	-0.00022024	0.0011845	0.013439	-5.5492e-05	-3.773e-05	-8.0407e-05	-5.31
- 111-	34 «	-0.10733	-0.087036	-0.020493	0.0055695	-0.00010252	-0.00085855	-0.00045419	1.1146e-05	-2.3067e-05	-0.0011539	-0.00023311	0.0010662	0.013176	-5.281e-05	-6.8605e-05	-0.00014049	4.643





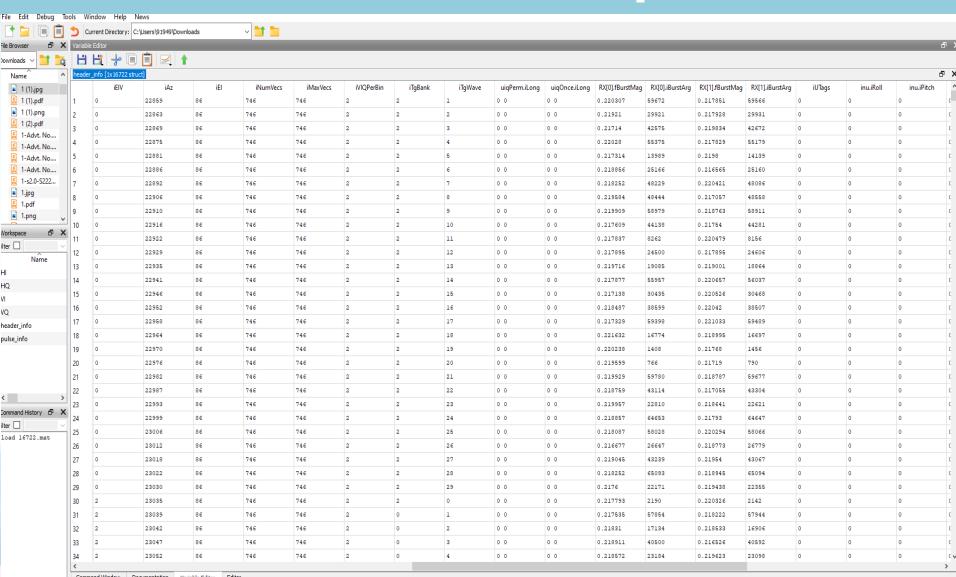
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1).jpg		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	^
1).pdf	1	0.0046711	0.34631	-0.13641	0.00077653	5.9128e-05	-0.014587	-0.0065613	-4.9531e-05	0.00032055	-0.0015125	-0.0017242	-0.00018579	0.0091133	0.00013953	-0.00025463	0.0015016	-2.4438e-06	
1).png	2	0.054596	0.30847	-0.10718	0.0022335	0.00085592	-0.013313	-0.0068169	0.00037158	-0.00039852	-0.0015125	-0.0018549	-0.00020838	0.0093994	-2.1935e-05	0.00010449	0.0012331	5.4777e-05	0
2).pdf Advt. No	3	0.13794	0.22095	-0.11829	0.002985	0.00076509	-0.012527	-0.0066128	-4.7326e-05	0.00031507	-0.0017886	-0.001317	-0.00032759	0.0087585	1.7822e-05	1.3709e-05	0.0014033	7.3314e-06	
Advt. No	4	-0.062073	0.41333	-0.14484	0.0055065	0.00031042	-0.011925	-0.0071278	0.00015652	-0.00024134	-0.0019088	-0.0017571	-0.00076461	0.0090752	0.00015813	3.9458e-05	0.0010443	0.00019592	0
Advt. No	5	0.18909	0.44287	-0.15192	0.0072651	0.00068283	-0.013004	-0.0058861	0.00018001	-3.1769e-05	-0.0019131	-0.0011959	-0.0007484	0.0081902	-0.0002045	-7.7546e-05	0.00098276	-4.524e-05	
Advt. No	6	-0.070251	0.30981	-0.15796	0.0061455	0.00048828	-0.010727	-0.0060463	-0.00016385	0.00012171	-0.0020971	-0.0012426	-0.00078917	0.008255	-9.9182e-05	-0.00010788	0.00094748	2.9802e-05	4
s2.0-S222	7	0.2121	0.29175	-0.15704	0.0060787	0.00034392	-0.010674	-0.0058765	0.00022042	-0.0002358	-0.0021162	-0.001245	-0.00095582	0.0073204	7.8022e-05	0.0001328	0.00068355	6.6459e-05	
pg odf	8	0.037216	0.26721	-0.17053	0.0075722	9.7752e-05	-0.0096741	-0.0046215	6.926le-05	0.00019878	-0.0020294	-0.00095797	-0.00098181	0.007164	5.3108e-05	-5.0545e-05	0.00072145	0.00015801	
ong	9	-0.09729	0.1485	-0.15228	0.0067482	-7.7069e-05	-0.0087547	-0.0045643	0.00012589	-0.00014061	-0.0020151	-0.0011339	-0.0008707	0.0061836	0.000117	0.00010383	0.00053549	-0.00019109	
₽ X	10	-0.12854	0.22711	-0.1441	0.0065117	0.00014704	-0.0071449	-0.0032387	0.00014454	1.2636e-05	-0.0021296	-0.0006218	-0.0010691	0.0057297	-7.1526e-05	-2.8193e-05	0.00029337	6.9976e-05	0
	11	-0.21552	0.1853	-0.14459	0.005291	-4.9889e-05	-0.006052	-0.0026016	9.4593e-05	0.00011307	-0.001996	-0.00096011	-0.00088382	0.0054054	-2.4498e-05	7.3731e-05	0.00052428	4.8041e-05	
Name	12	0.1286	0.11752	-0.13776	0.0053024	5.3823e-05	-0.0048065	-0.0030537	0.00011963	8.9765e-05	-0.0018859	-0.00037026	-0.00062656	0.0046844	4.9889e-05	-2.0206e-05	0.00024676	-4.7505e-05	0
	13	0.13824	0.13458	-0.12338	0.0055199	-0.00014728	-0.0042706	-0.0013142	7.6592e-05	-1.4424e-05	-0.0019627	-0.00054526	-0.0010014	0.0045395	-0.00012916	-7.2837e-05	0.00022972	3.5584e-05	
	14	0.21777	0.10641	-0.13782	0.0054722	1.1086e-05	-0.003603	-0.0010266	0.00013697	0.00015223	-0.0017638	-8.5533e-05	-0.00055385	0.003912	0.00012118	2.3901e-05	0.0002324	-8.6606e-05	0
	15	-0.21027	0.026306	-0.12946	0.0060863	4.0829e-05	-0.0014887	-0.0011849	-9.7573e-05	3.2783e-05	-0.0016351	-0.00028801	-0.00048423	0.0036898	-1.651e-05	-4.4525e-05	6.5506e-05	-5.0843e-05	-
	16	0.20825	0.0034094	-0.13477	0.0055809	0.00022805	-0.0014024	-1.5378e-05	6.2883e-05	-8.9407e-06	-0.0017643	0.00020862	-0.00062466	0.0032663	-0.00012237	-3.8326e-05	0.00011396	-8.3447e-07	-
fo	17	0.2088	-0.014061	-0.13068	0.0053253	7.5221e-05	-0.00072169	-0.00039482	3.8743e-06	-8.9407e-06	-0.0015626	0.00021195	-0.00019932	0.0026312	7.2956e-05	-4.8757e-05	6.7413e-05	-6.6936e-05	0
	18	0.053543	-0.058395	-0.11166	0.0053635	-9.1136e-05	-0.00029182	-5.0724e-05	3.9637e-05	3.9816e-05	-0.0015054	0.00029624	-0.00023419	0.0026655	-9.1791e-05	6.6638e-05	1.812e-05	-7.4983e-05	
	19	0.023956	-0.098389	-0.10626	0.0045891	-0.00044012	-0.00032067	0.00061202	-3.3498e-05	6.2823e-05	-0.001411	0.0007565	-5.9605e-05	0.0025005	5.4896e-05	3.5763e-06	7.7069e-05	2.1279e-05	0
	20	0.0078163	-0.096954	-0.050827	0.0038567	-0.00036156	0.00015426	5.0902e-05	3.7074e-05	0.00016242	-0.0013266	0.00063872	6.2406e-05	0.0024223	-7.7486e-07	-2.5988e-05	-9.5844e-05	-0.00013816	
	21	0.12189	-0.11438	-0.085724	0.0039978	-0.00010359	0.00045955	0.00045025	6.5565e-07	8.4877e-05	-0.001265	0.0010209	0.00023293	0.0025167	-9.9897e-05	8.8632e-05	5.5611e-05	0.0001058	1
>	22	0.08609	-0.1463	-0.045181	0.0035334	-8.7023e-05	0.00062585	0.00072074	8.285e-06	0.00011688	-0.0011973	0.00092149	0.00035381	0.0024529	-6.938e-05	8.3506e-05	-4.7684e-07	-5.3525e-05	
listory 🗗 🗙	23	0.11502	-0.17053	-0.071747	0.0043411	-0.0002625	0.0013576	-4.9829e-05	7.987e-06	3.3677e-05	-0.0011201	0.0012803	0.00045872	0.0023861	-4.4107e-06	-6.9857e-05	-4.2856e-05	-3.8803e-05	2
~ ~	24	0.12982	-0.22449	-0.078125	0.0041656	0.00010693	0.0011163	0.00084257	-6.7174e-05	4.6074e-05	-0.00095963	0.0010481	0.00062442	0.0028982	-0.00021011	-3.5167e-06	5.9009e-06	1.1563e-05	
722.mat	25	0.21301	-0.24072	-0.032181	0.0032091	7.0632e-05	0.00088787	0.00053287	3.9935e-05	-9.8348e-06	-0.00099897	0.0013547	0.00075746	0.003006	-0.00014144	4.0412e-05	-1.1206e-05	-6.8307e-05	1
	26	-0.20197	-0.26721	-0.066559	0.0025988	-1.2696e-05	0.0011997	0.00029683	1.0192e-05	8.4043e-06	-0.00092173	0.0014634	0.00087094	0.0031767	-0.00011152	-5.1558e-05	1.3053e-05	5.728e-05	
	27	0.17657	-0.2088	-0.07843	0.0020618	-5.4717e-05	0.0016026	0.0011129	5.3644e-06	1.2994e-05	-0.00091648	0.0014367	0.0010376	0.0034342	-0.00010544	-5.2512e-05	-5.3644e-06	2.4736e-05	
	28	0.18127	-0.29834	-0.049286	0.0028305	-0.00023985	0.0017266	0.00030422	4.1723e-07	3.8385e-05	-0.00083756	0.0015469	0.0013084	0.0037098	-0.00019145	7.9274e-06	-9.1672e-05	2.4855e-05	7
	29	-0.19824	-0.41638	-0.053207	0.0021887	2.5094e-05	0.0024977	0.0007503	3.8922e-05	-4.9949e-05	-0.00092769	0.0016794	0.001255	0.0038538	1.049e-05	1.6928e-05	7.1824e-05	-3.7611e-05	
	30	-0.21277	-0.31677	-0.045929	0.0015588	-0.00015688	0.0022316	0.0010548	9.2447e-05	-3.9339e-06	-0.00099993	0.0016508	0.0015516	0.0040817	-0.000135	4.0114e-05	-5.1856e-06	3.6538e-05	5
	31	-0.12622	-0.42896	-0.034729	0.0018196	-0.00013047	0.0020084	0.00049567	8.4281e-05	-6.1035e-05	-0.00084805	0.0016775	0.0016403	0.0039654	-0.00013393	-2.7537e-05	-3.8147e-06	3.8147e-06	4
	32	-0.16827	-0.39893	-0.016304	0.0015855	-0.00012052	0.0024462	0.0008409	-7.2539e-05	-0.00010163	-0.0009203	0.0015755	0.0016227	0.0045834	-4.9293e-05	-4.9055e-05	6.4552e-05	-4.2737e-05	
	33	0.030243	-0.3761	-0.039688	0.0011239	-9.6858e-05	0.0024986	0.0011749	-5.1022e-05	2.8312e-05	-0.0008986	0.0017486	0.0015841	0.0045033	9.1791e-06	1.6689e-05	2.8491e-05	7.2479e-05	-
	34	-0.19043	-0.37708	-0.013412	0.00015843	2.5332e-05	0.0023413	0.0009923	4.7386e-05	3.2961e-05	-0.0010486	0.001873	0.0016894	0.004612	1.2755e-05	5.7638e-05	-5.6446e-05	0.00014204	€ ∨
																			-





Number of samples







$$S = I + jQ$$

$$|s| = \sqrt{Real\{s\}^2 + Imag\{s\}^2}$$

$$\Delta = Arg\{s\} = \arctan\left[\frac{Imag\{s\}}{Real\{s\}}\right]$$

$$s^* = Real\{s\} - j Imag\{s\}.$$





$$T_0 = \frac{1}{M} \sum_{n=1}^{M} s_n * s_n$$

$$R_0 = \frac{1}{M} \sum_{n=1}^{M} s'_n * s'_n$$

$$R_1 = \frac{1}{M-1} \sum_{n=1}^{M-1} s'_n * s'_{n+1}$$

$$R_2 = \frac{1}{M-2} \sum_{n=1}^{M-2} s'_n * s'_{n+2}$$

$$s = I + jQ$$

s' denotes the clutter-filtered time series, s denotes the original unfiltered time series and the * denotes a complex conjugate





```
Lag [0] = (I + jQ) \times conj (I + jQ)

= (I + jQ) \times (I - jQ)

= (0.707 + j0.707) \times (0.707 - j0.707)

= 0.707 \times 0.707 - j(0.707 \times 0.707) + j(0.707 \times 0.707) - j^2(0.707 \times 0.707)

= 0.5 - j0.5 + j0.5 - j^2(0.5)

= 0.5 + j0 + 0.5

= 1 + j0
```

R0 has only magnitude, phase will always be zero





Stationary target:

I&Q samples for PRF₂ will ideally have exactly the same phase and magnitude as I&Q samples taken at PRF₁.eg. PRF₁ = 0.707 + j0.707 & PRF₂ = 0.707 + j0.707

Calculating the auto-correlation of the first lag will provide the phase difference between PRF₁ and PRF₂.

The phase of the resultant vector provides the phase difference between PRF₁ & PRF₂.

Lag [1]=
$$(I_2 + jQ_2) \times conj(I_1 + jQ_1)$$

= $(I_2 + jQ_2) \times (I_1 - jQ_1)$
= $(0.707 + j0.707) \times (0.707 - j0.707)$
= $0.707 \times 0.707 - j(0.707 \times 0.707) + j(0.707 \times 0.707) - j^2(0.707 \times 0.707)$
= $0.5 + j0 - j^2(0.5)$
= $0.5 + j0 + 0.5$
= $1 + j0$ => Phase difference = 0 deg





Moving target:
$$PRF_1 = 0.707 + j0.707$$

 $PRF_2 = 1 + j0$

Lag [1] =
$$(I_2 + jQ_2) \times \text{conj} (I_1 + jQ_1)$$

= $(I_2 + jQ_2) \times (I_1 - jQ_1)$
= $(1 + j0) \times (0.707 - j0.707)$
= $(1x0.707) - j(1x0.707) + j(0x0.707) - j^2(0 \times 0.707)$
= $0.707 - j0.707 + j0 - j^2(0)$
= $0.707 - j0.707$

Phase = -45deg. or $-\pi/4$

Phase value from R1 for velocity measurement





Reflectivity

Reflectivity

$$dBZ = 10\log\left[\frac{T_0 - N}{N}\right] + dBZ_0 + 20\log r + ar + CCOR$$

1st Term : $10\log\left[\frac{T_0-N}{N}\right]$ Signal to Noise Ratio

2rd Term: dBZo: Calibration Reflectivity

3th Term: 20 log r: Range Normalization

4th Term:ar: Gaseous Attenuation Correction

5th Term: CCOR: Clutter Correction





Velocity

Velocity

$$V = \frac{\lambda}{4\pi\tau_s}\theta_1$$
 where $\theta_1 = \arg\{R_1\}$.

 λ is the radar wavelength, is the sampling time (1/PRF). θ 1 is constrained to be on the interval [- π , π]





Spectrum Width

Spectrum Width

$$Variance = 2 \ln \left[\frac{R_0}{|R_1|} \right]$$

$$R_0$$
, R_1 , R_2 "accurate" algorithm for SNR >> 0 to 5 dB

$$Variance = \frac{2}{3} \ln \left[\frac{|R_1|}{|R_2|} \right]$$

$$W = \frac{\sqrt{Variance}}{\pi}$$

Width is normalized to the Nyquist Interval [-1, 1], To obtain the width in meters per second, one multiplies The output width by Vu





Range Averaging

It can be performed over 2, 3, ..., 16 bins. This is accomplished by simply averaging the *T*0, *R*0, *R*1 and *R*2 values.

Thresholds can be applied on the bins to exclude the bins which does not satisfy the quality criteria

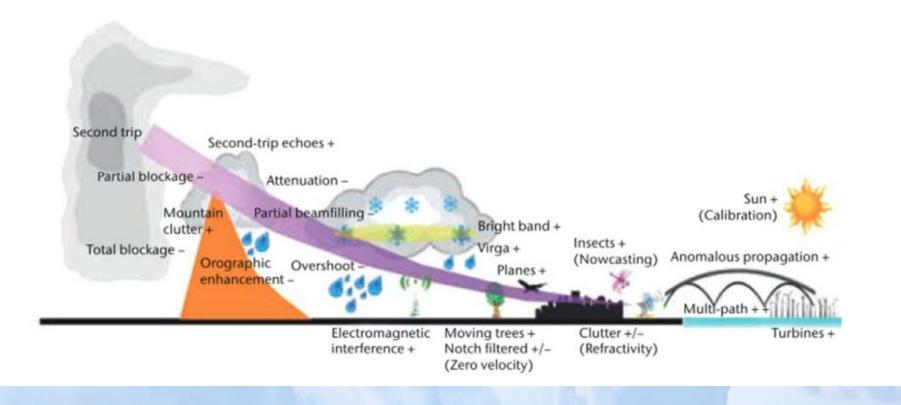
Bin size is determined by the pulse width





Factors affecting radar data

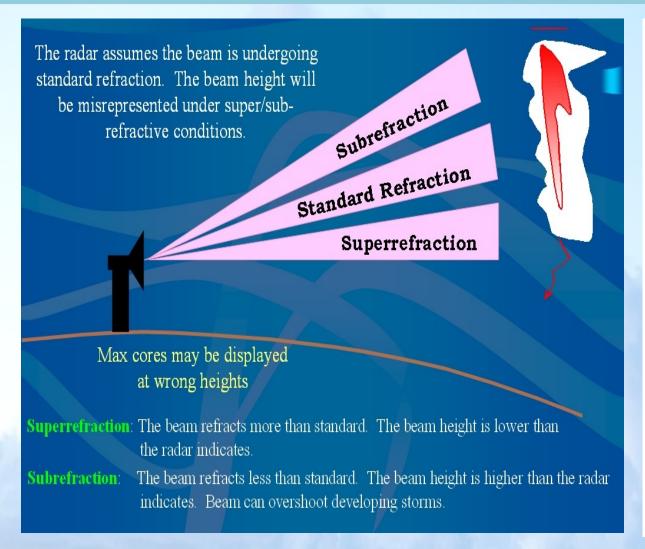
Error sources on weather radar observation

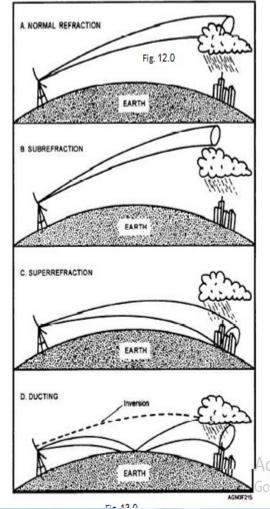






Factors affecting radar data

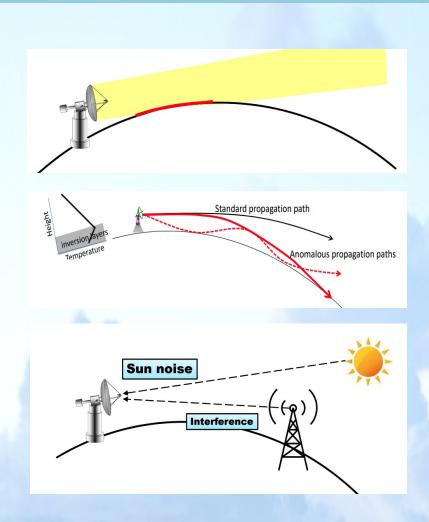


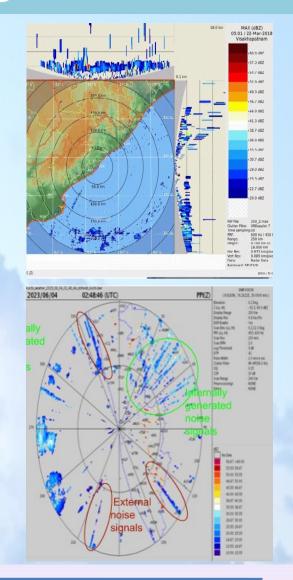






Factors affecting radar data

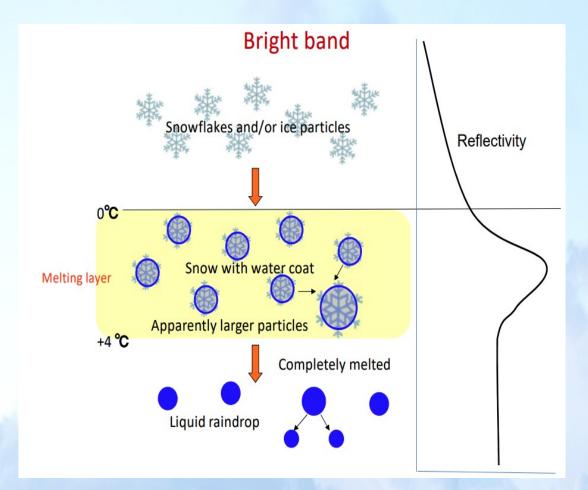


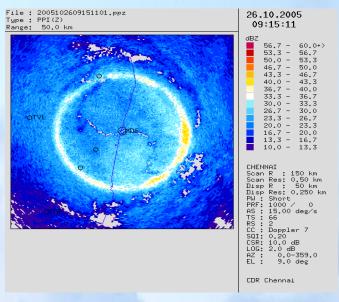






Bright band

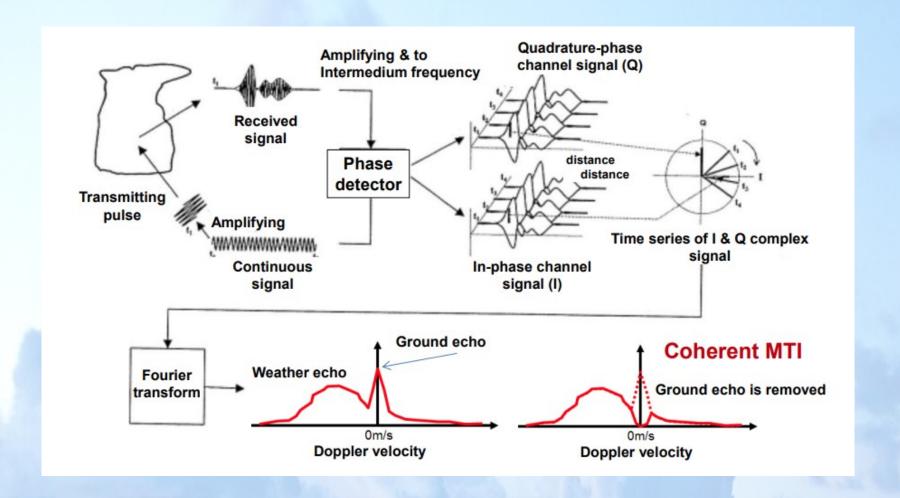








Removing clutter



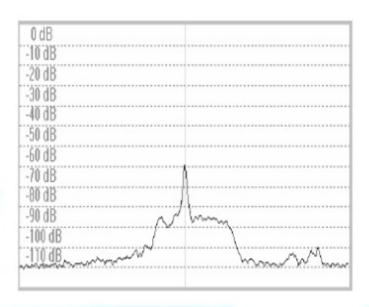


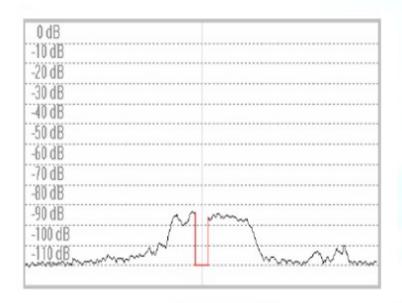


Clutter Filter

Time series mode – IIR Filter (velocity

Weather Data with zero velocity (tangetial elements will also be removed)





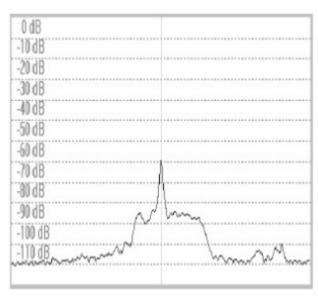


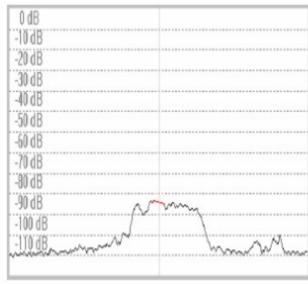


Clutter Filter

Frequency domain – by FFT

Interpolation across 0 Hz region



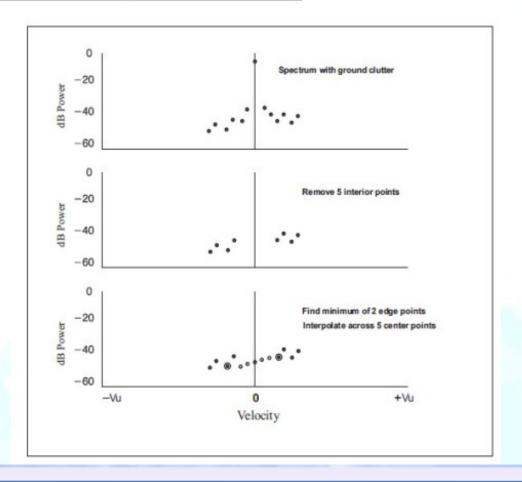






Clutter Filter

Frequency domain – by FFT







Thresholding

Signal quality Index (SQI)

The signals which are very weak to be of any use or the spectrum width is too high to justify further analysis

SQI = f(SNR, SW)

$$SQI = \frac{|R_1|}{R_0}$$

$$SQI = \frac{SNR}{SNR+1} e^{\frac{-\pi^2 W^2}{2}}$$

The SQI is the normalized magnitude of the autocorrelation at lag 1 and varies between 0 for an uncorrelated signal (white noise) to 1 for a noise-free zero-width signal (pure tone). Mean velocity estimates are degraded when the spectrum, width is large or when the signal-to-noise ratio is weak.

For very large SNR's the SQI is a function of the spectrum width only. For a zero-width pure tone (W=0), the SQI is a function of the SNR only (for example, for W=0, an SNR of 1corresponds to SQI=0.5). The SQI threshold is typically set to a value of 0.4 to 0.5.





Thresholding

Clutter correction Threshold (CCOR)

To is the total unfiltered power. By comparing the total filtered and unfiltered powers at each range bin, a clutter power, and hence a clutter correction, for that bin can be derived

$$CCOR_{est} = 10\log \frac{S}{C+S} = 10\log \frac{1}{CSR+1}$$

The clutter power is computed from:

$$C = T_0 - R_0 = [C + S + N] - [S + N]$$

The signal power S is then computed from:

$$S = \left| R_1 \right| \exp \frac{\pi^2 w^2}{2}$$

The default threshold is set to -18db





Thresholding

LOG

A threshold parameter called LOG is also calculated to provide a signal strength estimate that is useful for qualifying reflectivity. It is the ratio of Signal plus Noise to Noise, which always has a positive representation in dB

$$LOG = 10\log\left[\frac{R_0}{N}\right]$$
 (when applied to the other parameter)

The default threshold is set to 0.75db





Thresholds

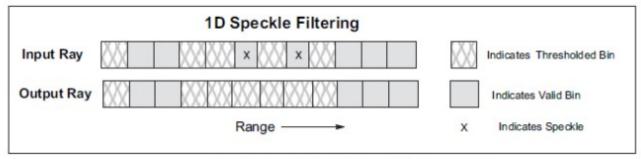
ID	Criterion Name	Pass Criterion
LOG	(Signal+Noise)-to-Noise Ratio	LOG > threshold
SQI	Signal Quality Index	SQI > threshold
CCOR	Clutter Correction	CCOR > threshold
SIG	Weather Signal Power	SIG > threshold
PMI	Polarimetric Meteo Index	PMI > threshold





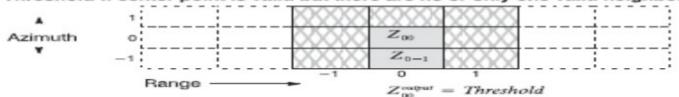
Speckle Filter

A speckle filter is a final pass over each output ray, in which isolated bins are removed. Speckle filters remove isolated data points that are likely to be noise, interference, aircraft, birds, or other point targets. Meteorological targets typically occupy multiple range bins, so they are not affected by the speckle filters

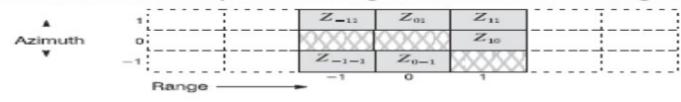


2D 3x3 Filtering Concepts

Threshold if center point is valid but there are no or only one valid neighbor.



Fill thresholded center point with average if there 6 or more valid neighbors.





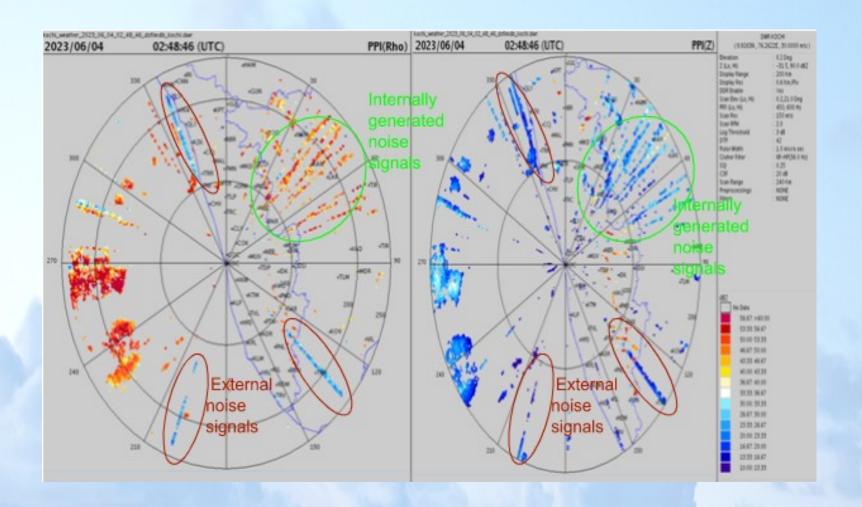
Post processing

Non-Meteorological (birds, insects, etc.)	Metr (Non-Uniform) (hail, melting snow, etc.)	<u>Metr (Uniform)</u> (rain, snow, etc.)
	Hail Wet Aggregates	8.0 mm 7.4 mm 5.8 mm 5.3 mm 3.5 mm 2.7 mm
Complex scattering from pulse-to-pulse. Horizontal and vertical pulses change in different manners from pulse-to-pulse	Somewhat complex scattering from pulse-to-pulse. Moderate differences from pulse-to-pulse for the horizontal and vertical pulses	Well-behaved scattering from pulse-to-pulse. Little differences from pulse-to- pulse for the horizontal and vertical pulses
Low CC (< 0.7)	Moderate CC (0.80 to 0.97)	High CC (> 0.97)





Post processing







Thank you Any Questions? bibraj.r@imd.gov.in



